

## **Tut 8**

### **Qn 1**

A texture pattern whose extent is given by

$$0 \leq s \leq 1 \quad 0 \leq t \leq 1$$

is to be mapped to a cylinder with axis

$$X = 3 \quad Y = 5$$

and radius 3. The top and bottom of the cylinder is given by  $Z = \pm 4$ . Suppose the mapping is such that  $s$  maps to  $\theta$  and  $t$  maps to  $z$ , such that

$$s = 0 \text{ maps to } \theta = 0 \quad s = 1 \text{ maps to } \theta = 2\pi$$

$$t = 0 \text{ maps to } Z = -4 \quad t = 1 \text{ maps to } Z = +4$$

Further assume that the mapping is linear.

- Calculate the texture-to-surface transformation, i.e. the transformation from  $(s, t)$  to  $(\theta, z)$ .
- Suppose the cylinder is rotated about  $y$  by  $+30^\circ$  and then parallel project with a projection vector of  $(1, 1, -2)$  to the  $(x, y)$  image plane. Calculate the MODELVIEW transformation matrix and projection transformation matrix.
- Hence give an expression for image space to texture space transformation i.e., the transformation from  $(x, y)$  to  $(s, t)$ .
- What is the advantage of pixel order scanning compared with texture scanning?
- The method in c) is complicated because it involves inverse transformation and thus it is impractical. Suggest a simpler method to implement pixel order scanning.

### **Qn 2**

The parametric equation of a ball is

$$X = 5(\cos\alpha)(\cos\beta) + 10$$

$$Y = 5(\sin\alpha)(\cos\beta) + 50$$

$$Z = 5(\sin\beta)$$

A logo is mapped to the surface of the ball such that

$(s, t) = (0, 0)$  maps to  $(\alpha, \beta) = (0, 0)$

$(s, t) = (1, 0)$  maps to  $(\alpha, \beta) = (\pi/2, 0)$

$(s, t) = (1, 1)$  maps to  $(\alpha, \beta) = (\pi/4, \pi/4)$

Derive the texture  $(s, t) \rightarrow$  surface  $(\alpha, \beta)$  transformation.

### **OpenGL Mini-project Progress**

Now you should program texture into your scene. Start with a flat plane, which is the simplest. Then proceed to more exotic objects if you have time.