

# Univariate CoR: Nonparametric Threshold Modeling

Spike protein antibody

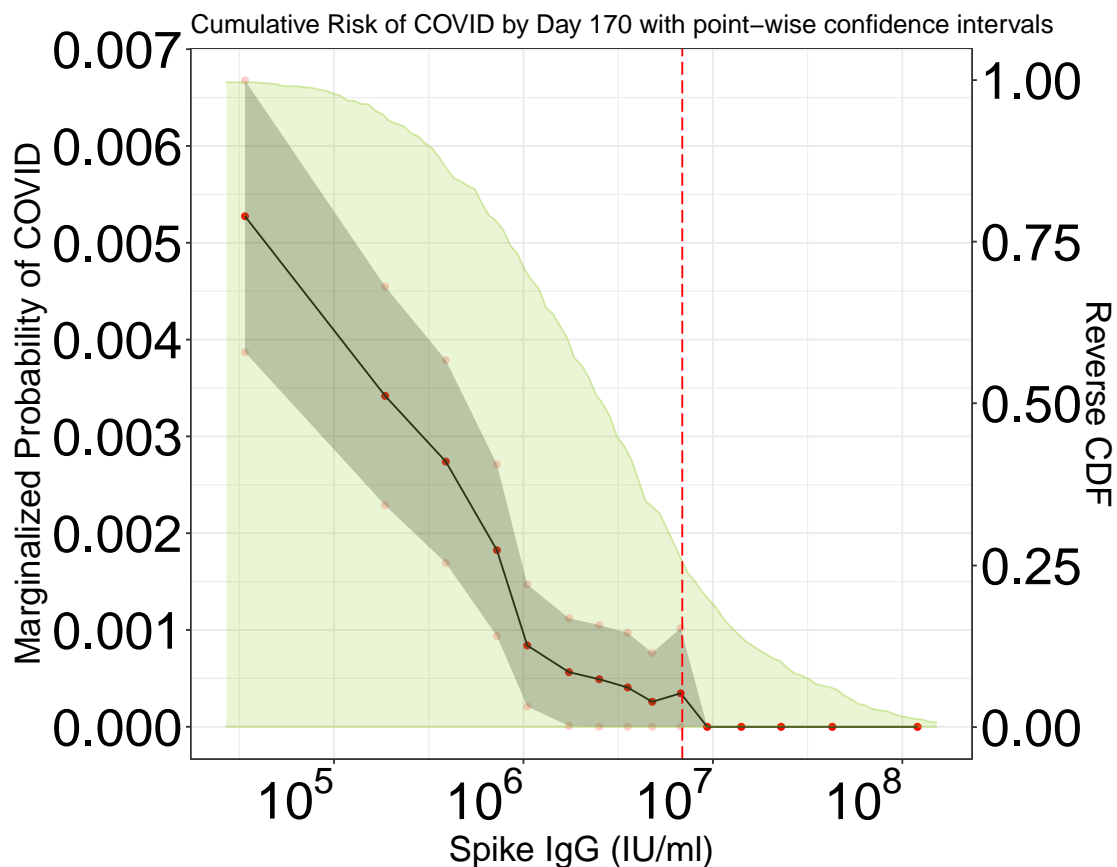


Figure 1: Adjusted threshold-response function for a range of thresholds of the Day 57 Spike protein antibody activity levels with point-wise 95% confidence intervals. The dashed red line marks the threshold after which no more COVID events are observed.

log10-Threshold	Threshold	Risk estimate	CI left	CI right
4.531	$3.40 \cdot 10^4$	0.00527	0.00387	0.00668
5.588	$3.87 \cdot 10^5$	0.00274	0.00169	0.00379
5.860	$7.24 \cdot 10^5$	0.00182	0.00094	0.00271
6.236	$1.72 \cdot 10^6$	0.00056	0.00001	0.00112
6.395	$2.48 \cdot 10^6$	0.00049	0.00000	0.00105
6.677	$4.75 \cdot 10^6$	0.00026	0.00000	0.00076
6.832	$6.79 \cdot 10^6$	0.00035	0.00000	0.00102
7.151	$1.42 \cdot 10^7$	0.00000	0.00000	1.00000
7.356	$2.27 \cdot 10^7$	0.00000	0.00000	1.00000
8.081	$1.21 \cdot 10^8$	0.00000	0.00000	1.00000

Figure 2: Table of risk estimates for range of thresholds of Spike protein antibody activity levels with point-wise 95% confidence intervals.

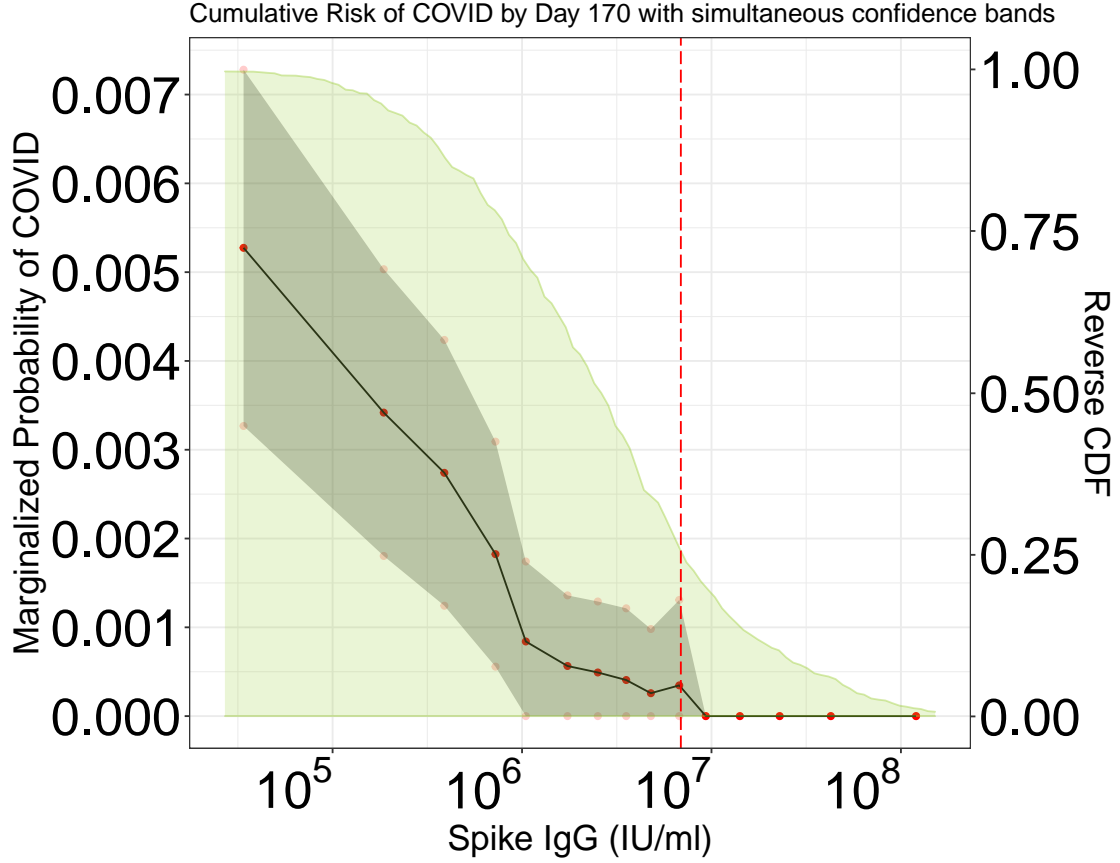


Figure 3: Adjusted threshold-response function for a range of thresholds of the Spike protein antibody activity levels with simultaneous 95% confidence bands. The dashed red line marks the threshold after which no more COVID events are observed.

log10-Threshold	Threshold	Risk estimate	CI left	CI right
4.531	$3.40 \cdot 10^4$	0.00527	0.00327	0.00728
5.588	$3.87 \cdot 10^5$	0.00274	0.00124	0.00424
5.860	$7.24 \cdot 10^5$	0.00182	0.00056	0.00309
6.236	$1.72 \cdot 10^6$	0.00056	0.00000	0.00136
6.395	$2.48 \cdot 10^6$	0.00049	0.00000	0.00129
6.677	$4.75 \cdot 10^6$	0.00026	0.00000	0.00098
6.832	$6.79 \cdot 10^6$	0.00035	0.00000	0.00131
7.151	$1.42 \cdot 10^7$	0.00000	0.00000	1.00000
7.356	$2.27 \cdot 10^7$	0.00000	0.00000	1.00000
8.081	$1.21 \cdot 10^8$	0.00000	0.00000	1.00000

Figure 4: Table of risk estimates for range of thresholds of Spike protein antibody activity levels with simultaneous 95% confidence bands

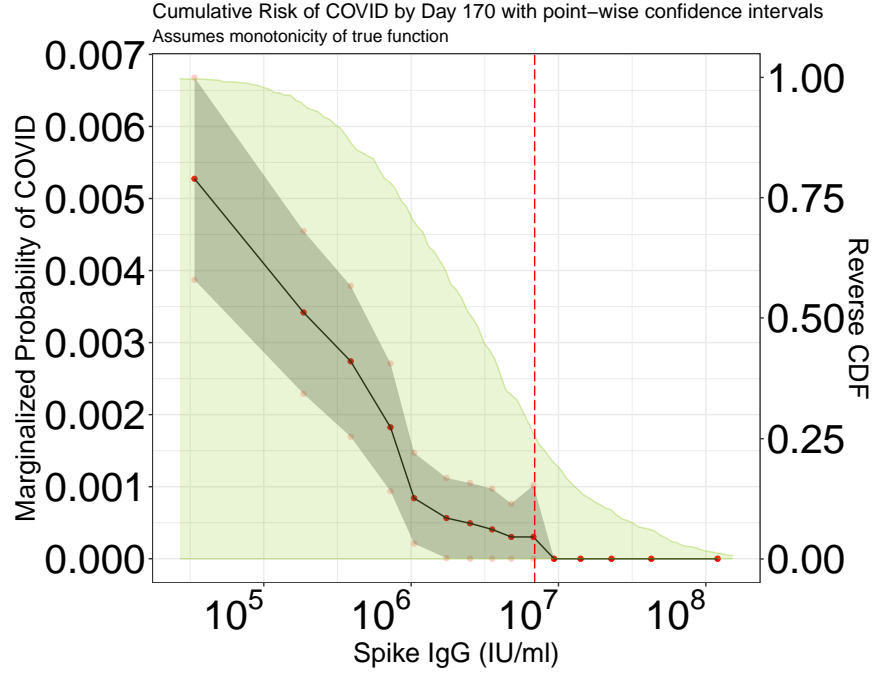


Figure 5: Assuming nonincreasing monotonicity of the true function, the plot shows the estimated (monotone) adjusted threshold-response function for a range of thresholds of the Spike protein antibody activity levels with point-wise 95% confidence intervals. The dashed red line marks the threshold after which no more COVID events are observed.

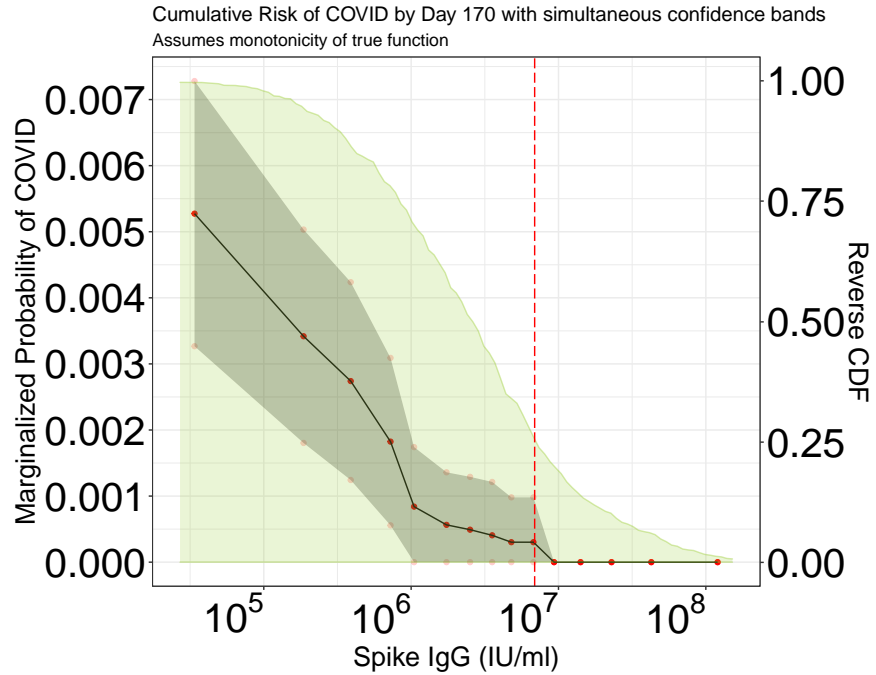


Figure 6: Assuming nonincreasing monotonicity of the true function, the plot shows the estimated (monotone) adjusted threshold-response function for a range of thresholds of the Spike protein antibody activity levels with simultaneous 95% confidence intervals. The dashed red line marks the threshold after which no more COVID events are observed.

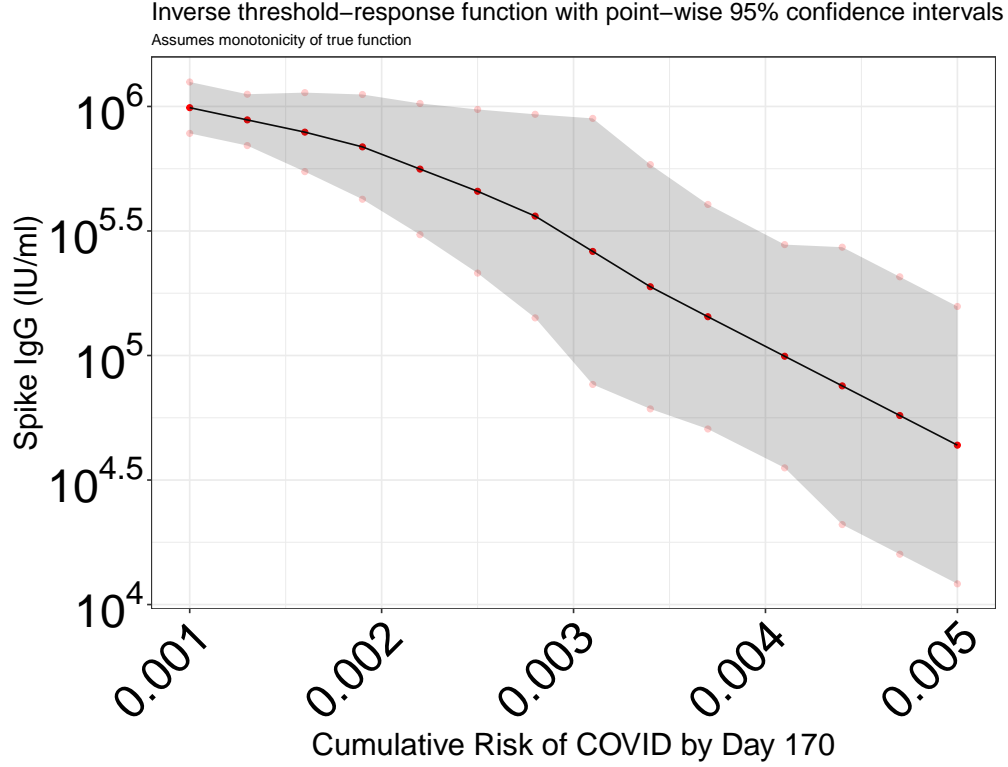


Figure 7: The inverse adjusted threshold-response function with pointwise 95% confidence intervals.

Risk	Threshold est.	CI left	CI right
0.001	$1.00 \cdot 10^6$	$7.76 \cdot 10^5$	$1.26 \cdot 10^6$
0.0013	$8.91 \cdot 10^5$	$6.92 \cdot 10^5$	$1.12 \cdot 10^6$
0.0016	$7.94 \cdot 10^5$	$5.50 \cdot 10^5$	$1.15 \cdot 10^6$
0.0019	$6.92 \cdot 10^5$	$4.27 \cdot 10^5$	$1.12 \cdot 10^6$
0.0022	$5.62 \cdot 10^5$	$3.09 \cdot 10^5$	$1.02 \cdot 10^6$
0.0025	$4.57 \cdot 10^5$	$2.14 \cdot 10^5$	$9.77 \cdot 10^5$
0.0028	$3.63 \cdot 10^5$	$1.41 \cdot 10^5$	$9.33 \cdot 10^5$
0.0031	$2.63 \cdot 10^5$	$7.59 \cdot 10^4$	$8.91 \cdot 10^5$
0.0034	$1.91 \cdot 10^5$	$6.17 \cdot 10^4$	$5.89 \cdot 10^5$
0.0037	$1.45 \cdot 10^5$	$5.01 \cdot 10^4$	$4.07 \cdot 10^5$
0.0041	$1.00 \cdot 10^5$	$3.55 \cdot 10^4$	$2.82 \cdot 10^5$
0.0044	$7.59 \cdot 10^4$	$2.09 \cdot 10^4$	$2.69 \cdot 10^5$
0.0047	$5.75 \cdot 10^4$	$1.58 \cdot 10^4$	$2.09 \cdot 10^5$
0.005	$4.37 \cdot 10^4$	$1.20 \cdot 10^4$	$1.58 \cdot 10^5$

Figure 8: This analysis assumes monotonicity of the true function. The table displays the estimated threshold of protection of Spike protein antibody activity level at a range of risk levels with pointwise 95% confidence intervals.

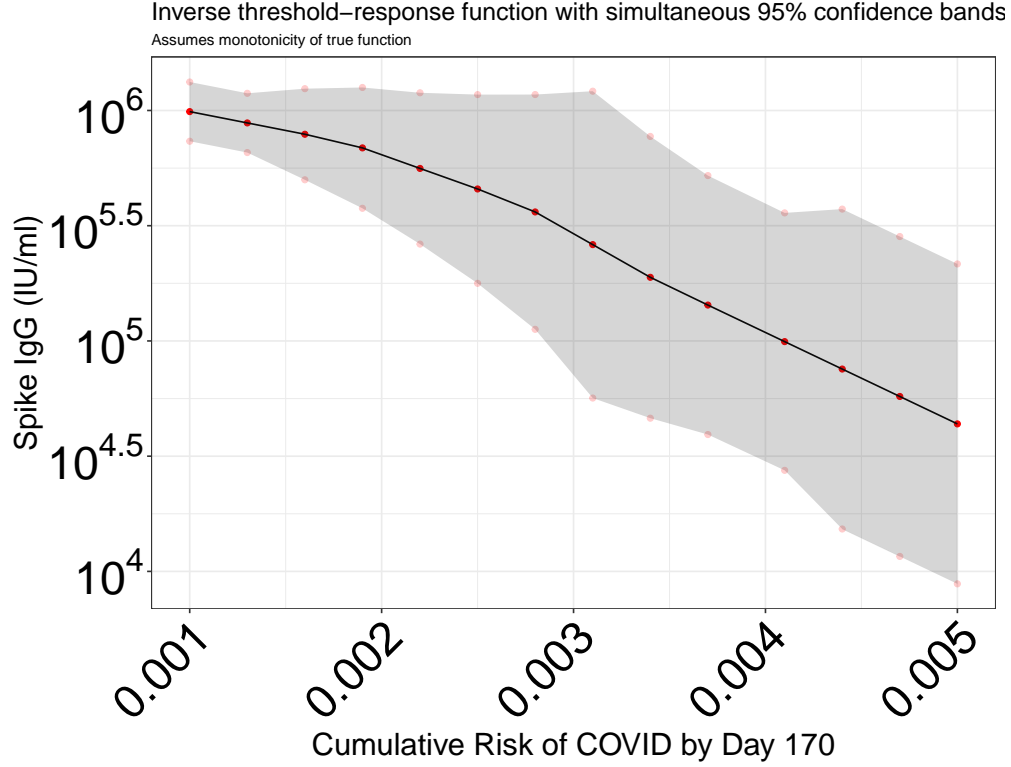


Figure 9: This analysis assumes monotonicity of the true function. The plot shows the inverse adjusted threshold-response function with simultaneous 95% confidence intervals.

Risk	Threshold est.	CI left	CI right
0.001	$1.00 \times 10^6$	$7.41 \times 10^5$	$1.32 \times 10^6$
0.0013	$8.91 \times 10^5$	$6.61 \times 10^5$	$1.17 \times 10^6$
0.0016	$7.94 \times 10^5$	$5.01 \times 10^5$	$1.23 \times 10^6$
0.0019	$6.92 \times 10^5$	$3.80 \times 10^5$	$1.26 \times 10^6$
0.0022	$5.62 \times 10^5$	$2.63 \times 10^5$	$1.20 \times 10^6$
0.0025	$4.57 \times 10^5$	$1.78 \times 10^5$	$1.17 \times 10^6$
0.0028	$3.63 \times 10^5$	$1.12 \times 10^5$	$1.17 \times 10^6$
0.0031	$2.63 \times 10^5$	$5.62 \times 10^4$	$1.20 \times 10^6$
0.0034	$1.91 \times 10^5$	$4.57 \times 10^4$	$7.76 \times 10^5$
0.0037	$1.45 \times 10^5$	$3.89 \times 10^4$	$5.25 \times 10^5$
0.0041	$1.00 \times 10^5$	$2.75 \times 10^4$	$3.63 \times 10^5$
0.0044	$7.59 \times 10^4$	$1.51 \times 10^4$	$3.72 \times 10^5$
0.0047	$5.75 \times 10^4$	$1.15 \times 10^4$	$2.82 \times 10^5$
0.005	$4.37 \times 10^4$	$8.91 \times 10^3$	$2.14 \times 10^5$

Figure 10: This analysis assumes monotonicity of the true function. The table displays the estimated threshold of protection of Spike protein antibody activity level at a range of risk levels with simultaneous 95% confidence bands