

GE2262 Business Statistics

Topic 3 Discrete & Continuous Probability Distributions

Reference

Levine, D.M., Krehbiel, T.C. and Berenson, M.L., *Business Statistics: A First Course*, Pearson Education Ltd, Chapter 3 & 5 & 6

Outline

- Discrete Probability Distribution
- Binomial Distribution
- Continuous Probability Distribution
- Normal Distribution

Random Variables

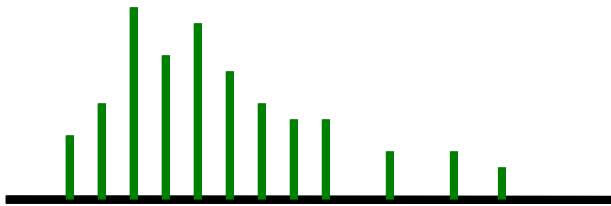
Random Variable

outcomes of an experiment with probabilistic occurrence



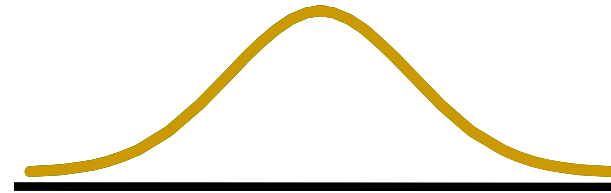
Discrete Random Variable

produces outcomes that come from a **counting process**
(e.g. number of courses you are taking in this semester)



Continuous Random Variable

produce outcomes that come from a **measurement**
(e.g. your annual salary, or your weight)



Discrete Probability Distributions

- A probability distribution for a discrete variable is a mutually exclusive listing of all possible numerical outcomes for that variable and a probability of occurrence associated with each outcome
 - The probabilities are obtained based on either priori knowledge (priori probability) or empirical approach (empirical probability)
 - Examples
 - Probability of selecting a black card from a deck of cards
 - Probability of a respondent who will purchase a HDTV
- The probability distribution of a variable forms a theoretical model which allows us to derive statistics and probabilities for the events related to the variable

Discrete Probability Distribution

Experiment: Toss 2 coins let X = No. of heads



Probability Distribution

X Value

Probability

0

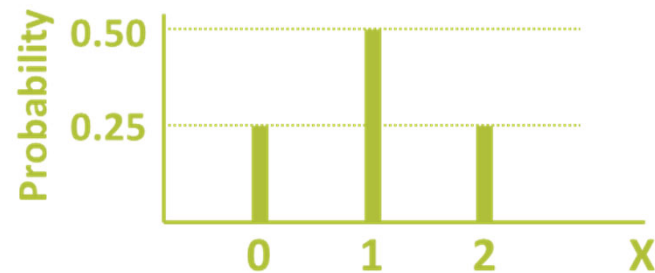
$1/4 = 0.25$

1

$2/4 = 0.50$

2

$1/4 = 0.25$



Discrete Probability Distribution

Cont'd

Probability Distribution	
<u>X Value, x_i</u>	<u>Probability, $P(X = x_i)$</u>
0	$1/4 = 0.25$
1	$2/4 = 0.50$
<u>2</u>	<u>$1/4 = 0.25$</u>
Total	1

- Mutually exclusive (Nothing in common)
- Collectively exhaustive (Nothing left out)

$$0 \leq P(X = x_i) \leq 1 \qquad \sum P(X = x_i) = 1$$

Discrete Random Variables – Measuring Center

Cont'd

■ Expected value (Mean)

- Weighted average of all possible values of X
- Corresponding probability is treated as weight

$$\mu = E(X) = \sum_{i=1}^N x_i P(X = x_i)$$

E.g. Toss 2 coins, count the number of heads

X = number of heads

Compute the expected value of X:

$$\mu = x_1 P(X = x_1) + x_2 P(X = x_2) + x_3 P(X = x_3)$$

X	P(X)
0	0.25
1	0.50
2	0.25

Discrete Random Variables – Measuring Variation

Cont'd

■ Variance

- Weighted average squared deviation about the mean

$$\sigma^2 = \sum_{i=1}^N [x_i - E(X)]^2 P(X = x_i)$$

■ Standard deviation

- Square root of variance

$$\sigma = \sqrt{\sigma^2} = \sqrt{\sum_{i=1}^N [x_i - E(X)]^2 P(X = x_i)}$$

E.g. Toss 2 coins, count the number of heads

X = number of heads

Compute the variance of X:

$$\sigma^2 = (x_1 - \mu)^2 P(X = x_1) + (x_2 - \mu)^2 P(X = x_2) + (x_3 - \mu)^2 P(X = x_3)$$

X	P(X)
0	0.25
1	0.50
2	0.25

Discrete Random Variables – Example

Cont'd

- Roll a fair die once. What is the expected value of the number rolled?

Number Rolled (x_i)	Probability $P(X = x_i)$	$x_i P(X = x_i)$
1	1/6	$(1)(1/6) = 1/6$
2	1/6	$(2)(1/6) = 2/6$
3	1/6	$(3)(1/6) = 3/6$
4	1/6	$(4)(1/6) = 4/6$
5	1/6	$(5)(1/6) = 5/6$
6	1/6	$(6)(1/6) = 6/6$
		$\mu = E(X) = 3.5$

- The expected value of the number rolled is 3.5

Discrete Random Variables – Example

Cont'd

- For the results of rolling a fair die, the expected value of the number rolled is 3.5
- Since you can never obtain a number of 3.5 by rolling a die, so what is the meaning of these statistics?
- How much money should we be willing to put up in order to have the opportunity of rolling a fair die if we were to be paid, in dollars, the amount on the face of the die?
 - On any particular roll, our payoff will be \$1.0, \$2.0, ..., or \$6.0, but over many many rolls, the payoff can be expected to average out to \$3.5 per roll
 - If you pay less than \$3.5 for a roll, you are going to make a profit in long run
 - If you pay more than \$3.5 for a roll, you are going to loss in long run

Discrete Random Variables – Exercise

Cont'd

- Assume the following table shows the return per \$1,000 for an investment under different economic conditions

Return in amount, Y_i	Economic Condition	$P(Y_i)$
-\$200	Recession	0.2
+ 50	Stable Economy	0.5
+ 350	Expanding Economy	0.3

- Compute the expected return and standard deviation

Should you, from a statistical stand point, invest or not?

Calculating the Mean and Variance in Calculator (For Casio fx-50F)

Date Set:

X_j	20	30	40	50	60	75
$P(X_j)$	0.1	0.1	0.15	0.25	0.2	0.2

1. Change to "Lin" mode

MODE **MODE** 5 1

2. Clear previous data

SHIFT **CLR** 1 **EXE**

3. Input data

20	SHIFT	,	0.1	M+	30	SHIFT	,	0.1	M+
40	SHIFT	,	0.15	M+	50	SHIFT	,	0.25	M+
60	SHIFT	,	0.2	M+	75	SHIFT	,	0.2	M+

4. Calculate descriptive statistics

Mean: **SHIFT** 2 1 1 **EXE** = 50.5

Population standard deviation: **SHIFT** 2 1 2 **EXE** = 17.02204453

Binomial Distribution

- A mathematical model is a mathematical expression representing some underlying phenomenon
- With such mathematical expressions available, the exact probability of occurrence of any particular outcome of the random variable can be computed
- For discrete random variables, this mathematical expression is known as a **probability distribution function**
- One of the such probability distribution functions is called **Binomial Distribution**
 - A very important mathematical model used in many business situations

Binomial Distribution

Cont'd

What is the probability that, among 3 students, any 2 of them getting a pass in the test, with the probability of passing the test equals 0.7?

Student	A	B	C	Probability
Case 1	P	P	F	$0.7 \times 0.7 \times 0.3 = 0.147$
Case 2	P	F	P	$0.7 \times 0.3 \times 0.7 = 0.147$
Case 3	F	P	P	$0.3 \times 0.7 \times 0.7 = 0.147$

$$P(\text{Any 2 getting pass}) = 0.147 + 0.147 + 0.147 = 0.441$$

What is the probability that, among **30** students, any **20** of them getting a pass in the test, with the probability of passing the test equals 0.7?

Binomial Distribution – Conditions

Cont'd

- 'n' repetition of identical trials
 - E.g. totally 3 students
- 2 mutually exclusive outcomes (success and failure) in each trial
 - E.g. getting a pass or fail in the test
- Constant probability of success, π , in each trial
 - E.g. probability of getting a pass in the test for each student is 0.7, which is constant
- Trials are independent
 - E.g. the outcome of one student does not affect the outcome of the others

Binomial Distribution

Cont'd

- The binomial probability for a discrete random variable X is computed as

$$P(X = x) = \frac{n!}{x! (n - x)!} \pi^x (1 - \pi)^{(n-x)}$$

Probability mass
function

where $P(X = x)$ = probability that $X = x$ events of interest (e.g. success)

n = number of observations

π = probability of an event of interest

X = number of events of interest in the sample ($X = 0, 1, 2, \dots, n$)

$n! = n (n - 1) (n - 2) \dots (1)$; $0! = 1$

$\frac{n!}{x!(n-x)!}$ = no. of combinations of x successes
out of n trials

π^x = total probability of having x successes

$(1 - \pi)^{(n-x)}$ = total probability of having
($n - x$) failures

Binomial Distribution – Example

What is the probability that, among 3 students, any 2 of them getting a pass in the test, with the probability of passing the test equals 0.7?

Cont'd

X = no. of students passing the test out of 3 students
 X follows Binomial distribution ($n = 3, X = 2, \pi = 0.7$)

$$\begin{aligned} P(X = 2) &= \frac{n!}{x!(n-x)!} \pi^x (1-\pi)^{(n-x)} \\ &= \frac{3!}{2!(3-2)!} 0.7^2 (1-0.7)^{(3-2)} \\ &= 0.441 \end{aligned}$$

What is the probability that, among **30** students, any **20** of them getting a pass in the test, with the probability of passing the test equals 0.7?

Binomial Distribution

Cont'd

- Possible applications for the Binomial Distribution
 - ❑ A manufacturing plant labels items as either defective or acceptable
 - ❑ A firm bidding for contracts will either get a contract or not
 - ❑ A marketing research firm receives survey responses of “yes, I will buy” or “no, I will not”
 - ❑ New job applicants either accept the offer or reject it

Binomial Distribution – Exercise

Cont'd

An experiment about the interest of going to the cinema is conducted in a secondary school. Five students are selected randomly. Assume the probability of going to cinema within a week is 0.1.

X = no. of students going to cinema out of 5 students
 X follows Binomial distribution ($n = 5, \pi = 0.1$)

The probability of 3 students going to the cinema out of these 5 students:

Binomial Distribution – Exercise

Cont'd

- What is the probability that there are 3 or more students going to the cinema within a week?

$$P(X \geq 3) = P(X = 3) + P(X = 4) + P(X = 5)$$

- What is the probability that there are less than 3 students going to the cinema?

$$P(X < 3) = P(X = 0) + P(X = 1) + P(X = 2)$$

Binomial Distribution Mean and Standard Deviation

Binomial Probability Distribution:

x_i	$P(x_i)$
0	0.59049
1	0.32805
2	0.0729
3	0.0081
4	0.00045
5	0.00001

$$\mu = \sum x_i P(X = x_i)$$

$$\sigma^2 = \sum (x_i - \mu)^2 P(X = x_i)$$

Binomial Distribution Mean and Standard Deviation

Cont'd

- If X follows a Binomial Distribution of size n and probability π , it can be shown that

$$\mu = n\pi$$

$$\begin{aligned} &= (5)(0.1) \\ &= 0.5 \end{aligned}$$

$$\sigma^2 = n\pi(1 - \pi)$$

$$\begin{aligned} &= (5)(0.1)(1-0.1) \\ &= 0.45 \end{aligned}$$

$$\sigma = \sqrt{n\pi(1 - \pi)}$$

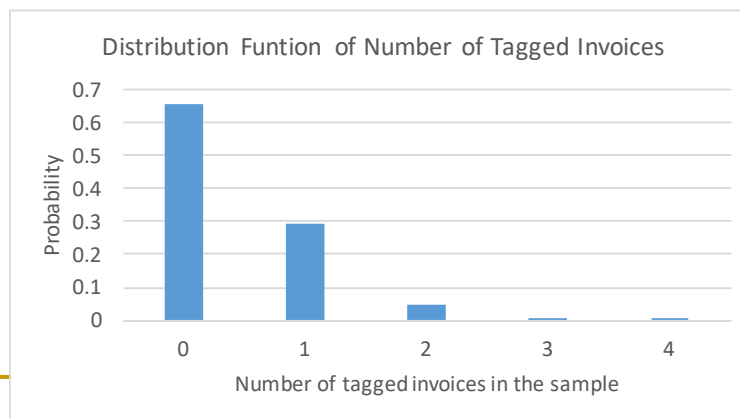
$$\begin{aligned} &= \sqrt{(5)(0.1)(1-0.1)} \\ &= 0.6708 \end{aligned}$$

Binomial Distribution

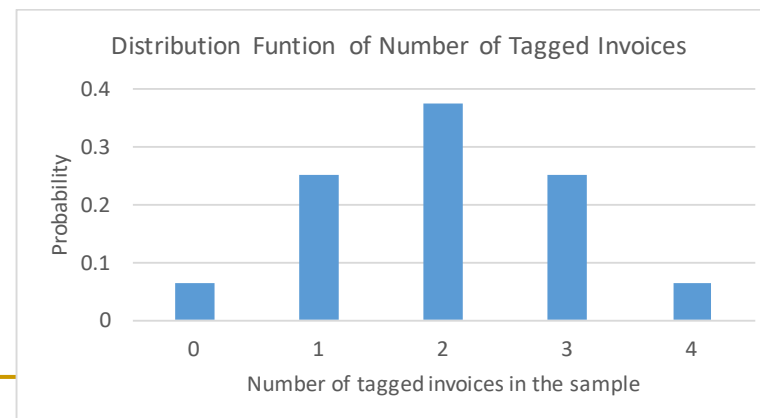
Cont'd

- The shape of a Binomial Distribution depends on the values of n and π
 - Whenever $\pi = 0.5$, the distribution is symmetrical, regardless of how large or small the value of n
 - Whenever $\pi \neq 0.5$, the distribution is skewed
 - $\pi < 0.5$, right-skewed; $\pi > 0.5$, left-skewed

$n = 4, \pi = 0.1$



$n = 4, \pi = 0.5$



Binomial Distribution in Excel

- Using Excel to find out the probability that 2 students out of 5 going to cinema within 1 week
 - Type the required information (n , X , π)
 - Use BINOM.DIST function

	A	B	C
1	Binomial Distribution		
2			
3	Number of trials	n	5
4	Probability	π	0.1
5	Total number of successes in n trial	X	2
6			
7	P (X=2)		

Insert Function [?] [X]

Search for a function:

Type a brief description of what you want to do and then click Go

Or select a category: Statistical

Select a function:

- BETA.DIST
- BETA.INV
- BINOM.DIST**
- BINOM.INV
- CHISQ.DIST
- CHISQ.DIST.RT
- CHISQ.INV

BINOM.DIST(number_s, trials, probability_s, cumulative)
Returns the individual term binomial distribution probability.

[Help on this function](#)

OK Cancel

Function Arguments [?] [X]

BINOM.DIST

Number_s: C5 = 2

Trials: C3 = 5

Probability_s: C4 = 0.1

Cumulative: 0 = FALSE

Returns the individual term binomial distribution probability.

Cumulative is a logical value: for the cumulative distribution function, use TRUE; for the probability mass function, use FALSE.

Cumulative:
where 1 is used to calculate $P(X \leq 2)$
0 is used to calculate $P(X=2)$

OK Cancel

Binomial Distribution in Excel

Cont'd

- Using Excel to find out the probability that 2 students out of 5 going to cinema with 1 week

	A	B	C	D	E
1	Binomial Distribution				
2					
3	Number of trials	n	5		
4	Probability	π	0.1		
5	Total number of successes in n trial	X	2		
6					
7	P (X=2)	=BINOM.DIST(C5,C3,C4,0)			=BINOM.DIST(X,n, π ,0)
8		BINOM.DIST(number_s, trials, probability_s, cumulative)			

↓

	A	B	C
1	Binomial Distribution		
2			
3	Number of trials	n	5
4	Probability	π	0.1
5	Total number of successes in n trial	X	2
6			
7	P (X=2)	0.0729	

Continuous Probability Distributions

- A continuous variable is a variable that can be assume **any value on a continuum** (can assume an uncountable number of values)
- Examples
 - Time required to travel from home to campus
 - Temperature of a drink
 - Height, in inches
- These can potentially take on any value depending only on the ability to precisely and accurately measure
- In practice, a discrete numerical variable with large range of values is often considered as a continuous variable

Continuous Probability Distributions

– Example

- The probability distribution as shown is obtained by categorizing the amount of soft drink (X) in 10,000 1-liter bottles filled on a recent day

- $P(X < 1.025) = 0.0048$
 - $P(1.025 \leq X < 1.030) = 0.0122$
 - $P(X < 1.030) = 0.0048 + 0.0122$
 $= 0.0170$
 - $P(X < 1.042) = ?$
-
- $P(1.032 \leq X < 1.042) = ?$
 - $P(X = 1.042) = ?$

Cont'd

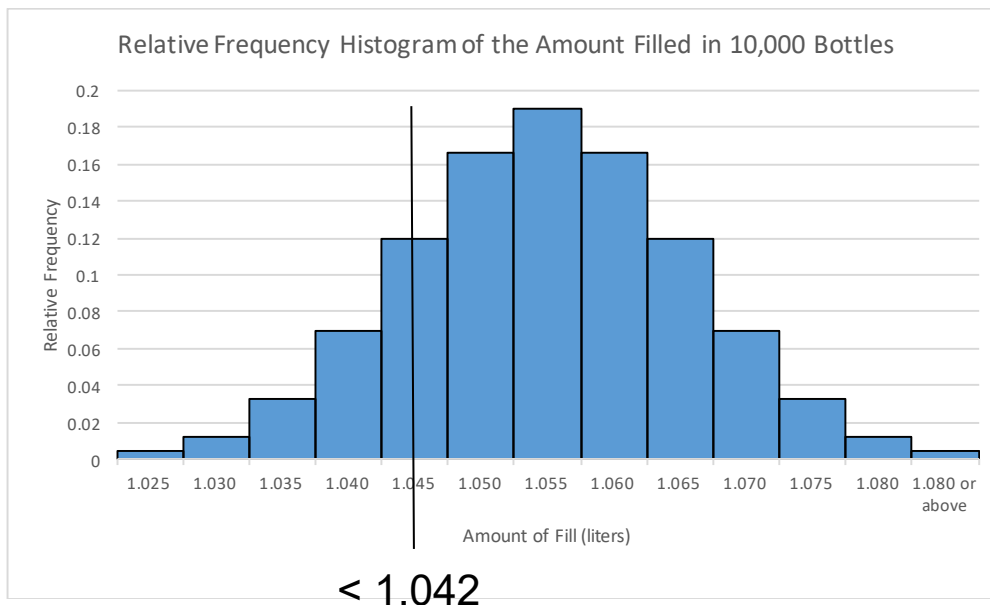
Amount of Fill (liters)	Frequency	Relative Frequency
< 1.025	48	0.0048
1.025 < 1.030	122	0.0122
1.030 < 1.035	325	0.0325
1.035 < 1.040	695	0.0695
1.040 < 1.045	1198	0.1198
1.045 < 1.050	1664	0.1664
1.050 < 1.055	1896	0.1896
1.055 < 1.060	1664	0.1664
1.060 < 1.065	1198	0.1198
1.065 < 1.070	695	0.0695
1.070 < 1.075	325	0.0325
1.075 < 1.080	122	0.0122
1.080 or above	48	0.0048
		<hr/> 1.0000

Continuous Probability Distributions

– Example

Cont'd

- Any required probabilities concerning the amount of soft drink filled can be obtained either from the raw data observed or from the relative frequency histogram



- Treat the relative frequency as the area of each group
 $P(X < 1.042)$ = the area on the left of 1.042
 $= 0.0048 + 0.0122 + 0.0325 + 0.0695$
 $+ (1.042 - 1.040) / 0.005 * 0.1198$
 $= 0.1190 + 0.0479 = 0.1669$
- The area under a single point is 0.
Hence, $P(X = 1.042) = 0$

Continuous Probability Distributions

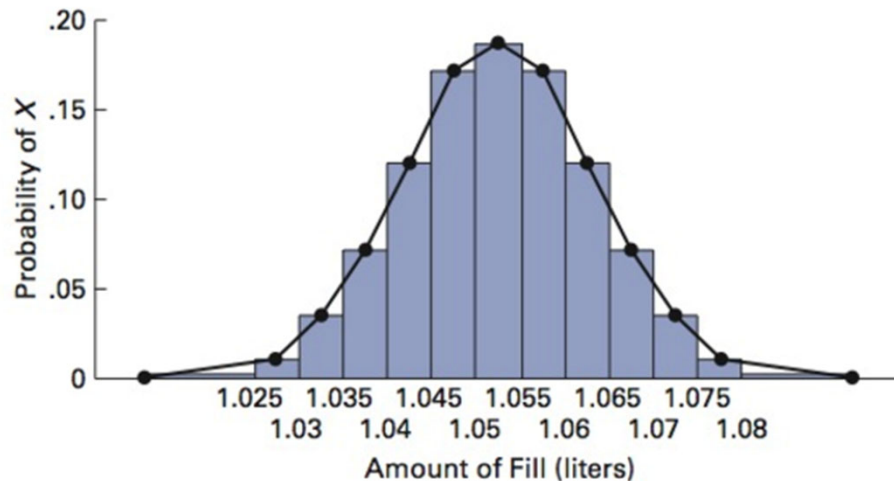
Cont'd

- Computing the probability of a continuous variable over a specified interval is like determining the **area** of the corresponding relative frequency histogram over the same interval
 - It is time consuming to construct such relative frequency histogram as many data values need to be collected
 - Sometimes it may not be possible to get the required data points
- Is there an alternative way to compute probabilities of a continuous variable without involving the relative frequency histogram?

Continuous Probability Distributions

Cont'd

- The figure below shows the relative frequency histogram and percentage polygon for the distribution of the amount filled in 10,000 bottles
 - Polygon is a graph made by joining the middle top points of each class interval of relative frequency histogram



- Determining the area of a relative frequency histogram over an interval is approximately equivalent to finding the area under the polygon over the same interval
- If we can assume that the polygon actually follows some known mathematical curve, then finding the area under such curve becomes very easy

Continuous Probability Distributions

Cont'd

■ Probability Density Function

- A probability density function, or density function of a continuous random variable is a function that describes the relative **likelihood** for this random variable to take on a given value
 - One may consider a density function is an approximation to the percentage polygon of its relative frequency distribution
 - A density function, f , for a random variable X has the following features:
 - $f(x) \geq 0$ for all x of X
 - The area bounded by the curve of $f(x)$ and the x -axis is equal to 1
-
- The most important form of density function is called the **Normal Density Function**

Normal Distribution

Cont'd

- If the density function of a continuous random variable can be best described by normal density function, we say the random variable follows a Normal Distribution
- The **Normal Density Function** is defined as:

$$f(x) = \frac{1}{\sqrt{2\pi}\sigma} e^{-\left(\frac{1}{2}\right)\left[\frac{x-\mu}{\sigma}\right]^2}$$

where x = any value that the continuous random variable X can take in the range of $-\infty$ to $+\infty$

μ = mean of the population

σ = standard deviation of the population

e = the mathematical constant approximated by 2.71828...

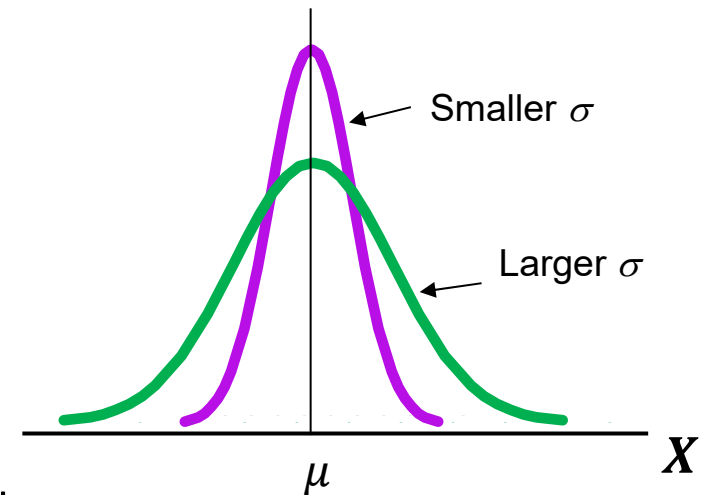
π = the mathematical constant approximated by 3.14159...

- Often denoted as **$X \sim N(\mu, \sigma^2)$**

Normal Distribution

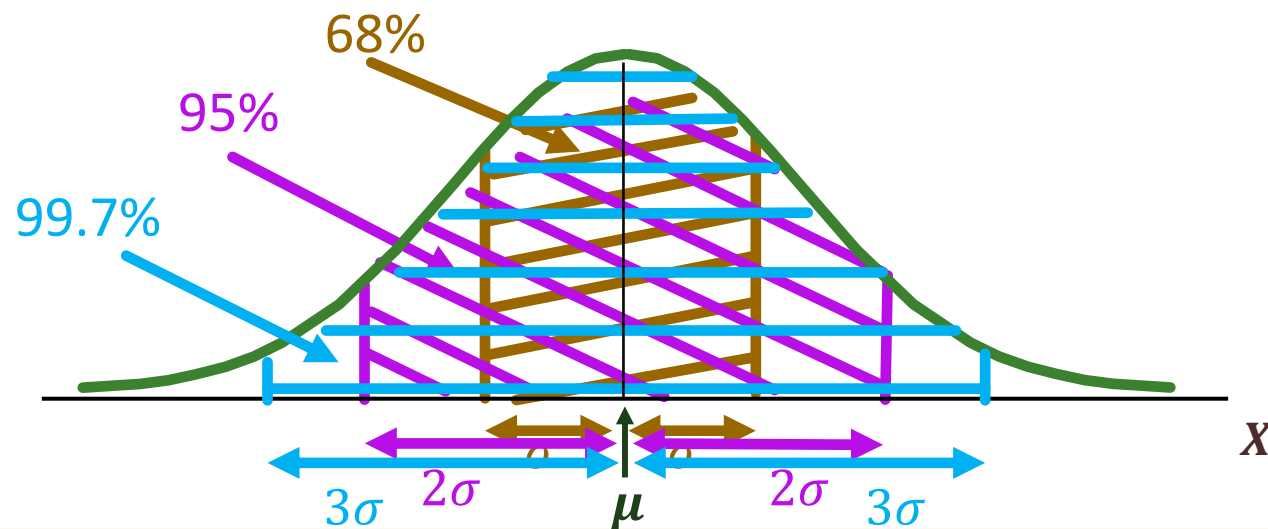
Cont'd

- For $X \sim N(\mu, \sigma^2)$
 - Has an infinite theoretical range, i.e.
 $-\infty$ to $+\infty$
 - Bell shaped
 - Symmetrical about $X = \mu$
 - Mean, median and mode are identical
 - The spread is determined by σ
 - For smaller σ , the X values are clustered more closely around μ
 - For larger σ , the X values are more spread out and away from μ
 - Follows the **Empirical Rule**



The Empirical Rule

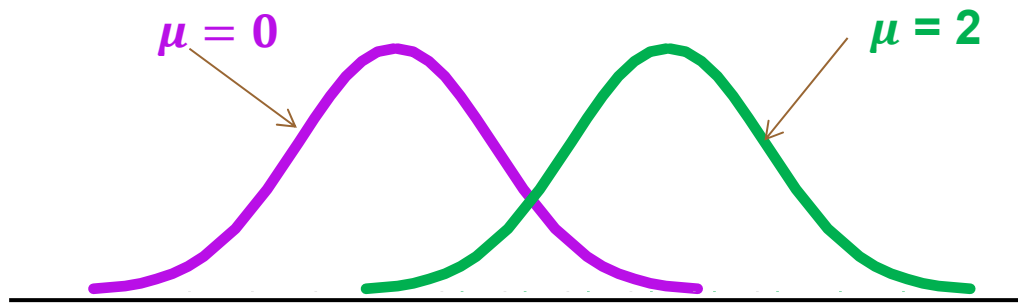
- The Empirical Rule said that
 - Area within $\mu \pm \sigma$ equals 68% approximately
 - Area within $\mu \pm 2\sigma$ equals 95% approximately
 - Area within $\mu \pm 3\sigma$ equals 99.7% approximately



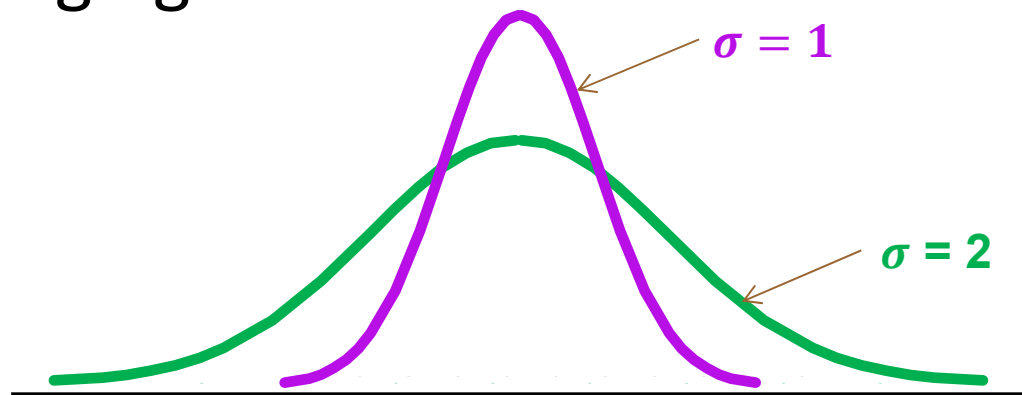
Normal Distribution

Cont'd

- Changing μ shifts the distribution left or right

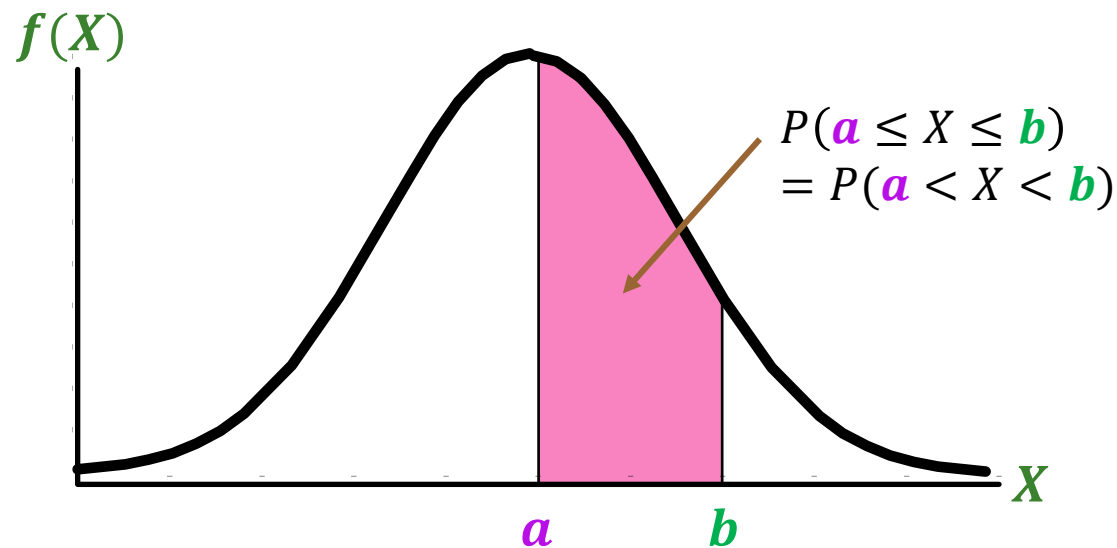


- Changing σ increases or decreases the spread



Computing Normal Probabilities

- The **total area** under the curve is **1**
- Probability is measured by the **area under the curve**
- Note that the probability of any individual value is zero by definition, i.e. $P(X = a) = 0$

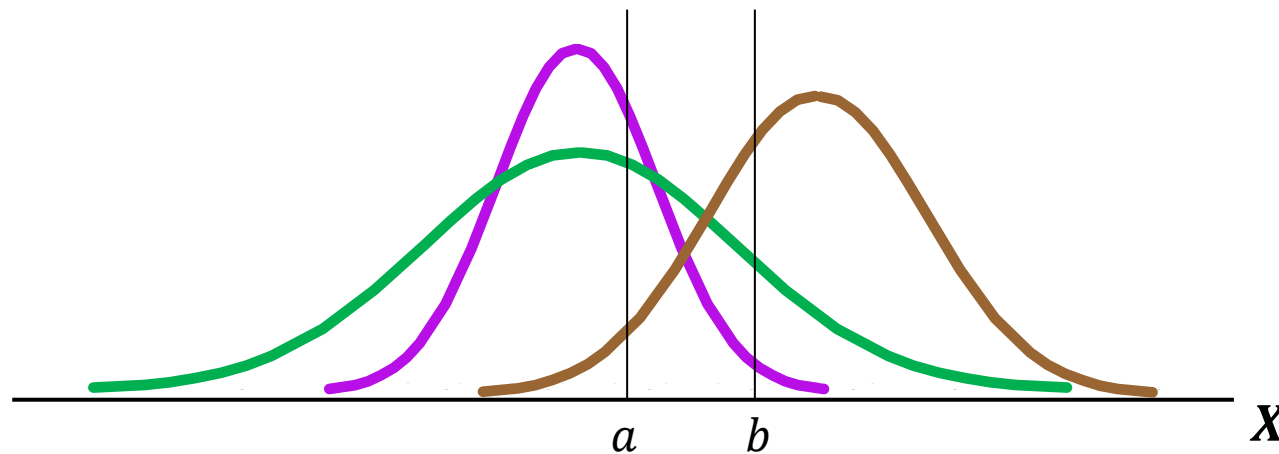


Computing Normal Probabilities

Cont'd

- Area under the curve is computed as

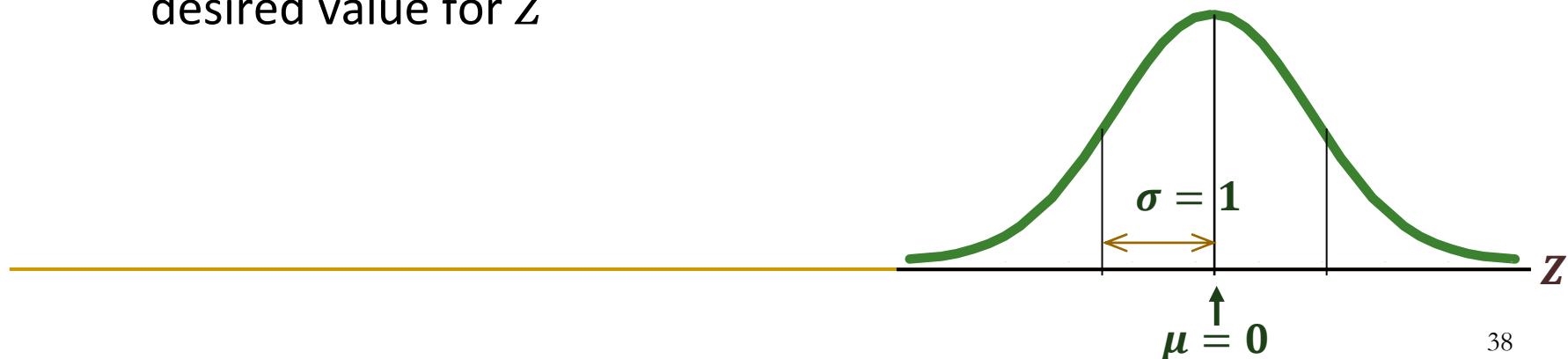
$$P(a \leq X \leq b) = \frac{1}{\sqrt{2\pi}\sigma} \int_a^b e^{-\left(\frac{1}{2}\right)\left[\frac{x-\mu}{\sigma}\right]^2} dx$$



- Varying the parameters μ and σ , we obtain different Normal Distributions

The Standardized Normal Distribution

- When a random variable Z follows a Normal Distribution with $\mu = 0$ and $\sigma = 1$, we say Z follows a **Standard Normal Distribution**
- Often denoted as $Z \sim N(0, 1^2)$
- An advantage of Z distribution is that the probabilities for Z are available on standard normal tables
 - A table gives the probability that Z is between the $-\infty$ and a desired value for Z



The Standardized Normal Distribution

Cont'd

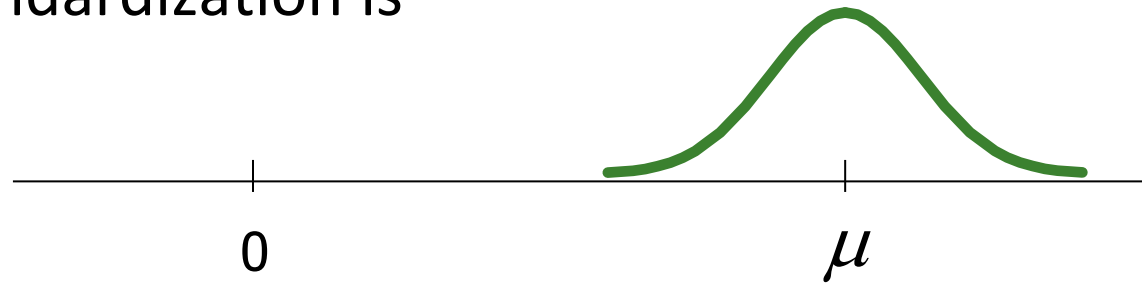
- For any $X \sim N(\mu, \sigma^2)$, it can be standardized to $Z \sim N(0, 1^2)$ with the following formula

$$Z = \frac{X - \mu}{\sigma}$$

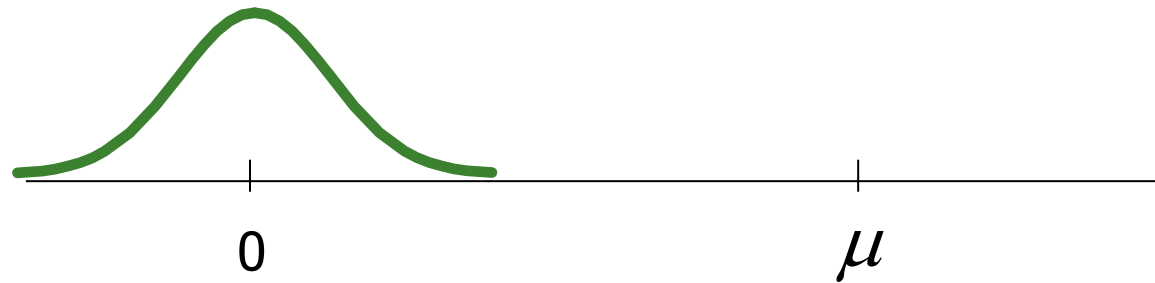
Standardization of Normal Distributions

- The idea of standardization is

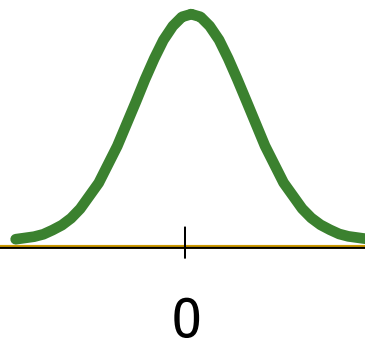
Step 1: X



Step 2: $X - \mu$



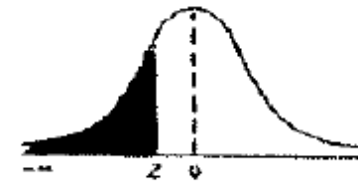
Step 3: $Z = \frac{X - \mu}{\sigma}$



The Standardized Normal Table

The column gives the value of Z to the second decimal point

The Cumulative Standardized Normal Distribution Entry represents area under the cumulative standardized normal distribution from $-\infty$ to Z



Z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
-6.0	0.000000001									
-5.5	0.000000019									
-5.0	0.000000287									
-4.5	0.000003398									
-4.0	0.000031671									
-3.9	0.00005	0.00005	0.00004	0.00004	0.00004	0.00004	0.00004	0.00004	0.00003	0.00003
-3.8	0.00007	0.00007	0.00007	0.00006	0.00006	0.00006	0.00006	0.00005	0.00005	0.00005
-3.7	0.00011	0.00010	0.00010	0.00010	0.00009	0.00009	0.00008	0.00008	0.00008	0.00008
-3.6	0.00016	0.00015	0.00015	0.00014	0.00014	0.00013	0.00013	0.00012	0.00012	0.00011
-3.5	0.00023	0.00022	0.00022	0.00021	0.00020	0.00019	0.00019	0.00018	0.00017	0.00017
-3.4	0.00034	0.00032	0.00031	0.00030	0.00029	0.00028	0.00027	0.00026	0.00025	0.00024

The row shows the value of Z to the first decimal point

The value within the table gives the probability from $Z = -\infty$ up to the desired Z value
 $P(Z < -3.45) = 0.00028$

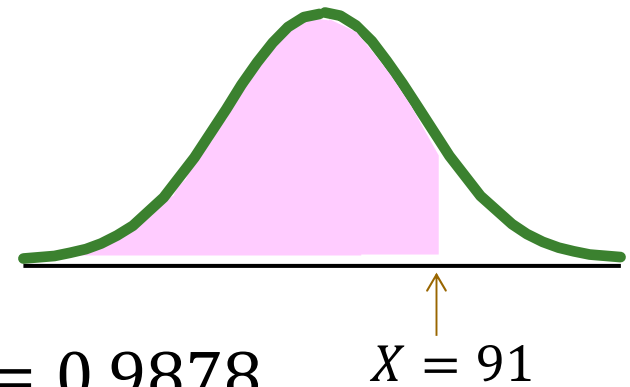
Computing Normal Probabilities – Example

- A set of final exam scores was normally distributed with a population mean 73 and population standard deviation 8
- 1. What is the probability of getting a score not higher than 91 on this exam?

Let the score be X , and $X \sim N(73, 8^2)$

$$P(X \leq 91)$$

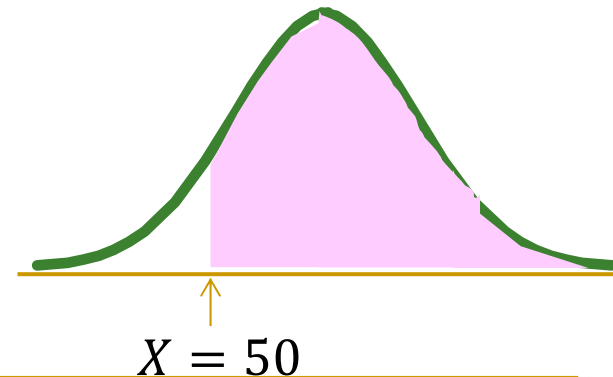
$$= P\left(Z \leq \frac{91-73}{8}\right) = P(Z \leq 2.25) = 0.9878$$



Computing Normal Probabilities – Exercise

Cont'd

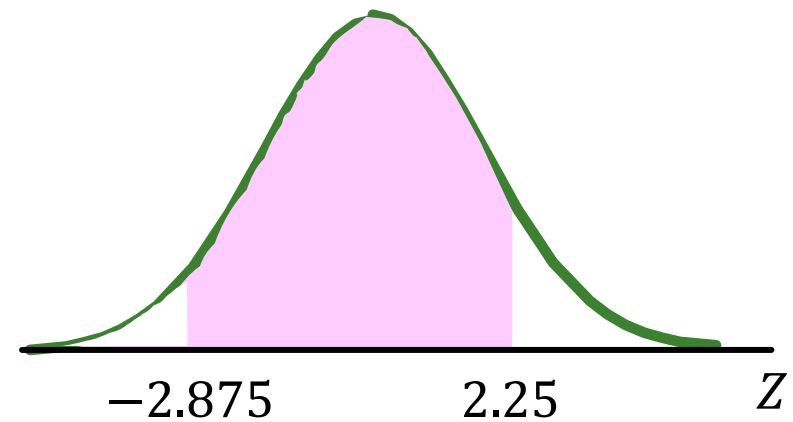
2. If the passing score is 50, what is the chance that a student can pass the exam?



Computing Normal Probabilities – Exercise

Cont'd

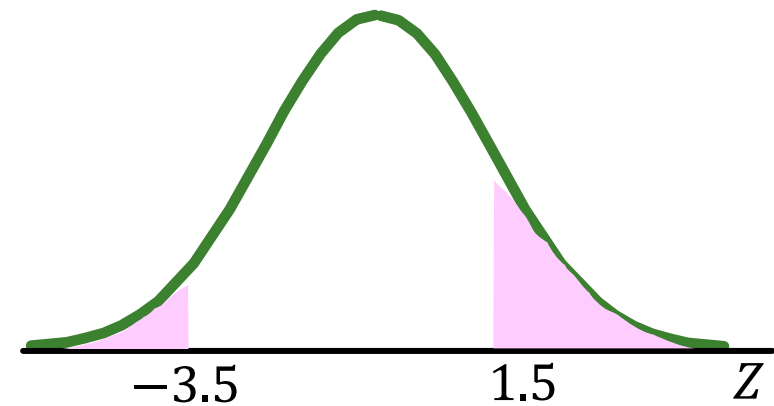
3. What percentage of students scored between 50 and 91?



Computing Normal Probabilities – Exercise

Cont'd

4. What percentage of students scored below 45 or above 85?

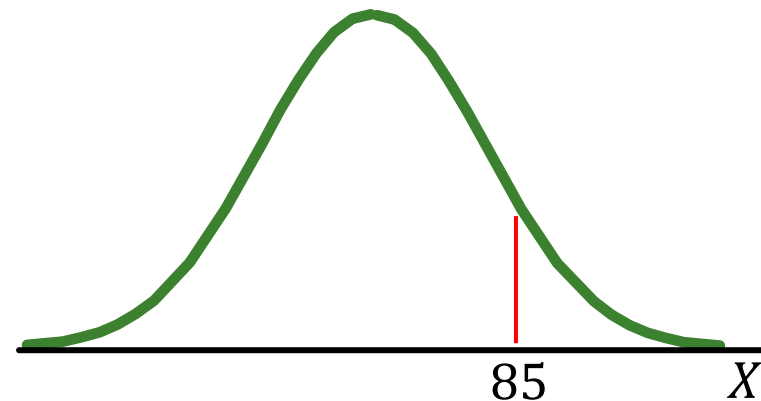


Computing Normal Probabilities – Exercise

Cont'd

5. What is the probability for a student to score exactly 85?

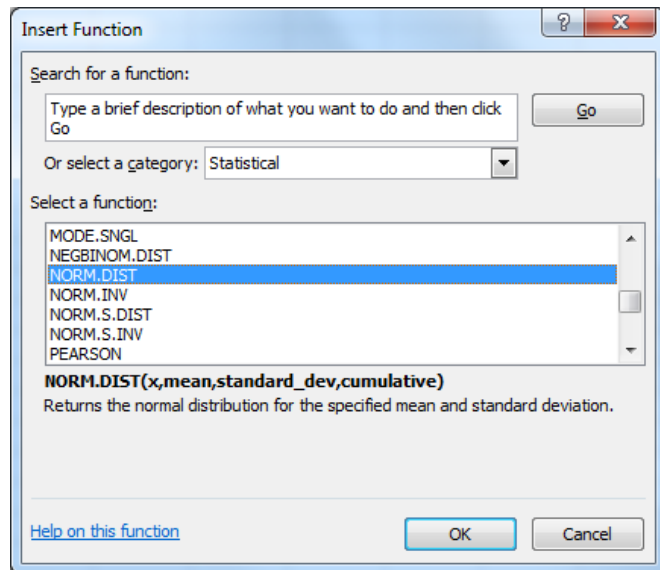
Not an area,
but just a line!!!



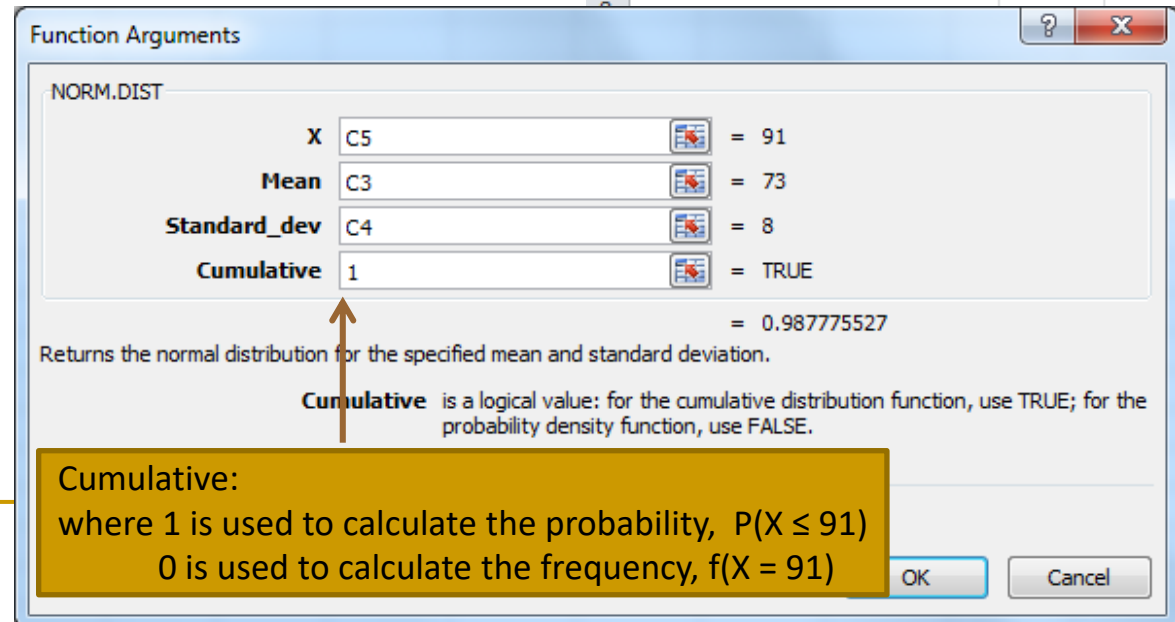
Computing Normal Probabilities in Excel

Step 1: Type the given information (μ , σ , X)

Step 2: Insert the “NORM.DIST” function



B7		f_x	
	A	B	C
1	Normal Distribution		
2			
3	Population Mean	$\mu =$	73
4	Population Standard Deviation	$\sigma =$	8
5		$X =$	91
6			
7	P(X ≤ 91)		



Computing Normal Probabilities in Excel

Cont'd

NORM.DIST ☐ ☒ f_x `=NORM.DIST(C5,C3,C4,1)`

	A	B	C	D	E
1	Normal Distribution				
2					
3	Population Mean	$\mu =$	73		
4	Population Standard Deviation	$\sigma =$	8		
5		$X =$	91		
6					
7	$P(X \leq 91)$	<code>=NORM.DIST(C5,C3,C4,1)</code>			
8		<code>NORM.DIST(x, mean, standard_dev, cumulative)</code>			

$=NORM.DIST(X, \mu, \sigma, 1)$

B7 f_x `=NORM.DIST(C5,C3,C4,1)`

	A	B	C	D
1	Normal Distribution			
2				
3	Population Mean	$\mu =$	73	
4	Population Standard Deviation	$\sigma =$	8	
5		$X =$	91	
6				
7	$P(X \leq 91)$	0.98778		

Recovering X Values from Known Probabilities

- With a given (cumulative) probability, we can use the Z table to recover the Z value
- With μ and σ of the X variable, we can recover the X value

Recovering X Values – Example

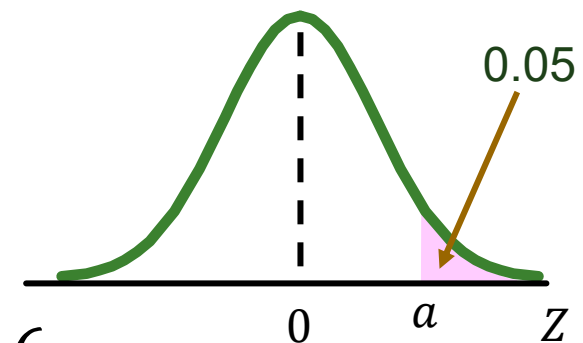
- Given that the exam scores, X , follow normal distribution with mean 73 and standard deviation 8, i.e. $X \sim N(73, 8^2)$
- 1. What is the minimum score a student needs in order to be in the top 5% of the class?

For $P(Z \geq a) = 0.05$, $a = 1.645$

$$\text{As } Z = \frac{X - \mu}{\sigma},$$

$$\text{hence } X = \mu + Z\sigma$$

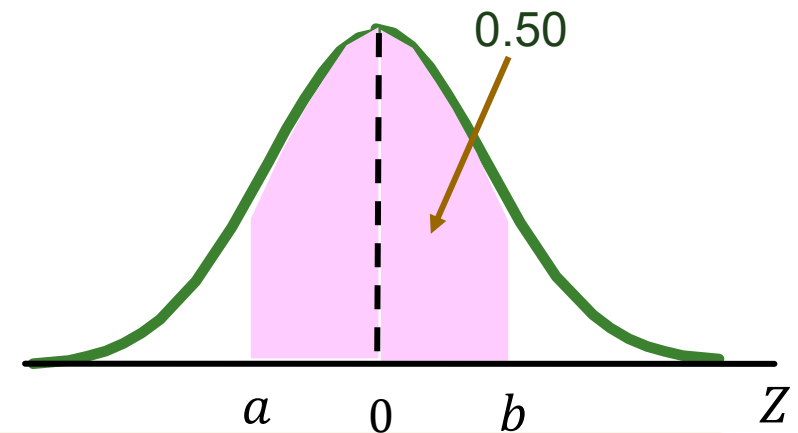
$$= 73 + 1.645 \times 8 = 86.16$$



Recovering X Values – Exercise

Cont'd


2. The middle 50% of the students scored between what two scores?

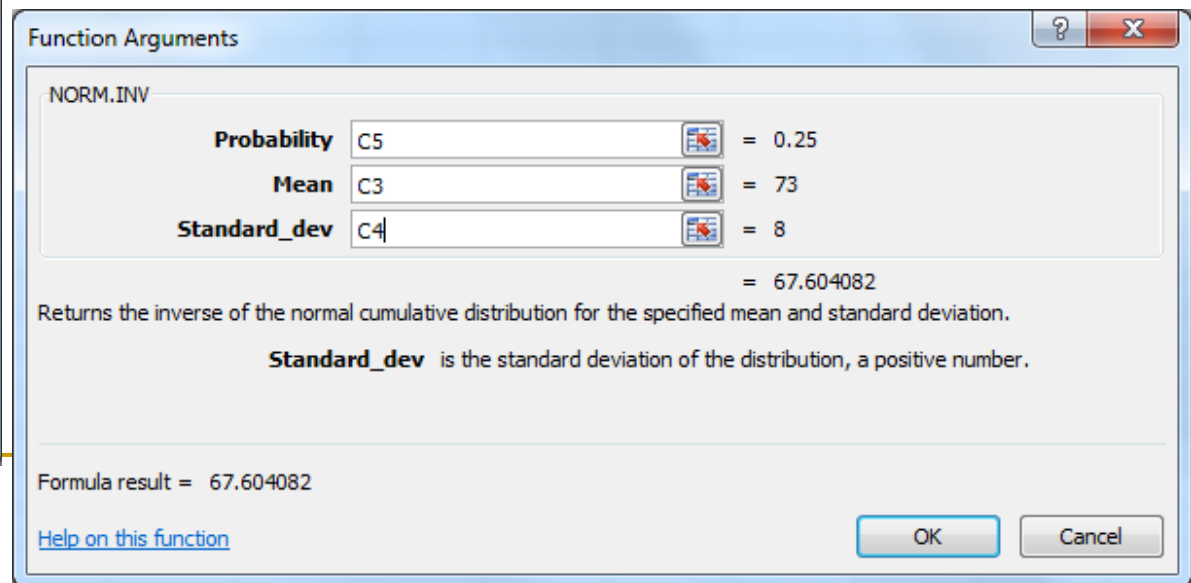
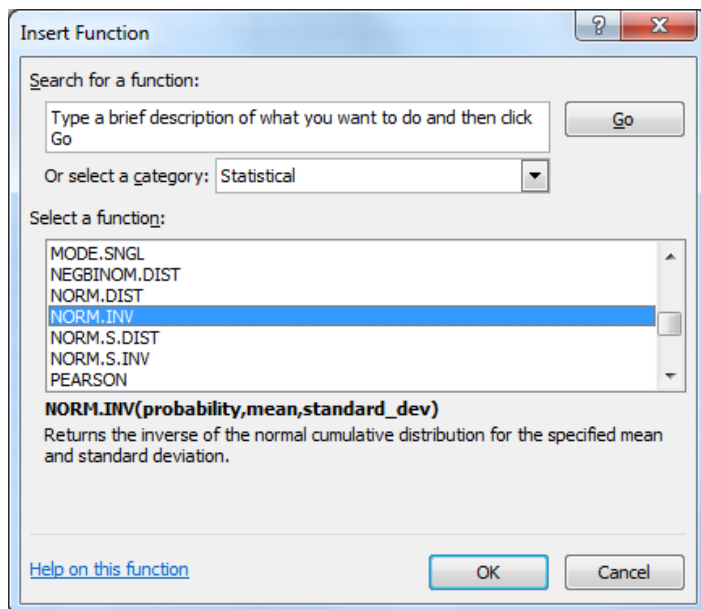


Recovering X Values in Excel

Step 1: Type the given information (μ , σ , P)

Step 2: Insert the “NORM.S.INV” function for recovering Z value; “NORM.INV” for recovering X value

B7			
	A	B	C
1	Normal Distribution		
2			
3	Population Mean	$\mu =$	73
4	Population Standard Deviation	$\sigma =$	8
5	Cumulative Probability	$P =$	0.25
6			
7	Z		
8	X		



Recovering X Values in Excel

Cont'd

B8		f_x	=NORM.INV(C5,C3,C4)	
	A	B	C	D
1	Normal Distribution			
2				
3	Population Mean	$\mu =$	73	
4	Population Standard Deviation	$\sigma =$	8	
5	Cumulative Probability	$P =$	0.25	
6				
7	Z	-0.67449	← =NORM.S.INV(P)	
8	X	67.60408	← =NORM.INV(P, μ , σ)	

Importance of Normal Distribution

- Most **common** continuous distribution used in statistics
- Provides the basis for statistical inference because of its relationship to the **Central Limit Theorem**
 - To be discussed in Topic 4
- Can be used to **approximate** various **discrete probability distributions**, such as Binomial distribution, for large sample size, therefore, simplifying computations
 - To be discussed in Topic 7

You Sometimes Get More Than You Pay For

- According to McDonald's "fact sheet", their ice cream cones weigh 3.7 ounces and contain 170 calories
- Do the ice cream cones really weigh exactly 3.7 ounces?
- To get 3.7 ounces for every cone would require a very fine-tuned machine, or an employee with a very good skill and sense of timing
- Thus, we expect some natural variation in the weight of these cones



You Sometimes Get More Than You Pay For

Cont'd

- If you buy one ice cream cone everyday through out the week, you may be surprised that they all weighed more than 3.7 ounces
- How likely this would happened?