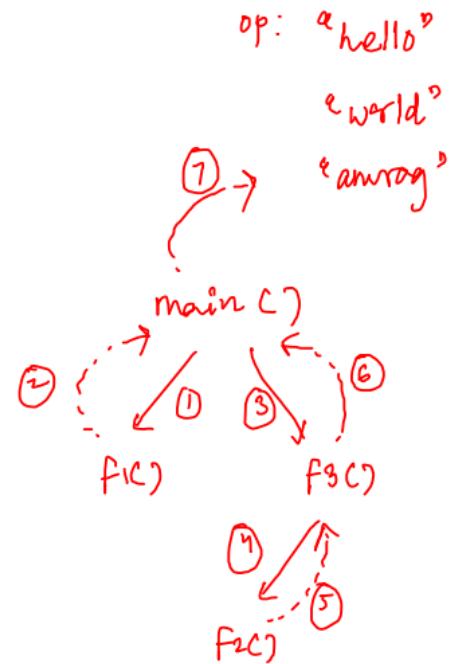


```
function f1() {  
  1. console.log("Hello");  
}
```

```
function f2() {  
  1. console.log("World");  
}  
  
function f3() {  
  1. f2();  
  2. console.log("amrag");  
}
```

```
function main() {  
  1. f1();  
  2. f3();  
}  
  
main();
```



\* How function calling works? (Recap)



stack

1. main is waiting for f1() to complete
- \* always function which is on top of stack will be running.

## \* Recursion : (VVVIMP)

→ It is function calling itself until a condition is met.

function f() { ① }

1. console.log("Hello");  
2. f();  
3

function main() {  
1. f();  
3  
main();

function f() { ② }

1. console.log("Hello");  
2. f();  
3

function f() { ③ }

1. console.log("Hello");  
2. f();  
3

function f() { ④ }

1. console.log("Hello");  
2. f();  
3

function f() { ⑤ }

1. console.log("Hello");  
2. f();  
3

so on until infinite times

op: "Hello"  
"hello"  
"hello"  
"hello"  
"hello"  
"hello"

keep on growing



Stack

function  $F(cnt) \stackrel{=0}{\equiv} P$

```
1. if (cnt == 3) {  
2.     return;  
3. }
```

```
8. console.log("Hello");  
4. f(cnt + 1);  
}  
  
f(0);
```

\* Base Case,

⇒ termination condition  
in recursion

function  $F(cnt) \stackrel{=1}{\equiv} f \cdot F$

```
1. if (cnt == 3) {  
2.     return;  
3. }
```

```
8. console.log("Hello");  
4. f(cnt + 1);  
}
```

function  $F(cnt) \stackrel{=2}{\equiv} f \cdot f \cdot P$

```
1. if (cnt == 3) {  
2.     return;  
3. }
```

```
8. console.log("Hello");  
4. f(cnt + 1);  
}
```

function  $F(cnt) \stackrel{=3}{\equiv} f \cdot f \cdot f \cdot f$

```
1. if (cnt == 3) {  
2.     return;  
3. }
```

```
8. console.log("Hello");  
4. f(cnt + 1);  
}
```

op:  
"Hello"  
"Hello"  
"Hello"

Stack

\* How to solve problems using recursion ?

1. faith (vishwas, believe)
2. Logic (do some work, give rem-work to recursion) (\* Cannot give entire work to recursion)
3. BaseCase
4. Recursive tree (function calls tree)

Q1: print "ACClOJOB" n times

```
function print (n) {  
    if(n == 0){  
        return;  
    }  
    print (n-1);  
    console.log ("ACClOJOB");  
}
```

1.  $\text{print}(n) \rightarrow \text{"ACClOJOB" will be printed } n \text{ times}$

\* There is no code, nothing is there, but put a blind faith.

2.  $\text{print}(5) \rightarrow \text{"ACClOJOB"}$

"ACClOJOB"

"ACClOJOB"

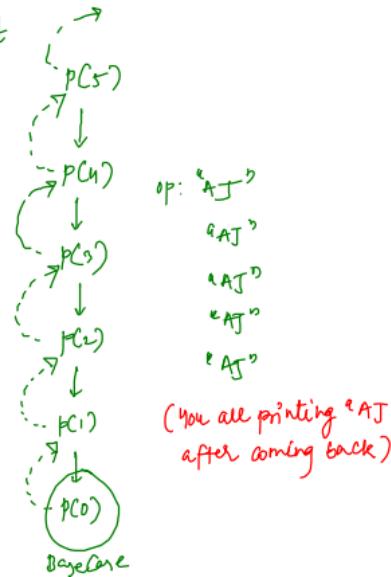
"ACClOJOB"

"ACClOJOB"

3. think about smallest  
Input possible  
(n)

draw the recursive  
tree and decide

4. recursive tree



$\text{print}(4) \rightarrow \text{"ACClOJOB"}$

"ACClOJOB"

"ACClOJOB"

"ACClOJOB"

"ACClOJOB"

(you are printing AJ  
after coming back)

# another way :

$n \rightarrow n-1 \rightarrow n-2 \rightarrow \dots \rightarrow 0$

```
function print (cnt, w) {  
    if (cnt == n) {  
        return;  
    }
```

```
    console.log ('ACCOJOBJ');  
    print (cnt + 1, w);  
}  
  
op: "AJ"  
     "AJ"  
     "AJ"  
     "AJ"  
     "AJ"  
     "AJ"
```

The diagram illustrates the recursive calls for the function print(1, 5). It shows a vertical sequence of six nodes, each labeled p(i, 5) where i ranges from 0 to 5. An arrow points from p(0, 5) to p(1, 5), another from p(1, 5) to p(2, 5), and so on. The node p(5, 5) at the bottom is highlighted with a green circle.

$$cnt = 0$$

$$n = 5$$

1. print (cnt, n)

→ It will print " $n - cnt$ " times

⇒ It will print  $cnt \rightarrow n$  timer

2. print (0, 5)

⇒ "AJ"  
 "AJ"  
 "AJ"  
 "AJ"  
 "AJ"

print(1, 5) ⇒ "AJ"  
 "AJ"  
 "AJ"  
 "AJ"

## \* pre, in, post Areas :

```
function print (n) {  
    if(n == 0) {  
        return;  
    }  
    print (n-1);  
    console.log ("ACC10JOB");  
}  
;
```

The diagram illustrates the execution stack frames for the `print` function. The stack grows from bottom to top. The frames are labeled with their respective code snippets and the state of the stack (e.g., "AT").

\* Area After rec. call  
is called post area

(post-order  
way of solving)

[ Dynamic programming ]  
(getting the Answer)

```
function print (n) {  
    if(n == 0) {  
        return;  
    }  
    console.log ("ACC10JOB"); → "AT"  
    print (n-1);  
    }  
;
```

The diagram illustrates the execution stack frames for the `print` function. The stack grows from bottom to top. The frames are labeled with their respective code snippets and the state of the stack (e.g., "AT"). A red annotation on the right side of the diagram reads: "(you are printing up AT while going down)".

\* Area before recursion Call is  
called pre area

(pre-order way)  
of solving

(forming the answer)  
(answer will be achieved  
at the Basecase)

\* Area in between  
recursion call is  
call in area

## \* Why Recursion, why not Iteration :

① "a b c d e f"  
print all permutations -

$\stackrel{6}{\Rightarrow} n! \Rightarrow 6! \Rightarrow 720$   
 $6 \times 5 \times 4 \times 3 \times 2 \times 1$

a b c d f e

a b c f d e

② solving sudoku  
(explore possibilities)

5	3			7				
6			1	9	5			
	9	8				6		
8			6				3	
4		8		3				1
7			2				6	
	6			2	8			
		4	1	9			5	
			8		7	9		

9:35 - 9:50 pm

Break

## \* Recursively print numbers :

(1 to N)

IP: n = 5

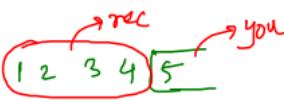
OP: 1 2 3 4 5

3. function print(n) {

    if(n == 0) {

        return;

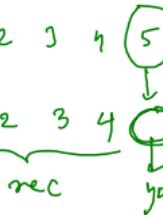
}

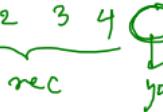
    print(n-1) //   
    process.stdout.write(n + " ") ;

}

(post-way)

1. print(n)  $\Rightarrow$  will print all numbers from 1 to N increasingly.

2. print(5)  $\Rightarrow$  1 2 3 4 

print(4)  $\Rightarrow$  

4. 

OP: 1 - 2 - 3 - 4 - 5 -

# another way: (pre-way)

3. function print (curr-num, n) {

```
    if (curr-num > n) {  
        return;  
    }
```

```
    process.stdout.write(curr-num + " ");
```

```
    print (curr-num + 1, n); // [1] [2 3 4 5]  
    ↓  
    curr rec
```

↓

op: 1 2 3 4 5

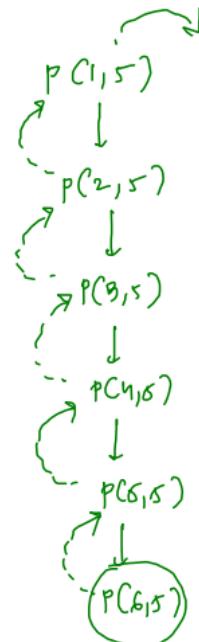
1. print (curr-num, n)

⇒ It will print all numbers  
from curr-num → n

2. print (1, 5) ⇒ 1 2 3 4 5

print (2, 5) ⇒ 2 3 4 5

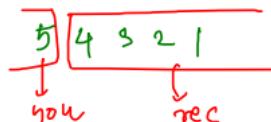
4.



## \* Reverse print Recursion :

ip:  $n = 5$

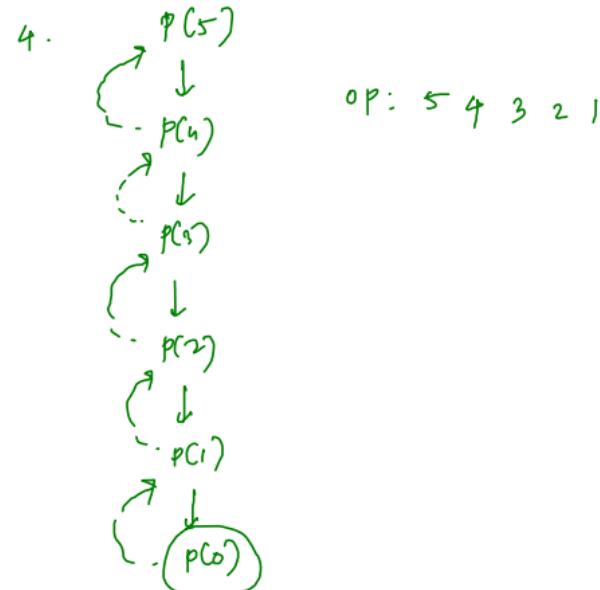
op: 5 4 3 2 1

3. function print(n) {  
    if ( $n == 0$ ) {  
        return;  
    }  
    process.stdout.write( $n + " "$ );  
    print( $n - 1$ ); //   
}

(pre-way)

1.  $\text{print}(n) \Rightarrow$  print all the numbers from  $n$  to 1 decreasingly.

2.  $\text{print}(5) \Rightarrow 5 4 3 2 1$   
 $\text{print}(4) \Rightarrow 4 3 2 1$



# another way (post-way):

3. function print (curr-num, n) {

    if (curr-num > n) {

        return;

}

    print (curr-num + 1, n); //  $\begin{matrix} 5 \\ 4 \\ 3 \\ 2 \\ 1 \end{matrix}$   
    process.stdout.write(curr-num);     ↓  
  rec  
  num

}

1. print (curr-num, n)

→ will print all numbers from  
 $n \rightarrow curr-num$

2. print(1, 5)  $\Rightarrow$  5 4 3 2 1

print(2, 5)  $\Rightarrow$  5 4 3 2

4.  $\begin{array}{c} p(1, 5) \\ \downarrow \\ p(2, 5) \\ \downarrow \\ p(3, 5) \\ \downarrow \\ p(4, 5) \\ \downarrow \\ p(5, 5) \\ \downarrow \\ p(6, 5) \end{array}$  op: 5 4 3 2 1