

* Array of Arrays (2D Arrays) :

```
684 const friends1 = ["Amit", "Rohit", "Anoop"];
685 const friends2 = ["Vishal", "Saurabh", "Piyush", "Sujata"];
686 const friends3 = ["Akram", "JavaScript"];
687
688 const allFriends = [friends1, friends2, friends3];
689
690 console.log(allFriends);
691 console.log(allFriends[0]);
692 console.log(allFriends[1]);
693 console.log(allFriends[2]);
```

2D Matrix

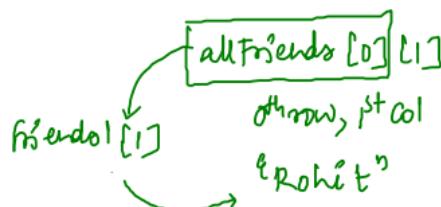
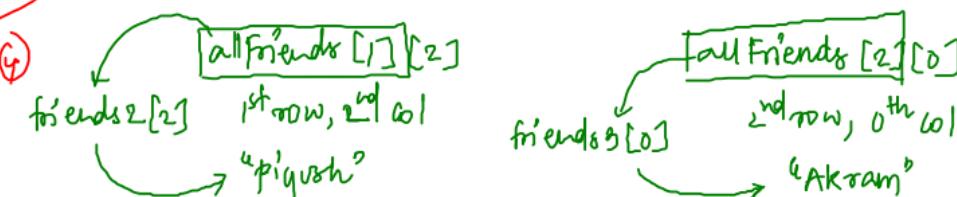
rows ↓

0	1	2	3
0	"Amit"	"Rohit"	"Anoop"
1	"Vishal"	"Saurabh"	"Piyush"
2	"Akram"	"JavaScript"	"Sujata"

← Columns →

```
[ 0 { "Amit", "Rohit", "Anoop" }, →③
    0   1   2
  1 { "vishal", "saurabh", "piyush", "sujata" }, →④
    0   1   2   3
  2 [ "Akram", "JavaScript" ] →②
]

```



* If the smaller arrays or the rows do not have equal length they are called as "Jagged Arrays".

allFriends

=

0	1	2	3
"Amit"	"Rohit"	"Anoop"	
"Vishal"	"Saurabh"	"Piyush"	"Sujata"
"Akram"	"JavaScript"		

* no. of rows

⇒ no. of smaller arrays

allFriends = [[3], [4], [2]].length

* no. of cols

→ no. of ele's in a smaller array
(each row)

No. of rows = 3 = allFriends.length

No. of cols ⇒ row-0 → 3 = allFriends[0].length = ["Amit", "Rohit", "Anoop"].length

row-1 → 4 = allFriends[1].length

row-2 → 2 = allFriends[2].length

Given a $n \times n$ matrix, print it Accordingly

↓ ↓
rows cols

if $n = 3$

	0	1	2
0	1	2	3
1	4	5	6
2	7	8	9

mat =

	0	1	2	3
0	1	2	3	4
1	1	2	3	4
2	1	2	3	4
3	1	2	3	4

op:

1	2	3
4	5	6
7	8	9

op:

1	2	3	4
1	2	3	4
1	2	3	4
1	2	3	4

(no. of cols in)
row 0

```
for(let i=0; i<mat[0].length; i++) {
    process.stdout.write(mat[0][i] + ' ');
}
```

(no. of cols in)
row 1

```
for(let i=0; i<mat[1].length; i++) {
    process.stdout.write(mat[1][i] + ' ');
}
```

* i is being used to refer the column number.

- ① $i=0 \rightarrow \text{mat}[0][0]$
- ② $i=1 \rightarrow \text{mat}[0][1]$
- ③ $i=2 \rightarrow \text{mat}[0][2]$
- ④ $i=3 \times$

```

725 const rows = mat.length;
726 // as the no.of cols are same for every row
727 const cols = mat[0].length;
728
729 // go to every row
730 for (let r = 0; r < rows; r++) {
    // iterate on cols of that row
    // when in case of jagged arrays (no.of cols in each row diff)
    // const cols = mat[r].length;
    for (let c = 0; c < cols; c++) {
        process.stdout.write(mat[r][c] + " ");
    }
    console.log();
}

```

mat =

	0	1	2
0	1	2	3
1	4	5	6
2	7	8	9

3x3

$$\begin{aligned}
 \text{rows} &= [\underbrace{[1, 2, 3]}_0, \underbrace{[4, 5, 6]}_1, \underbrace{[7, 8, 9]}_2] \cdot \text{length} \\
 &= 3
 \end{aligned}$$

$$\text{cols} = \underbrace{[1, 2, 3]}_{0 \ 1 \ 2} \cdot \text{length} = 3 \quad \textcircled{2} \quad r = 1$$

$$\textcircled{1} \quad r = 0$$

$$\begin{aligned}
 \rightarrow c = 0 &\rightarrow \text{mat}[0][0] \rightarrow 1 \\
 \rightarrow c = 1 &\rightarrow \text{mat}[0][1] \rightarrow 2 \\
 \rightarrow c = 2 &\rightarrow \text{mat}[0][2] \rightarrow 3 \\
 \rightarrow \cancel{c = 3} &\quad (3 < 3)
 \end{aligned}$$

$$\begin{aligned}
 \rightarrow c = 0 &\rightarrow \text{mat}[1][0] \rightarrow 4 \\
 \rightarrow c = 1 &\rightarrow \text{mat}[1][1] \rightarrow 5 \\
 \rightarrow c = 2 &\rightarrow \text{mat}[1][2] \rightarrow 6 \\
 \rightarrow \cancel{c = 3} &\quad (3 < 3)
 \end{aligned}$$

$$\textcircled{3} \quad r = 2$$

$$\begin{aligned}
 \rightarrow c = 0 &\rightarrow \text{mat}[2][0] \rightarrow 7 \\
 \rightarrow c = 1 &\rightarrow \text{mat}[2][1] \rightarrow 8 \\
 \rightarrow c = 2 &\rightarrow \text{mat}[2][2] \rightarrow 9 \\
 \rightarrow \cancel{c = 3} &\quad (3 < 3)
 \end{aligned}$$

$$\textcircled{4} \quad \cancel{c = 3} \quad (3 < 3)$$

Create $n \times n$ matrix in the following pattern :

$$\text{If } n = 3$$

$\text{mat} =$	0	1	2
0	1	2	3
1	1	2	3
2	1	2	3

if $n = 4$

$mat =$	0	1	2	3
0	1	2	3	4
1	1	2	3	4
2	1	2	3	4
3	1	2	3	4

to Create a smaller array
ie; a row

2. add it to the bigger array i.e; matrix

const mat = [];

```
const arr = []
```

```
for(let i=0; i<3; i++) {
```

arr.push(i+1);

3

$$avr1 \rightarrow [i=0] [i=1] [i=2] [1, 2, 9]$$

mat.push(cart);

`mat → [] [[1, 2, 9]]`

```
const arr2 = []
```

```
for( let i=0; i<3 ; i++ ) {
```

arr2.push(i+1);

3

$\text{arr2} \rightarrow$ ~~i=0 i=1 i=2~~ [1, 2, 3]

mat.push(ant2);

$$\text{mat} \rightarrow \left[\begin{array}{c} [1, 2, 9] \\ [1, 2, 9] \end{array} \right] \rightarrow [[1, 2, 9], [1, 2, 9]]$$

$\Rightarrow n = 3$

```

13 v function createMatrix(n) {
14   const mat = [];
15   for (let r = 0; r < n; r++) {
16     const arr = [];
17     for (let c = 0; c < n; c++) {
18       arr.push(c + 1);
19     }
20     mat.push(arr);
21   }
22   return mat;
23 }
```

③ $r = 2$

$\rightarrow \text{arr} = []$

$\rightarrow c = 0 \rightarrow [] \rightarrow [1]$

$\rightarrow c = 1 \rightarrow [1] \rightarrow [1, 2]$

$\rightarrow c = 2 \rightarrow [1, 2] \rightarrow [1, 2, 3]$

$\rightarrow \cancel{\times} 3 \quad (3 < 3)$

$\rightarrow \cancel{[1, 2, 3], [1, 2, 3]}$

\downarrow

$\text{mat} = [[1, 2, 3], [1, 2, 3], [1, 2, 3]]$

$\text{mat} = []$

① $r = 0$

$\rightarrow \text{arr} = []$

$\rightarrow c = 0 \rightarrow [] \rightarrow [1]$

$\rightarrow c = 1 \rightarrow [1] \rightarrow [1, 2]$

$\rightarrow c = 2 \rightarrow [1, 2] \rightarrow [1, 2, 3]$

$\rightarrow \cancel{\times} 3 \quad (3 < 3)$

$\rightarrow [] \rightarrow [[1, 2, 3]]$

② $r = 1$

$\rightarrow \text{arr} = []$

$\rightarrow c = 0 \rightarrow [] \rightarrow [1]$

$\rightarrow c = 1 \rightarrow [1] \rightarrow [1, 2]$

$\rightarrow c = 2 \rightarrow [1, 2] \rightarrow [1, 2, 3]$

$\rightarrow \cancel{\times} 3 \quad (3 < 3)$

$\rightarrow \cancel{[[1, 2, 3]]}$

\downarrow

$[[1, 2, 3], [1, 2, 3]]$

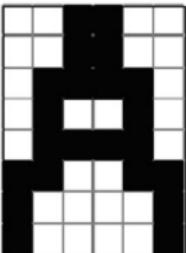
④ $\cancel{\times} 3 \quad (3 < 3)$

	0	1	2
0	1	2	3
1	1	2	3
2	1	2	3

★ Some use layers:



(a)



(b)

0	0	1	1	0	0
0	0	1	1	0	0
0	1	1	1	1	0
0	1	0	0	1	0
0	1	1	1	1	0
1	1	0	0	1	1
1	0	0	0	0	1
1	0	0	0	0	1

(c)

→ matrix can be used in representing images



→ can be used to
design a chess game

9:25 PM
— 9:40 PM
BREAK

Q: print Matrix Column wise :

	0	1	2
0	1	2	3
1	4	5	6
2	7	8	9

$N \times M \rightarrow 3 \times 3$

op: 1 4 7 2 5 8 3 6 9

* go to each column and iterate on row elements

$\text{mat}[0][0] \rightarrow 1$
 $\text{mat}[1][0] \rightarrow 4$ } Col = 0
 $\text{mat}[2][0] \rightarrow 7$ } Row = 0 $\rightarrow 2$
 $\text{mat}[0][1] \rightarrow 2$ } Col = 1
 $\text{mat}[1][1] \rightarrow 5$ } Row = 0 $\rightarrow 2$
 $\text{mat}[2][1] \rightarrow 8$

```
970 function printMatrixColumnwise(mat, n, m) {  
971     // Write code here and print output  
972  
973     // go to every column  
974     for (let c = 0; c < m; c++) {  
975         // iterate on rows  
976         for (let r = 0; r < n; r++) {  
977             process.stdout.write(mat[r][c] + " ");  
978         }  
979     }  
980 }
```

① $c = 0$

$\rightarrow r = 0 \rightarrow \text{mat}[0][0] \rightarrow 1$
 $\rightarrow r = 1 \rightarrow \text{mat}[1][0] \rightarrow 4$
 $\rightarrow r = 2 \rightarrow \text{mat}[2][0] \rightarrow 7$

② $c = 1$

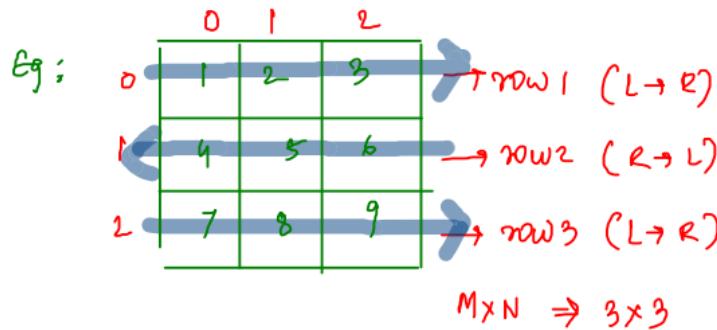
$\rightarrow r = 0 \rightarrow \text{mat}[0][1] \rightarrow 2$
 $\rightarrow r = 1 \rightarrow \text{mat}[1][1] \rightarrow 5$
 $\rightarrow r = 2 \rightarrow \text{mat}[2][1] \rightarrow 8$

③ $c = 2$

$\rightarrow r = 0 \rightarrow \text{mat}[0][2] \rightarrow 3$
 $\rightarrow r = 1 \rightarrow \text{mat}[1][2] \rightarrow 6$
 $\rightarrow r = 2 \rightarrow \text{mat}[2][2] \rightarrow 9$

Q: Alternate Matrix Traversal :

* odd row \rightarrow print L to R
even row \rightarrow print R to L



Op: 1 2 3 6 5 4 7 8 9

① $r = 0$

$r \% 2 == 0$ (even)

print L \rightarrow R

$\rightarrow c = 0 \rightarrow mat[0][0] \rightarrow 1$

$\rightarrow c = 1 \rightarrow mat[0][1] \rightarrow 2$

$\rightarrow c = 2 \rightarrow mat[0][2] \rightarrow 3$

② $r = 1$

$r \% 2 == 0$ (odd)

print R \rightarrow L

$\rightarrow c = 2 \rightarrow mat[1][2] \rightarrow 6$

$\rightarrow c = 1 \rightarrow mat[1][1] \rightarrow 5$

$\rightarrow c = 0 \rightarrow mat[1][0] \rightarrow 4$

rowIdx(r) = even ($L \rightarrow R$)
= odd ($R \rightarrow L$)

rowIdx(r) → rows
cols → cols

```

984 function printElementsAlternately(mat, m, n) {
985   // Write code here and print output
986   for (let r = 0; r < m; r++) {
987     if (r % 2 == 0) {
988       for (let c = 0; c < n; c++) {
989         process.stdout.write(mat[r][c] + " ");
990       }
991     } else {
992       for (let c = n - 1; c >= 0; c--) {
993         process.stdout.write(mat[r][c] + " ");
994       }
995     }
996   }
997 }
```

Q: Transpose of Matrix :

	0	1	2	3	4
0	1	2	3	4	5
1	6	7	8	9	10
2	11	12	13	14	15
3	16	17	18	19	20
4	21	22	23	24	25

	0	1	2	3	4
0	1	6	11	16	21
1	2	7	12	17	22
2	3	8	13	18	23
3	4	9	14	19	24
4	5	10	15	20	25

rows \leftrightarrow cols

\Rightarrow 2 concepts \rightarrow iterating colwise as seen in a previous problem
 \Rightarrow creating matrix that we had in discussion

```

1001 function matrixTranspose(mat, n) {
1002     //Write your code here
1003     const transMat = [];
1004     for (let c = 0; c < n; c++) {
1005         const arr = [];
1006         for (let r = 0; r < n; r++) {
1007             arr.push(mat[r][c]);
1008         }
1009         transMat.push(arr);
1010     }
1011
1012     return transMat;
1013 }
```

	0	1	2
0	1	2	3
1	4	5	6
2	7	8	9

③ $c = 2$
 $arr = []$
 $\rightarrow r = 0 \rightarrow [3]$
 $\rightarrow r = 1 \rightarrow [3, 6]$
 $\rightarrow r = 2 \rightarrow [3, 6, 9]$
 $\rightarrow transMat = [\underline{[1, 4, 7]}, \underline{[2, 5, 8]}]$
 $[1, 4, 7], [2, 5, 8], [3, 6, 9]]$

1	4	7
2	5	8
3	6	9

① $c = 0$
 $arr = []$
 $\rightarrow r = 0 \rightarrow [1]$
 $\rightarrow r = 1 \rightarrow [1, 4]$
 $\rightarrow r = 2 \rightarrow [1, 4, 7]$
 $\rightarrow transMat = [[1, 4, 7]]$

② $c = 1$
 $arr = []$
 $\rightarrow r = 0 \rightarrow [2]$
 $\rightarrow r = 1 \rightarrow [2, 5]$
 $\rightarrow r = 2 \rightarrow [2, 5, 8]$
 $\rightarrow transMat = [\underline{[1, 4, 7]}, [1, 4, 7], [2, 5, 8]]$

Improve SC: $O(N^2) \rightarrow O(1)$ [Inplace]:

	0	1	2	3	4
0	1	2	3	4	5
1	6	7	8	9	10
2	11	12	13	14	15
3	16	17	18	19	20
4	21	22	23	24	25

	0	1	2	3	4
0	1	6	11	16	21
1	2	7	12	17	22
2	3	8	13	18	23
3	4	9	14	19	24
4	5	10	15	20	25

$$[r, c] \leftrightarrow [c, r]$$

$$\boxed{\text{mat}[1][0] \leftrightarrow \text{mat}[0][1]}$$

$$\text{mat}[2][0] \leftrightarrow \text{mat}[0][2]$$

$$\text{mat}[3][0] \leftrightarrow \text{mat}[0][3]$$

$$\text{mat}[4][0] \leftrightarrow \text{mat}[0][4]$$

$$\text{mat}[2][1] \leftrightarrow \text{mat}[1][2]$$

$$\text{mat}[3][1] \leftrightarrow \text{mat}[1][3]$$

$$\text{mat}[4][1] \leftrightarrow \text{mat}[1][4]$$

```

for(let r = 0; r < n; r++) {
    for(let c = 0; c < n; c++) {
        swap([mat[r][c], mat[c][r]]);
    }
}
    
```

⇒ This fails due to double swaps

① $r = 0$

$\rightarrow c = 0 \rightarrow \text{swap}(\text{mat}[0][0], \text{mat}[0][0])$

$\rightarrow c = 1 \rightarrow \boxed{\text{swap}(\text{mat}[0][1], \text{mat}[1][0])}$

$\rightarrow c = 2 \rightarrow \text{swap}(\text{mat}[0][2], \text{mat}[2][0])$

$\rightarrow c = 3 \rightarrow \text{swap}(\text{mat}[0][3], \text{mat}[3][0])$

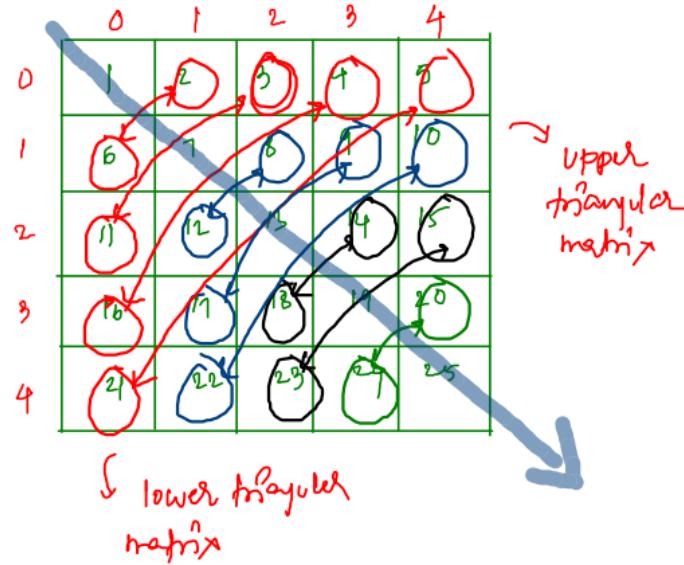
$\rightarrow c = 4 \rightarrow \text{swap}(\text{mat}[0][4], \text{mat}[4][0])$

double times
swap

② $r = 1$

$\rightarrow c = 0 \rightarrow \boxed{\text{swap}(\text{mat}[1][0], \text{mat}[0][1])}$

→ avoid double swaps,



$$r=0 \rightarrow \text{stop} = 0$$

$$r=1 \rightarrow \text{stop} = 1$$

$$r=2 \rightarrow \text{stop} = 2$$

* perform `swap(mat[r][c], mat[c][r])`

either on upper triangular matrix /
lower triangular matrix

```
for (let r = 0; r < n; r++) {  
    for (let c = 0; c < r; c++) {  
        swap(mat[r][c], mat[c][r]);  
    }  
}
```

* $T: \frac{n(n+1)}{2} = O(N^2)$

SC: $O(1)$

* only works for $N \times N$ matrix