



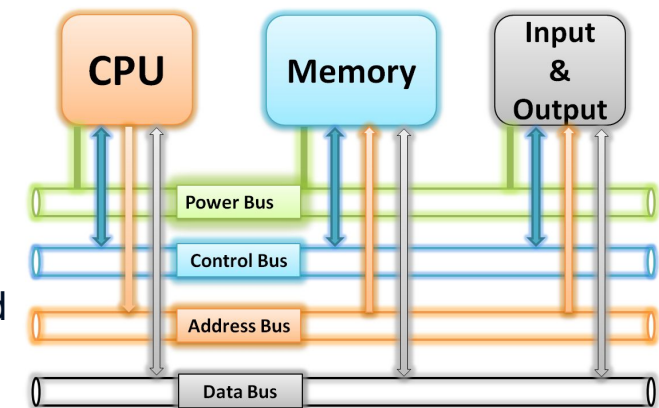
**Yrkes
Akademin**
Vi hjälper dig att lyckas!

Programming

Introduction

Computer System

- ❖ What is a computer system?
 - An electronic device designed to retrieve, process and store **data** using an **instruction set**.
- ❖ Basic System Architecture: three components connected to a bus system
 - Processor
 - The computing and controlling part of a computer system which processes data
 - Memory (RAM)
 - Is used by the processor to retrieve and store data
 - Is organized in bytes and every byte can be addressed
 - I/O Devices
 - Are used by the processor to communicate with the external world
- ❖ Instruction Set (typically 100 to 1000 micro instructions)
 - A set of primitive arithmetic, logical and controlling micro instructions executable by a processor.
 - E.g. Add two numbers, jump to an address, load/store data from/to memory, and etc.



Numbering Systems

- ❖ What is data? Binary numerical values.
- ❖ Base 10 numbering system (**decimal**)
 - There are **10** digits starting from **0** and ending to **9**.
 - All numbers are created by combining the **10** digits.
 - E.g. $123_{10} = 1 \times 10^2 + 2 \times 10^1 + 3 \times 10^0 = 123$
- ❖ Base 2 numbering system (**binary**)
 - There are only **2** digits; **0** and **1**. All numbers are created by combining the **2** digits.
 - E.g. $0b1011 = 1011_2 = 1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 1 \times 2^0 = 8 + 0 + 2 + 1 = 11_{10}$
- ❖ Base 8 numbering system (**octal**)
 - There are **8** digits; 0, 1, 2, 3, 4, 5, 6, 7. All numbers are created by combining the **8** digits.
 - E.g. $056_8 = 5 \times 8^1 + 6 \times 8^0 = 40 + 6 = 46_{10}$

Numbering Systems

❖ Base 16 numbering system (**hexadecimal**)

- There are **16** digits; 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, A, B, C, D, E and F.
- $A_{16} = 10_{10}$, $B_{16} = 11_{10}$, $C_{16} = 12_{10}$, $D_{16} = 13_{10}$, $E_{16} = 14_{10}$ and $F_{16} = 15_{10}$
- E.g. $0xF6_{16} = 15 \times 16^1 + 6 \times 16^0 = 240 + 6 = 246_{10}$

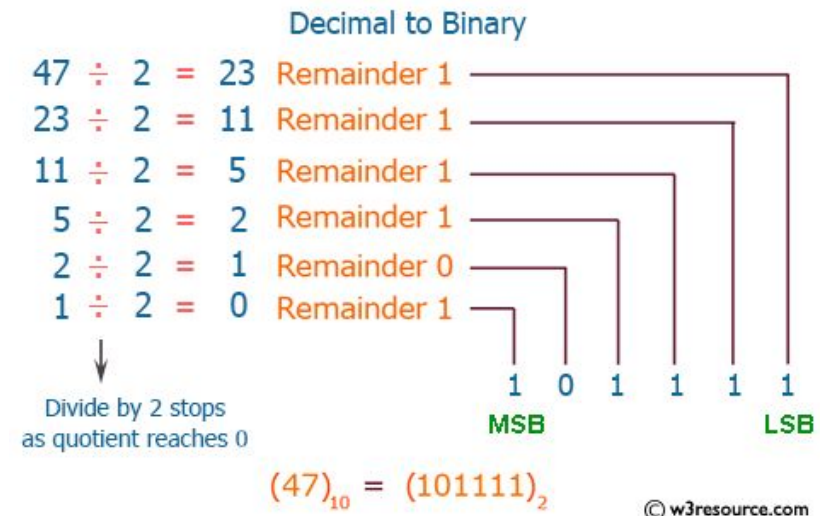
❖ Convert from **decimal** to **binary** and vice versa

➤ Decimal to binary

- Successive division by 2 of the decimal number until the result of the division gets 0. The remainders from bottom to top are the digits of the binary number.
- **MSB** means the **M**ost **S**ignificant **B**it
- **LSB** means the **L**east **S**ignificant **B**it

➤ Binary to Decimal: Sum of binary digits times 2 power of their position.

- E.g. $0b101010 = 1 \times 2^5 + 0 \times 2^4 + 1 \times 2^3 + 0 \times 1^2 + 1 \times 2^1 + 0 \times 2^0 = 32 + 0 + 8 + 0 + 2 + 0 = 42$



Numbering Systems

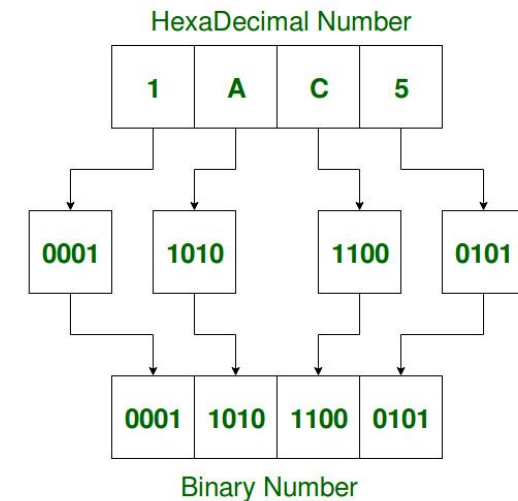
❖ Convert from **hexadecimal** to **binary** and vice versa

➤ Hexadecimal to binary

- Convert each hex digit to its equivalent 4 binary digits
- Discard any leading zeros at the left of the binary number.
- E.g. **0x1AC5** = 0001 1010 1100 0101 = **0b1101011000101**

➤ Binary to hexadecimal

- Every 4 binary digits (start from right) to its equivalent hex digit
- E.g. **0b1101011000101** = 0001 1010 1100 0101 = **0x1AC5**



❖ Binary arithmetic operations are like what we do for decimal numbers. For example

- Addition - probably we have some carry out numbers
- Subtraction - probably we need to borrow
- **Overflowing and borrowing an imaginary digit are possible**

$$\begin{array}{r}
 \begin{array}{ccccccc}
 & & 2 & 1 & & & \\
 & 0 & 0 & 2 & 2 & & \\
 1 & 1 & 0 & 0 & 1 & 1 & \\
 - & 1 & 1 & 1 & 0 & 0 & \\
 \hline
 & 1 & 0 & 1 & 1 & 1 &
 \end{array}
 \begin{array}{r}
 51 \\
 - 28 \\
 \hline
 23
 \end{array}
 \end{array}
 \qquad
 \begin{array}{r}
 \begin{array}{cccc}
 0 & 1 & 1 & 1 \\
 0 & 0 & 1 & 1 & 7 \\
 + & 1 & 0 & 1 & 0 & 1 & 21 \\
 \hline
 1 & 1 & 1 & 0 & 0 & = 28
 \end{array}
 \end{array}$$

Numbering Systems

❖ Binary negative numbers: 2's complement

- A placeholder is required. E.g. one byte \equiv 8 bits
- **MSB** is the sign bit. **0** means positive and **1** means negative
- Invert the digits and then add 1 to the inverted value.

The result is the negative value of the the positive number

0 0 0 1 0 1 0 0 → Binary number
1 1 1 0 1 0 1 1 → One's complement

| |
|-----------------|
| 1 1 1 0 1 0 1 1 |
| + 1 |
| 1 1 1 0 1 1 0 0 |

→ 2s complement

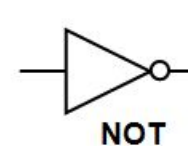
❖ Boolean Algebra

| TTL Voltage Level | CMOS Voltage Level | Voltage Level | Binary Value | Boolean Value |
|-------------------|--------------------|---------------|--------------|---------------|
| 0.0v - 0.5v | 0.0v - 0.8v | L (Low) | 0 | F (False) |
| 2.0v - 5.0v | 2.0v - 3.3v | H (High) | 1 | T (True) |

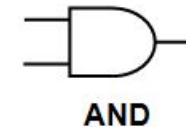
- TTL and CMOS voltage levels depend on the used technologies and input/output voltages are different
- In boolean algebra NOT, AND, OR, XOR and parentheses () operators are defined

Boolean Algebra and Symbols

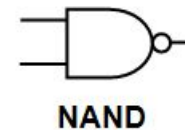
- ❖ **NOT** operator (\bar{A} , $!A$, $\sim A$)
- ❖ **OR** operator ($A + B$, $A || B$, $A | B$)
- ❖ **AND** operator ($A \bullet B$, $A \&\& B$, $A \& B$)
- ❖ **XOR** operator ($A \oplus B$, $!=$, \wedge)
- ❖ **Parentheses ()**
 - Are used to prioritize expressions
- ❖ **NAND** which is NOT AND
 - For example $\overline{A \bullet B}$
- ❖ **NOR** which is NOT OR
 - For example $\overline{A + B}$
- ❖ **XNOR** which is NOT XOR
 - For example $\overline{A \oplus B}$



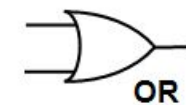
| Input Output | |
|--------------|---|
| I | F |
| 0 | 1 |
| 1 | 0 |



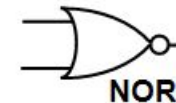
| Inputs | | Output |
|--------|---|--------|
| A | B | F |
| 0 | 0 | 0 |
| 1 | 0 | 0 |
| 0 | 1 | 0 |
| 1 | 1 | 1 |



| Inputs | | Output |
|--------|---|--------|
| A | B | F |
| 0 | 0 | 1 |
| 1 | 0 | 1 |
| 0 | 1 | 1 |
| 1 | 1 | 0 |



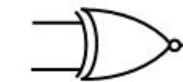
| Inputs | | Output |
|--------|---|--------|
| A | B | F |
| 0 | 0 | 0 |
| 1 | 0 | 1 |
| 0 | 1 | 1 |
| 1 | 1 | 1 |



| Inputs | | Output |
|--------|---|--------|
| A | B | F |
| 0 | 0 | 1 |
| 1 | 0 | 0 |
| 0 | 1 | 0 |
| 1 | 1 | 0 |



| Inputs | | Output |
|--------|---|--------|
| A | B | F |
| 0 | 0 | 0 |
| 0 | 1 | 1 |
| 1 | 0 | 1 |
| 1 | 1 | 0 |



EXCLUSIVE NOR

| Inputs | | Output |
|--------|---|--------|
| A | B | F |
| 0 | 0 | 1 |
| 0 | 1 | 0 |
| 1 | 0 | 0 |
| 1 | 1 | 1 |

EXCLUSIVE OR

Operators

❖ Logical operators

➤ Zero is interpreted as FALSE (0) and any number except zero is interpreted as TRUE (1)

➤ There are NOT(!), AND(&&) and OR(||)

➤ De Morgan's laws

■ $\overline{(A \bullet B)} = \bar{A} + \bar{B}$ and $\overline{(A + B)} = \bar{A} \bullet \bar{B}$

➤ Some examples

■ !0 is true, !12 is false, 12 && 0 is false, 0 || 12 is true, 0 != 12 is true and 0 == 12 is false

■ !(0 && 12) = (!0 || !12) = (1 || 0) = 1 (true) and !(0 || 12) = (!0 && !12) = (1 && 0) = 0 (false)

| A | B | \bar{A} | \bar{B} | $A+B$ | $A \cdot B$ | $\overline{A+B}$ | $\bar{A} \cdot \bar{B}$ | $\overline{A \cdot B}$ | $\bar{A} + \bar{B}$ |
|---|---|-----------|-----------|-------|-------------|------------------|-------------------------|------------------------|---------------------|
| 0 | 0 | 1 | 1 | 0 | 0 | 1 | 1 | 1 | 1 |
| 0 | 1 | 1 | 0 | 1 | 0 | 0 | 0 | 1 | 1 |
| 1 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 1 | 1 |
| 1 | 1 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 |

De Morgan's laws

❖ Relational Operators

➤ The defined relational operators are ==, !=, >, >=, < and <=

■ E.g. (7 == 12) is false, (7 != 12) is true, (7 > 12) is false, (7 >= 12) is false, (7 < 12) is true and (7 <= 12) is true

Operators

❖ Bitwise operators

- There are NOT(~), AND(&), OR(|), XOR(^), Shift to left(<<) and Shift to right(>>)
- Are used to perform bit-level operations
- A placeholder is required.
- Some examples
 - $5 \& 3 = 1$, $5 | 3 = 7$ and $5 \wedge 3 = 6$
 - $5 \gg 1 = 2$ and $5 \ll 1 = 10$
 - $\sim 0 = 0b11111111 = 255 = 0xFF$

| | Decimal value | | Binary value |
|-------------|---------------|---|--------------|
| Input 1 | 5 | | 00000101 |
| Input 2 | 3 | ➔ | 00000011 |
| | | | ↓ |
| Bitwise And | 1 | | 00000001 |
| Bitwise Or | 7 | ➔ | 00000111 |
| Bitwise XOR | 6 | | 00000110 |

| Operator | Description |
|----------|---------------------|
| & | Bitwise AND |
| | Bitwise OR |
| ^ | Bitwise XOR |
| ~ | Bitwise NOT |
| << | Bitwise left shift |
| >> | Bitwise right shift |

❖ Bit manipulation

- The memory is organized by bytes. Not possible to access data in bit level directly
- Using bitwise operators and masks we can manipulate data in the bit level
- E.g. to reset the second bit of 10101010 we can **AND** it with 11111101 => 10101000

Bit manipulation

- ❖ Setting the ***n*th** bit of a number (N bits)
 - Facts: $(D | 0) = D$ and $(D | 1) = 1$; D is a bit (0 or 1)
 - Result = $(\text{number} | (1 \ll n))$; $N > n \geq 0$
- ❖ Resetting(clearing) the ***n*th** bit of a number (N bits)
 - Facts: $(D \& 1) = D$ and $(D \& 0) = 0$; D is a bit (0 or 1)
 - Result = $(\text{number} \& \sim(1 \ll n))$; $N > n \geq 0$
- ❖ Toggling the ***n*th** bit of a number (N bits)
 - Facts: $(D \wedge 1) = \sim D$ and $(D \wedge 0) = D$; D is a bit (0 or 1)
 - Result = $(\text{number} \wedge (1 \ll n))$; $N > n \geq 0$
- ❖ Getting the value of the ***n*th** bit of a number (N bits)
 - $\text{bit_value} = (\text{number} \gg n) \& 1$; $N > n \geq 0$ and bit_value is 0 or 1
- ❖ Changing the value of the ***n*th** bit of a number (N bits)
 - Result = $(\text{number} \& \sim(1 \ll n)) | (D \ll n)$; $N > n \geq 0$ and **D** is 0 or 1

Example: Toggle the third bit of 53

```
00110101
^
00000100 = (1 << 2)
-----
00110001
```