

# EE 4211 Computer Vision

## Lecture 13: Summary and Presentation

Semester B, 2021-2022

# Schedules

Week	Date	Topics
1	Jan. 11 (face to face)	Introduction/Imaging
2	Jan. 18 (online)	Image enhancement in spatial domain
3	Jan. 25 (online)	Image enhancement in frequency domain (HW1 out)
4	Feb. 8 (online)	Morphological processing
5	Feb. 15 (online)	Image restoration (HW1 due)
6	Feb. 22 (online)	Midterm (no tutorials this week)
7	Mar. 1 (online)	Edge detection (HW2 out)
8	Mar. 8 (online)	Image segmentation
9	Mar. 15 (online)	Face recognition with PCA, LDA (tutorial on segmentation) (HW2 due)
10	Mar. 22 (online)	Face recognition based on deep learning (Quiz on two code questions, 1 hour) Image segmentation based on deep learning
11	Mar. 29 (online)	Object detection with traditional methods Object detection based on deep learning (tutorial on detection)
12	Apr. 5	Events / Public Holidays
13	Apr. 12 (online)	Summary and Invited project presentation

# Course Content

- First for the summary and the report information
- Then 6 group students will do presentation with the following sequence

55771909	CHAN Ka Yang	5 detection
56224506	LAU Shing Kuen	5 detection
55359060	LO Yuk Long	5 detection
55809965	WONG Ho Sum	5 detection
55691100	CHOW Wai Kit	13 Detection
55228060	KUK Man Ho	13 Detection
55691239	NG Chun Hei	13 Detection
56063675	NG King Hon	13 Detection
55956246	NANDI Mitsumi	3 Detection
55907774	PATRA Yuvraj	3 Detection
55877661	RAHMAN Alvi	3 Detection
55701944	CHAN Yiu Yu	10 Segmentation
56204372	CHENG Cheung Yu	10 Segmentation
56046680	LEUNG Chun Wai	10 Segmentation
55670096	RUAN Yuyan	10 Segmentation
55709099	LAI Daniel	8 Segmentation
55689686	TSO Tsz Shing	8 Segmentation
55678611	YANG Alva	8 Segmentation
55679306	CHAN Timothy Chit Yin	14 Segmentation
55701030	CHENG Kwan Ho	14 Segmentation
55684920	TSUI Wai Chiu	14 Segmentation

- 10 mins for presentation and ~5 mins for Q & A

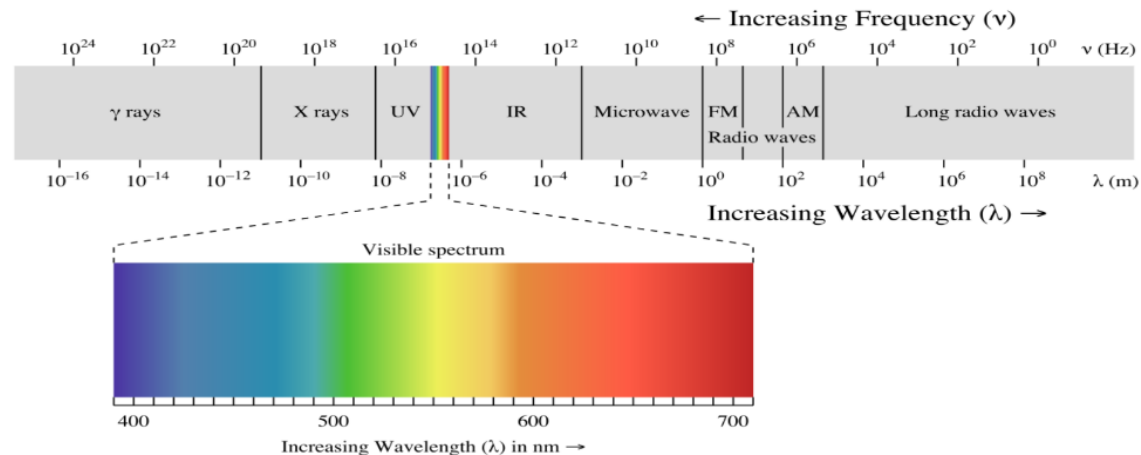
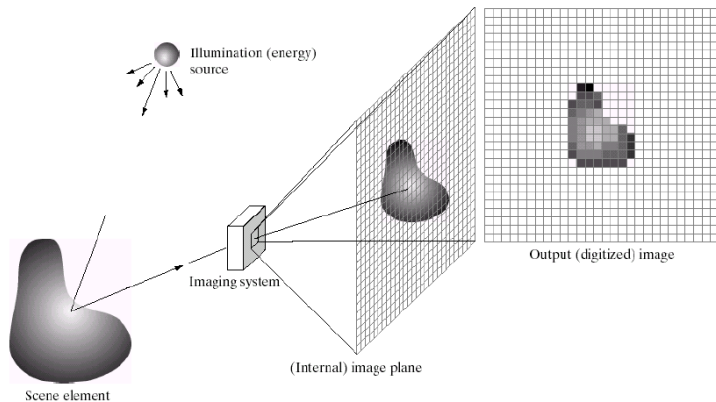
# Final exam

- Online mode May 6<sup>th</sup>, 9:30 AM -11:30 AM
- 10% Multiple answers, 10% True/False, 80% calculation and understanding questions
- You are responsible for receiving the questions on Canvas, except the Multiple answers and True/False questions, please **hand-write all answers on blank answer sheets, compile the answers into a single PDF file, and upload the file to canvas/assignment before the deadline of the exam.**
- You have extra 15 mins to upload your results through [canvas/assignment](#)
- If you found there are some problems to upload your results, please [send me your results through email asap](#) (yxyuan.ee@cityu.edu.hk)

# Lecture 1: Digital image fundamentals

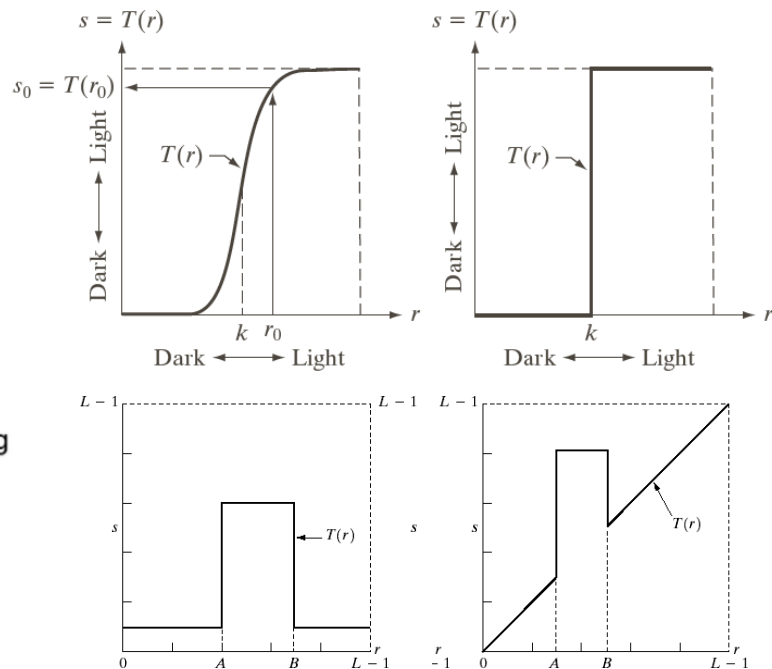
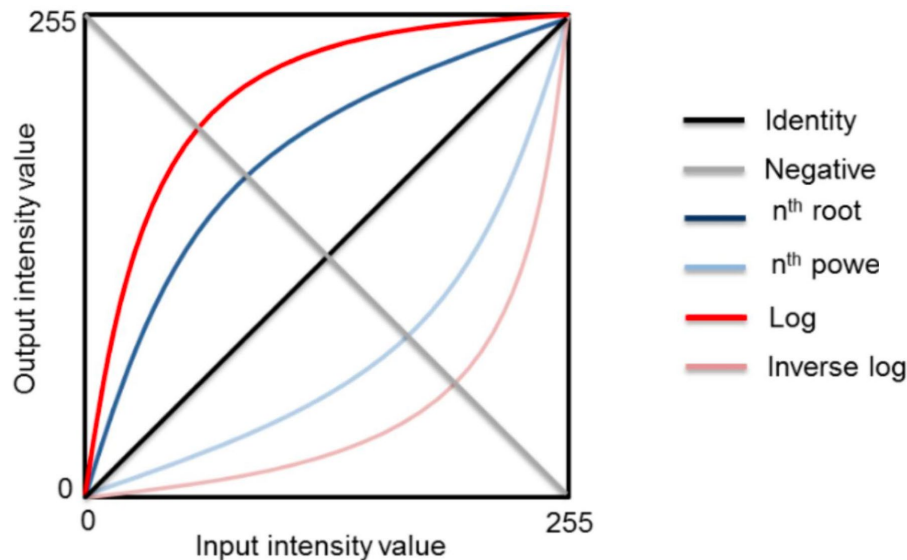
## ■ Section

- How to visualize light: Reflected light, Absorbed light, Emitted light
- Different image systems: the differences, the suitable applications
- For example, X-Rays can be utilized to identify the holes in the dental
- Microwave Imaging can be utilized for weather forecast



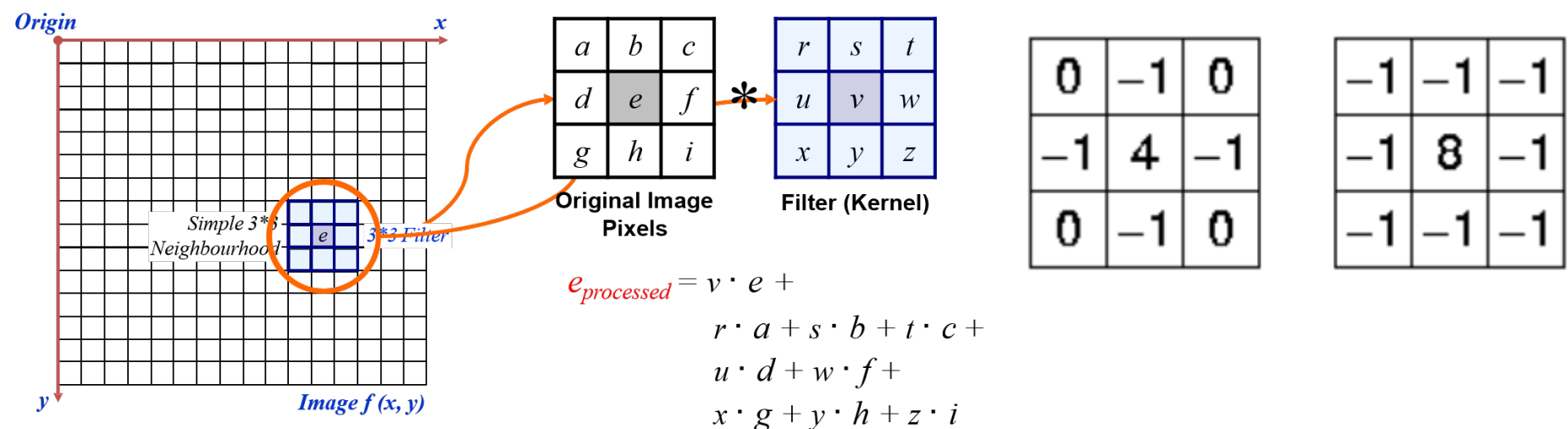
# Lecture 2: Image enhancement: Spatial Domain

- **Point processing** – Gray values change without any knowledge of its surroundings (Part I)(subjective)
  - Log, power-law, linear, piecewise linear (Contrast Stretching, Intensity-level Slicing)
  - Histogram Equalization (pdf->cdf->transformation) (calculate)



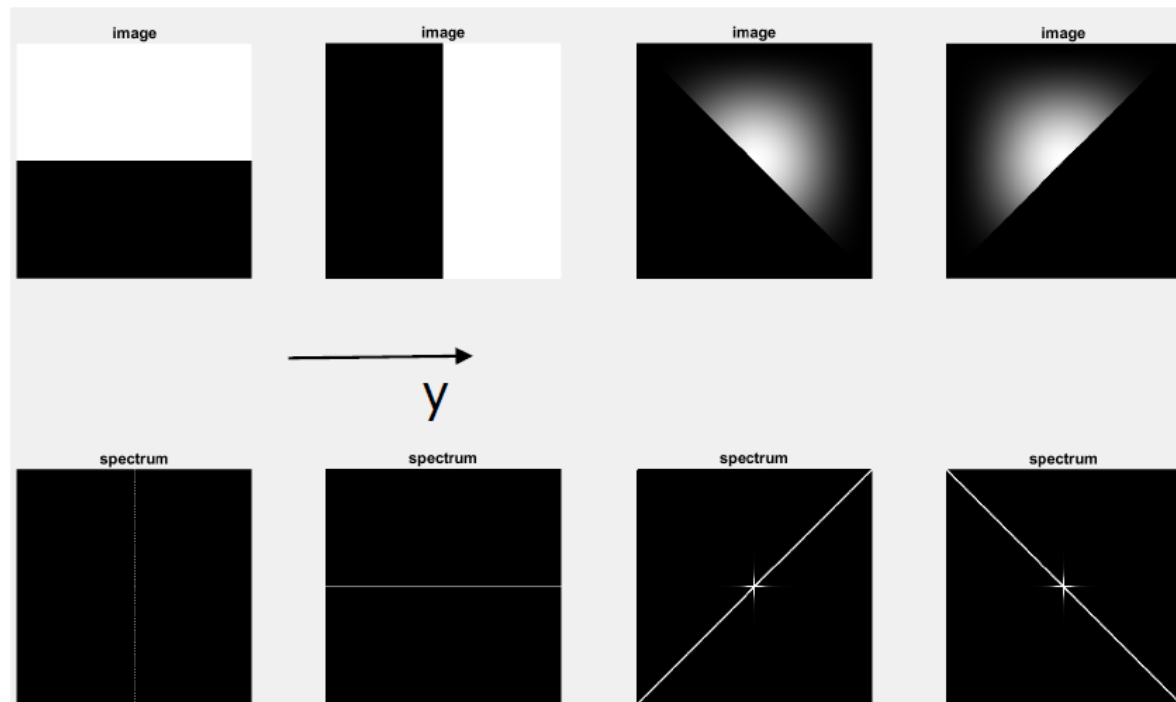
# Lecture 2: Image enhancement: Spatial Domain

- **Neighborhood processing (filtering)** – Gray values change depending on the gray values in a small neighborhood of pixels around the given pixel (Part I)
  - Smoothing filters: Averaging filters, Order-Statistics filters
  - Median filters
  - Sharpening: Laplacian filters, Sobel filter



# Lecture 3: Image enhancement: Frequency Domain

- Frequency transformation (matching image with spectrum)
- Need to know specific corresponding information
  - The longitudinal periodic changes in the spatial domain are reflected on the X-axis of the spectrum
  - The periodic change across horizon in the spatial domain is reflected on the Y-axis of the spectrum





# Important Fourier Transform Pairs

rectangle centred at origin  
with sides of length  $X$  and  $Y$

When  $X$  is larger than  $Y$ , then the value

$$F(u, v) = \int \int f(x, y) e^{-j2\pi(ux+vy)} dx dy,$$

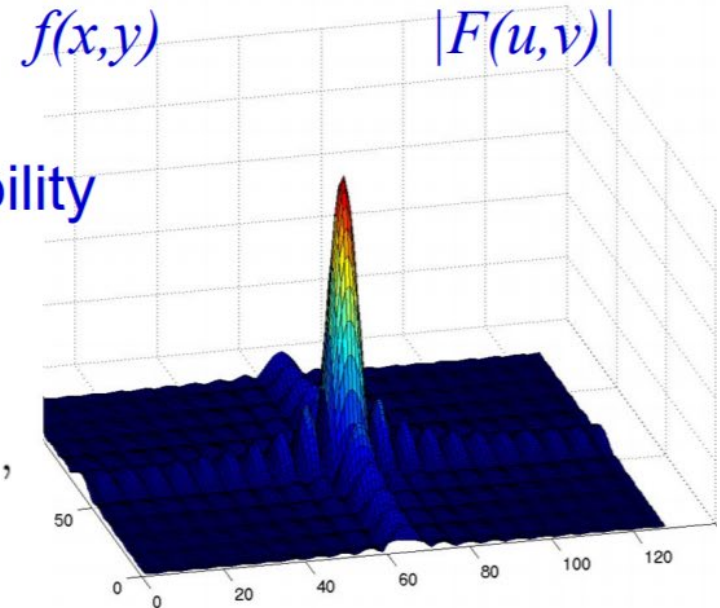
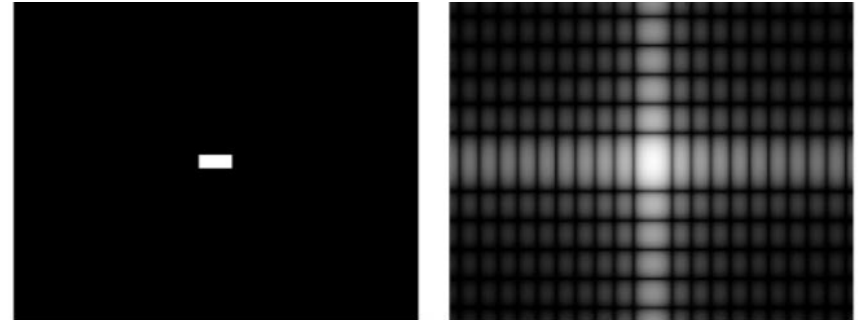
$$= \int_{-X/2}^{X/2} e^{-j2\pi ux} dx \int_{-Y/2}^{Y/2} e^{-j2\pi vy} dy, \quad \text{separability}$$

$$= \left[ \frac{e^{-j2\pi ux}}{-j2\pi u} \right]_{-X/2}^{X/2} \left[ \frac{e^{-j2\pi vy}}{-j2\pi v} \right]_{-Y/2}^{Y/2},$$

$$= \frac{1}{-j2\pi u} [e^{-juX} - e^{juX}] \frac{1}{-j2\pi v} [e^{-jvY} - e^{jvY}],$$

$$= XY \left[ \frac{\sin(\pi Xu)}{\pi Xu} \right] \left[ \frac{\sin(\pi Yv)}{\pi Yv} \right]$$

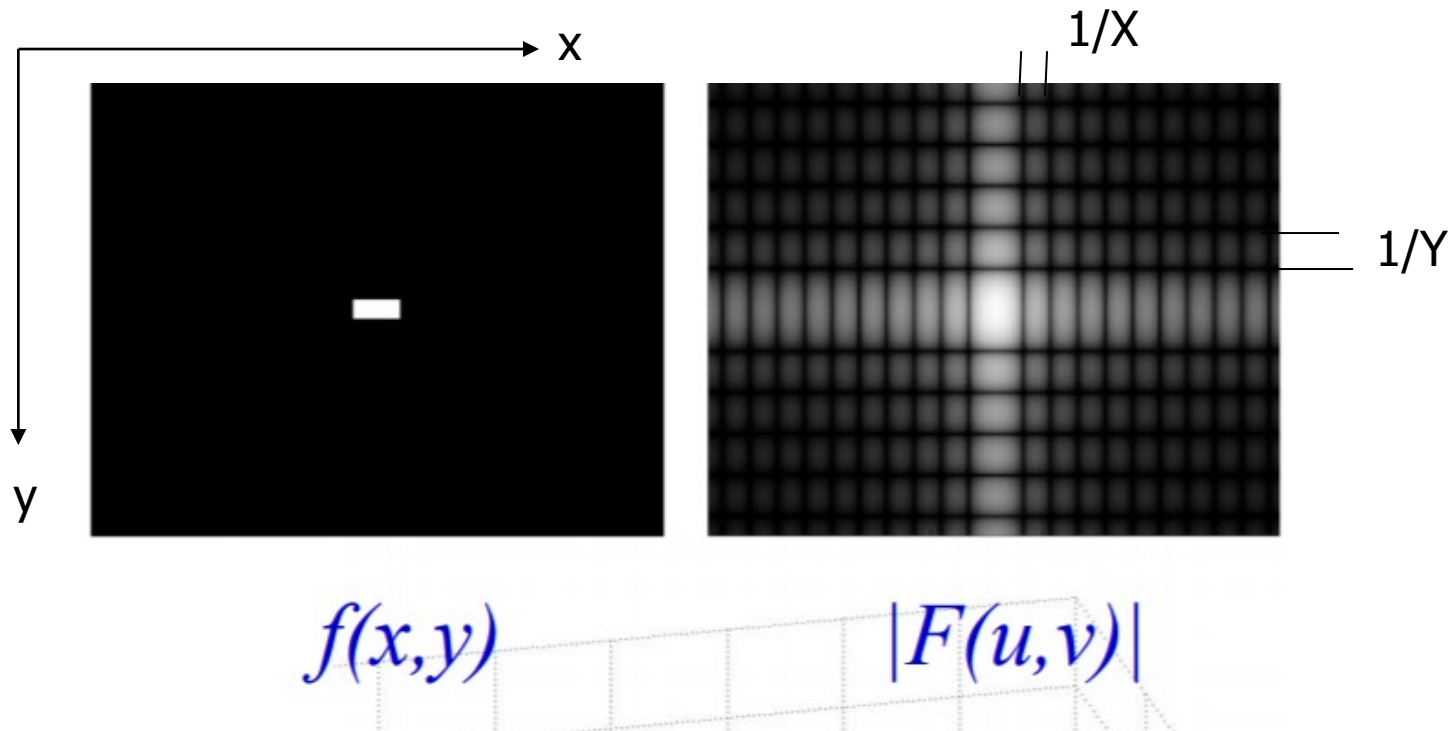
$$= XY \text{sinc}(\pi Xu) \text{sinc}(\pi Yv).$$



$|F(u,v)|$

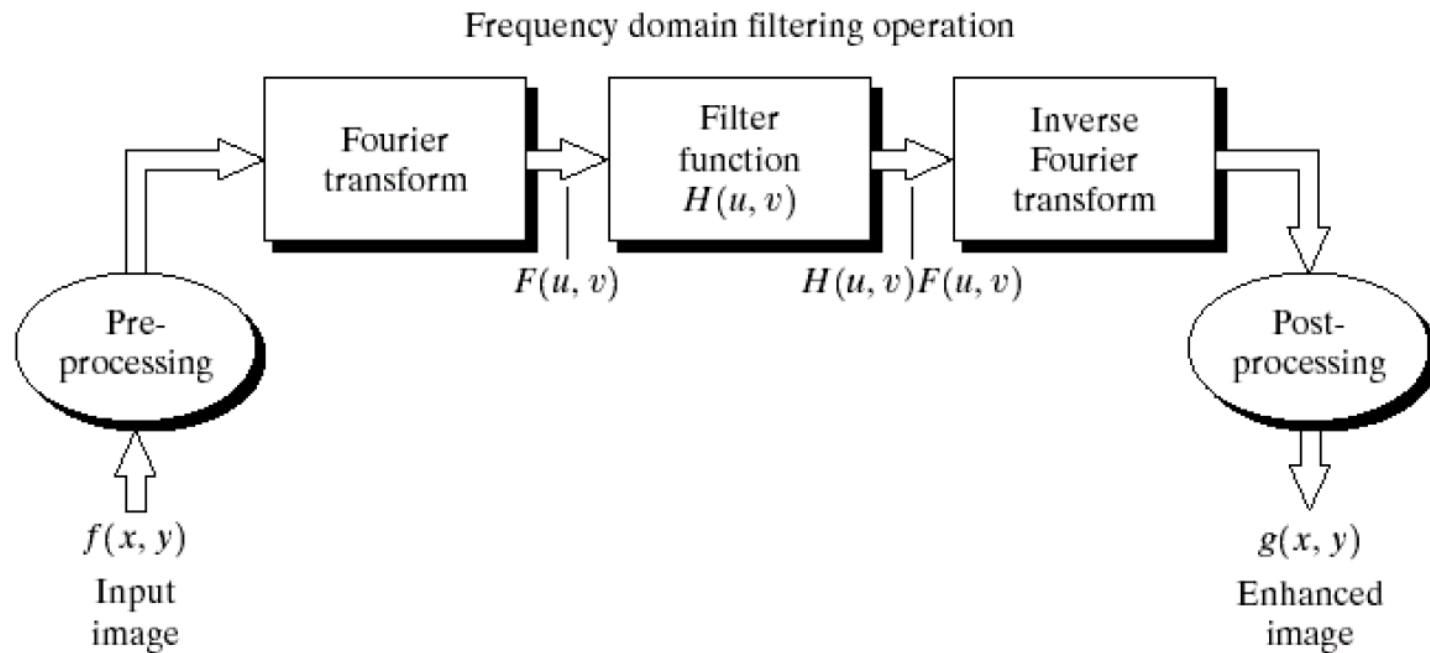
# Important Fourier Transform Pairs

- The zero crossing of the spectrum is closer in the horizontal direction because the rectangle is longer in that direction



# Lecture 3: Image enhancement: Frequency Domain

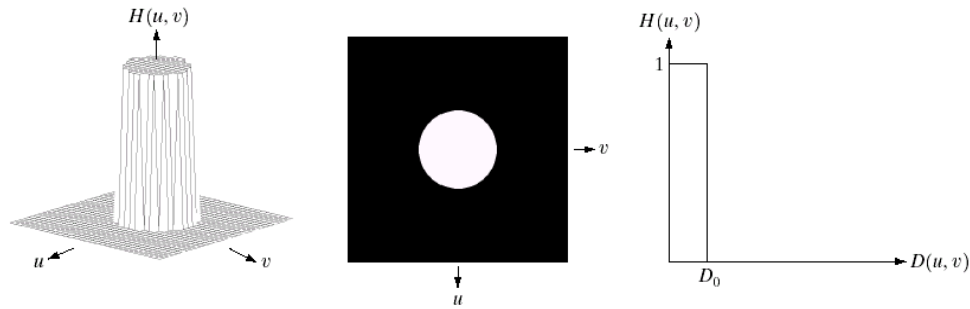
- Image Enhancement in Frequency Domain (workflow)



# Lecture 3: Image enhancement: Frequency Domain

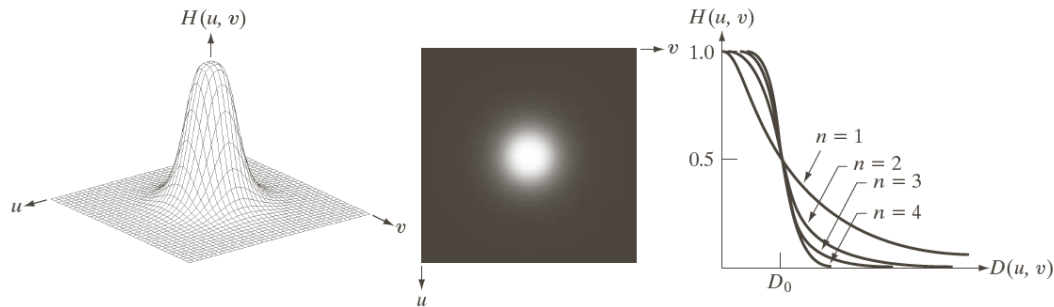
- Filtering in Frequency Domain
  - **Low-Pass Filtering** (ideal, butterworth, gaussian): passes all frequencies with magnitudes below a specific level, and attenuates all frequencies above that level.
  - **High-Pass Filtering**: does the opposite.
  - **Laplacian Filtering**: sharpen
  - **Homomorphic Filtering** (Principle, separating Illumination and Reflection)
    - Illumination and Reflection have different characteristics: Illumination components tend to be slow in spatial variation (low frequency components); Reflection of various objects tends to vary abruptly (high frequency components)
  - **Selective Filtering – Bandpass/Bandreject, Notch Filters** (A “notch” filter rejects (or passes) frequencies at a specific point)

# Comparison with different filter banks



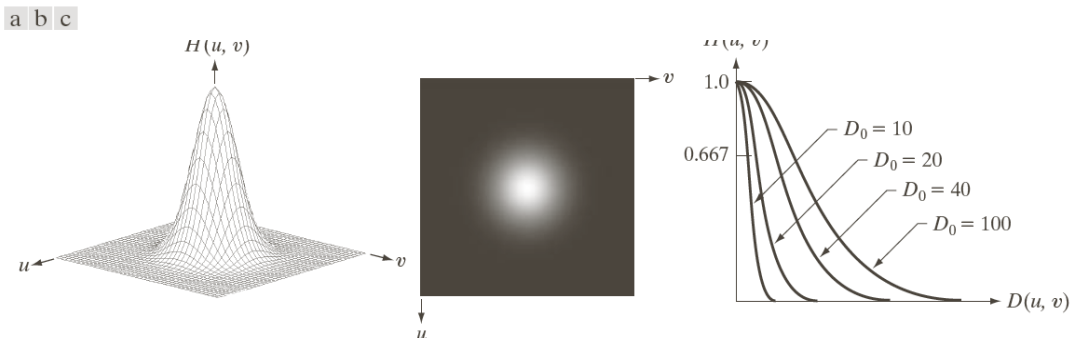
## ■ Ideal low filter bank

- all frequencies inside a circle of radius  $D_0$  are passed with no attenuation
- Presence of ripples/waves whenever there are boundaries in the image – “ringing effect”



## ■ Butterworth lowpass filter

- Reduces “ringing” while keeping clear cutoff
- Tradeoff between amount of ringing and sharpness of cutoff



## ■ Gaussian lowpass filter

- No ringing, but allows high frequencies to pass

a b c

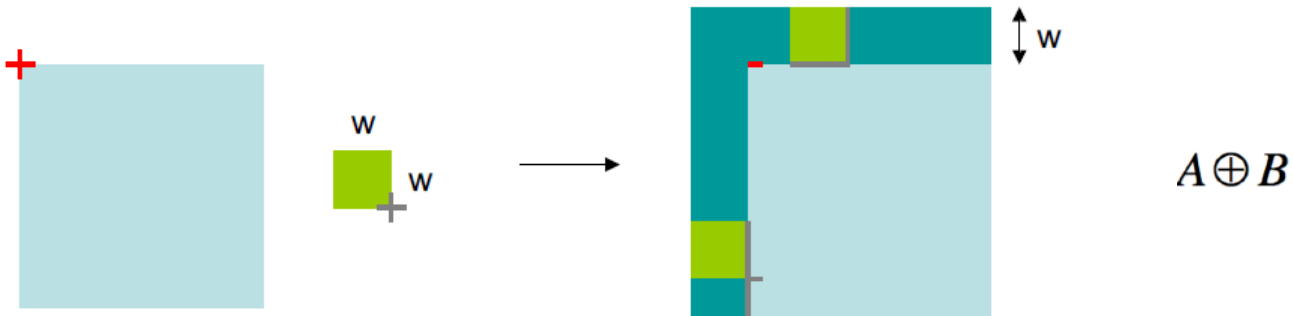
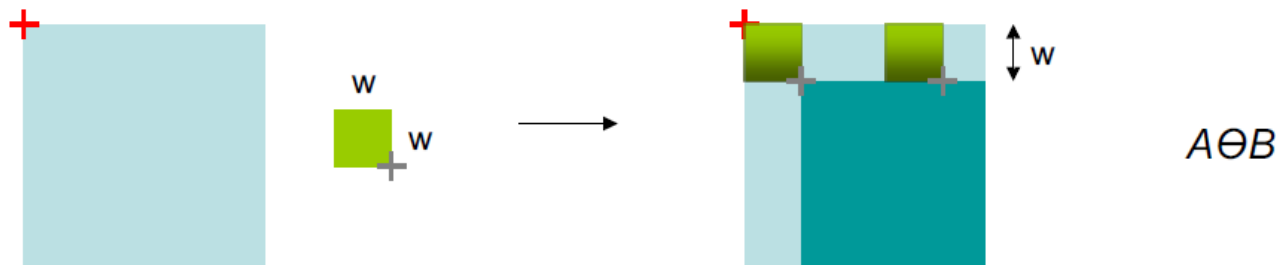
(a) Perspective plot of the transfer function  
(b) Filter displayed as an image  
(c) Filter radial cross sections for various values

# Lecture 4: Morphological processing

- Basic Morphological operations (calculate)
  - Hit: If any **ONE** of the '1's in the SE is covered by the image, We say that the SE **hits** the image at the pixel position (the one on which the SE is centered).
  - Fit: If **ALL** of the '1's in the SE are covered by the image, we say that the SE **fits** the image at the pixel position (the one on which the SE is centered).
  - **Dilation**
  - **Erosion**
  - **Opening**: Erosion followed by Dilation
  - **Closing**: Dilation followed by Erosion

# Lecture 4: Morphological processing

- Applying **Fit** to an entire image is denoted Erosion
- Interpretation: shift B by z, if it is completely inside A, output a 1
- Applying **Hit** to an entire image is denoted Dilation
- Interpretation: **reflect B**, shift by z, if it overlaps with A, output a 1 at the center of B



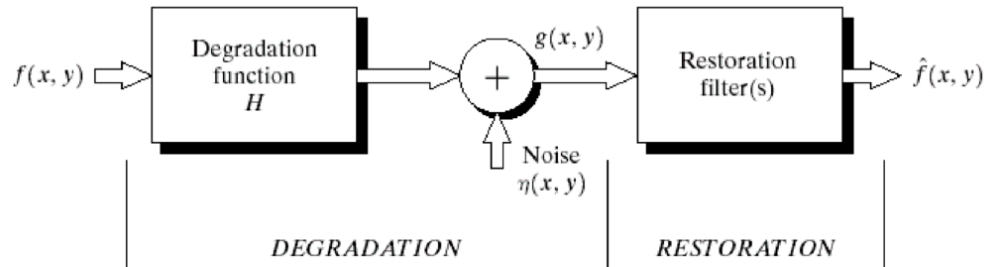
# Lecture 4: Morphological processing

- Morphological Algorithms (understand and can calculate with formula)
  - Hit or Miss Transform
  - Boundary Extraction
  - Hole Filling
  - Connected Components
  - Skeletons



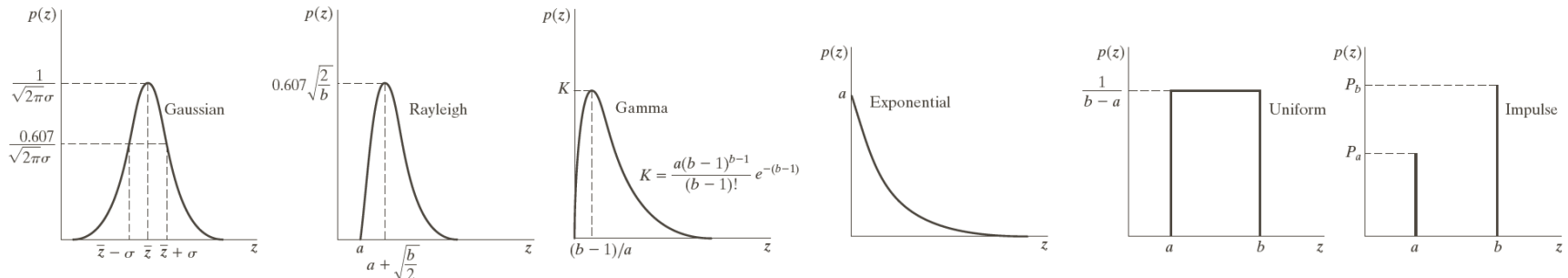
# Lecture 5: Image restoration

- Degradation & Restoration Process Models (Principle)
  - Consists of 2 parts – Degradation function & Noise function



$$G(u, v) = H(u, v)F(u, v) + N(u, v)$$

- Noise Models (6 types)



# Lecture 5: Image restoration

- Restoration in the presence of noise only (spatial filtering)
  - **Mean filters:** Arithmetic mean, Geometric Mean, Harmonic Mean Filter, Contraharmonic Mean
  - **Order-statistics filters:** min, max, median, midpoint, alpha-trimmed mean
  - **Adaptive mean filters:** preserve edge
- Estimation of the degeneration function
  - Observation
  - Experimentation
  - Modeling (motion blur, atmospheric blur)
- **Inverse filtering** (challenges and solutions)  $G(u, v) = H(u, v)F(u, v) + N(u, v)$ 
  - **Question:** If any points in  $H(u, v)$  are zero –division by zero
  - **Solution:** Do not take zero-points of  $H(u, v)$  into account  $\hat{F}(u, v) = \frac{G(u, v)}{H(u, v)} = \frac{H(u, v)F(u, v)}{H(u, v)} + \frac{N(u, v)}{H(u, v)} = F(u, v) + \frac{N(u, v)}{H(u, v)}$
  - **Problem:** If  $H(u, v)$  becomes very small, the second term becomes very large, and it overshadows the  $F(u, v)$ .
  - **Solution:** Limit the restoration to a specific radius about the origin in the spectrum – the restoration cutoff frequency

# Example

- Given the Contraharmonic Mean Filter and the image patch, please calculate the filter results in the center

$$\hat{f}(x, y) = \frac{\sum_{(s,t) \in S_{xy}} g(s, t)^{Q+1}}{\sum_{(s,t) \in S_{xy}} g(s, t)^Q}$$

1	200	200
200	200	200
200	200	200

(a)

1	1	1
1	1	200
1	1	1

(b)

- (1) if Q=-1 for image patch a and b
- (2) if Q=1 for image patch a and b

If Q is negative with -1

1	1	1
1	1	1
1	1	200

➔

1	1	1
1	1.124	1
1	1	200

If Q is positive with 1

1	200	200
200	200	200
200	200	200

➔

1	200	200
200	199.87	200
200	200	200

# Lecture 7: Segmentation – Categories

- Edge-based Segmentation
  - Finding boundary between adjacent regions
- Threshold-based Segmentation
  - Finding regions by grouping pixels of similar gray values
- Region-based Segmentation
  - Finding regions directly using growing or splitting
- Motion-based Segmentation
  - Finding regions by comparing successive frames of a video sequence to identify regions that correspond to moving objects

# Lecture 7: Edge-based Segmentation

- Finding discontinuities (sharp, local changes in intensity) as boundary of regions
- Discontinuities in digital images (**Spatial filters**)
  - Point (**Laplacian**)
  - Line (**horizontal, -45 degree, vertical, 45 degree**)
  - Edges (**Roberts, Prewitt, Sobel, LOG, Canny**)
- Techniques
  - Point detection
  - Edge (pixel) detection
  - Edge formation from edge pixels – **Edge linking, Hough Transform**

# Lecture 7: Edge-based Segmentation

- Finding discontinuities (sharp, local changes in intensity) as boundary of regions

- Discontinuities in digital images (**Spatial filters**)

- Point (**Laplacian**)
  - Line (**horizontal, -45 degree, vertical, 45 degree**)
  - Edges (**Roberts, Prewitt, Sobel, LOG, Canny**)

-1	-1	-1
2	2	2
-1	-1	-1

- Techniques

-1	0
0	1

-1	-1	-1
0	0	0
1	1	1

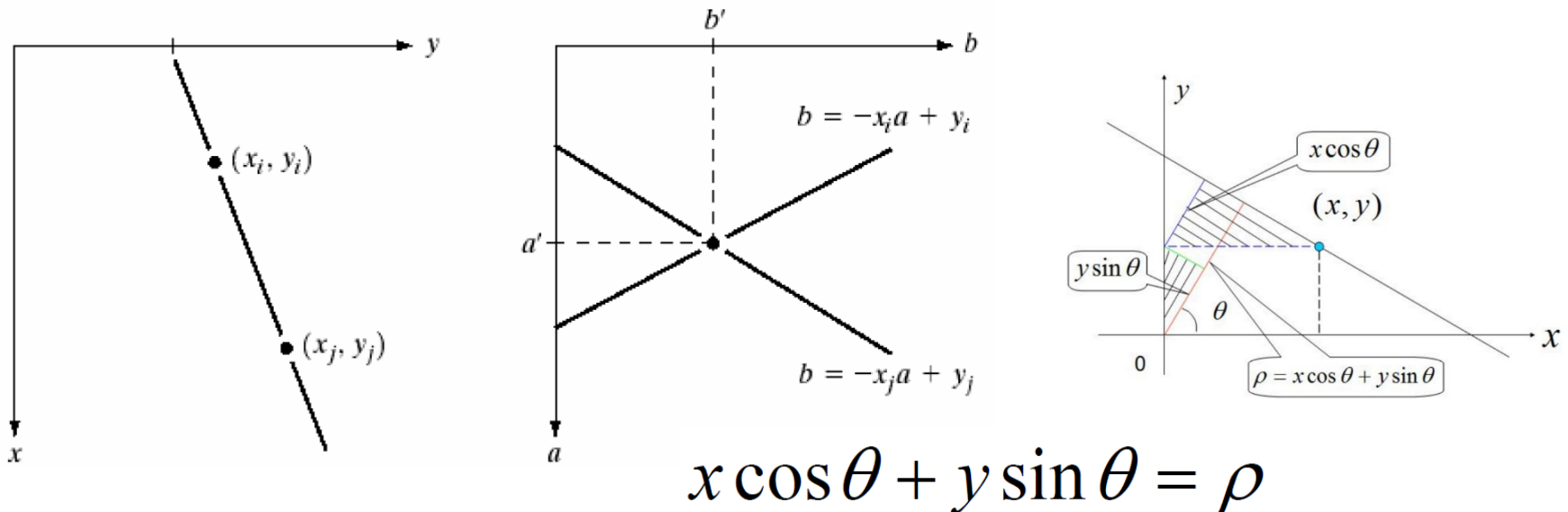
-1	-2	-1
0	0	0
1	2	1

Non-maximal suppression  
Double threshold

- Point detection
  - Edge (pixel) detection
  - Edge formation from edge pixels – **Edge linking, Hough Transform**

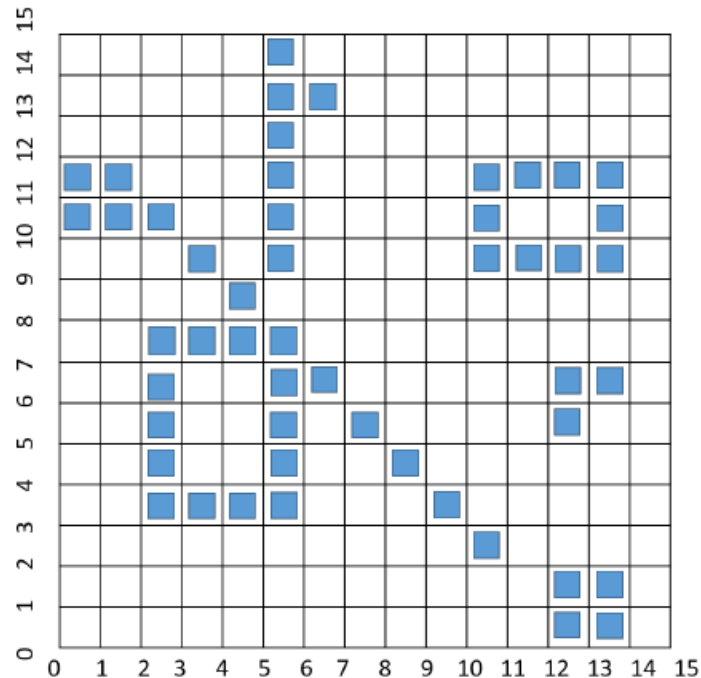
# Hough transform

- Motivation: isolated points
- Problem with this method:  $a$  approaches infinity as the line gets perpendicular to the  $x$  axis. (if a line is perpendicular to  $x$  axis, then this line is represented  $x=M$ .  $a \rightarrow \infty$ )  $y_i = ax_i + b$
- Solution: use the representation of the line as:



# Example

- If we apply the Hough transform on the image below, what would be the maximum values for the accumulator cell in the  $(\rho, \theta)$  space? What are the corresponding  $(\rho, \theta)$  values.



Solution:

The maximum value is 11. There are two lines correspond to this values, with  $\rho = 12/\sqrt{2}$ ,  $\theta = \pi/4$  or  $\rho = 5$ ,  $\theta = 0$ .



# Lecture 8: Image segmentation

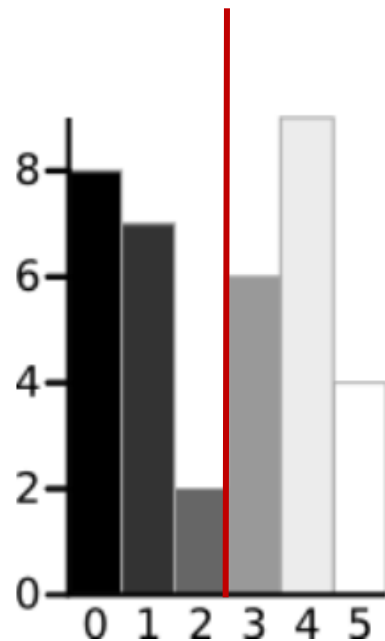
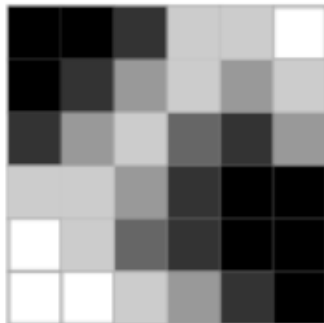
- Threshold based segmentation
  - Basic Global Thresholding
  - Optimum Global Thresholding (OSTU)
  - Multiple Thresholding
  - Variable Thresholding
- Region based segmentation
  - Region grow
  - K-means methods
- Understand principle of these segmentation methods and able to calculate the steps in the segmentation.

# Algorithm: Basic Global Thresholding

- Select an initial estimate for the global threshold,  $T$
- Threshold the image using  $T$ . This will produce two groups of pixels:  $G_1$  consisting of all pixels with intensity values  $> T$ , and  $G_2$  consisting of pixels with values  $\leq T$ .
- Compute the average (mean) intensity values  $m_1$  and  $m_2$  for the pixels in  $G_1$  and  $G_2$ , respectively.
- Compute a new threshold value:  $T = \frac{1}{2}(m_1 + m_2)$
- Repeat Steps 2 through 4 until the difference between values of  $T$  in successive iterations is smaller than a predefined parameter  $\Delta T$ .

# Otsu's Method

- View thresholding as a statistical-decision theory problem
- **Objective:** Maximizes the between-class variance (minimize the within-class variance)



Within-Class Variance

$$\sigma_W^2 = W_b \sigma_b^2 + W_f \sigma_f^2 = 0.4722 * 0.4637 + 0.5278 * 0.5152 = 0.4909$$

When the threshold is 3, the calculation of background

$$\text{Weight } W_b = \frac{8 + 7 + 2}{36} = 0.4722$$

$$\text{Mean } \mu_b = \frac{(0 \times 8) + (1 \times 7) + (2 \times 2)}{17} = 0.6471$$

$$\begin{aligned} \text{Variance } \sigma_b^2 &= \frac{((0 - 0.6471)^2 \times 8) + ((1 - 0.6471)^2 \times 7) + ((2 - 0.6471)^2 \times 2)}{17} \\ &= \frac{(0.4187 \times 8) + (0.1246 \times 7) + (1.8304 \times 2)}{17} \\ &= 0.4637 \end{aligned}$$

When the threshold is 3, the calculation of foreground

$$\text{Weight } W_f = \frac{6 + 9 + 4}{36} = 0.5278$$

$$\text{Mean } \mu_f = \frac{(3 \times 6) + (4 \times 9) + (5 \times 4)}{19} = 3.8947$$

$$\begin{aligned} \text{Variance } \sigma_f^2 &= \frac{((3 - 3.8947)^2 \times 6) + ((4 - 3.8947)^2 \times 9) + ((5 - 3.8947)^2 \times 4)}{19} \\ &= \frac{(4.8033 \times 6) + (0.0997 \times 9) + (4.8864 \times 4)}{19} \\ &= 0.5152 \end{aligned}$$

# K-means

- Partition the data points into K clusters randomly. Find the centroids of each cluster.
- For each data point:
  - Calculate the distance from the data point to each cluster.
  - Assign the data point to the closest cluster.
- Recompute the centroid of each cluster.
- Repeat steps 2 and 3 until there is no further change in the assignment of data points (or in the centroids).

$$\sum_{i \in \text{clusters}} \left\{ \sum_{j \in \text{elements of } i\text{'th cluster}} \|x_j - \mu_i\|^2 \right\}$$

# K-means

- The input dataset is shown below, we first select (3,3) and (2,2) as cluster centers.
- Please calculate the process for the K-means method

No	X	Y
1	1	1
2	2	3
3	1	2
4	3	3
5	2	2
6	3	1

$$\begin{aligned}
 1. \ D1 &= \{(1, 1), (2, 2)\} \\
 &= \sqrt{(2-1)^2 + (2-1)^2} \\
 &= 1.41
 \end{aligned}$$

$$\begin{aligned}
 2. \ D1 &= \{(2, 3), (2, 2)\} \\
 &= \sqrt{(2-2)^2 + (2-3)^2} \\
 &= 1
 \end{aligned}$$

$$\begin{aligned}
 3. \ D1 &= \{(1, 2), (2, 2)\} \\
 &= \sqrt{(2-1)^2 + (2-2)^2}
 \end{aligned}$$

$$\begin{aligned}
 1. \ D2 &= \{(1, 1), (3, 3)\} \\
 &= \sqrt{(3-1)^2 + (3-1)^2} \\
 &= 2.82
 \end{aligned}$$

$$\begin{aligned}
 2. \ D2 &= \{(2, 3), (3, 3)\} \\
 &= \sqrt{(3-2)^2 + (3-3)^2} \\
 &= 1
 \end{aligned}$$

$$\begin{aligned}
 3. \ D2 &= \{(1, 2), (3, 3)\} \\
 &= \sqrt{(3-1)^2 + (3-2)^2}
 \end{aligned}$$

# K-means

- The input dataset is shown below, we first select (3,3) and (2,2) as cluster centers.
- Please calculate the process for the K-means method

No	X	Y
1	1	1
2	2	3
3	1	2
4	3	3
5	2	2
6	3	1

$$\begin{aligned}
 4. \text{ D1} &= \{(3, 3), (2, 2)\} \\
 &= \sqrt{(2-3)^2 + (2-3)^2} \\
 &= 1.41
 \end{aligned}$$

$$\begin{aligned}
 5. \text{ D1} &= \{(2, 2), (2, 2)\} \\
 &= \sqrt{(2-2)^2 + (2-2)^2} \\
 &= 0
 \end{aligned}$$

$$\begin{aligned}
 6. \text{ D1} &= \{(3, 1), (2, 2)\} \\
 &= \sqrt{(2-3)^2 + (2-1)^2} \\
 &= 1.41
 \end{aligned}$$

$$\begin{aligned}
 4. \text{ D2} &= \{(3, 3), (3, 3)\} \\
 &= \sqrt{(3-3)^2 + (3-3)^2} \\
 &= 0
 \end{aligned}$$

$$\begin{aligned}
 5. \text{ D2} &= \{(2, 2), (3, 3)\} \\
 &= \sqrt{(3-2)^2 + (3-2)^2} \\
 &= 1.41
 \end{aligned}$$

$$\begin{aligned}
 6. \text{ D2} &= \{(3, 1), (3, 3)\} \\
 &= \sqrt{(3-3)^2 + (3-1)^2} \\
 &= 2
 \end{aligned}$$

# K-means

No	X	Y
1	1	1
2	2	3
3	1	2
4	3	3
5	2	2
6	3	1

$$C1 = \{(1, 1), (1, 2), (2, 2), (3, 1)\}$$

$$C2 = \{(2, 3), (3, 3)\}$$

$$\text{Mean} = \left( \frac{x_1 + x_2 + \dots + x_n}{n}, \frac{y_1 + y_2 + \dots + y_n}{n} \right)$$

$$C1 = \left( \frac{1+1+2+3}{4}, \frac{1+2+2+1}{4} \right)$$

$$\text{New } C1 = (1.75, 1.5)$$

$$C2 = \left( \frac{2+3}{2}, \frac{3+3}{2} \right)$$

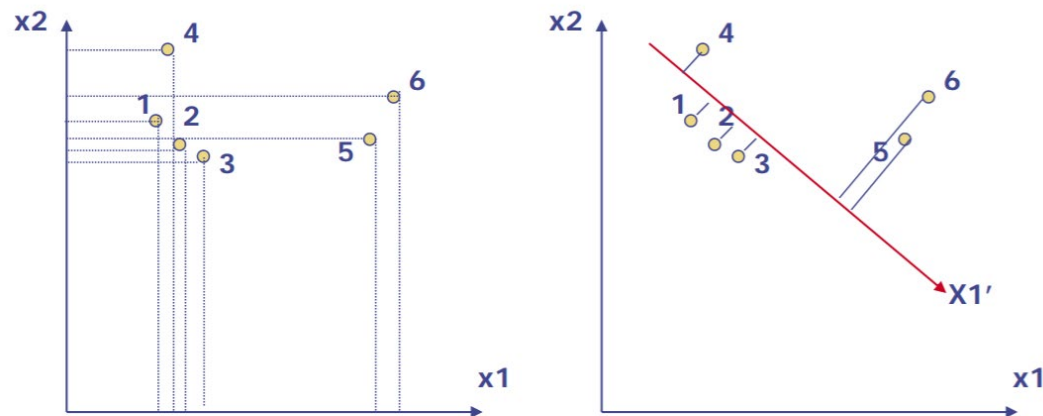
$$\text{New } C2 = (2.5, 3)$$

- Repeat until no points move

# Lecture 9: PCA and LDA for face recognition

- Introduction to face recognition
- **Principal Component Analysis (PCA)**
  - converts a set of observations of possibly **correlated variables** into a set of values of linearly **uncorrelated variables** called principal components
  - **Purpose:** Identify the orientation with largest variance

$$\alpha_1 = \arg \max_{\alpha} \left( \text{var}(\alpha^T \mathbf{X}) \right), \alpha \in \mathbb{R}^{p \times 1}$$



PCA projection



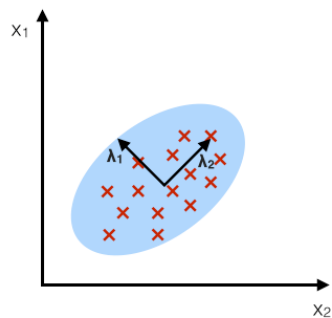
# Linear Discriminant Analysis (LDA)

- Eigenfaces **exploit the max scatter of the training images** in face space
  - PCA
- Fisherfaces attempt to **maximize the between class scatter, while minimizing the within class scatter.**
  - Goal: find the best separation between two classes

$$J(w) = \frac{w^T S_B w}{w^T S_W w}$$

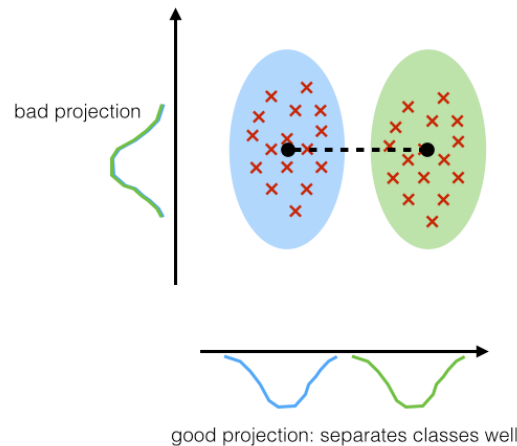
## PCA:

component axes that maximize the variance



## LDA:

maximizing the component axes for class-separation



# PCA Example

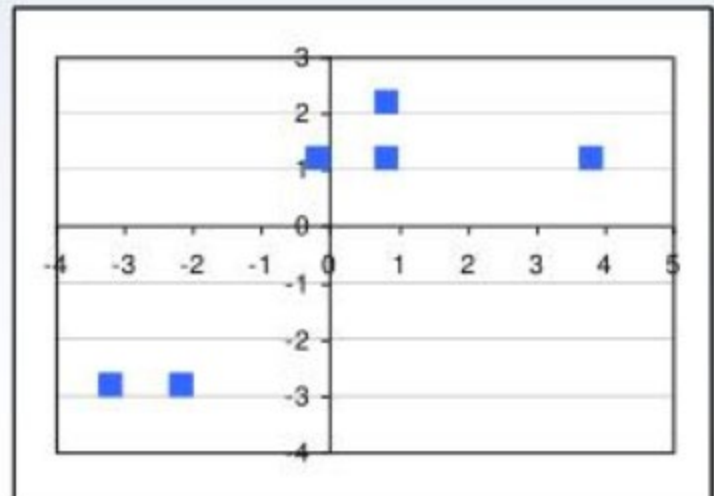
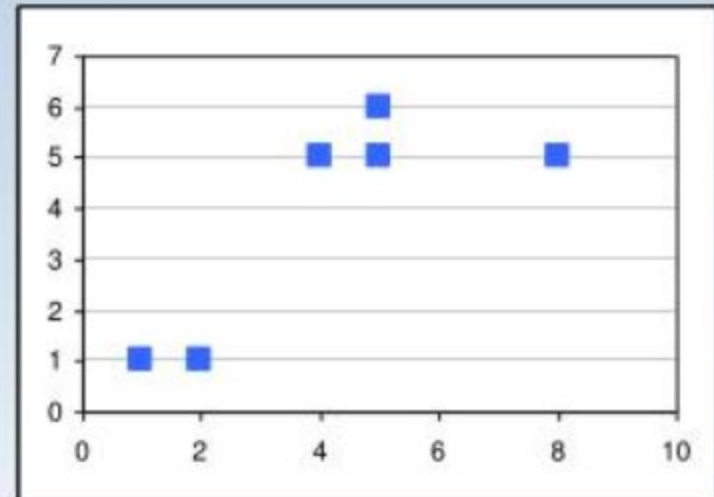
## 1) Calculate Principal Component

### Step 1.1: Get some Data

### Step 1.2: Subtract the mean

$$\bar{x} = 4.17 \quad \bar{y} = 3.83$$

Point	X	Y	$X - \bar{X}$	$Y - \bar{Y}$
A	1	1	-3.17	-2.83
B	2	1	-2.17	-2.83
C	4	5	-0.17	1.17
D	5	5	0.83	1.17
E	5	6	0.83	2.17
F	8	5	3.83	1.17



# PCA Example

## Step 1.3: Covariance matrix calculation

$$C = \begin{pmatrix} 5.139 & 3.694 \\ 3.694 & 4.139 \end{pmatrix} \quad \begin{array}{l} \text{Positive cov}_{ij} \text{ values} \\ \rightarrow x \text{ and } y \text{ values increase together in dataset} \end{array}$$

## Step 1.4: Eigenvectors and eigenvalues calculation –Principal axis

a) Calculate eigenvalues  $\lambda$  of matrix C

$$C - \lambda \cdot E = \begin{pmatrix} 5.139 - \lambda & 3.694 \\ 3.694 & 4.139 - \lambda \end{pmatrix} \quad \text{Where E is identity matrix}$$

The characteristic polynomial is the determinant. The roots of the function, that appears if you set the polynomial equals zero, are the eigenvalues

$$\begin{aligned} \det(C - \lambda \cdot E) &= (5.139 - \lambda)(4.139 - \lambda) - (3.694)^2 \\ &= \lambda^2 - 9.278\lambda + 7.620 \end{aligned} \quad \Rightarrow \quad \begin{array}{l} \lambda_1 = 8.367 \\ \lambda_2 = 0.911 \end{array}$$

# PCA Example

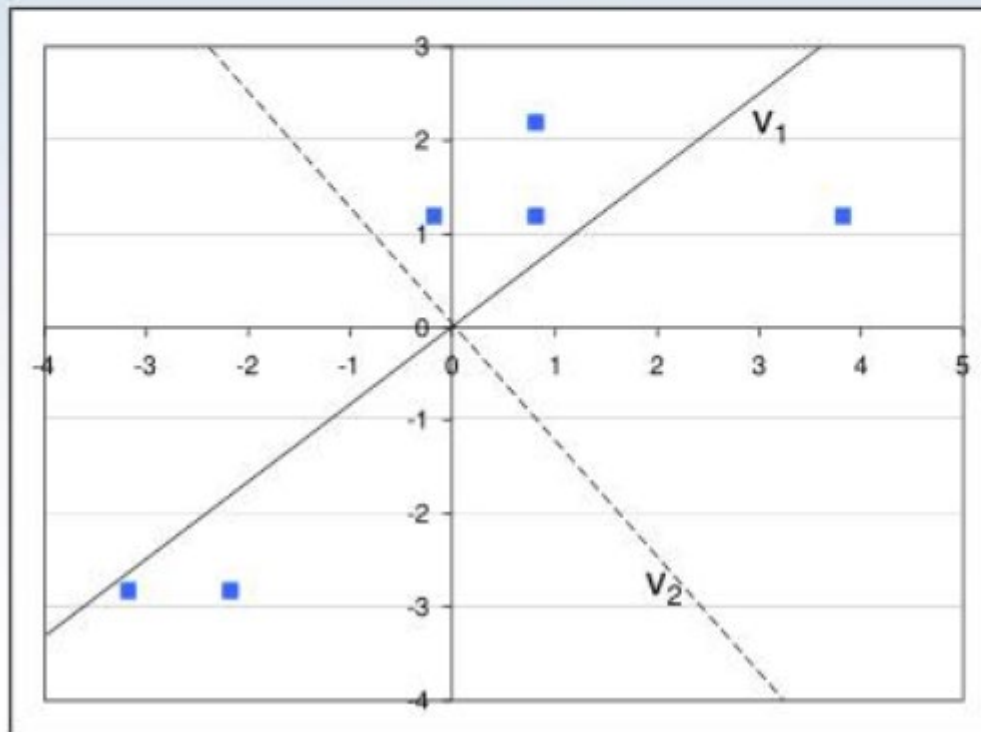
b) Calculate eigenvectors  $v_1$  and  $v_2$  out of eigenvalues  $\lambda_1$  and  $\lambda_2$  via properties of eigenvectors (see matrix algebra background(3/3))

$$\begin{pmatrix} 5.139 & 3.694 \\ 3.694 & 4.139 \end{pmatrix} \begin{pmatrix} x_1 \\ y_1 \end{pmatrix} = 8.367 \begin{pmatrix} x_1 \\ y_1 \end{pmatrix}$$

$$\Rightarrow v_1 = \begin{pmatrix} x_1 \\ y_1 \end{pmatrix} = \begin{pmatrix} -0.753 \\ -0.658 \end{pmatrix}$$

$$\begin{pmatrix} 5.139 & 3.694 \\ 3.694 & 4.139 \end{pmatrix} \begin{pmatrix} x_2 \\ y_2 \end{pmatrix} = 0.911 \begin{pmatrix} x_2 \\ y_2 \end{pmatrix}$$

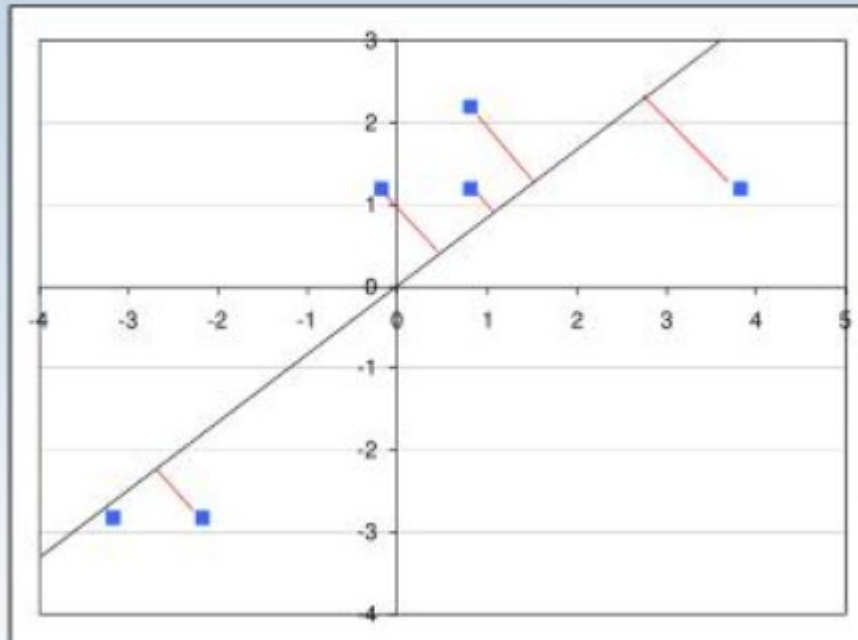
$$\Rightarrow v_2 = \begin{pmatrix} x_2 \\ y_2 \end{pmatrix} = \begin{pmatrix} 0.658 \\ -0.753 \end{pmatrix}$$



Eigenvector  $v_1$  with highest eigenvalue fits the best. This is our principal component

# PCA Example

## 2) Select the dividing point along the principal axis



**Step 2.1: Calculate projections on principal axis**

# LDA Example

- For the given data below, please calculate the Within-class scatter matrix and Between-class scatter matrix.

- $X1=\{(3,2),(2,3),(2,4),(5,3)\}$

- $X2=\{(9,8),(8,9),(8,7),(7,8)\}$

- The LDA projection is then obtained as the solution of the generalized eigen value problem

$$S_W^{-1}S_B w = \lambda w$$

$$\Rightarrow |S_W^{-1}S_B - \lambda I| = 0$$

$$X1 = [3, 2; 2, 3; 2, 4; 5, 3];$$

$$X2 = [9, 8; 8, 9; 8, 7; 7, 8];$$

$$\text{Mu1} = \text{mean}(X1);$$

$$\text{Mu2} = \text{mean}(X2);$$

$$S1 = \text{cov}(X1);$$

$$S2 = \text{cov}(X2);$$

$$S_W = S1 + S2;$$

$$S_B = (\text{Mu1} - \text{Mu2}) * (\text{Mu1} - \text{Mu2})';$$

- Calculate eigenvalue and eigenvectors, where the eigenvector represent the project direction

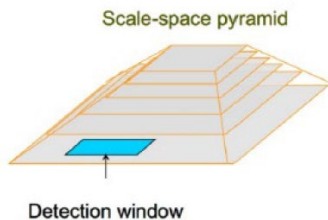
# Lecture 10: face recognition

- Section A
  - Introduction of deep learning
  - DeepFace
  - FaceNet
- Section B: Deep learning in image segmentation
  - **Models:** Fully Convolutional Network, DeconvNet, SegNet, U-Net, PSPNet, DeepLab v1, v2, v3, v3+, transformer
  - Loss functions: **Cross entropy (CE)**, Weighted cross entropy, Balanced cross entropy (BCE), Focal loss, Dice loss, Tversky loss
  - Able to choose suitable loss functions



# Lecture 11: Detection

- HOG
- DPM(Deformable Part Model):capture spatial relationships



locations

scales

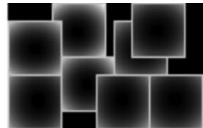
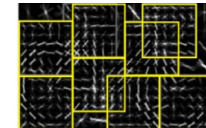
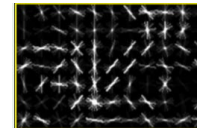
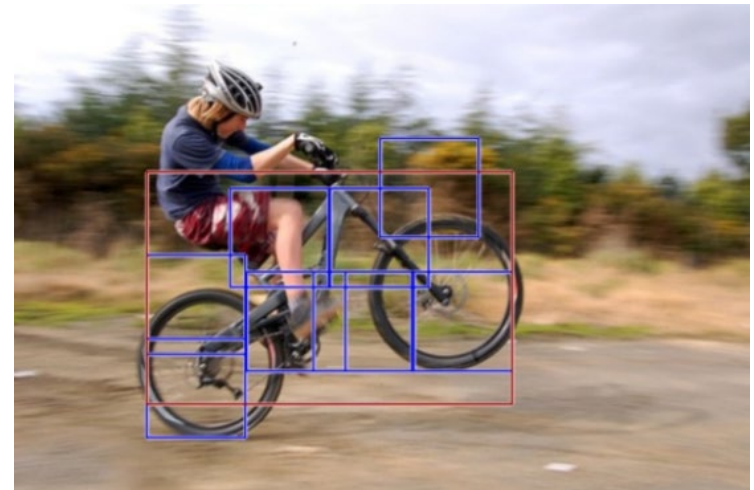
**Scan image(s) at all scales and locations**

**Extract features over windows**

**Run window classifier at all locations**

**Fuse multiple detections in 3-D position & scale space**

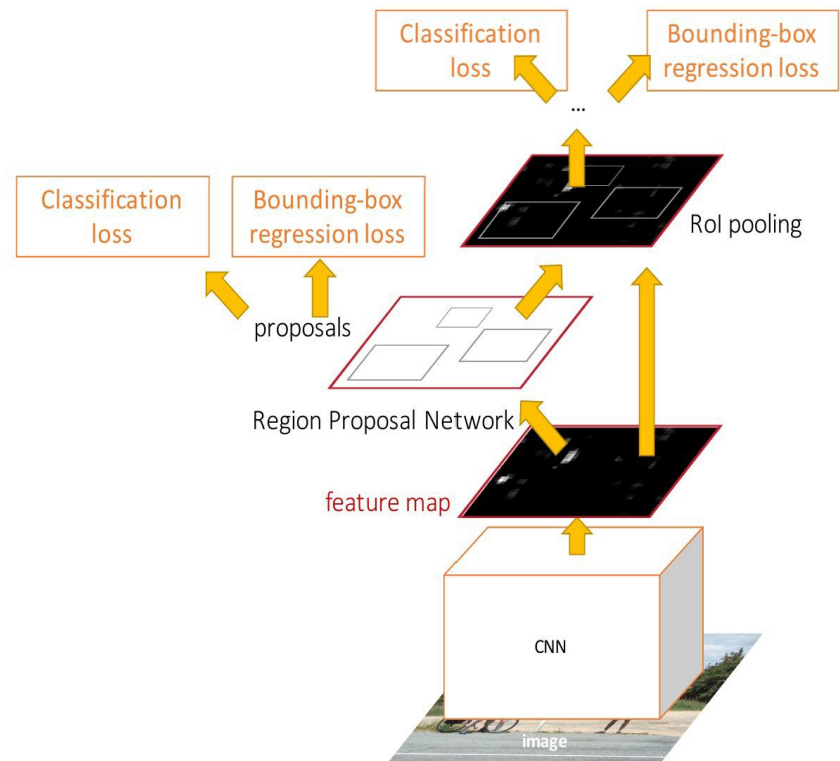
Object detections with bounding boxes





# Lecture 11: Detection

- Section B
  - RCNN (Selective Search)
  - Fast-RCNN (region of interest)
  - Faster-RCNN (region proposal network)
  - Mask-RCNN (segmentation)



# Report writing

- Suggestion: latex(overleaf) or word.
- Template: use online paper template.
  - <https://www.overleaf.com/latex/templates/cvpr-2022-author-kit/qbmjsdxryffn>
  - <https://cvpr2022.thecvf.com/author-guidelines> (search for 'word')
- Just for a case study: Squeeze-and-Attention Networks for Semantic Segmentation
  - include abstract, introduction, related work (not necessary in our report), method, results.
- 4-8 pages are good enough for your project



## The Last Message For You

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天高任鸟飞, 海阔凭鱼跃

The sky is unlimited for birds to fly at ease,  
as the ocean is boundless for fish to leap at  
will.

-- 阮阅 《诗话总龟前集》