

* Spiral Traversal :

	0	1	2	3	4	5	6
0	11	12	13	14	15	16	17
1	21	22	23	24	25	26	27
2	31	32	33	34	35	36	37
3	41	42	43	44	45	46	47
4	51	52	53	54	55	56	57

op : 11 12 13 14 15 16 17 21 31 41 51 61 71 81
55 54 53 52 51 41 31 21 22 23 24
25 26 36 46 45 44 43 42 32 33
34 35

* TC : How many times each element is visited/touched by your code.

⇒ each ele is visited once.

⇒ there are $n * m$ elements

TC : $(n * m + 1)$ no. of times each ele visited.

TC : $O(rows * cols)$

	minC	minC	maxC	maxC		
0	0	1	2	3	4	5
minR →	①	12	13	14	15	16
minR →	④	②	23	24	25	26
maxR →	③	⑧	⑨	34	35	36
4	41	⑦	42	43	44	45
	51	52	53	54	55	56
					⑤	57

= 35

② Right wall ($(1,6)$, $(2,6)$, $(3,6)$, $(4,6)$)

[$r = \text{minR}$ to maxR , maxC]

```
for(let r = minR ; r <= maxR ; r++) {
    psw(mat[r][maxC] + " ");
}
maxC--;
6--,
```

⑤

④ Left wall ($(0,0)$, $(1,0)$, $(2,0)$)

[$r = \text{maxR}$ to minR , minC]

```
for(let r = maxR ; r >= minR ; r--) {
    psw(mat[r][minC] + " ");
}
minC++;
```

① top wall → minC

② right wall → maxC

③ bottom wall → maxR

④ left wall → minR

① Top wall ($(0,0)$, $(0,1)$, $(0,2)$, $(0,3)$,
 $(0,4)$, $(0,5)$, $(0,6)$)

[minR , $C = \text{minC}$ to maxC]

```
for(let c = minC ; c <= maxC ; c++) {
    psw(mat[minR][c] + " ");
}
minR++;
```

(once the job of wall is completed move to next possible wall)

③ Bottom Wall ($(4,5)$ $(4,4)$ $(4,3)$,
 $(3,2)$ $(3,1)$ $(3,0)$)

[maxR , $C = \text{maxC}$ to minC]

```
for(let c = maxC ; c >= minC ; c--) {
    psw(mat[maxR][c] + " ");
}
maxR--;
```

* Repeat the boundary printing process
* until all the elements in the matrix are covered/touched/printed;

* Alternate Matrix Sum :

	0	1	2	3
0	10	1	2	3
1	7	6	13	9
2	14	11	12	16
3	5	4	15	8

4 x 4 Chess Board

black squares sum

$$= 10 + 2 + 6 + 9 + 14 + 12 + 4 + 8 \\ = 75$$

white squares sum

$$= 1 + 3 + 7 + 13 + 11 + 16 + 5 + 15 \\ = 71$$

1. Iterating on all elements of matrix (r, c)

2. you need to decide whether the current box (r, c) belongs to white square/black square

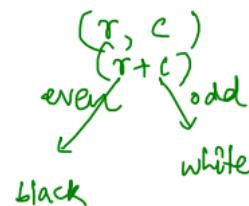
$$\text{bsum} = 0 \\ \text{wsum} = 0$$

$$(0, 0) \xrightarrow{\text{b}} \text{bsum} \\ \downarrow w \quad \uparrow \text{wsum} \\ += \text{mat}(0)(0)$$

$$(0, 1) \xrightarrow{\text{b}} \text{bsum} \\ \downarrow w \quad \uparrow \text{wsum} \\ += \text{mat}(0)(1)$$

$$(0, 2) \xrightarrow{\text{b}} \text{bsum} \\ \downarrow w \quad \uparrow \text{wsum} \\ += \text{mat}(0)(2)$$

$$(0, 3) \xrightarrow{\text{b}} \text{bsum} \\ \downarrow w \quad \uparrow \text{wsum} \\ += \text{mat}(0)(3)$$



black

$$\begin{aligned} (0, 0) &= 0 \\ (0, 2) &= 2 \\ (1, 1) &= 2 \\ (1, 3) &= 4 \\ (2, 0) &= 2 \\ (2, 2) &= 4 \\ (2, 1) &= 4 \\ (2, 3) &= 6 \end{aligned}$$

white

$$\begin{aligned} (0, 1) &= 1 \\ (0, 3) &= 3 \\ (1, 0) &= 1 \\ (1, 2) &= 3 \\ (2, 1) &= 3 \\ (2, 3) &= 5 \\ (2, 0) &= 3 \\ (2, 2) &= 5 \end{aligned}$$

* Diagonal Difference :

		cols-3	cols-2	cols-1
0	1	5	9	13
1	2	6	10	14
2	3	7	11	15
3	4	8	12	16
4	11	18	19	20
N x N = 5 x 5				

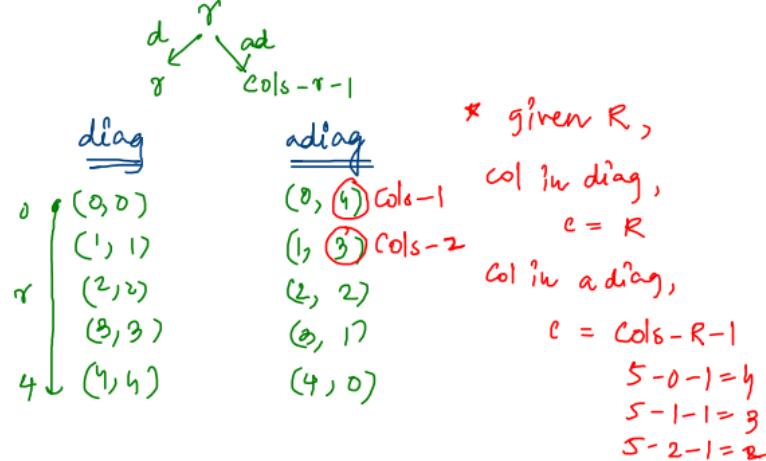
anti diagonal

diagonal

$$\text{diag} = 21 + 14 + 11 + 8 + 17 = X$$

$$\text{ad diag} = 1 + 6 + 11 + 16 + 25 = Y$$

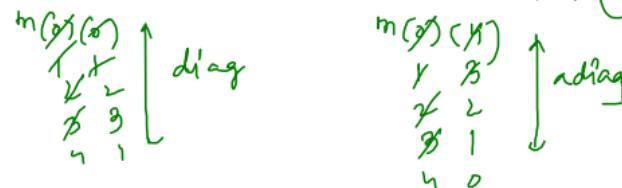
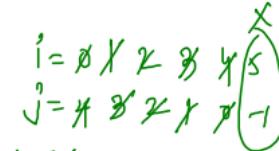
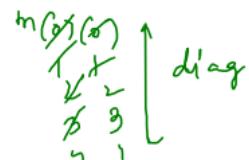
$$\text{ans} = \text{abs}(X - Y)$$



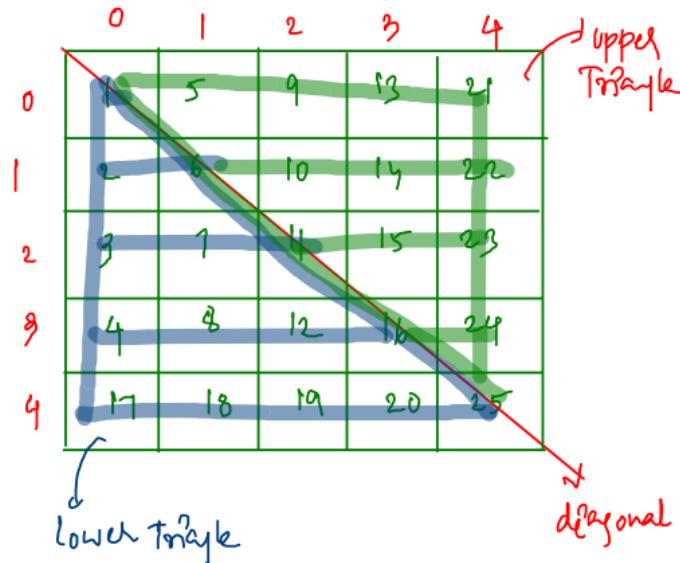
for (let r = 0; r < rows; r++) {

 diag += mat[0][r];

 ad diag += mat[0][cols - r - 1];



* Sum of upper and lower triangle :



* (r, c)
 \nearrow upperTriangle
 \searrow lowerTriangle
 How to decide?

$$lsum = 0$$

$$usum = 0$$

lowerTriangle $(r >= c)$

$$(0, 0) (0 >= 0)$$

$$(1, 0) (1 >= 0)$$

$$(1, 1) (1 >= 1)$$

$$(2, 0) (2 >= 0)$$

$$(2, 1) (2 >= 1)$$

$$(2, 2) (2 >= 2)$$

$$(3, 0) (3 >= 0)$$

$$(3, 1) (3 >= 1)$$

$$(3, 2)$$

$$(3, 3)$$

upperTriangle $(r <= c)$

$$(0, 0) (0 <= 0)$$

$$(0, 1) (0 <= 1)$$

$$(0, 2) (0 <= 2)$$

$$(0, 3) (0 <= 3)$$

$$(0, 4) (0 <= 4)$$

$$(1, 1) (1 <= 1)$$

$$(1, 2) (1 <= 2)$$

$$(1, 3)$$

$$(1, 4)$$

$$(2, 2) (2 <= 2)$$

* Toeplitz Matrix :

	0	1	2	3	4
0	1	5	9	13	21
1	2	6	10	14	22
2	3	7	11	15	23
3	4	8	12	16	24
4	17	18	19	20	25

$$\begin{aligned}
 (0,0) &\rightarrow (1,1) & (r,c) \\
 (0,1) &\rightarrow (1,2) & \downarrow \\
 (0,2) &\rightarrow (1,3) & (r+1, c+1)
 \end{aligned}$$

All elements in a same diagonal must be equal

$$\begin{aligned}
 m(0)(0) &= m(1)(1) = m(2)(2) = m(3)(3) = m(4)(4) \\
 m(0)(1) &= m(1)(2) = m(2)(3) = m(3)(4) \\
 m(0)(2) &= m(1)(3) = m(2)(4)
 \end{aligned}$$

$$\begin{aligned}
 c+1 &< \text{cols} \\
 r+1 &< \text{rows} \\
 (3,4) & 5 < 5 \times 4 < 5 \\
 (4,5) & \text{out of box} \\
 r+1, c+1 & \text{is valid}
 \end{aligned}$$

$$\begin{array}{ll}
 i = \emptyset & j = \emptyset \\
 i = \emptyset & j = \emptyset \\
 i = \emptyset & j = 1 \\
 i = \emptyset & j = 1 \\
 i = \emptyset & j = 2 \\
 i = \emptyset & j = 2 \\
 i = \emptyset & j = 3 \\
 i = \emptyset & j = 3 \\
 i = \emptyset & j = 4 \\
 i = \emptyset & j = 4 \\
 i = \emptyset & j = 4 \\
 i = \emptyset & j = 4
 \end{array}$$

1. keep iterating on all elements of matrix

2. At (r, c) check whether the next diagonal element is equal or not

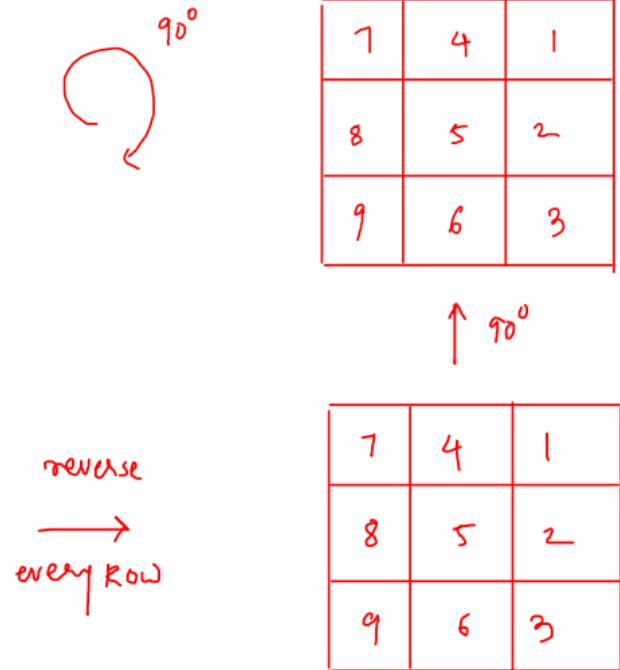
$$\begin{array}{c}
 +1 \\
 (3,1) \rightarrow (4,2) \\
 +1
 \end{array}$$

* Rotate Matrix by 90° :

1	2	3
4	5	6
7	8	9

cols \leftrightarrow Rows
↓ transpose

1	4	7
2	5	8
3	6	9



7	4	1
8	5	2
9	6	3

7	4	1
8	5	2
9	6	3