

Q1: Given 8 jobs with the following (v, s, f)-values (v=value, s= start time, and f= finish times): a=(3.5,0,6), b=(2,1,4), c=(3,3,5), d=(3,3,8), e=(6.5,4,7), f=(2.5,5,9), g=(12,6,10), h=(8,8,11).

Find a set of mutually compatible jobs with the maximal total value.

Sort by finish time: b=(2, 1, 4), c=(3, 3, 5), a=(3.5, 0, 6), e=(6.5, 4, 7), d=(3, 3, 8), f=(2.5, 5, 9), g=(12, 6, 10), h=(8, 8, 11)

Compute p array: p[b]=0, p[c]=0, p[a]=0, p[e]=b, p[d]=0, p[f]=c, p[g]=a, p[h]=d

State transition equation: $M[j] = \max \{ v_j + M[p[j]], M[j-1] \}$

$M[b] = \max \{ v_b + M[0], M[0] \} = \max \{ 2 + 0, 0 \} = 2$

$M[c] = \max \{ v_c + M[0], M[b] \} = \max \{ 3 + 0, 2 \} = 3$

$M[a] = \max \{ v_a + M[0], M[c] \} = \max \{ 3.5 + 0, 3 \} = 3.5$

$M[e] = \max \{ v_e + M[b], M[a] \} = \max \{ 6.5 + 2, 3.5 \} = 8.5$

$M[d] = \max \{ v_d + M[0], M[e] \} = \max \{ 3 + 0, 8.5 \} = 8.5$

$M[f] = \max \{ v_f + M[c], M[d] \} = \max \{ 2.5 + 3, 8.5 \} = 8.5$

$M[g] = \max \{ v_g + M[a], M[f] \} = \max \{ 12 + 3.5, 8.5 \} = 15.5$

$M[h] = \max \{ v_h + M[d], M[g] \} = \max \{ 8 + 8.5, 15.5 \} = 16.5$

Thus, select jobs {h, e, b} with the maximal total value 16.5.