

EE4211 Assignment 1

Question 1a:

$$\text{output} = \frac{1}{9} \times (2 + 7 + 4 + 6 + 5 + 1 + 5 + 1 + 4) = 3.89$$

Question 1b:

$$\text{output} = \text{median}(1, 1, 2, 5, 5, 5, 6, 7, 7) = 5$$

Question 1c:

$$\text{output} = 1 \times (4 + 5 + 2 + 3 + 6 + 2 + 7 + 5) - 8 \times 1 = 26$$

Question 1d:

i	0	1	2	3	4	5	6	7
h_i	2	4	5	2	3	3	3	3

Question 1e:

i	0	1	2	3	4	5	6	7
h_i	$\frac{2}{25}$	$\frac{4}{25}$	$\frac{5}{25}$	$\frac{2}{25}$	$\frac{3}{25}$	$\frac{3}{25}$	$\frac{3}{25}$	$\frac{3}{25}$
C_i	$\frac{2}{25}$	$\frac{6}{25}$	$\frac{11}{25}$	$\frac{13}{25}$	$\frac{16}{25}$	$\frac{19}{25}$	$\frac{22}{25}$	$\frac{25}{25}$
$7C_i$	1	2	3	4	4	5	6	7

Equalized image

y\x	0	1	2	3	4
0	4	7	6	3	1
1	3	3	6	1	2
2	4	5	3	7	4
3	4	2	6	5	2
4	3	7	5	2	4

i	0	1	2	3	4	5	6	7
h_i	$\frac{0}{25}$	$\frac{2}{25}$	$\frac{4}{25}$	$\frac{5}{25}$	$\frac{5}{25}$	$\frac{3}{25}$	$\frac{3}{25}$	$\frac{3}{25}$

Question 2:

Image A – Spectrum 1: a fast-varying image has high frequency contents.

Image B – Spectrum 2: a slow-varying image has low frequency contents.

Image C – Spectrum 4: strong directional features result in orthogonal lines in Fourier.

Image D – Spectrum 3: a periodic pattern results in isolated points in Fourier.

Image E – Spectrum 5: a fast-varying image has higher frequency contents.

Question 3a:

$$\begin{aligned}
 g(x, y) &= \frac{1}{4} (f(x, y + 1) + f(x + 1, y) + f(x - 1, y) + f(x, y - 1)) \\
 G(x, y) &= \frac{1}{4} \left(e^{\frac{j2\pi}{N}} + e^{\frac{j2\pi u}{M}} + e^{\frac{-j2\pi u}{M}} + e^{\frac{-j2\pi v}{N}} \right) F(u, v) \\
 &= H(u, v) F(u, v) \\
 \therefore H(u, v) &= \frac{1}{2} \left(\cos\left(\frac{2\pi u}{M}\right) + \cos\left(\frac{2\pi v}{N}\right) \right)
 \end{aligned}$$

Question 3b:

From $H(u, v) = \frac{1}{2} \left(\cos\left(\frac{2\pi u}{M}\right) + \cos\left(\frac{2\pi v}{N}\right) \right)$, u range from 0 to M , so the value for $\cos\left(\frac{2\pi u}{M}\right)$ will be 1 when $u = 0$ and -1 when $u = M/2$, and similar when considering v . The amplitude of the filter decreases as the distance from the origin of the filter decrease, which is a characteristic of a lowpass filter.

Question 4:

Codes:

```
%% ini
clc;
clear;
close all;

%% laplacian transform
Image = imread('skeleton_orig.tif');
filter1 = fspecial('laplacian', 0);

temp1 = im2double(Image);
sharpen1 = imfilter(temp1, filter1);
sharpen2 = imsubtract(temp1, sharpen1);

%% sobel transform
filter2 = fspecial('sobel');
sharpen3 = imfilter(temp1, filter2);

%% average 5x5 smoothing on sobel imag
filter3 = 1/ (5. ^2)*ones (5);
sharpen4 = imfilter(sharpen3, filter3);

%% product of smoothing and laplacian transform
product1 = immultiply(sharpen2, sharpen4);

%% add the original image and product
sharpen5 = imadd(temp1, product1);

%% gamar transform
gamma1 = 0.5;
sharpen6 = imadjust(sharpen5,[],[],gamma1);

figure;
subplot(1,2,1);imshow(Image); title('Orginal');
subplot(1,2,2);imshow(sharpen6);title('Enhanced Image');
```

The original image and the enhanced

