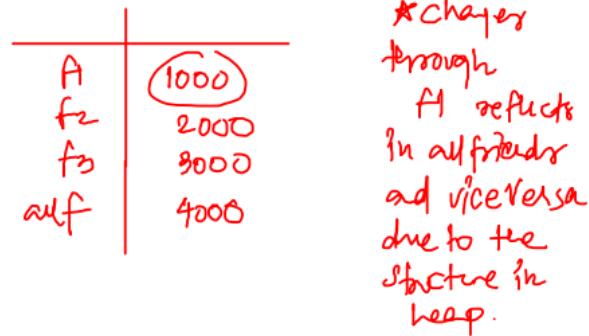
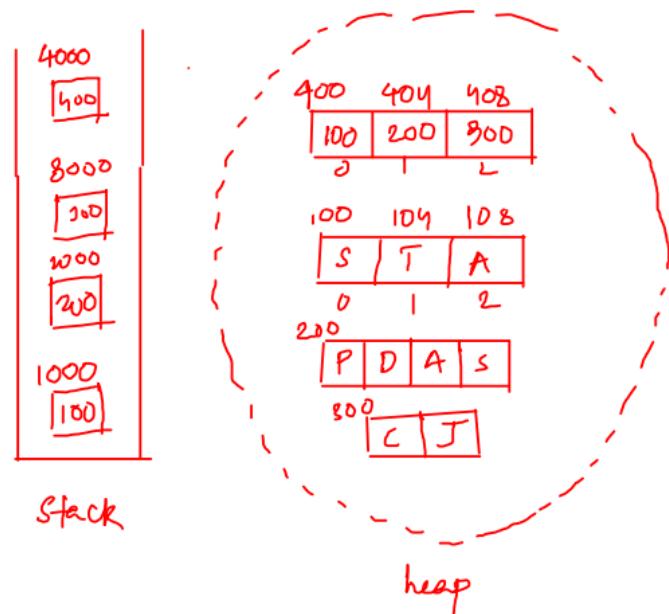
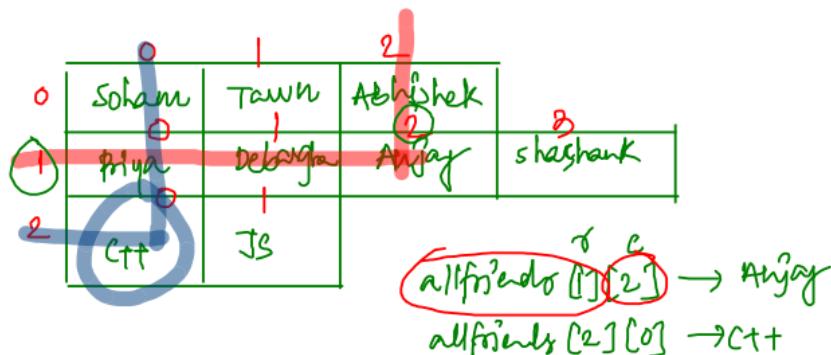


* Array of Array (2D Array) :

```

759 const friends1 = ["Soham", "Tarun", "Abhishek"];
760 const friends2 = ["Priya", "Debargha", "Anjay", "Shashank"];
761 const friends3 = ["C++", "JavaScript"];
762
763 const allFriends = [friends1, friends2, friends3];
764 console.log(allFriends);
765 console.log(allFriends[0]);
766 console.log(allFriends[1]);
767 console.log(allFriends[2]);
    
```

for simplicity on paper we represent them as matrices!



← column →

0 1 2

→ allFriends [[], [], []]

↑ rows ↓

0	"soham"	"Tawn"	"Abhishek"
1	"priya"	"Debangha"	"Anujay"
2	"C++"	"JavaScript"	"ishareshank"

- * When there different no. of cols in each row
It is called "Jagged Array".
- * In general, no. of cols will be same in every row.

Q: No. of rows

$$\begin{aligned}
 \underline{\text{A:}} \quad & \text{no. of rows} = 3 \\
 &= \text{no. of smaller Arrays} \\
 &= \text{no. of elements in allFriends} \\
 &= \text{allFriends.length}
 \end{aligned}$$

Q: No. of cols

$$\begin{aligned}
 \underline{\text{A:}} \quad & \text{no. of cols} = \text{length of each row} \\
 &= \text{no. of elements in each smaller array.}
 \end{aligned}$$

$$\text{row} = 0 \Rightarrow \text{allFriends}[0].length$$

$$\text{row} = 1 \Rightarrow \text{allFriends}[1].length$$

$$\text{row} = 2 \Rightarrow \text{allFriends}[2].length$$

Q: Given an $N \times M$ matrix, print it as follows
 rows cols

If $N = 3, M = 3$

	0	1	2
0	10	11	12
1	15	13	14
2	16	17	18

3×3

op:

10	11	12
15	13	14
16	17	18

→ go to every row,
 and print that row by travelling
 each column;

rows = 3
 cols = 3

for (let r = 0; r < rows; r++) {
 for (let c = 0; c < cols; c++) {

psw (m[r][c] + ' ');

}

console.log();

① $r = 0$

$\rightarrow c = 0 \rightarrow m[0][0]$
 $\rightarrow c = 1 \rightarrow m[0][1]$
 $\rightarrow c = 2 \rightarrow m[0][2]$

② $r = 1$

$\rightarrow c = 0 \rightarrow m[1][0]$
 $\rightarrow c = 1 \rightarrow m[1][1]$
 $\rightarrow c = 2 \rightarrow m[1][2]$

}

③ $r = 2$

$\rightarrow c = 0$
 $\rightarrow c = 1$
 $\rightarrow c = 2$

④ $r = 3 \times$
 $(3 < 3)$

Q: Create a $N \times M$ matrix in the following pattern?

0 1 2

eg: $\$t$, $n=3$, $m=4$

mat = [[1, 2, 3, 4], [1, 2, 3, 4], [1, 2, 3, 4]]

Op:

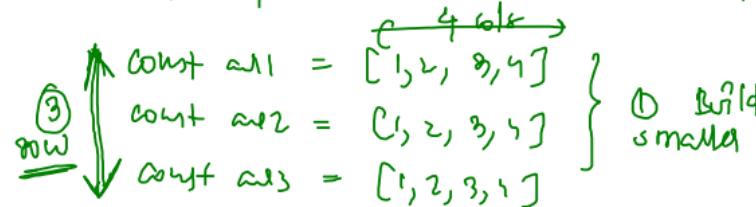
	0	1	2	3
0	1	2	3	4
1	1	2	3	4
2	1	2	3	4

3x4

matrix = [];

```
for (let r=0; r<rows; r++) {  
    const smallArr = [];  
    for (let c=0; c<cols; c++) {  
        smallArr.push(c+1);  
    }  
    matrix.push(smallArr);  
}
```

→ To build an entire matrix,
= first you need to build smaller arrays

③ 
const arr1 = [1, 2, 3, 4]
const arr2 = [1, 2, 3, 4]
const arr3 = [1, 2, 3, 4]

const mat = [arr1, arr2, arr3] ② store
smaller
in bigger

→ c=0, [1] r=0 [1, 2, 3, 4]
→ c=1, [1, 2] r=1 [1, 2, 3, 4]
→ c=2, [1, 2, 3] r=2 [1, 2, 3, 4]
→ c=3, [1, 2, 3, 4] r=3 [1, 2, 3, 4]
→ c=4 (4 < 4) X

* Print matrix column wise :

Op:	0	1	2	3	4
0	1	2	3	4	5
1	6	7	8		
2	9	10	11	12	
3	13	14	15	16	

Op: 1 5 9 13 2 6 10 14
3 7 11 15 4 8 12 16

* fix col

→ go to every row

$r=0, c=0$	$r=0, c=1$
$r=1, c=0$	$r=1, c=1$
$r=2, c=0$	$r=2, c=1$
$r=3, c=0$	$r=3, c=1$
$c=0$	$c=1$
$r=0 \rightarrow 3$	$r=0 \rightarrow 3$
	$c=2$
	$r=0 \rightarrow 3$
	$r=0 \rightarrow 3$

for (let c=0; c < cols; c++) {

 for (let r=0; r < rows; r++) {

 pw(m(r)c) + " ");

}

$O(rows \times cols)$
 $O(N)$
forward col
 $\Rightarrow O(N \times m)$

* TC: $O(rows \times cols) \Rightarrow O(N \times m)$

SC: $O(1)$

* Alternate Matrix traversal :

ip:

	0	1	2	3
0	1	2	3	4
1	5	6	7	8
2	9	10	11	12
3	13	14	15	16

odd rows

(1st, 3rd, 5th, etc...)
(L → R)

even rows

(2nd, 4th, 6th, etc...)
(R → L)

In 0-indexing terms

odd rows

(1st, 3rd, 5th, etc...)
(R → L)

even rows

(0th, 2nd, 4th, etc...)
(L → R)

```
for (let r = 0; r < rows; r++) {
```

```
    if (r % 2 == 0) {
```

```
        for (let c = 0; c < cols; c++) {
```

```
            psw(m[r][c] + ' ');
```

```
}
```

★ TC : O(nxm)

★ SC : O(1)

```
    else {
```

```
        for (let c = cols - 1; c >= 0; c--) {
```

```
            psw(m[r][c] + ' '>,
```

```
}
```

* Transpose of a Matrix : [In-place]

	0	1	2	3	4
0	1	2	3	4	5
1	6	7	8	9	10
2	11	12	13	14	15
3	16	17	18	19	20
4	21	22	23	24	25

Interchange
rows \leftrightarrow cols

	0	1	2	3	4
0	1	6	11	16	21
1	2	7	12	17	22
2	3	8	13	18	23
3	4	9	14	19	24
4	5	10	15	20	25

$$m(0)(0) \leftrightarrow m(0)(1)$$

$$m(0)(1) \leftrightarrow m(1)(0)$$

	0	1	2	3	4
0	1	2	3	4	5
1	6	7	8	9	10
2	11	12	13	14	15
3	16	17	18	19	20
4	21	22	23	24	25

$$m(1)(0) \leftrightarrow m(0)(1)$$

$$m(2)(0) \leftrightarrow m(0)(2)$$

$$m(2)(1) \leftrightarrow m(1)(2)$$

$$m(3)(0) \leftrightarrow m(0)(3)$$

$$m(3)(1) \leftrightarrow m(1)(3)$$

$$m(3)(2) \leftrightarrow m(2)(3)$$

	0	1	2	3	4
0	1	2	3	4	5
1	6	7	8	9	10
2	11	12	13	14	15
3	16	17	18	19	20
4	21	22	23	24	25

$r=0 \quad r=1 \quad r=2$
 1 time 2 times 3 times

$r=3 \quad r=4$
 4 times 5 times

$$\text{rows} \Rightarrow 1 + 2 + 3 + 4 + 5$$

$$n \text{ rows} \Rightarrow 1 + 2 + 3 + \dots + n$$

$$\Rightarrow \frac{n(n+1)}{2} \Rightarrow O(N^2), \text{ SC: } O(1)$$

$r = 0, c = 0 \downarrow$
 $r = 1, c = 0, 1 \downarrow$
 $r = 2, c = 0, 1, 2 \downarrow$
 $r = 3, c = 0, 1, 2, 3 \downarrow$
 $r = 4, c = 0, 1, 2, 3, 4 \downarrow$

$c = 0 \rightarrow r$

for (let $r = 0; r < \text{rows}; r++$) {

 for (let $c = 0; c < r; c++$) {

 let temp = $m(r)(c)$;

$m(r)(c) = m(c)(r)$;

$m(c)(r) = \text{temp}$;

}
}

* $N \times M$
 matrix
 why not
 work
 as this doesn't
 have a
 diagonal, hence
 we will use the
 extra space
 approach

O(N)

Inher
loop will
not run
 $j < i$
 $i < 0 \times$

```

90  function hw1(n) {
91    for (let i = 0; i < n; i++) {
92      for (let j = 0; j < i; j++) {
93        console.log("*");
94        break;
95      }
96    }
97  }  $i_2 \leq N$ 
98
99 function hw2(n) {  $i \rightarrow \sqrt{n}$ 
100 let i = 1;
101 while (i ** 2 <= n) {  $O(\sqrt{n})$ 
102   i = i + 1;
103 }
104
105
106 function hw3(m, n) {
107   while (m != n) {  $m \neq 0$ 
108     if (m > n) {
109       m = m - n;
110     } else {
111       n = n - m; loop
112     }
113   } (at) max(m,n)
114 }
```

$$m = 4, n = 0$$

$$m = 4 - 0 = 4$$

$$m = 4 - 0 = 4$$

Infinite

$$m = 4, n = 1$$

$$m = 4 - 1 = 3$$

$$m = 3 - 1 = 2$$

$$m = 2 - 1 = 1$$

```

116 function hw4(n) {
117   let i = 1;
118   while (i < n) {
119     let j = n;
120     while (j > 0) {
121       j = parseInt(j / 2);
122     }
123     i = i * 2;
124   }
125 }
```

$$j = n \xrightarrow{1/2} 0$$

$$\left. \begin{array}{l} \\ \end{array} \right\} O(\log_2^n)$$

$$i = 1 \xrightarrow{+2} n$$

$$O(\log_2^n)$$

```

127 function hw5(n) {
128   for (let i = 0; i < parseInt(n / 2); i++) {
129     for (let j = 1; j < n - parseInt(n / 2); j++) {
130       let m = 1;  $n - \frac{n}{2} = \frac{n}{2}$ 
131       while (m <= n) {
132         m = m * 2;
133       }
134     }
135   }
136 }
```

$$\left. \begin{array}{l} \\ \end{array} \right\} O((\log_2^n)^2)$$

$$O(n^e \log_2^n)$$

$$i = 0 \xrightarrow{+1} \frac{n}{2} \rightarrow O(n_2)$$

$$j = 1 \xrightarrow{+1} \frac{n}{2} \rightarrow O(n_2)$$

$$\boxed{m > 0, n > 0}$$

$$O(\max(m, n))$$

$$m = 1, h = 4$$

$$n = 4 - 1 = 3$$

$$n = 3 - 1 = 2$$

$$n = 2 - 1 = 1$$

$$\left. \begin{array}{l} \textcircled{3} \simeq m \text{ times} \\ \textcircled{3} \simeq n \text{ times} \end{array} \right\}$$

$$\left. \begin{array}{l} \textcircled{3} \simeq n \text{ times} \\ \textcircled{3} \simeq m \text{ times} \end{array} \right\}$$