

Recurrent Neural Networks 2

CS 287

(Based on Yoav Goldberg's notes)

Review: Representation of Sequence

- ▶ Many tasks in NLP involve sequences

$$w_1, \dots, w_n$$

- ▶ Representations as matrix dense vectors \mathbf{X}
(Following YG, slight abuse of notation)

$$\mathbf{x}_1 = \mathbf{x}_1^0 \mathbf{W}^0, \dots, \mathbf{x}_n = \mathbf{x}_n^0 \mathbf{W}^0$$

- ▶ Would like fixed-dimensional representation.

Review: Sequence Recurrence

- ▶ Can map from dense sequence to dense representation.
- ▶ $\mathbf{x}_1, \dots, \mathbf{x}_n \mapsto \mathbf{s}_1, \dots, \mathbf{s}_n$
- ▶ For all $i \in \{1, \dots, n\}$

$$\mathbf{s}_i = R(\mathbf{s}_{i-1}, \mathbf{x}_i; \theta)$$

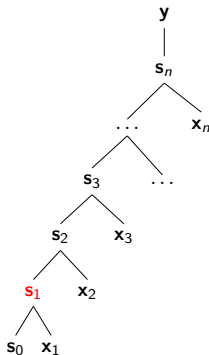
- ▶ θ is shared by all R

Example:

$$\begin{aligned}\mathbf{s}_4 &= R(\mathbf{s}_3, \mathbf{x}_4) \\ &= R(R(\mathbf{s}_2, \mathbf{x}_3), \mathbf{x}_4) \\ &= R(R(R(R(\mathbf{s}_0, \mathbf{x}_1), \mathbf{x}_2), \mathbf{x}_3), \mathbf{x}_4)\end{aligned}$$

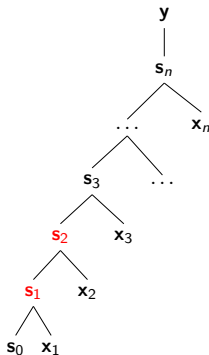
Review: BPTT (Acceptor)

- ▶ Run forward propagation.
- ▶ Run backward propagation.
- ▶ Update all weights (shared)



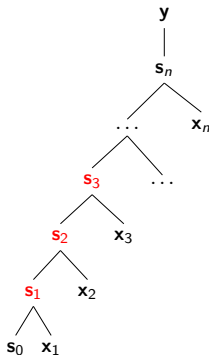
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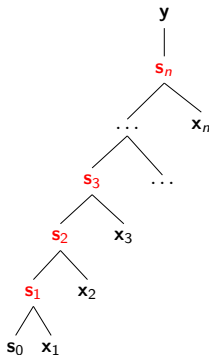
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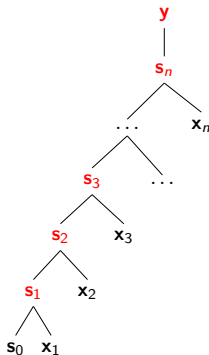
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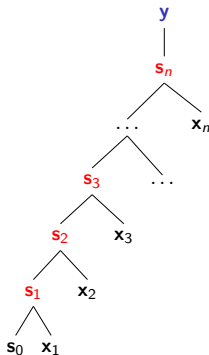
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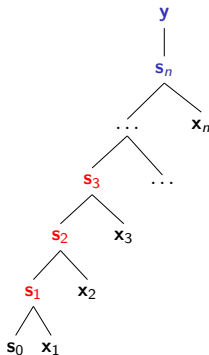
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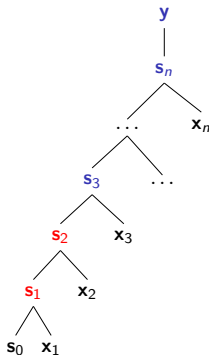
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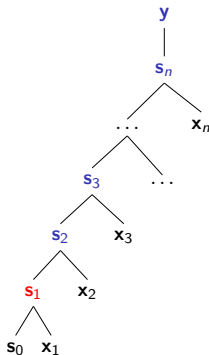
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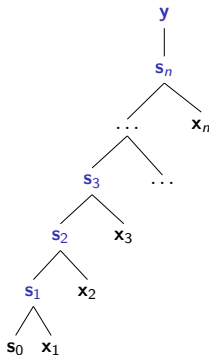
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Issues

- ▶ Can be inefficient, but batch/GPUs help.
- ▶ Model is much deeper than previous approaches.
 - ▶ This matters a lot, focus of next class.
- ▶ Variable-size model for each sentence.
 - ▶ Have to be a bit more clever in Torch.

Quiz

Consider a ReLU version of the Elman RNN with function R defined as

$$NN(\mathbf{x}, \mathbf{s}) = \text{ReLU}(\mathbf{s}\mathbf{W}^s + \mathbf{x}\mathbf{W}^x + \mathbf{b}).$$

We use this RNN with an acceptor architecture over the sequence $\mathbf{x}_1, \dots, \mathbf{x}_5$. Assume we have computed the gradient for the final layer

$$\frac{\partial L}{\partial \mathbf{s}_5}$$

What is the symbolic gradient of the previous state $\frac{\partial L}{\partial \mathbf{s}_4}$?

What is the symbolic gradient of the first state $\frac{\partial L}{\partial \mathbf{s}_1}$?

Answer

Chain rule, then relu cases, then to indicator notation

$$\begin{aligned}\frac{\partial L}{\partial s_{4,i}} &= \sum_j \frac{\partial s_{5,j}}{\partial s_{4,i}} \frac{\partial L}{\partial s_{5,j}} \\ &= \sum_j \begin{cases} W_{i,j}^s \frac{\partial L}{\partial s_{5,j}} & s_{5,j} > 0 \\ 0 & o.w. \end{cases} \\ &= \sum_j \mathbf{1}(s_{5,j} > 0) W_{i,j}^s \frac{\partial L}{\partial s_{5,j}}\end{aligned}$$

Answer

Multiple applications of Chain rule, combine relu cases.

$$\begin{aligned}\frac{\partial L}{\partial s_{1,i}} &= \sum_{j_2} \cdots \sum_{j_5} \frac{\partial s_{5,j_5}}{\partial s_{4,j_4}} \frac{\partial L}{\partial s_{5,j_5}} \\ &= \sum_{j_2} \cdots \sum_{j_5} \mathbf{1}(s_{2,j_2} > 0 \wedge \dots \wedge s_{5,j} > 0) W_{i,j_2}^s \cdots W_{j_4,j_5}^s \cdots \frac{\partial L}{\partial s_{5,j}}\end{aligned}$$

The Promise of RNNs

- ▶ We hope to learn a model with memory.
- ▶ For acceptors this means long-range interaction.

How can you not see this movie?

You should not see this movie.

- ▶ Memory interaction here is at \mathbf{s}_1 , but gradient signal is at \mathbf{s}_n

Vanishing Gradients

- ▶ Gradients at early layers go through many squashing layers.
- ▶ For instance consider quiz with hardtanh

$$\sum_{j_2} \dots \sum_{j_5} \mathbf{1}((0 < s_{2,j_2} < 1) \wedge \dots \wedge (0 < s_{5,j} < 1)) W_{i,j_2}^s \dots W_{j_4,j_5}^s \frac{\partial L}{\partial s_{5,j}}$$

- ▶ The indicator term causes a tendency towards *vanishing gradients*.

LSTMs