

* Sum of digits :

eg: 1325

$$\text{op: } 1 + 3 + 2 + 5 = \textcircled{11}$$

eg: 565423

$$\text{op: } 5 + 6 + 5 + 4 + 2 + 3 = \textcircled{25}$$

$$9254 \quad \text{sum} = 0 \quad \text{if}$$

$$\begin{aligned} \textcircled{1} \quad 9254 \% 10 &= 4 \\ \text{sum} &= \text{sum} + 4 = 0 + 4 = 4 \\ \text{num} &= 9254 / 10 = 925 \end{aligned}$$

$$\begin{aligned} \textcircled{2} \quad 925 \% 10 &= 5 \\ \text{sum} &= \text{sum} + 5 = 4 + 5 = 9 \\ \text{num} &= 925 / 10 = 92 \end{aligned}$$

$$\begin{aligned} \textcircled{3} \quad 92 \% 10 &= 2 \\ \text{sum} &= \text{sum} + 2 = 9 + 2 = 11 \\ \text{num} &= 92 / 10 = 9 \end{aligned}$$

$$132\cancel{5} \% 10 = \textcircled{5}$$

$$\downarrow \quad 1325 / 10 = 132$$

$$13\cancel{2} \% 10 = \textcircled{2}$$

$$\downarrow \quad 132 / 10 = 13$$

$$\cancel{13} \% 10 = \textcircled{3}$$

$$\downarrow \quad 13 / 10 = 1$$

$$\cancel{1} \% 10 = \textcircled{1}$$

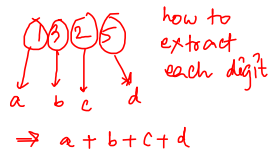
$$\downarrow \quad 1 / 10 = 0$$

0 (stop) (until num = 0)

$$\textcircled{4} \quad 9 \% 10 = 9$$

$$\text{sum} = \text{sum} + 9 = 11 + 9 = \textcircled{20}$$

$$\text{num} = 9 / 10 = 0$$



let sum = 0;

1. extract last digit,
const d = num % 10;
sum = sum + d;

2. remove last digit,
num = num / 10;

3. repeat step 1 and 2
until num becomes 0.
(digit extraction)

* Reverse of a Number :

eg: 1325

op: 5231

1000 100 10 1
1 3 2 5

$$\Rightarrow 5 * 1 + 2 * 10 + 3 * 100 + 1 * 1000$$

$$\Rightarrow 5 + 20 + 300 + 1000 = 1325$$

$$\textcircled{3} \quad 13 \% 10 = 3$$

$$\text{rev} = 52 * 10 + 3 = 523$$

$$13 / 10 = 1$$

$$\textcircled{4} \quad 1 \% 10 = 1$$

$$\text{rev} = 523 * 10 + 1$$

$$= 5231$$

$$1 / 10 = 0$$

1000 100 10 1
5 2 3 1

$$\Rightarrow 1 * 1 + 3 * 10 + 2 * 100 + 5 * 1000$$

$$\Rightarrow 1 + 30 + 200 + 5000$$

$$\Rightarrow 5231$$

$$1325 \% 10 = \textcircled{5} \quad 0 * 10 + 5 = 5$$

$$132 \% 10 = \textcircled{2} \quad 5 * 10 + 2 = 52$$

$$13 \% 10 = \textcircled{3} \rightarrow 1 * 10 = \textcircled{1} \rightarrow 0$$

$$52 * 10 + 3 = 523 \quad 523 * 10 + 1 = 5231$$

let rev = 0;

1. extract last digit,

const d = num % 10;

rev = rev * 10 + digit;

2. remove last digit,

num = num / 10;

3. repeat step 1 and 2

until num becomes 0.

(digit extraction)

$$\textcircled{1} \quad 1325 \% 10 = 5$$

$$\text{rev} = 0 * 10 + 5 = 0 + 5 = 5$$

$$1325 / 10 = 132$$

$$\textcircled{2} \quad 132 \% 10 = 2$$

$$\text{rev} = 5 * 10 + 2 = 52$$

$$132 / 10 = 13$$

* HCF of two numbers:

eg: 75, 90

highest common factor
(a) greatest common divisor (HCF/GCD)

→ X is a number such that
 $\checkmark 75 \% X = 0$ and $\checkmark 90 \% X = 0$
and X is the largest possible number

```
for (let num = min(a, b); num > 0; num--) {  
  if (a % num == 0 && b % num == 0) {  
    console.log(num);  
    break;  
  }  
}
```

* 1st Common divisor from back side

$$75 \% 5 = 0$$

$$90 \% 5 = 0$$

so 5 is a common divisor/factor

* a, b, $\boxed{GCD \leq \min(a, b)}$

→ the common divisor cannot be greater than $\min(a, b)$ for sure.

75, 90 you cannot divide

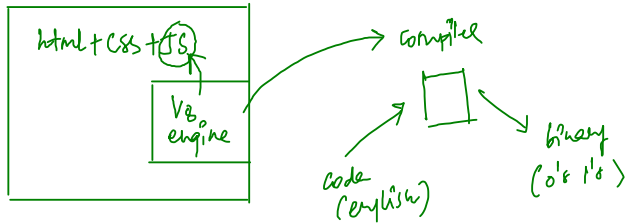
$$> 75, 75 \% 80 = 75$$

$$75 \% 76 = 75$$

$75 \% X \neq 0$ (hmm)
if $X > 75$

* process.stdout.write :

google chrome



C/C++/Java/python
or
mingw JDK python

① Install a compiler

JS

① web browser
(chrome)

* process.stdout.write is

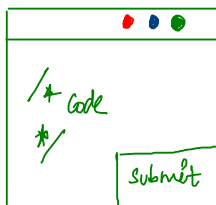
not a part of V8 engine
hence chrome doesn't understand
it. But how are you able
to submit it in your online
IDE?

→ because backend server
has node.js which provides
libuv.

* process.stdout.write can only print
text/strings.

→ number
PSW(123); ~~X~~

Online IDE



JS Code



output



Backend Server (Computer over the Internet)

The code sent from online IDE will run here and op is sent back.

V8 engine + libuv

how will you get V8 engine on server to run JS?

(Node.js)

(runtime environment for JS)

Improving check prime : $[2, n-1] \rightarrow [2, \sqrt{n}]$

earlier, $n=13 \rightarrow 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12$
 $[2, 12] \simeq n \text{ checks} \simeq n \text{ iterations}$

Now, $n=13 \rightarrow [2, \sqrt{13}]$ is enough
 $2, 3 \simeq \sqrt{n} \text{ checks} \simeq \sqrt{n} \text{ iterations}$

$n = 10^8 \Rightarrow [2, 10^8 - 1] \simeq 10^8 \text{ checks} \simeq 10^8 \text{ iterations} \rightarrow 1 \text{ cr}$
 $\Rightarrow [2, \sqrt{10^8}] \simeq 10^4 \text{ checks} \simeq 10^4 \text{ iterations} \leftarrow \text{huge improvement}$
 $[2, 10^4] \rightarrow 10 \text{ K}$

* why \sqrt{n} is enough?

eg: 36

2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35

multiplier

36
 2×18
 3×12
 4×9
 6×6
 \sqrt{n} point

$$\rightarrow 2 \times 18 = 36$$

$$36 \% 2 = 0$$

$$36 \% 18 = 0$$

$$18 \times 2 = 36$$

Both are same

$$36 \% 4 = 0$$

$$36 \% 9 = 0$$

Both are same

24
 2×12
 3×8
 4×6
 \sqrt{n} point

$$24 \% 2 = 0$$

$$24 \% 12 = 0$$

} same

$$24 \% 3 = 0$$

$$24 \% 8 = 0$$

} same

$$\sqrt{24} = 4.8989 \dots \approx 4$$