

Ex 3-4)

$$x(t) = t^2, \quad -\pi < t < \pi, \quad T_0 = 2\pi, \quad \omega_0 = \frac{2\pi}{T_0} = 1,$$

$$C_R = \frac{1}{2\pi} \int_{-\pi}^{\pi} \underbrace{t^2}_{u} \cdot \underbrace{e^{-jRt}}_{v'} dt.$$

$$\Rightarrow \frac{1}{2\pi} \left[ \cancel{\left. \frac{t^2 \cdot e^{-jRt}}{(-jR)} \right|_{-\pi}^{\pi}} - \frac{2}{(jR)} \int_{-\pi}^{\pi} t \cdot e^{-jRt} dt \right]$$

$$e^{-jR\pi} = (e^{-j\pi})^R = (-1)^R$$

$$e^{jR\pi} = (e^{j\pi})^R = (-1)$$

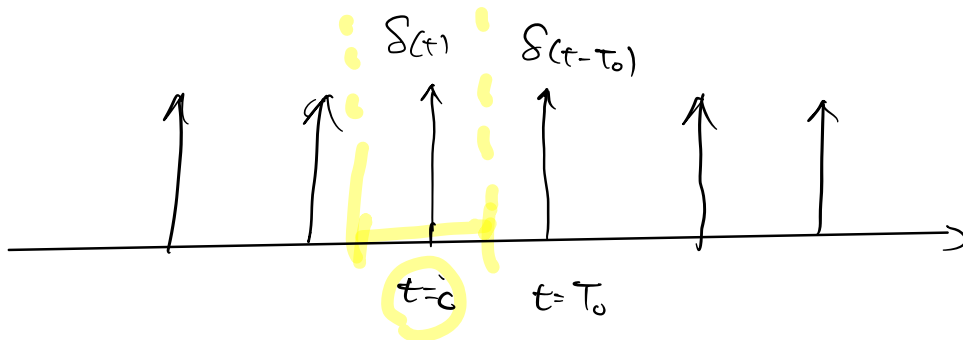
$$\Rightarrow \frac{1}{jR\pi} \left[ \left( \frac{t}{(-jR)} - \frac{1}{(-jR)^2} \right) e^{-jRt} \right]_{-\pi}^{\pi}$$

$$= \frac{1}{jR\pi} \left[ \left( \frac{\pi}{(-jR)} - \frac{1}{(-jR)^2} \right) (-1)^R + \left( \frac{-\pi}{(-jR)} - \frac{1}{(-jR)^2} \right) (-1)^R \right]$$

$$= \frac{1}{jR\pi} \cdot \frac{2\pi}{(jR)} (-1)^R = \frac{2(-1)^R}{R^2} = C_R.$$

Ex 3-3) Impulse train  $\delta_{T_0}(t)$

$$\delta_{T_0}(t) = \sum_{k=-\infty}^{\infty} \delta(t - kT_0)$$



$$C_0 = \frac{1}{T_0} \int_{-\frac{T_0}{2}}^{\frac{T_0}{2}} \delta(t) dt = \left( \frac{1}{T_0} \right)$$

$$\begin{aligned} C_R &= \frac{1}{T_0} \int_{-\frac{T_0}{2}}^{\frac{T_0}{2}} \delta_{T_0}(t) e^{-jR\omega_0 t} dt \\ &= \frac{1}{T_0} \int_{-\frac{T_0}{2}}^{\frac{T_0}{2}} \sum_{m=-\infty}^{\infty} \delta(t - mT_0) e^{-jR\omega_0 t} dt \\ &= \left( \frac{1}{T_0} \right) \end{aligned}$$

$\delta(t)$  at  $t=0$        $\delta(t)$  at  $t=T_0$

$$a_0 = 2C_0 = \frac{2}{T_0} \quad \begin{aligned} a_R &= 2\operatorname{Re}(C_R) = \frac{2}{T_0} \\ b_R &= -2\operatorname{Im}(C_R) = \emptyset \end{aligned}$$

$$\delta_{T_0}(t) = \sum_{k=-\infty}^{\infty} \delta(t - kT_0)$$

$$= \frac{1}{T_0} \sum_{k=-\infty}^{\infty} e^{-jk\omega_0 t}$$

$$= \frac{1}{T_0} + \frac{2}{T_0} \sum_{k=1}^{\infty} \cos(k\omega_0 t)$$