

* Check prime :

Eg: $n = 17$

Op: true

Eg: $n = 25$

Op: false

Eg: 25

$[2, 24]$

$$25 \div 1, 2 == 0$$

$$25 \div 1, 3 == 0$$

$$25 \div 1, 4 == 0$$

$$\boxed{25 \div 1, 5 == 0} \quad \checkmark$$

↓
not a prime

$$25 \div 1, 6$$

;

;

$$25 \div 1, 24 == 0$$

1. In general in real world, how will you solve this,
what is a prime number?

→ a number is prime if it is only divisible
by 1 and itself, (not divisible by any other
number apart from 1, itself)

Eg: 103

$[2, 102]$

$$103 \div 1, 2 == 0$$

$$103 \div 1, 3 == 0$$

$$103 \div 1, 4 == 0$$

...

...

...

$$103 \div 1, 102 == 0$$

* factors of number \Rightarrow number % x == 0
 \Rightarrow then x is a factor
of that number

Q: Is 103 a prime number?

a) true

b) false

c) none

2. How to convert the previous approach to code?

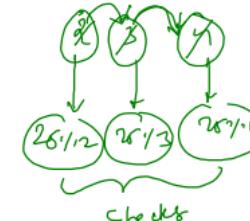
$N = 25 \rightarrow$ we are checking from $(2 \rightarrow 24) (2 \rightarrow N-1)$

① for loop helps us to take from 2 to 24

num = $\underbrace{2}_{\text{init}} \underbrace{\times 2 \times 2 \times \dots \times 24}_{\text{operation}} \xrightarrow{\text{num} < N}$
 $\downarrow + + + +$
condition (a) $\text{num} \leq 24$
 $\text{num} \leq N-1$

variables,
conditions,
loops,
type annotations etc..

```
for(let num = 2; num < N; num++) {  
    if(N % num == 0) {  
        console.log("Not a prime");  
    }  
    else {  
        console.log("prime");  
    }  
}
```



* we found a number apart from 1 & N which divides N \rightarrow not a prime

fg: $N = 25$

num = $\cancel{2}$ $\xrightarrow{+1} \cancel{3}$ $\xrightarrow{+1} \cancel{4}$ $\xrightarrow{+1} \cancel{5}$
 \downarrow \downarrow \downarrow \downarrow
 $25 \mod 2 == 0$ $25 \mod 3 == 0$ $25 \mod 4 == 0$ $25 \mod 5 == 0$
(false) (false) (false) (true)
"prime" "prime" "prime" "not prime"

→ the 1st version of code did not work, because we are deciding by looking at a single number every time, we need to check with all $[2, N-1]$ and then only decide.

```
let isPrime = true; (assume "it is prime")
for (let num = 2; num < N; num++) {
    if (N % num == 0) {
        isPrime = false;
        break;
    }
}
if (isPrime) console.log("prime")
else console.log("not prime")
```

* check/ flag variable



$25 \cdot 1, 5 = 0$
→ at least one number
is enough
meaningful

25
11
8
9
10
:
24

Further Improving check prime :

$(q \rightarrow q_5)$

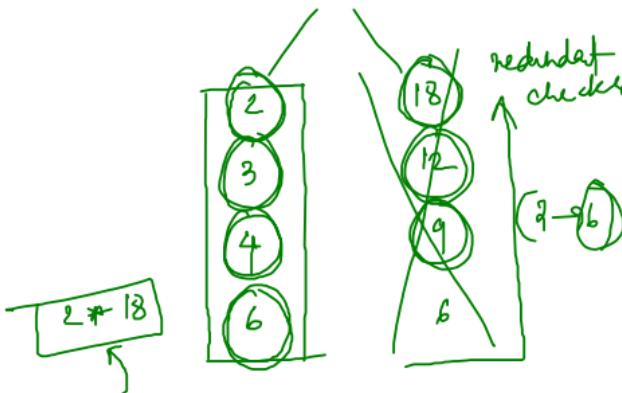
→ earlier approach takes N iterations / N checks

(can we decrease this checks / iterations) $\Rightarrow \sqrt{n}$ checker / iterations

e.g. :

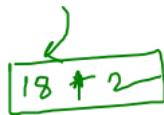
36

(factors of 36)



$$36 \% 2 == 0 \quad \text{Both are same}$$

$$36 \% 18 == 0$$



$$36 \% 2 == 0$$

$$36 \% 3 == 0$$

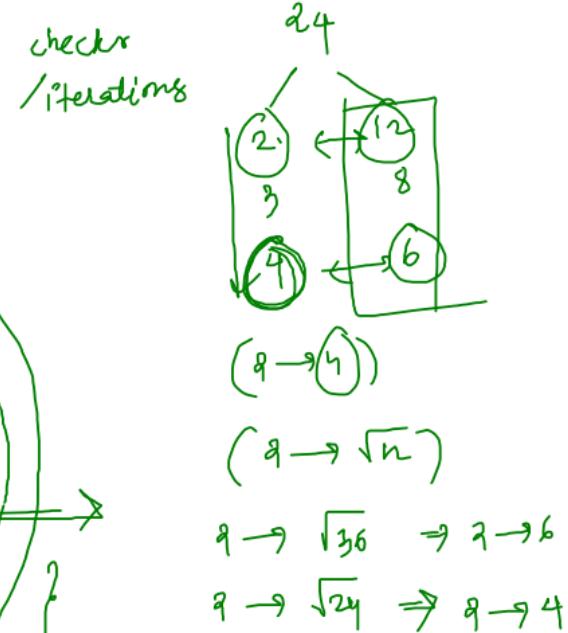
$$36 \% 4 == 0$$

$$36 \% 6 == 0$$

$$36 \% 9 == 0$$

$$36 \% 12 == 0$$

$$36 \% 18 == 0$$



$(q \rightarrow q_4)$

$(q \rightarrow \sqrt{n})$

$q \rightarrow \sqrt{36} \Rightarrow q \rightarrow 6$

$q \rightarrow \sqrt{24} \Rightarrow q \rightarrow 4$

36

$$1. \quad \textcircled{2}, \textcircled{3}, \textcircled{4}, 5, 6, 7, 8, \textcircled{9}, \dots \textcircled{18} \rightarrow 5 \quad (q \rightarrow N-1)$$

$$2. \quad 2, 3, 4, 5, 6 \quad (q \rightarrow \sqrt{n}) \rightarrow \text{why?}$$

$$36 \% \textcircled{9} = 0 \rightarrow \cancel{36 \% \textcircled{18} = 0}$$

are same checkers
(duplicates)

not necessary redundant

$$\cancel{36 \% \textcircled{4} = 0} \rightarrow \cancel{36 \% \textcircled{9} = 0}$$

4, 9
duplicates

$$\frac{36}{4} = \textcircled{9}$$

$$\frac{36}{9} = 4$$

$$num <= \sqrt{n}$$

$$(num)^2 <= (\sqrt{n})^2$$

$$(num)^2 <= n$$

$$num * num <= n \\ (or)$$

$$num * * 2 <= n$$

Q: Sum of digits :

Eg: $n = 1325$

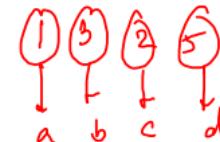
Op: $1+3+2+5 = 11$

Eg: $n = 565423$

Op: $5+6+5+4+2+3 = 25$

1. How do I get individual digits from a number?

$$1325 \cdot \frac{1}{10} = 5 \\ \downarrow \\ 1325/10$$



$$132 \cdot \frac{1}{10} = 2 \\ \downarrow \\ 132/10$$

$$\Rightarrow a+b+c+d$$

$$13 \cdot \frac{1}{10} = 3 \\ \downarrow \\ 13/10$$

$$1 \cdot \frac{1}{10} = 1$$

num $\cdot \frac{1}{10}$ (last dig)

→ remove last dig

$$\rightarrow \text{num} = \text{num}/10$$

$$\downarrow \\ 1/10$$

$$0 \times$$

~~$$1325 \cdot \frac{1}{10} = 5$$~~

$$132 \cdot \frac{1}{10} = 2$$

$$13 \cdot \frac{1}{10} = 1$$

$$1 \cdot \frac{1}{10} = 1$$

```

322 function SumofDigits(n) {
323   let sum = 0;
324   n = Number(n);
325   while (n > 0) {
326     const digit = n % 10; // extract digit
327     sum = sum + digit; // sum += digit;
328     n = parseInt(n / 10); // remove the digit
329   }
330
331   console.log(sum);
332 }

```

★ In 1st iteration, digit variable is created  and when the while loop or any other loop moves to the next iteration all the things that are newly created in previous iteration are deleted/removed. That means when it goes to 2nd iteration a one more new  is created, the old digit is lost already.

$$n = \cancel{1} \cancel{3} \cancel{2} 5 \quad \text{sum} = 0 \neq x 10 \text{ (1)}$$

$$\cancel{1} \cancel{3} \cancel{2} \cancel{1} \cancel{3} \times 0$$

① $1325 > 0$

$\text{digit} = 1325 \% 10 = 5$

 $\text{sum} = 0 + 5 = 5$
 $n = \text{pt}(1325/10) = 132$

③ $13 > 0$

 $\text{digit} = 13 \% 10 = 3$
 $\text{sum} = 7 + 3 = 10$
 $n = \text{pt}(13/10) = 1$

② $132 > 0$

 $\text{digit} = 132 \% 10 = 2$
 $\text{sum} = 5 + 2 = 7$
 $n = \text{pt}(132/10) = 13$

④ $1 > 0$

 $\text{digit} = 1 \% 10 = 1$
 $\text{sum} = 10 + 1 = 11$
 $n = \text{pt}(1/10) = 0$

⑤ $0 > 0$ (false)
terminate while

Q: Reverse a number :

$$\text{eg: } n = 1325$$

$$\text{op: } 5231$$

$$\begin{array}{r} 5 & 2 & 3 & 1 \\ 1000 & 100 & 10 & 1 \\ \downarrow & \downarrow & \downarrow & \downarrow \\ 1 & 3 & 2 & 5 \end{array}$$

$$\Rightarrow 1*5 + 10*2 + 100*3 + 1000*1$$

$$\Rightarrow 5 + 20 + 300 + 1000 = 1325$$

$$1325 \% 10 = 5$$

$$\begin{array}{r} 1325 \\ \% 10 \\ \downarrow \end{array}$$

$$132 \% 10 = 2$$

$$\begin{array}{r} 132 \\ \% 10 \\ \downarrow \end{array}$$

$$13 \% 10 = 3$$

$$\begin{array}{r} 13 \\ \% 10 \\ \downarrow \end{array}$$

$$1 \% 10 = 1$$

$$\begin{array}{r} \% 10 \\ \downarrow \\ 0 \times \end{array}$$

$$\text{rev} = 0$$

$$\text{rev} = \text{rev} * 10 + \text{digit}$$

$$\begin{aligned} ① \quad \text{rev} &= 0 * 10 + 5 \\ &= 0 + 5 = 5 \end{aligned}$$

$$\begin{aligned} ② \quad \text{rev} &= 5 * 10 + 2 \\ &= 50 + 2 = 52 \end{aligned}$$

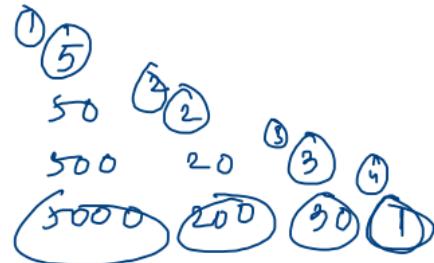
$$\begin{aligned} ③ \quad \text{rev} &= 52 * 10 + 3 \\ &= 520 + 3 = 523 \end{aligned}$$

$$\begin{aligned} ④ \quad \text{rev} &= 523 * 10 + 1 \\ &= 5230 + 1 = 5231 \end{aligned}$$

5231

$$\begin{array}{r} 1000 \ 100 \ 10 \ 1 \\ | \ 3 \ 2 \ 5 \end{array} \rightarrow \begin{array}{r} 1000 \ 100 \ 10 \ 1 \\ 5 \ 2 \ 3 \ 1 \end{array}$$

`rev = rev * 10 + d`



$$1325 \% 10 = 5 \neq 1000$$

$$132 \% 10 = 2 \neq 100$$

$$13 \% 10 = 3 \neq 10$$

$$1 \% 10 = 1 \neq 1$$

$$\overline{\overline{5000 + 200 + 30 + 1}} = 5231$$

- solve all problems of loops-1
 - (palindrome, HCF, power)
 - (armstrong numbers in range)
 - (link) u c hat (gym)

