

# Minimum Spanning Trees

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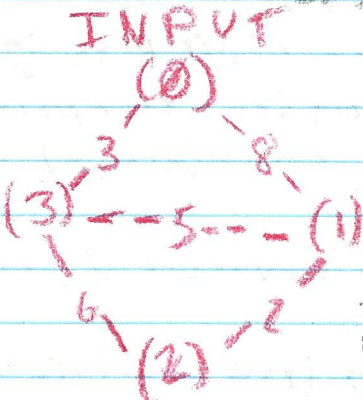
completed using the Kruskal Algorithm

- greedy algo.  
- greedy choice

is to pick smallest weighted edge that does not cause a cycle in MST so far!

DEF. a graph consisting of the subset of edges which together connect all connected nodes, while minimizing the total sum of weights on the edges

Routine uses undirected graphs as input/output



**OUTPUT MIN SPANNING TREE**

(0)

(3) --- 5 --- (1)

(2)

involves rem. the edges that AREN'T VITAL TO connecting every node

**MINIMUM S.T.**

↓ wasted space & efficiency

• A single graph can have many MSTs

- "Minimum weight spanning tree"

For a weighted, connected, undirected graph has weight  $\leq$  weight of every other spanning tree (sum of weights given to each edge of spanning tree)

Uses Union-Find algorithm

- Has  $V-1$  edges (where  $V$  = # of vertices in given graph)
- Steps for finding MST w/ Kruskal's Algorithm
  - 1) sort all edges in non-decreasing order of their weight
  - 2) pick smallest edge, check if it forms a cycle w/ spanning tree so far. IF cycle formed include this edge. Else, discard it
  - 3) Repeat Step #2 until there are  $(V-1)$  edges in S.T.