

CS4335 Tutorial 8

Question 5a.

```
minDiff() {  
    int min = positive infinity;  
    for (int i = 1; i <= x.size; i++)  
        if(abs(x[i]-1 < min)  
            min = x[i]-1;  
    return min;  
}
```

Question 5b.

```
minDiff (int left, int right) {  
    if (right - left == 0 || right - left == 1) return min (x[left] - left, x[right] - right);  
    int mid = floor ((left + right) / 2);  
    if (x[mid] > mid) return minDiff (left, mid);  
    else return minDiff (mid, right);  
}  
minDiff (1, x.size);
```

Question 5c.

$$\begin{aligned}T(n) &= T\left(\frac{n}{2}\right) + 1 \\&= T\left(\frac{n}{2^2}\right) + 1 + 1 \\&= T\left(\frac{n}{2^k}\right) + k\end{aligned}$$

$$\begin{aligned}\frac{n}{2^k} &= 1 \\k &= \log_2 n\end{aligned}$$

$$\begin{aligned}T(n) &= T(1) + \log_2 n \\&= 1 + \log_2 n \\T(n) &= O(\log n)\end{aligned}$$

Question 6a.

```
maxNumberOfSquaredIntervals(int[] X) {  
    for (int i = 1; i <= X.size; i++) {  
        find the shortest squared interval Y end at i;  
        if (Y.size == 0) return null;  
    }  
    find max number of compatible Y intervals n with interval scheduling algorithm;  
    return n;  
}
```

Question 6b.

Running time at worst case:

$$O(n^2) + O(n) \\ = O(n^2)$$

Question 6c.

Let A = maximal set of non-overlapped squared interval.

If A has interval X starts at time i.

Replace X with another interval Y starts at time i.

A's optimality is unchanged.

For each I, A can contain at most one interval starting at i.

Thus, the problem is equivalent to the interval scheduling problem and the algorithm is correct.