

What are social networks?

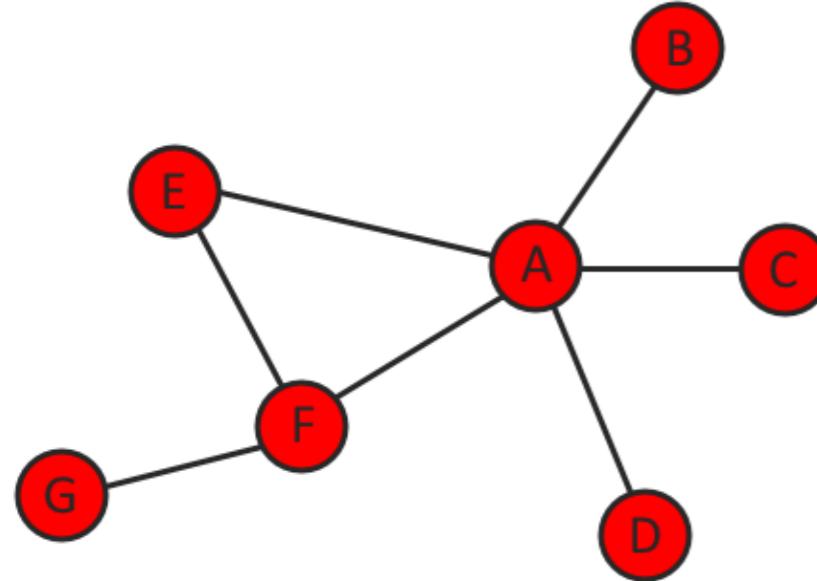
NETWORK ANALYSIS IN R



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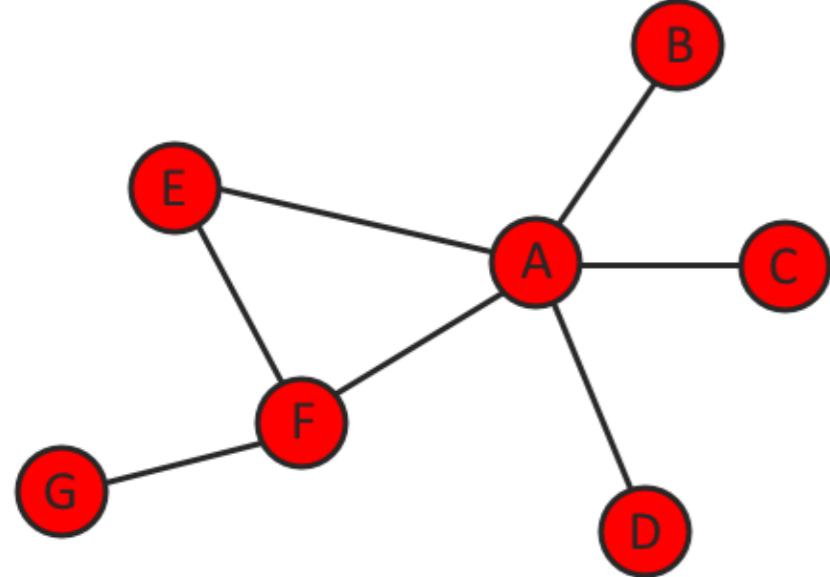
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Network data: adjacency matrix



	A	B	C	D	E	F	G
A	0	1	1	1	1	1	0
B	1	0	0	0	0	0	0
C	1	0	0	0	0	0	0
D	1	0	0	0	0	0	0
E	1	0	0	0	0	1	0
F	1	0	0	0	1	0	1
G	0	0	0	0	0	1	0

Network data: edgelist



A	B
A	C
A	D
A	E
A	F
E	F
F	G

The igraph R package

A	B
A	C
A	D
A	E
A	F
E	F
F	G

```
library(igraph)
```

2 columns

```
g <- graph.edgelist(as.matrix(df),  
                     directed = FALSE)
```

```
g
```

```
IGRAPH UN-- 7 7 --  
+ attr: name (v/c)  
+ edges (vertex names):  
[1] A--B A--C A--D A--E A--F E--F F--G
```

7 vertices and 7 edges

Adding Vertex Attributes

```
g <- set_vertex_attr(  
  g,  
  "age",  
  value = c(  
    20, 25, 21, 23, 24, 23, 22  
  ))
```

Adding Edge Attributes

```
g <- set_edge_attr(  
  g,  
  "frequency",  
  value = c(  
    2, 1, 1, 1, 3, 2, 4  
  ))
```

Adding attributes II

edges.df

from	to	frequency
A	B	2
A	C	1
A	D	1
A	E	1
A	F	3
E	F	2
F	G	4

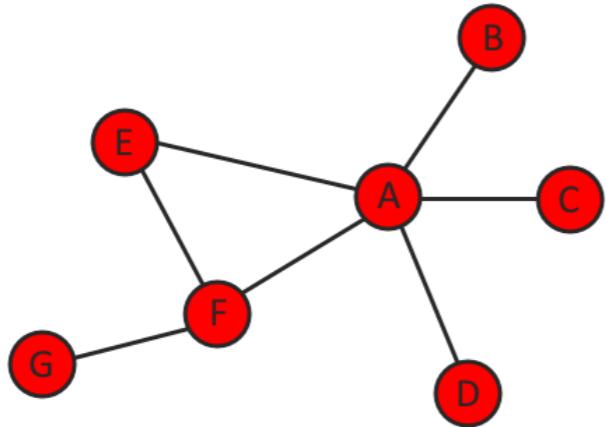
vertices.df

name	age
A	20
B	25
C	21
D	23
E	24
F	23
G	22

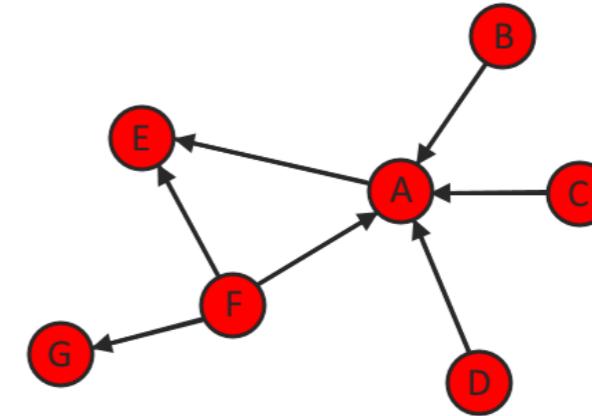
```
graph_from_data_frame(d = edges.df, vertices = vertices.df,  
                      directed = FALSE)
```

Directionality

Undirected



Directed



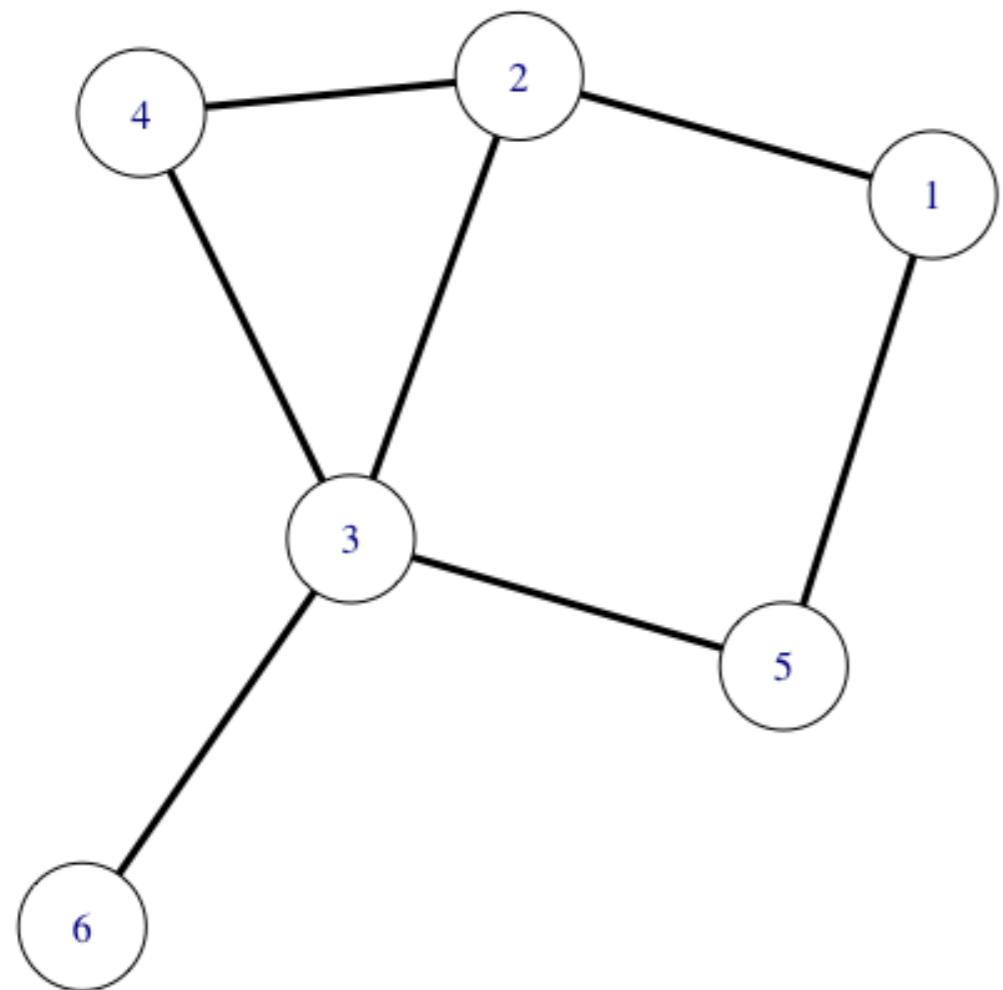
Undirected:

```
IGRAPH UN-- 7 7 --
+ attr: name (v/c)
+ edges (vertex names):
[1] A--B A--C A--D A--E A--F E--F F--G
```

Directed:

```
IGRAPH DN-- 7 7 --
+ attr: name (v/c)
+ edges (vertex names):
[1] A->E B->A C->A D->A F->A F->E F->G
```

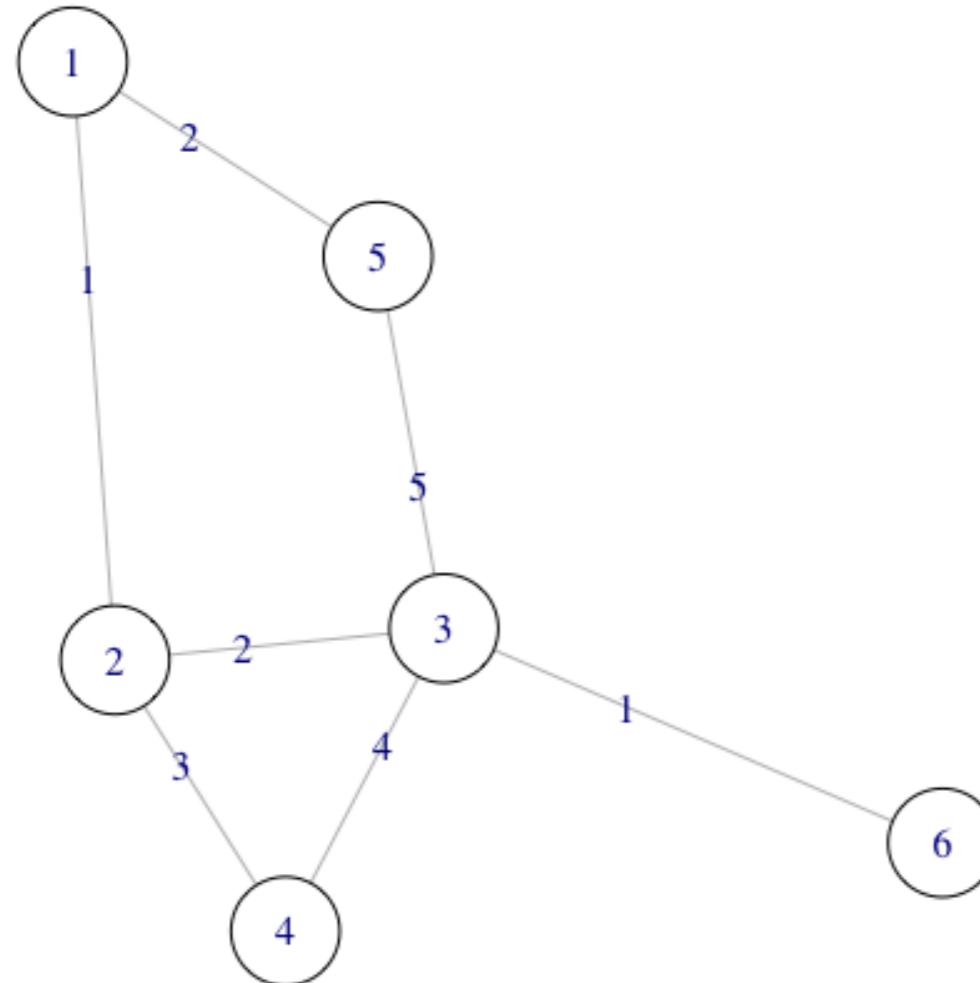
The adjacency matrix (part 1)



`as_adjacency_matrix(g)`

	1	2	3	4	5	6
1	0	1	0	0	1	0
2	1	0	1	1	0	0
3	0	1	0	1	1	1
4	0	1	1	0	0	0
5	1	0	1	0	0	0
6	0	0	1	0	0	0

The adjacency matrix (part 2)



```
as_adjacency_matrix(g,  
attr="weight")
```

	1	2	3	4	5	6
1	0	1	0	0	2	0
2	1	0	2	3	0	0
3	0	2	0	4	5	1
4	0	3	4	0	0	0
5	2	0	5	0	0	0
6	0	0	1	0	0	0

A network as a data frame

```
as_data_frame(g, what = "both")
```

```
$nodes  
  name  
  a    a  
  b    b  
  c    c  
  d    d  
  e    e
```

```
$ties  
  from to weight  
  1    a   b     1  
  2    a   e     2  
  3    b   c     2  
  4    b   d     3  
  5    c   d     4  
  6    c   e     5
```

Mapping representations

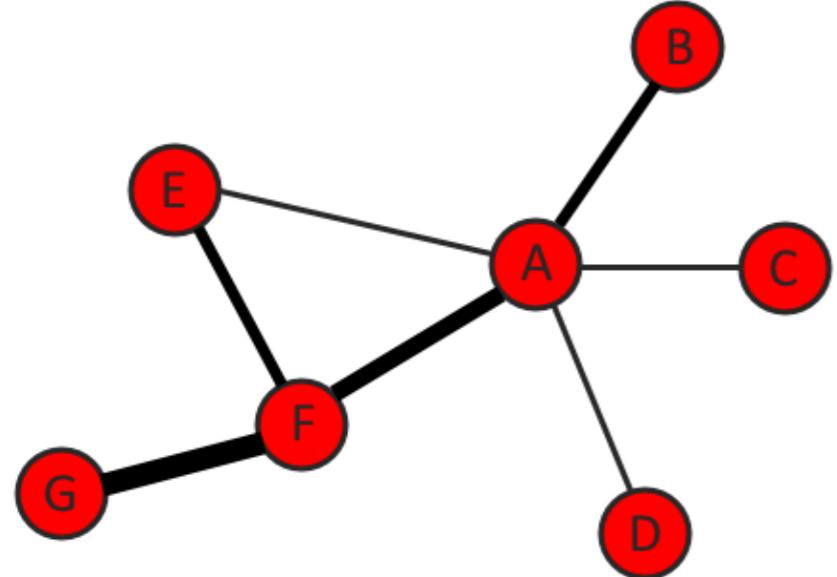
```
# graph to matrix
A <- as_adjacency_matrix(g)

# matrix to graph
g <- graph_from adjacency_matrix(A)
# graph to data frame
df = as_data_frame(g, what = "both")

# data frame to graph
g <- graph_from_data_frame(df$ties, vertices = df$nodes)
# matrix to data frame
df = as_data_frame(graph_from adjacency_matrix(A), what = "both")

# data frame to matrix
A <- as_adjacency_matrix(graph_from_data_frame(df$ties,
vertices = df$nodes))
```

Subsetting networks



`[[` filters the object and returns a `data.frame` but we can apply the same filter with a `[` and return `igraph` object.

```
E(g)[[inc('E')]]
```

```
+ 2/7 edges (vertex names):  
tail head tid hid frequency  
4   E   A   5   1       1  
6   F   E   6   5       2
```

```
E(g)[[frequency>=3]]
```

```
+ 2/7 edges (vertex names):  
tail head tid hid frequency  
5   F   A   6   1       3  
7   G   F   7   6       4
```

`edges.df`

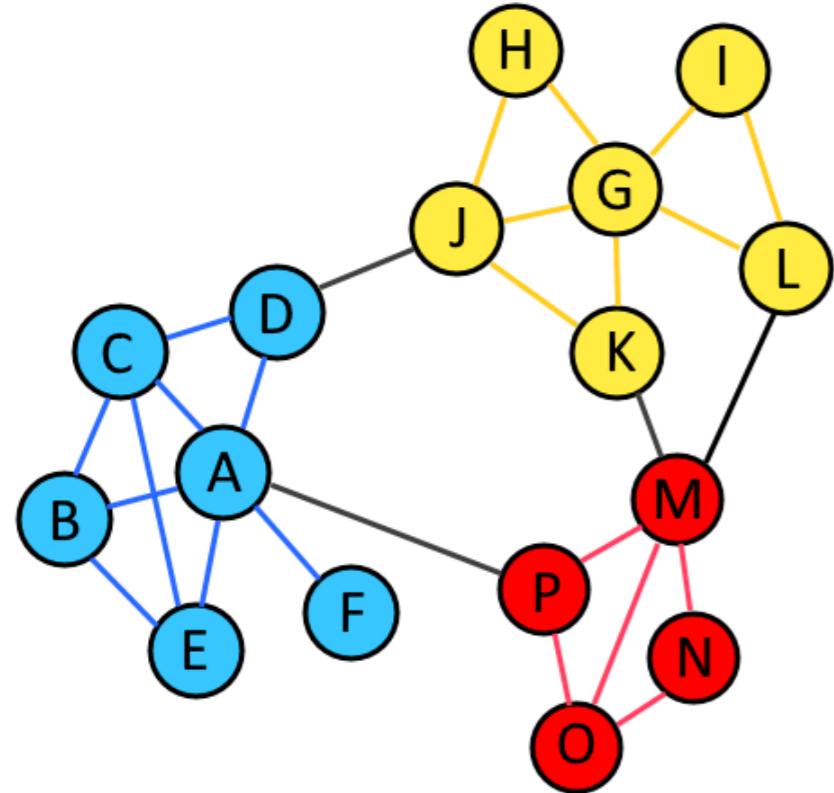
from	to	frequency
A	B	2
A	C	1
A	D	1
A	E	1
A	F	3
E	F	2
F	G	4

```
# Create a new igraph object by deleting  
edges that are less than 2 hours long  
g2 <- delete_edges(g1, E(g1)[hours < 2])
```

```
# Assign largest cliques output to object 'lc'  
lc <- largest_cliques(g)
```

```
# Create two new undirected subgraphs, each  
# containing only the vertices of each largest  
# clique.  
gs1 <- as.undirected(subgraph(g, lc[[1]]))  
gs2 <- as.undirected(subgraph(g, lc[[2]]))
```

Fast-greedy detection



`fastgreedy.community(g)`

IGRAPH clustering fast greedy,
groups: 3, mod: 0.5

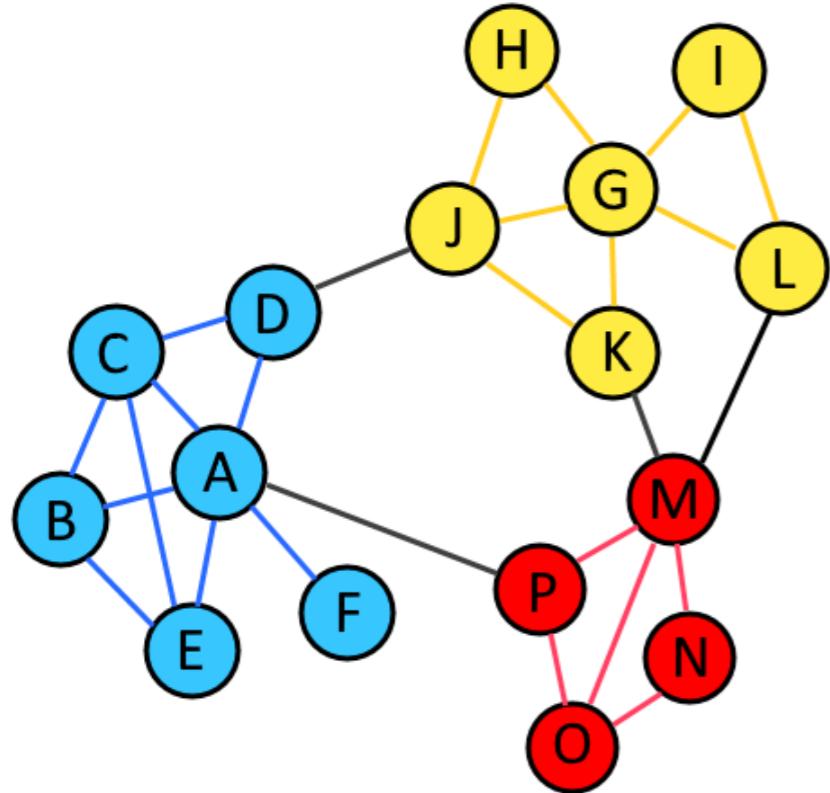
+ groups:

\$`1`
[1] "A" "B" "C" "D" "E" "F"

\$`2`
[1] "J" "G" "H" "I" "K" "L"

\$`3`
[1] "M" "N" "O" "P"

Edge-betweenness detection



```
edge.betweenness.community(g)
```

```
IGRAPH clustering edge betweenness,  
groups: 3, mod: 0.5
```

```
+ groups:
```

```
$`1`  
[1] "A" "B" "C" "D" "E" "F"
```

```
$`2`  
[1] "J" "G" "H" "I" "K" "L"
```

```
$`3`  
[1] "M" "N" "O" "P"
```

```
plot(g)
```

Getting information from graph object

```
v(g)
```

```
+ 7/7 vertices, named:  
[1] A B C D E F G
```

```
gorder(g)
```

```
[1] 7
```

```
vertex_attr(g)
```

```
$name  
[1] "A" "B" "C" "D" "E" "F" "G"  
  
$age  
[1] 20 25 21 23 24 23 22
```

```
E(g)
```

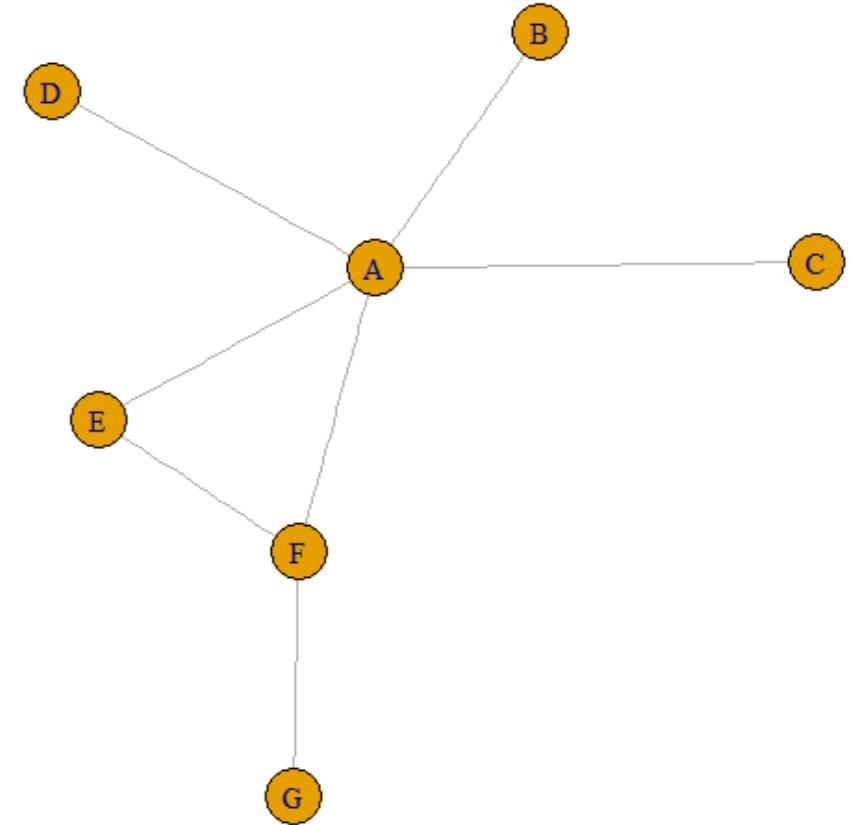
```
+ 7/7 edges (vertex names):  
[1] A--B A--C A--D A--E A--F E--F F--G
```

```
gsize(g)
```

```
[1] 7
```

```
edge_attr(g)
```

```
$frequency  
[1] 2 1 1 1 3 2 4
```



```
is.directed(g)
```

```
[1] TRUE
```

```
is.weighted(g)
```

```
[1] FALSE
```

Exploring the network

```
# explore the set of nodes and print the number of nodes  
V(g)  
vcount(g)  
  
# explore the set of ties and print the number of ties  
E(g)  
ecount(g)  
# add the name attribute "Madrid network" to the network and print it  
g$name <- "Madrid network"  
g$name  
# add node attribute id and print the node `id` attribute  
V(g)$id <- 1:vcount(g)  
  
# print the tie `weight` attribute  
E(g)$weight
```

Is there an edge between A & E?

```
g['A', 'E']
```

```
[1] 1
```

Find the starting vertex of all edges:

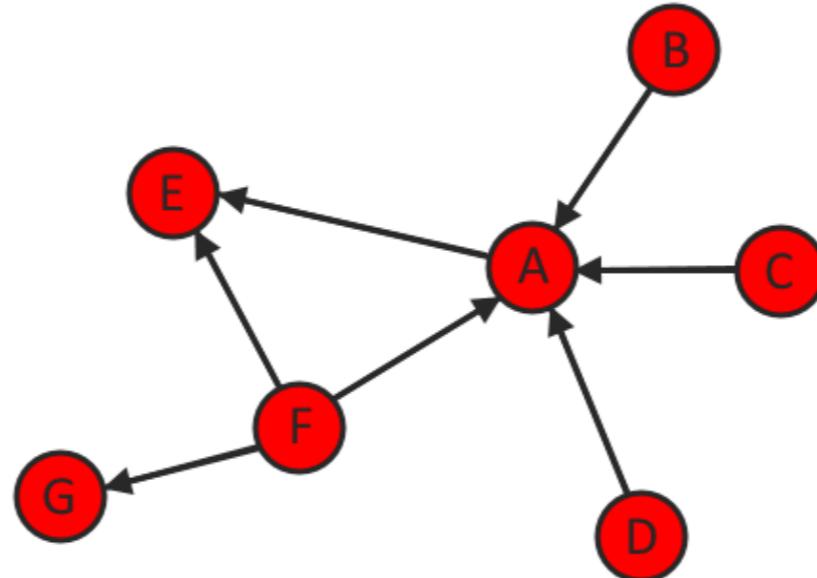
```
head_of(g, E(g))
```

```
+ 7/7 vertices, named:  
[1] A B C D F F F
```

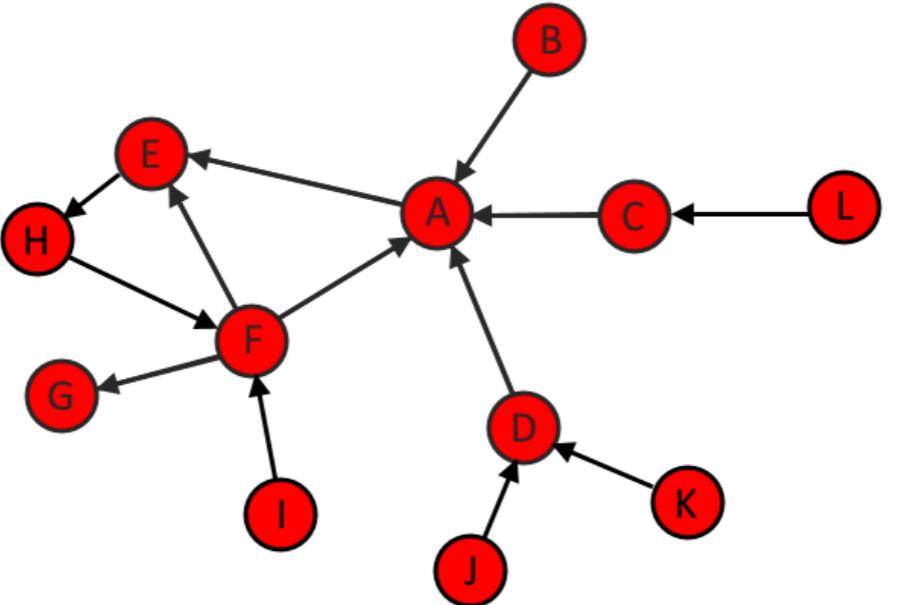
Show all edges to or from A:

```
incident(g, 'A', mode=c("all"))
```

```
+ 5/7 edges (vertex names):  
[1] A->E B->A C->A D->A F->A
```



Identifying neighbors



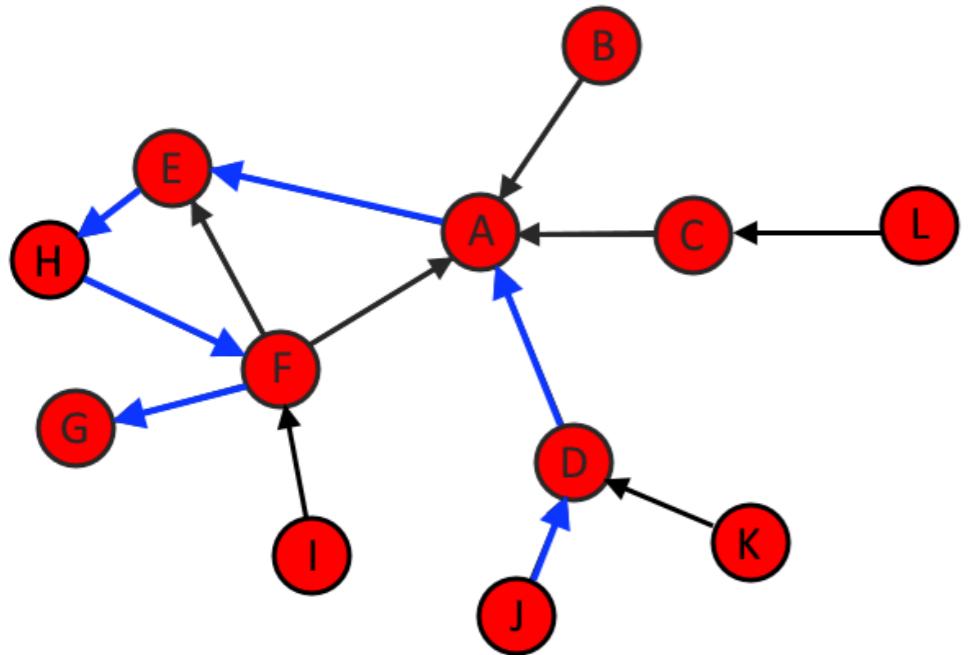
```
neighbors(g, "F", mode = c("all"))
```

```
+ 5/12 vertices, named:  
[1] A E G H I
```

```
x <- neighbors(  
  g, "F", mode = c("all")  
)  
  
y <- neighbors(  
  g, "D", mode = c("all")  
)  
  
intersection(x,y)
```

```
A
```

Paths



```
farthest_vertices(g)
```

```
$vertices  
+ 2/12 vertices, named:
```

```
[1] J G
```

```
$distance
```

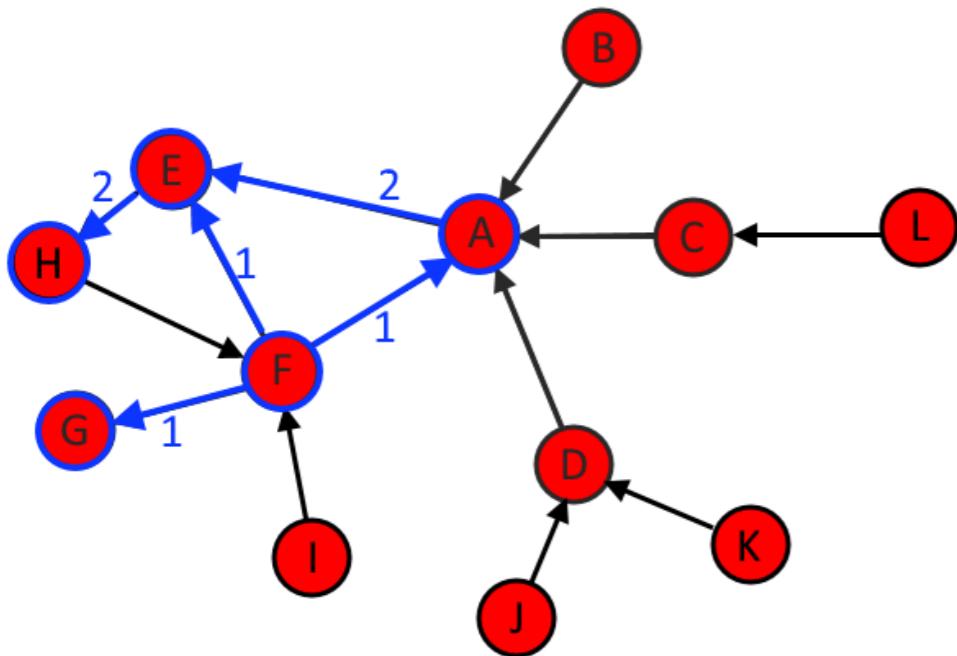
```
[1] 6
```

```
get_diameter(g)
```

```
+ 7/12 vertices, named:
```

```
[1] J D A E H F G
```

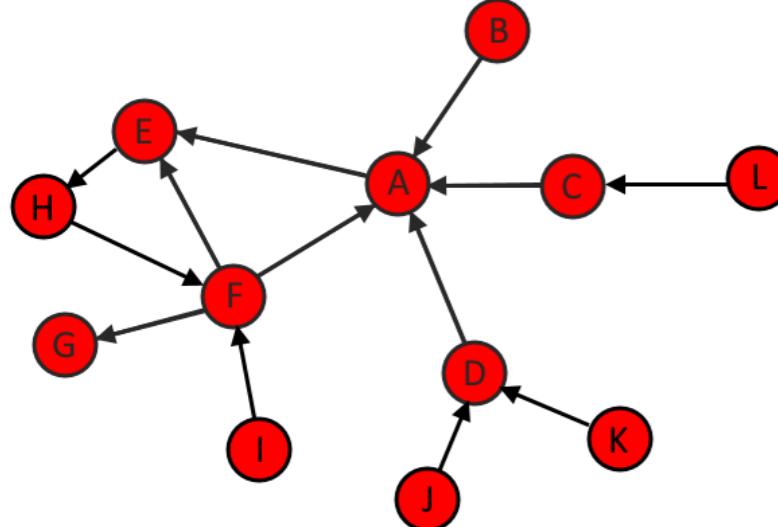
Identifying vertices reachable in N steps



```
ego(g, 2, 'F', mode=c('out'))
```

```
+ 5/12 vertices, named:  
[1] F A E G H
```

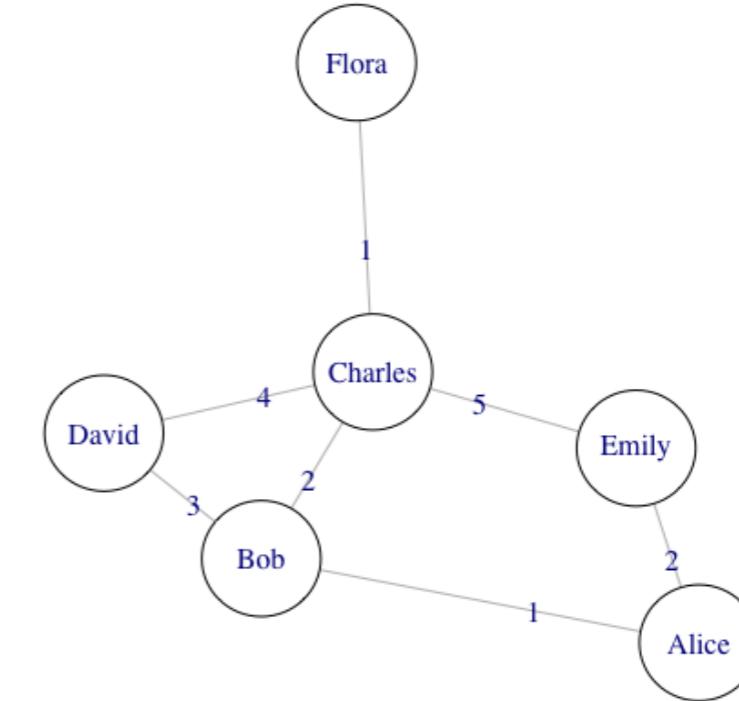
Out-degree and in-degree



	out-degree	in-degree
A	1	4
B	1	0
C	1	1
D	1	2
E	1	2
F	3	2
G	0	1
H	1	1
I	0	1
J	1	0
K	1	0

```
degree(g, mode = c("out"))
```

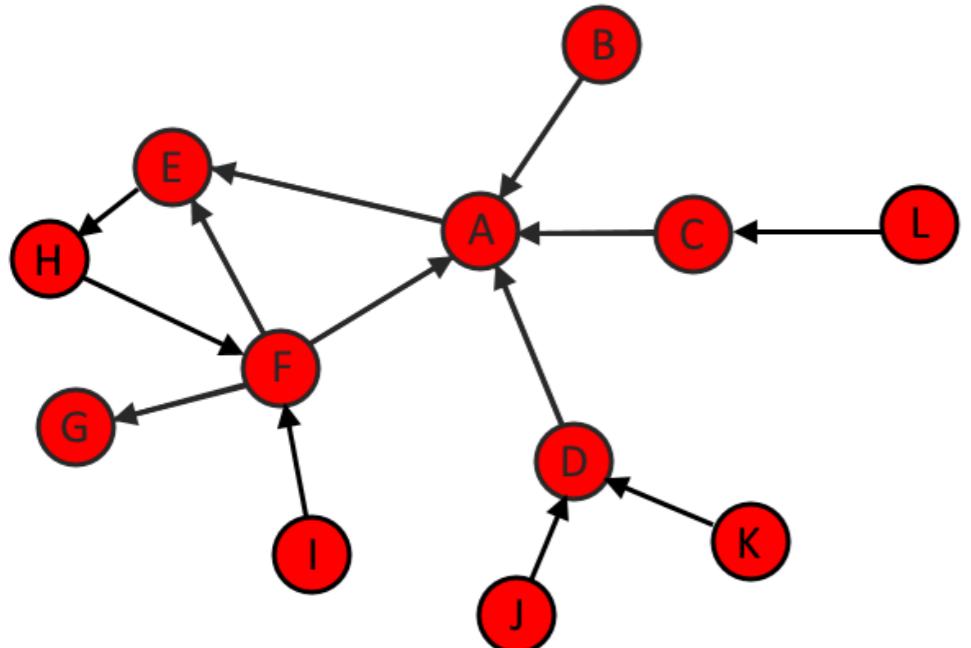
```
A B C D E F G H I J K L  
1 1 1 1 1 3 0 1 1 1 1 1
```



```
# compute node strengths  
strength(g)
```

```
Charles Alice  
12 3
```

Betweenness



I to H:

I → F → E → H
I → F → A → E → H

K to E:

K → D → A → E

B to G:

B → A → E → H → F → G

betweenness(g, directed = TRUE)

A	B	C	D	E	F	G	H	I	J	K	L
24	0	5	10	23	16	0	17	0	0	0	0

betweenness(g, directed = TRUE,
normalized = TRUE)

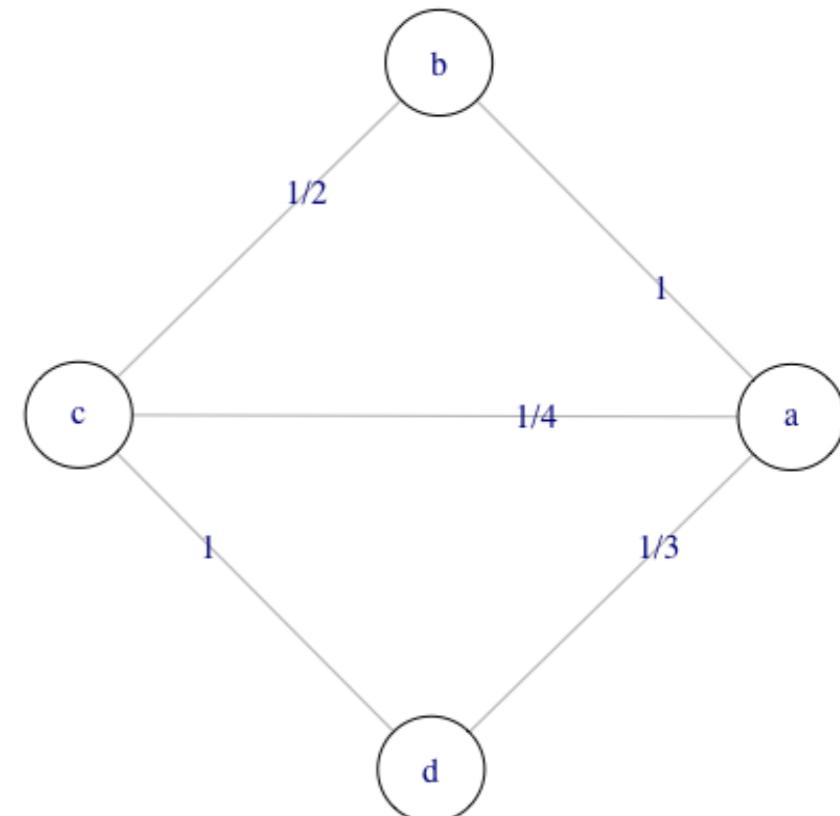
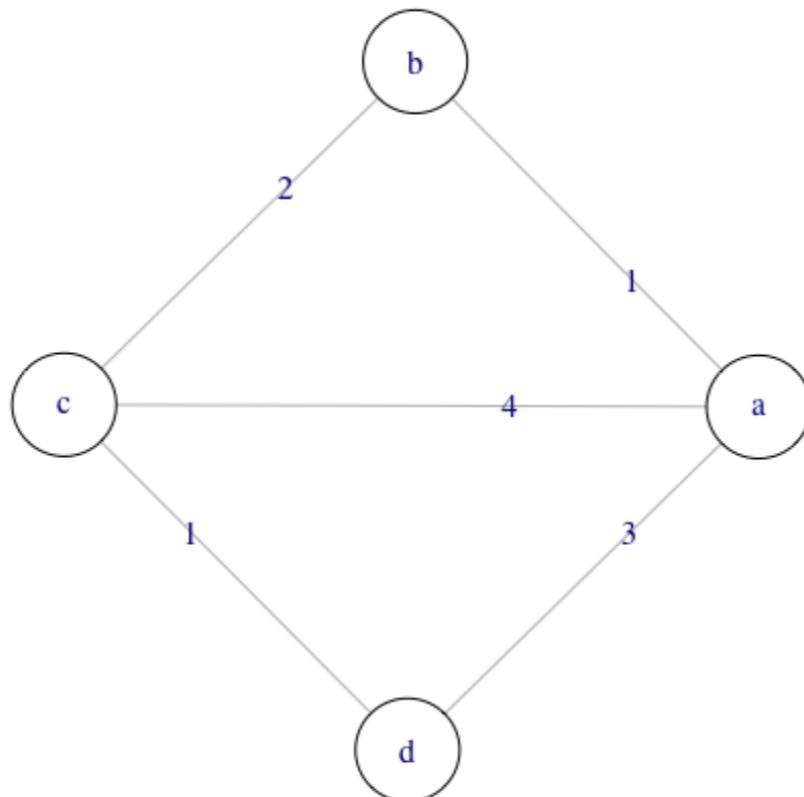
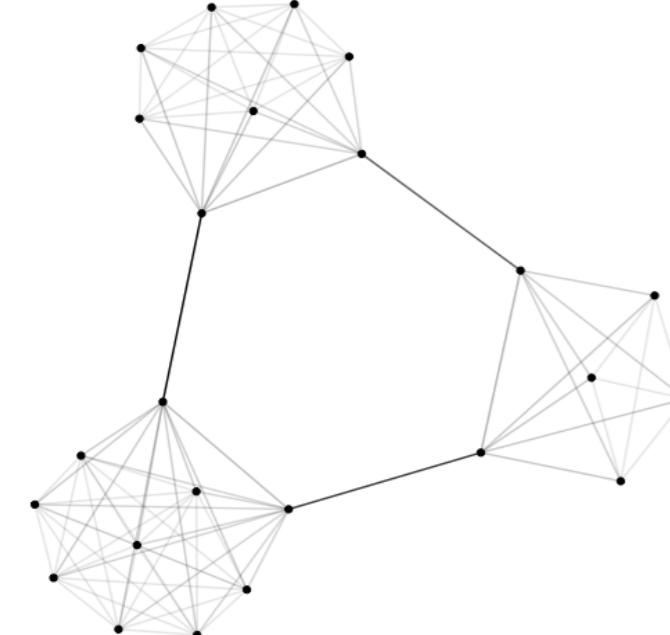
A	B	C	D	E	F
0.22	0.00	0.05	0.09	0.21	0.15

G	H	I	J	K	L
0.00	0.15	0.00	0.00	0.00	0.00

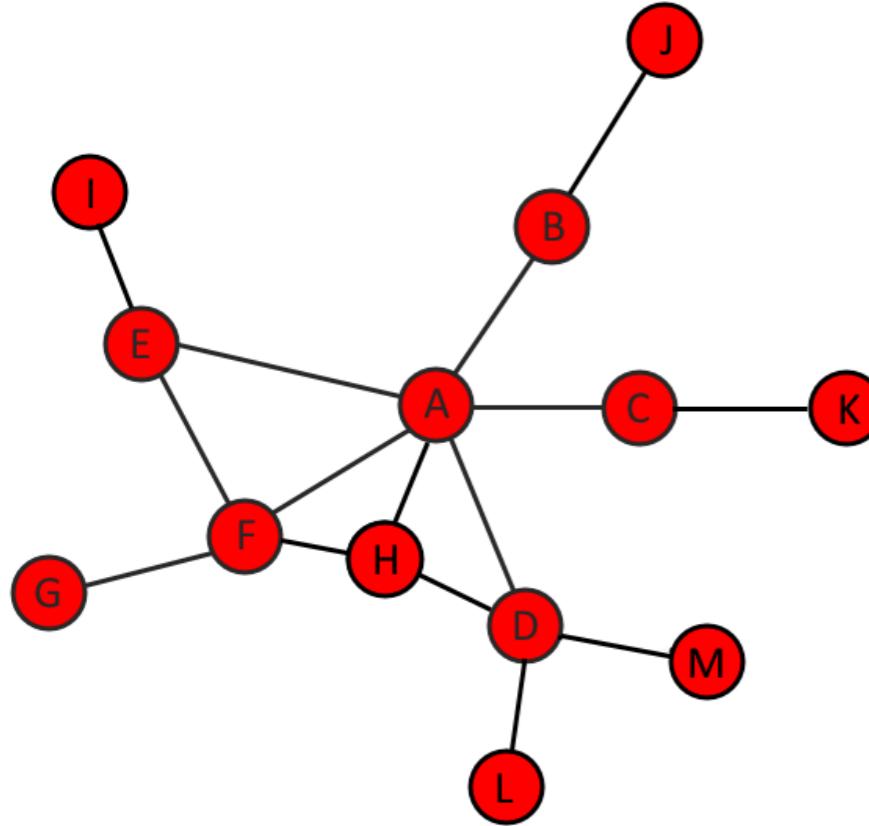
- `closeness()`: a measure that quantifies how close a node is to all other nodes in the network in terms of shortest path distance.

Computing betweenness

```
# compute distance weights for ties  
dist_weight = 1 / E(g)$weight  
  
# compute weighted betweenness on ties  
edge_betweenness(g, weights = dist_weight)
```



Eigenvector centrality



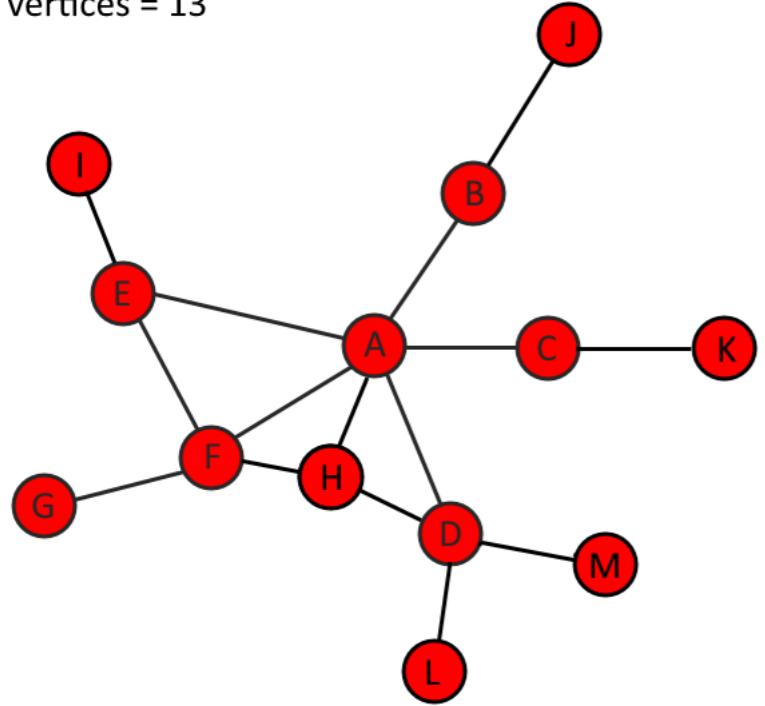
```
eigen_centrality(g)$vector
```

A	B	C	D	E	F	G
1.00	0.33	0.33	0.63	0.58	0.76	0.23
H	I	J	K	L	M	
0.71	0.17	0.10	0.10	0.19	0.19	

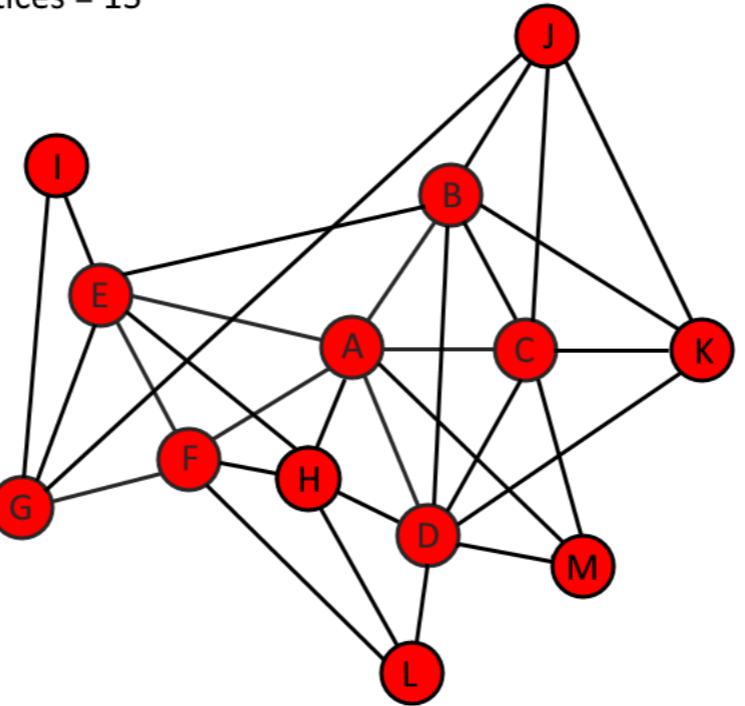
Eigenvector centrality is a measure of how well connected a vertex is. Vertices with the highest eigenvector centrality are those that are connected to many others but especially to other vertices who themselves are highly connected to others.

Density

density = 0.19
edges = 15
vertices = 13



density = 0.38
edges = 30
vertices = 13

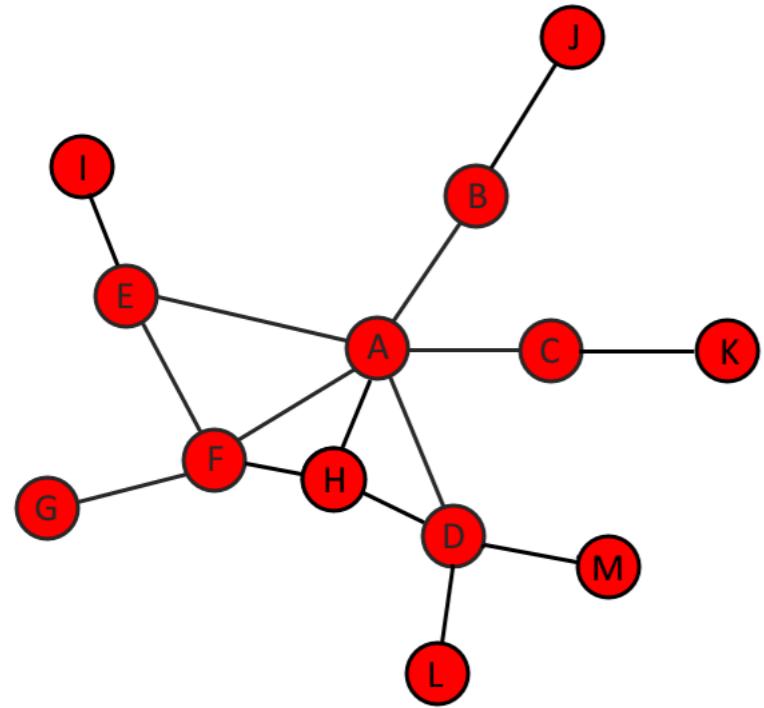


Is equivalent to the proportion of edges that actually do exist in a network out of all those that potentially could exist between every pair of vertices.

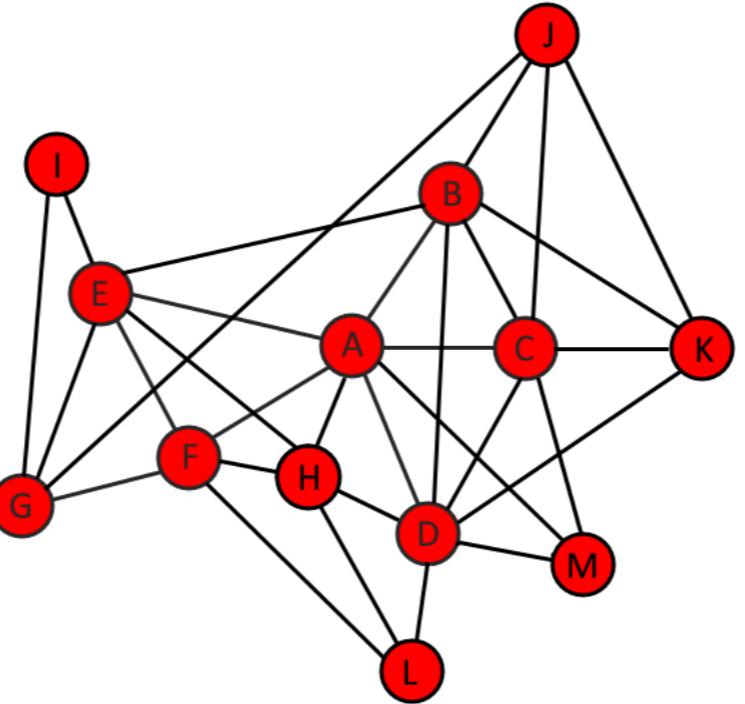
`edge_density(g)`

Average path length

average path length = 2.47



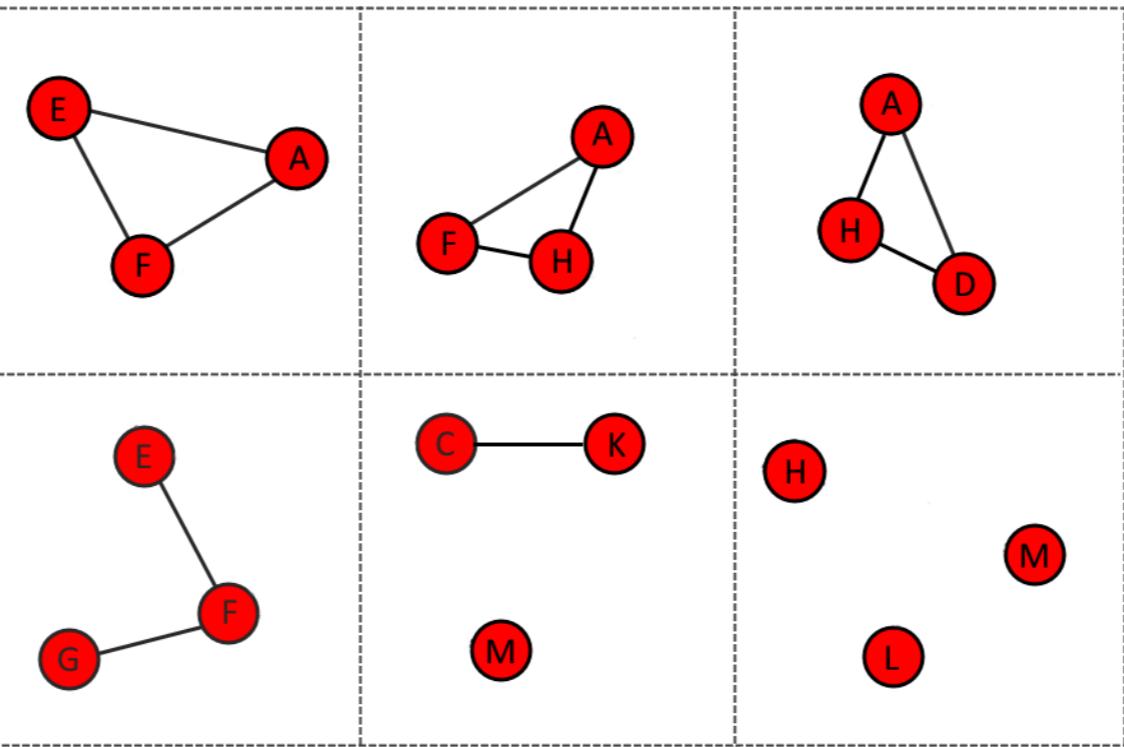
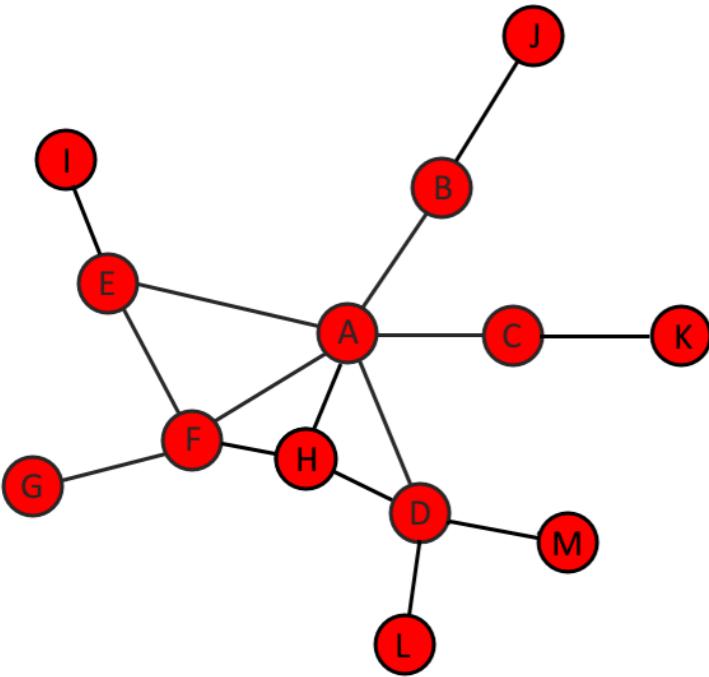
average path length = 1.81



the mean of the lengths of the shortest paths between all pairs of vertices in the network.

```
mean_distance(g, directed = FALSE)
```

Transitivity



`triangles(g)` Returns all closed triangles in the graph

```
# Show all triangles in the network.  
matrix(triangles(g), nrow = 3)
```

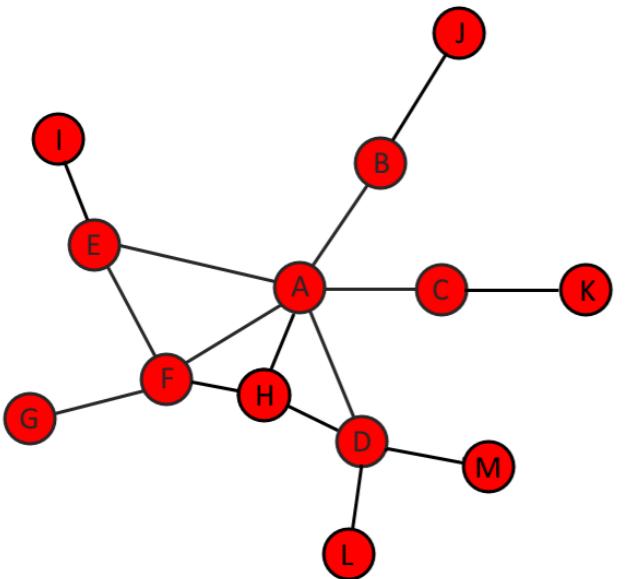
Global transitivity

`transitivity(g)`

```
[1] 0.26
```

Measures the probability that the adjacent vertices of a given vertex are connected

Local transitivity



```
transitivity(g,  
            vids = 'A',  
            type = "local")
```

0.2

```
count_triangles(g, vids = 'A')
```

3

```
transitivity(g,  
            vids = 'F',  
            type = "local")
```

0.33

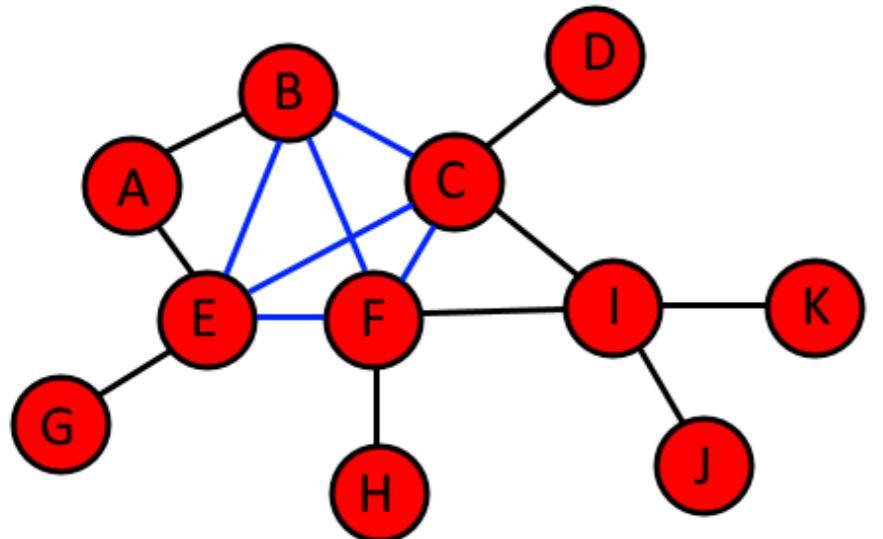
```
count_triangles(g, vids = 'F')
```

2

Identifying cliques

```
largest_cliques(g)
```

```
+ 4/11 vertices, named:  
[1] C F B E
```

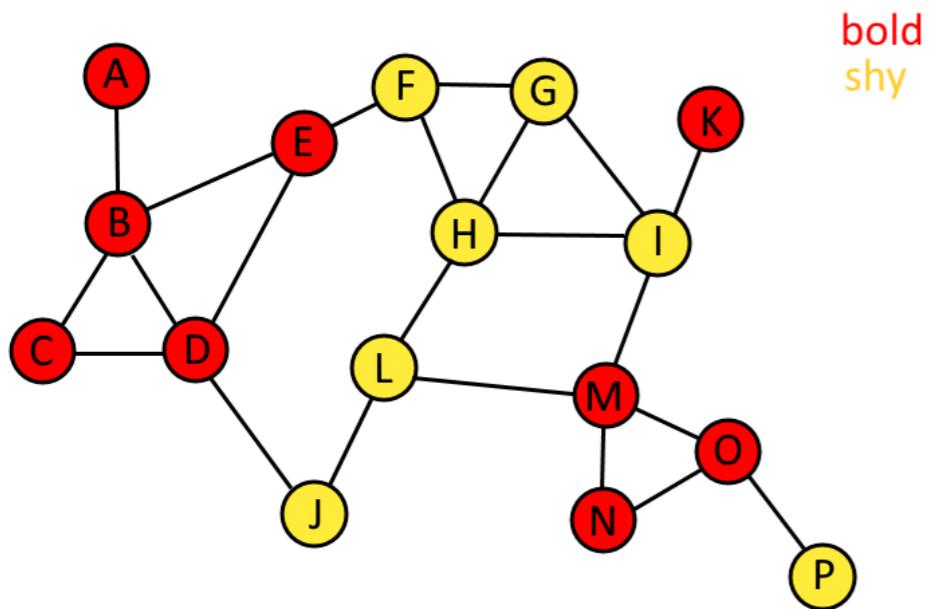


```
max_cliques(g)
```

```
...  
[[6]]  
+ 3/11 vertices, named:  
[1] A B E  
  
[[7]]  
+ 3/11 vertices, named:  
[1] I C F  
  
[[8]]  
+ 4/11 vertices, named:  
[1] E B F C
```

In a clique, every vertex is connected to every other vertex.

Assortativity



```
assortativity(g, values)
```

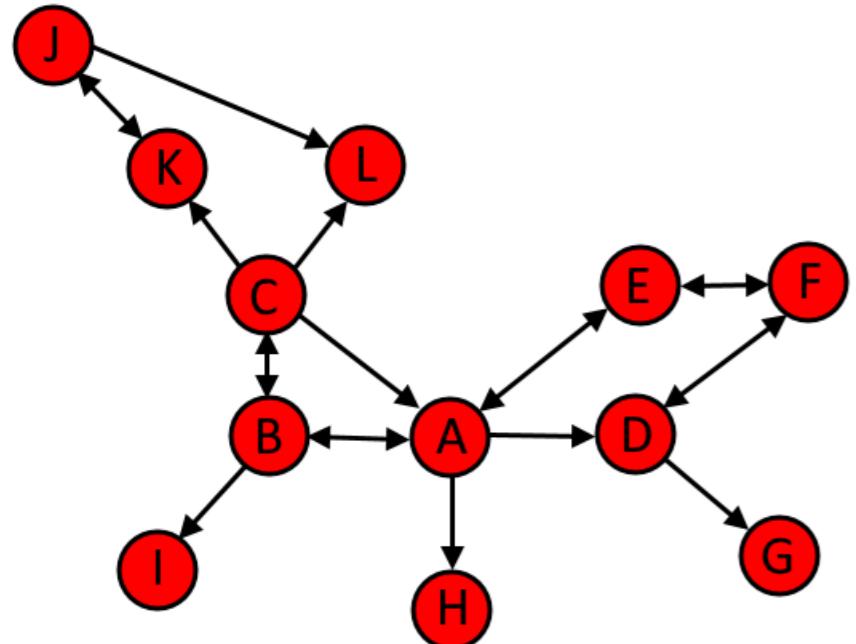
```
0.45
```

bold -> 1 and shy ->2

* 0 indicates no overall pattern of preferential attachment.

* +1 would indicate individuals only attach to similar individuals

* -1 would indicate that individuals actively avoid similar individuals.



```
reciprocity(g)
```

```
assortativity.degree(  
g,  
directed = FALSE  
)
```

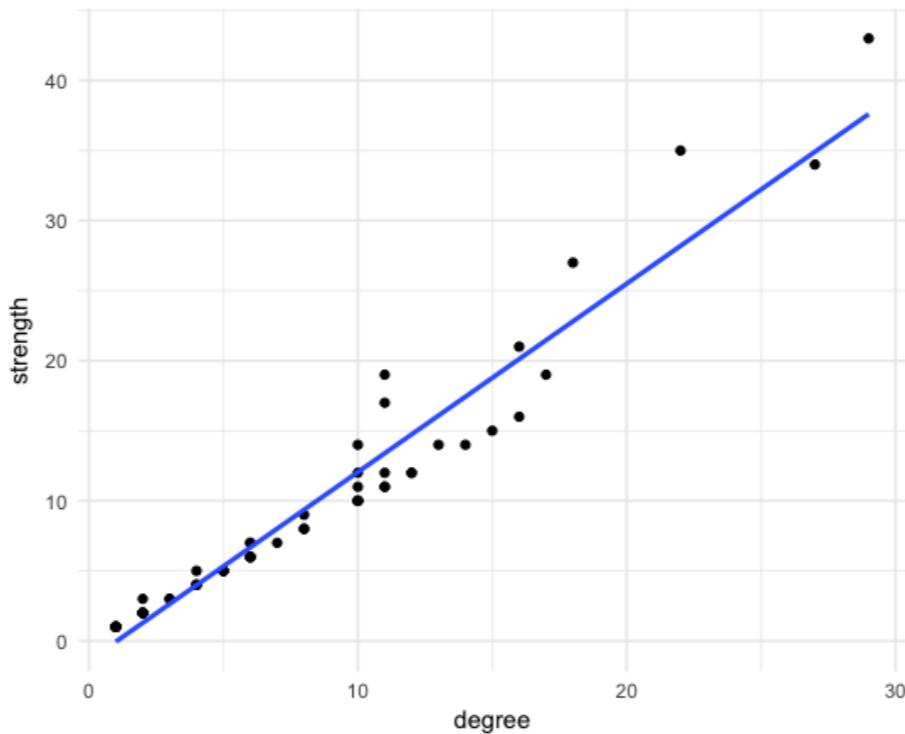
```
-0.31
```

In this example, we have a negative value for the assortativity degree indicating that highly connected individuals do not connect preferentially to other highly connected individuals.

```
0.6
```

Visualizing correlation

```
# scatterplot of degree and strength
ggplot(data = nodes, mapping = aes(x = degree, y = strength)) +
  geom_point() +
  geom_smooth(method = "lm", se = FALSE)
```



Computing correlation

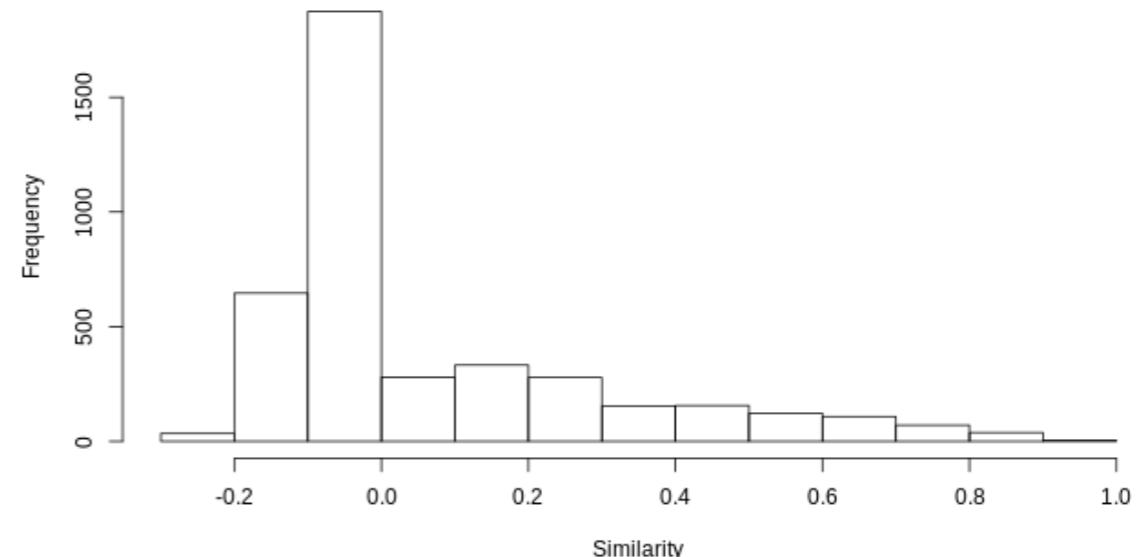
- Positive values indicate positive correlation
- Negative values indicate negative correlation
- Null values indicate no correlation

```
# Pearson correlation coefficient  
cor(nodes$degree, nodes$strength)
```

0.9708946

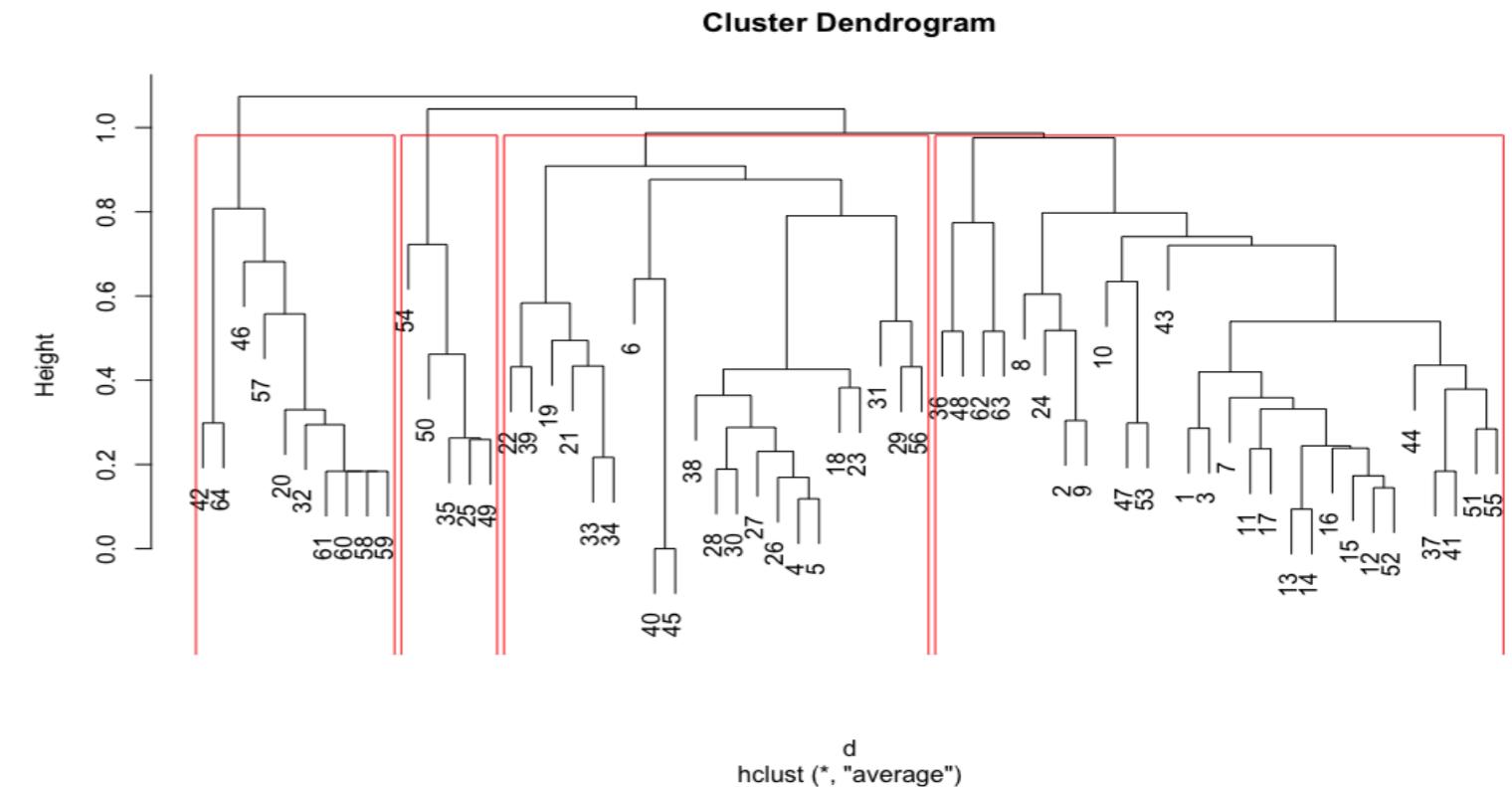
```
# graph to matrix  
A <- as adjacency matrix(g)  
  
# Compute the Pearson correlation matrix of A  
S <- cor(A)  
  
# Set the diagonal of S to 0  
diag(S) <- 0  
  
# Flatten S to be a vector  
flat_S <- as.vector(S)  
  
# Plot a histogram of similarities  
hist(flat_S, xlab = "Similarity",  
     main = "Histogram of similarity")
```

Histogram of similarity



Hierarchical clustering in R

```
# distance matrix from similarity matrix  
D <- 1-S  diag(S) = 0  
  
# distance object from distance matrix  
d <- as.dist(D)  
  
# average-linkage clustering method  
cc <- hclust(d, method = "average")  
  
# cut dendrogram at 4 clusters  
cutree(cc, k = 4)
```



```
[1] 1 1 1 2 2 2 1 1 1 1 1 1 1 1 1 1 1 1 1 1 2 2 3 2 2 2 1 4 2 2 2  
[29] 2 2 2 3 2 2 4 1 1 2 2 2 1 3 1 1 2 3 1 1 4 4 1 1 1 4 1 2  
[57] 3 3 3 3 3 1 1 3
```

The similarity measure

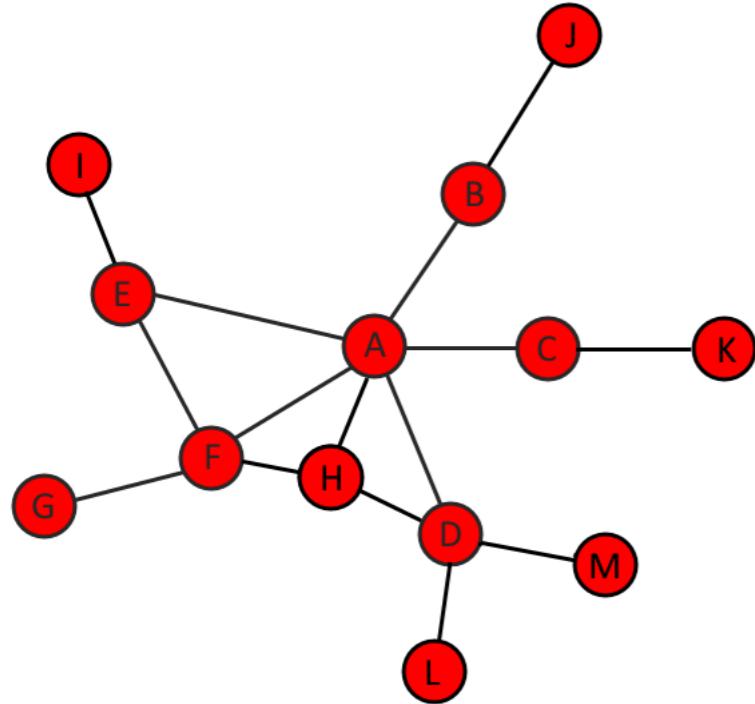
- **Single-linkage:** the similarity between two groups is the maximum of the similarities between nodes of different groups.
- **Complete-linkage:** the similarity between two groups is the minimum of the similarities between nodes of different groups.
- **Average-linkage:** the similarity between two groups is the average of the similarities between nodes of different groups.

The clustering algorithm

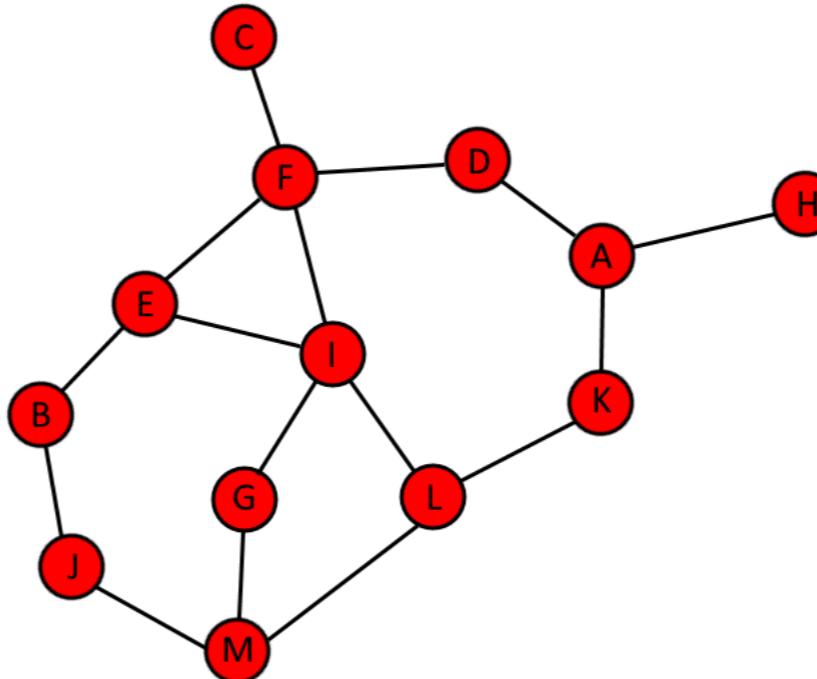
1. Evaluate the similarity measures for all node pairs.
2. Assign each node to a group of its own.
3. Find the pair of groups with the highest similarity and join them together into a single group.
4. Calculate the similarity between the new composite group and all others.
5. Repeat steps 3 and 4 until all nodes have been joined into a single group.

Random graphs

density = 0.19
vertices = 13



density = 0.21
vertices = 13



```
erdos.renyi.game(n = gorder(g), p.or.m = edge_density(g), type = "gnp")
```

Number of
vertices

Density
or
Number of edges

type = "gnp"
type = "gnm"

Random graphs & randomization tests

1. Generate 1000 random graphs based on the original network
 - e.g. with the same number of vertices and approximate density.
2. Calculate the **average path length** of the original network.
3. Calculate the average path length of the 1000 random networks.
4. Determine how many random networks have an average path length greater or less than the original network's average path length.

Generate 1000 random graphs:

```
gl <- vector('list',1000)

for(i in 1:1000){
  gl[[i]] <- erdos.renyi.game(
    n = gorder(g),
    p.or.m = edge_density(g),
    type = "gnp"
  )
}
```

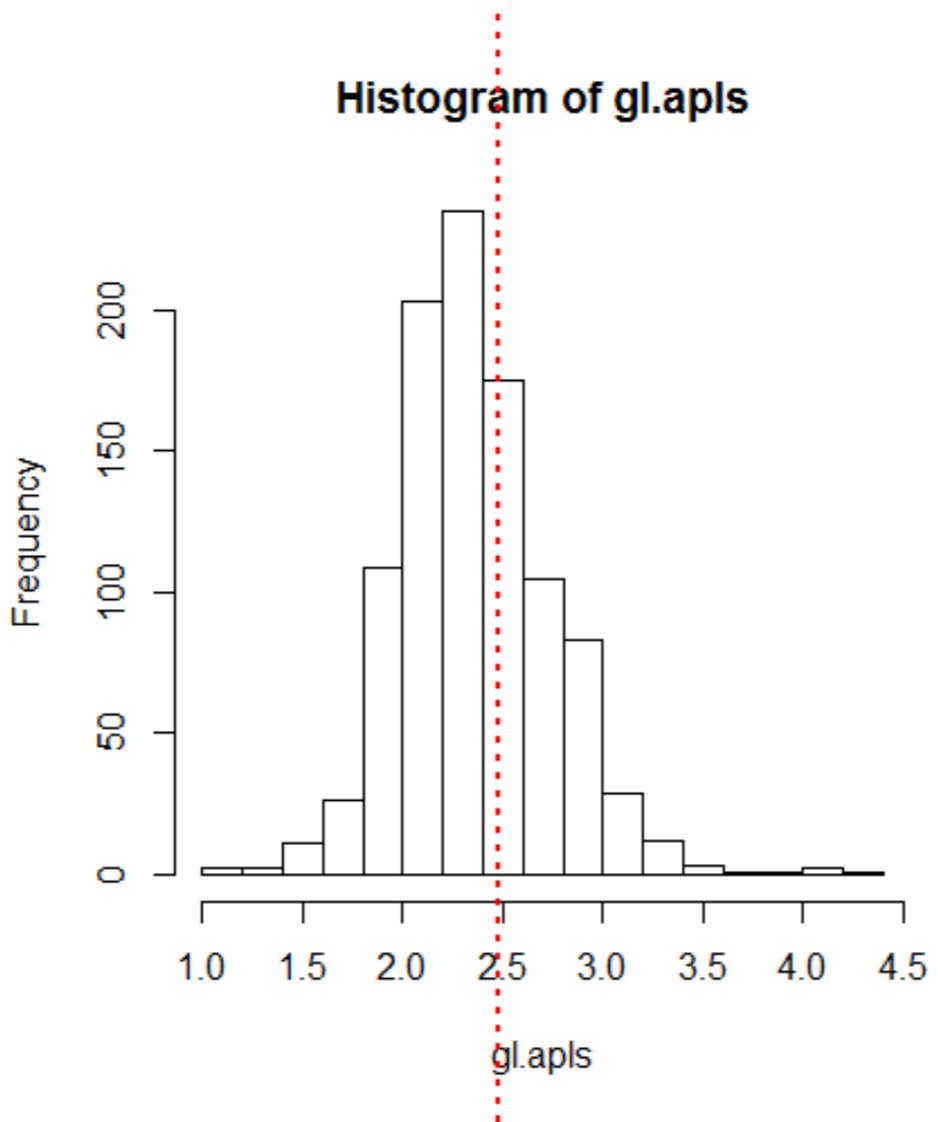
Calculate average path length of 1000 random graphs:

```
gl.apls <- unlist(
  lapply(gl, mean_distance, directed = FALSE)
)
```

Comparing to the original network

```
hist(gl.apls, breaks = 20)

abline(
  v = mean_distance(
    g, directed=FALSE
  ),
  col = "red",
  lty = 3,
  lwd = 2
)
```



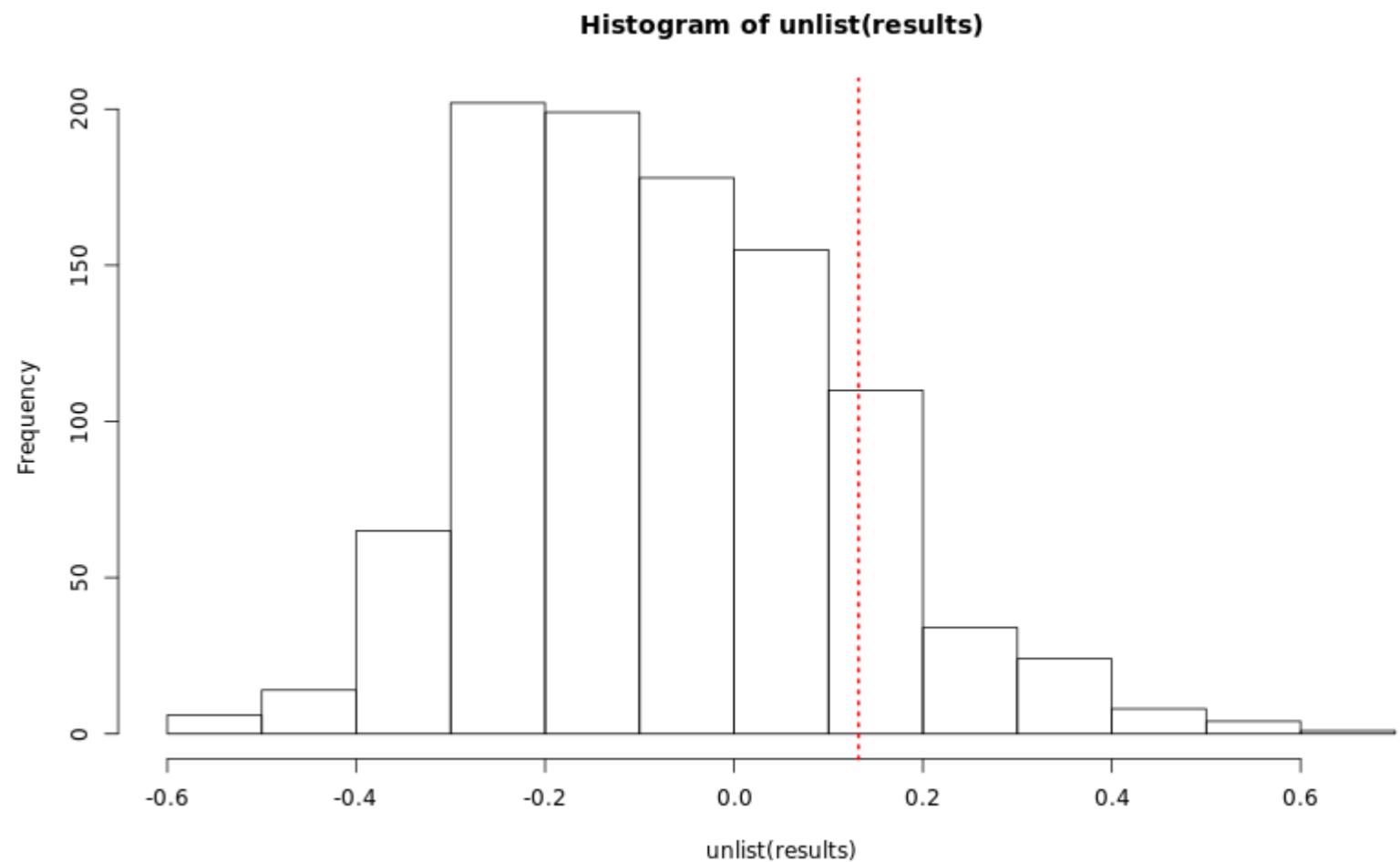
Or we can sample the groups

```
# Calculate the observed assortativity
observed.assortativity <- assortativity(g1, values)

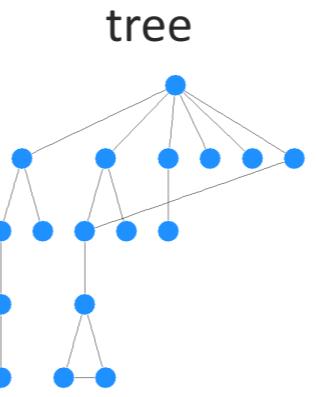
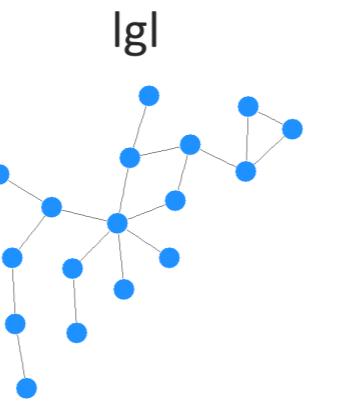
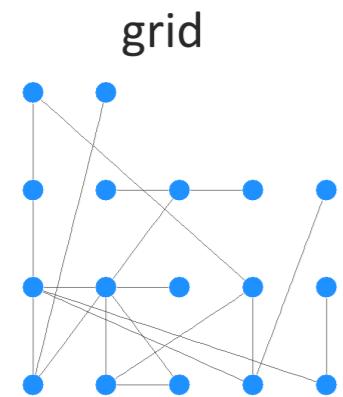
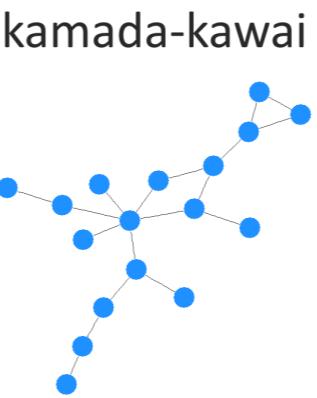
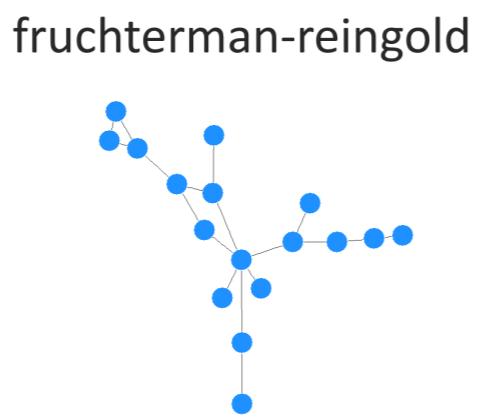
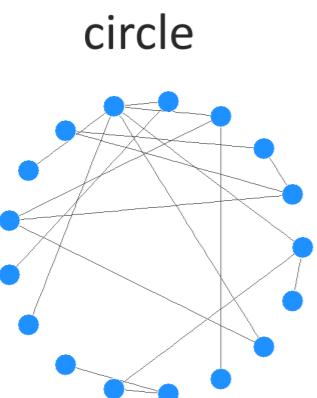
# Calculate the assortativity of the network
# randomizing the gender attribute 1000 times
results <- vector('list', 1000)

for(i in 1:1000){
  results[[i]] <- assortativity(g1, sample(values))
}

# Plot the distribution of assortativity values
# and add a red vertical line at the original
# observed value
hist(unlist(results))
abline(v = observed.assortativity,
       col = "red",
       lty = 3,
       lwd=2)
```



igraph layouts



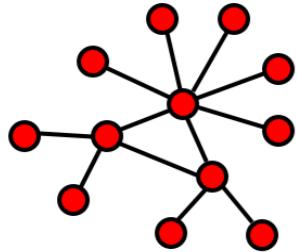
```
plot(g, layout = layout.fruchterman.reingold(g))
```

```
ls("package:igraph", pattern = "layout_")
```

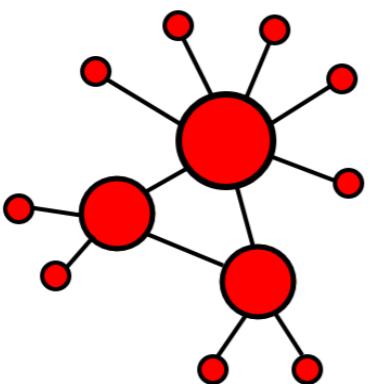
layout_as_bipartite
layout_as_star
layout_as_tree
layout_components
layout_in_circle
layout_nicely
layout_on_grid
layout_on_sphere
layout_randomly
layout_with_dh
layout_with_drl
layout_with_fr
layout_with_gem
layout_with_graphopt
layout_with_kk
layout_with_lgl
layout_with_mds
layout_with_sugiyama

Styling vertices and edges

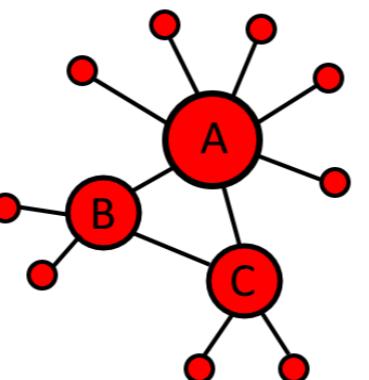
default



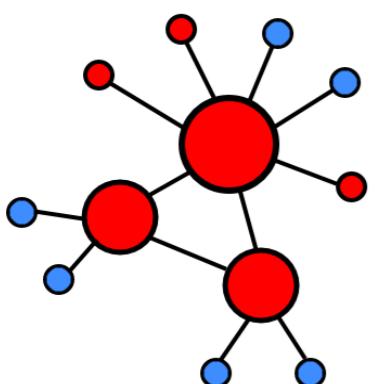
size



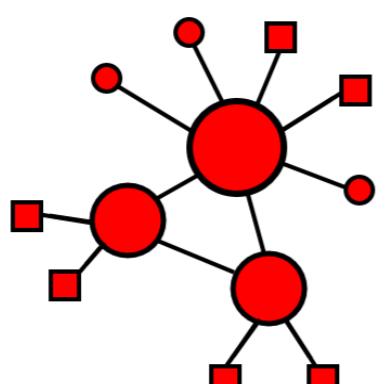
labels



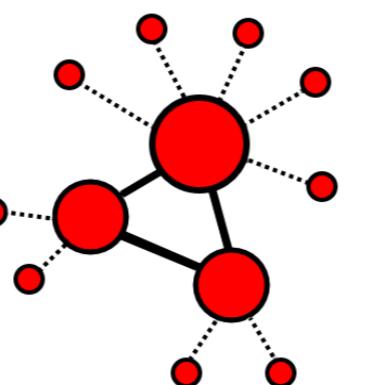
color



shape



edges



OTHER

margin Empty space margins around the plot, vector with length 4

frame if TRUE, the plot will be framed

main If set, adds a title to the plot

sub If set, adds a subtitle to the plot

NODES

vertex.color Node color

vertex.frame.color Node border color

vertex.shape One of "none", "circle", "square", "csquare", "rectangle", "crectangle", "vrectangle", "pie", "raster", or "sphere"

vertex.size Size of the node (default is 15)

vertex.size2 The second size of the node (e.g. for a rectangle)

vertex.label Character vector used to label the nodes NA

vertex.label.family Font family of the label (e.g. "Times", "Helvetica")

vertex.label.font Font: 1 plain, 2 bold, 3, italic, 4 bold italic, 5 symbol

vertex.label.cex Font size (multiplication factor, device-dependent)

vertex.label.dist Distance between the label and the vertex

vertex.label.degree The position of the label in relation to the vertex, where 0 right, "pi" is left, "pi/2" is below, and "-pi/2" is above

EDGES

edge.color Edge color

edge.width Edge width, defaults to 1

edge.arrow.size Arrow size, defaults to 1

edge.arrow.width Arrow width, defaults to 1

edge.lty Line type, could be 0 or "blank", 1 or "solid", 2 or "dashed", 3 or "dotted", 4 or "dotdash", 5 or "longdash", 6 or "twodash"

edge.label Character vector used to label edges

edge.label.family Font family of the label (e.g. "Times", "Helvetica")

edge.label.font Font: 1 plain, 2 bold, 3, italic, 4 bold italic, 5 symbol

edge.label.cex Font size for edge labels

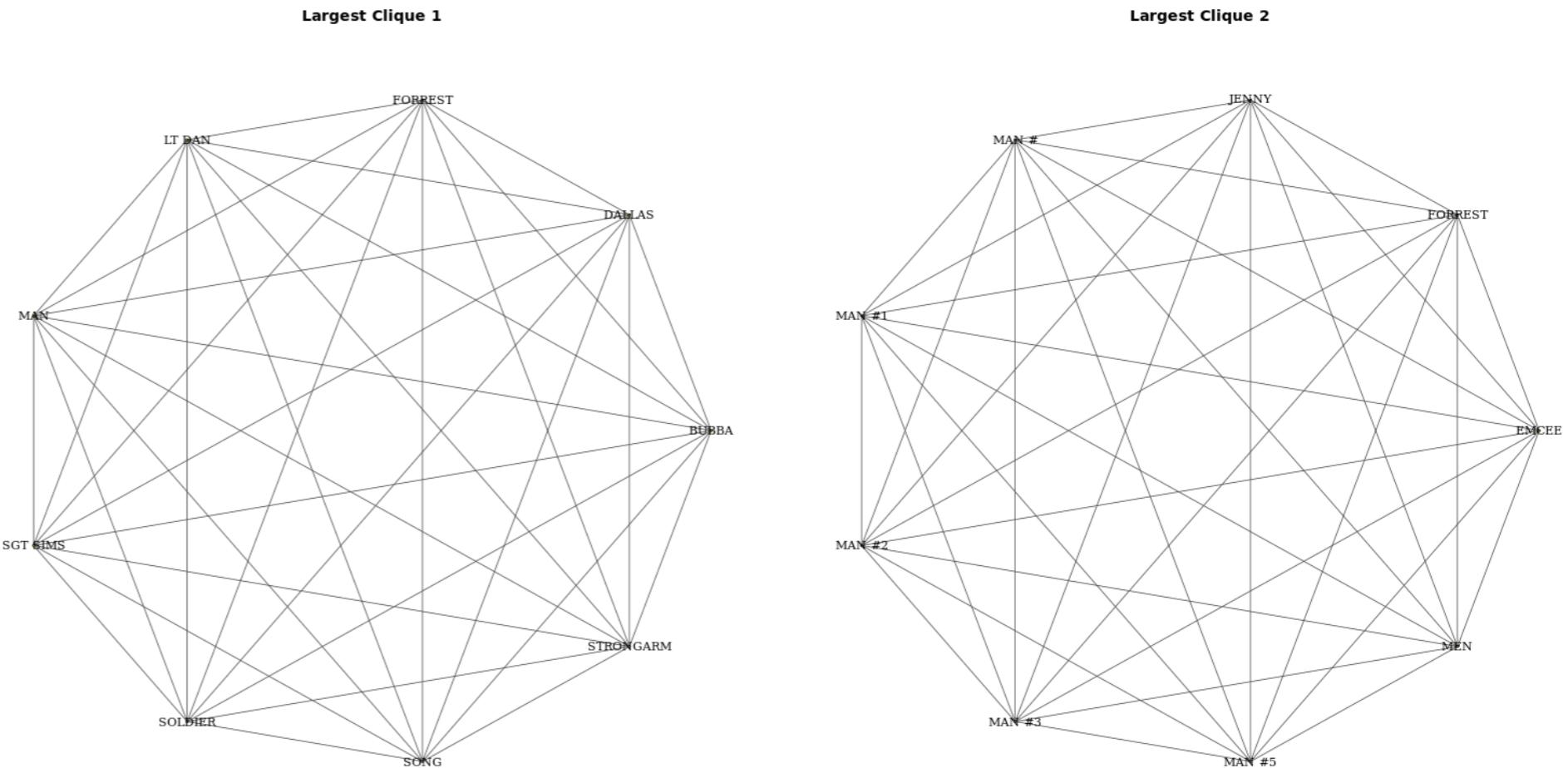
edge.curved Edge curvature, range 0-1 (FALSE sets it to 0, TRUE to 0.5)

arrow.mode Vector specifying whether edges should have arrows, possible values: 0 no arrow, 1 back, 2 forward, 3 both

Source: <https://kateto.net/netscix2016.html>

Side-by-side Plot Example

```
# Plot the two largest cliques side-by-side  
  
par(mfrow=c(1,2)) # To plot two plots side-by-side  
  
plot(gs1,  
      vertex.label.color = "black",  
      vertex.label.cex = 0.9,  
      vertex.size = 0,  
      edge.color = 'gray28',  
      main = "Largest Clique 1",  
      layout = layout.circle(gs1)  
)  
  
plot(gs2,  
      vertex.label.color = "black",  
      vertex.label.cex = 0.9,  
      vertex.size = 0,  
      edge.color = 'gray28',  
      main = "Largest Clique 2",  
      layout = layout.circle(gs2)  
)
```



```
x <- fastgreedy.community(g)  
length(x)
```

```
[1] 3
```

```
sizes(x)
```

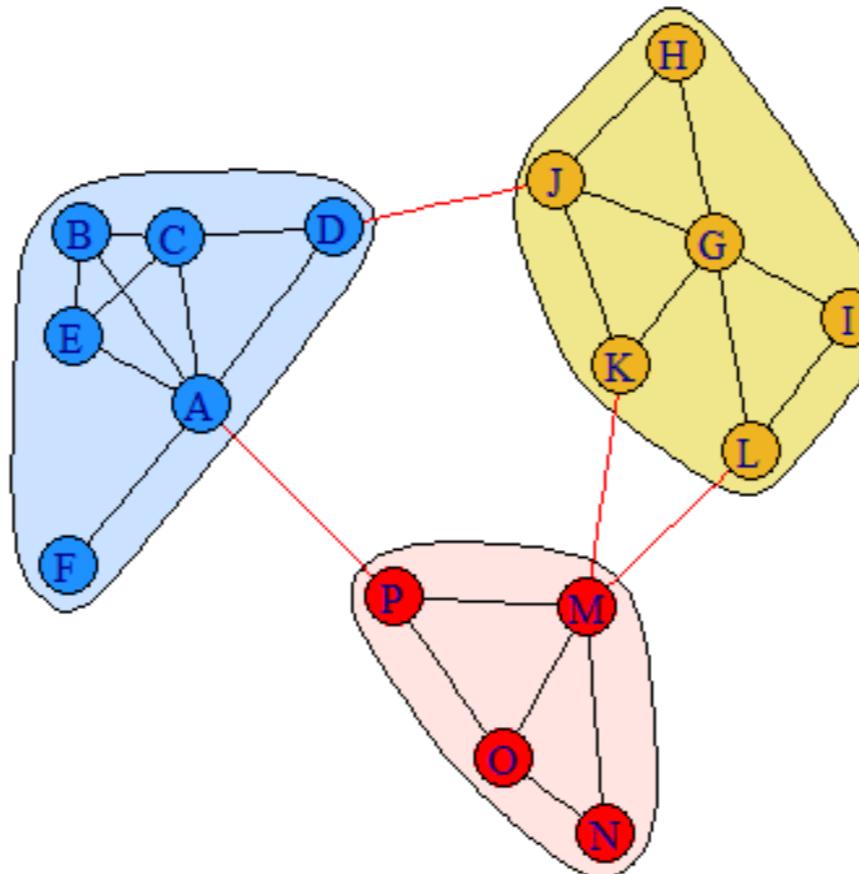
```
Community sizes
```

```
1 2 3  
6 6 4
```

```
membership(x)
```

```
A B C D E F J G H I K L M N O P  
1 1 1 1 1 1 2 2 2 2 2 3 3 3 3 3
```

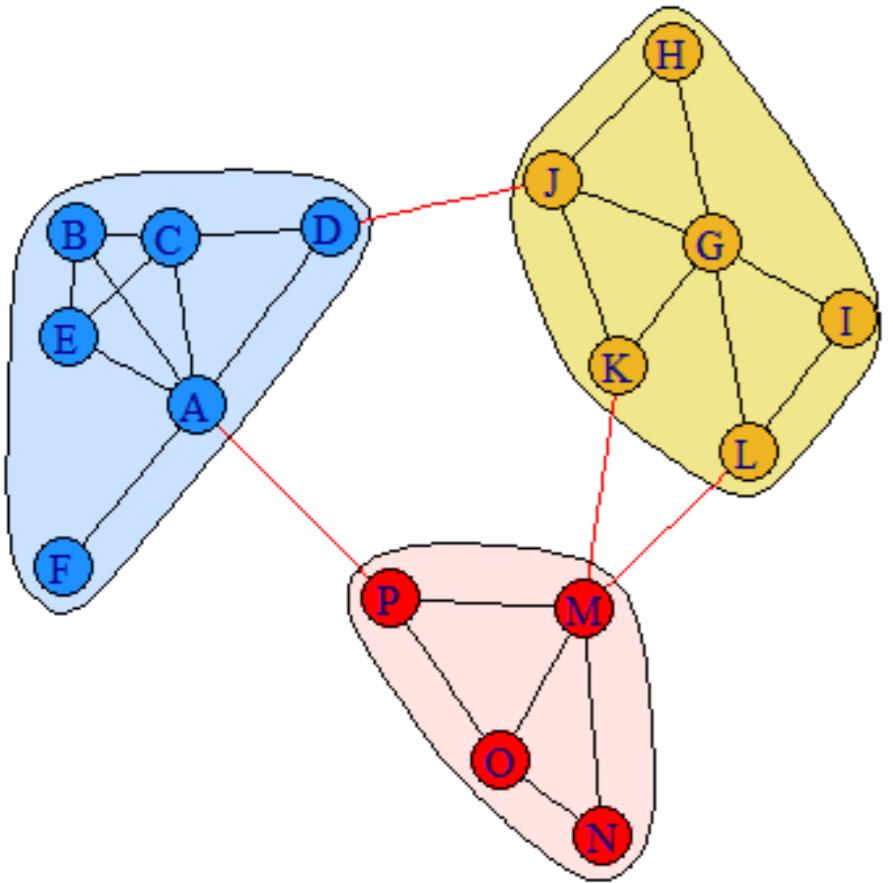
```
plot(x, g)
```



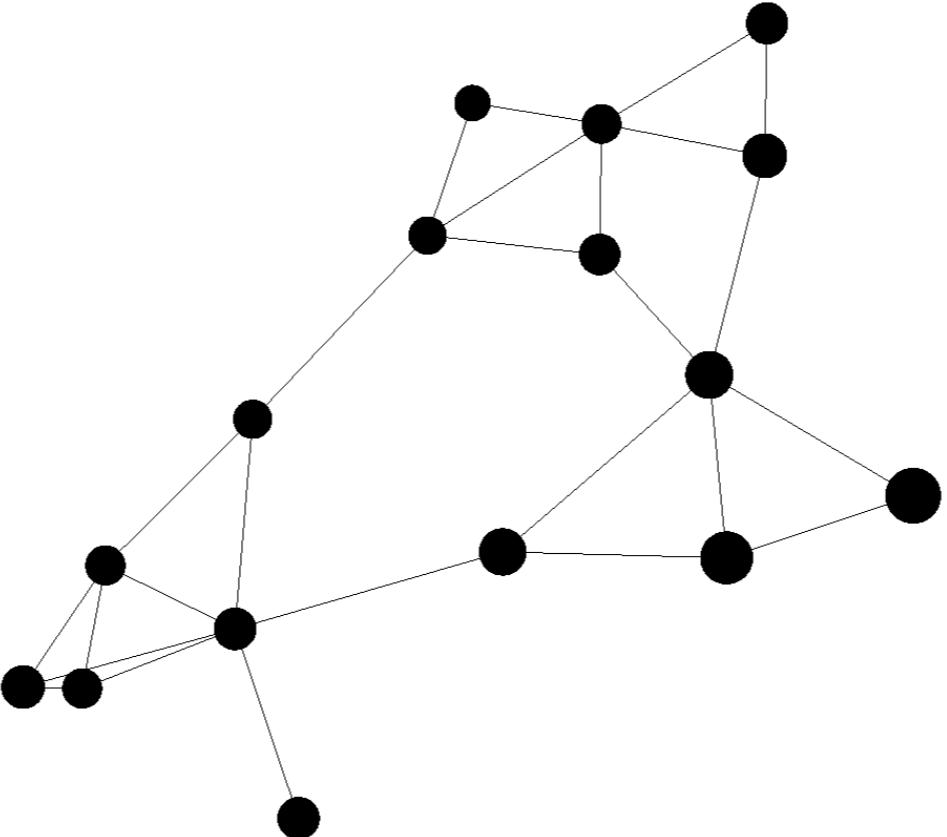
R network visualization packages

- igraph
- statnet
- ggnet
- ggnetwork
- ggraph
- visNetwork
- networkD3
- sigma
- rgexf (igraph to Gephi)
- **threejs**

Creating a threejs visualization

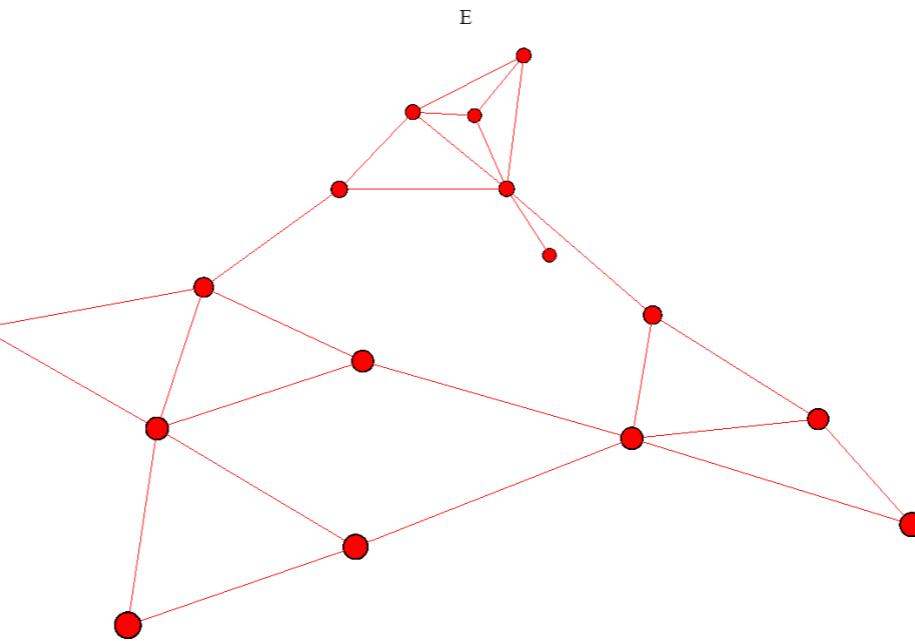


```
library(threejs)  
graphjs(g)
```



Adding attributes

```
g <- set_vertex_attr(  
  g,  
  "label",  
  value = V(g)$name  
)  
  
g <- set_vertex_attr(  
  g,  
  "color",  
  value = "mistyrose"  
)  
  
graphjs(g, vertex.size = 1)
```

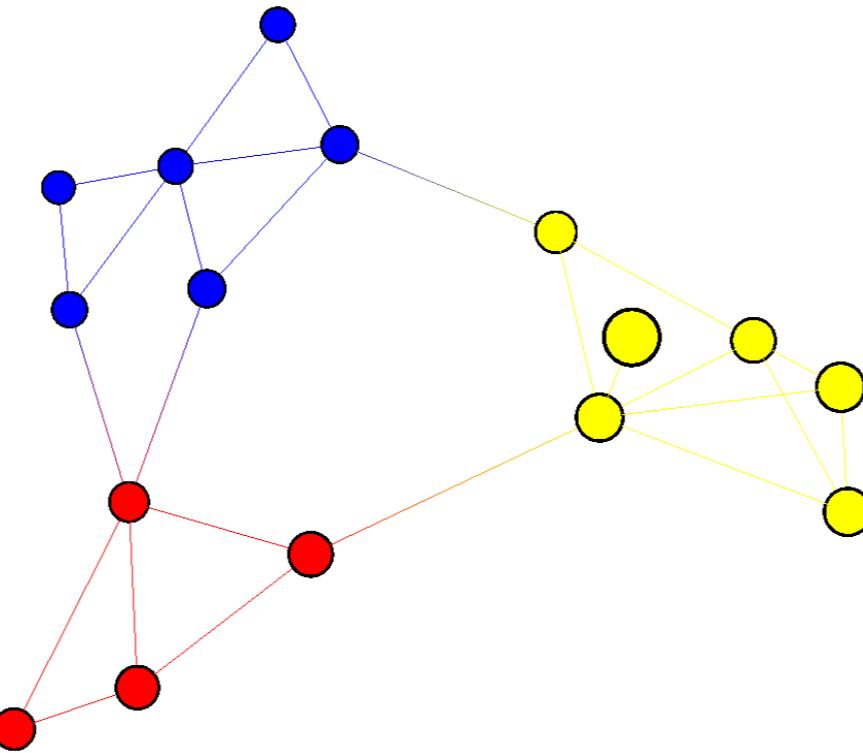


Coloring communities

```
x = edge.betweenness.community(g)
i <- membership(x)

g <- set_vertex_attr(
  g,
  "color",
  value = c(
    "yellow", "blue", "red"
  )[i]
)

graphjs(g)
```



visNetwork

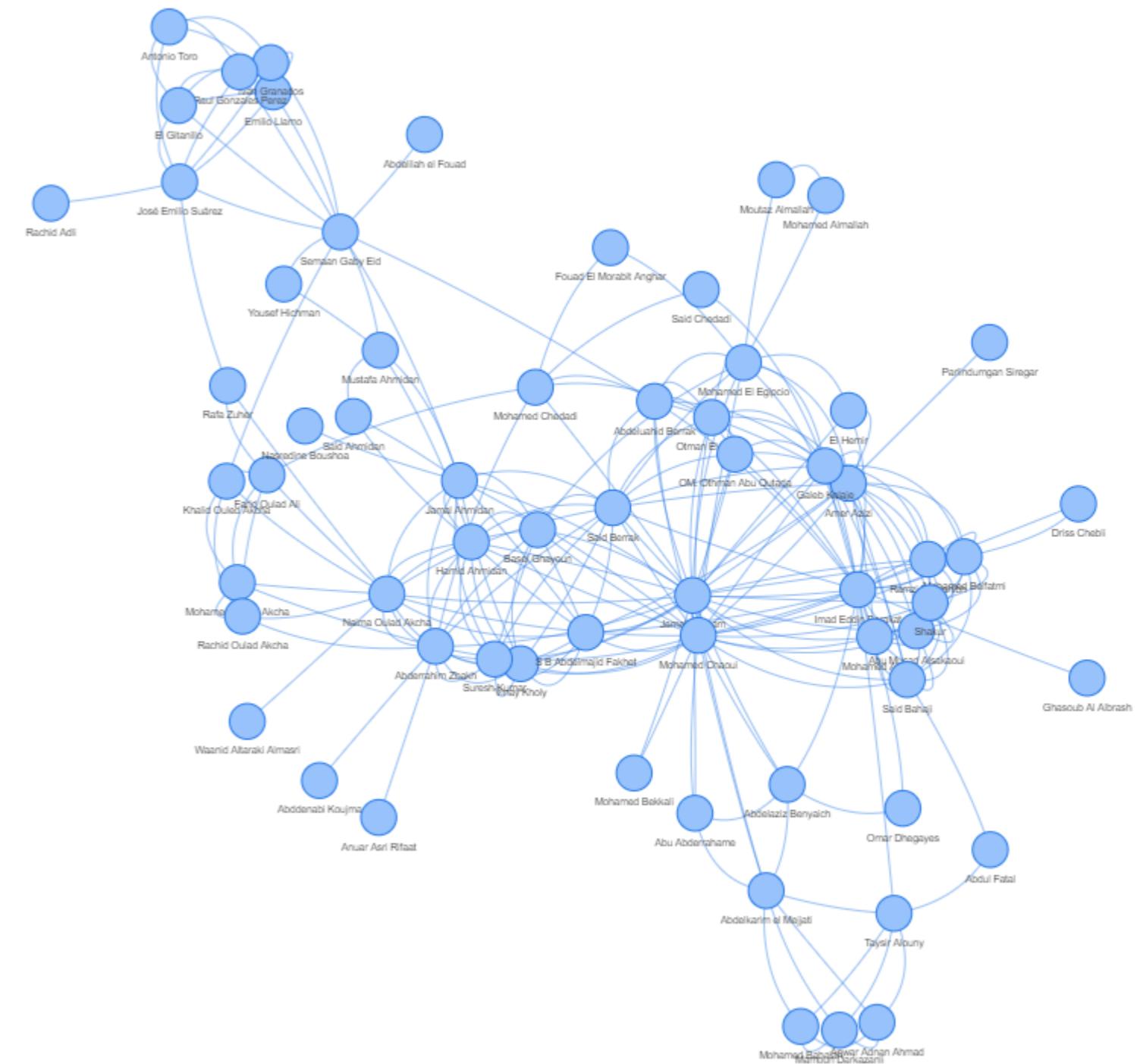
```
# From previous step  
data <- toVisNetworkData(g)  
  
# Visualize the network  
visNetwork(nodes = data$nodes,  
           edges = data$edges,  
           width = 800, height = 800)
```

```
head(data$nodes)
```

			id	degree	strength	cluster		label
Jamal Zougam	Jamal Zougam		29	43	1	1	Jamal Zougam	
Mohamed Bekkali	Mohamed Bekkali		2	2	1	1	Mohamed Bekkali	
Mohamed Chaoui	Mohamed Chaoui		27	34	1	1	Mohamed Chaoui	
Vinay Kholy	Vinay Kholy		10	10	2	2	Vinay Kholy	
Suresh Kumar	Suresh Kumar		10	10	2	2	Suresh Kumar	
Mohamed Chedadi	Mohamed Chedadi		7	7	2	2	Mohamed Chedadi	

```
head(data$edges)
```

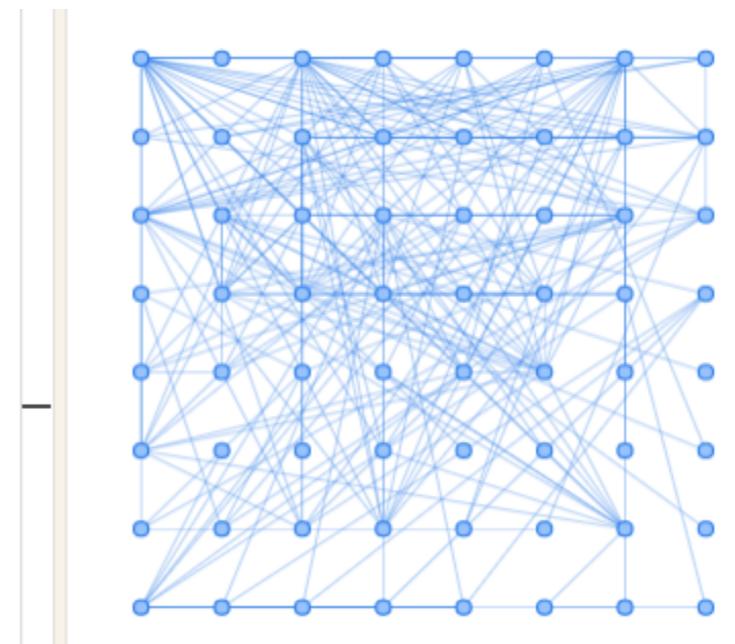
	from		to	weight	betweenness
1	Jamal Zougam	Mohamed Bekkali		1	47.41667
2	Jamal Zougam	Mohamed Chaoui		3	16.00000
3	Jamal Zougam	Vinay Kholy		1	27.08333
4	Jamal Zougam	Suresh Kumar		1	27.08333
5	Jamal Zougam	Mohamed Chedadi		1	47.66190
6	Jamal Zougam	Imad Eddin Barakat		4	268.00000



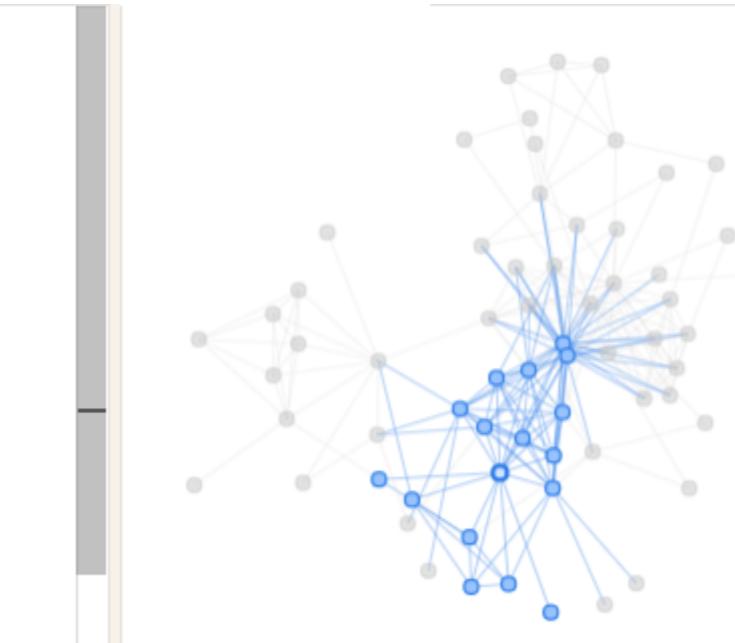
visNetwork

```
# See a list of possible layouts
ls("package:igraph", pattern = "layout_.")

# Update the plot
visNetwork(nodes = data$nodes, edges = data$edges,
           width = 300, height = 300) %>%
  # Change the layout to be on a grid
  visIgraphLayout(layout = "layout_on_grid")
```

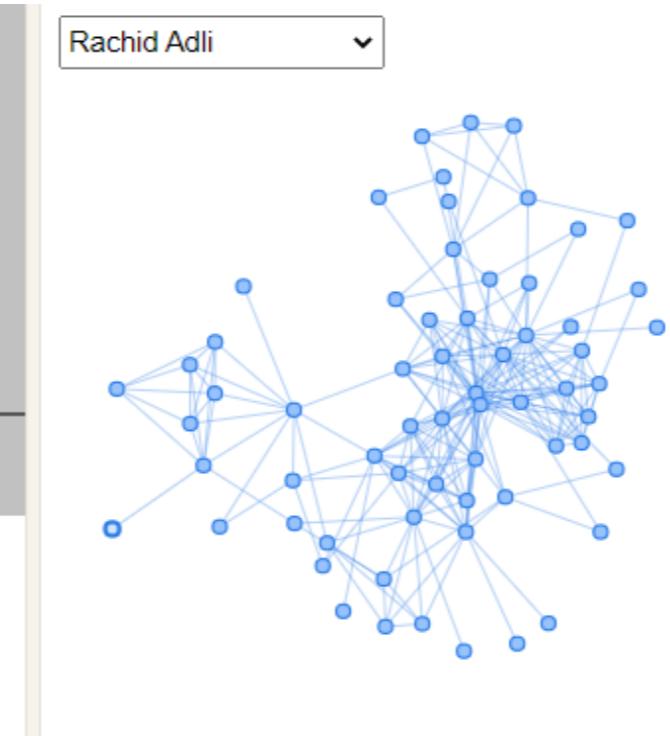


```
# Add to the plot
visNetwork(nodes = data$nodes, edges = data$edges,
           width = 300, height = 300) %>%
  # Choose an operator
  visIgraphLayout(layout = "layout_with_kk") %>%
  # Change the options to highlight
  # the nearest nodes and ties
  visOptions(highlightNearest = TRUE)
```



visNetwork

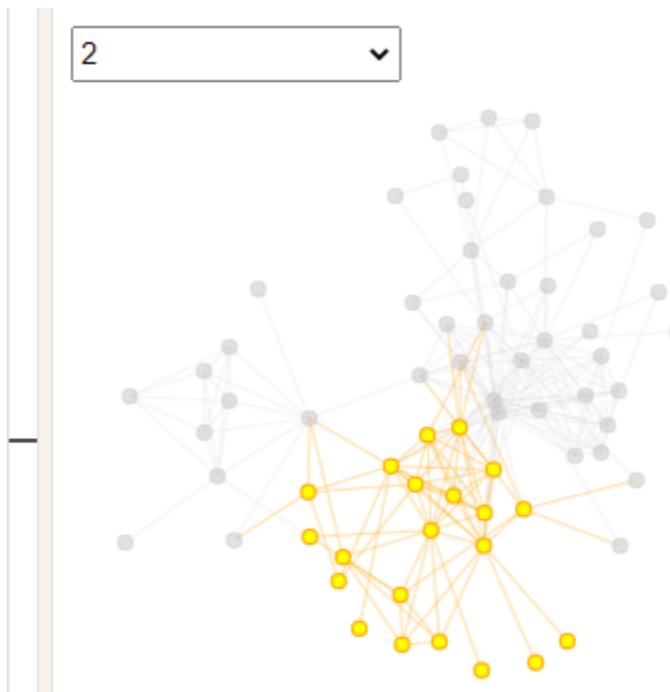
```
# Update the plot  
visNetwork(nodes = data$nodes, edges = data$edges,  
           width = 300, height = 300) %>%  
  visIgraphLayout(layout = "layout_with_kk") %>%  
# Change the options to allow selection  
# of nodes by ID  
visOptions(nodesIdSelection = TRUE)
```



```
# Copy cluster node attribute to color node attribute  
V(g)$color <- V(g)$cluster
```

```
# Convert g to vis network data  
data <- toVisNetworkData(g)
```

```
# Update the plot  
visNetwork(nodes = data$nodes, edges = data$edges,  
           width = 300, height = 300) %>%  
  visIgraphLayout(layout = "layout_with_kk") %>%  
# Change options to select by group  
visOptions(selectedBy = "group")
```



ggraph()

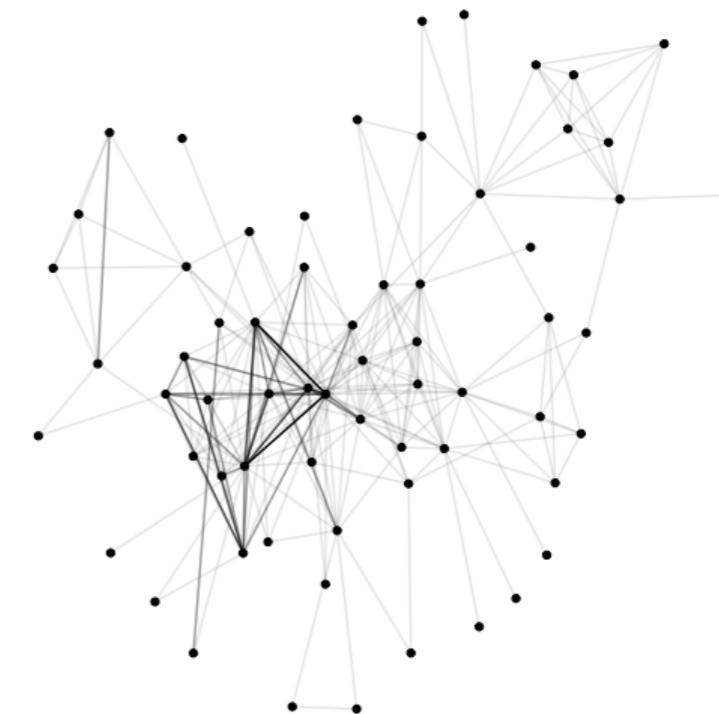
```
library(igraph)
library(dplyr)
library(ggplot2)
library(ggraph)
```

- Geometries for nodes have names starting `geom_node_`. For example, `geom_node_point()` draws each node as a point. `geom_node_text()` draws a text label on each node.
- Geometries for ties have names starting `geom_edge_`. For example, `geom_edge_link()` draws edges as a straight line between nodes.

For your convenience, `ggraph` is already loaded, the *graph theme* is set with the function `set_graph_style()`, and the network `g` is at your disposal.

```
# visualize the network
ggraph(g, layout = "with_kk") +
  geom_edge_link(aes(alpha = weight)) +
  geom_node_point()
```

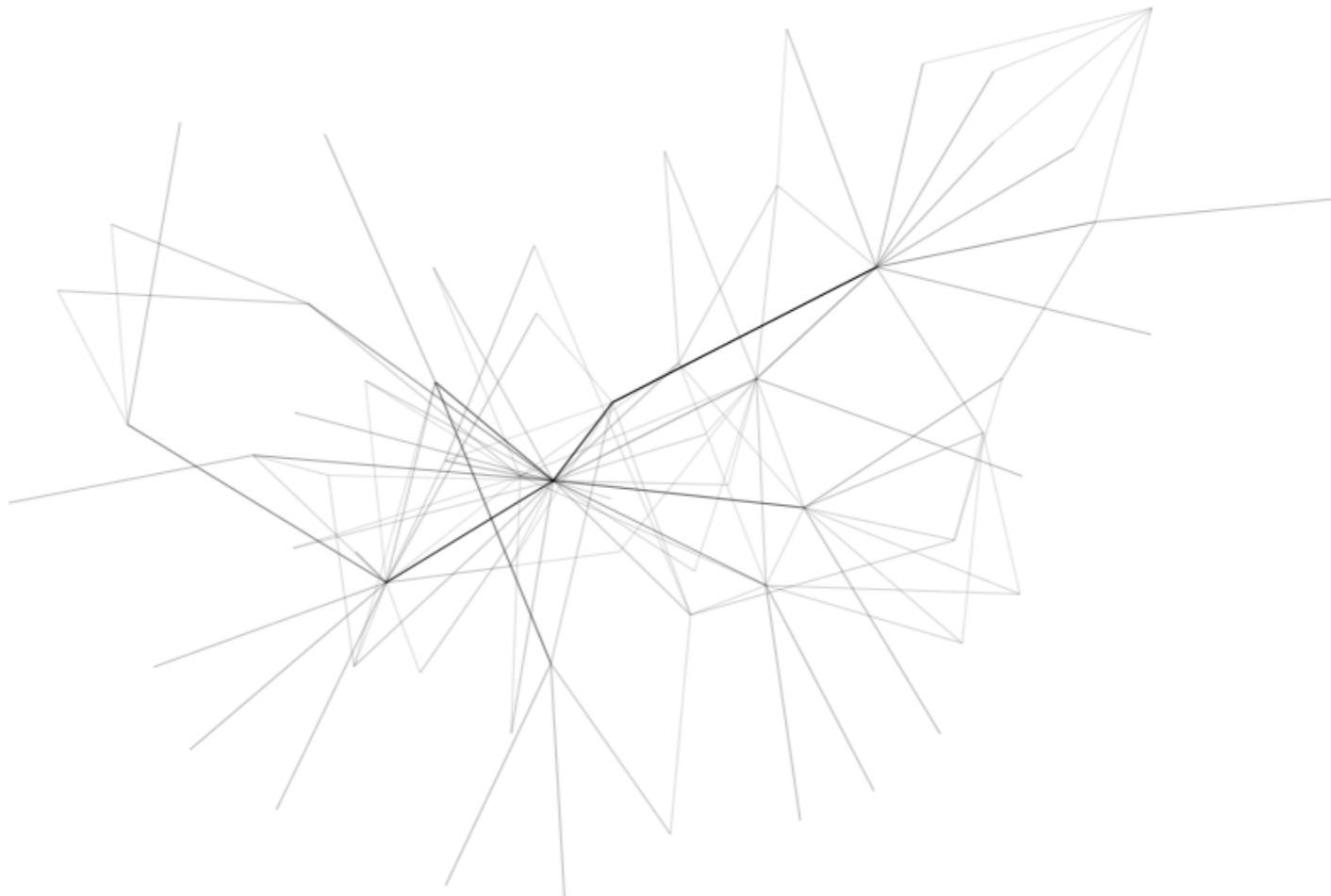
```
> ggraph:::igraphlayouts
[1] "as_bipartite"   "as_star"          "as_tree"         "in_circle"
[5] "nicely"        "with_dh"          "with_drl"        "with_gem"
[9] "with_graphopt" "on_grid"          "with_mds"        "with_sugiyama"
[13] "on_sphere"     "randomly"        "with_fr"         "with_kk"
[17] "with_lgl"
```



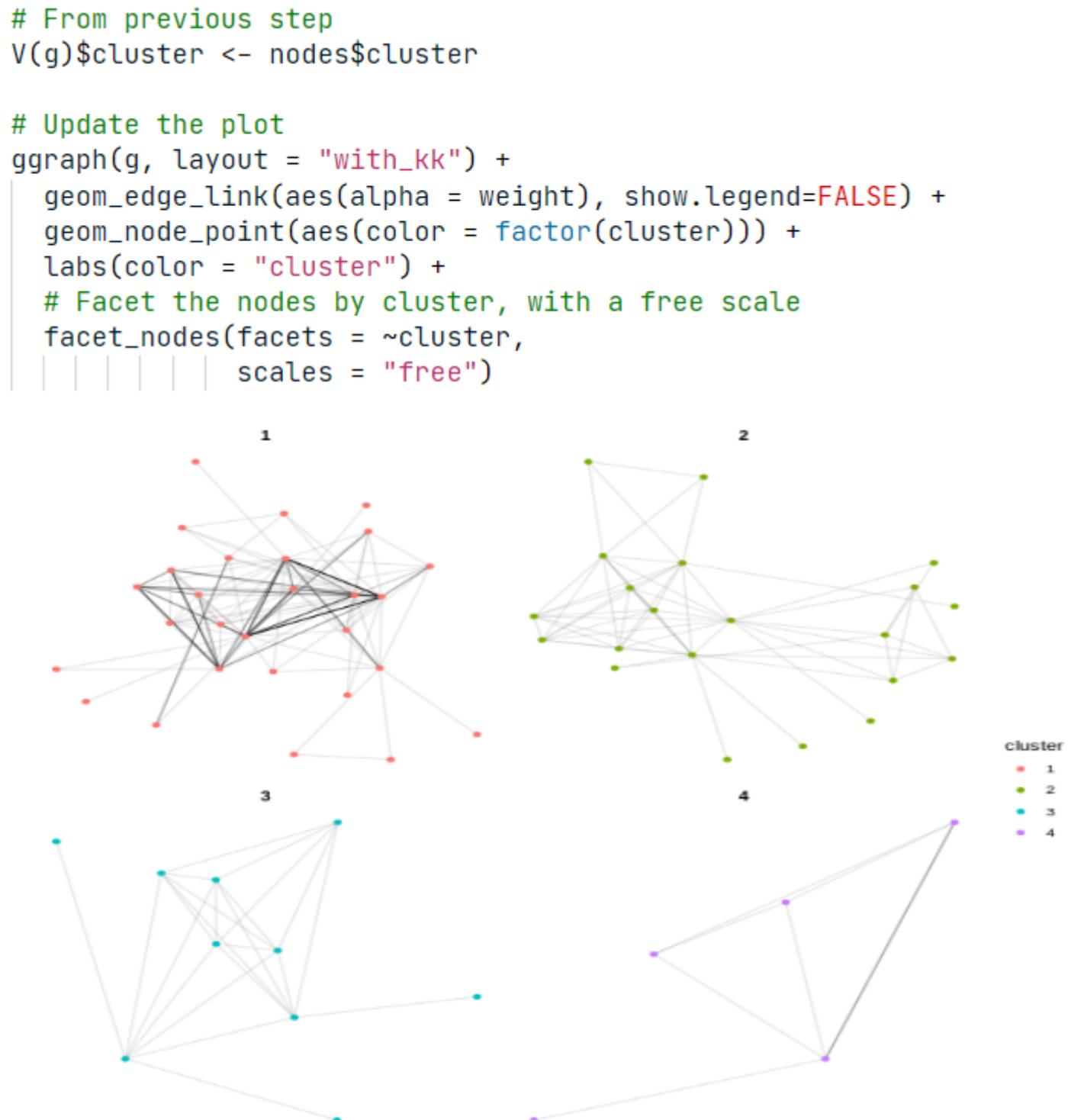
Applying filters to the network

```
# Calculate the median betweenness
median_betweenness = median(E(g)$betweenness)

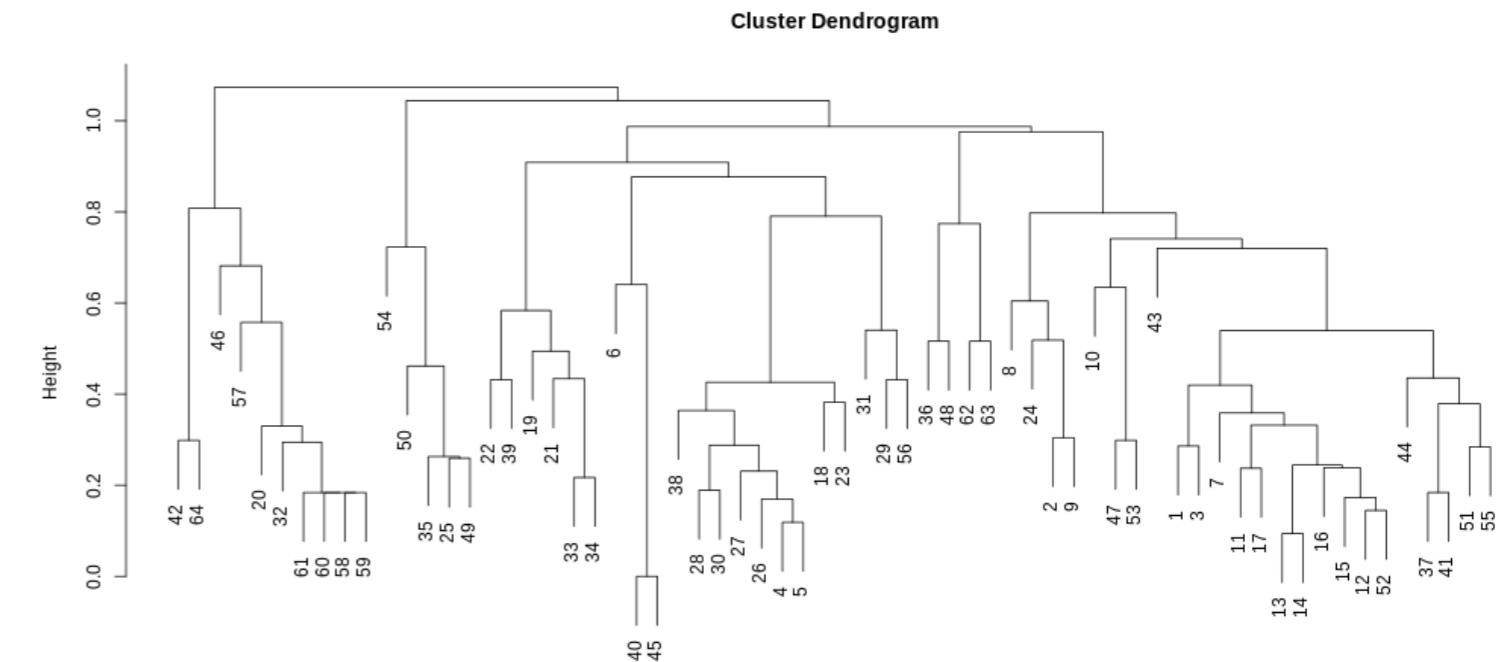
ggraph(g, layout = "with_kk") +
  # Filter ties for betweenness greater than the median
  geom_edge_link(aes(alpha = betweenness,
  filter = betweenness > median_betweenness)) +
  theme(legend.position="none")
```



Plotting clusters



plot(cc)



Motivation: social networks and predictive analytics

PREDICTIVE ANALYTICS USING NETWORKED DATA IN R

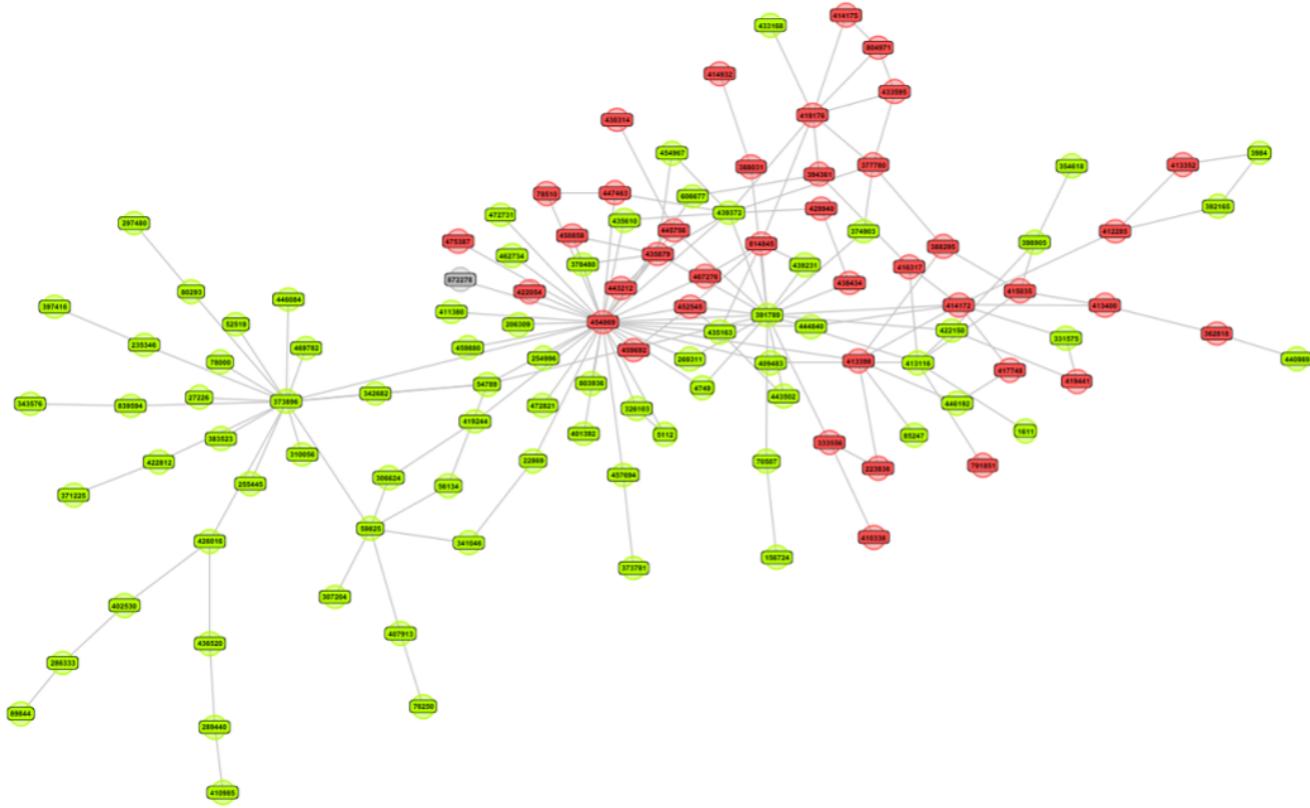
Bart Baesens, Ph.D.

Professor of Data Science, KU Leuven
and University of Southampton



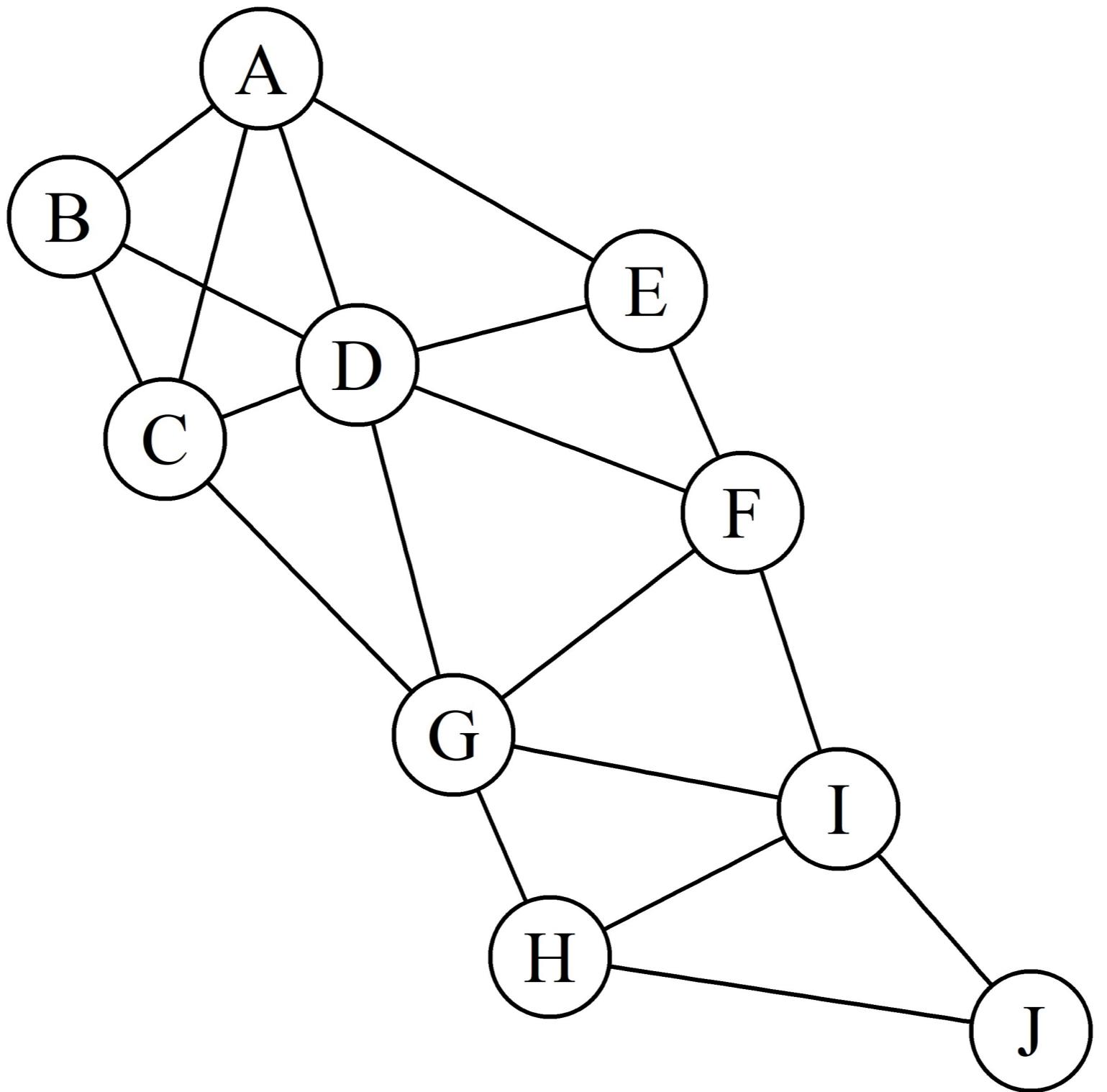
Applications

- Age
- Gender
- Fraud
- Churn
 - Customer defection
 - Companies predict who is most likely to churn using
 1. Machine learning techniques
 2. Social networks



Overview

- Labeled social networks
 - Construct and label networks
 - Network learning
- Homophily
 - Measure relational dependency
 - Heterophilicity and dyadicity
- Network featurization
 - Compute node features
- Predictive modeling with networks
 - Turn a network into a flat dataset
 - Predict churn among customers



Collaboration Network

```
library(igraph);

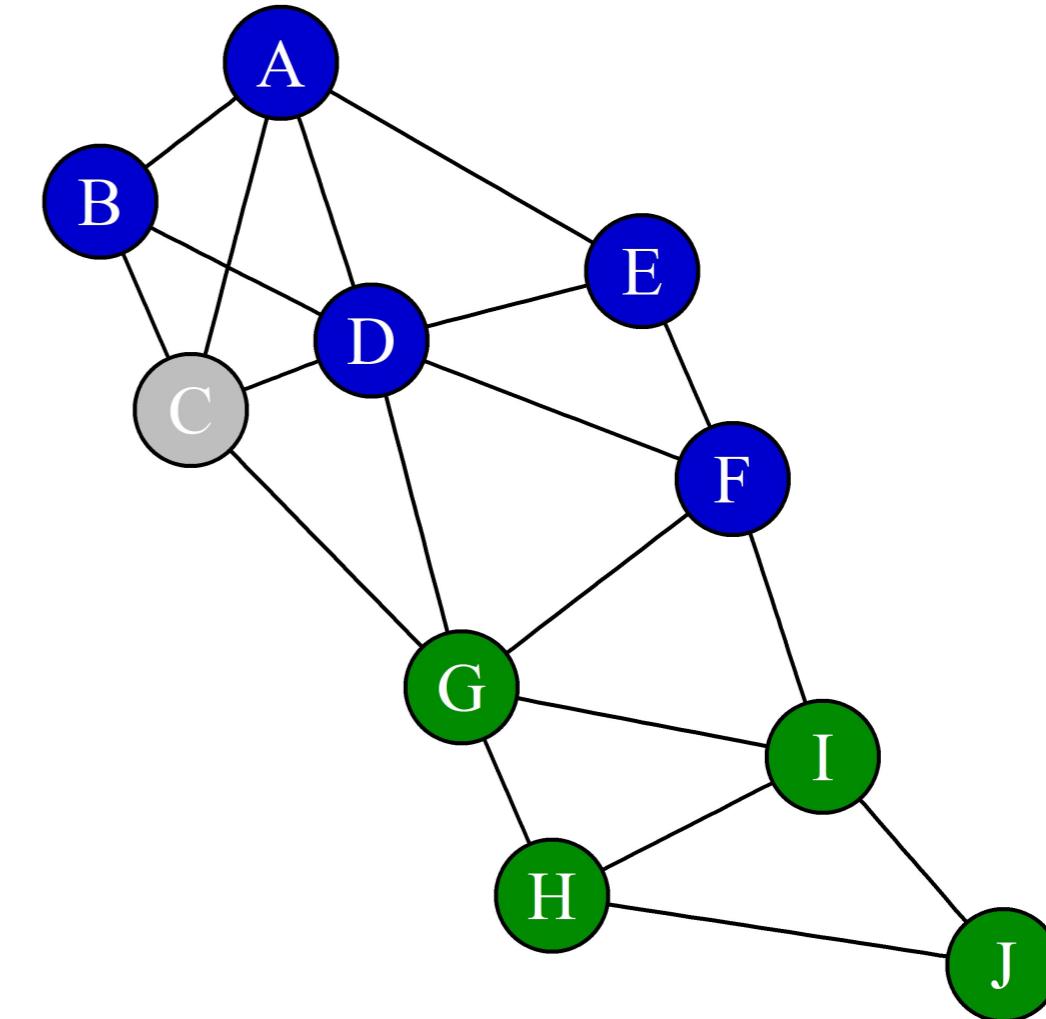
DataScienceNetwork <- data.frame(
  from = c('A', 'A', 'A', 'A', 'B', 'B', 'C', 'C', 'D', 'D', 'D', 'E',
          'F', 'F', 'G', 'G', 'H', 'H', 'I'),
  to = c('B', 'C', 'D', 'E', 'C', 'D', 'D', 'G', 'E', 'F', 'G', 'F', 'G', 'I',
         'I', 'H', 'I', 'J', 'J'))
g <- graph_from_data_frame(DataScienceNetwork, directed = FALSE)
```

```
pos <- cbind(c(2, 1, 1.5, 2.5, 4, 4.5, 3, 3.5, 5, 6),
              c(10.5, 9.5, 8, 8.5, 9, 7.5, 6, 4.5, 5.5, 4))
plot.igraph(g, edge.label = NA, edge.color = 'black', layout = pos,
            vertex.label = V(g)$name, vertex.color = 'white',
            vertex.label.color = 'black', vertex.size = 25)
```

Collaboration Network

```
v(g)$technology <-  
  c('R', 'R', '?', 'R', 'R',  
    'R', 'P', 'P', 'P', 'P')  
v(g)$color <- v(g)$technology
```

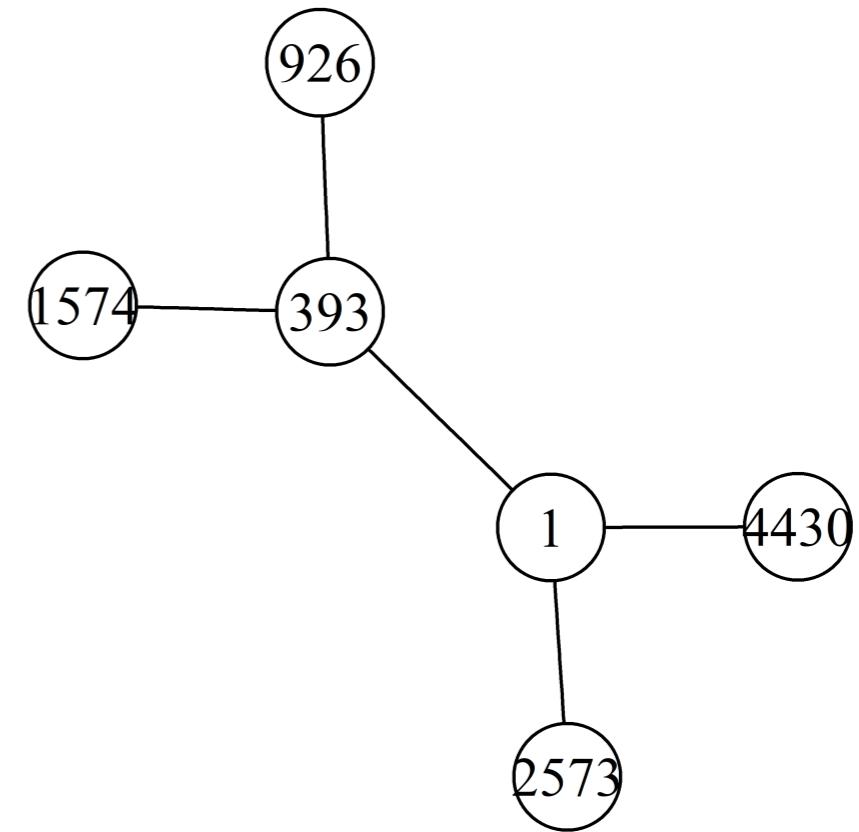
```
v(g)$color <- gsub('R', "blue3", v(g)$color)  
v(g)$color <- gsub('P', "green4", v(g)$color)  
v(g)$color <- gsub('?', "gray", v(g)$color)
```



Churn Network

edgeList

	from	to
1	1	393
2	1	2573
3	1	4430
4	393	926
5	393	1574



Let's practice!

PREDICTIVE ANALYTICS USING NETWORKED DATA IN R

Labeled networks and network learning

PREDICTIVE ANALYTICS USING NETWORKED DATA IN R



María Óskarsdóttir, Ph.D.

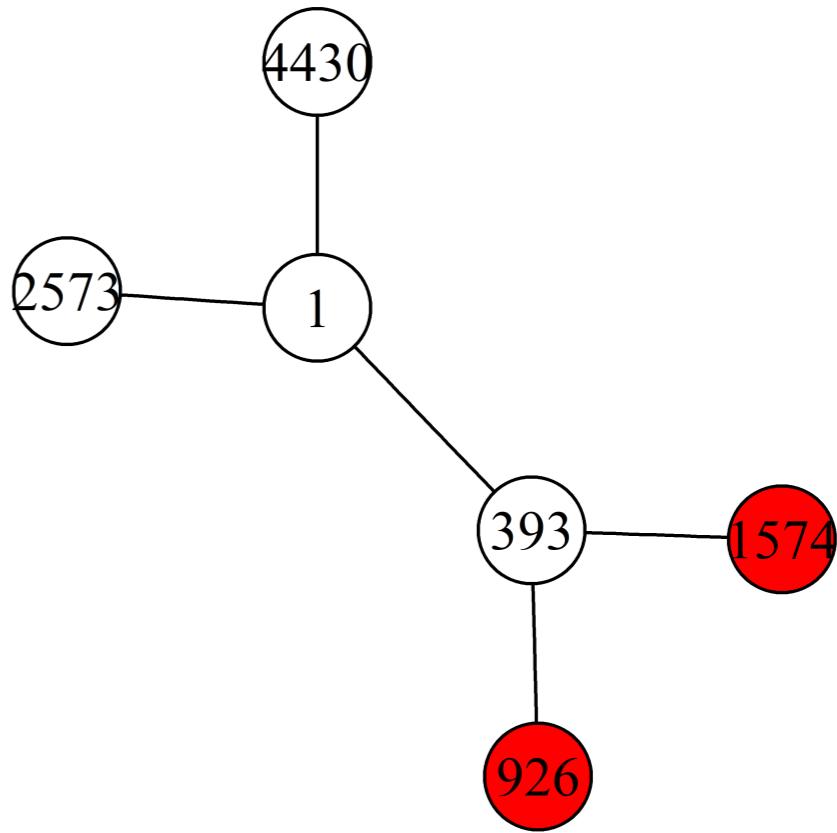
Post-doctoral researcher

customers

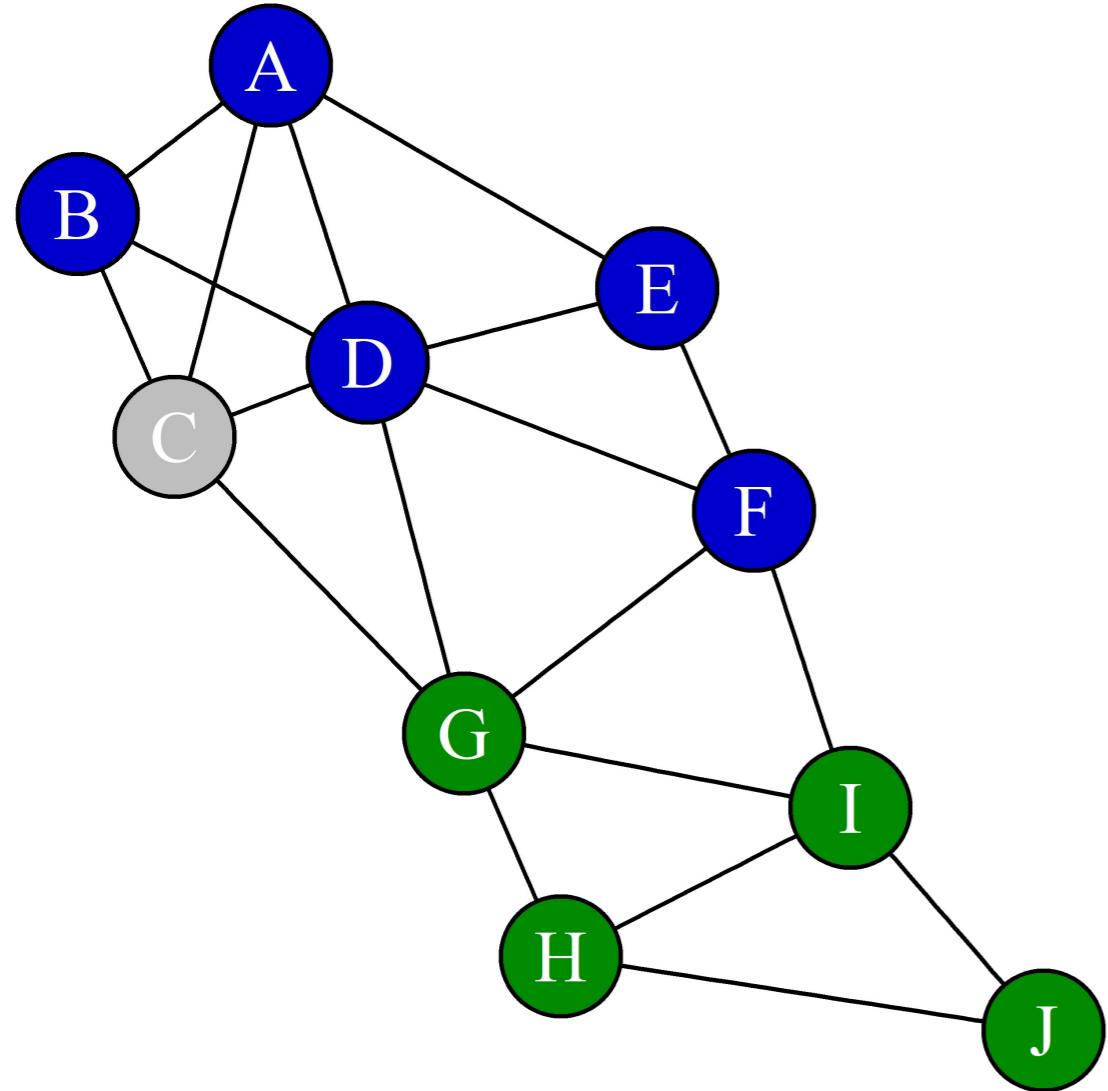
```
  id churn  
1   1    0  
2 393    0  
3 2573   0  
4 4430   0  
5 926    1  
6 1574   1
```

edgeList

```
  from  to  
1   1   393  
2   1   2573  
3   1   4430  
4 393   926  
5 393   1574
```

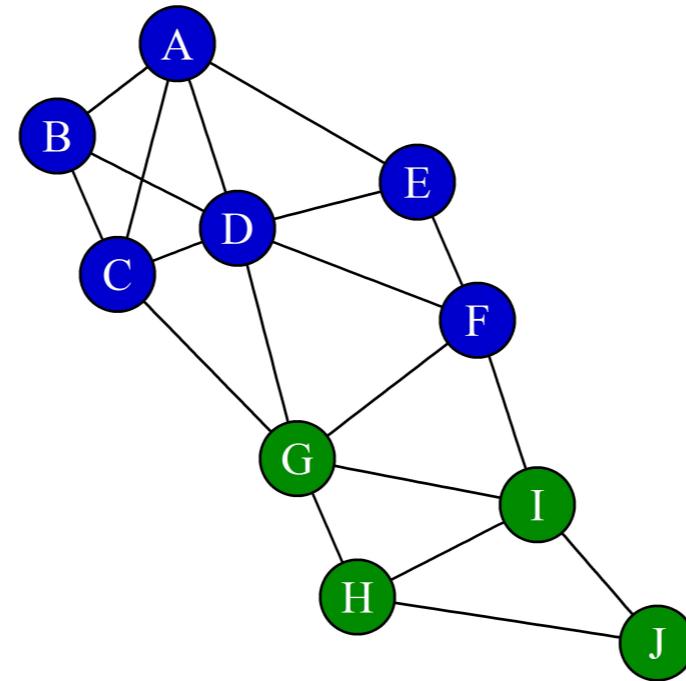


The Relational Neighbor Classifier



- Neighbors of **Cecelia**
 - A,B,D,G
- Neighbors of **Cecelia** that prefer R
 - A, B, D (75%)
- Neighbors of **Cecelia** that prefer Python
 - G (25%)
- **Cecelia** has a higher probability to prefer R

The Relational Neighbor Classifier



```
rNeighbors <- c(4,3,3,5,3,2,3,0,1,0)
pNeighbors <- c(0,0,1,1,0,2,2,3,3,2)
rRelationalNeighbor <- rNeighbors / (rNeighbors + pNeighbors)
rRelationalNeighbor
```

```
1.00 1.00 0.75 0.86 1.00 0.50 0.60 0.00 0.00 0.00
```

Let's practice!

PREDICTIVE ANALYTICS USING NETWORKED DATA IN R

Challenges of network-based inference

PREDICTIVE ANALYTICS USING NETWORKED DATA IN R



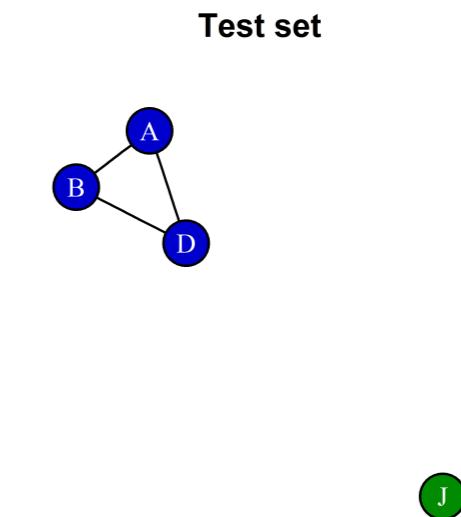
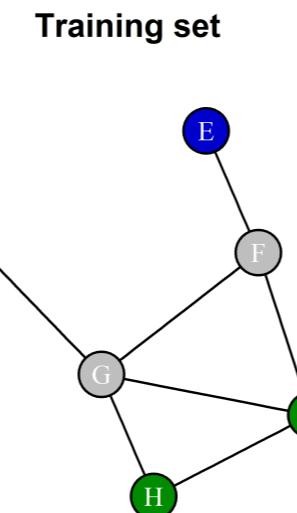
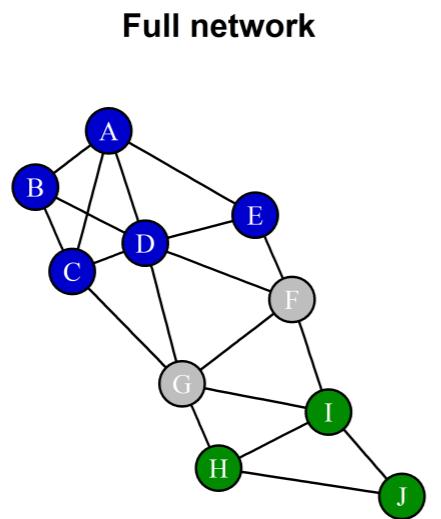
María Óskarsdóttir, Ph.D.

Post-doctoral researcher

First challenge

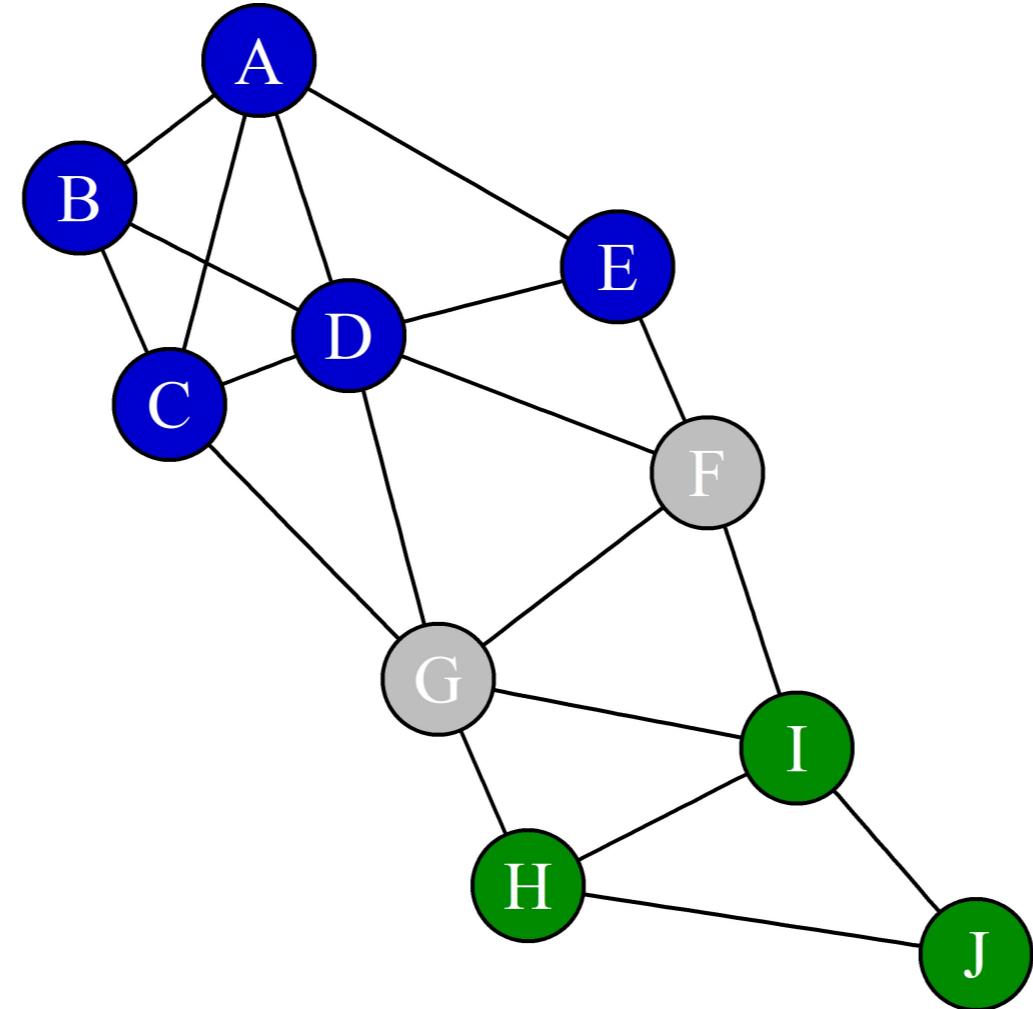
Splitting the data!

```
set.seed(1001)  
sampleVertices <- sample(1:10, 6, replace=FALSE)  
plot(induced_subgraph(g, V(g)[sampleVertices]))  
plot(induced_subgraph(g, V(g)[-sampleVertices]))
```



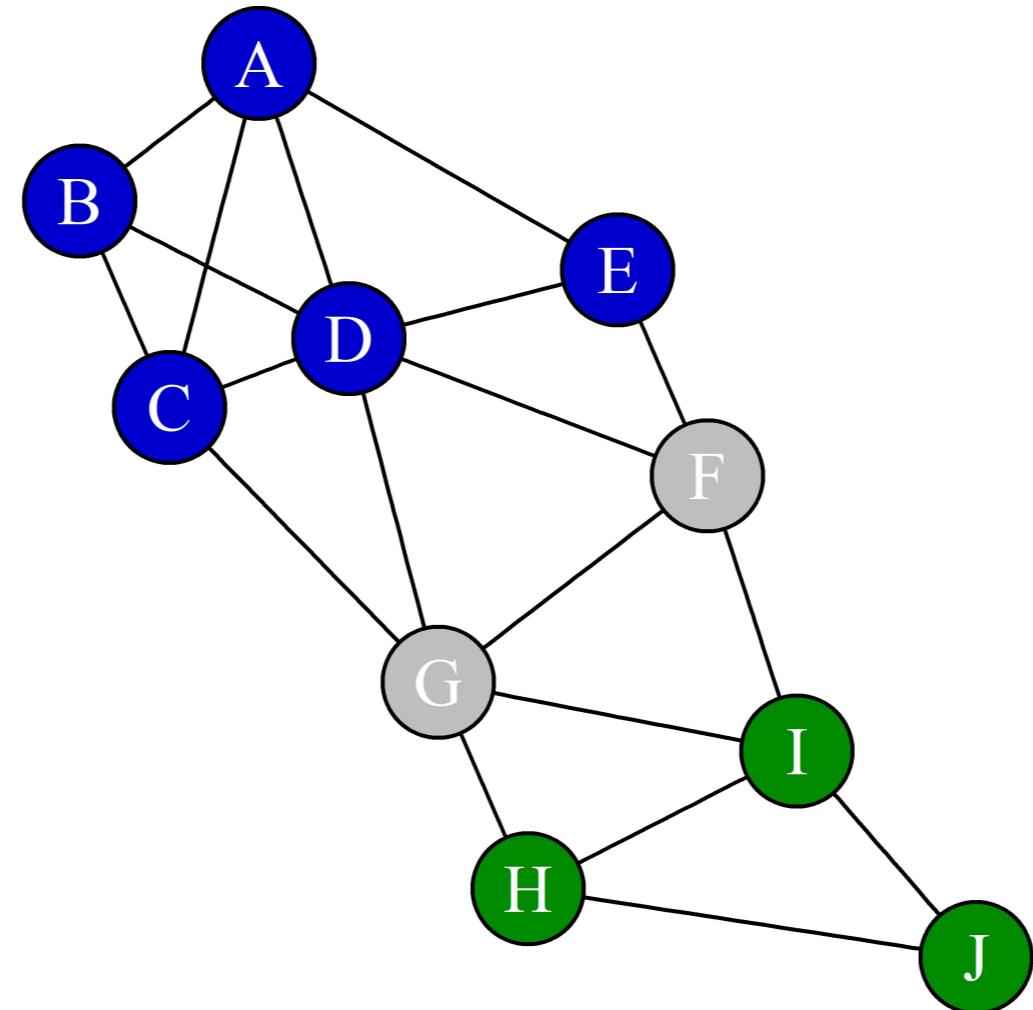
Second challenge

The observations in the dataset are not independent and identically distributed (iid)

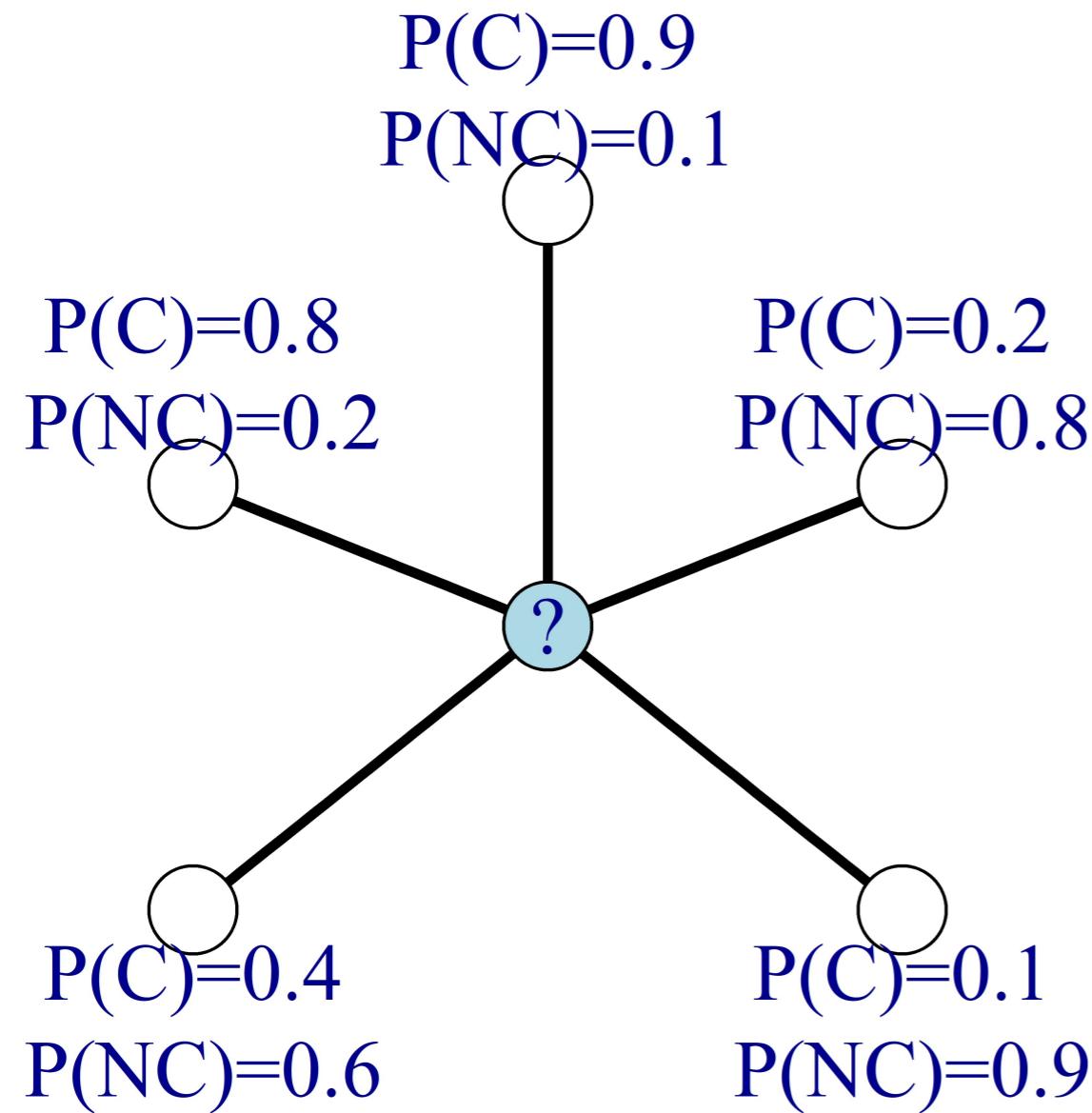


Third challenge

Collective Inference!



Probabilistic relational neighbor classifier



```
# probability churn (C)  
(0.9 + 0.2 + 0.1 + 0.4 + 0.8) / 5
```

0.48

```
# probability non-churn (NC)  
(0.1 + 0.8 + 0.9 + 0.6 + 0.2) / 5
```

0.52

Let's practice!

PREDICTIVE ANALYTICS USING NETWORKED DATA IN R

Homophily

PREDICTIVE ANALYTICS USING NETWORKED DATA IN R



Bart Baesens, Ph.D.

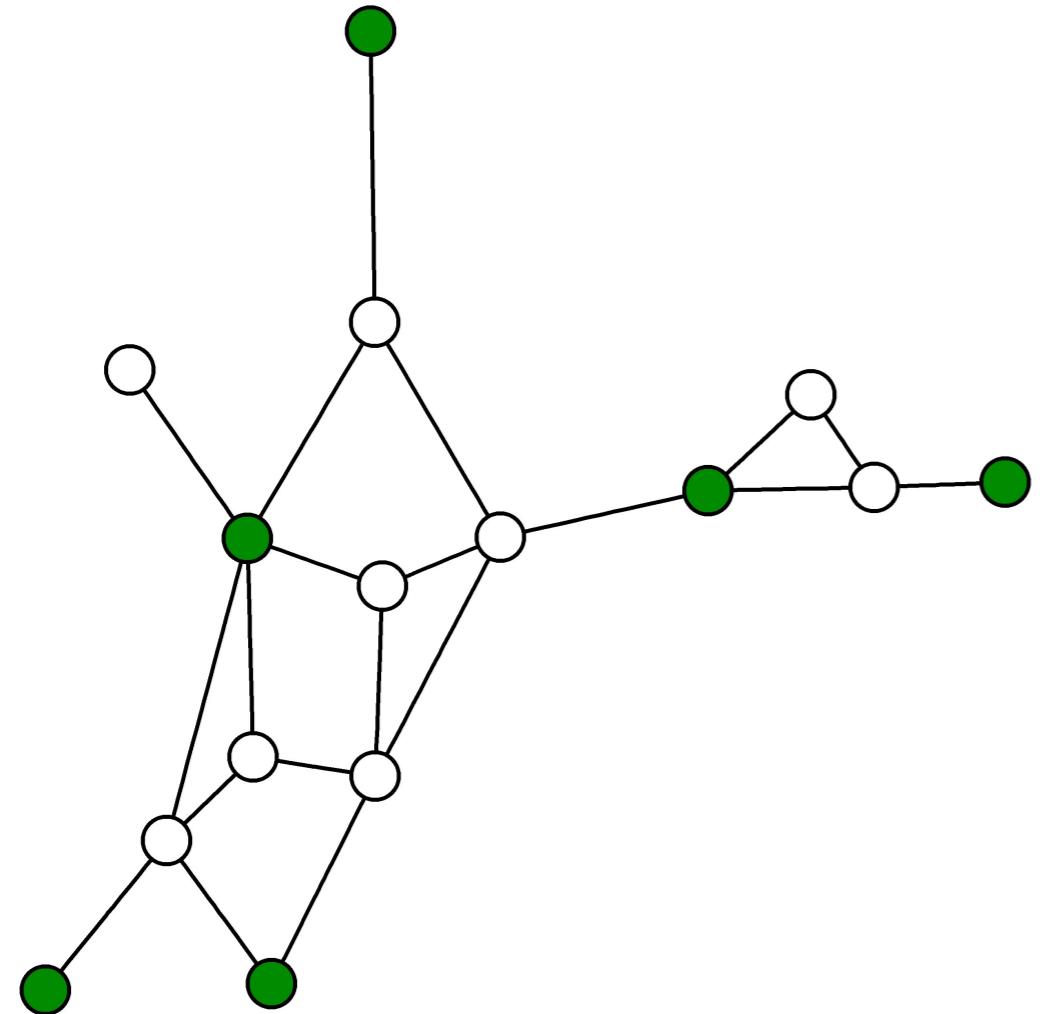
Professor of Data Science, KU Leuven
and University of Southampton

Homophily explained

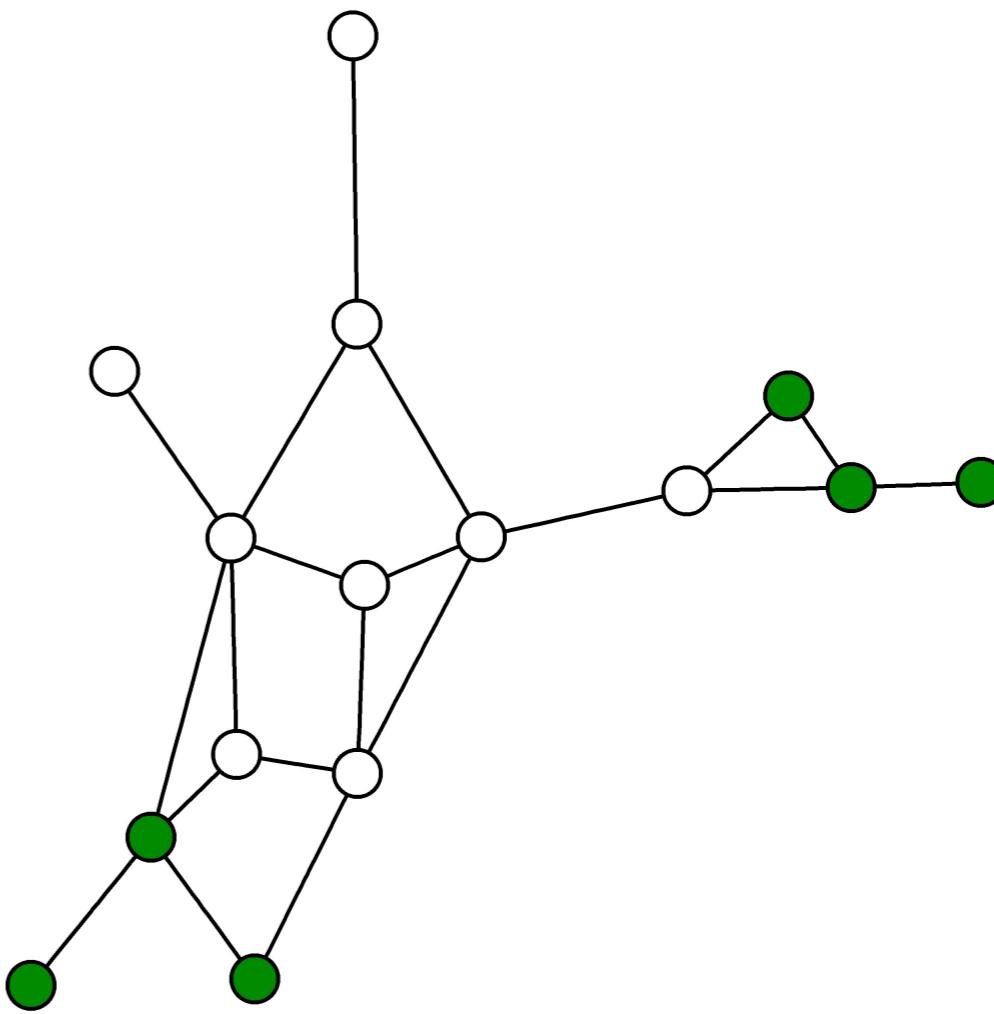
Birds of a feather flock together

- Share common property, hobbies, interest, origin, etc.
- Depends on:
 - Connectedness between nodes with **same** label
 - Connectedness between nodes with **opposite** labels

Homophilic Networks



- Not Homophilic



- Homophilic

```
names <- c('A','B','C','D','E','F','G','H','I','J')
tech <- c(rep('R',6),rep('P',4))
DataScientists <- data.frame(name=names,technology=tech)
DataScienceNetwork <- data.frame(
  from=c('A','A','A','A','B','B','C','C','D','D',
         'D','E','F','F','G','G','H','H','I'),
  to=c('B','C','D','E','C','D','D','G','E','F',
        'G','F','G','I','I','H','I','J','J'),
  label=c(rep('rr',7),'rp','rr','rr','rp','rr','rp',rep('pp',5)))
g <- graph_from_data_frame(DataScienceNetwork,directed = FALSE)
```

Add the technology as a node attribute

```
V(g)$label <- as.character(DataScientists$technology)
V(g)$color <- V(g)$label
V(g)$color <- gsub('R',"blue3",V(g)$color)
V(g)$color <- gsub('P',"green4",V(g)$color)
```

Types of edges

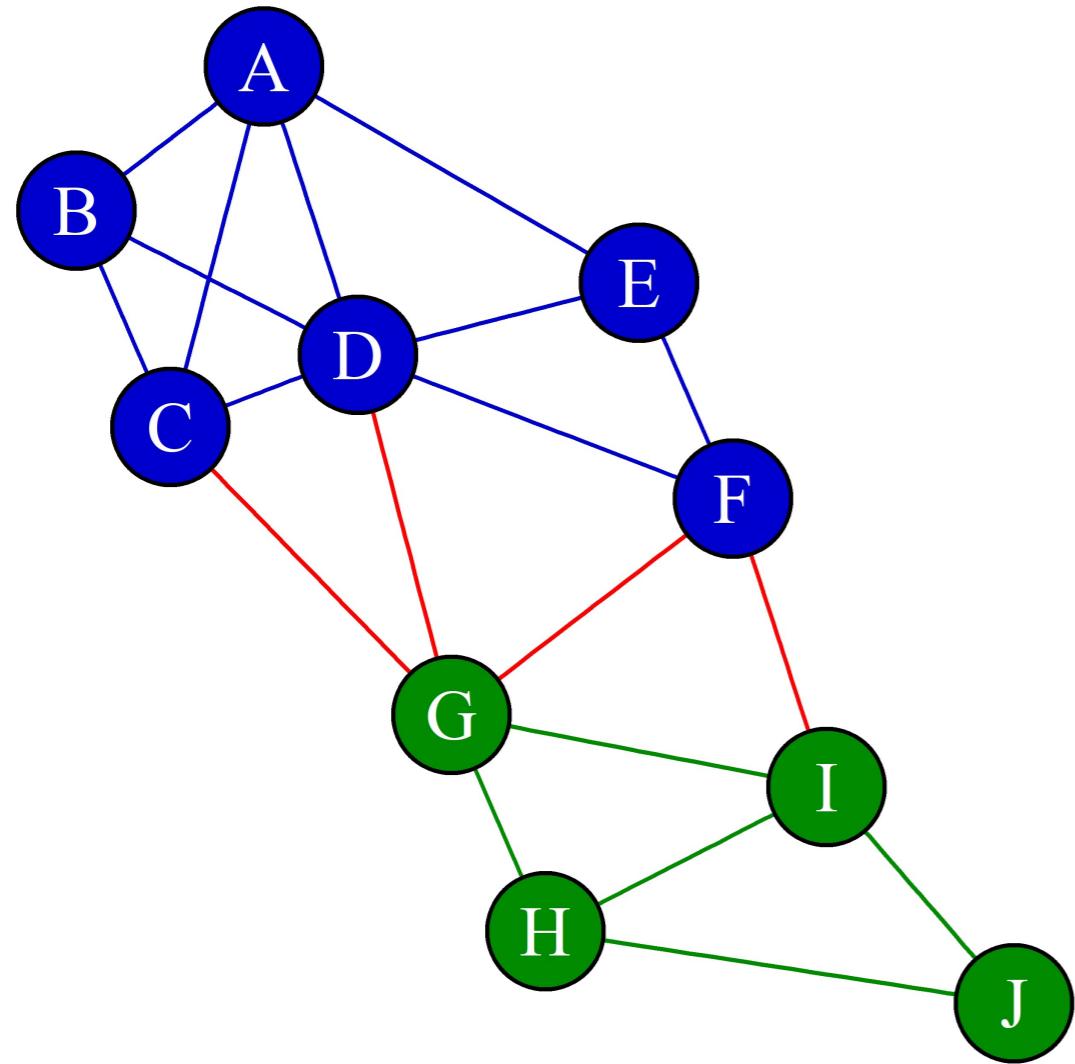
Code to color the edges

```
E(g)$color<-E(g)$label  
E(g)$color=gsub('rp','red',E(g)$color)  
E(g)$color=gsub('rr','blue3',E(g)$color)  
E(g)$color=gsub('pp','green4',E(g)$color)
```

Code to visualize the network

```
pos<-cbind(c(2,1,1.5,2.5,4,4.5,3,3.5,5,6),  
c(10.5,9.5,8,8.5,9,7.5,6,4.5,5.5,4))  
  
plot(g,edge.label=NA,vertex.label.color='white',  
layout=pos, vertex.size = 25)
```

Counting edge types



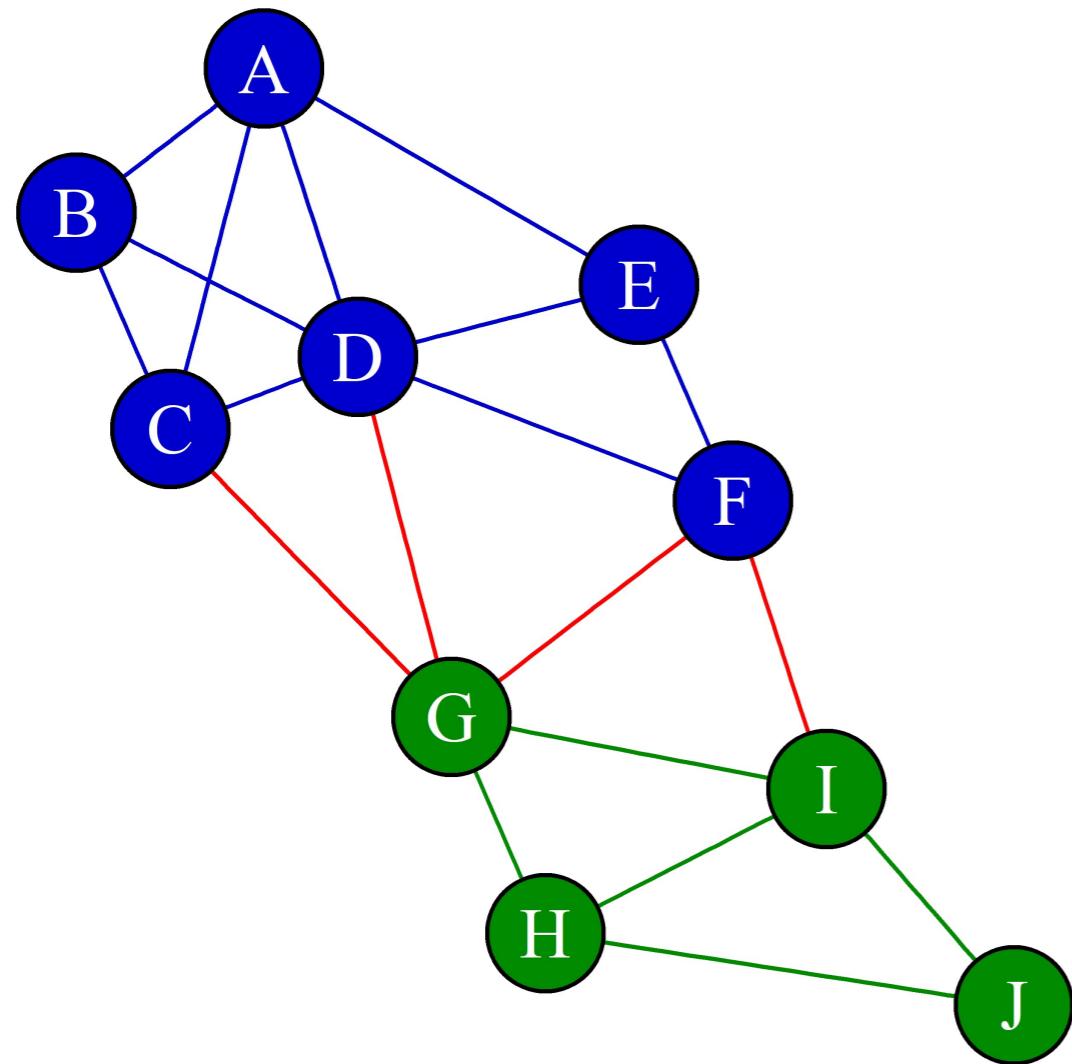
```
# R edges  
edge_rr<-sum(E(g)$label=='rr')
```

```
# Python edges  
edge_pp<-sum(E(g)$label=='pp')
```

```
# cross label edges  
edge_rp<-sum(E(g)$label=='rp')
```

- `edge_rr= 10`
- `edge_pp= 5`
- `edge_rp= 4`

Network connectance



$$p = \frac{2 \cdot \text{edges}}{\text{nodes}(\text{nodes}-1)}$$

```
p <- 2*edges/nodes*(nodes-1)
```

- $p = 0.42$
- Number of edges in a fully connected network: $\binom{\text{nodes}}{2} = \frac{\text{nodes}(\text{nodes}-1)}{2}$

Let's practice!

PREDICTIVE ANALYTICS USING NETWORKED DATA IN R

Dyadicity

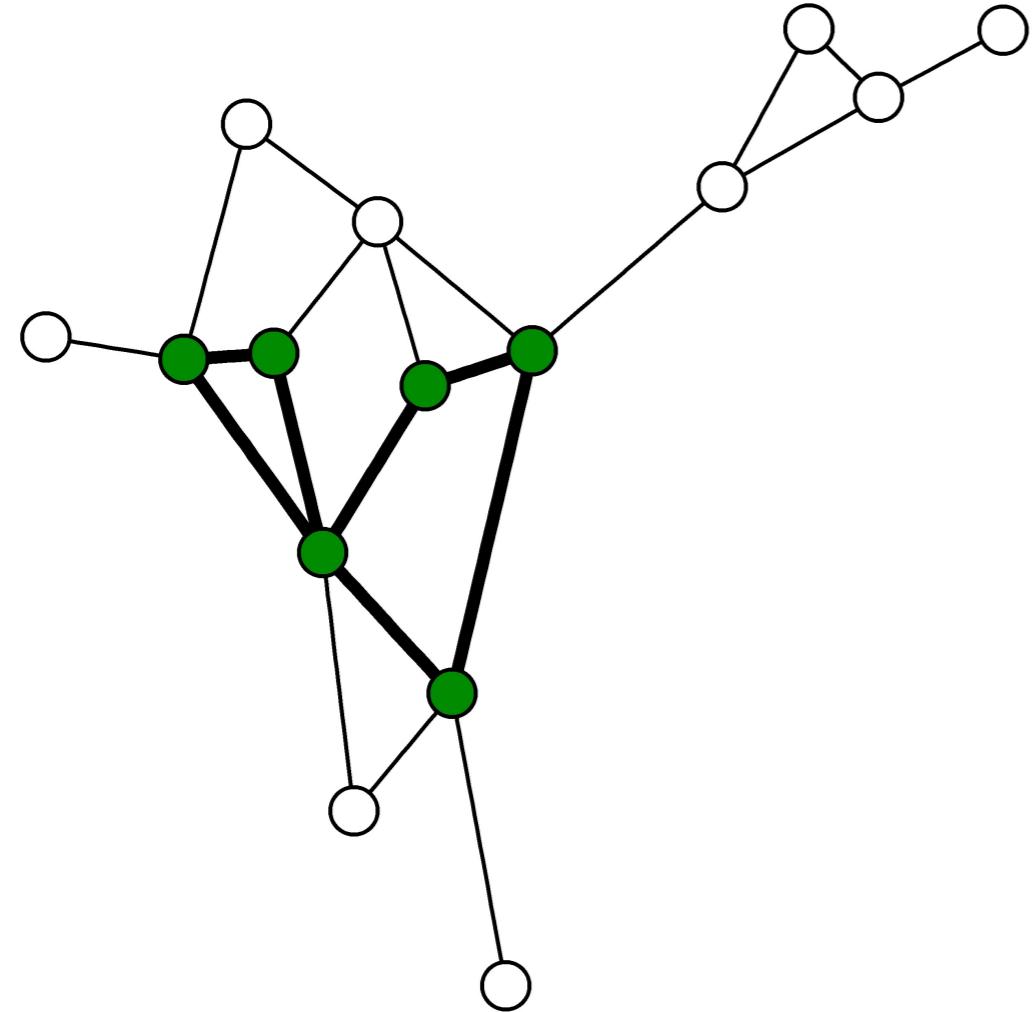
PREDICTIVE ANALYTICS USING NETWORKED DATA IN R



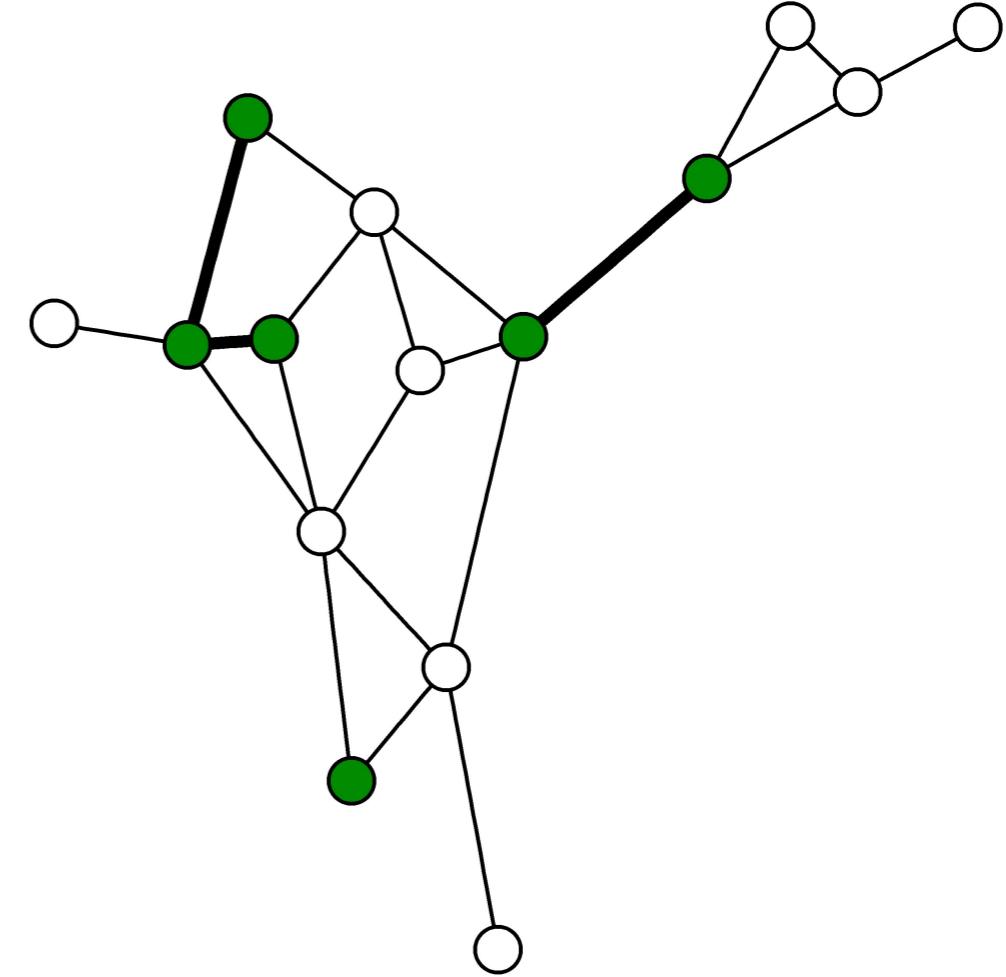
María Óskarsdóttir, Ph.D.

Post-doctoral researcher

Dyadicity



7 edges between green nodes



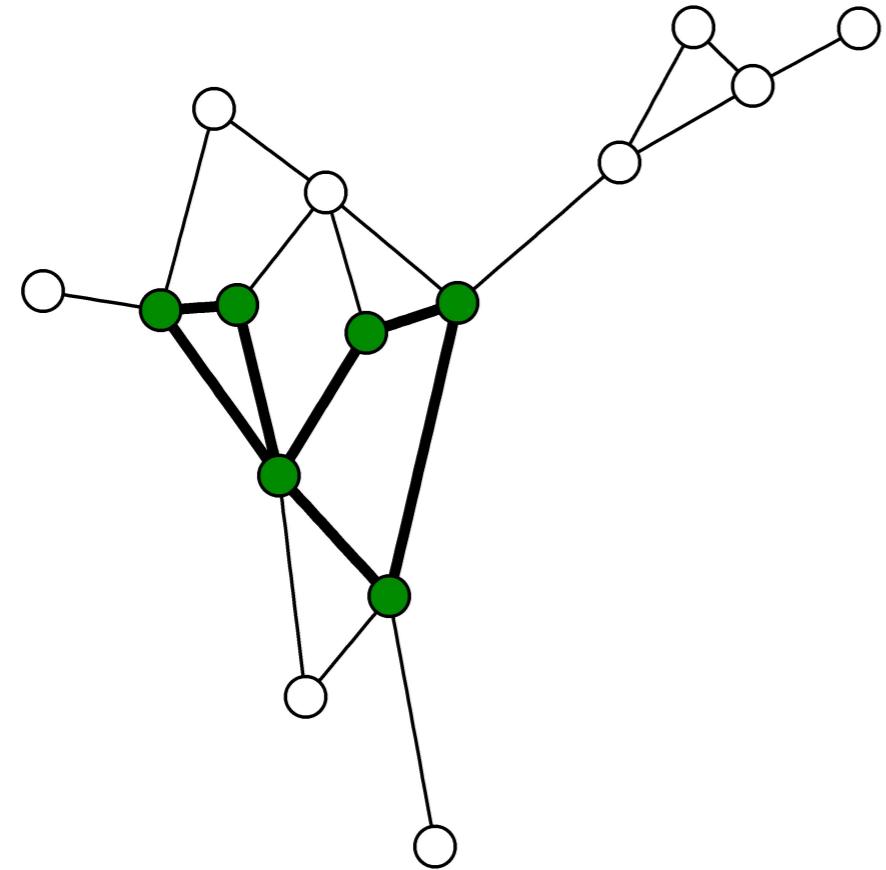
3 edges between green nodes

Dyadicity

Connectedness between nodes with the **same** label compared to what is expected in a random configuration of the network

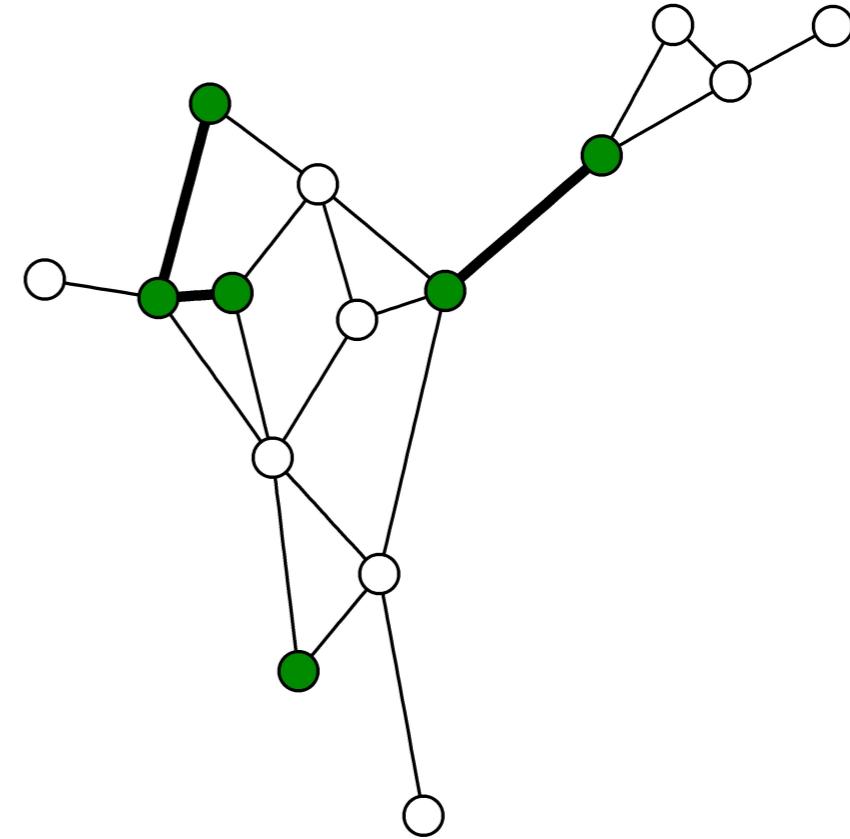
- Expected number of same label edges: $\binom{n_g}{2} \cdot p = \frac{n_g(n_g-1)}{2} \cdot p$
- Example:
 - Network with 9 white nodes, 6 green nodes, 21 edges, and connectance $p = 0.2$
 - Expected number of edges connecting two green nodes is 3 ($= \frac{6 \cdot 5 \cdot p}{2}$)
- Dyadicity equals the actual number of same label edges divided by the expected number of same label edge
 - $D = \frac{\text{number of same label edges}}{\text{expected number of same label edges}}$

Dyadicity



7 edges between green nodes

- $D = 7/3 = 2.33$



3 edges between green nodes

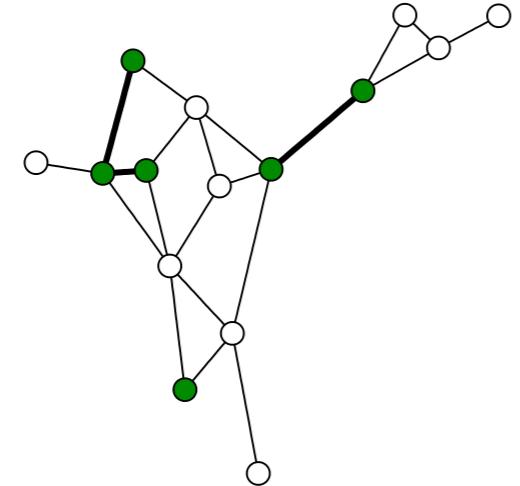
- $D = 3/3 = 1$

Types of Dyadicity

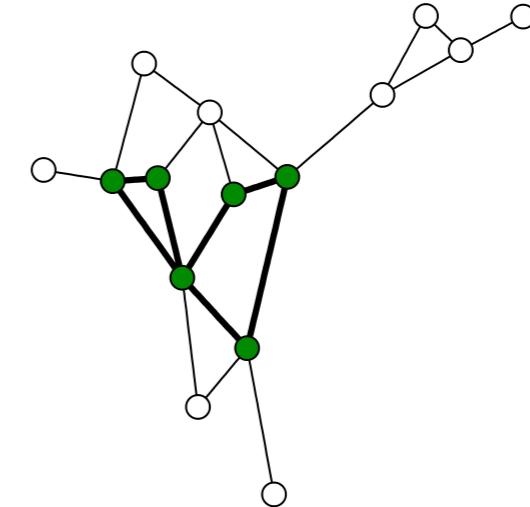
Three scenarios

1. $D > 1 \Rightarrow$ Dyadic
2. $D \simeq 1 \Rightarrow$ Random
3. $D < 1 \Rightarrow$ Anti-Dyadic

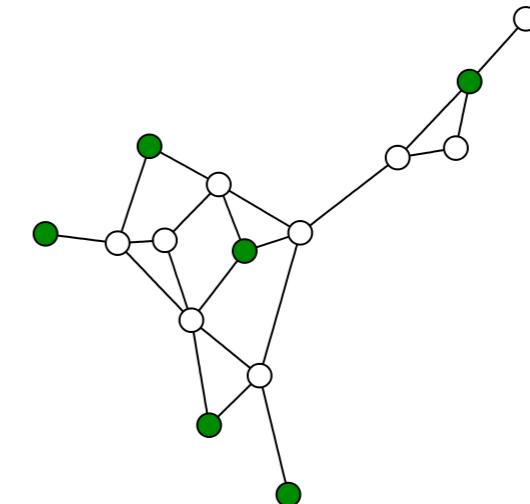
$$D = 1$$



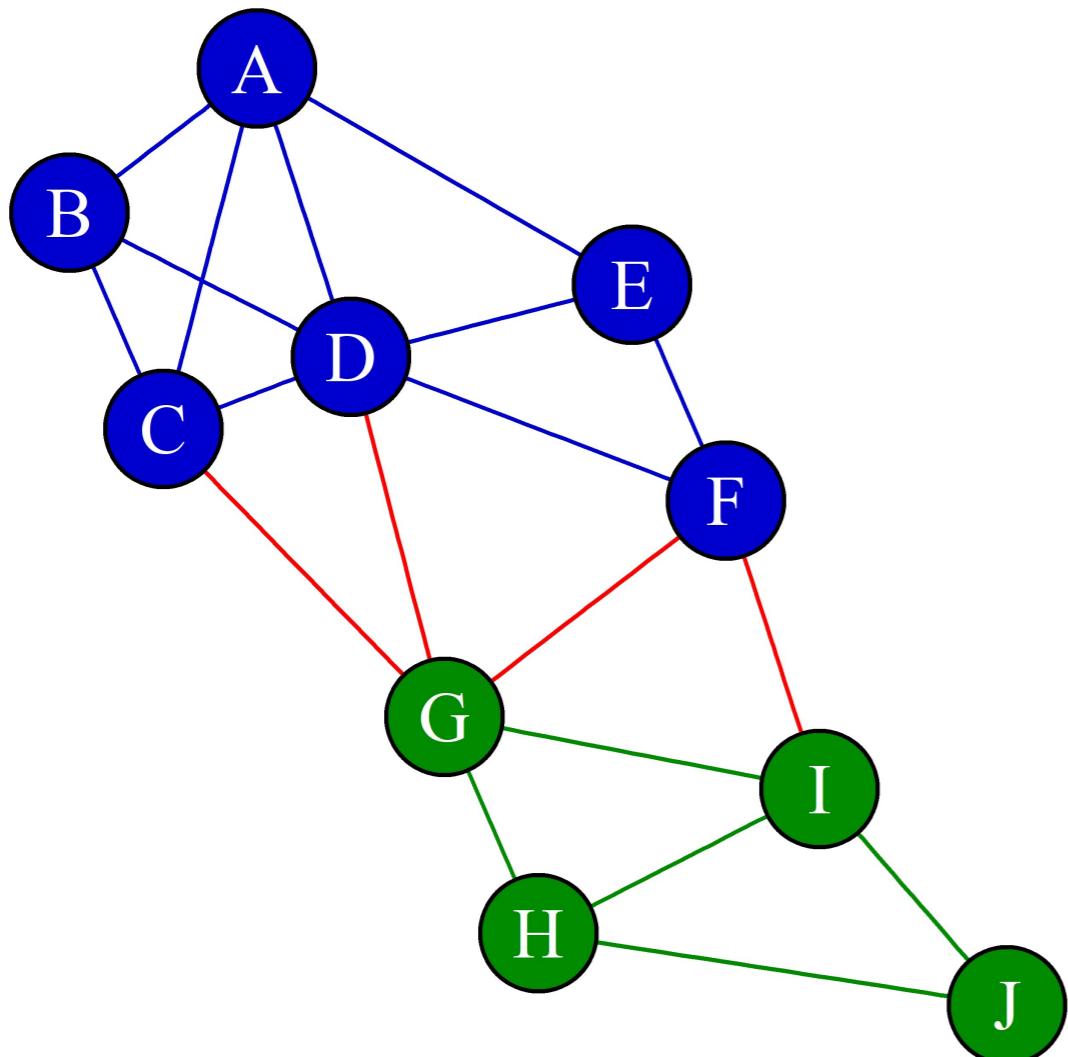
$$D = 2.33$$



$$D = 0$$



Dyadicity in the Network of Data Scientists



```
p <- 2 * 19 / (10 * 9)
expectedREdges <- 6 * 5 / 2 * p
expectedPEdges <- 4 * 3 / 2 * p
dyadicityR <- rEdges / expectedREdges
dyadicityP <- pEdges / expectedPEdges
dyadicityR
```

1.578947

dyadicityP

1.973684

Let's practice!

PREDICTIVE ANALYTICS USING NETWORKED DATA IN R

Heterophilicity

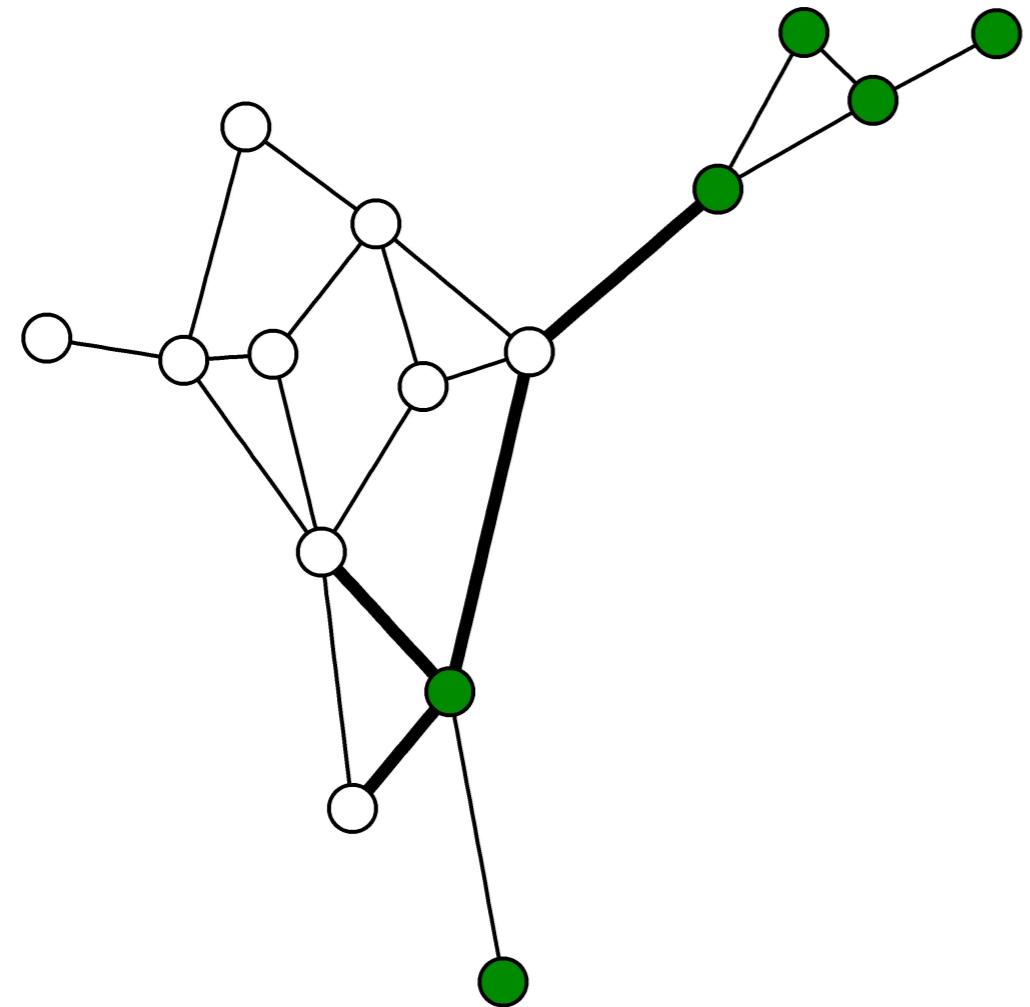
PREDICTIVE ANALYTICS USING NETWORKED DATA IN R



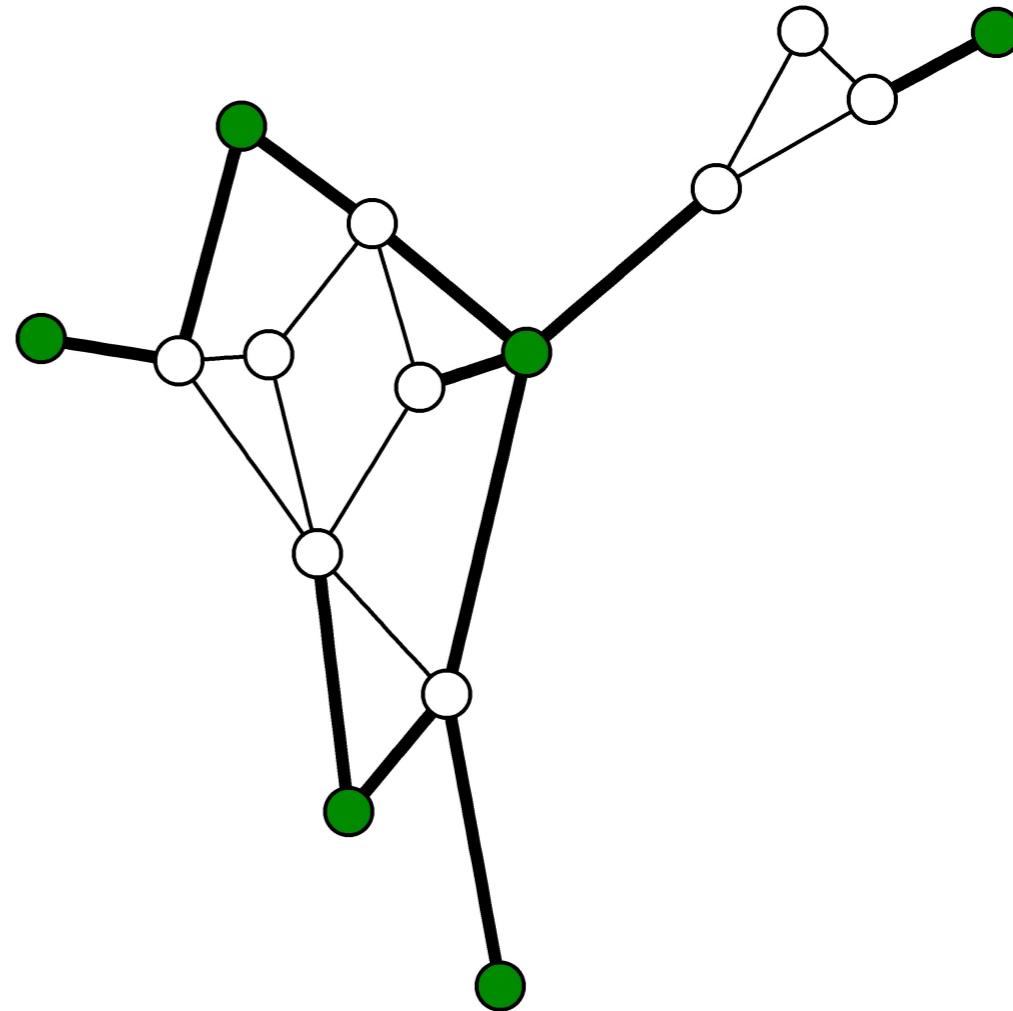
María Óskarsdóttir, Ph.D.

Post-doctoral researcher

Heterophilicity



4 cross label edges



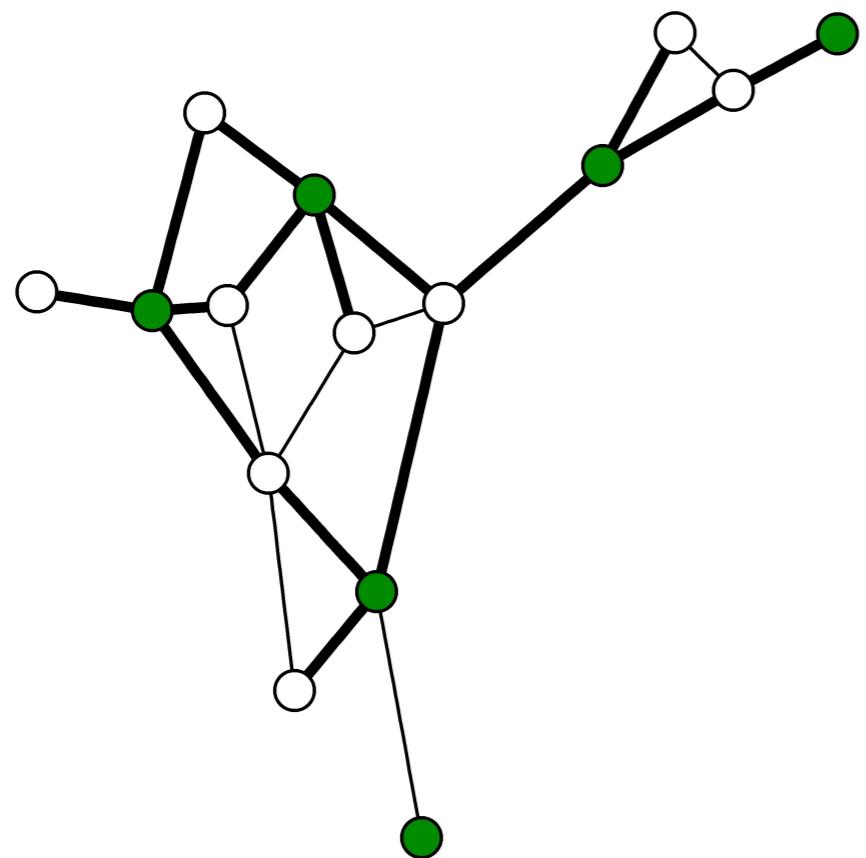
11 cross label edges

Heterophilicity

Connectedness between nodes with **different** labels compared to what is expected for a random configuration of the network

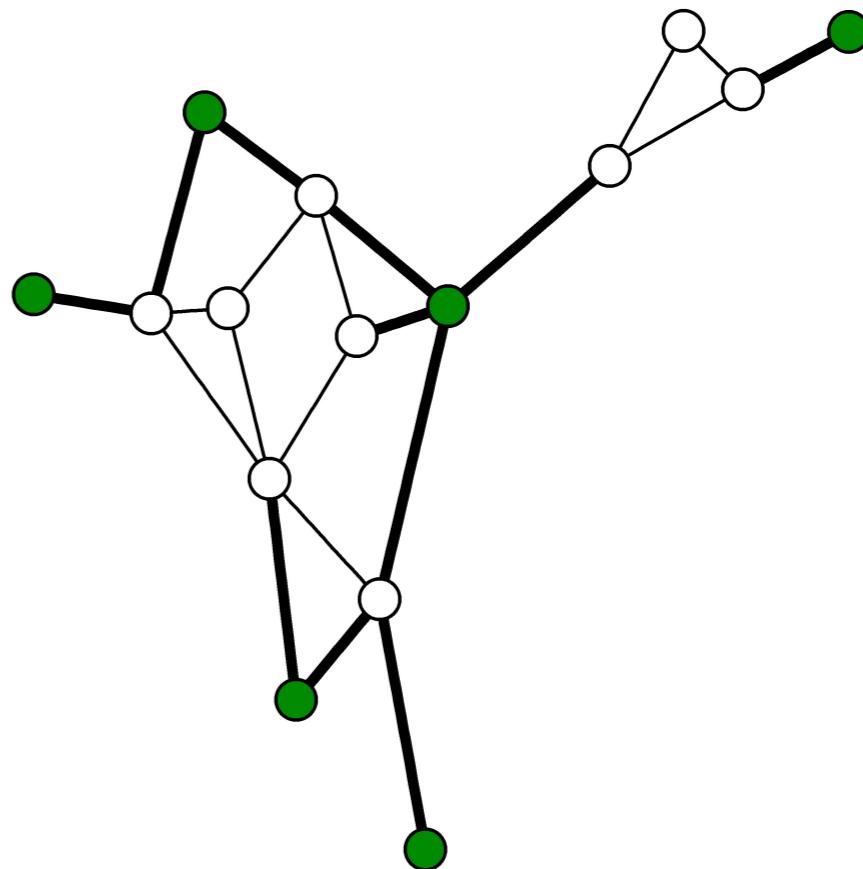
- Expected number of cross label edges = $n_w n_g p$
- Example:
 - Network with 9 white nodes, 6 green nodes, 21 edges, and connectance $p = 0.2$
 - Expected number of cross label edges is 11 ($= 9 \cdot 6 \cdot p$)
- Heterophilicity equals the actual number of cross label edges divided by the expected number of cross label edges
 - $$H = \frac{\text{number of cross label edges}}{\text{expected number of cross label edges}}$$

Heterophilicity



15 cross label edges

- $H = 15/11 = 1.39$



11 cross label edges

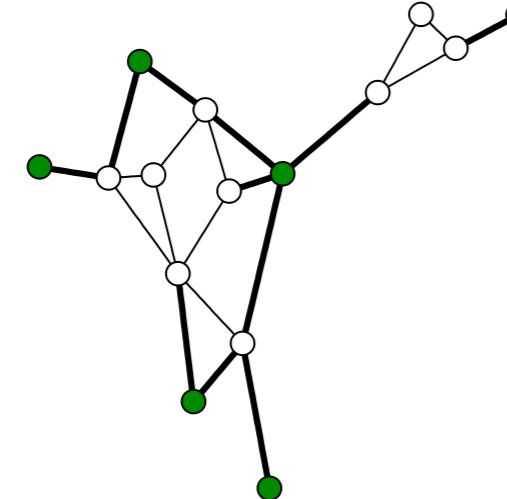
- $H = 11/11 = 1.02$

Types of Heterophilicity

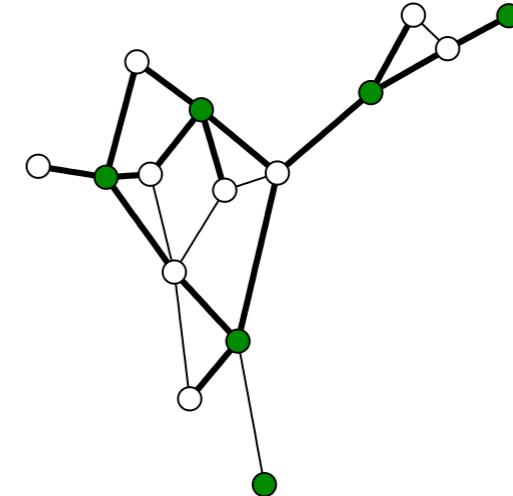
Three scenarios

1. $H > 1 \Rightarrow$ Heterophilic
 2. $H \simeq 1 \Rightarrow$ Random
 3. $H < 1 \Rightarrow$ Heterophobic

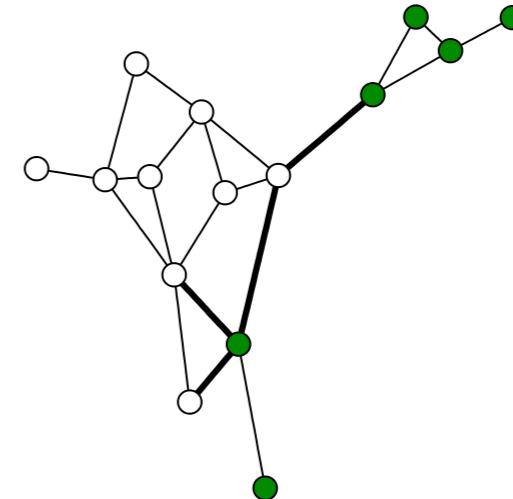
$$H = 1.02$$



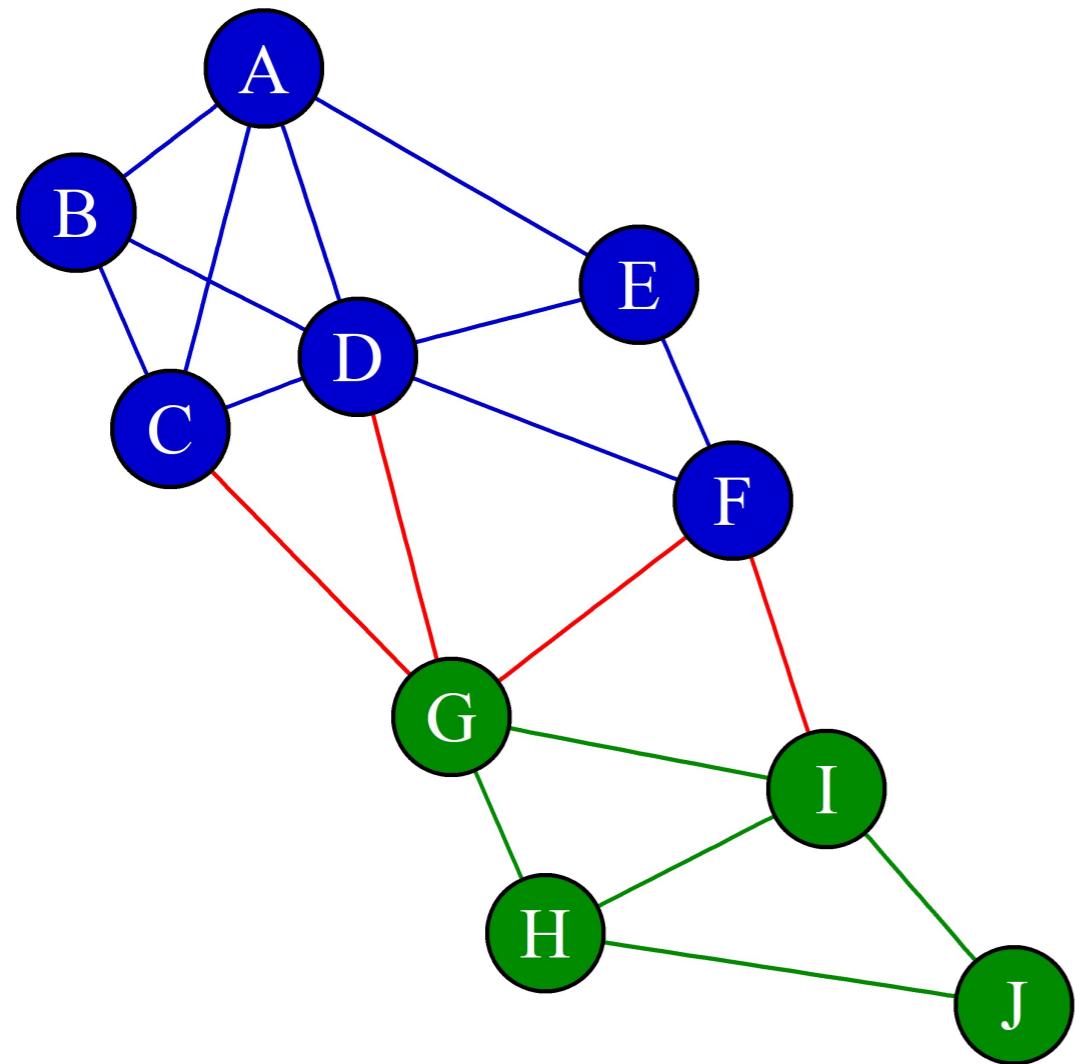
$$H = 1.39$$



$$H = 0.37$$



Heterophilicity in the network of data scientists



$p < -2 * 19 / (10 * 9)$

$m_rp < -6 * 4 * p$

$H_rp < -edge_rp / m_rp$

H_rp

0.3947368

Let's practice!

PREDICTIVE ANALYTICS USING NETWORKED DATA IN R

Summary of homophily

PREDICTIVE ANALYTICS USING NETWORKED DATA IN R

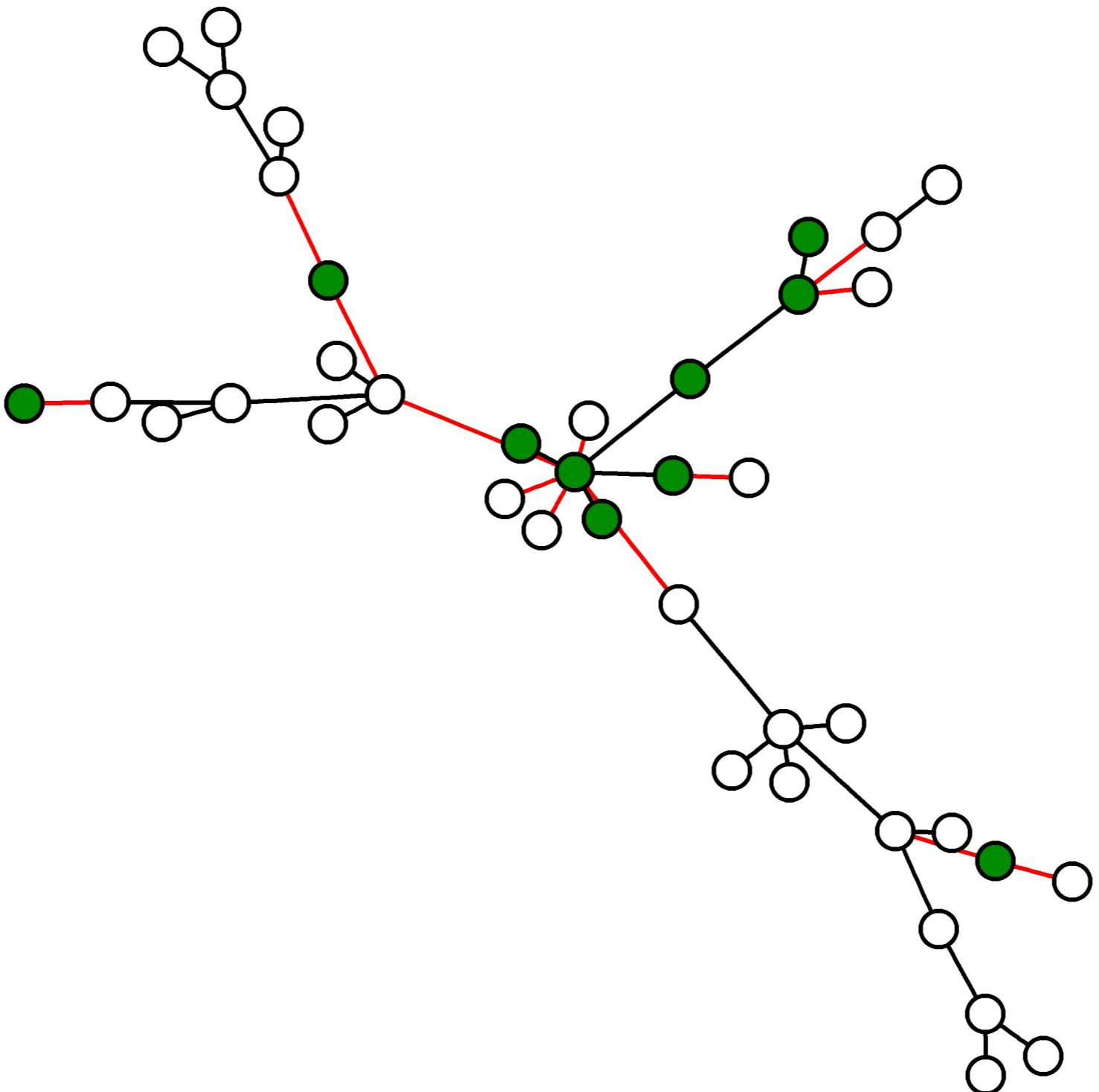


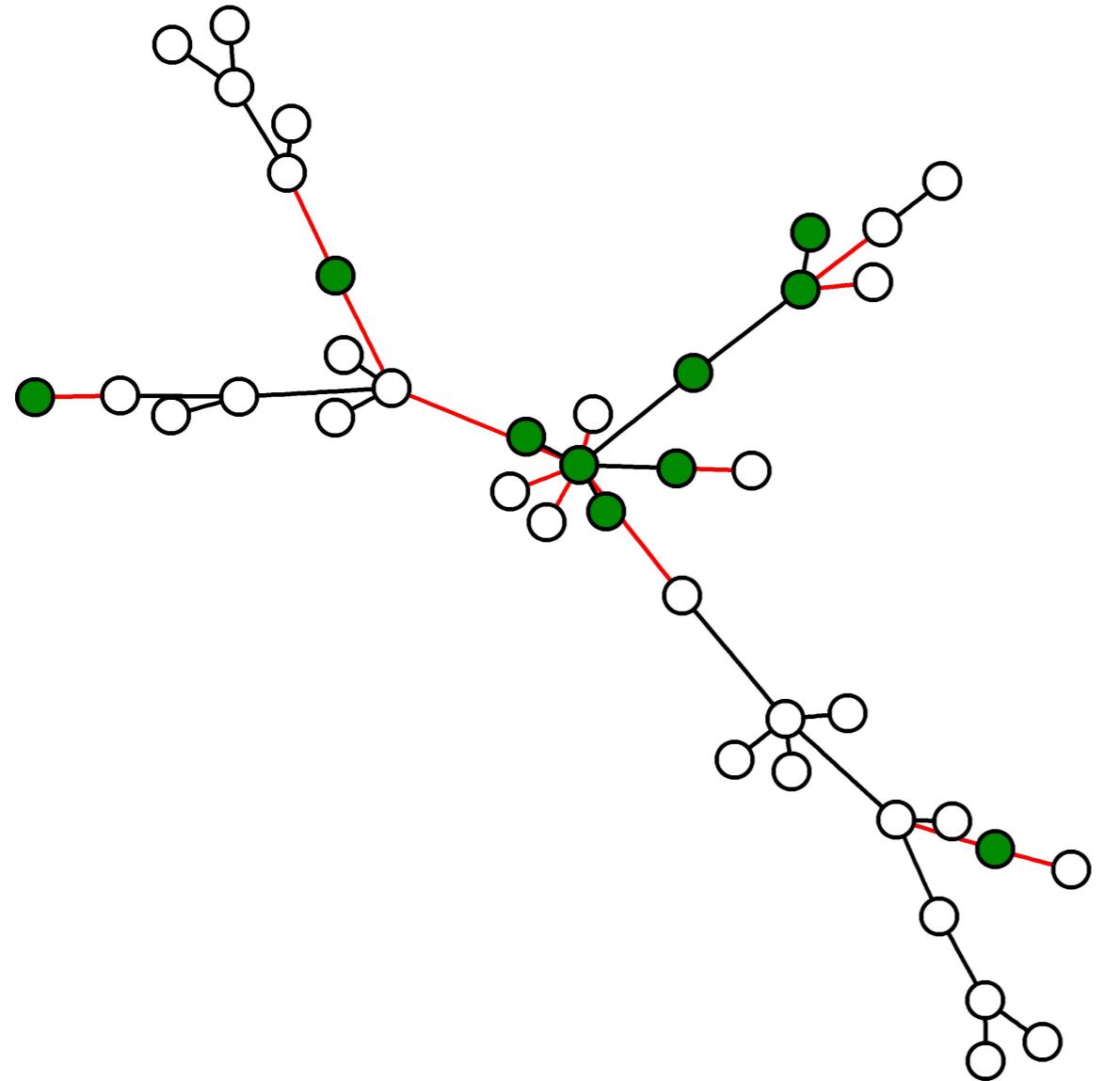
María Óskarsdóttir, Ph.D.

Postdoctoral researcher

Can I do predictive analytics with my network?

- Are the relationships between nodes important?
- Are the labels randomly spread through the network or is there some structure?
- Is the network homophilic?**





```
# Heterophilicity
e_mixed / m_mixed
```

```
N <- 40
E <- 39
n_green <- 10
n_white <- 30
e_green <- 6
e_mixed <- 13
p <- 2 * E / N / (N-1)
m_green <- n_green * (n_green-1)/2 * p
m_mixed <- n_green * n_white * p
# Dyadicity
e_green / m_green
```

2.666667

0.866667

⇒ Homophilic

Let's practice!

PREDICTIVE ANALYTICS USING NETWORKED DATA IN R

Basic Network features

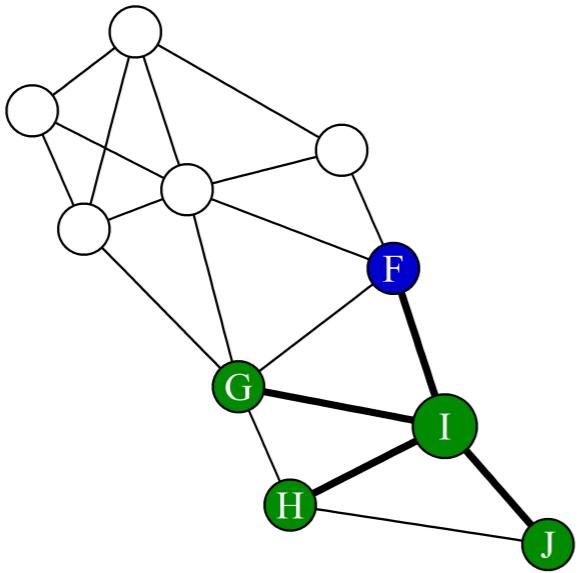
PREDICTIVE ANALYTICS USING NETWORKED DATA IN R



Bart Baesens, Ph.D.

Professor of Data Science, KU Leuven
and University of Southampton

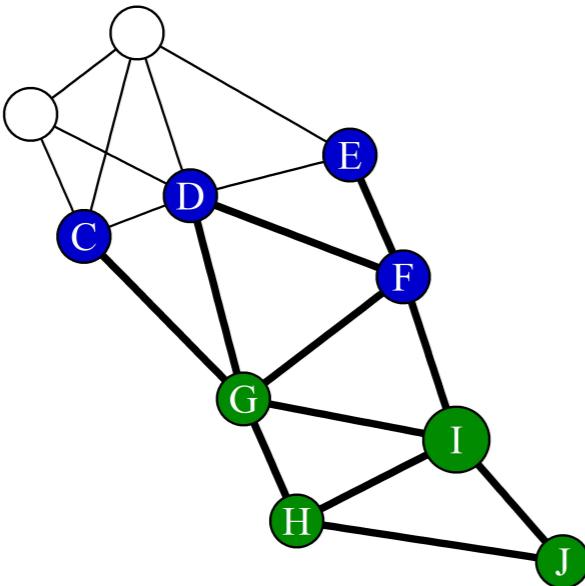
Neighborhood features



- First order degree
 - Number of connected nodes

```
degree(g)
```

A	B	C	D	E	F	G	H	I	J
4	3	4	6	3	4	5	3	4	2

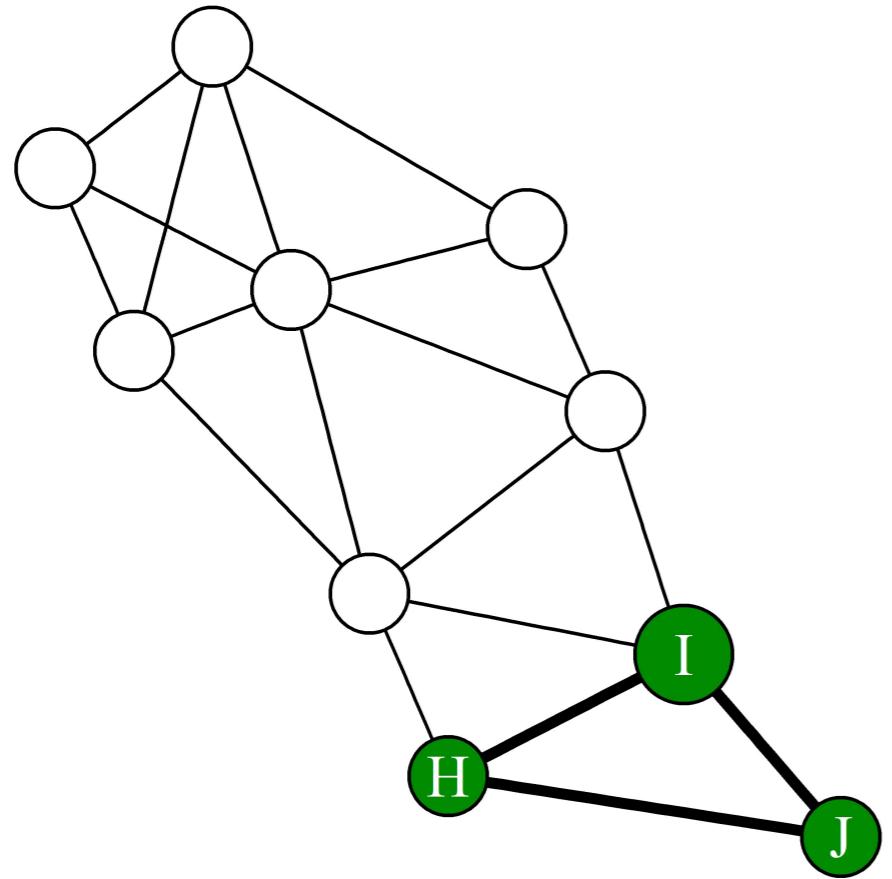


- Second order degree
 - Number of connected nodes that are two or less edges away

```
neighborhood.size(g, order = 2)
```

7	7	9	9	8	10	10	7	8	5
---	---	---	---	---	----	----	---	---	---

Neighborhood features - triangles

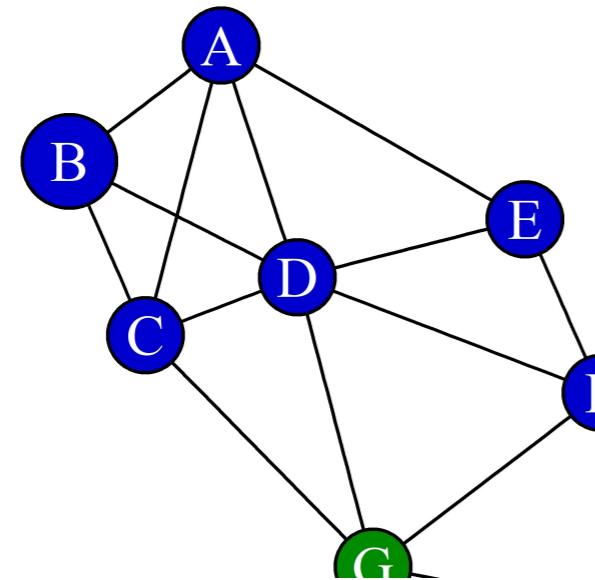


```
count_triangles(g)
```

```
4 3 4 7 2 3 4 2 3 1
```

Centrality features

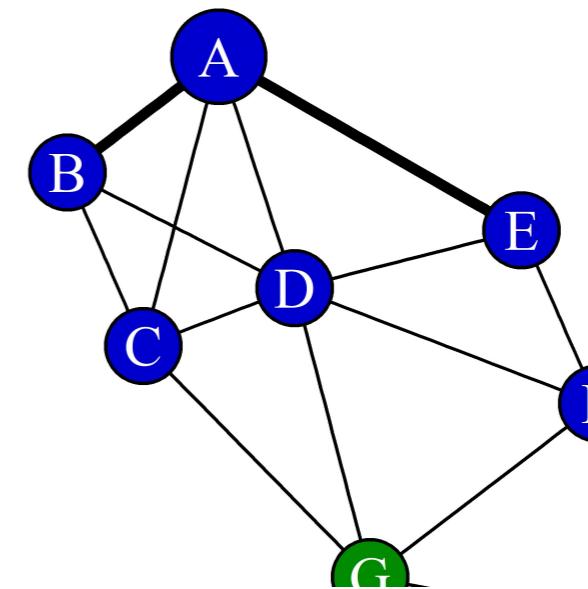
- Betweenness



`betweenness(g)`

A	B	C	D	E	F	G	H	I	J
1.00	0.00	3.32	8.10	0.92	5.37	11.47	2.07	5.77	0.00

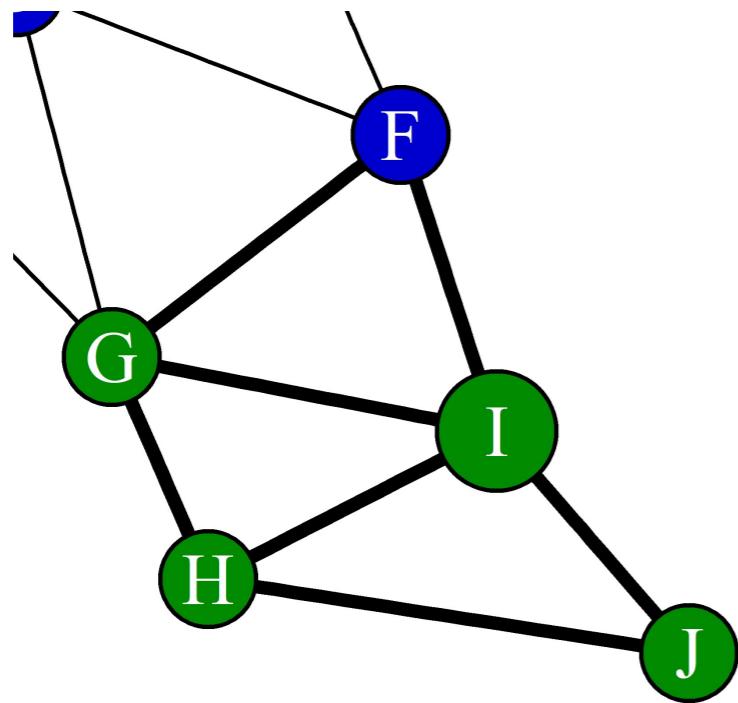
- Closeness



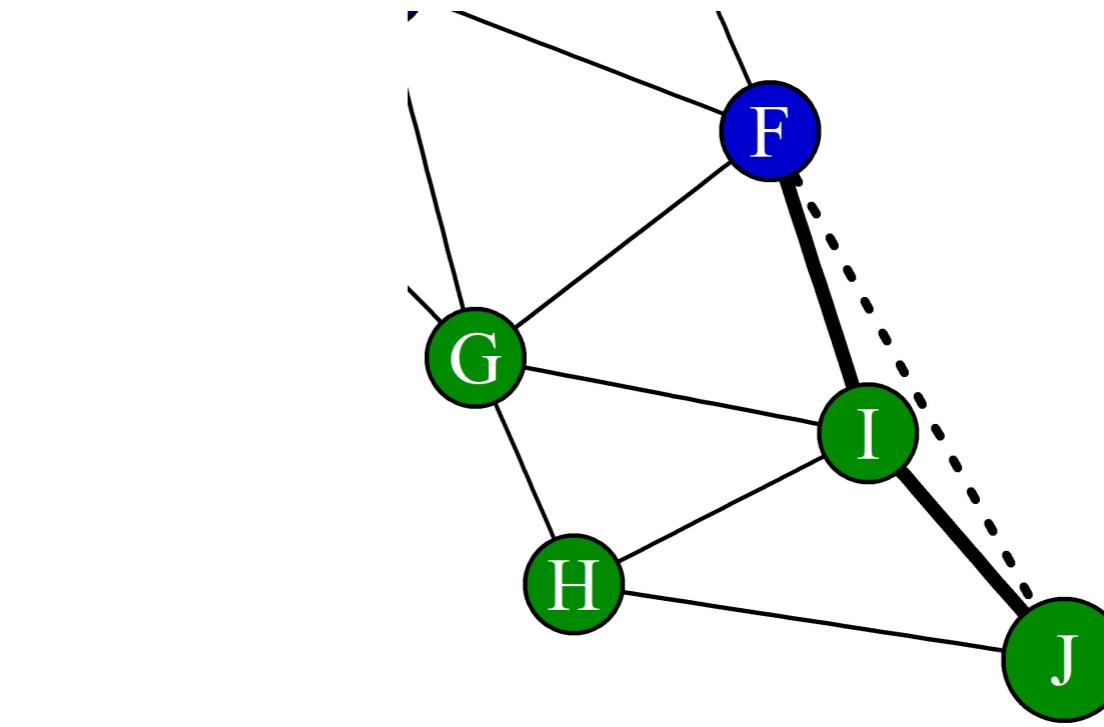
`closeness(g)`

A	B	C	D	E	F	G	H	I	J
0.06	0.05	0.07	0.08	0.06	0.07	0.08	0.06	0.06	0.04

Transitivity



```
transitivity(g,type = 'local')
```



```
0.67 1.00 0.67 0.47 0.67 0.50 0.40 0.67 0.50 1.00
```

Let's practice!

PREDICTIVE ANALYTICS USING NETWORKED DATA IN R

Link Based Features

PREDICTIVE ANALYTICS USING NETWORKED DATA IN R

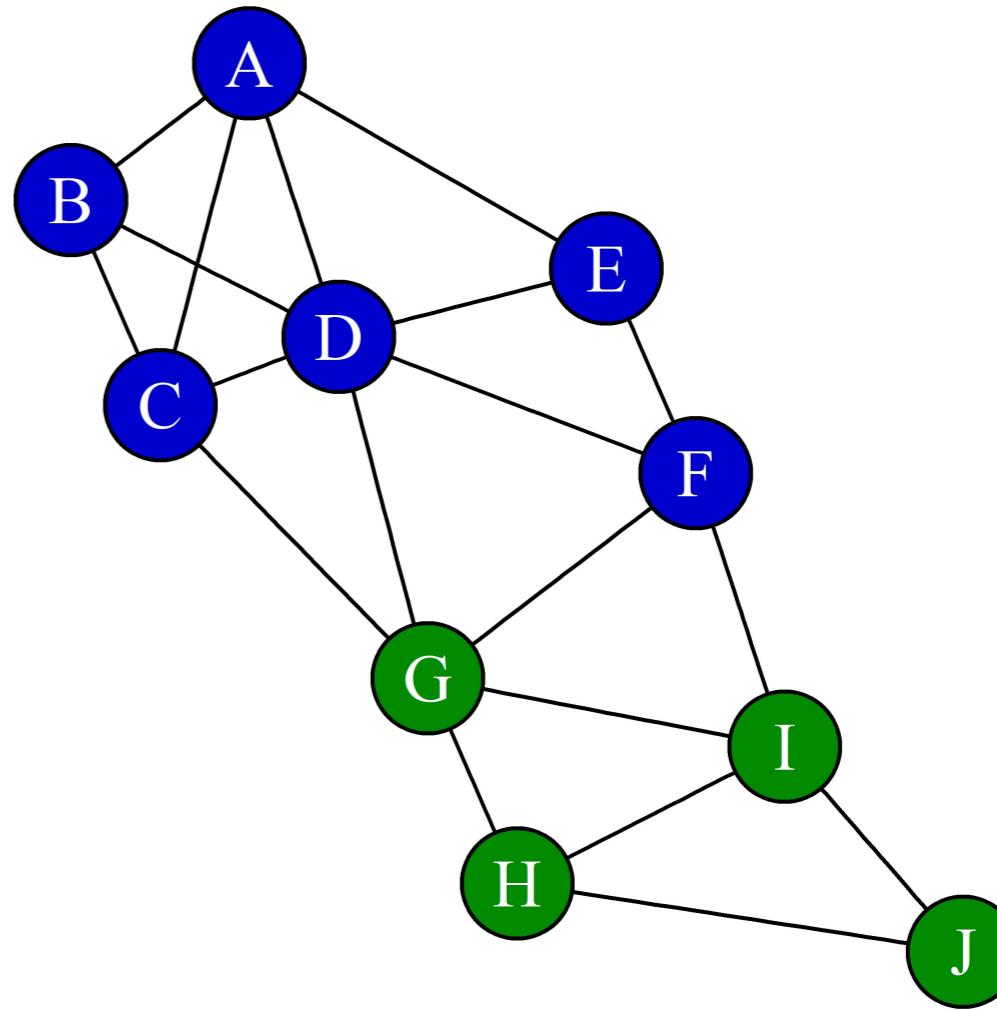


María Óskarsdóttir, Ph.D.

Post-doctoral researcher

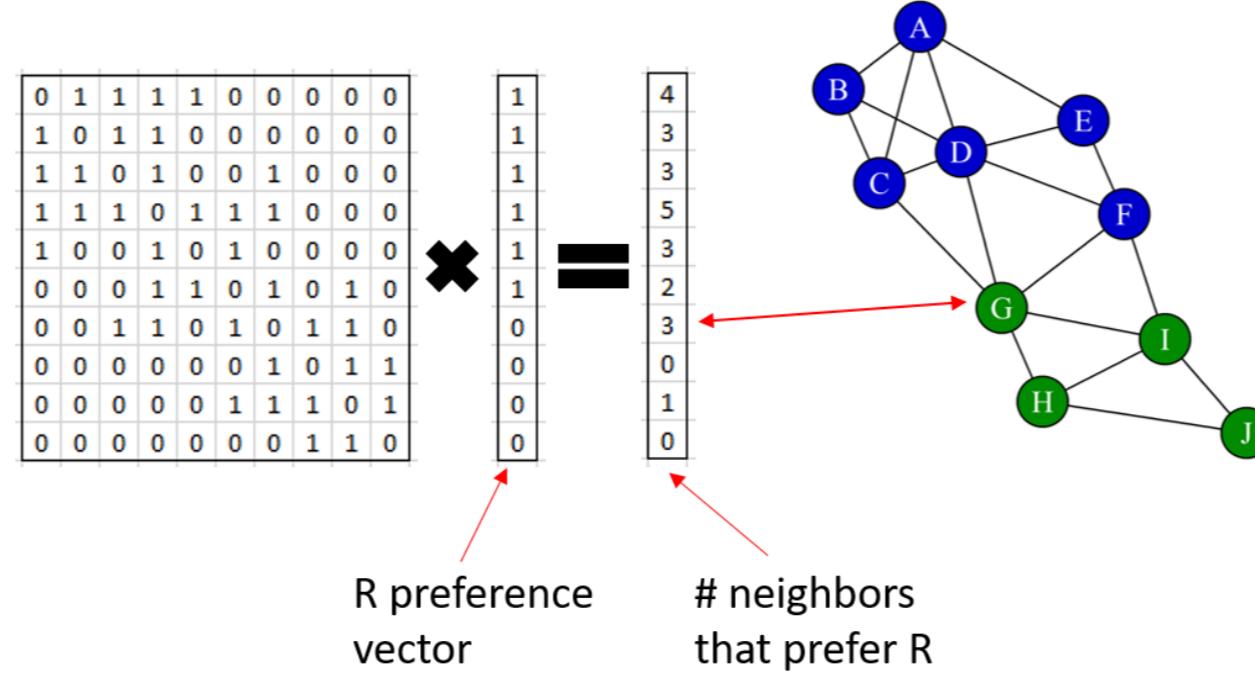
Adjacency matrices

	A	B	C	D	E	F	G	H	I	J
A	0	1	1	1	1	0	0	0	0	0
B	1	0	1	1	0	0	0	0	0	0
C	1	1	0	1	0	0	1	0	0	0
D	1	1	1	0	1	1	1	0	0	0
E	1	0	0	1	0	1	0	0	0	0
F	0	0	0	1	1	0	1	0	1	0
G	0	0	1	1	0	1	0	1	1	0
H	0	0	0	0	0	0	1	0	1	1
I	0	0	0	0	1	1	1	0	1	0
J	0	0	0	0	0	0	0	1	1	0



```
A <- get.adjacency(g)
```

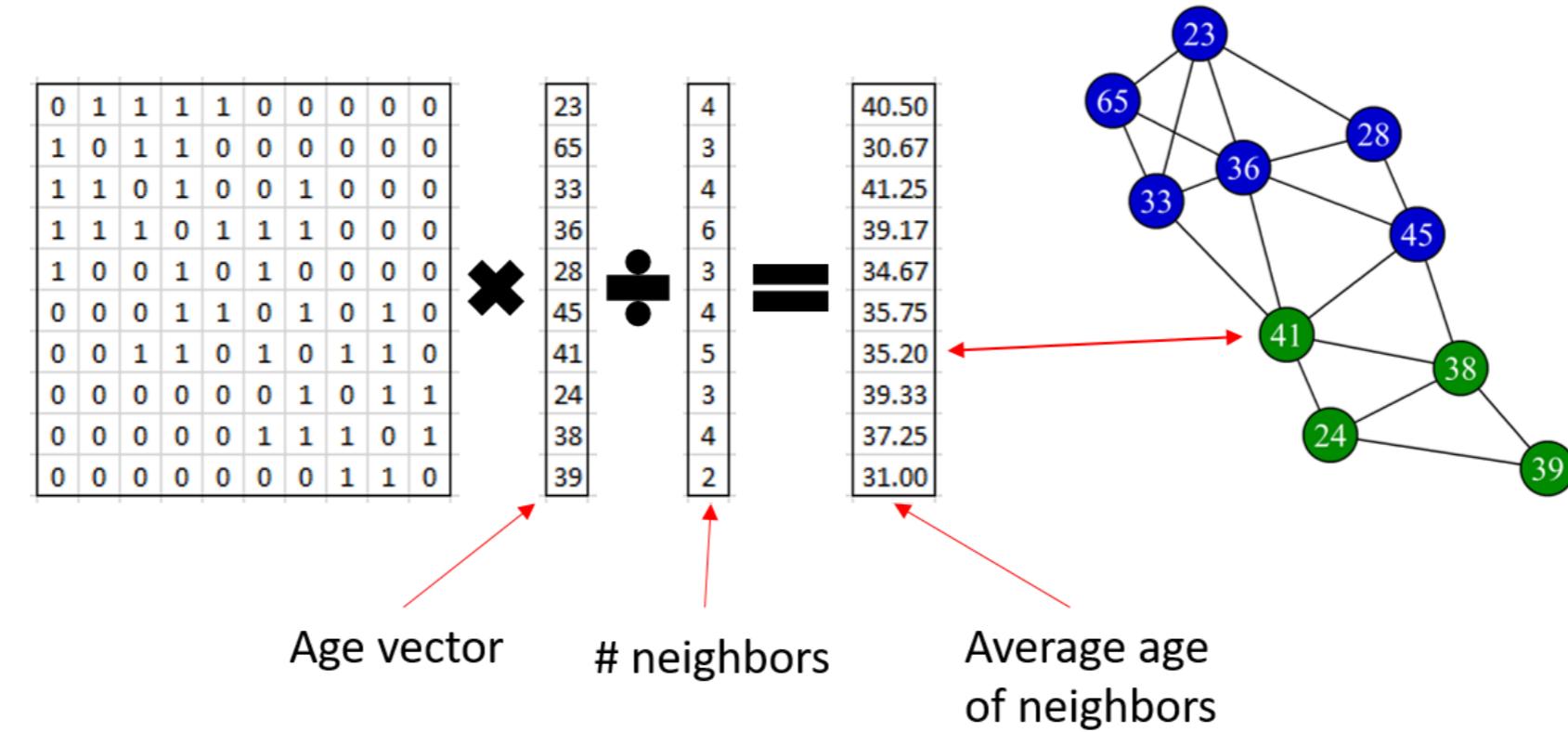
Link based features



```
preference <- c(1,1,1,1,1,1,0,0,0,0)
rNeighbors <- A %*% preference
as.vector(rNeighbors)
```

4 3 3 5 3 2 3 0 1 0

Neighborhood features



```
age <- c(23, 65, 33, 36, 28, 45, 41, 24, 38, 39)
degree <- degree(g)
averageAge <- A %*% age / degree
```

Let's practice!

PREDICTIVE ANALYTICS USING NETWORKED DATA IN R

PageRank

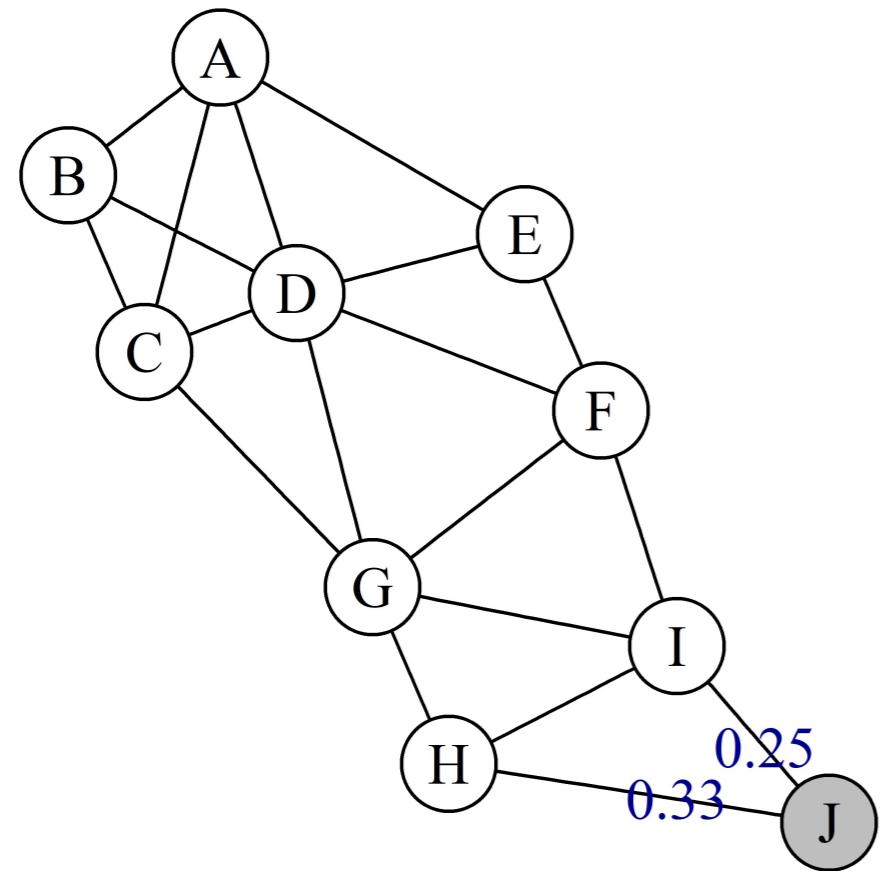
PREDICTIVE ANALYTICS USING NETWORKED DATA IN R



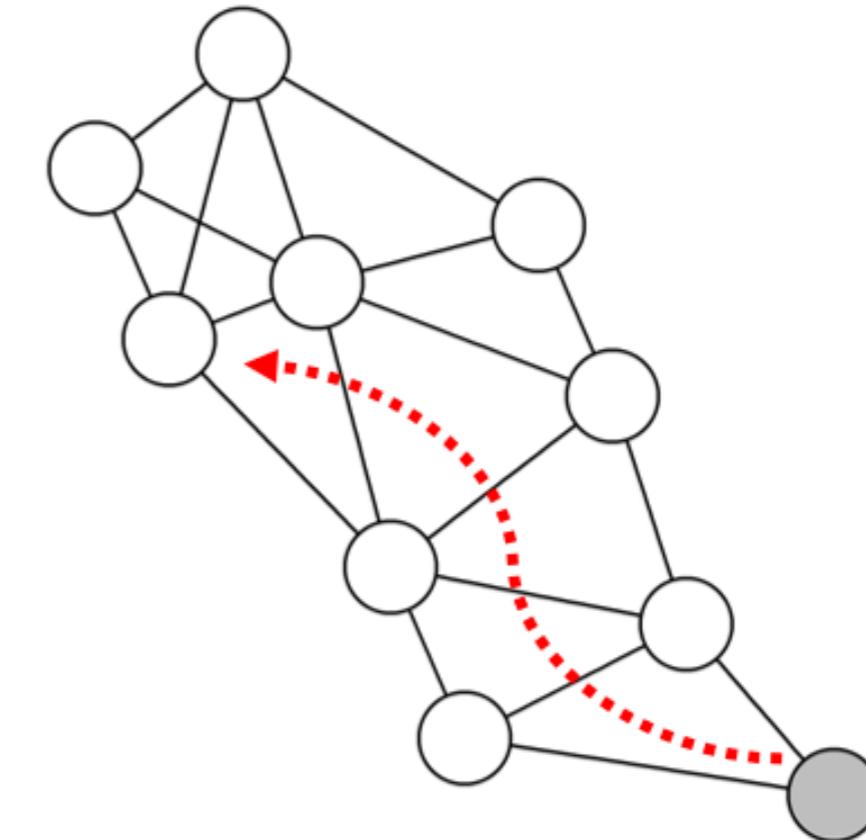
María Óskarsdóttir, Ph.D.

Post-doctoral researcher

The PageRank algorithm



$$\text{PageRank}_J = \alpha \cdot \left(\frac{1}{3} \cdot \text{PageRank}_H + \frac{1}{4} \cdot \text{PageRank}_I \right) + (1 - \alpha) \cdot e_J$$



$$+ \frac{1}{4} \cdot \text{PageRank}_I \Big) + (1 - \alpha) \cdot e_J$$

The PageRank algorithm

$$\vec{PR} = \alpha \cdot A \cdot \vec{PR} + (1 - \alpha) \cdot \vec{e}$$

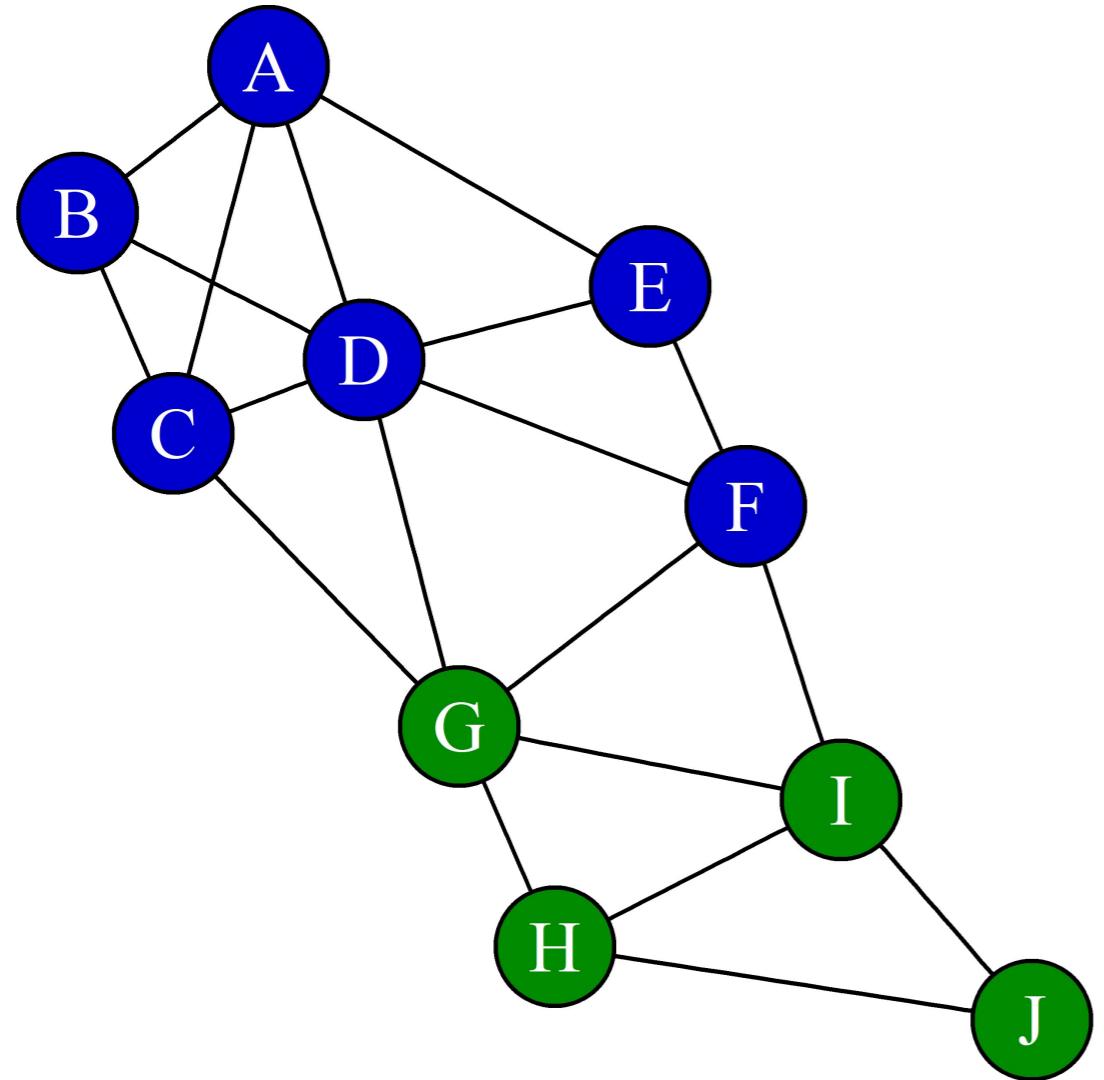
```
page.rank(g)
```

```
$vector
  A          B          C          D          E          F          G
0.10238312 0.07917232 0.10164910 0.14693274 0.07953551 0.10335821 0.12732387
  H          I          J
0.08675903 0.10994175 0.06294435
```

```
$value
[1] 1
```

```
$options
NULL
```

Personalized PageRank



```
page.rank(g,  
personalized = c(1,0,0,0,0,0,0,0,0,0))
```

```
$vector  
A          B          C          D          E  
0.25528911 0.10363533 0.12156935 0.16625582 0.09366836  
F          G          H          I          J  
0.07466596 0.08473039 0.03285162 0.04785657 0.01947748  
  
$value  
[1] 1  
  
$options  
NULL
```

Let's practice!

PREDICTIVE ANALYTICS USING NETWORKED DATA IN R

Extract a dataset

PREDICTIVE ANALYTICS USING NETWORKED DATA IN R



María Óskarsdóttir, Ph.D.

Post-doctoral researcher

```
V(g)$degree<-degree(g)
V(g)$triangles<-count_triangles(g)
V(g)$betweeness<-betweeness(g,normalized=TRUE)
V(g)$transitivity<-transitivity(g,type='local',isolates='zero')
A <- get.adjacency(g)
preference <- c(1,1,1,1,1,0,0,0,0)
age <- c(23,65,33,36,28,45,41,24,38,39)
V(g)$rNeighbors <- as.vector(A%*%preference)
V(g)$averageAge <- as.vector(A%*%age/V(g)$degree)
V(g)$pageRank<-page.rank(g)$vector
V(g)$personalizePageRank<-page.rank(g,
  personalized = c(1,0,0,0,0,0,0,0,0))$vector
g
```

```
IGRAPH UN-- 10 19 --
attr: name (v/c), degree (v/n), triangles (v/n), transitivity
| (v/n), rNeighbors (v/n), averageAge (v/n), pageRank (v/n),
| pPageRank (v/n), label (e/c)
edges (vertex names):
A--B A--C A--D A--E B--C B--D C--D C--G D--E D--F D--G E--F F--G F--I G--I G--H H--I H--J I--J
```

```
IGRAPH UN-- 10 19 --
attr: name (v/c), degree (v/n), triangles (v/n), transitivity
| (v/n), rNeighbors (v/n), averageAge (v/n), pageRank (v/n),
| pPageRank (v/n), label (e/c)
edges (vertex names):
[1] A--B A--C A--D A--E B--C B--D C--D C--G D--E D--F D--G E--F F--G F--I G--I G--H H--I H--J I--J
```

```
as_data_frame(g,what='vertices')
```

		name	degree	triangles	transitivity	rNeighbors	averageAge	pageRank	pPageRank
A	A	A	4	4	0.6666667	4	40.50000	0.10238312	0.25528911
B	B	B	3	3	1.0000000	3	30.66667	0.07917232	0.10363533
C	C	C	4	4	0.6666667	3	41.25000	0.10164910	0.12156935
D	D	D	6	7	0.4666667	5	39.16667	0.14693274	0.16625582
E	E	E	3	2	0.6666667	3	34.66667	0.07953551	0.09366836
F	F	F	4	3	0.5000000	2	35.75000	0.10335821	0.07466596
G	G	G	5	4	0.4000000	3	35.20000	0.12732387	0.08473039
H	H	H	3	2	0.6666667	0	39.33333	0.08675903	0.03285162
I	I	I	4	3	0.5000000	1	37.25000	0.10994175	0.04785657
J	J	J	2	1	1.0000000	0	31.00000	0.06294435	0.01947748

Preprocessing - missing values

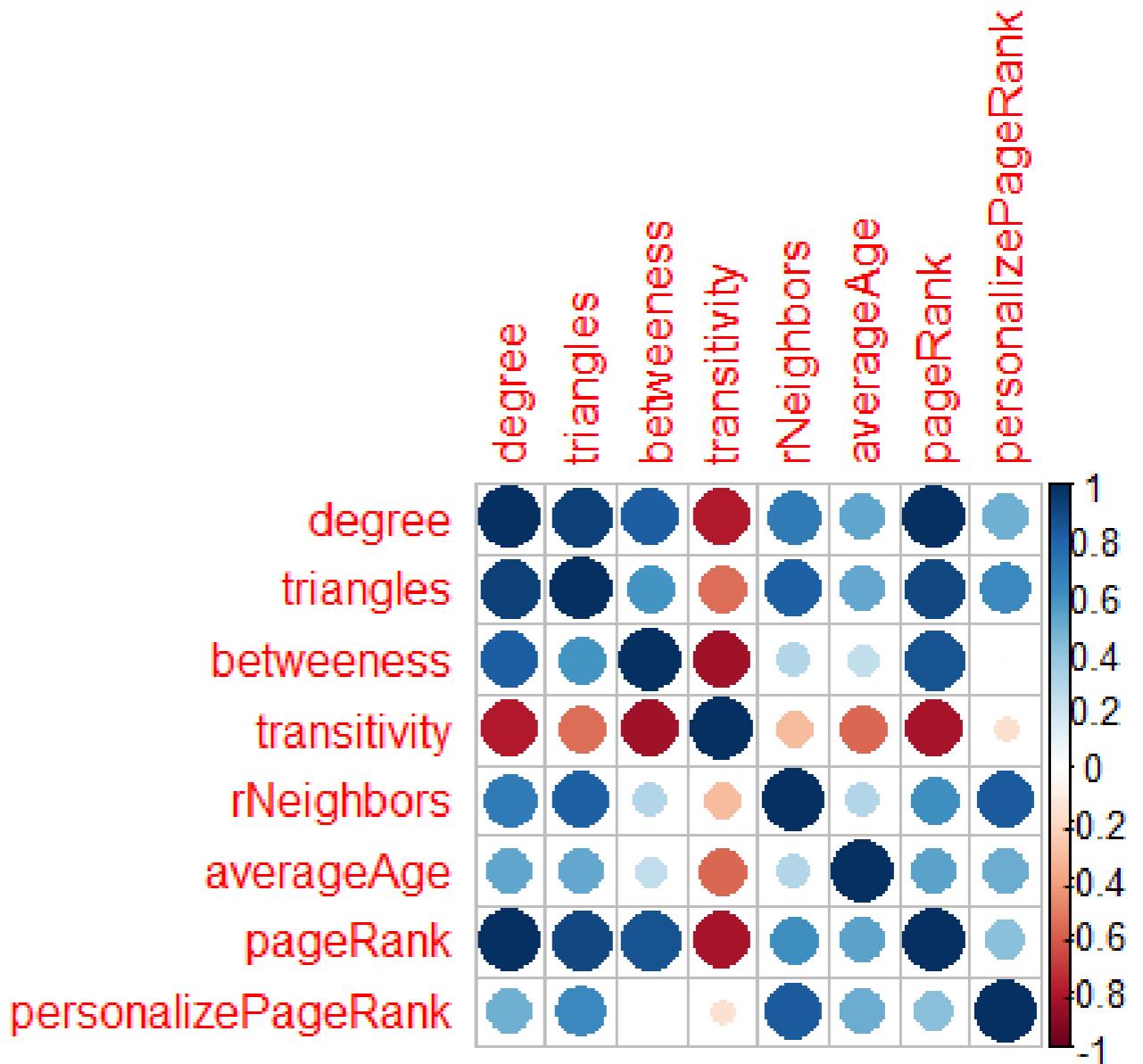
name	degree	triangles	transitivity	rNeighbors	averageAge	pageRank	pPageRank
A	4	4	0.6666667	4	40.50000	0.10238312	0.25528911
B	3	3	1.0000000	3	30.66667	0.07917232	0.10363533
C	NA	4	0.6666667	3	41.25000	0.10164910	0.12156935
D	6	7	0.4666667	5	39.16667	0.14693274	0.16625582
E	3	2	0.6666667	3	34.66667	0.07953551	0.09366836
F	4	3	0.5000000	2	35.75000	0.10335821	0.07466596
G	5	4	0.4000000	3	35.20000	0.12732387	0.08473039
H	2	2	0.6666667	0	39.33333	0.08675903	0.03285162
I	NA	3	0.5000000	1	37.25000	0.10994175	0.04785657
J	2	1	1.0000000	0	31.00000	0.06294435	0.01947748

```
sum(is.na(dataset$degree))
```

2

Preprocessing - correlated variables

```
library(corrplot)  
  
M <- cor(dataset[,-1])  
  
corrplot(M, method = 'circle')
```



Let's practice!

PREDICTIVE ANALYTICS USING NETWORKED DATA IN R

Building a predictive model

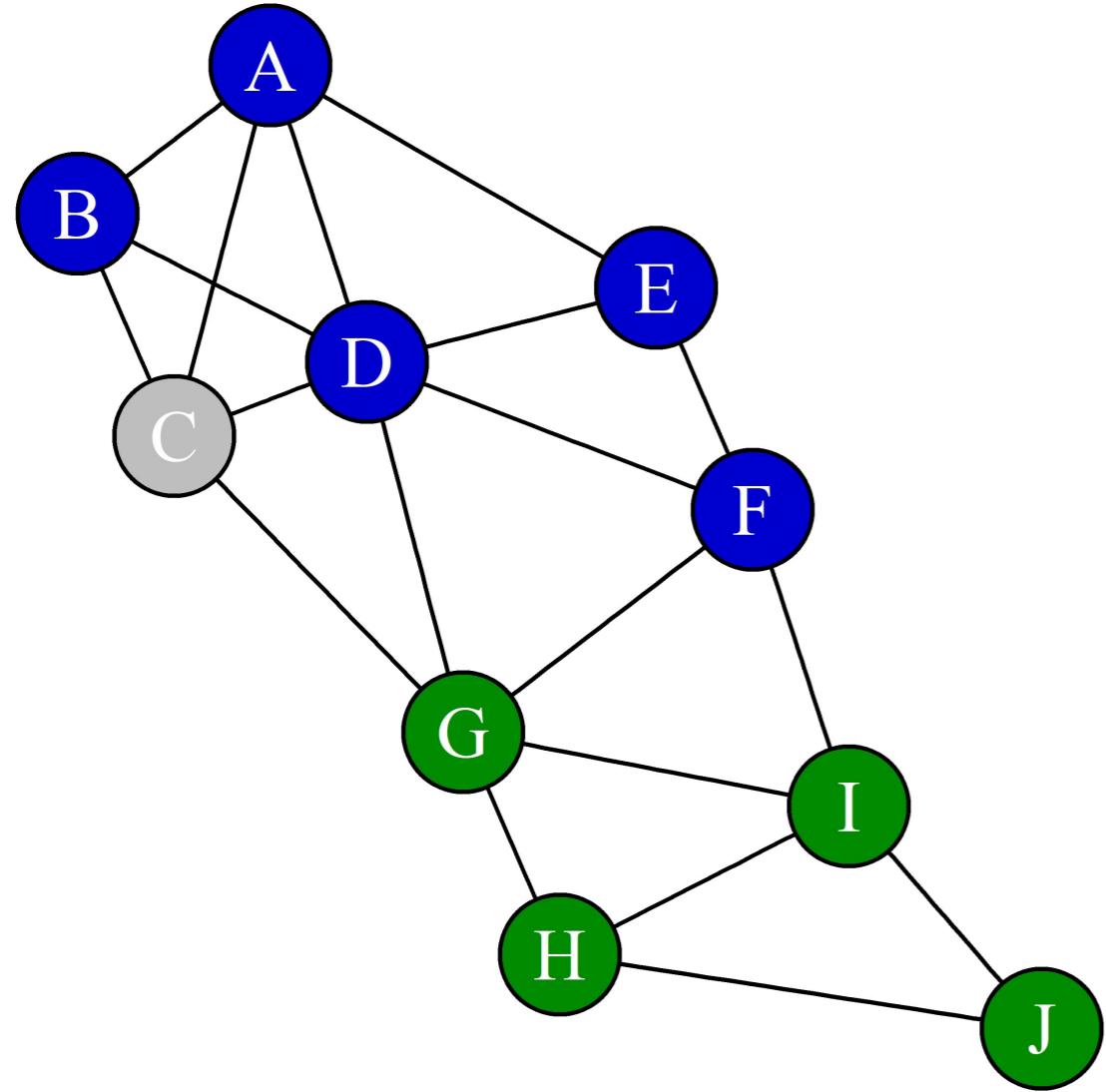
PREDICTIVE ANALYTICS USING NETWORKED DATA IN R



María Óskarsdóttir, Ph.D.

Post-doctoral researcher

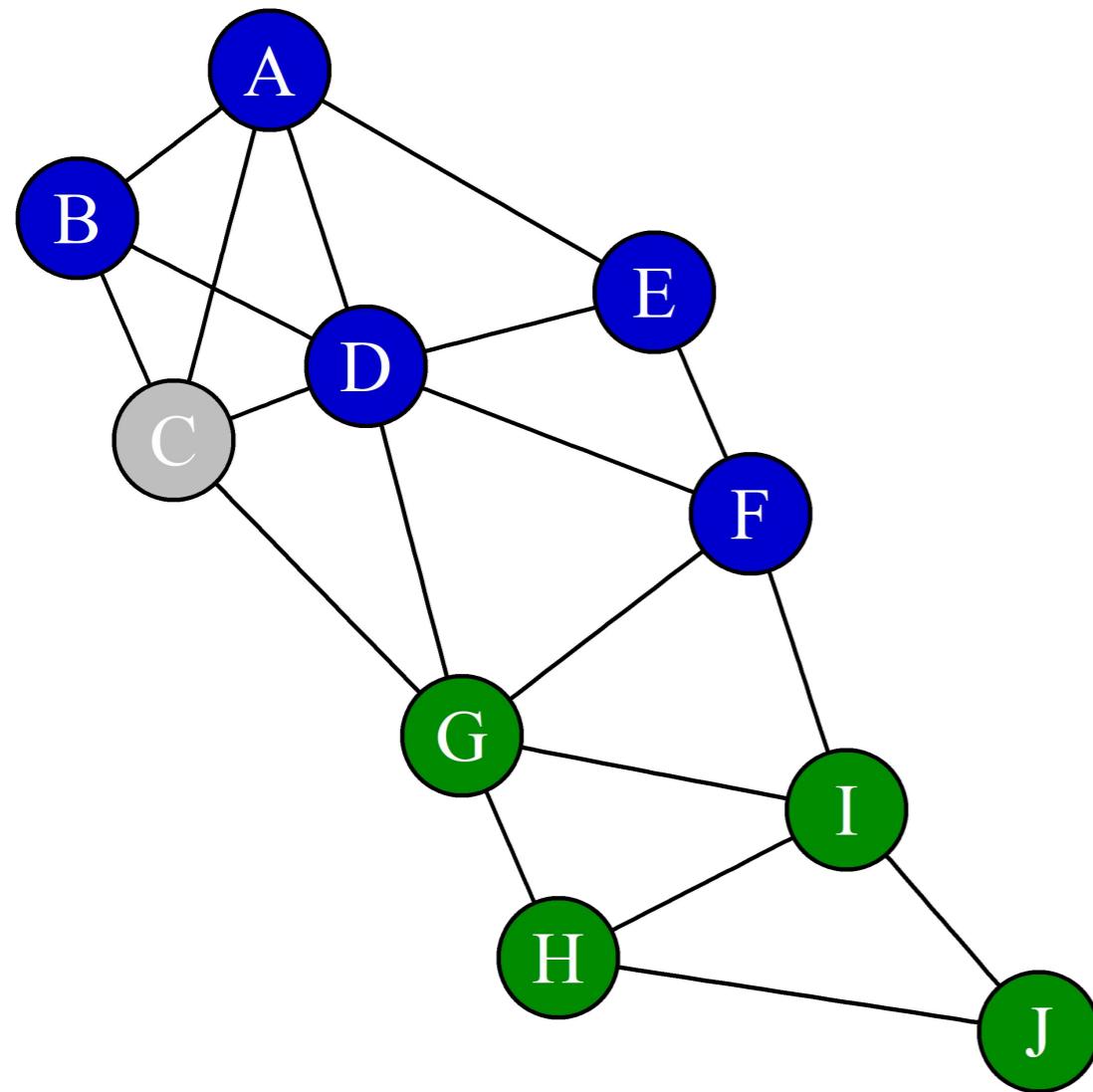
Predictive modeling



```
dataset$preference<-c(rep('R',2), '?',  
rep('R',3),rep('P',4))  
dataset[,c(1,9)]
```

name	preference
A	A
B	R
C	?
D	R
E	R
F	R
G	P
H	P
I	P
J	P

Predictive modeling

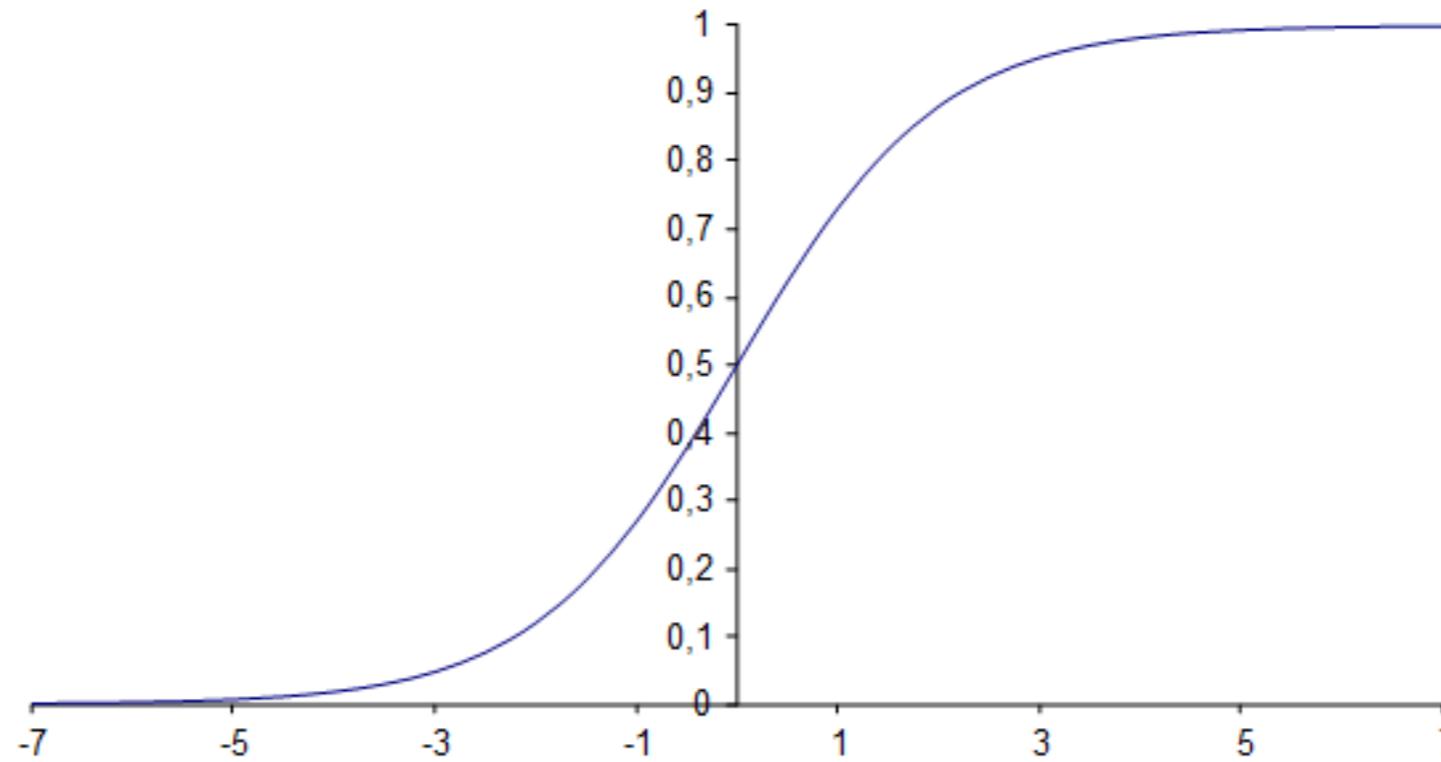


```
dataset$R<-c(1,1,'?',1,1,1,0,0,0,0)  
dataset[,c(1,9,10)]
```

	name	preference	R
A	A		R 1
B	B		R 1
C	C		? ?
D	D		R 1
E	E		R 1
F	F		R 1
G	G		P 0
H	H		P 0
I	I		P 0
J	J		P 0

```
training_set<-dataset[-3,-9]  
test_set<-dataset[3,-9]
```

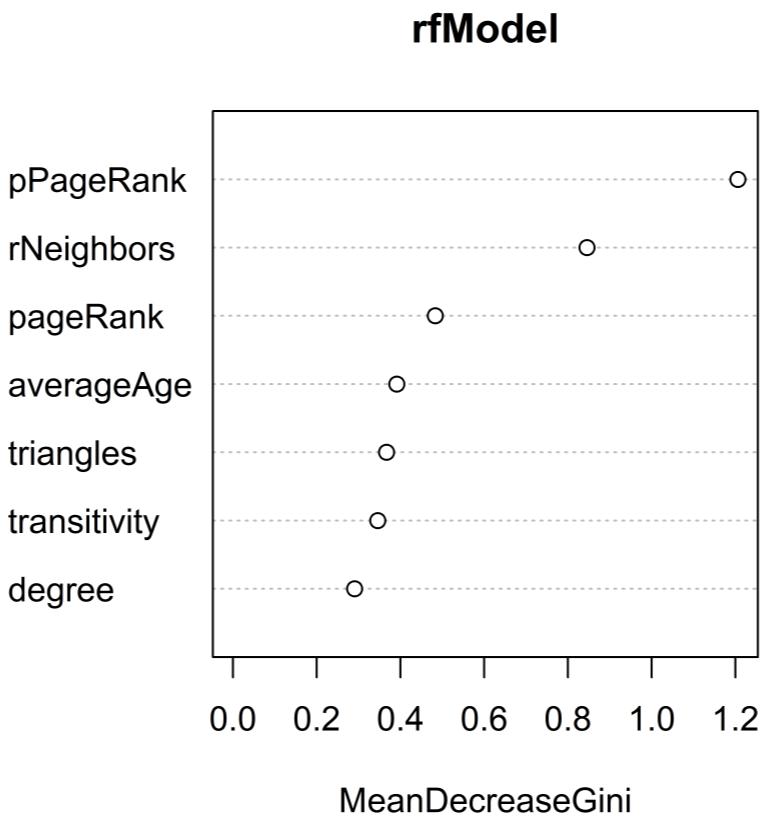
Logistic regression



```
glm(R~degree+pageRank, dataset=training_set,family='binomial')  
glm(R~., dataset=training_set,family='binomial')
```

Random forests

```
library(randomForest)  
rfModel<-randomForest(R~., dataset=training_set)  
varImpPlot(rfModel)
```



Let's practice!

PREDICTIVE ANALYTICS USING NETWORKED DATA IN R

Evaluating model performance

PREDICTIVE ANALYTICS USING NETWORKED DATA IN R



María Óskarsdóttir, Ph.D.

Post-doctoral researcher

Making predictions

```
library(pROC)
```

- Logistic regression

```
logPredictions <- predict(logModel, newdata = test_set, type = "response")
```

- Random forest

```
rfPredictions<- predict(rfModel, newdata = test_set, type='prob')
```

```
rfPredictions
```

```
attr(,"class")
```

```
0      1  
C 0.136 0.864  
"matrix" "votes"
```

AUC

- Probability that a randomly chosen churner gets a higher score than a randomly chosen non-churner
- Displays the trade-off between the model's sensitivity and specificity
- A number between:
 - **0.5**: random model
 - **1**: perfect model

```
library(pROC)  
auc(test_set$label, logPredictions)
```

Top decile lift

- How much better is the prediction model at identifying churners, compared to a random sample of customers
- Computes the proportion of actual churners amongst the 10% of customers with the highest predicted churn probability
- Lift value greater than 1 means that the model is better than a random model
- If, in the top 10% of the highest scores there are **60%** churners and in the whole population there are **10%** churners, then the lift is $60/10 = 6$

```
library(lift)  
TopDecileLift(test_set$label, predictions, plot=TRUE)
```

Let's practice!

PREDICTIVE ANALYTICS USING NETWORKED DATA IN R

Summary and final thoughts

PREDICTIVE ANALYTICS USING NETWORKED DATA IN R



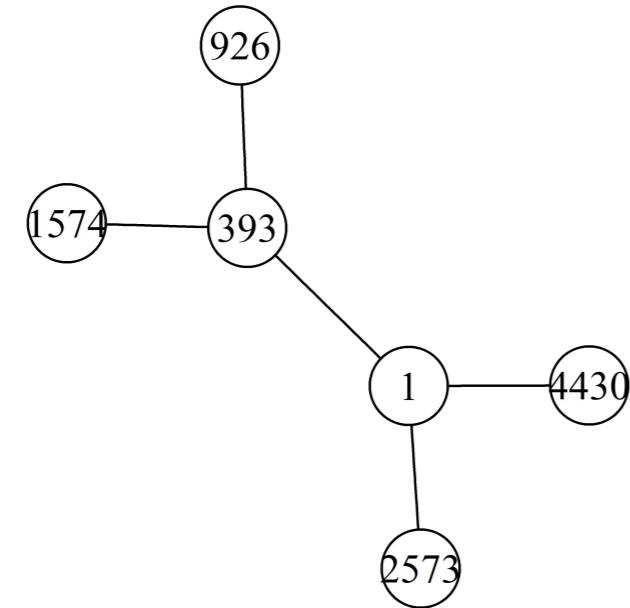
Bart Baesens, Ph.D.

Professor of Data Science, KU Leuven
and University of Southampton

Labeled networks

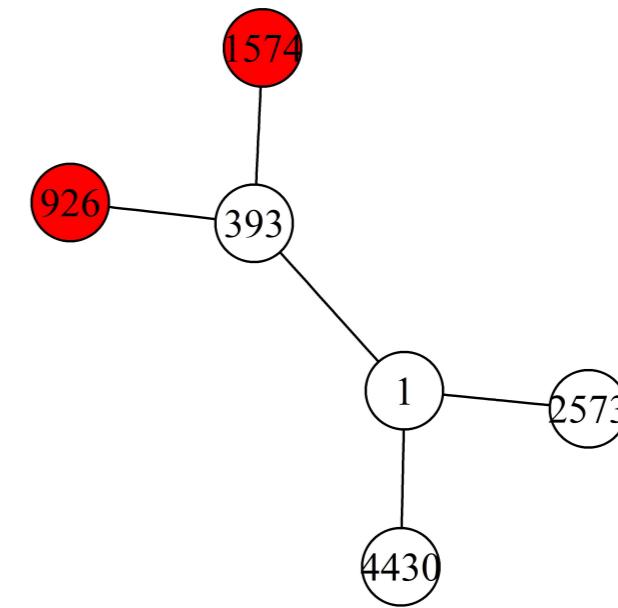
edgeList

```
from      to
1       1     393
2       1    2573
3       1   4430
4     393     926
5     393   1574
```

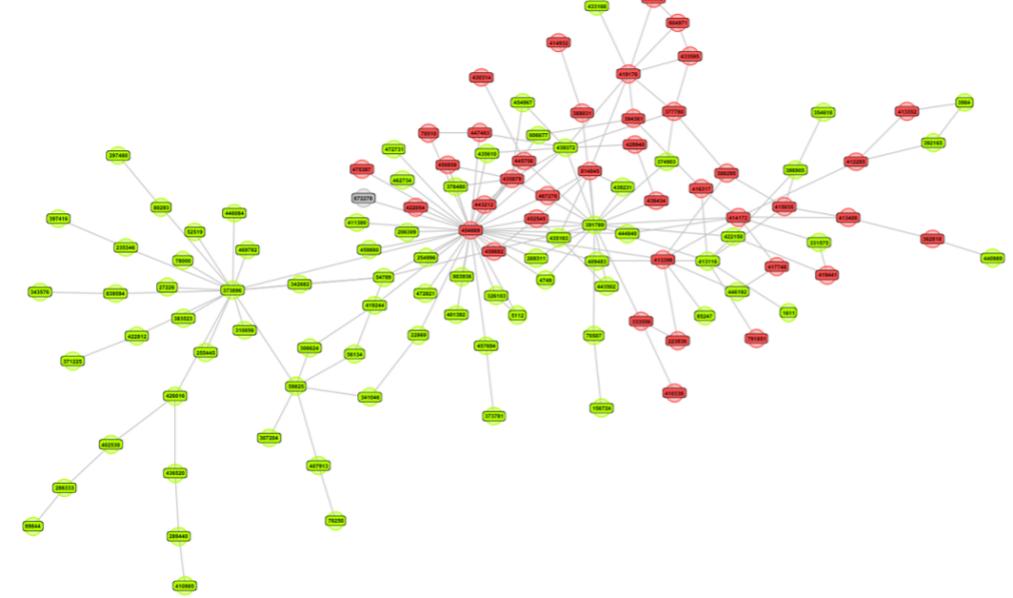


customers

```
id  churn
1   0
2   0
3   0
4   0
5   1
6   1
```



Homophily



Dyadicity: connectedness between nodes with same label

Birds of a feather flock together

Heterophilycty: connectedness between nodes with opposite labels

Network Featurization

```
g
IGRAPH UN-- 10 19 --
attr: name (v/c), label (e/c)
edges (vertex names):
A--B A--C A--D A--E B--C B--D C--D C--G D--E D--F D--G E--F F--G F--I G--I G--H H--I H--J I--J
```

```
V(g)$degree<-degree(g)
```

```
g
IGRAPH UN-- 10 19 --
attr: name (v/c), degree (v/n), triangles (v/n), transitivity
| (v/n), rNeighbors (v/n), averageAge (v/n), pageRank (v/n),
| pPageRank (v/n), label (e/c)
edges (vertex names):
A--B A--C A--D A--E B--C B--D C--D C--G D--E D--F D--G E--F F--G F--I G--I G--H H--I H--J I--J
```

1. Extract dataframe:

```
dataset <- as_data_frame(g, what='vertices')
```

2. Preprocess data set:

- Missing values, outliers, correlated variables, and normalization

3. Build model:

```
glm(R~., dataset=training_set, family='binomial')
```

4. Make predictions:

```
logPredictions <- predict(logModel, newdata=test_set, type="response")
```

5. Measure performance:

```
auc(test_set$label, logPredictions)  
TopDecileLift(test_set$label, predictions, plot=TRUE)
```

Congratulations!

PREDICTIVE ANALYTICS USING NETWORKED DATA IN R

Exploring your data set

CASE STUDIES: NETWORK ANALYSIS IN R



Edmund Hart

Instructor

```
library(igraph)
library(dplyr)
amzn_raw <- read.csv("datasets/amazon_purchase_no_book.csv")
head(amzn_raw)
```

```
from to title.from group.from categories.from salesrank.from
1 1 44 42 The NBA's 100 Greatest Plays DVD 33124 5
2 2 179 71 Africa Screams/Jack & The Bean DVD 53825 21

totalreviews.from totalreviews.1.from
1 13 13
2 13 13

title.to group.to
1 Pixote DVD
2 Jonny Quest - Bandit in Adventures Best Friend Video

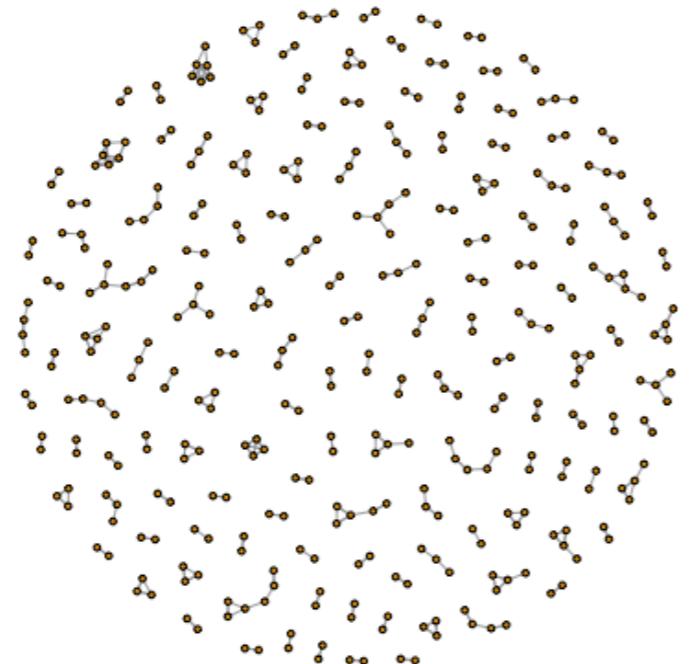
categories.to salesrank.to totalreviews.to totalreviews.1.to date
1 19685 15 24 24 2003-03-02
2 21571 5 2 2 2003-03-02
```

Creating the graph

```
amzn_g <- amzn_raw %>%  
  filter(date == "2003-03-02") %>%  
  select(from, to) %>%  
  graph_from_data_frame(directed = TRUE)  
gorder(amzn_g)  
gsize(amzn_g)
```

Visualize the graph

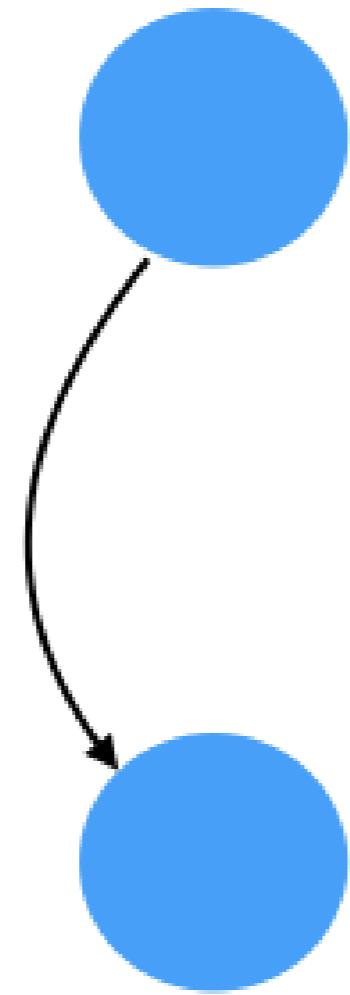
```
sg <- induced_subgraph(amzn_g, 1:500)
sg <- delete.vertices(sg, degree(sg) == 0)
plot(sg, vertex.label = NA, edge.arrow.width = 0,
     edge.arrow.size = 0, margin = 0, vertex.size = 2)
```



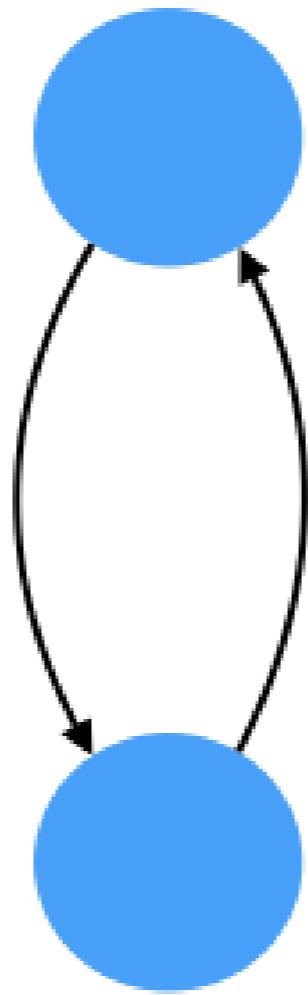
Null

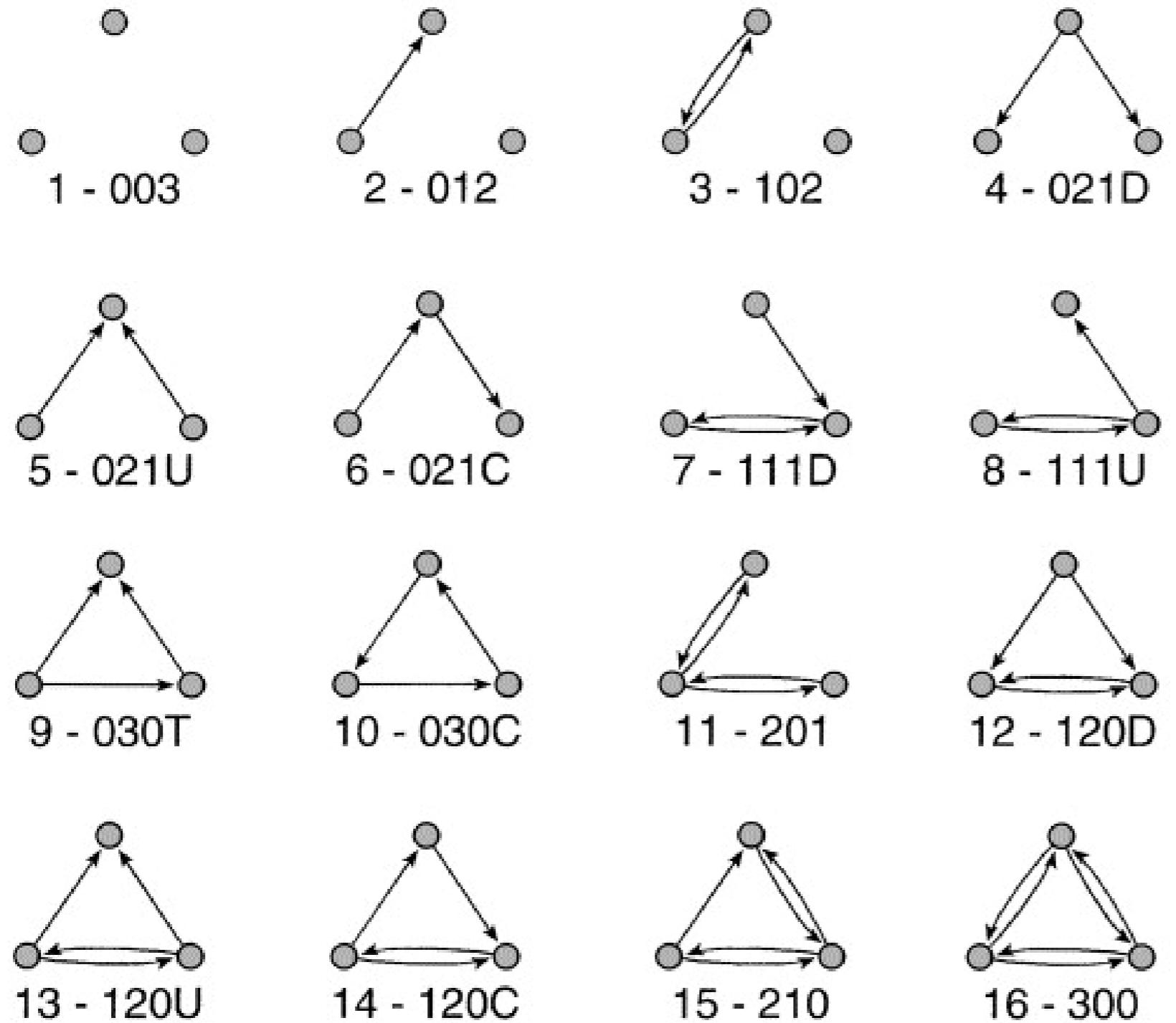


Asymmetric



Mutual





Let's practice

CASE STUDIES: NETWORK ANALYSIS IN R

Exploring temporal structure

CASE STUDIES: NETWORK ANALYSIS IN R



Edmund Hart

Instructor

Are important products always important?

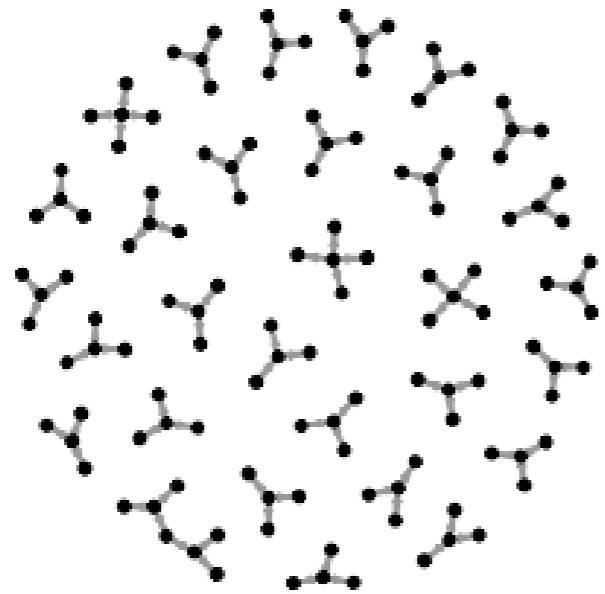
```
# Get unique Dates  
d <- sort(unique(amzn_raw$date))  
  
# Create graph from first date  
amzn_g <- graph_from_data_frame(  
  amzn_raw %>%  
    filter(date == d[1]) %>%  
    select(from, to), directed = TRUE  
)
```

Are important products always important?

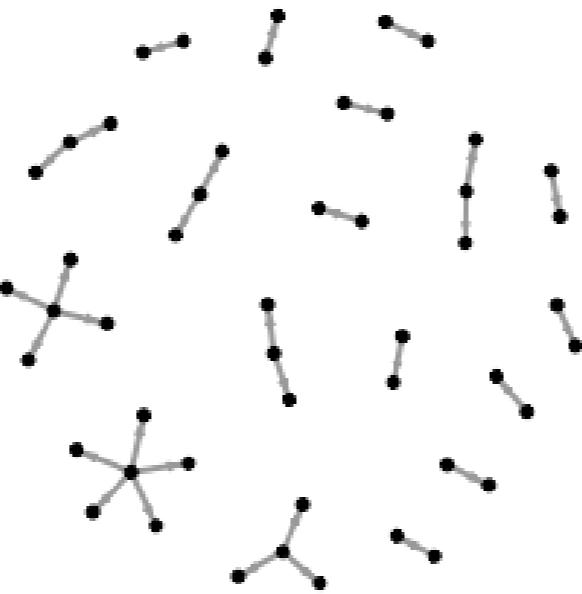
```
# Find products that are "important"  
high_out_degree <- degree(amzn_g, mode = "out") > 2  
  
low_in_degree <- degree(amzn_g, mode = "in") < 1  
  
important_nodes <- high_out_degree & low_in_degree  
  
imp_prod <- V(amzn_g)[important_nodes]  
  
# Store as a data frame to later join on  
tmp_df <- data.frame(imp_prod = as.numeric(names(imp_prod)))
```

```
## Create list to hold output
time_graph <- list()
## Create a 2x2 layout for plots and increase margins
par(mfrow = c(2, 2), mar = c(1.1, 1.1, 1.1, 1.1))
## Loop over the data to build
for(i in 1:length(d)){
  ## Create a data frame at each time stamp
  ip_df <- amzn_raw %>%
    filter(date == d[i]) %>%
    right_join(tmp_df, by = c("from" = "imp_prod")) %>%
    na.omit()
  ## Create an igraph object from that data frame
  time_graph[[i]] <- ip_df %>%
    select(from, to) %>%
    graph_from_data_frame(directed = TRUE)
  ## See what important vertices look like by date
  plot(time_graph[[i]], main = d[i]) }
```

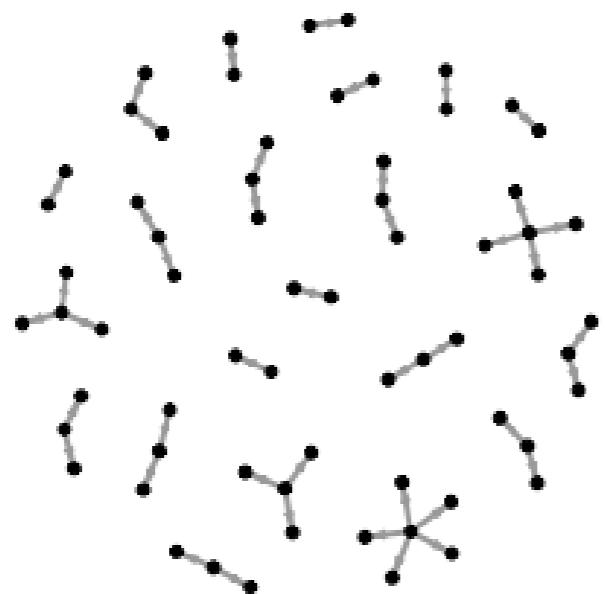
2003-03-02



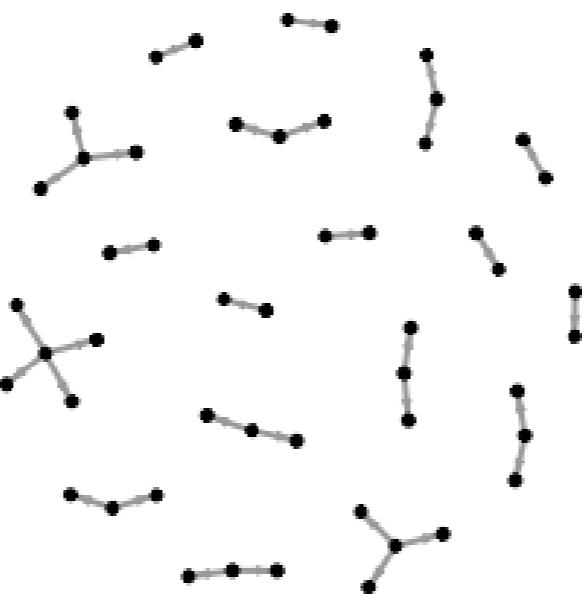
2003-03-12



2003-05-05



2003-06-01



Let's practice!

CASE STUDIES: NETWORK ANALYSIS IN R

Building a graph from raw data

CASE STUDIES: NETWORK ANALYSIS IN R



Edmund Hart

Instructor

Exploring the data

- Data is several days of all the tweets mentioning #rstats
- Key attributes for building a graph are:
 - screen name
 - raw text of the tweet

Anatomy of a tweet

1. *ReecheshJC*: "Hey #rstats, how do I do fct_lump but where I lump based on count values in a column?"
2. *kom_256*: "RT @elenagbg: Retweeted R-Ladies Madrid (@RLadiesMAD):\n\nEn el #OCSummit17... Fast Talks sobre #rstats organizado por... <https://t.co/CKY5aG...>"

```
library(igraph)
library(stringr)
raw_tweets <- read.csv("datasets/rstatstweets.csv",
  stringsAsFactors = FALSE)
```

Data sample, single row

```
user_name:      Karen Millidine
screen_name:    KJMillidine
tweet_text:     RT @Rbloggers: RStudio v1.1 Released
https://t.co/kCMHc689nY #rstats #DataScience
favorites:      0
retweets:       96
location:       None
expanded_url:   https://wp.me/pMm6L-ExV
in_reply_to_tweet_id: NA
in_reply_to_user_id: NA
dt:             10/10/17
```

Building the graph

```
## Get all the screen names  
all_sn <- unique(raw_tweets$screen_name)  
  
## Create graph  
retweet_graph <- graph.empty()  
  
## Add screen names as vertices  
retweet_graph <- retweet_graph + vertices(all_sn)
```

Building the graph

```
## Extract name and add edges
for(i in 1:dim(raw_tweets)[1]){
  # Extract retweet name
  rt_name <- find_rt(raw_tweets$tweet_text[i])
  # If there is a name add an edge
  if(!is.null(rt_name)){
    # Check to make sure the vertex exists, if not, add it
    if(!rt_name %in% all_sn){
      retweet_graph <- retweet_graph + vertices(rt_name)
    }
    # add the edge
    retweet_graph <- retweet_graph +
      edges(c(raw_tweets$screen_name[i], rt_name))
  }
}
```

Cleaning the graph

```
## Size the number of degree 0 vertices  
sum(degree(retweet_graph) == 0)  
  
## Trim and simplify  
retweet_graph <- simplify(retweet_graph)  
retweet_graph <- delete.vertices(retweet_graph,  
degree(retweet_graph) == 0)
```

Let's practice!

CASE STUDIES: NETWORK ANALYSIS IN R

Building a mentions graph

CASE STUDIES: NETWORK ANALYSIS IN R



Edmund Hart

Instructor

Recall tweet anatomy

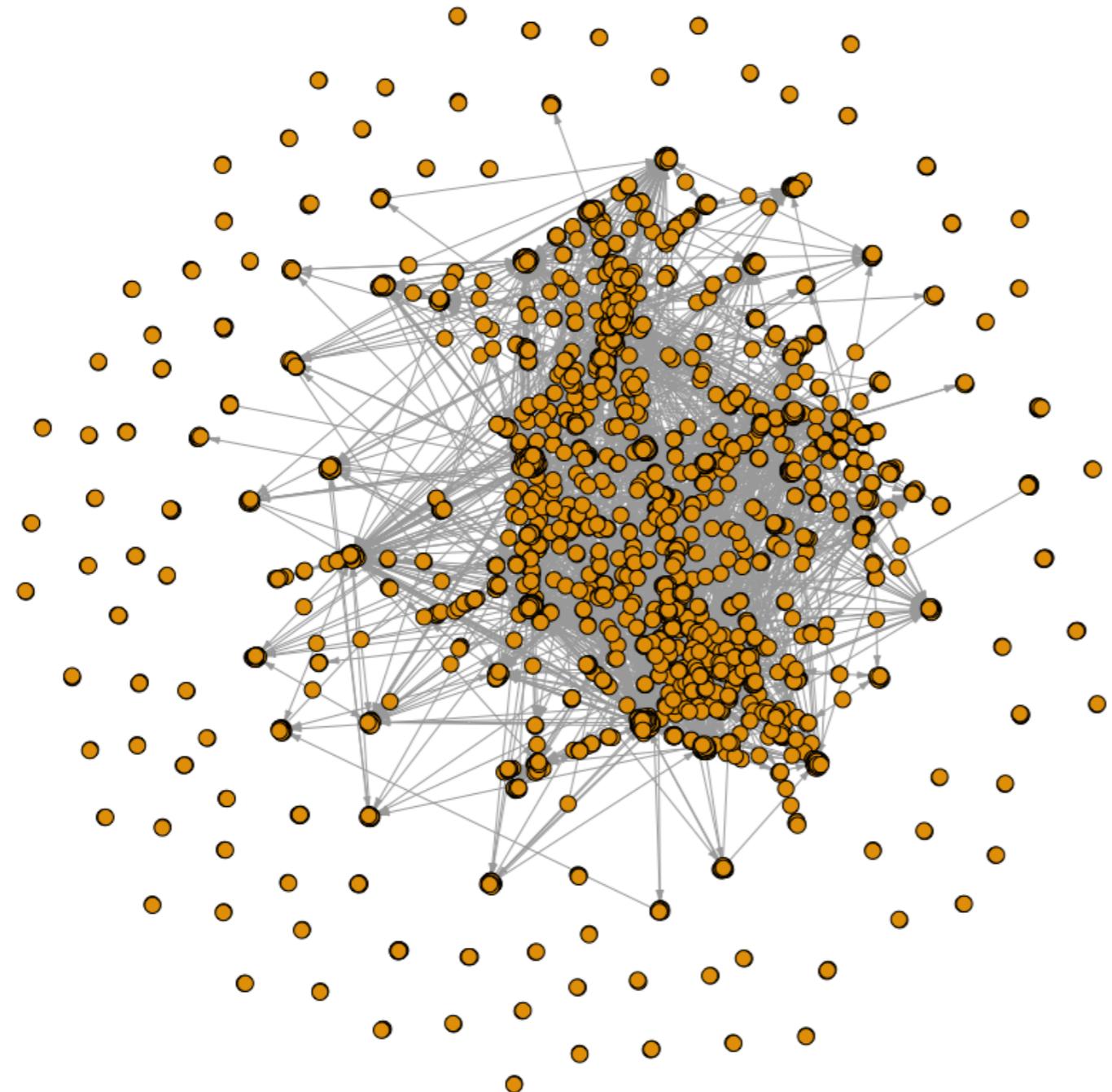
AlexisAchim: "@LAStools @Lees_Sandbox @jhollist
@LeahAWasser LidR is also available directly on CRAN #rstats"

timelyportfolio: "just might have a demo of @emeeks new
#reactjs/#d3js semiotic in #rstats in the works"

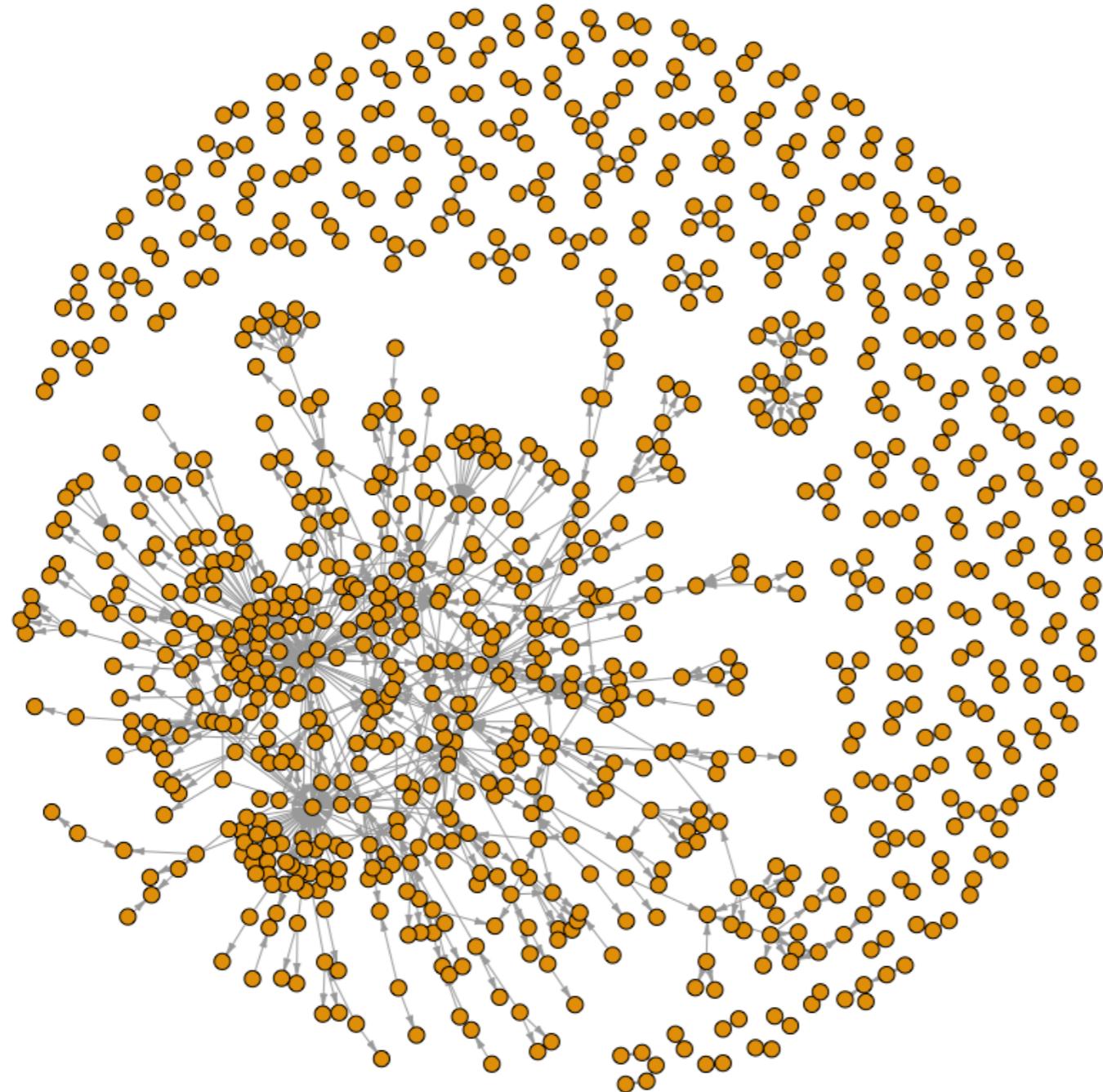
Build your mentions graph

```
ment_g <- graph.empty()
ment_g <- ment_g + vertices(all_sn)
for(i in 1:dim(raw_tweets)[1]) {
  ment_name <- mention_ext(raw_tweets$ tweet_text[i])
  if(length(ment_name) > 0 ) {
    # Add the edge(s)
    for(j in ment_name) {
      # Check to make sure the vertex exists, if not, add it
      if(!j %in% all_sn) {
        ment_g <- ment_g + vertices(j)  }
      ment_g <- ment_g + edges(c(raw_tweets$screen_name[i], j))
    }
  }
}
ment_g <- simplify(ment_g)
ment_g <- delete.vertices(ment_g, degree(ment_g) == 0)
```

Retweet Graph



Mentions Graph



Let's practice!

CASE STUDIES: NETWORK ANALYSIS IN R

Finding communities

CASE STUDIES: NETWORK ANALYSIS IN R



Edmund Hart
Instructor

Three different communities

```
undirected_ment_g <- as.undirected(ment_g)

ment_edg <- cluster_edge_betweenness(undirected_ment_g)
ment_eigen <- cluster_leading_eigen(undirected_ment_g)
ment_lp <- cluster_label_prop(undirected_ment_g)
```

Sizing the communities

```
length(ment_edg)  
length(ment_eigen)  
length(ment_lp)
```

```
173  
168  
212
```

```
table(sizes(ment_edg))
```

	2	3	4	5	6	7	8	9	11	12	18	19	20	23	24	26	28
103	21	14	7	3	3	1	2	1	2	2	1	1	1	1	2	1	1
31	33	38	40	41	52	58											
	1	1	1	1	1	1	1										

```
table(sizes(ment_eigen))
```

	2	3	4	5	6	7	9	10	12	18	23	26	29	30	32	34	35	58
103	22	14	7	4	3	1	1	1	1	1	1	1	1	1	1	1	1	
64	66	101																
	1	1	1															

```
table(sizes(ment_lp))
```

	2	3	4	5	6	7	8	9	10	11	12	13	16	25	26	67	70
103	32	22	19	8	5	4	3	5	1	2	3	1	1	1	1	1	1

Comparing communities

```
compare(ment_edg, ment_eigen, method = 'vi')
```

```
0.9761792
```

```
compare(ment_eigen, ment_lp, method = 'vi')
```

```
1.192238
```

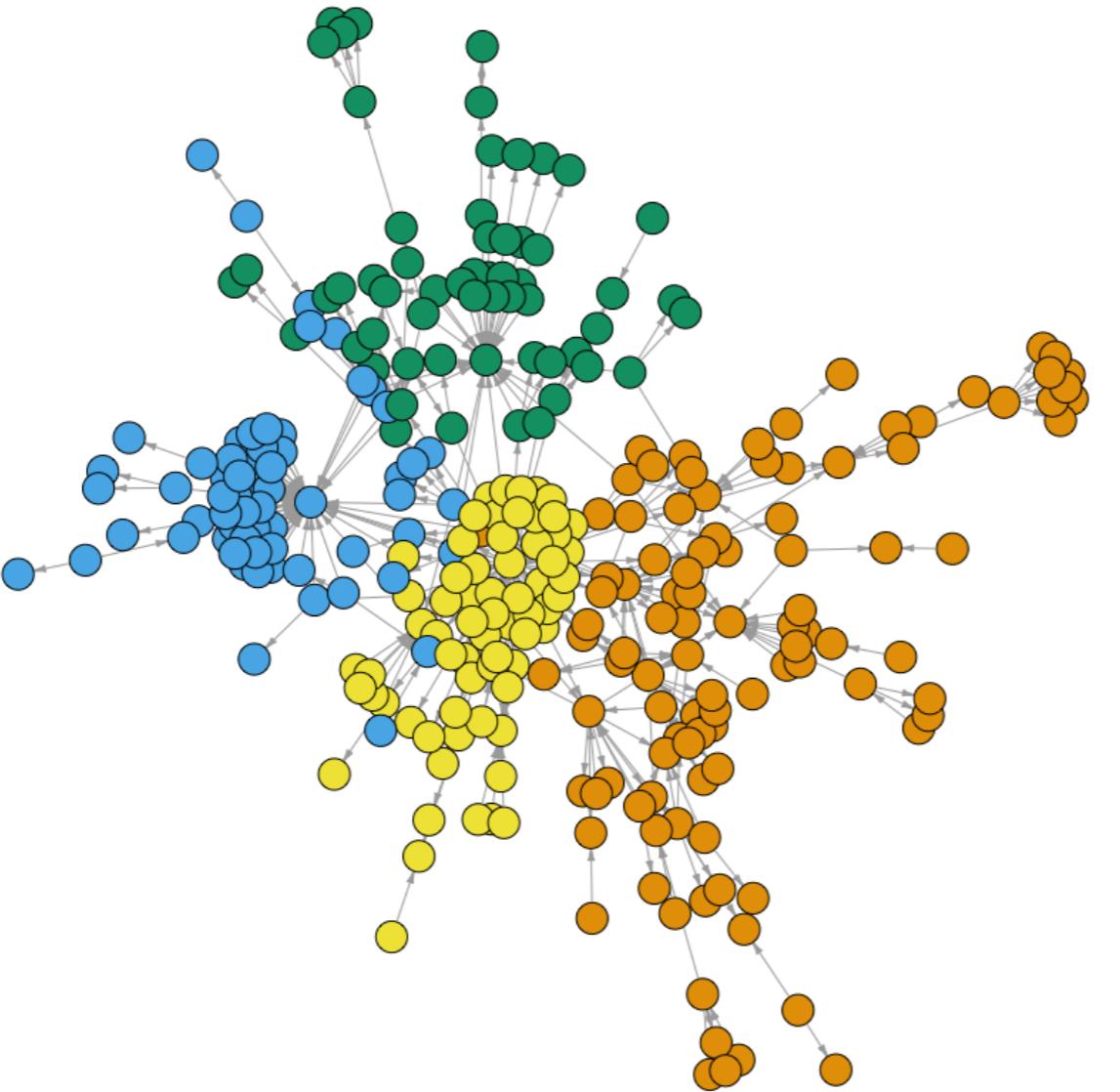
```
compare(ment_lp, ment_edg, method = 'vi')
```

```
0.9631608
```

Plotting community structure

```
lrg_eigen <- as.numeric(  
  names(ment_eigen[which(sizes(ment_eigen) > 45)])  
)  
  
eigen_sg <- induced.subgraph(ment_g,  
  V(ment_g)[ eigen %in% lrg_eigen])  
  
plot(eigen_sg, vertex.label = NA, edge.arrow.width = .8,  
  edge.arrow.size = 0.2,  
  coords = layout_with_fr(ment_sg), margin = 0,  
  vertex.size = 6, vertex.color =  
  as.numeric(as.factor(V(eigen_sg)$eigen)))
```

Mentions subgraph communities



Let's practice!

CASE STUDIES: NETWORK ANALYSIS IN R

Exploring our data

CASE STUDIES: NETWORK ANALYSIS IN R



Edmund Hart

Instructor

```
library(igraph)
library(dplyr)
library(lubridate)
bike_dat <- read.csv("datasets/bike2_test3.csv", stringsAsFactors = FALSE)
str(bike_dat)
```

```
'data.frame': 52800 obs. of 13 variables:
 $ tripduration : int 295 533 1570 2064 2257 296 412...
 $ from_station_id : int 49 165 25 300 85 174 75 45 85 99 ...
 $ from_station_name: chr "Dearborn St & Monroe St" ...
 $ to_station_id   : int 174 308 287 296 313 198 56 147 174 99 ...
 $ to_station_name : chr "Canal St & Madison St" ...
 $ usertype        : chr "Subscriber" "Subscriber" "Customer"...
 $ gender          : chr "Male" "Male" "" "" ...
 $ birthyear       : int 1964 1972 NA NA 1963 1973 1989 1965 1983 1983 ...
 $ from_latitude   : num 41.9 42 41.9 41.9 41.9 ...
 $ from_longitude  : num -87.6 -87.7 -87.6 -87.6 -87.6 ...
 $ to_latitude     : num 41.9 41.9 41.9 41.9 41.9 ...
 $ to_longitude    : num -87.6 -87.7 -87.6 -87.6 -87.6 ...
 $ geo_distance    : num 859 1882 2159 288 3044 ...
```

Creating the bike sharing graph

```
trip_df <- bike_dat %>%  
  group_by(from_station_id, to_station_id) %>%  
  summarize(weights = n())  
  
head(trip_df)
```

```
# A tibble: 6 x 3  
# Groups: from_station_id [1]  
  from_station_id to_station_id weights  
          <int>        <int>    <int>  
1             5            5        2  
2             5           14        1  
3             5           16        1  
4             5           25        3  
5             5           29        3  
6             5           33        1
```

Creating the bike sharing graph

```
trip_g <- graph_from_data_frame(trip_df[, 1:2])  
# add edge weights  
E(trip_g)$weight <- trip_df$weights  
# Quick exploration of our graph  
gsize(trip_g)
```

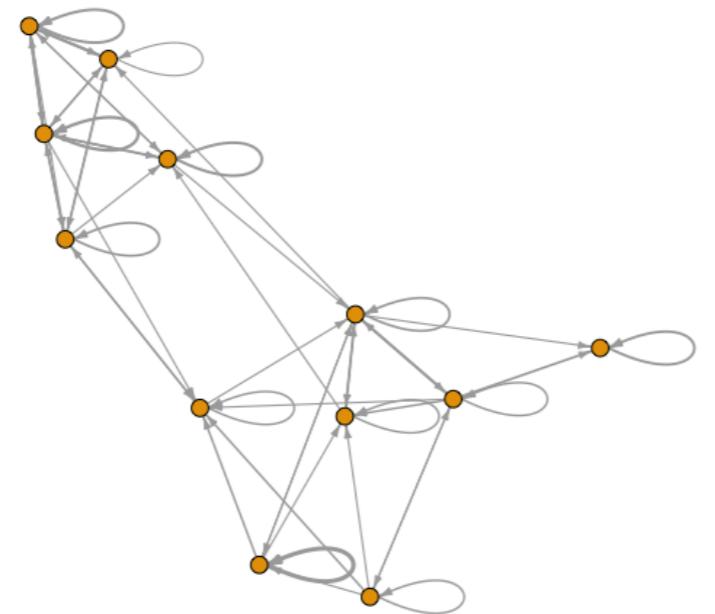
19052

```
gorder(trip_g)
```

300

Explore the graph

```
sg <- induced_subgraph(trip_g, 1:12)
plot(sg, vertex.label = NA, edge.arrow.width = 0.8,
     edge.arrow.size = 0.6,
     margin = 0,
     vertex.size = 6,
     edge.width = log(E(sg)$weight + 2))
```



Let's practice!

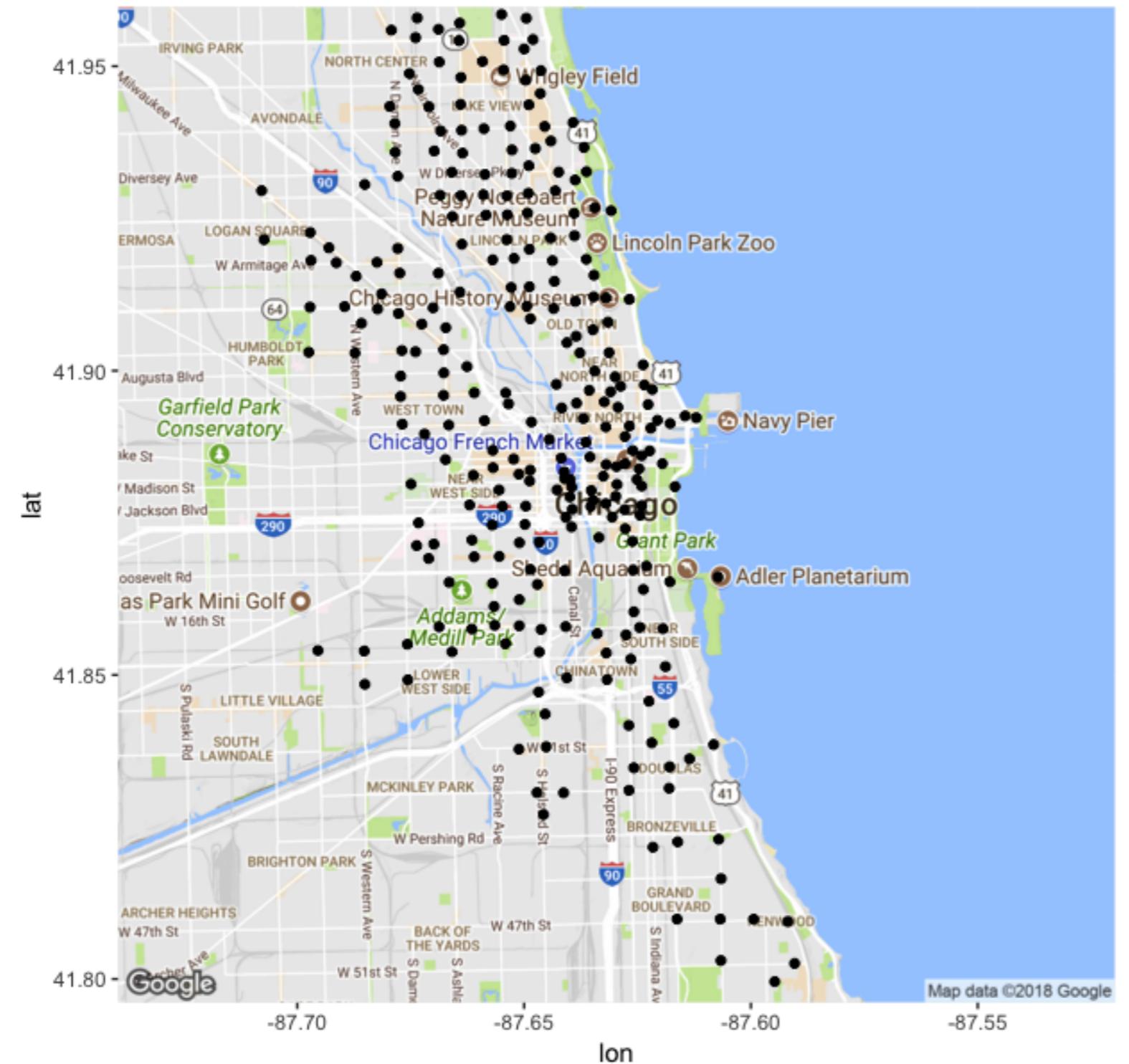
CASE STUDIES: NETWORK ANALYSIS IN R

Compare graph distance vs. geographic distance

CASE STUDIES: NETWORK ANALYSIS IN R



Edmund Hart
Instructor



Graph distance

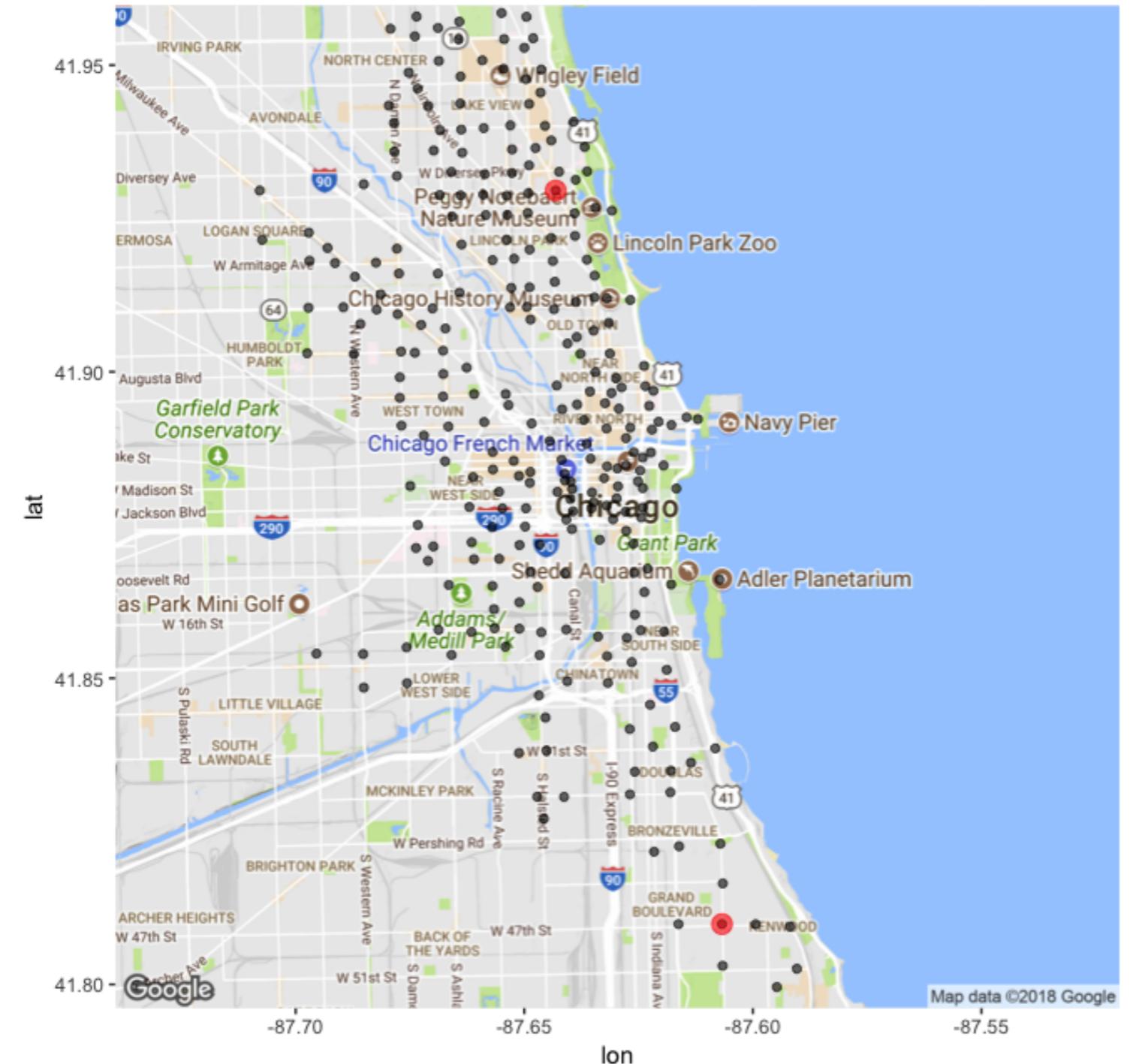
```
farthest_vertices(trip_g_simp)
```

```
$vertices  
+ 2/300 vertices, named, from 20dcfff:  
[1] 336 340
```

```
$distance  
[1] 5
```

```
get_diameter(trip_g_simp)
```

```
+ 4/300 vertices, named, from 20dcfff:  
[1] 336 267 76 340
```



Geographic distance

```
library(geosphere)
# Get the to stations coordinates
st_to <- bike_dat %>%
  filter(from_station_id == 336) %>%
  sample_n(1) %>%
  select(from_longitude, from_latitude)
# Get the from stations coordinates
st_from <- bike_dat %>%
  filter(from_station_id == 340) %>%
  sample_n(1) %>%
  select(from_longitude, from_latitude)
# find the geographic distance
farthest_dist <- distm(st_from, st_to, fun = distHaversine)
farthest_dist
```

```
[1, ] 13660.66
```

Geographic distance

```
bike_dist <- function(station_1, station_2, divy_bike_df){  
  st1 <- divy_bike_df %>%  
    filter(from_station_id == station_1) %>%  
    sample_n(1) %>%  
    select(from_longitude, from_latitude)  
  st2 <- divy_bike_df %>%  
    filter(from_station_id == station_2) %>%  
    sample_n(1) %>%  
    select(from_longitude, from_latitude)  
  
  farthest_dist <- distm(st1, st2, fun = distHaversine)  
  return(farthest_dist)  
}
```

Let's practice!

CASE STUDIES: NETWORK ANALYSIS IN R

Connectivity

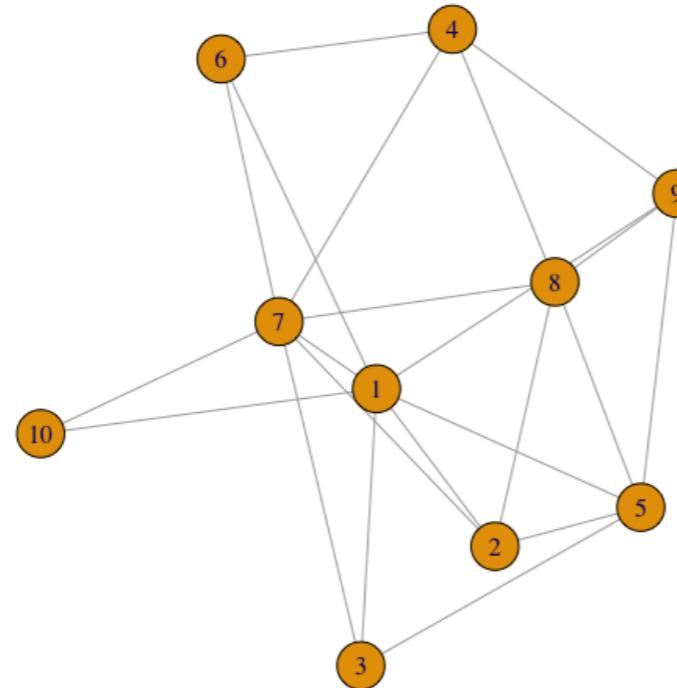
CASE STUDIES: NETWORK ANALYSIS IN R



Edmund Hart
Instructor

Measuring connectivity

```
rand_g <- erdos.renyi.game(10, 0.4, "gnp", directed = FALSE)  
plot(rand_g)
```



Measuring connectivity

```
rand_g <- erdos.renyi.game(10, 0.4, "gnp", directed = FALSE)  
vertex_connectivity(rand_g)
```

```
2
```

```
edge_connectivity(rand_g)
```

```
2
```

Minimum number of cuts

```
min_cut(rand_g, value.only = FALSE)
```

```
$value
[1] 2

$cut
+ 2/18 edges from 17a8fad:
[1] 10--7 10--1

$partition1
+ 1/10 vertex, from 17a8fad:
[1] 10

$partition2
+ 9/10 vertices, from 17a8fad:
[1] 1 2 3 4 5 6 7 8 9
```

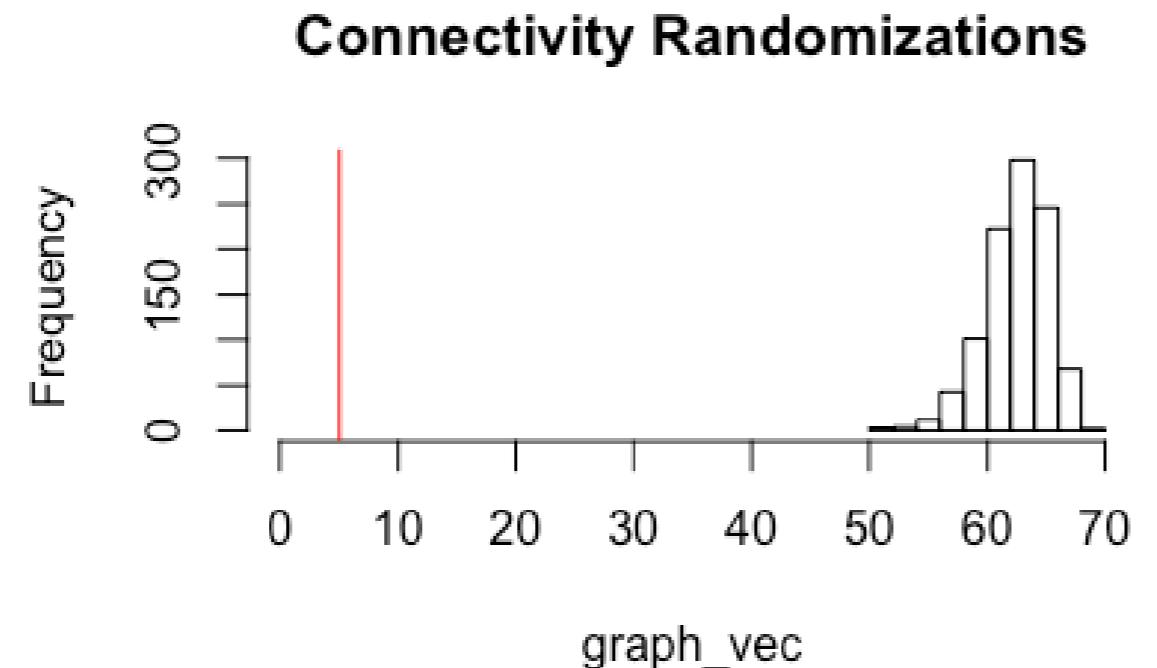
Connectivity randomizations

```
# Get parameters to simulate graph
nv <- gorder(trip_g_ud)
ed <- edge_density(trip_g_ud)

# Empty vector to store output
graph_vec <- rep(NA, 1000)
# Generate 1000 random graphs and find the edge connectivity
for(i in 1:1000) {
  w1 <- erdos.renyi.game(nv, ed, "gnp", directed = TRUE)
  graph_vec[i] <- edge_connectivity(w1)
}
```

Connectivity randomizations

```
# Find actual connectivity  
econn <- edge_connectivity(trip_g_ud)  
hist(graph_vec, xlim = c(0, 140))  
abline(v = edge_connectivity(trip_g_ud))
```



Let's practice!

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Other packages for plotting graphs

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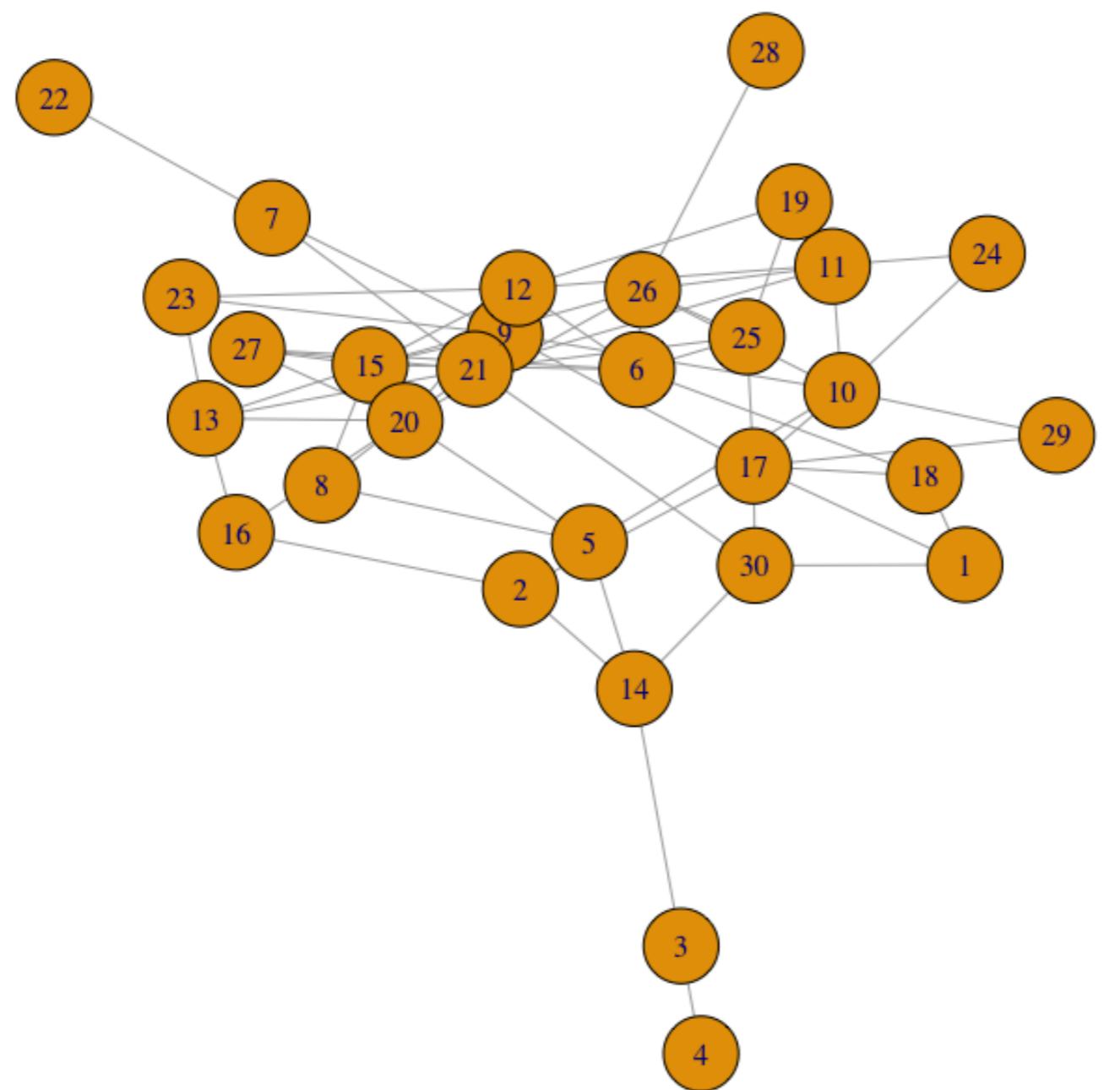
Instructor

Generating data to plot

```
library(ggnetwork)
library(igraph)
library(GGally)
library(intergraph)

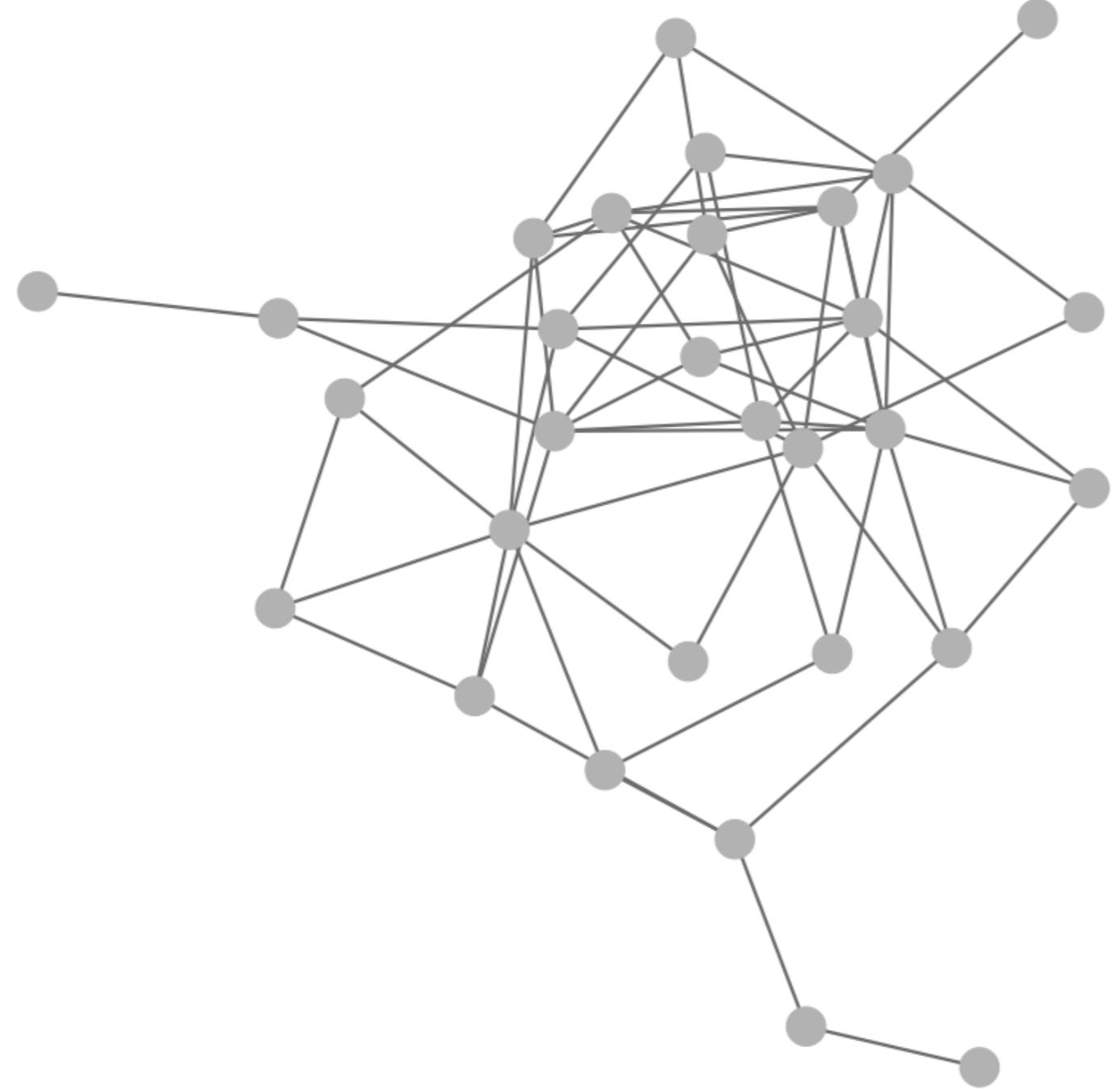
rand_g <- erdos.renyi.game(30, .15, "gnp", directed = F)
rand_g <- simplify(rand_g)

plot(rand_g)
```



Basic ggnet2

```
net <- asNetwork(rand_g)  
ggnet2(net)
```

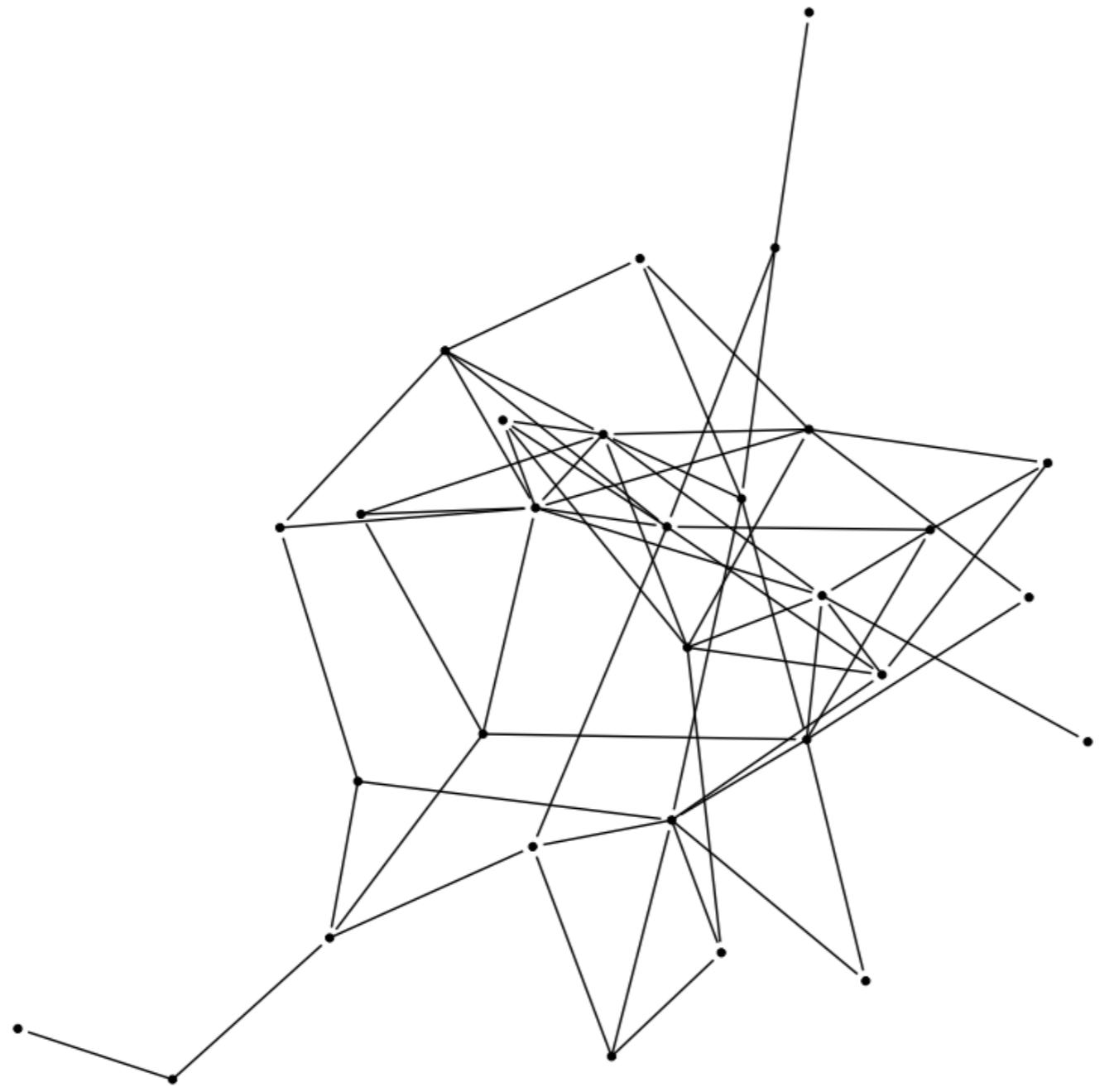


Basic ggnetwork

```
gn <- ggnetwork(rand_g)
g <- ggplot(gn, aes(x = x, y = y, xend = xend, yend = yend)) +
  geom_edges() +
  geom_nodes() +
  theme_blank()
head(gn)
```

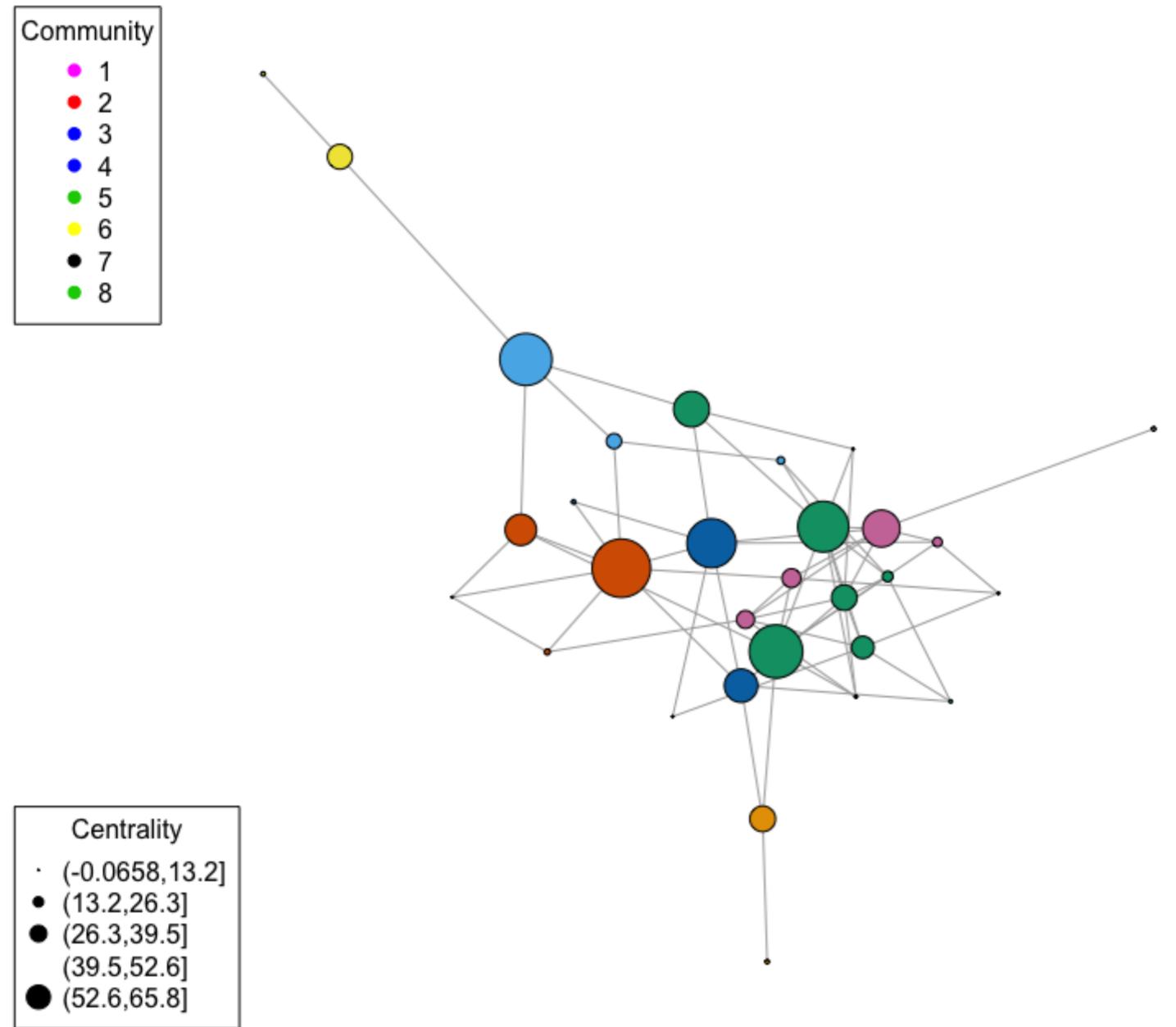
	x	y	na.x	vertex.names	xend	yend	na.y	
1	0.4729841	0.01697675	FALSE		1	0.4729841	0.01697675	NA
2	0.1883442	0.42284666	FALSE		2	0.1883442	0.42284666	NA
3	0.3485247	0.82865654	FALSE		3	0.3485247	0.82865654	NA
4	0.3905894	1.00000000	FALSE		4	0.3905894	1.00000000	NA

```
plot(g)
```



Plotting graphs with attributes

```
# Add attributes
V(rand_g)$cent <- betweenness(rand_g)
V(rand_g)$comm <- membership(cluster_walktrap(rand_g))
# Make plot
plot(rand_g, vertex.label = NA, margin = 0,
      vertex.color = V(rand_g)$comm,
      vertex.size = V(rand_g)$cent / 6)
# Add legend for community membership
legend('topleft', legend= sort(unique( V(rand_g)$comm)),
       col= sort(unique(V(rand_g)$comm)), pch = 19, title = "Community")
# Add cuts and then get quantiles for size legend
cc <- cut(V(rand_g)$cent, 5)
scaled <- quantile(V(rand_g)$cent, seq(0.3, 0.9, length = 5)) / 25
# Add size legend for centrality
legend('bottomleft', legend= levels(cc),
       pt.cex = scaled, pch = 19, title = "Centrality")
```



ggnet2 plot with attributes

```
net <- asNetwork(rand_g)

ggnet2(net,
       node.size = "cent",
       node.color = "comm",
       edge.size = 0.8,
       color.legend = "Community Membership",
       color.palette = "Spectral",
       edge.color = c("color", "gray88"),
       size.cut = TRUE,
       size.legend = "Centrality")
```

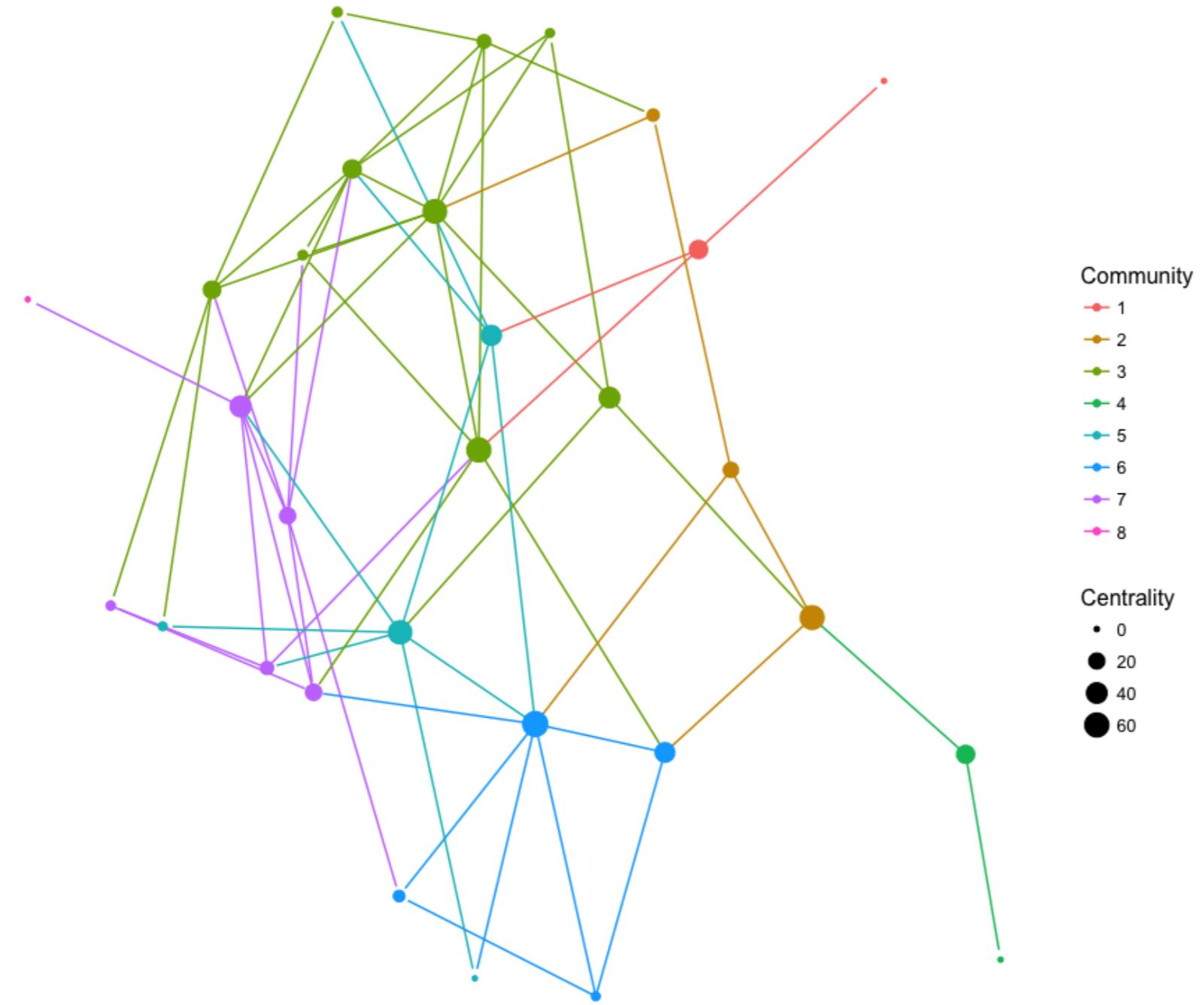


ggnetwork plot with attributes

```
gn <- ggnetwork(rand_g)

g <- ggplot(gn, aes(x = x, y = y, xend = xend, yend = yend)) +
  geom_edges(aes(color = as.factor(comm))) +
  geom_nodes(aes(color = as.factor(comm), size = cent)) +
  theme_blank() +
  guides(
    color = guide_legend(title = "Community"),
    size = guide_legend(title = "Centrality"))

plot(g)
```



Let's practice!

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Interactive visualizations

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Edmund Hart
Instructor

Generating some data

```
library(igraph)
library(ggnetwork)
library(ggiraph)
library(htmlwidgets)
library(networkD3)

# Create random graph
rand_g <- erdos.renyi.game(30, 0.12, "gnp", directed = FALSE)
rand_g <- simplify(rand_g)

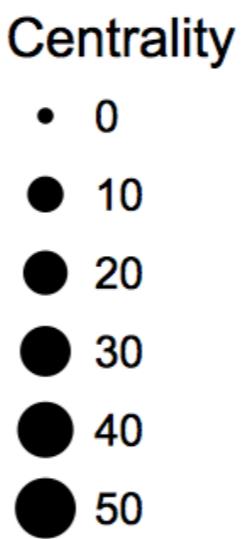
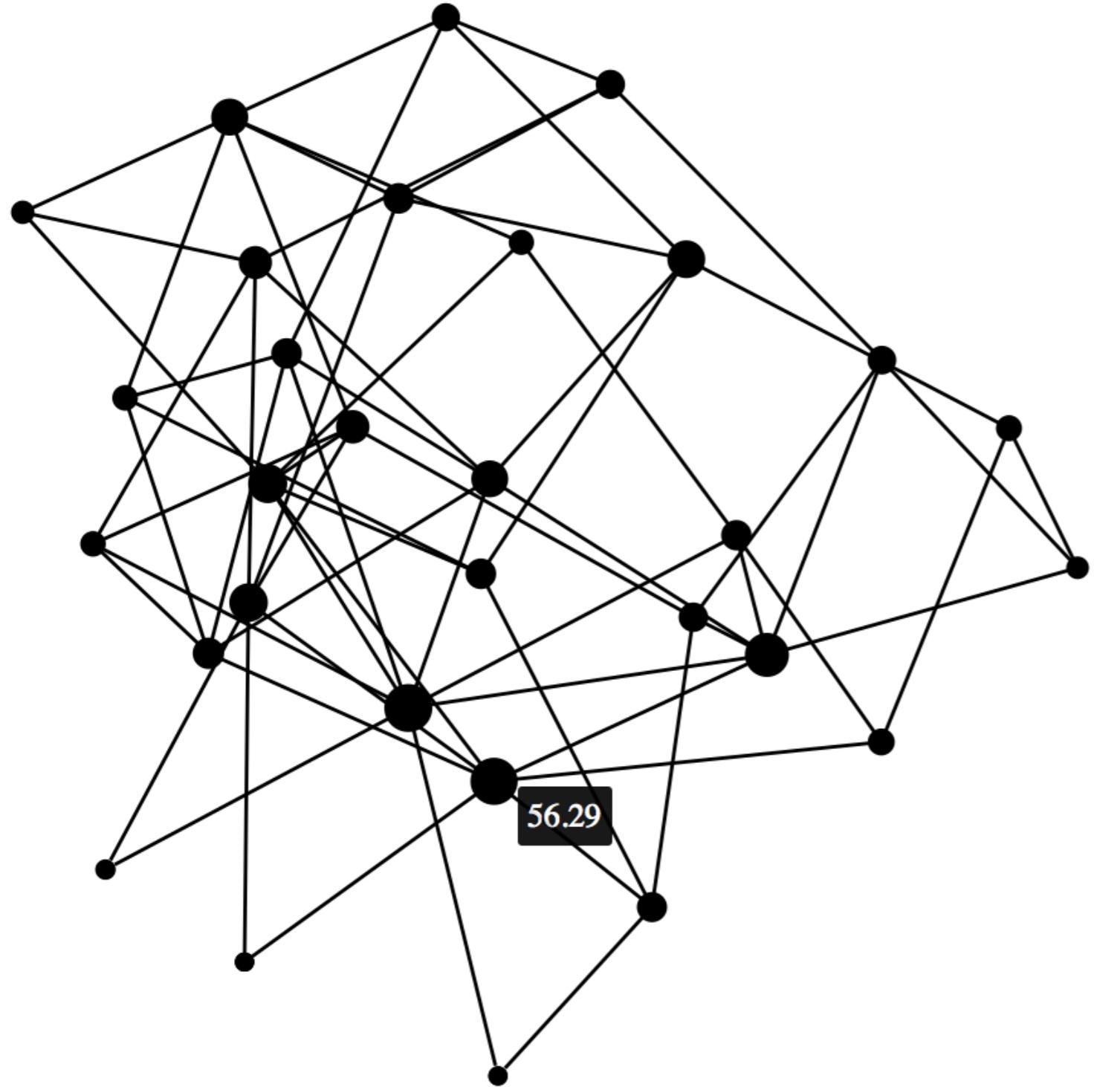
V(rand_g)$cent <- betweenness(rand_g)
```

Interactive plots with ggiraph

```
# Plot graph with ggplot2 and ggnetwork
g <- ggplot(ggnetwork(rand_g),
             aes(x = x, y = y, xend = xend, yend = yend)) +
  geom_edges(color = "black") +
  geom_nodes(aes(size = cent)) + theme_blank() +
  guides(size = guide_legend(title = "Centrality"))

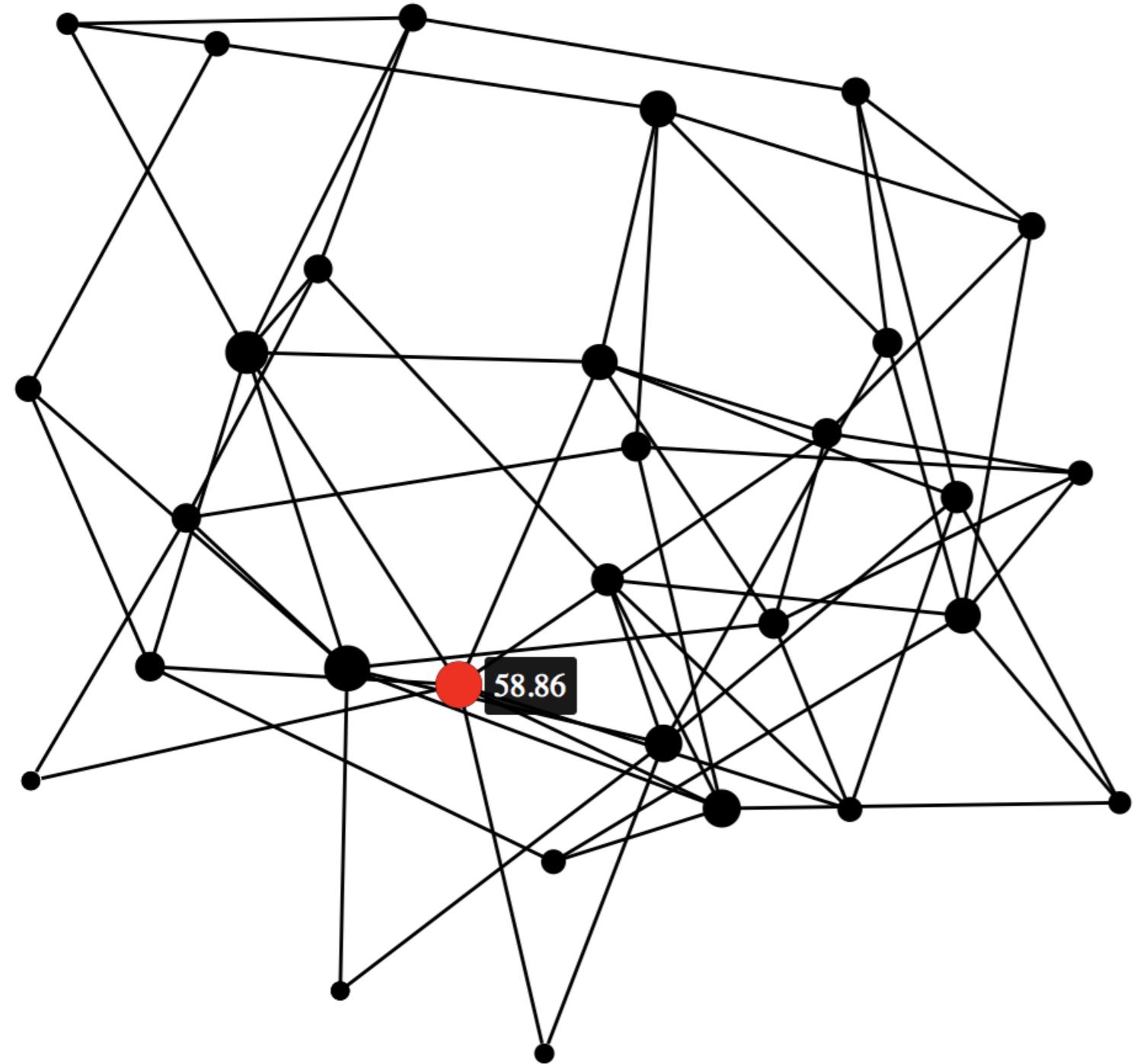
# Create ggiraph object
my_gg <- g + geom_point_interactive(aes(tooltip = round(cent, 2)),
                                      size = 2)

# Display ggiraph object
ggiraph(code = print(my_gg))
```



ggiraph customization

```
my_gg <- g + geom_point_interactive(aes(tooltip = round(cent, 2),  
                                         data_id = round(cent, 2)),  
                                         size = 2)  
  
hover_css = "cursor:pointer;fill:red;stroke:red;r:5pt"  
  
ggiraph(code = print(my_gg),  
        hover_css = hover_css,  
        tooltip_offx = 10,  
        tooltip_offy = -10)
```

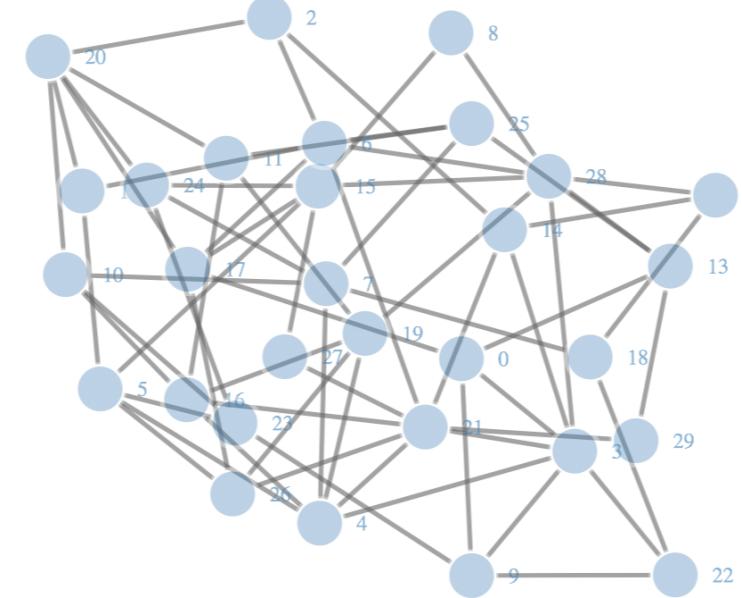


cent

- 0
- 10
- 20
- 30
- 40
- 50

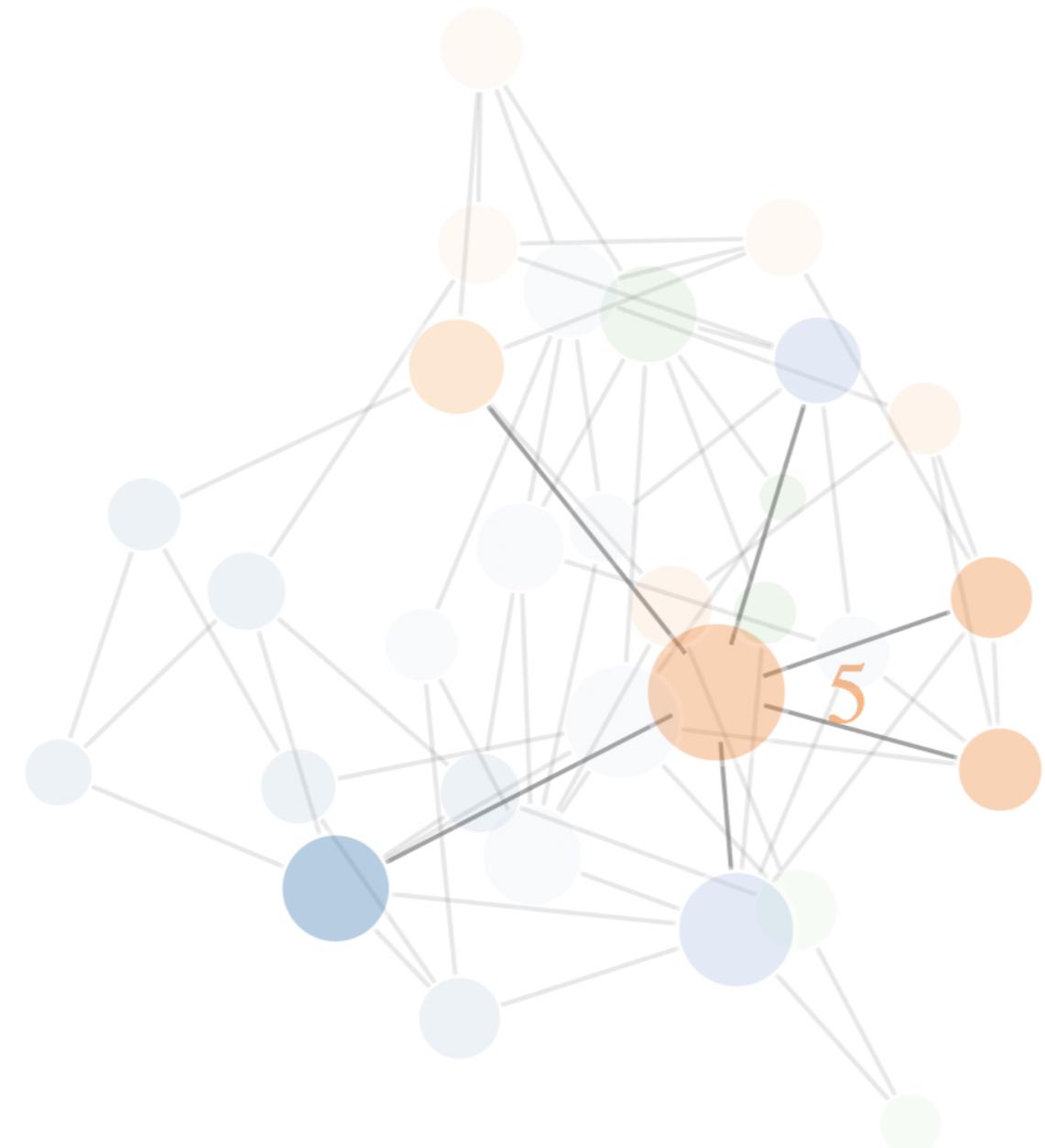
Plotting with networkD3

```
# Convert the igraph object  
nd3 <- igraph_to_networkD3(rand_g)  
  
# Create a simple network  
simpleNetwork(nd3$links)
```



More complex networkD3

```
# Add attributes, group is community, and cent is centrality.  
nd3$nodes$group = V(rand_g)$comm  
nd3$nodes$cent = V(rand_g)$cent  
  
# Plot the graph  
forceNetwork(Links = nd3$links,  
             Nodes = nd3$nodes,  
             Source = 'source',  
             Target = 'target',  
             NodeID = 'name',  
             Group = 'group',  
             Nodesize = 'cent',  
             legend = T,  
             fontSize = 20)
```



Let's practice!

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Alternative visualizations

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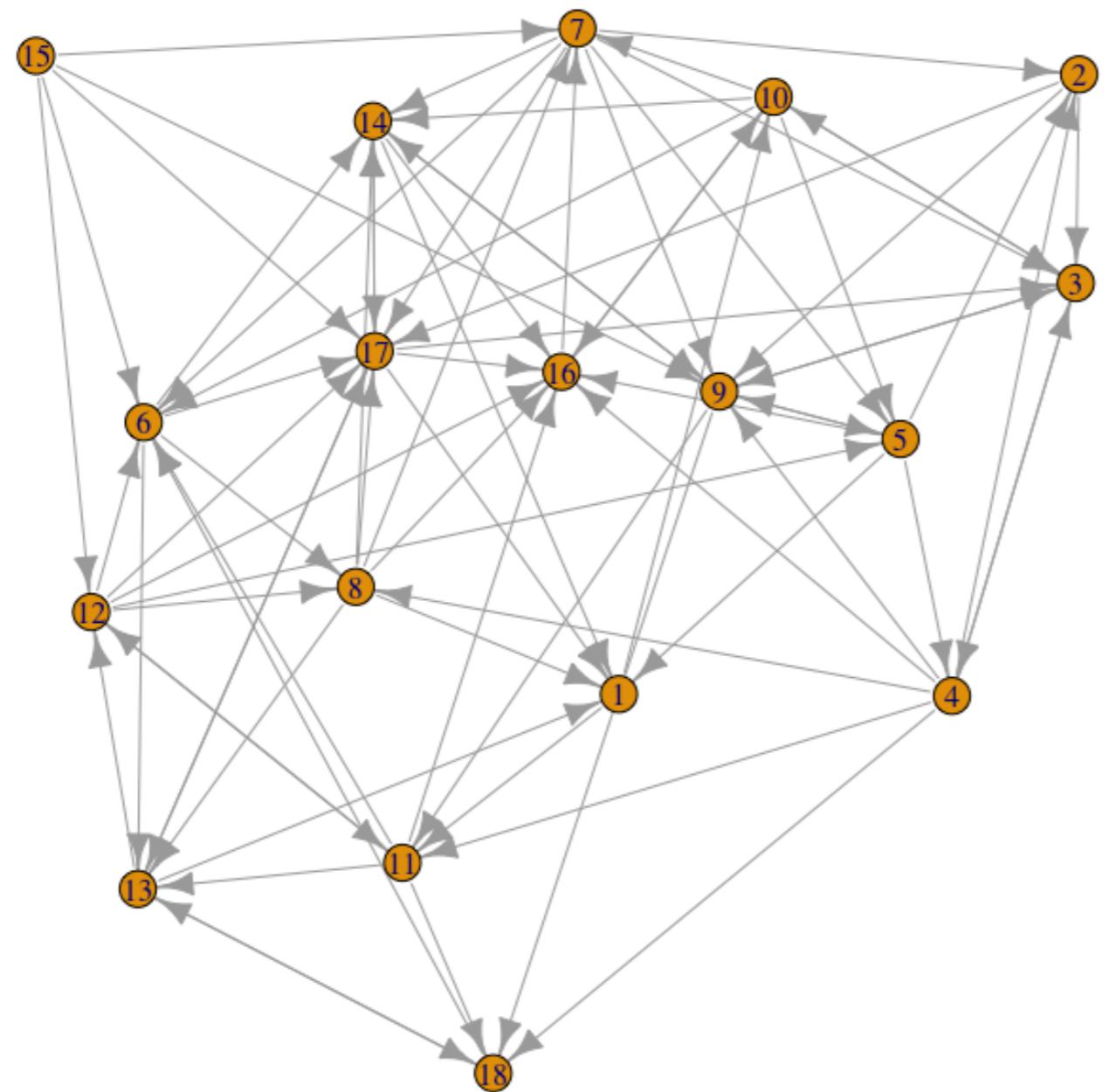
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Instructor

Introduction to hive plots

```
library(HiveR)
library(igraph)

# Create random graph
rand_g <- erdos.renyi.game(18, 0.3, "gnp", directed = TRUE)

# Plot random graph
plot(rand_g, vertex.size = 7)
```



Introduction to hive plots

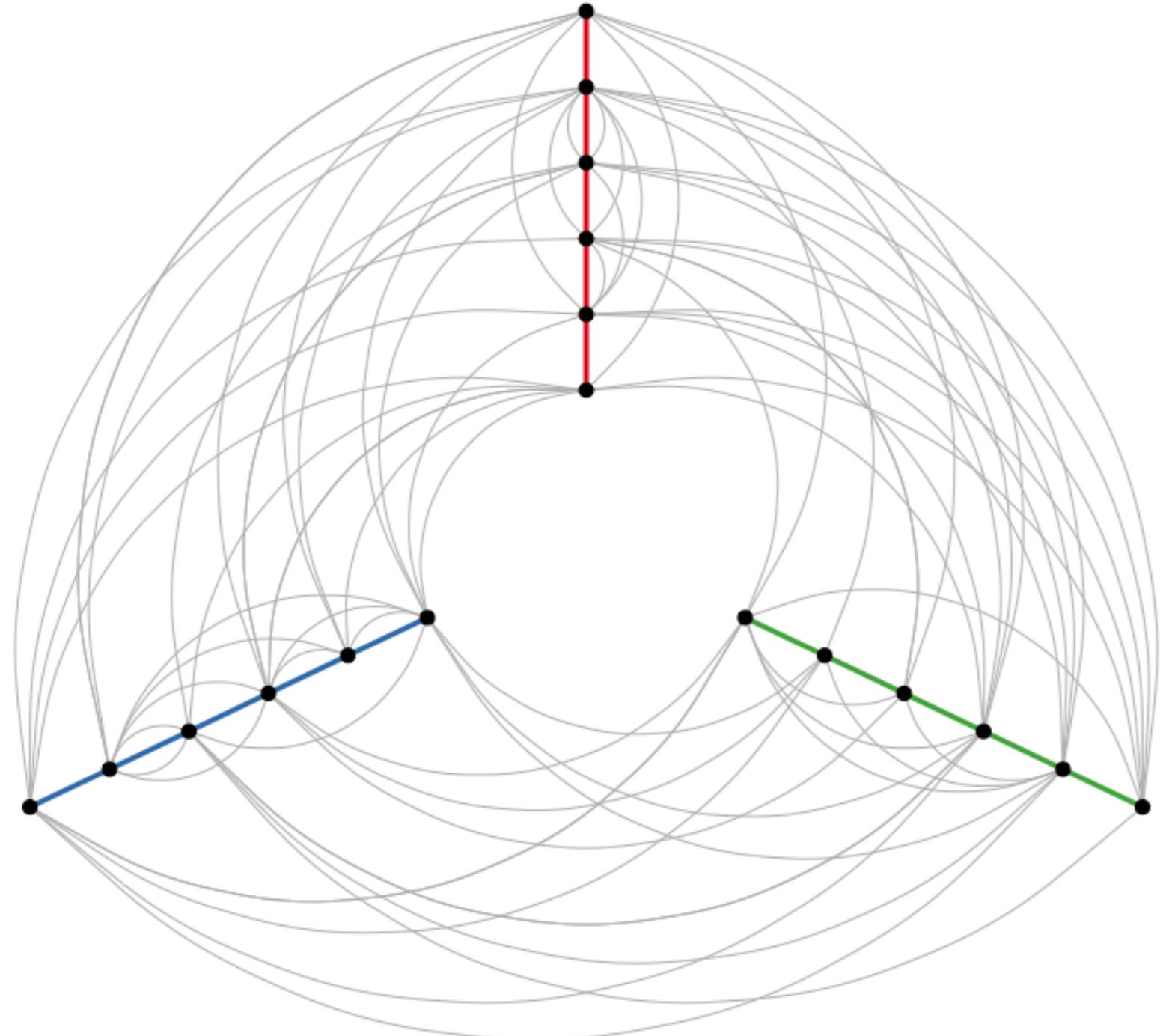
```
# Convert to dataframe for hive plots and add weights
rand_g_df <- as.data.frame(get.edgelist(rand_g))
rand_g_df$weight <- 1
# Convert to hive object
rand_hive <- edge2HPD(edge_df = rand_g_df)
# Set the axis and the radius of each node
rand_hive$nodes$axis <- sort(rep(1:3, 6))
rand_hive$nodes$radius <- as.double(rep(1:6, 3))
```

Introduction to hive plots

```
# See how nodes are modified  
rand_hive$nodes
```

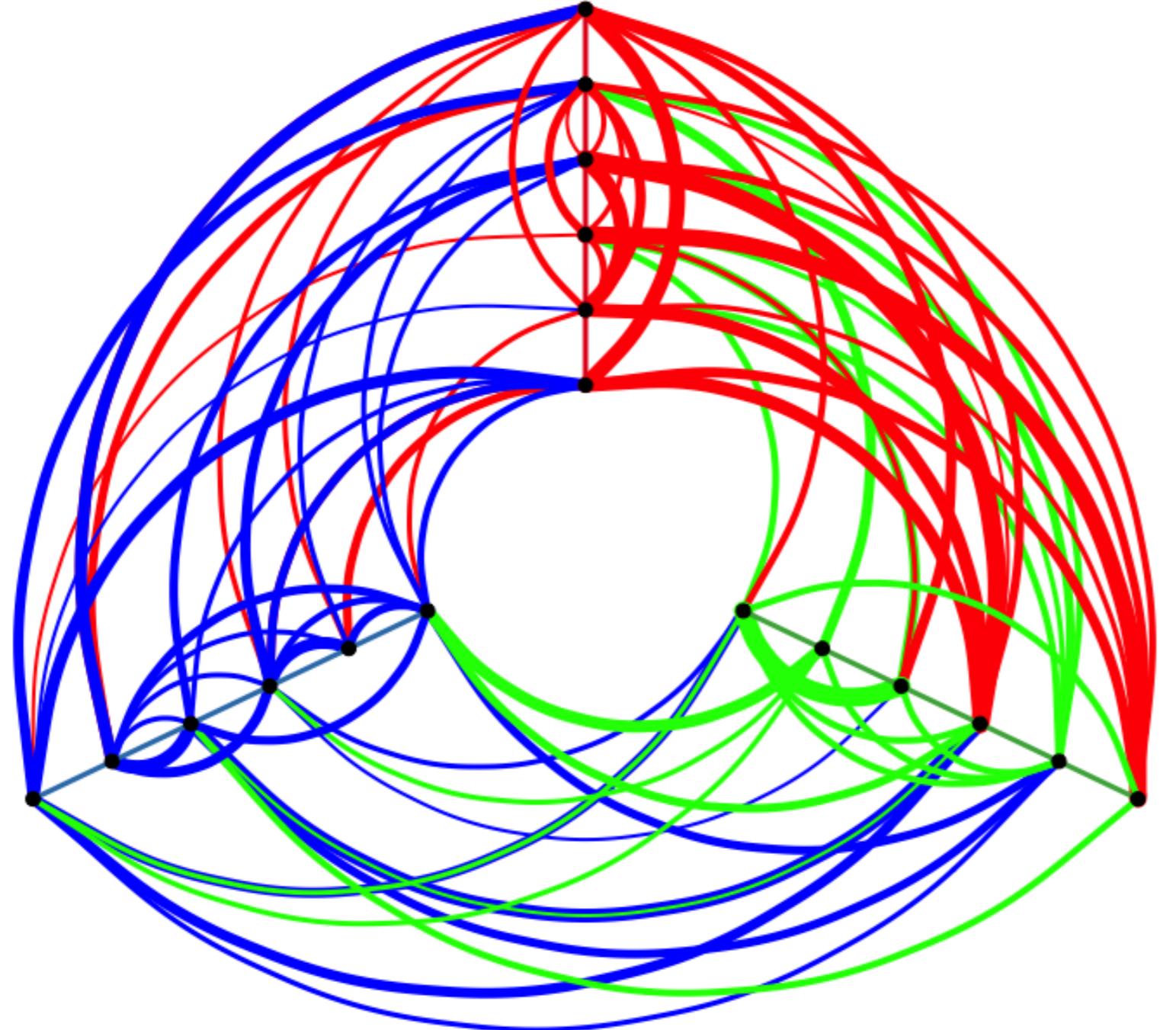
```
id lab axis radius size color  
1 2 1 1 1 black  
2 8 1 2 1 black  
3 9 1 3 1 black  
4 3 1 4 1 black  
5 4 1 5 1 black  
6 7 1 6 1 black  
7 11 2 1 1 black  
8 14 2 2 1 black  
9 18 2 3 1 black
```

```
# See hive plot  
plotHive(rand_hive, method = "abs", bkgnd = "white")
```



Modifying hive plots

```
# Setting location of each node
rand_hive$nodes$axis <- sort(rep(1:3, 6))
rand_hive$nodes$radius <- as.double(rep(1:6, 3))
# Add weights to each edge
rand_hive$edges$weight <- as.double(
  rpois(length(rand_hive$edges$weight), 5)
)
# Add color based on edge origination
rand_hive$edges$color[rand_hive$edges$id1 %in% 1:6] <- 'red'
rand_hive$edges$color[rand_hive$edges$id1 %in% 7:12] <- 'blue'
rand_hive$edges$color[rand_hive$edges$id1 %in% 13:18] <- 'green'
# Plot
plotHive(rand_hive, method = "abs", bkgnd = "white")
```

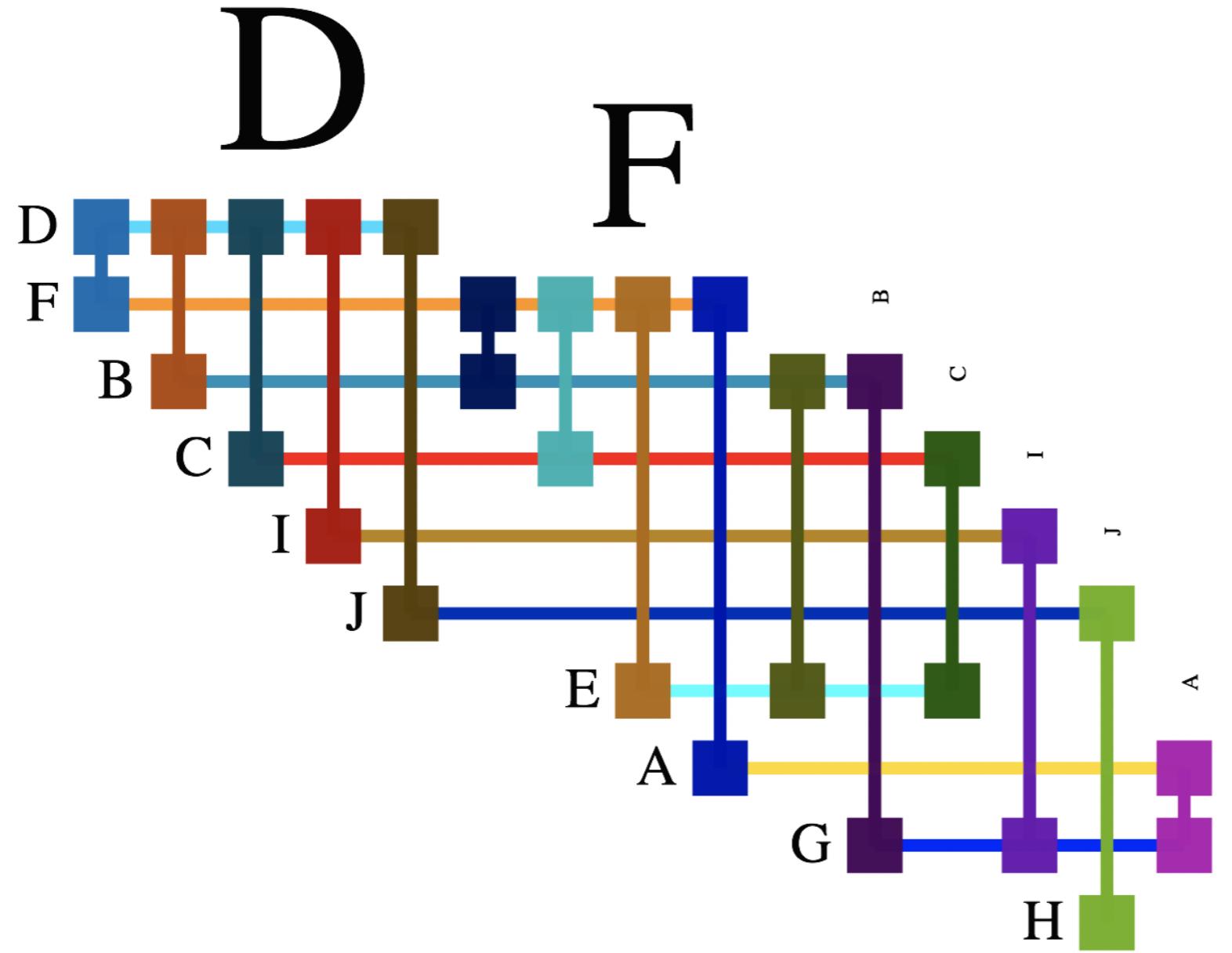


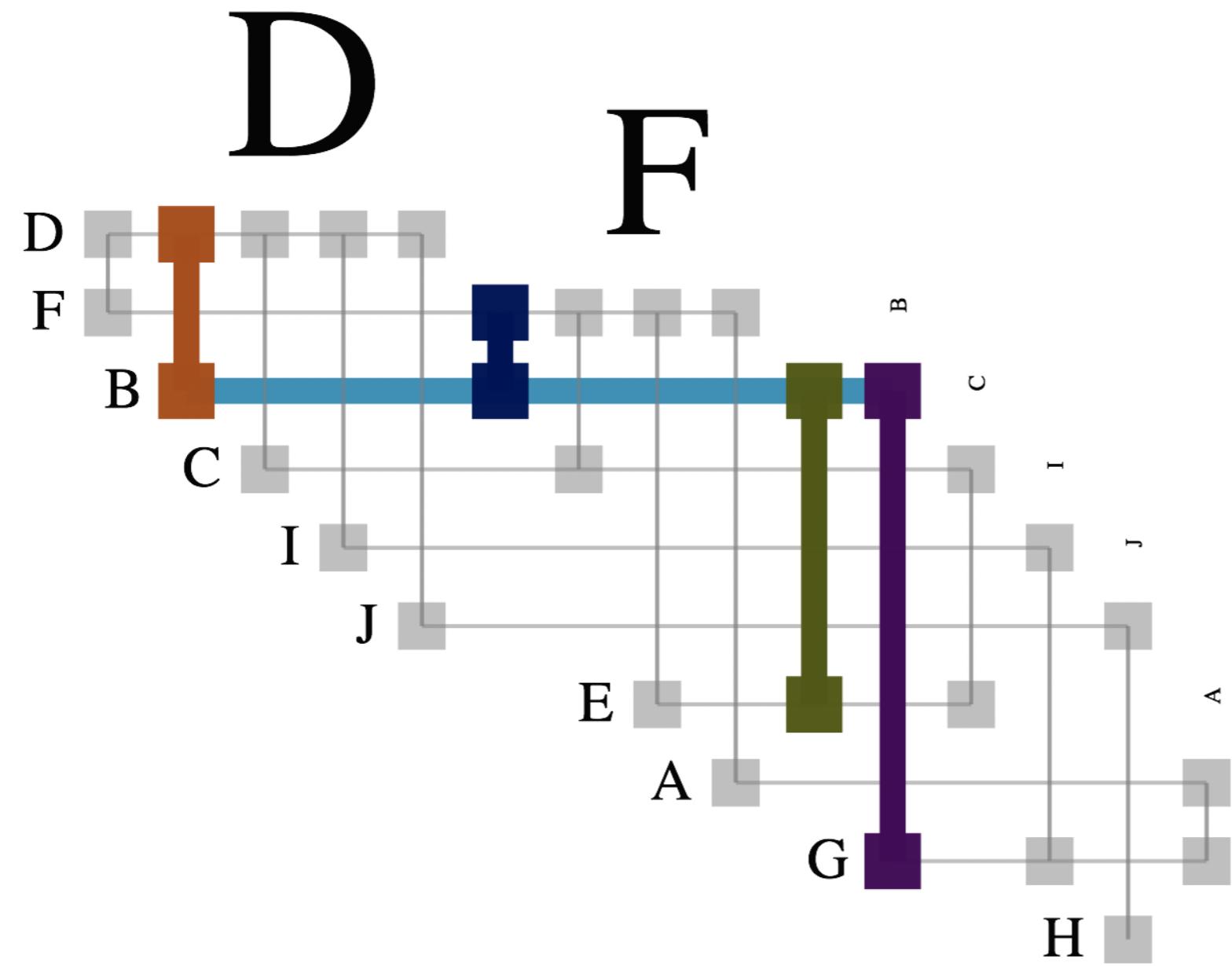
Biofabric plots

```
# Create random graph
rand_g <- erdos.renyi.game(10, 0.3, "gnp", directed = FALSE)
rand_g <- simplify(rand_g)

# Add names to vertices
V(rand_g)$name <- LETTERS[1:length(V(rand_g))]

# Create biofabric plot
biofbc <- bioFabric(rand_g)
bioFabric_htmlwidget(biofbc)
```





Let's practice!

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