MA1200 TAKE HOME PROBLEM SET 2

The following is the second take-home assignment of MA1200, which counts 3 points of total 100 of your final score of the course.

Please submit it via canvas in a pdf file (you can handwrite the answers and take photos by your phone, then make it into a pdf file, see for example, https://www.wikihow.com/Convert-JPG-to-PDF) for how to combine jpg files to a pdf; you can also do it by note-taking apps on an iPad or an Surface)

- Q1. $f(x) = 3x^2 + 18x + 8$, find the range, and sketch the grapph.
- Q2. Factorize $3x^3 + 4x^2 17x 6$ into product of three linear factors (hint, try x = 2)
- Q3. Express $\frac{x^2 + 11x + 20}{(x-1)(x+3)^2}$ into partial fractions.
- Q4. Rewrite $3\cos(x) 4\sin(x)$ as $r\cos(x + \alpha)$, where r > 0 and $\alpha \in (0, \pi/2)$. (hint, $\cos(a + b) = \cos(a)\cos(b) \sin(a)\sin(b)$)
 - Q5. Solve $3\cos(x) 4\sin(x) = 5/2$
 - Q6. Solve $\sin(3\theta) = \cos(2\theta)$

The assignment is due on 23:59 of Oct 23, Friday.

You will lose 1 point for each day of late submission. All submissions after the midnight of Oct 26 will be marked as 0.

Date: October 14, 2020.

1

MA ROO. HWZ. 0.5 point each. Q1 fix1 = 3 x2+18x+8 = 3(x2+6x+9)+8-27 = $3(X+3)^2-19$. Tange $[-19, \infty)$ Q2. - f(x) = 3x3+4x2-17x-6. $f(2) = 0 \Rightarrow 3x^{3} + 6x^{2} - 17 - 6 = (x-2)(3x^{2} + 10x + 3)$ = (x+2)(x+3)(3x+1) Q3. x2+11x+20 A B C (X+3)2 = A + B C (X+3)2 X2+11 x +20 = A(x+3) + B(x-1)(x+3) + C(x-1) X =1 => (+11+20 = 16A =) A=2 $X = -3 \Rightarrow 9 - 33 + 20 = -40 \Rightarrow 0 = 1$ € 20 = 9A - 3B - C = 18-1-3B X=0 X-1