EE2331 Data Structures and Algorithms

Linked Lists

Linear List

- Each element in the list has a unique predecessor (previous) and successor (next).
- Unordered/Random list
 - There is no ordering of the data.
- Ordered list
 - The data are arranged according to a key. A key is one or more fields within a structure that is used to identify the data or otherwise control its use.
- General list
 - Data can be inserted and deleted anywhere and there are no restrictions on the operations that can be used to process the list.
- Restricted list
 - Insertion, deletion and processing of data are restricted to specific locations, e.g. the two ends of the list. Stack and Queue are examples of restricted list.

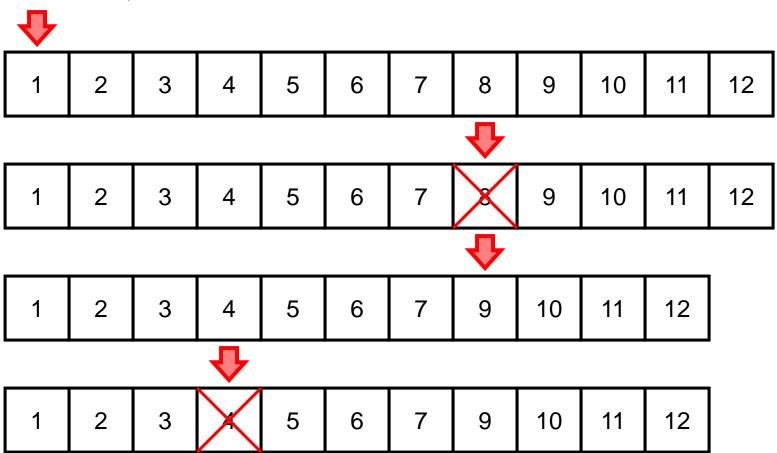
Josephus Problem



- People are standing in a circle waiting to be executed. Counting begins at a specified point in the circle and proceeds around the circle in a specified direction. After a specified number of people are skipped, the next person is **executed**. The procedure is repeated with the remaining people, starting with the next person, going in the same direction and skipping the same number of people, until only one person remains, and is **freed**.
- The problem given the number of people (*n*), starting point, direction, and number to be skipped (*k*) is to choose the position in the initial circle to avoid execution (i.e. guessing who is the survivor).

The Josephus Problem

■ If k = 7, n = 12



Array Implementation

- A simple approach is by writing a program to simulate the counting-out game. But what data structure should be use?
- With a list using array implementation
 - Array has the advantage of random access (i.e. direct access to any position)
 - However, the insert and delete operation may involve substantial data movement
 - Another disadvantage of representing a list using an array is that the maximum length of the list needs to be determined a priori

Linked List & Node Structure

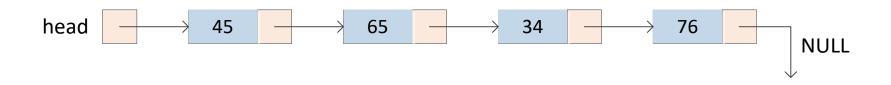
A sequence of nodes (elements), each containing arbitrary data and links (pointers) pointing to the next and/or previous nodes

```
data link
```

- It contains pointer(s) of the same type
 - Recursive data structure (self-referential datatype)
- A list is formed by linking nodes together in a sequential manner
- In typical C++ implementations, we shall define the node using struct, and the linked list is defined as a class.

Linked List Example

- In the C++ terminology, a linked list is classified as a container. In Java, it is called a collection.
- The address of the first node in the list is stored in a separate pointer variable usually called head, first, or list.
- The null pointer (NULL, physical value 0 in C/C++) is used to denote the end of the list, or not a valid address.
- Example: a linked list of 4 integers.



Common Operations on Linked List

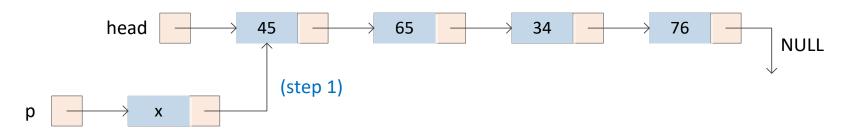
Find Length & Find Node

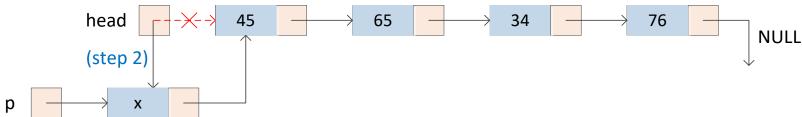
To find the length of the linked list

To search an element x from the beginning of the list

Insert Node (at front)

Insert a new element x at the front of the list

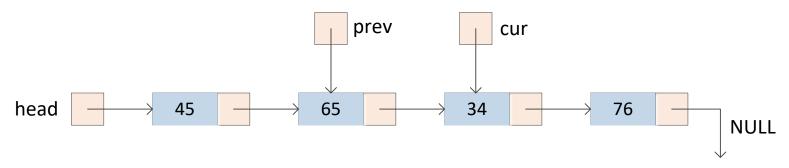




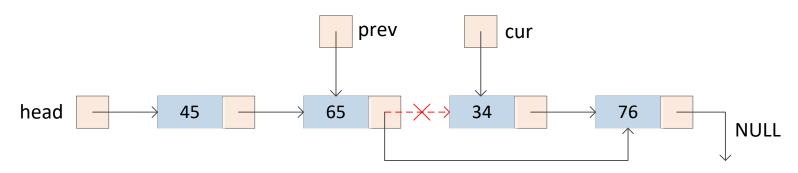
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Remove Node

1. Locate the node storing the value x, e.g. x = 34

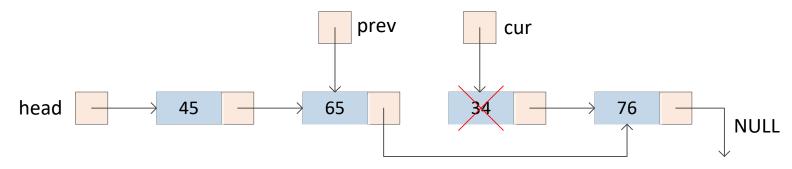


Update the links

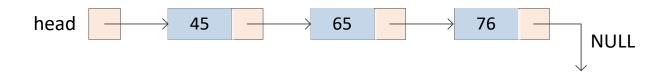


Remove Node (cont.)

3. Physically delete the node



4. Structure of the list after removing the element 34



Remove Node (cont.)

- Remove the element x (1st instance) from the linked list
- To remove a node from the linked list, we need to know the reference to its predecessor.

```
node *cur = head;
node *prev = NULL;  // prev points to the predecessor of cur
while (cur != NULL && cur->info != x) {
                                          // search x
  prev = cur;
  cur = cur->link;
}
// if cur == NULL, x is not found in the linked list
if (cur != NULL) { // \text{cur->info} == x
  if (prev != NULL) // why checking this?
     prev->link = cur->link;  // skip cur node
                      // cur is the first node in the list
  else
     head = cur->link; // x is the first node
             //free the storage of the removed node
  delete cur;
```

Insert Node

Insert a new element x into an ordered list

```
node *p = new node;
p \rightarrow info = x;
if (head == NULL || x <= head->info) {
   p->link = head;  //insert at front
  head = p;
                        //head != NULL && x > head->info
} else {
   node *prev = head;  // x to be inserted between prev and cur
   node *cur = head->link; // i.e. prev->info < x <= cur->info
   while (cur != NULL && x > cur->info) { // search position
      prev = cur;
      cur = cur->link;
   // x not exist OR x <= cur->info, so insert node p after node prev
   p->link = prev->link;
   prev->link = p;
```

Remark

- Because you can't go backward in a singly linked list, for removing/inserting node, you usually need to use a pair of pointers – predecessor and current, to keep track of the previous node and update its link.
- For a linked list of size n, you generally should test your algorithm against the two boundary cases: n=0 and n=1 in addition to the general case.

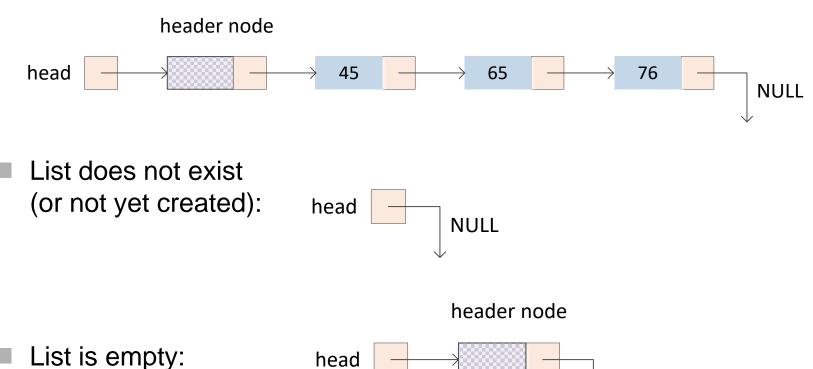
Common Problems

- Null-pointer exception is a common error in programs that manipulate linked list.
- A pointer must be properly initialized or tested for not equal to NULL before you can use it to access a data member (dereferencing) or the next node.
- Broken list due to deletion of nodes
- Losing reference to some nodes (memory leak)

Other Variants of Linked List

Linked List with Header Node

The data field of the header node is NOT used to store valid data.
Some metadata may be stored in the header node.



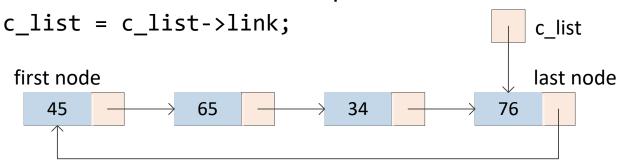
NULL

Why Header Node?

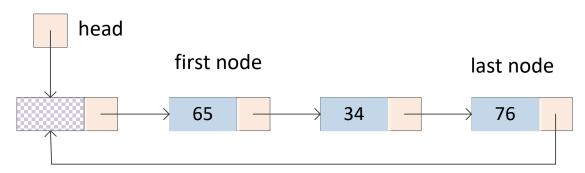
- Header node is guaranteed to exist at all times.
- Header node makes all list nodes intrinsically the same having a predecessor.
- Having a sentinel zeroth node simplifies a lot of operations you might want to perform on a linked list - for example, a lot of operations no longer need to explicitly check for an empty list.

Circularly Linked List

- The link of the last node points back to the first node.
- When the pointer c_list reaches the last node in the list, it can revisit the first node in one step:

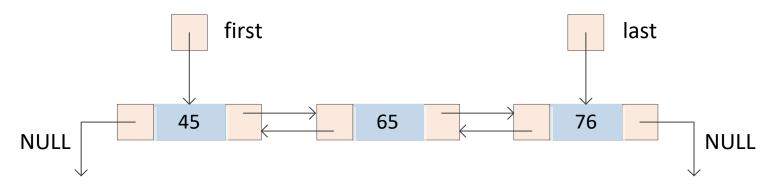


Circular list with header



Doubly Linked List

With a doubly-linked list, we can traverse the list in the forward or backward direction.



Insert Node on Doubly Linked List

Insert element x after the current node in a

doubly-linked list

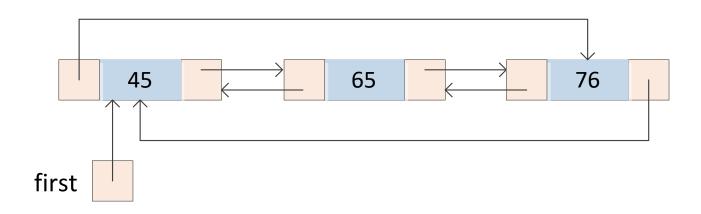
```
nodeType<Type> *p = new nodeType<Type>;
p \rightarrow info = x;
// assume current is a pointer to current node
p->next = current->next; //(1)
p->back = current;
                              //(2)
if (current->next != NULL) //current has a successor
   current->next->back = p; //(3)
                              //(4)
current->next = p;
```

Remove Node on Doubly Linked List

Remove the node pointed by p in a doubly-linked list

Circular Doubly Linked List

Circular doubly-linked list is used in the OS for dynamic memory allocation and de-allocation. The algorithm is called **boundary-tag method**.



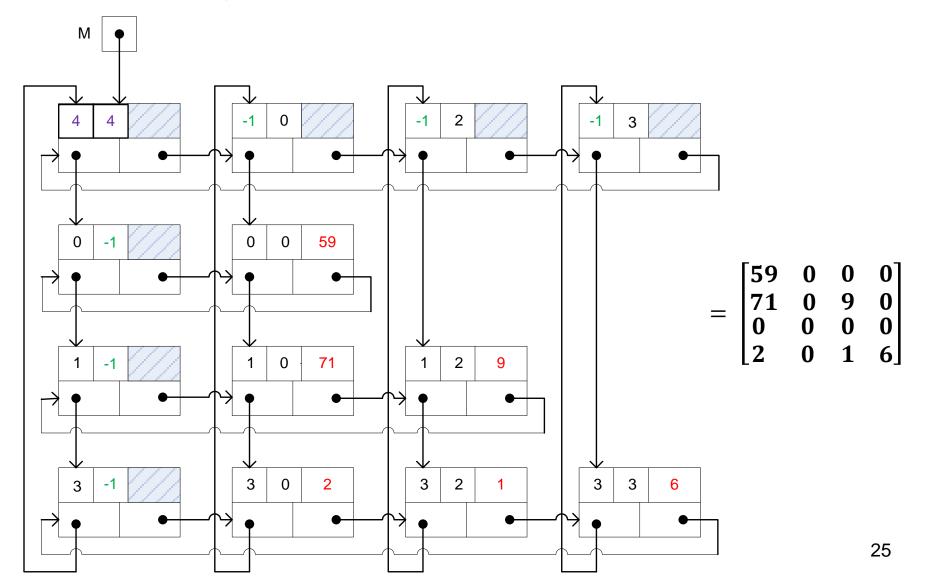
Orthogonal List

- Linked representation of sparse matrix
- Non-zero elements in a row (or column) are connected in a circular linked list with header.

```
struct node {
    int row, col;
    double value;
    node *down, *right;
};
node *M;    //reference pointer to the sparse matrix
```

Example:
$$M = \begin{bmatrix} 59 & 0 & 0 & 0 \\ 71 & 0 & 9 & 0 \\ 0 & 0 & 0 & 0 \\ 2 & 0 & 1 & 6 \end{bmatrix}$$

In this example, values of nRow and nCol of the sparse matrix are stored in the dummy header node pointed at by **M**. The header of each circular list stores the respective row/column number.



Get Value from Matrix

```
//Return the value of matrix[i][j]
//Precondition: i < nRow and j < nCol</pre>
double getValue(node *m, int i, int j) {
   node *p, *q;
   int found;
   // search vertically
   found = 0;
   p = m - down;
   while (p != m && !found) {
      if (p->row < i)
         p = p - > down;
      else if (p->row == i) {
         //found the row
         found = 1;
      } else {
         // row not exist!
         // terminate the loop
         p = m;
```

```
// then search horizontally
//p points to header of row i
if (found) {
   q = p->right;
   while (q != p) {
      if (q->col < j)
         q = q->right;
      else if (q\rightarrow col == j) {
         //value of matrix[i][i]
         return q->value;
      } else {
         // col not exist!
          //terminate the loop
          q = p;
// not exist -> 0
return 0; //matrix[i][j] == 0
```

Class Exercise

- Search last node of a list
- Remove last node of a list
- The given singly linked list has a dummy header
 - Input: a pointer to node structure, list, which points to the head of a linked list
 - Precondition: list is a valid linked list with header

Search the Last Node

```
// Output: a pointer p points to the last node of the list
node* searchLastNode(node *list) {
```

Remove the Last Node

```
// singly linked list with header hode
void removeLastNode(node *list) {
```

Linked List C++ Implementation

- Operations that we would perform on a linked list:
- Initialize the list.
- Clear the list.
- Determine if the list is empty.
- Print the list.
- Find the length of the list.
- Make a copy of the list, e.g. assignment operator= and the copy constructor.
- Search the list for a given item.
- Insert an item to the list.
 - The requirement of the insert operation depends on the representation invariant or the intended uses of the list.
 - For ordered list, we need to maintain the ordering of list elements.
 - If it is used as a queue, insertion is performed at the rear (end of list).
 - If it is used as a stack, insertion is performed at the front.

Linked List C++ Implementation

- Remove an item from the list. Similar to the case of insertion.
- Traverse the list (in the application program that uses the linked list object), i.e. retrieve the elements one by one (in some specific order) to carry out the required computation on each node.
 - To implement the traversal, we shall make use of an iterator.
 - A linked list is a container that holds together a collection of items.
 - An iterator is an object that produces each element of a container, one at a time.
 - The two basic operations on an iterator are the dereference operator *, and the pre-increment operator ++ (advance to the next element).
- There can be other operations on the linked list, e.g. reverse the list, merge two lists, etc.
- We want the linked list class to be generic such that it can be used to process different data types.