

Please complete the following exercises. Feel free to work with classmates, but each student must turn in **UNIQUE** work, not photocopies or identical replicates. When applicable, use **APA format** in communicating your results in text. **Show your work!** If any question involves any math at all, show your work. When it doubt, write it out. Always show more than you think you need.

1) WRITE-UP - Textbook Problems

Cohen Chap	Exercises	Pts	Off
5	A *1, 2, *5, 6, 7, 9, 10	5	
	B *1, *8, 9, *10 11, 12, 13 ←Advance Section	5	
	C 3, 4	2	
6	A *1, 2, 4, *5, 6	5	
	B *1, 2, *4, 5, 8	5	
	C 1, 2, 3	2	
7	A *7, 8	2	
	B *3, *4, 6	3	
	C 1, 5	2	
8	A 3, 9, *10	3	
	B 6	1	
	C 2 (altered) (Use G-Power, no syntax or code)	1	

2) SUMMARY – Supplementary Reading

The ASA's Statement on p-Values: Context, Process, and Purpose	Pts	Off
Half Page Read the article and summarize the main points for future reference.	5	

3) R SYNTAX – Section C: Ihno's data set – add to the skeleton R notebook and knit to .pdf & upload

Cohen Chap	Exercises	Pts	Off
5	C 3, 4	2	
6	C 1, 2, 3	2	
7	C 1, 2, 3, 4, 5	5	

Grading

		Earned	Possible
CORRECTNESS	<i>a subset of spot-checked items: must show work, especially items from back of book or done in class</i>		50
COMPLETENESS	<i>more than one item is missing or skipped: 25/50 roughly half the assignment is completed: 10/50</i>		50
		<div style="border: 2px solid black; width: 100px; height: 20px;"></div>	100

5 A *1. Calculated z-value → p-value ... 1-tailed & 2-tailed

a) If the **calculated z** for an experiment equals **1.35**, what is the corresponding **p-value**?

1-tail: p = _____ 2-tail: p = _____

b) If the **calculated z** for an experiment equals **- 0.7**, what is the corresponding **p-value**?

1-tail: p = _____ 2-tail: p = _____

c) If the **calculated z** for an experiment equals **2.2**, what is the corresponding **p-value**?

1-tail: p = _____ 2-tail: p = _____

5 A 2. alpha → critical z-value ... 1-tailed & 2-tailed

a) If **alpha** were set to the unusual value of **.08**, what would be the magnitude of the **critical z**?

1-tail: z_{cv} = _____ 2-tail: z_{cv} = _____

b) If **alpha** were set to the unusual value of **.03**, what would be the magnitude of the **critical z**?

1-tail: z_{cv} = _____ 2-tail: z_{cv} = _____

c) If **alpha** were set to the unusual value of **.007**, what would be the magnitude of the **critical z**?

1-tail: z_{cv} = _____ 2-tail: z_{cv} = _____

5 A *5. sample mean → p-value (2-tailed)

An English professor suspects that her current class of **36 students** is unusually good at verbal skills. She looks up the verbal SAT score for each student and is pleased to find that the **mean for the class is 540**.

Assuming that the general population of students has a **mean verbal SAT score of 500** with a **standard deviation of 100**, what is the **two-tailed** p value corresponding to this class?

POPULATION PARAMETERS

μ = _____

σ = _____

n = _____

SAMPLE STATISTICS

\bar{X} = _____

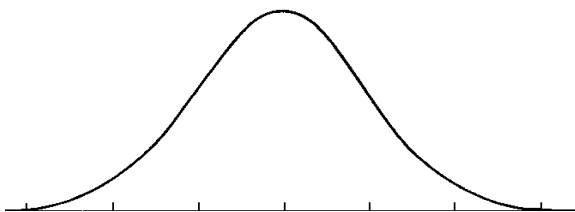
$\sigma_{\bar{X}}$ = _____

**Standard Error
for the Mean**

$$\sigma_{\bar{X}} = \frac{\sigma}{\sqrt{n}}$$

Formula 5.1

$$z = \frac{\bar{X} - \mu}{\sigma_{\bar{X}}}$$



z = _____

2-tail: p = _____

Consider a situation in which you have **calculated the z score** for a group of participants and have obtained the unusually high value of **20**.

Which of the following statements would be **true**, and which would be **false**?

Explain your answer in each case.

a.) You must have made a calculation error because z scores cannot get so high.

☐ TRUE ☐ FALSE **EXPLAIN.**

b.) The null hypothesis cannot be true.

☐ TRUE ☐ FALSE **EXPLAIN.**

c.) The null hypothesis can be rejected, even if a very small alpha is used.

☐ TRUE ☐ FALSE **EXPLAIN.**

d.) The difference between the sample mean and the hypothesized population mean must have been quite large.

☐ TRUE ☐ FALSE **EXPLAIN.**

5	A	7. Very large z-score
Suppose the z score mentioned in Exercise 6 involved the measurement of height for a group of men. If $\mu = 69$ inches and $\sigma = 3$ inches, <u>how</u> can a group of men have a z score equal to 20?		
Give a numerical example illustrating how this can occur.		
5	A	9. One-tail vs. Two-tails
Describe a situation in which a one-tailed hypothesis test seems justified.		
Describe a situation in which a two-tailed test is clearly called for.		
5	A	10. One-tail vs. Two-tails
Describe a case in which it would probably be appropriate to use an alpha smaller than the conventional .05 (e.g., .01).		
Describe a case in which it might be appropriate to use an unusually large alpha (e.g., .1).		

A psychiatrist is testing a new antianxiety drug, which seems to have the potentially harmful side effect of lowering the heart rate. For a **sample of 50** medical students whose pulse was measured after 6 weeks of taking the drug, the **mean heart rate was 70 beats per minute (bpm)**.

If the mean heart rate for the **population** is **72 bpm** with a **standard deviation of 12**, can the psychiatrist conclude that the new drug lowers heart rate significantly? (Set $\alpha = .05$ and perform a one-tailed test.)

POPULATION PARAMETERS

$$\mu = \underline{\hspace{2cm}}$$

$$\sigma = \underline{\hspace{2cm}}$$

SAMPLE STATISTICS

$$\bar{X} = \underline{\hspace{2cm}}$$

$$\sigma_{\bar{X}} = \underline{\hspace{2cm}}$$

$$n = \underline{\hspace{2cm}}$$

$$H_0 : \underline{\hspace{2cm}}$$

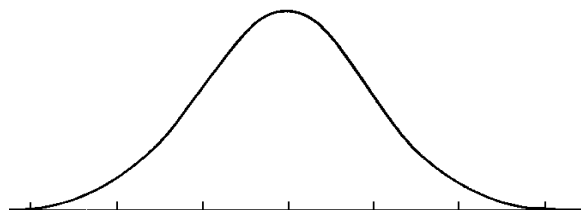
$$H_a : \underline{\hspace{2cm}}$$

Standard Error
for the Mean

$$\sigma_{\bar{X}} = \frac{\sigma}{\sqrt{n}}$$

Formula 5.1

$$z = \frac{\bar{X} - \mu}{\sigma_{\bar{X}}}$$



$$z = \underline{\hspace{2cm}}$$

$$1\text{-tail: } p = \underline{\hspace{2cm}}$$

- ☐ Provides evidence that new drug lowers heart rate
- ☐ No evidence that the new drug lowers heart rate

Imagine that you are testing a new drug that seems to **raise** the number of T cells in the blood and therefore has enormous potential for the treatment of disease. After treating **100 patients**, you find that their **mean T cell count is 29.1**. Assume that μ and σ (hypothetically) are **28 and 6**, respectively.

POPULATION PARAMETERS

$$\mu = \underline{\hspace{2cm}}$$

$$\sigma = \underline{\hspace{2cm}}$$

SAMPLE STATISTICS

$$\bar{X} = \underline{\hspace{2cm}}$$

$$\sigma_{\bar{X}} = \underline{\hspace{2cm}}$$

$$n = \underline{\hspace{2cm}}$$

$$H_0 : \underline{\hspace{2cm}}$$

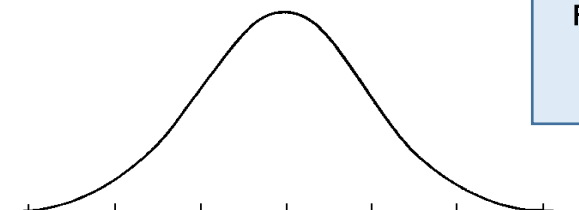
$$H_a : \underline{\hspace{2cm}}$$

Standard Error
for the Mean

$$\sigma_{\bar{X}} = \frac{\sigma}{\sqrt{n}}$$

Formula 5.1

$$z = \frac{\bar{X} - \mu}{\sigma_{\bar{X}}}$$



$$z = \underline{\hspace{2cm}}$$

$$\text{2-tail: } p = \underline{\hspace{2cm}}$$

- a.) Test the null hypothesis at the **.05 level, two-tailed.**

- ☐ Provides evidence that new drug increases T cells
☐ No evidence that the new drug increases T cells

- b.) Test the same hypothesis at the **.10 level, two-tailed.**

- ☐ Provides evidence that new drug increases T cells
☐ No evidence that the new drug increases T cells

- c.) **Describe** in practical terms what it would mean to **commit a Type I error** in this example.

- d.) **Describe** in practical terms what it would mean to **commit a Type II error** in this example.

- e.) How might you **justify** the use of .10 for alpha in similar experiments?

- a) Assuming everything else in the previous problem stayed the same, what would happen to your calculated z if the **population standard deviation (σ)** were **3** instead of **6**?

Standard Error
for the Mean

$$\sigma_{\bar{X}} = \frac{\sigma}{\sqrt{n}}$$

Formula 5.1

$$z = \frac{\bar{X} - \mu}{\sigma_{\bar{X}}}$$

$$z = \underline{\hspace{2cm}} \rightarrow \underline{\hspace{2cm}}$$

- b) What **general statement** can you make about how changes in σ affect the calculated value of z ?

Referring to Exercise 8, suppose that **mean (\bar{X}) is equal to 29.1** *regardless of the sample size*.

How large would n have to be for the calculated z to be statistically significant at the **.01 level (two-tailed)**?

Formula 5.1

$$z = \frac{\bar{X} - \mu}{\sigma_{\bar{X}}}$$

$$n = \underline{\hspace{2cm}}$$

5 B 11. Define 'alpha'

Alpha stands for which of the following?

- a) The proportion of experiments that will attain statistical significance ☐ TRUE
- b) The proportion of experiments for which the null hypothesis is true that will attain statistical significance ☐ TRUE
- c) The proportion of statistically significant results for which the null hypothesis is true ☐ TRUE
- d) The proportion of experiments for which the null hypothesis is true ☐ TRUE

5 B 12. Errors in hypothesis testing

In the last few years, an organization has conducted **200 clinical trials** to test the effectiveness of antianxiety drugs.

Suppose, however, that **all** of those drugs were obtained from the same **fraudulent** supplier, which was later revealed to have been sending only inert substances (e.g., distilled water, sugar pills) instead of real drugs. If **alpha = .05** was used for all hypothesis tests...

How many **of these 200** experiments would you expect to **yield significant** results?

How many **Type I errors** would you expect?

How many **Type II errors** would you expect?

5 B 13. Errors in hypothesis testing

Since she arrived at the university, Dr. Pine has been very productive and successful. She has already performed **20 experiments** that have **each** attained the **.05** level of statistical significance.

What is your best guess for the number of **Type I errors** she has made so far?

For the number of **Type II errors**?

- a) In the past 10 years, previous stats classes who took the same **mathquiz** that Ihno's students took averaged 28 with a standard deviation of 8.5. What is the **two-tailed p value** for Ihno's students with respect to that past population? (Don't forget that the *N* for mathquiz is not 100.)

write code to find mean & n in your R syntax file

POPULATION PARAMETERS

$$\mu = \underline{\hspace{2cm}}$$

$$\sigma = \underline{\hspace{2cm}}$$

$$n = \underline{\hspace{2cm}}$$

SAMPLE STATISTICS

$$\bar{X} = \underline{\hspace{2cm}}$$

$$\sigma_{\bar{X}} = \underline{\hspace{2cm}}$$

$$H_0 : \underline{\hspace{2cm}}$$

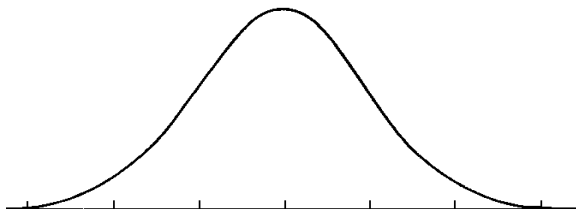
$$H_a : \underline{\hspace{2cm}}$$

Standard Error
for the Mean

$$\sigma_{\bar{X}} = \frac{\sigma}{\sqrt{n}}$$

Formula 5.1

$$z = \frac{\bar{X} - \mu}{\sigma_{\bar{X}}}$$



$$z = \underline{\hspace{2cm}}$$

$$\text{2-tail: } p = \underline{\hspace{2cm}}$$

Would you say that Ihno's class performed **significantly better** than previous classes?

☐ Provides evidence Ihno's class performed **significantly better** than previous classes

☐ No evidence that Ihno's class performed any differently than previous classes

EXPLAIN.

- b) In the past 10 years, previous stats classes who took the same **statquiz** that Ihno's students took averaged 6.1 with a standard deviation of 2.5. What is the **two-tailed p value** for Ihno's students with respect to that past population?

write code to find mean & n in your R syntax file

POPULATION PARAMETERS

$$\mu = \underline{\hspace{2cm}}$$

$$\sigma = \underline{\hspace{2cm}}$$

$$n = \underline{\hspace{2cm}}$$

SAMPLE STATISTICS

$$\bar{X} = \underline{\hspace{2cm}}$$

$$\sigma_{\bar{X}} = \underline{\hspace{2cm}}$$

$$H_0 : \underline{\hspace{2cm}}$$

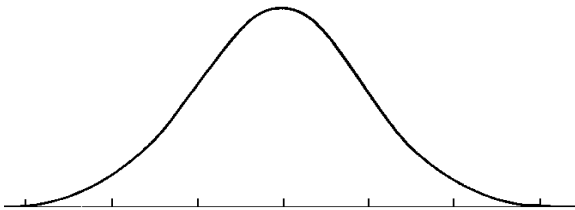
$$H_a : \underline{\hspace{2cm}}$$

Standard Error
for the Mean

$$\sigma_{\bar{X}} = \frac{\sigma}{\sqrt{n}}$$

Formula 5.1

$$z = \frac{\bar{X} - \mu}{\sigma_{\bar{X}}}$$



$$z = \underline{\hspace{2cm}}$$

$$\text{2-tail: } p = \underline{\hspace{2cm}}$$

Would you say that Ihno's class performed **significantly better** than previous classes?

- ☐ Provides evidence Ihno's class performed **significantly better** than previous classes
- ☐ No evidence that Ihno's class performed any differently than previous classes

EXPLAIN.

Test both the **mathquiz** and **statquiz** variables for their resemblance to **normal distributions**.

Based on **skewness**, **kurtosis**, and the **Shapiro-Wilk statistic**, which variable has a sample distribution that is **not** very consistent with the *assumption of normality in the population*?

MATHQUIZ

Skewness

Kurtosis

Shapiro-Wilk

stat = _____

p = _____

<-- Type **R code** into Skeleton and Knit to get **pdf** including output

☐ **NORMAL** (or normal'ish) ☐ **NOT NORMAL**

Sketch a plot you made in R by hand (histogram &/or qq plot)

STATQUIZ

Skewness

Kurtosis

Shapiro-Wilk

stat = _____

p = _____

<-- Type **R code** into Skeleton and Knit to get **pdf** including output

☐ **NORMAL** (or normal'ish) ☐ **NOT NORMAL**

Sketch a plot you made in R by hand (histogram &/or qq plot)

Formula 6.1

$$s_{\bar{X}} = \frac{s}{\sqrt{n}}$$

6 A *1. Standard Error for the Mean

The unbiased **variance** (s^2) **200** participants is **55**.

a) What is the value of the estimated **standard error of the mean** ($s_{\bar{X}}$)?

$S_{\bar{X}} = \underline{\hspace{2cm}}$

b) If the variance were the same but the sample were increased to **1800 participants**, what would be the new value of $s_{\bar{X}}$?

$S_{\bar{X}} = \underline{\hspace{2cm}}$

6 A 2. Sample Mean: z-score and p-value

A survey of **144 college students** reveals a mean beer consumption **rate of 8.4** beers per week, with a **standard deviation of 5.6**.

a) If the **national average is seven** beers per week, what is **the z score** for the college students? What **p value** does this correspond to?

POPULATION PARAMETERS

$$H_0: \mu = \underline{\hspace{2cm}}$$

$$n = \underline{\hspace{2cm}}$$

SAMPLE STATISTICS

$$\bar{X} = \underline{\hspace{2cm}}$$

$$SD: s_X = \underline{\hspace{2cm}} \rightarrow SE: s_{\bar{X}} = \underline{\hspace{2cm}}$$

Formula 6.1

$$s_{\bar{X}} = \frac{s}{\sqrt{n}}$$

Formula 6.2A

$$z = \frac{\bar{X} - \mu}{s_{\bar{X}}}$$

$z = \underline{\hspace{2cm}}$

2-tail: $p = \underline{\hspace{2cm}}$

b) If the **national average were four** beers per week, what would the **z score** be? What can you say about the **p value** in this case?

$z = \underline{\hspace{2cm}}$

2-tail: $p = \underline{\hspace{2cm}}$

6 A 4. One Sample Mean: df and Critical Values of t

a.) In a one-group t test based on a sample of **20 participants**, what is the value for df?

df = $\underline{\hspace{2cm}}$

b.) What are the **two-tailed critical t** values for $\alpha = .05$? For $\alpha = .01$?

$\alpha = .05: t_{cv} = \underline{\hspace{2cm}}$ $\alpha = .01: t_{cv} = \underline{\hspace{2cm}}$

c.) What is the **one-tailed critical t** for $\alpha = .05$? For $\alpha = .01$?

$\alpha = .05: t_{cv} = \underline{\hspace{2cm}}$ $\alpha = .01: t_{cv} = \underline{\hspace{2cm}}$

6 A *5. One Sample Mean: t-score and Critical Values of t (change n)

Twenty-two stroke patients performed a maze task. The mean number of trials (\bar{X}) for success was 14.7 with $s = 6.2$. If the population mean (μ) for this task is 6.5...

a.) What is the calculated value for t ? What is the critical t for a .05, two-tailed test?

POPULATION PARAMETERS

$H_0: \mu = \underline{\hspace{2cm}}$

$n = \underline{\hspace{2cm}}$

SAMPLE STATISTICS

$\bar{X} = \underline{\hspace{2cm}}$

SD: $s_X = \underline{\hspace{2cm}} \rightarrow$ SE: $s_{\bar{X}} = \underline{\hspace{2cm}}$

Formula 6.1

$$s_{\bar{X}} = \frac{s}{\sqrt{n}}$$

Formula 6.3

$$t = \frac{\bar{X} - \mu}{s_{\bar{X}}}$$

$$df = n - 1$$

$t(\underline{\hspace{1cm}}) = \underline{\hspace{2cm}}$

$t_{cv} = \underline{\hspace{2cm}}$

b.) If only 11 patients had been run but the data were the same as in part a, what would be the calculated value for t ?

$t(\underline{\hspace{1cm}}) = \underline{\hspace{2cm}}$

$t_{cv} = \underline{\hspace{2cm}}$

How does this value compare with the t value calculated in part a?

6 A 6. One Sample Mean: t-score and Critical Values of t (change n)

a.) Referring to part a of Exercise 5, what would the calculated t value be if $s = 3.1$ (all else remaining the same)?

$t(\underline{\hspace{1cm}}) = \underline{\hspace{2cm}}$

b.) Comparing the t values you calculated for Exercises 5a and 6a, what can you say about the relation between t and the sample standard deviation?

A high school is proud of its advanced chemistry class, in which its **16 students** scored an **average of 89.3** on the statewide exam, with **s = 9**.

- a.) Test the null hypothesis that the advanced class is just a random selection from the state population ($\mu = 84.7$), using $\alpha = .05$ (two-tailed).

POPULATION PARAMETERS

$$H_0: \mu = \underline{\hspace{2cm}}$$

$$n = \underline{\hspace{2cm}}$$

SAMPLE STATISTICS

$$\bar{X} = \underline{\hspace{2cm}}$$

$$SD: s_X = \underline{\hspace{2cm}} \rightarrow SE: s_{\bar{X}} = \underline{\hspace{2cm}}$$

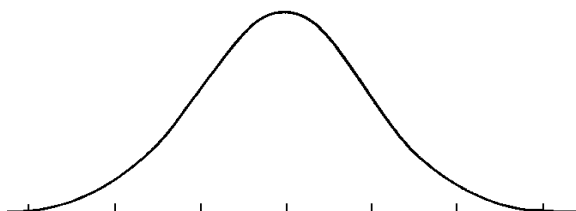
Formula 6.1

$$s_{\bar{X}} = \frac{s}{\sqrt{n}}$$

Formula 6.3

$$t = \frac{\bar{X} - \mu}{s_{\bar{X}}}$$

$$df = n - 1$$



$$t(\underline{\hspace{1cm}}) = \underline{\hspace{2cm}}$$

$$t_{cv} = \underline{\hspace{2cm}}$$

$$2\text{-tail: } p = \underline{\hspace{2cm}}$$

- ☐ Provides evidence the advanced chemistry class at this school is not a random selection from the state.
- ☐ No evidence that the advanced chemistry class at this school is not a random selection from the state.

- b.) Test the same hypothesis at the **.01 level** (two-tailed).

- ☐ Provides evidence the advanced chemistry class at this school is not a random selection from the state.
- ☐ No evidence that the advanced chemistry class at this school is not a random selection from the state

Considering your decision with respect to the null hypothesis, what type of error (Type I or Type II) **could you be making?**

- ☐ Type I
- ☐ Type II

Are serial killers more introverted than the general population?

A sample of **14 serial killers** serving life sentences was tested and found to have a **mean** introversion score (\bar{X}) of **42** with $s = 6.8$. If the **population mean (μ) is 36**, are the serial killers significantly more introverted at the .05 level? (Perform the appropriate **one-tailed test**, *although normally it would not be justified.*)

POPULATION PARAMETERS

$$H_0: \mu = \underline{\hspace{2cm}}$$

$$n = \underline{\hspace{2cm}}$$

SAMPLE STATISTICS

$$\bar{X} = \underline{\hspace{2cm}}$$

$$SD: s_X = \underline{\hspace{2cm}} \rightarrow SE: s_{\bar{X}} = \underline{\hspace{2cm}}$$

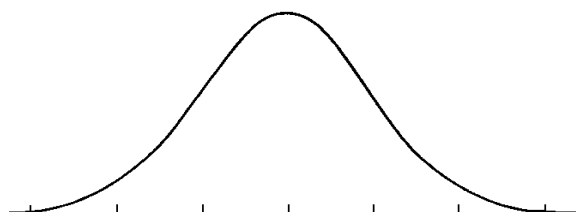
Formula 6.1

$$s_{\bar{X}} = \frac{s}{\sqrt{n}}$$

Formula 6.3

$$t = \frac{\bar{X} - \mu}{s_{\bar{X}}}$$

$$df = n - 1$$



$$t(\underline{\hspace{1cm}}) = \underline{\hspace{2cm}}$$

$$t_{cv} = \underline{\hspace{2cm}}$$

$$1\text{-tail: } p = \underline{\hspace{2cm}}$$

EXPLAIN CONCLUSION: Are serial killers more introverted than the general population?

☐ Yes

☐ NO

A psychologist studying the dynamics of marriage wanted to know how many hours per week the average American couple spends discussing marital problems. The sample mean (\bar{X}) of **155 randomly selected** couples turned out to be **2.6 hours**, with **$s = 1.8$** .

- a.) Find the **95% confidence interval for the mean** (μ) of the population.

POPULATION PARAMETERS

$\mu \leftarrow$ 95% CI for

$n =$ _____

SAMPLE STATISTICS

$\bar{X} =$ _____

SD: $s_X =$ _____ \rightarrow SE: $s_{\bar{X}} =$ _____

Formula 6.1

$$s_{\bar{X}} = \frac{s}{\sqrt{n}}$$

Formula 6.3

$$df = n - 1$$

Formula 6.6

$$\bar{X} \pm t_{cv} \cdot s_{\bar{X}}$$

$t_{cv} =$ _____

95% CI: (_____ , _____)

- b.) A European study had already estimated the population mean to be **3 hours per week** for European couples. Are the American couples **significantly different** from the European couples at the **.05 level**?

☐ Yes

☐ NO

Show how your answer to part a makes it easy to answer part b.

If the psychologist in exercise 4 wanted the **width of the confidence interval to be only half an hour**, how many couples would have to be sampled?

Formula 6.5

$$n = \left(\frac{4s}{W} \right)^2$$

$n =$ _____

A psychologist would like to know how many casual friends are in the average person's social network. She interviews a random sample of people and determines for each the **number of friends** or social acquaintances they see or talk to at least once a year. The data are as follows:

5, 11, 15, 9, 7, 13, 23, 8, 12, 7, 10, 11, 21, 20, 13

- a.) Find the **90% confidence interval for the mean** number of friends for the entire population.

POPULATION PARAMETERS

$\mu \leftarrow$ CI for

$n =$ _____

SAMPLE STATISTICS

$\bar{X} =$ _____

SD: $s_X =$ _____ \rightarrow SE: $s_{\bar{X}} =$ _____

Formula 6.1

$$s_{\bar{X}} = \frac{s}{\sqrt{n}}$$

Formula 6.3

$$df = n - 1$$

Formula 6.6

$$\bar{X} \pm t_{cv} \cdot s_{\bar{X}}$$

$t_{cv} =$ _____

90% CI: (_____ , _____)

- b.) Find the **95% CI**.

$t_{cv} =$ _____

95% CI: (_____ , _____)

- c.) If a previous researcher had predicted a **population mean of 10** casual friends per person, could that prediction be **rejected as an hypothesis at the .05 level, twotailed?**

☐ Yes

☐ NO

EXPLAIN.

6	C	1. One Sample: Confidence Interval for the Mean
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Perform **one-sample t tests** to determine whether the baseline, pre-, or postquiz **anxiety scores** of Ihno's students differ significantly ($\alpha = .05$, **two-tailed**) from the mean ($\mu = 18$) found by a very large study of college students across the country. Find the **95% CI for the population mean** for each of the three anxiety measures.

Type **R code** into Skeleton and Knit to get **pdf** including output

	Sample Mean	95% CI (71.63, 72.91)	Test value = 18 $t(99) = 24.744, p=.013$	Ihno's different?
Baseline				<input type="checkbox"/> Different <input type="checkbox"/> Same
Pre-quiz				<input type="checkbox"/> Different <input type="checkbox"/> Same
Post-Quiz				<input type="checkbox"/> Different <input type="checkbox"/> Same

6	C	2. One Sample: Confidence Interval for the Mean
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Perform a one-sample t test to determine whether the average **baseline heart rate** of Ihno's **male** students differs significantly from the mean HR ($\mu = 70$) for college-aged men at the **.01 level, two-tailed**. Find the **99% CI** for the population mean represented by Ihno's male students.

	Sample Mean	99% CI (71.63, 72.91)	Test value = 70 $t(99) = 24.744, p=.013$	Ihno's different?
MALE Baseline				<input type="checkbox"/> Different <input type="checkbox"/> Same

6	C	3. One Sample: Confidence Interval for the Mean
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Perform a one-sample t test to determine whether the average **postquiz heart rate** of Ihno's **female** students differs significantly ($\alpha = .05$, **two-tailed**) from the mean resting HR ($\mu = 72$) for college-aged women. Find the **95% CI** for the population mean represented by Ihno's female students.

	Sample Mean	95% CI (71.63, 72.91)	Test value = 72 $t(99) = 24.744, p=.013$	Ihno's different?
FEMALE Post-Quiz				<input type="checkbox"/> Different <input type="checkbox"/> Same

In a study of a new treatment for phobia, the data for the experimental group were $\bar{X}_1 = 27.2$, $S_1 = 4$, and $n_1 = 15$. The data for the control group were $\bar{X}_2 = 34.4$, $S_2 = 14$, and $n_2 = 15$.

a.) Calculate the **separate-variances** t value.

experimental

$$n_1 = \underline{\hspace{2cm}}$$

$$\bar{X}_1 = \underline{\hspace{2cm}}$$

$$S_1 = \underline{\hspace{2cm}}$$

control

$$n_2 = \underline{\hspace{2cm}}$$

$$\bar{X}_2 = \underline{\hspace{2cm}}$$

$$S_2 = \underline{\hspace{2cm}}$$

SAMPLE DIFFERENCE

$$df = \underline{\hspace{2cm}}$$

$$\bar{X}_1 - \bar{X}_2 = \underline{\hspace{2cm}}$$

$$SE = \underline{\hspace{2cm}}$$

$$H_0 : \underline{\hspace{2cm}}$$

$$H_a : \underline{\hspace{2cm}}$$

Separate variances

$$SE = \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$$

Formula 7.8

$$t = \frac{\bar{D} - 0}{SE}$$

$$\min(n_1, n_2) - 1 < df < n_1 + n_2 - 2$$

$$t(\underline{\hspace{2cm}}) = \underline{\hspace{2cm}}$$

b.) Calculate the **pooled-variance** t value.

SAMPLE DIFFERENCE

$$df = \underline{\hspace{2cm}}$$

$$\bar{X}_1 - \bar{X}_2 = \underline{\hspace{2cm}}$$

$$s_p^2 = \underline{\hspace{2cm}}$$

$$SE = \underline{\hspace{2cm}}$$

Pooled variance - Formula 7.6

$$s_p^2 = \frac{(n_1 - 1)s_1^2 + (n_2 - 1)s_2^2}{n_1 + n_2 - 2}$$

$$SE = \sqrt{s_p^2 \left(\frac{1}{n_1} + \frac{1}{n_2} \right)}$$

Formula 7.8

$$t = \frac{\bar{D} - 0}{SE}$$

$$df = n_1 + n_2 - 2$$

$$t(\underline{\hspace{2cm}}) = \underline{\hspace{2cm}}$$

a.) Design a **true experiment** involving two groups (i.e., the experimenter decides, at random, in which group each participant will be placed).

b.) Design a **quasi-experiment** (i.e., an observational study) involving groups not created, but only selected, by the experimenter.

How are your **conclusions** from this experiment **limited**, even if the results are statistically significant?

On the first day of class, a third-grade teacher is told that **12 of his students are “gifted,”** as determined by IQ tests, and the **remaining 12 are not.** In reality, the two groups have been carefully matched on IQ and previous school performance.

At the end of the school year, the gifted students have a grade **average of 87.2** with **s = 5.3**, whereas the other students have an **average of 82.9**, with **s = 4.4**.

Perform a t test to decide whether you can conclude from these data that false expectations can affect student performance; use $\alpha = .05$, two-tailed. ← use separate variances (not pooled)

“gifted”

$$n_1 = \underline{\hspace{2cm}}$$

$$\bar{X}_1 = \underline{\hspace{2cm}}$$

$$s_1 = \underline{\hspace{2cm}}$$

“not gifted”

$$n_2 = \underline{\hspace{2cm}}$$

$$\bar{X}_2 = \underline{\hspace{2cm}}$$

$$s_2 = \underline{\hspace{2cm}}$$

SAMPLE DIFFERENCE

$$df = \underline{\hspace{2cm}}$$

$$\bar{X}_1 - \bar{X}_2 = \underline{\hspace{2cm}}$$

$$SE = \underline{\hspace{2cm}}$$

$$H_0 : \underline{\hspace{2cm}}$$

$$H_a : \underline{\hspace{2cm}}$$

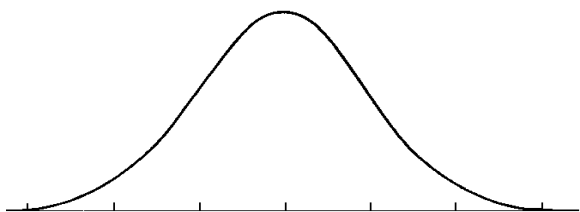
Separate variances

$$SE = \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$$

Formula 7.8

$$t = \frac{\bar{D} - 0}{SE}$$

$$\min(n_1, n_2) - 1 < df < n_1 + n_2 - 2$$



$$t(\underline{\hspace{2cm}}) = \underline{\hspace{2cm}}$$

$$t_{cv} = \underline{\hspace{2cm}}$$

CONCLUSION:

7 B *4. Two Independent Sample Mean Difference: Confidence Interval

A researcher tested the diastolic blood pressure of **60 marathon runners** and **60 nonrunners**. The **mean** for the runners was **75.9 mmHg** with **s = 10**, and the **mean** for the nonrunners was **80.3 mmHg** with **s = 8**.

"runners"	"non-runner"	SAMPLE DIFFERENCE
$n_1 = \underline{\hspace{2cm}}$	$n_2 = \underline{\hspace{2cm}}$	$df = \underline{\hspace{2cm}}$
$\bar{X}_1 = \underline{\hspace{2cm}}$	$\bar{X}_2 = \underline{\hspace{2cm}}$	$\bar{X}_1 - \bar{X}_2 = \underline{\hspace{2cm}}$
$s_1 = \underline{\hspace{2cm}}$	$s_2 = \underline{\hspace{2cm}}$	$SE = \underline{\hspace{2cm}}$

a.) Find the 95% confidence interval for the difference of the population means.

← use separate variances (not pooled)

Separate variances

$$SE = \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$$

$$\min(n_1, n_2) - 1 < df < n_1 + n_2 - 2$$

Formula 7.10

$$\bar{X}_1 - \bar{X}_2 \pm t_{CV} \cdot SE$$

95% CI: (_____ , _____)

b.) Find the 99% confidence interval for the difference of the population means.

99% CI: (_____ , _____)

c.) Use the confidence intervals you found in parts a and b to test the null hypothesis that running has no effect on blood pressure at the **.05** and **.01** levels, **two** tailed.

H_0 : _____

H_a : _____

Alpha = .05

- ☐ Runners are different
☐ no difference

Alpha = .01

- ☐ Runners are different
☐ no difference

A psychologist is studying the concentration of a certain enzyme in saliva as a possible indicator of chronic anxiety level.

A **sample of 12** anxiety neurotics yields a **mean** enzyme concentration of **3.2** with **s = .7**. For comparison purposes, a sample of **20 subjects** reporting low levels of anxiety is measured and yields a **mean** enzyme concentration of **2.3**, with **s = .4**.

- a.) Perform a t test ($\alpha = .05$, two-tailed) to determine whether the two populations sampled **differ** with respect to their mean saliva concentration of this enzyme. **← use pooled variances (not separate)**

"neurotics"

$$n_1 = \underline{\hspace{2cm}}$$

$$\bar{X}_1 = \underline{\hspace{2cm}}$$

$$s_1 = \underline{\hspace{2cm}}$$

"low anx"

$$n_2 = \underline{\hspace{2cm}}$$

$$\bar{X}_2 = \underline{\hspace{2cm}}$$

$$s_2 = \underline{\hspace{2cm}}$$

SAMPLE DIFFERENCE

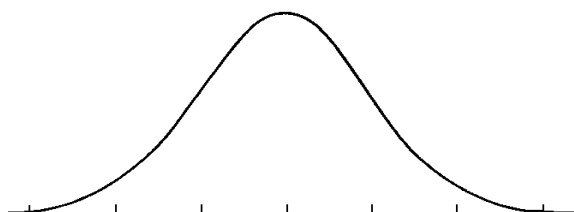
$$df = \underline{\hspace{2cm}}$$

$$\bar{X}_1 - \bar{X}_2 = \underline{\hspace{2cm}}$$

$$SE = \underline{\hspace{2cm}}$$

$$H_0 : \underline{\hspace{2cm}}$$

$$H_a : \underline{\hspace{2cm}}$$



Pooled variance - Formula 7.6

$$s_p^2 = \frac{(n_1 - 1)s_1^2 + (n_2 - 1)s_2^2}{n_1 + n_2 - 2}$$

$$SE = \sqrt{s_p^2 \left(\frac{1}{n_1} + \frac{1}{n_2} \right)}$$

Formula 7.8

$$t = \frac{\bar{D} - 0}{SE}$$

$$df = n_1 + n_2 - 2$$

$$t(\underline{\hspace{2cm}}) = \underline{\hspace{2cm}}$$

$$t_{cv} = \underline{\hspace{2cm}}$$

CONCLUSION:

- b.) Based on your answer to part a, what **type of error** (Type I or Type II) might you be making?

☐ Type I

☐ Type II

7	C	1. Two Independent Sample Mean Difference: Hypothesis Test
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Perform a two-sample t test to determine whether there is a statistically significant **difference** in **baseline heart rate** between the men and the women of Ihno's class.

Type R code into Skeleton and Knit to get pdf including output

Do you have homogeneity of variance? Explain.

☐ yes

☐ no

Report your **results** as they might appear in a journal article.
Include the **95% CI** for this gender difference.

7	C	2. Two Independent Sample Mean Difference: Hypothesis Test
---	---	--

Perform a two-sample t test to determine whether there is a statistically significant **difference** in **phobia** between the men and the women of Ihno's class.

Type R code into Skeleton and Knit to get pdf including output

Do you have homogeneity of variance? Explain.

☐ yes

☐ no

Report your **results** as they might appear in a journal article.
Include the **95% CI** for this gender difference.

7

C

3. Two Independent Sample Mean Difference: Hypothesis Test

Perform a two-sample t test to determine whether the students in the **“impossible to solve”** condition exhibited significantly **higher postquiz HEART RATES** than the students in the **“easy to solve”** condition.

Type R code into Skeleton and Knit to get pdf including output

Is this t test significant at the .05 level? Explain.

☐ yes☐ no

Is this t test significant at the .01 level? Explain.

☐ yes☐ no

Find the 99% CI for the difference of the two population means.

99% CI: (_____ , _____)

7

C

4. Two Independent Sample Mean Difference: Hypothesis Test

Perform a two-sample t test to determine whether the students in the **“impossible to solve”** condition exhibited significantly **higher postquiz ANXIETY** than the students in the **“easy to solve”** condition.

Type R code into Skeleton and Knit to get pdf including output

Is this t test significant at the .05 level? Explain.

☐ yes☐ no

Is this t test significant at the .01 level? Explain.

☐ yes☐ no

Find the 99% CI for the difference of the two population means.

99% CI: (_____ , _____)

Perform a two-sample t test to determine whether **coffee drinkers** exhibited significantly higher **postquiz heart rates** than **nondrinkers** at the .05 level.

Type **R code** into Skeleton and Knit to get **pdf** including output

t(_____) = _____

2-tail: p = _____

- ☐ Coffee drinkers are different
☐ no difference

Is this t test significant at the .01 level?

- ☐ Coffee drinkers are different
☐ no difference

Find the **99% CI** for the **difference** of the two population means...

99% CI: (_____ , _____)

... and explain its connection to your decision regarding the null hypothesis at the .01 level.

8	A	3. Cohen's d
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If the **mean** verbal SAT score is **510** for women and **490** for men, what is the **d** ?

d = _____

8	A	9. Extremely large t-value
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The **t value** calculated for a particular two group experiment was – **23**.

Which of the following can you conclude?

- ☐ a. A calculation error must have been made.
- ☐ b. The number of participants must have been large.
- ☐ c. The effect size must have been large.
- ☐ d. The expected t was probably large.
- ☐ e. The alpha level was probably large.

Explain your choice.

8	A	*10. Cohen's d
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Suppose you are in a situation in which it is **more important to reduce Type II errors** than to worry about Type I errors.

Which of the following could be helpful in reducing Type II errors?

- ☐ a. Make alpha unusually large (e.g., .1).
- ☐ b. Use a larger number of participants.
- ☐ c. Try to increase the effect size.
- ☐ d. All of the above.
- ☐ e. None of the above.

Explain your choice.

8	B	6. Power & Sample Size
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A **drug** for treating headaches has a side effect of lowering diastolic blood pressure **by 8 mmHg** compared to a **placebo**. If the **population standard deviation** is known to be **6 mmHg**,

- a.) What would be the **power** of an experiment ($\alpha = .01$, **two-tailed**) comparing the drug to a placebo using **15 participants per group**?

power = _____

- b.) How **many participants** would you need per group to attain **power = .95**, with $\alpha = .01$, **two-tailed**?

n = _____

8	C	2. Power & Sample Size -- USE G*Power SOFTWARE --
---	---	---

~~Given the adjusted effect size from part a of the previous exercise,~~

I am changing this problem!

How many participants of each gender (assuming equal sample sizes) would be needed for power to be **.8**, with alpha = **.05**, **two-tailed** test?

For a small effect size ($d = .2$)

n = _____

For a medium effect size ($d = .5$)

n = _____

For a large effect size ($d = .8$)

n = _____