Psy/Educ 6600: Unit 6 Homework

Categorical Data - Binomial and Chi Squared Tests

Your Name

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PREPARATION

Load Packages

Make sure the packages are **installed** (Package tab)

```
library(tidyverse)
                     # Loads several very helpful 'tidy' packages
library(readxl)
                      # Read in Excel datasets
library(furniture)
                    # Nice tables (by our own Tyson Barrett)
library(afex)
                     # Analysis of Factorial Experiments
library(emmeans)
                     # Estimated marginal means (Least-squares means)
library(lsmeans)
                     # Least-Squares Means
library(multcomp)
                     # Simultaneous Inference in General Parametric Models
library(pander)
                     # Make tables display nicer
```

Other Datasets for Section B's

```
coupleIQs <- data.frame(couple = 1:10,</pre>
                        boy
                               = c(110, 100, 120, 90, 108, 115, 122, 110, 127, 118),
                               = c(105, 108, 110, 95, 105, 125, 118, 116, 118, 126))
schizo metal <- data.frame(patient = 1:9,
                           year_2 = c(5, 7, 4, 2, 5, 3, 5, 6, 4),
                           year 3 = c(3, 6, 5, 2, 4, 4, 6, 5, 3)
woman_parents <- data.frame(home_broken</pre>
                                           = c(7, 3),
                            home\_complete = c(8, 12),
                            row.names = c("self divorced", "self married")) %>%
  as.matrix() %>%
  as.table()
react_wealth <- data.frame(poor</pre>
                                   = c(16, 8, 6),
                           middle = c(10, 6, 14),
                           wealthy = c(7, 5, 18),
                           row.names = c("ignores", "talks", "helps")) %>%
  as.matrix() %>%
  as.table()
speed_voice <- data.frame(child = c(5, 2),</pre>
                          woman = c(3, 4),
                          man = c(1, 6),
                          row.names = c("fast", "slow")) %>%
  as.matrix() %>%
  as.table()
data_12b4 <- data.frame(child = c(10, 12, 15, 11, 5, 7,
                        woman = c(17, 13, 16, 12, 7, 8, 3),
                        man = c(20, 25, 14, 17, 12, 18, 7)
```

Ihno's Dataset for Section C's

Import Data, Define Factors, and Compute New Variables

- Make sure the **dataset** is saved in the same *folder* as this file
- Make sure the that folder is the working directory

NOTE: I added the second line to convert all the variables names to lower case. I still kept the F as a capital letter at the end of the five factor variables.

```
ihno_clean <- read_excel("Ihno_dataset.xls") %>%
  dplyr::rename_all(tolower) %>%
  dplyr::mutate(genderF = factor(gender,
                                  levels = c(1, 2),
                                 labels = c("Female",
                                             "Male"))) %>%
  dplyr::mutate(majorF = factor(major,
                                levels = c(1, 2, 3, 4,5),
                                labels = c("Psychology",
                                            "Premed",
                                            "Biology",
                                            "Sociology",
                                            "Economics"))) %>%
  dplyr::mutate(reasonF = factor(reason,
                                 levels = c(1, 2, 3),
                                  labels = c("Program requirement",
                                             "Personal interest",
                                             "Advisor recommendation"))) %>%
  dplyr::mutate(exp_condF = factor(exp_cond,
                                    levels = c(1, 2, 3, 4),
                                   labels = c("Easy",
                                               "Moderate",
                                               "Difficult",
                                               "Impossible"))) %>%
  dplyr::mutate(coffeeF = factor(coffee,
                                 levels = c(0, 1),
                                 labels = c("Not a regular coffee drinker",
                                             "Regularly drinks coffee"))) %>%
  dplyr::mutate(hr_base_bps = hr_base / 60)
```

Chapter 19: Binomial Distribution

coupleIQs - Paired Measures: Teenage Couple IQs

11B 6: Matched t-Test (1-sided)

TEXTBOOK QUESTION: Do teenage boys tend to date teenage girls who have a lower IQ than they do? To try to answer this question, 10 teenage couples (i.e., who are dating regularly) are randomly selected, and each member of each couple is given an IQ test. The results are given in the following table (each column represents a different couple):

coupleIQs %>% pander::pander()

couple	boy	girl
1	110	105
2	100	108
3	120	110
4	90	95
5	108	105
6	115	125
7	122	118
8	110	116
9	127	118
10	118	126

TEXTBOOK QUESTION: Perform a one-tailed matched t test ($\alpha = .05$) to determine whether the boys have higher IQs than their girlfriends. What can you conclude?

NOTE: The homework skeleton shows the two-tailed test by mistake.

Paired t-test

19B 2: Sign Test (1-sided)

TEXTBOOK QUESTION: Perform the sign test on the data from Exercise 11B6 using the same alpha level and number of tails. Did you reach the same conclusion with the sign test as with the matched t test? If not, explain the discrepancy.

couple	boy	girl	sign
1	110	105	positive
2	100	108	negative
3	120	110	positive
4	90	95	negative
5	108	105	positive
6	115	125	negative
7	122	118	positive
8	110	116	negative
9	127	118	positive
10	118	126	negative

```
coupleIQs_table <- coupleIQs_wide %>%
  dplyr::select(sign) %>%
  table()

coupleIQs_table %>% pander::pander()
```

negative	positive
5	5

```
coupleIQs_table %>%
binom.test(alternative = "greater")
```

Exact binomial test

schizo_mental - Repeated Measures: Mental condition over time

19B 3: Sign Test

year_2	$year_3$	sign
		0
5	3	decline
7	6	decline
4	5	gain
2	2	NA
5	4	decline
3	4	$_{ m gain}$
5	6	$_{ m gain}$
6	5	decline
4	3	decline
	7 4 2 5 3 5	7 6 4 5 2 2 5 4 3 4 5 6 6 5

```
schizo_metal_table <- schizo_metal_wide %>%
  dplyr::select(sign) %>%
  table()

schizo_metal_table %>% pander::pander()
```

decline	gain
5	3

```
schizo_metal_table %>%
binom.test() # default: alternative = "two.sided"
```

Exact binomial test

Chapter 20: Chi-Squared Tests

Tutorials: Chi-squared Test

Goodenss of Fit (1-way) - Equally Likely

TEXTBOOK Example: Often, especially in an experimental context, the expected frequencies are based on more abstract theoretical considerations. For instance, imagine that a developmental psychologist is studying color preference in toddlers. Each child is told that he or she can take one toy out of four that are offered. All four toys are identical except for color: red, blue, yellow, or green. Forty children are run in the experiment, and their color preferences are as follows: red, 13; blue, 9; yellow, 15; and green, 3. These are the obtained frequencies. The expected frequencies depend on the null hypothesis. If the null hypothesis is that toddlers in general have no preference for color, we would expect the choices of colors to be equally divided among the entire population of toddlers. Hence, the expected frequencies would be 10 for each color.

Use the chisq.test() function to perform a Goodnes-of-Fit or one-way Chi-Squared test to see if the observed counts are significantly different from being equally distributed.

NOTE: You do not need to declare any options inside the chisq.test() function, as the default is to use equally likely probabilities.

The following code chunk shows how to create and display a table of the observed and expected counts for any 1-way Chi-squated test.

HINT You may *copy-and-paste* this code for the rest of the assignment, but make sure to change the name of the model (chisq toy color appears twice before the \$-sign).

	red	blue	yellow	green
Observed	13	9	15	3
Expected	10	10	10	10

To display the full output, type and run the name the model is save as.

```
# Diplay the full output
chisq_toy_color
```

```
Chi-squared test for given probabilities
```

```
data: .
X-squared = 8.4, df = 3, p-value = 0.03843
```

Goodenss of Fit (1-way) - Hypothesised Probabilities

TEXTBOOK Example: Imagine that the population of a city is made up of three ethnic groups, which I will label A, B, and C. The obtained frequencies were 28, 18, and 2. You could test the null hypothesis that sample is representative of a population proportions which is half group A and a third group B.

The chisq.test() function may also be used to perform a Goodnes-of-Fit or one-way Chi-Squared test to see if the observed counts are significantly different from those expected from a set of hypothesised probabilies.

NOTE: You **DO** need to declare the probabilities, as the default is to use equally likely probabilities. You may do this by including $p = c(p_1, p_2, \ldots, p_k)$ within the chisq.test() function. The p_i 's maybe typed as decimals or fractions, but make suer they add up to exactly 1!

Use the same code chunk to display a table of the observed and expected counts for any 1-way Chi-squated test.

HINT You may *copy-and-paste* this code for the rest of the assignment, but make sure to change the name of the model (chisq_ethnic appears twice before the \$-sign).

	A	В	С
Observed	28	18	2
Expected	24	16	8

To display the full output, type and run the name the model is save as.

```
# Diplay the full output chisq_ethnic
```

```
Chi-squared test for given probabilities
```

```
data: .
X-squared = 5.4167, df = 2, p-value = 0.06665
```

Test for Independence (2-way) - vs. Association

TEXTBOOK Example: Suppose that the researcher has interviewed 30 women who have been married: 10 whose parents were divorced and 20 whose parents were married. Half of the 30 women in this hypothetical study have gone through their own divorce; the other half are still married for the first time. To know whether the divorce of a person's parents makes the person more likely to divorce, we need to see the breakdown in each category- that is, how many currently divorced women come from "broken" homes and how many do not, and similarly for those still married. These frequency data are generally presented in a contingency (or cross-classification) table:

```
# Display the observed counts
woman_parents %%
addmargins() %>%
pander::pander()
```

	home_broken	home_complete	Sum
$\operatorname{self_divorced}$	7	8	15
\mathbf{self} _married	3	12	15
\mathbf{Sum}	10	20	30

The chisq.test() function may also be used to perform a two-way Chi-Squared test for independence. In this case, the observed counts are compared to those expected if there is no association between the two factors.

```
# Run the 2-way chi-square test for independence
chisq_divorces <- woman_parents %>%
    chisq.test(correct = FALSE) #IF 2x2, add correct = FALSE
```

To display the counts expected if the variables are independent, start with the model name and add \$expected at the end. Then pipe on both the addmargins() and pander::pander() functions to print the counts.

```
# Request the expected counts based on "no association"
chisq_divorces$expected %>%
  pander::pander()
```

	home_broken	home_complete
self_divorced	5	10
self _married	5	10

To display the full output, type and run the name the model is save as.

```
# Diplay the full output
chisq_divorces
```

```
Pearson's Chi-squared test
```

```
data: .
X-squared = 2.4, df = 1, p-value = 0.1213
```

Blind taste test of soft drinks (given counts)

20A 3: 1-way Chi-squared Test - Goodness-of-Fit (equally likely)

TEXTBOOK QUESTION: A soft drink manufacturer is conducting a blind taste test to compare its best-selling product (X) with two leading competitors (Y and Z). Each subject tastes all three and selects the one that tastes best to him or her. (a) What is the appropriate null hypothesis for this study? (b) If 27 subjects prefer product X, 15 prefer product Y, and 24 prefer product Z, can you reject the null hypothesis at the .05 level?

DIRECTIONS: Use the chisq.test() function to perform a Goodnes-of-Fit or one-way Chi-Squared test to see if the observed counts (c(X = 27, Y = 15, Z = 24)) are significantly different from being equally distributed among the three soft drinks. Save the fitted model as chisq_soda.

NOTE: You do not need to declare any options inside the chisq.test() function, as the default is to use equally likely probabilities.

Run the 1-way chi-square test for equally likely

DIRECTIONS: Follow the tutorial to create a table comparing the observed and expected counts.

HINT You may *copy-and-paste* the code from the chunked named tutorial_chiSq_GoF_EL_counts, but remember to change the name of the model (appears before the \$-sign in two places).

Request the observed and expected counts

DIRECTIONS: Place the model's name (chisq_soda) in the following chunck, so that when run it will display the full output of the Chi-squared test.

Psychiatric Hospital Admits by Season

20A 7: 1-way Chi-squared Test - Goodness-of-Fit (equally likely)

TEXTBOOK QUESTION: It has been suggested that admissions to psychiatric hospitals may vary by season. One hypothetical hospital admitted 100 patients last year: 30 in the spring; 40 in the summer; 20 in the fall; and 10 in the winter. Use the chi-square test to evaluate the hypothesis that mental illness emergencies are evenly distributed throughout the year.

DIRECTIONS: Use the chisq.test() function to perform a Goodnes-of-Fit or one-way Chi-Squared test to see if the observed counts (c(spring = 30, summer = 40, fall = 20, winter = 10)) are significantly different from being equally distributed among the four seasons. Save the fitted model as chisq season.

NOTE: You do not need to declare any options inside the chisq.test() function, as the default is to use equally likely probabilities.

Run the 1-way chi-square test for equally likely

DIRECTIONS: Follow the tutorial to create a table comparing the observed and expected counts.

HINT You may *copy-and-paste* the code from the chunked named tutorial_chiSq_GoF_EL_counts, but remember to change the name of the model (appears before the \$-sign in two places).

Request the observed and expected counts

DIRECTIONS: Place the model's name (chisq_season) in the following chunck, so that when run it will display the full output of the Chi-squared test.

20A 8: 1-way Chi-squared Test - Goodness-of-Fit (hypothesised probabilities)

TEXTBOOK QUESTION: Of the 100 psychiatric patients referred to in the previous exercise, 60 were diagnosed as schizophrenic, 30 were severely depressed, and 10 had a bipolar disorder. Assuming that the national percentages for psychiatric admissions are 55% schizophrenic, 39% depressive, and 6% bipolar, use the chi-square test to evaluate the null hypothesis that this particular hospital is receiving a random selection of psychiatric patients from the national population.

DIRECTIONS: Use the chisq.test() function to perform a Goodnes-of-Fit or one-way Chi-Squared test to see if the observed counts (c(Schizophrenic = 60, Depressed = 30, Bipolar = 10)) are significantly different from being equally distributed among the three diagnoses. Save the fitted model as chisq rx.

NOTE: You **DO** need to declare the probabilities, as the default is to use equally likely probabilities. You may do this by including p = c(.55, .39, .06) within the chisq.test() function.

Run the 1-way chi-square test for hypothesized probabilities

DIRECTIONS: Follow the tutorial to create a table comparing the observed and expected counts.

HINT You may *copy-and-paste* the code from the chunked named tutorial_chiSq_GoF_EL_counts, but remember to change the name of the model (appears before the \$-sign in two places).

Request the observed and expected counts

DIRECTIONS: Place the model's name (chisq_rx) in the following chunck, so that when run it will display the full output of the Chi-squared test.

react wealth Reaction to Wealth

20B 4: 2-way Chi-squared Test - Independence

TEXTBOOK QUESTION: A social psychologist is studying whether people are more likely to help a poor person or a rich person who they find lying on the floor. The three conditions all involve an elderly woman who falls down in a shopping mall (when only one person at a time is nearby). The independent variable concerns the apparent wealth of the woman; she is dressed to appear either poor, wealthy, or middle class. The reaction of each bystander is classified in one of three ways: ignoring her, asking if she is all right, and helping her to her feet. The data appear in the contingency table below. (a) Test the null hypothesis at the .01 level. Is there evidence for an association between the apparent wealth of the victim and the amount of help provided by a bystander? (b) Calculate Cramer's phi for these data. What can you say about the strength of the relationship between the two variables?

Display the observed counts
react_wealth %>%
 addmargins() %>%

pander::pander()

	poor	middle	wealthy	Sum
ignores	16	10	7	33
talks	8	6	5	19
\mathbf{helps}	6	14	18	38
\mathbf{Sum}	30	30	30	90

DIRECTIONS: Use the chisq.test() function to perform a two-way Chi-Squared test for independence to see if the observed counts provide evidence of an association between the level of wealth and reaction. Save the fitted model as chisq_react_wealth.

NOTE: You do not need to declare any options inside the chisq.test() function, as the default is test for independence when given a table. The correct = FALSE id needed only for 2x2 tables.

Run the 2-way chi-square test for independence

DIRECTIONS: Display the counts expected if reaction is independent of wealth by starting with the model name chisq_react_wealth and adding \$expected at the end.

Request the expected counts based on "no association"

DIRECTIONS: Place the model's name (chisq_react_wealth) in the following chunck, so that when run it will display the full output of the Chi-squared test.

speed_voice Dichotimize Reaction Time to Voice Calling for Help

20B 8: 2-way Chi-squared Test - Independence

TEXTBOOK QUESTION: In Exercise 12B4, the dependent variable was the amount of time a subject listened to taperecorded cries for help from the next room before getting up to do something. If some subjects never respond within the time allotted for the experiment, the validity of using parametric statistical techniques could be questioned. As an alternative, subjects could be classified as fast or slow responders (and possibly, nonresponders). The data from Exercise 12B4 were used to classify subjects as fast responders (less than 12 seconds to respond) or slow responders (12 seconds or more). The resulting contingency table is shown in the following table:

Display the observed counts
speed_voice %>%
 addmargins() %>%
 pander::pander()

	child	woman	man	Sum
fast	5	3	1	9
\mathbf{slow}	2	4	6	12
Sum	7	7	7	21

TEXTBOOK QUESTION: (a) Test the null hypothesis ($\alpha = .05$) that speed of response is independent of type of voice heard.

DIRECTIONS: Use the chisq.test() function to perform a two-way Chi-Squared test for independence to see if the observed counts provide evidence of an association between the level of wealth and reaction. Save the fitted model as chisq_speed_voice.

NOTE: You do not need to declare any options inside the chisq.test() function, as the default is test for independence when given a table. The correct = FALSE id needed only for 2x2 tables.

Run the 2-way chi-square test for independence

DIRECTIONS: Display the counts expected if reaction is independent of wealth by starting with the model name chisq_speed_voice and adding \$expected at the end.

Request the expected counts based on "no association"

DIRECTIONS: Place the model's name (chisq_speed_voice) in the following chunck, so that when run it will display the full output of the Chi-squared test.

Diplay the full output

TEXTBOOK QUESTION: (b) How does your conclusion in part a compare with the conclusion you drew in Exercise 12B4? Categorizing the dependent variable throws away information; how do you think that loss of information affects power?

data_12b4 %>%
 pander::pander()

child	woman	man
10	17	20
12	13	25
15	16	14
11	12	17
5	7	12
7	8	18
2	3	7

```
data_12b4 %>%
 tidyr::gather(key = voice,
               value = seconds,
               child, woman, man) %>%
 dplyr::mutate(voice = factor(voice,
                              levels = c("child", "woman", "man"))) %>%
 dplyr::mutate(id = row_number()) %>%
 afex::aov_4(seconds ~ voice + (1|id),
             data = .) %>%
 summary()
Anova Table (Type 3 tests)
Response: seconds
                                     ges Pr(>F)
     num Df den Df
                      MSE
                               F
voice
               18 26.476 3.7464 0.29392 0.04362 *
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

ihno clean Ihno's Dataset

20C 1a: 1-way Chi-squared Test - Goodness-of-Fit (equally likely)

TEXTBOOK QUESTION: (a) Perform a one-way chi square test to determine whether you can reject the null hypothesis that, at Ihno's university, there are the same number of students majoring in each of the five areas represented in Ihno's class, if you assume that Ihno's students represent a random sample with respect to major area.

DIRECTIONS: Use the chisq.test() function to perform a Goodnes-of-Fit or one-way Chi-Squared test to see if the observed counts are significantly different from being equally distributed among the five majors. Save the fitted model as chisq_ihno_major.

HINT: Since you are working from a full dataset, you will need to pipe a dplyr::select(majorF) step onto the ihno_clean dataset to first select out just the majorF variable and then pipe on the table() function to tablulate the observed counts for each major. Then and only then, you may add the chisq.test() function.

NOTE: You do not need to declare any options inside the chisq.test() function, as the default is to use equally likely probabilities.

Run the 1-way chi-square test for equally likely

DIRECTIONS: Follow the tutorial to create a table comparing the observed and expected counts.

HINT You may *copy-and-paste* the code from the chunked named tutorial_chiSq_GoF_EL_counts, but remember to change the name of the model (appears before the \$-sign in two places).

Request the observed and expected counts

DIRECTIONS: Place the model's name (chisq_ihno_major) in the following chunck, so that when run it will display the full output of the Chi-squared test.

20C 1b: Repeat, separately for each gender

"Female".

TEXTBOOK QUESTION: (b) Perform the test in part a separately for both the males and the females in Ihno's class.
DIRECTIONS: Perform the same test you did in part a, but separately for each level of the gender variable HINT You may <i>copy-and-paste</i> the code from the chunked named 20c1a_chiSq_GoF_EL_test, but do NOT same the model as anything.
NOTE: You will need to add a dplyr::filter(genderF == "Male") step before the selecting of major.
HINT You may copy-and-paste the code chunk directly above, changing only "Male" to

20C 3: 2-way Chi-squared Test - Independence

TEXTBOOK QUESTION: Conduct a two-way chi-square analysis of Ihno's data to test the null hypothesis that the proportion of females is the same for each of the five represented majors in the entire university population. Request a statistic to describe the strength of the relationship between gender and major.

NOTE: The furniture package includes a very helpful function called tableX() which creates a nice cross-tabulation given the names of two variables.

```
ihno_clean %>%
  furniture::tableX(genderF, majorF)
genderF
        Psychology Premed Biology Sociology Economics Total
  Female 19
                            11
                                     12
                                               4
                                                          57
  Male
                     14
                            10
                                     3
                                               6
                                                          43
         10
  Total
         29
                     25
                            21
                                     15
                                               10
                                                          100
```

DIRECTIONS: Use the chisq.test() function to perform a two-way Chi-Squared test for independence to see if the observed counts are significantly different from those expected is there is no association between gender and major.

HINT: Since you are working from a full dataset, you will need to pipe a dplyr::select(genderF, majorF) step onto the ihno_clean dataset to first select out just the genderF and majorF variables. Then pipe on the table() function to cross-tablulate the observed counts. Then and only then, you may add the chisq.test() function.

NOTE: If you do not save the model to a name, the full output will be displayed.