

* Generate Subarray : [any continuous segment of array]

e.g.: $[10, \textcircled{20}, 30, \textcircled{40}]$

10	20	30	40	
10	20	30		20
10	20	30		20 30
10	20	30		20 30 40
10	20	30		30
10	20	30		30 40
				40

$20, 40 \Rightarrow$ is not a subarray
because they are not continuous

Q: How to generate all subarrays starting with $\text{arr}[0] \Rightarrow 10$?
* Using running stream.

let subarr = " ";

for(let i = 0; i < n; i++) {

subarr = subarr + arr[i] + " ";

console.log(subarr);

}

~~10~~

~~10~~ → cl("10")

~~10 20~~ → cl("10 20")

~~10 20 30~~ → cl("10 20 30")

~~10 20 30 40~~ → cl("10 20 30 40")

Q: Now generate all subarrays using previous slide logic.

```
805 | for (let start = 0; start < n; start++) {  
806 |   let subarr = "";  
807 |   for (let end = start; end < n; end++) {  
808 |     subarr += arr[end] + " ";  
809 |     console.log(start, end, subarr);  
810 |   }  
811 }
```

① start = 0

→ subarr = " "

→ end = start = 0, subarr += arr[0] + " " = "10 "

→ end = 1, subarr += arr[1] + " " = "10 20 "

→ end = 2, subarr += arr[2] + " " = "10 20 30 "

→ end = 3, subarr += arr[3] + " " = "10 20 30 40"

② start = 1

→ subarr = "1 "

→ end = start = 1, subarr += arr[1] + " "
= "20 "

→ end = 2, subarr += arr[2] + " "
= "20 30 "

→ end = 3, subarr += arr[3] + " "
= "20 30 40 "

③ start = 2 {

= ④
}

④ start = 3 {

⑤
}

* Zero Sum Subarrays :

Eg : [3, 4, -1, 3, 1, 3] → [3, 4, -1] → [3, 4, -1, 3]

Op: (3, 4, -1) → 0 [0, 2]

(4, -1, 3) → 0 [1, 3]

(-1, 3, 1, 3) → 0 [2, 5]

→ Instead of running string for printing subarray to get sum of each subarray lets use running sum.

```
991 function zeroSubarray(arr) {  
992     //Write your code here  
993     const n = arr.length;  
994     let isFound = false; // I did not find any subarr with 0 sum  
995  
996     for (let start = 0; start < n; start++) {  
997         let sum = 0;  
998         for (let end = start; end < n; end++) {  
999             sum += arr[end];  
1000             // at every point sum => sum of arr[start....end]  
1001             if (sum == 0) {  
1002                 console.log(`Subarray found from Index ${start} to ${end}`);  
1003                 isFound = true;  
1004             }  
1005         }  
1006     }  
1007     if (isFound == false) {  
1008         console.log(-1);  
1009     }  
1010 }
```

* Find split point :

e.g.: $\left[\begin{matrix} 0 & 1 & 2 & 3 & 4 \\ 6, -4, 3, 2, -3 \end{matrix} \right]$

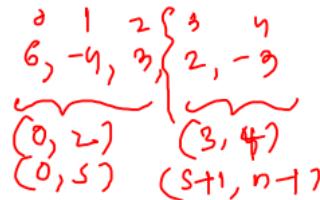
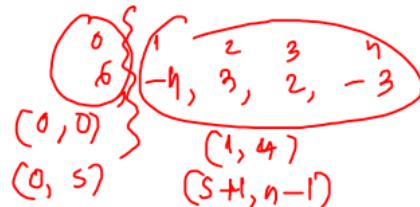
s $s+1$
1 2
2 2

op: 1

e.g.: $\left[\begin{matrix} 0 & 1 & 2 & 3 & 4 \\ 100, 10, 20, 30, 40 \end{matrix} \right]$

s
100 100

op: 0



```
for(let split = 0; split < n-1; split++) {
```

```
    const lsum = sum(arr, 0, split);
```

```
    const rsum = sum(arr, split+1, n-1);
```

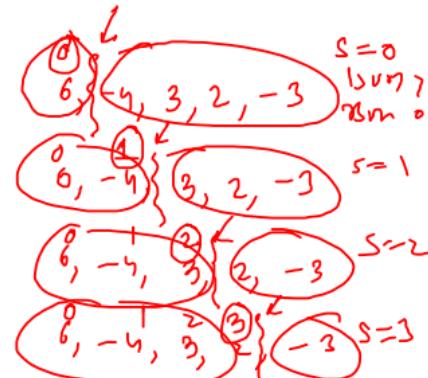
```
    if(lsum == rsum) {
```

```
        return split;
```

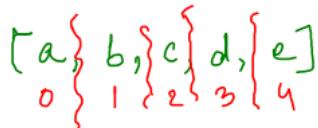
```
}
```

↑

```
return -1;
```



efficient way :



① $s = 0, 0 \rightarrow 0 \curvearrowright 1 \quad 1 \rightarrow 4 \curvearrowright 4 \quad \{ \quad \} \quad \textcircled{5}$

② $s = 1, 0 \rightarrow 1 \curvearrowright 2 \quad 2 \rightarrow 4 \curvearrowright 3 \quad \{ \quad \} \quad \textcircled{5}$

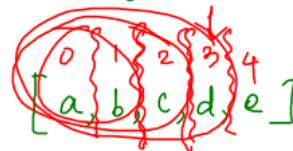
③ $s = 2, 0 \rightarrow 2 \curvearrowright 3 \quad 3 \rightarrow 4 \curvearrowright 2 \quad \{ \quad \} \quad \textcircled{5}$

④ $s = 3, 0 \rightarrow 3 \curvearrowright 4 \quad 4 \rightarrow 4 \curvearrowright 1 \quad \{ \quad \} \quad \textcircled{5}$

* total = $5 + 5 + 5 + 5 = 20$
 $= (n-1) * n$ Iterations
 $= 4 * 5 = 20$ Iterations

① totalSum $\Rightarrow a+b+c+d+e$

② runningSum



* RS will give you
the leftsum

① $s = 0$

RS += arr[s]

RS = a

rsSum = total - RS
 $= a+b+c+d+e - a$
 $= b+c+d+e$

② $s = 1$

RS += arr[s]

RS = a+b

rsSum =
 $a+b+c+d+e - (a+b)$
 $= c+d+e$

③ $s = 2$

RS += arr[s]

RS = a+b+c

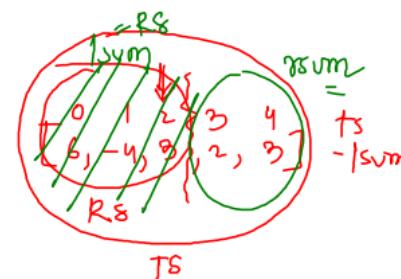
rsSum =
 $a+b+c+d+e - (a+b+c)$
 $= d+e$

④ $s = 3$

RS += arr[s]

RS = a+b+c+d

rsSum =
 e
 $(a+b+c+d+e)$
 $- (a+b+c+d)$



* geometric triplets:

Q: What is G.P?

Ex: $2, 4, 8, 16, 32, 64, \dots$

$\underbrace{2}_{2}, \underbrace{4}_{2}, \underbrace{8}_{2}, \underbrace{16}_{2}, \underbrace{32}_{2}, \underbrace{64}_{2}$

a, b, c, d, e

$$\Rightarrow \frac{b}{a} = \frac{c}{b} = \frac{d}{c} = \frac{e}{d} = r$$

Ex: $9, 27, 81, 243$

$\underbrace{9}_{3}, \underbrace{27}_{3}, \underbrace{81}_{3}, \underbrace{243}_{3}$

$\begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 \\ [1, 2, 6, 10, 18, 54] \end{matrix}$

$$1, 2, 6 \Rightarrow \frac{2}{1} = 2 \neq \frac{6}{2}$$

$$2, 6, 18 \Rightarrow \frac{6}{2} = 3 = \frac{18}{6} \quad (3 = 3)$$

∴

Op: print all such triplets

$$a, b, c \rightarrow G.P \quad \text{and}(i), \text{and}(j), \text{and}(k)$$

$$\frac{b}{a} = \frac{c}{b}$$

$$\frac{\text{and}(j)}{\text{and}(i)} \Leftrightarrow \frac{\text{and}(k)}{\text{and}(j)}$$

$$\Rightarrow b^2 = ac$$

$$\text{and}(j) * \text{and}(i)$$

$$= \text{and}(i) * \text{and}(k)$$

* Array Subtraction :

$$\begin{array}{r} & 9 \\ & \downarrow \\ 1 & & 2 & 3 \\ \downarrow & \downarrow & \downarrow & \downarrow \\ 0 & 1 & 2 & 3 \end{array}$$

eg: $[1, 2, 3, 4] \rightarrow \text{arr}, n=4$

$$\cancel{\cancel{[8, 6]}} \rightarrow \text{arr2, m=2}$$

$$\begin{array}{r} 8 \\ 6 \\ \downarrow \\ 0 \\ \downarrow \\ 1 \\ \downarrow \\ 1 \end{array}$$

$$\text{res} = [8] \cancel{[3, 9]} \cancel{[9, 1]} [8, 1, 1]$$

$$c = 0$$

$$\text{diff} = (\text{arr}(i) + c \text{only}) - \text{arr}(j)$$

$$= (4+0) - 6$$

$$= -2$$

$$\text{diff} < 0 \Rightarrow c = -1, \text{diff} = -2 + 10 = 8$$

```

1124 function findSubtraction(a, n, b, m) {
1125   //Write your code here
1126   const res = [];
1127   let carry = 0;
1128   let i = n - 1;
1129   let j = m - 1;
1130
1131   while (i >= 0 || j >= 0) {
1132     // let diff = (arr[i] + carry) - arr[j];
1133     let diff = a[i] + carry;
1134     if (j >= 0) diff -= b[j];
1135
1136     if (diff < 0) {
1137       carry = -1;
1138       diff += 10;
1139     } else if (carry == 0) {
1140       res.push(diff);
1141       i--;
1142       j--;
1143     }
1144   }
1145 }
```

$$\begin{aligned}
\text{diff} &= \text{arr}(1) + \text{carry} \\
&= 2 + (-1) \\
&= 1
\end{aligned}$$

$$\begin{aligned}
\text{diff} &= \text{arr}(2) + \text{carry} \\
&= 1 + 0 \\
&= 0
\end{aligned}$$

$$\begin{aligned}
\text{diff} &= (\text{arr}(i) + \text{carry}) - \text{arr}(j) \\
&= (3 + (-1)) - 8 = (3 - 1) - 8 \\
&= 2 - 8 = -6
\end{aligned}$$

$$\text{diff} < 0, c = -1, \text{diff} = -6 + 10 = 4$$

Ex: $[1, 2, 3, 4] \rightsquigarrow \text{arr1}$
 $[5, 6, 7, 8] \rightsquigarrow \text{arr2}$

* $\text{num}(\text{arr1}) < \text{num}(\text{arr2})$

- 1. swap
- 2. subtract \rightsquigarrow same
- 3. multiply -1

① arr1 $\rightarrow [5, 6, 7, 8]$

arr2 $\rightarrow [1, 2, 3, 4]$

$$\begin{array}{r} 5 & 6 & 7 & 8 \\ - & 1 & 2 & 3 & 4 \\ \hline 4 & 4 & 9 & 4 \end{array}$$

$$\Rightarrow [4, 4, 4, 4] \\ \Rightarrow [-4, 4, 4, 4]$$

② multiply -1,

$$\rightarrow -4444$$

Ex:

$\begin{array}{r} 0 & 1 & 2 \\ | & | & | \\ 1 & 2 & 3 \end{array} \rightsquigarrow \text{arr1}$
 $\begin{array}{r} 1 & 2 & 3 & 4 \\ | & | & | & | \\ 0 & 1 & 2 & 3 \end{array} \rightsquigarrow \text{arr2}$

arr1 $\rightarrow [1, 2, 3, 4]$

arr2 $\rightarrow [1, 2, 3]$

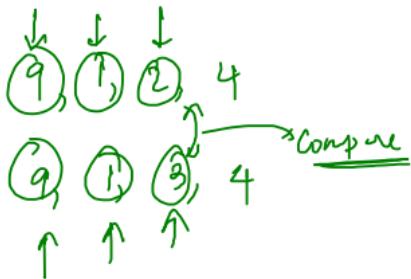
$$\underline{\quad \quad \quad \quad}$$

$$\underline{\quad \quad \quad \quad}$$

$$\underline{\quad \quad \quad \quad}$$

$$\underline{\quad \quad \quad \quad}$$

Q: How to check $\text{num}(\text{arr1}) < \text{num}(\text{arr2})$?



1. find 1st non equal elements

if ($\text{arr1}[i] < \text{arr2}[i]$)

return true

$i < 3$

$\Rightarrow \text{num}(a) < \text{num}(b)$

else

return false

9 | ③ 4 → a

9 | ② 1 → b

* $\text{len}(\text{arr1}) > \text{len}(\text{arr2})$

return false

$\Rightarrow 3 < 2 \rightarrow \text{false}$

$\text{len}(\text{arr1}) < \text{len}(\text{arr2})$

return true

$\Rightarrow \text{num}(a) > \text{num}(b)$

9 9 9 9 → n=4

9 9 9 9 → m=4