

Exercise 4 (26.10.2015)

- 1) Read the rest of chapter 2 from Haykin's book (2nd edition). Summarize or sketch your insights in mind-map or an outline or a summary.
- 2) Consider the space of instances X corresponding to all points in the x, y plane. Give the VC dimension of the following hypothesis spaces:
 - a. H_r = the set of all rectangles in the x, y plane. i.e. $H_r = \{((a < x < b) \wedge (c < y < d)) \mid a, b, c, d \in \mathbb{R}\}$
 - b. H_c = the set of all circles in the x, y plane. Points inside the circle are classified as positive examples.
 - c. H_t = the set of all triangle in the x, y plane. Points inside the triangle are classified as positive examples.
- 3)

Definition: consistent learner

 - A learner is **consistent** if it outputs hypotheses that perfectly fit the training data, whenever possible. It is quite reasonable to ask that a learning algorithm be consistent, given that we typically prefer a hypothesis that fits the training data over one that does not.

Task:

 - Write a consistent learner for H_r from last Exercise (i.e. $H_r = \{((a < x < b) \wedge (c < y < d)) \mid a, b, c, d \in \mathbb{R}\}$). Generate a variety of target concept rectangles at random, corresponding to different rectangles in the plane. Generate random examples of each of these target concepts, based on a uniform distribution of instances within the rectangle from $(0,0)$ to $(100, 100)$. Plot the generalization error as a function of the number of training examples, m . On the same graph, plot the theoretical relationship between e and m , for $d = .95$. Does theory fit experiment?
- 4) Rephrase the Ex2.21 of chapter 2 from Haykin's book in such way that the next students will understand it better.
- 5) Please upload 3 questions and their brief answers on the reading material in a separate txt file.