

AST 3033.

D. Levinthal

508 keen

X6760

X1492

text The Physical Universe

R. Shu

recommended: structure and evolution of stars

M. Schwarzschild

Prob.

Ch 1

~~constellations~~

overview, constellations, solar system, greek astronomy

Ch 2

light optics telescopes

2.3, 2.5

Ch 3

General Physics

3.4, 3.5, 3.6, 3.7

newtons laws

3.10, 3.13, 3.16

gravity, gauss' law

conservation of energy

centripetal acceleration.

Electro Magnetism.

~~the~~ Quantum Mechanics

Uncertainty principle

hydrogen atom.

Pauli exclusion principle

Special relativity

time dilatation

length contraction

~~doppler~~ doppler shift.

mass; energy equivalence

Ch 4.

Statistical mechanics.

4.1 4.2 4.5 4.8

thermodynamics, entropy

and problems to

Second law.

be handed out.

connection of QM to SM

Ideal gas law

Quantum Statistical Mechanics.

Ch 5 Stars

Sun, Luminosity, Blackbody radiation  
stellar types

5.1, 5.4, 5.5, 5.11, 5.13, 5.14  
and problem to be handed  
out.

Stellar structure (Schwarzschild)

Hydrostatic Equilibrium  
radiative transport  
Convection.

Ch 6 nuclear energy

nucleosynthesis

proton~~ia~~ proton chain

CNO cycle

Helium burning.

~~Calculation of~~ energy production density of stars

6.1, 6.5 6.7 6.10 6.12 6.13 6.14

Ch 7 White dwarfs neutron stars black holes

7.1, 7.3 7.4, 7.5, 7.7, 7.8, 7.9

Structure of white dwarfs

Chandrasekhar mass limit

neutron stars / pulsars

Black holes / General relativity

Ch 8 Theoretical Hertzsprung - Russell diagram

stellar properties / evolution

Population I / II stars

HR diagram

radiation pressure in high mass stars

red giants

red super giants

planetary nebula

Super novae

8.1 8.3 8.4 8.6 8.7

ch 9      Observational Hertzsprung-Russell diagram  
9.2 9.5 9.8 9.9 9.10 9.12

Stellar types

distances - magnitudes

star clusters

H R diagrams

moving cluster distance

Cepheid variables,

Virial theorem of clusters.

ch 10      Binary stars.      10.1 10.3 10.4 10.5 10.6

orbit parameters

stellar masses

roche surfaces

mass transfer

contact binaries

Semi detached binaries

Algol type binaries

accretion disks

nova



recommended: Eddington Internal structure of stars  
Mathematical theory of relativity.  
Weinberg General relativity.

## lecture 1.

①. Background to course Astro 3033  
prof. D. Levithal  
508 keen

text: Physical Universe F Shu, \$35.00  
University Science Books.

highly recommended: Structure and Evolution of Stars.  
M. Schwarzschild.  
Dover press \$6.00

## ②. student background.

How many have taken calculus  
" 2048  
" 2049  
" Physics majors.

Pass out syllabus.

Grades	10%	homework.			
	1 or 2	midterms	discuss	25%	25%
	1	final	cumulative	40%	55%

Solutions to problems will be passed out  
ie can't be turned in afterwards  
Note: most problems are trivial plug ins  
don't worry about the quantity.

Shu's book will be direct ordered from publisher  
this saves \$12.00 But. ~~we need~~ money orders  
should be sent by mail/tues to get them soon  
Kay Caudill 302 keen will collect money orders

Pass out syllabus

①. overview

Stars : structure / evolution, galaxies, cosmology

Astronomy : passive experimental science (for the most part)

# Symbols.

$x$  = position vector  
 $v$  = velocity =  $\frac{dx}{dt} = \dot{x}$  vector  
 $m$  = mass scalar  
 $c$  speed of light =  $3 \times 10^8$  m/sec. scalar  
 $F$  force vector  
 $a$  acceleration. =  $dv/dt = \dot{v}$  vector  
 $T$  = kinetic energy =  $\frac{1}{2}mv^2$  scalar.

$V$  (or  $U$  sometimes) Potential Energy  $F_x = -\frac{dV}{dx}$   
 $L$  Lagrangian  $T - V$

$H$  hamiltonian = total energy =  $T + V$

$\psi(x, t)$  wave function. (psi)

$h$  planks constant.

$\hbar = h/2\pi$

$G$  gravitational constant.

$e$  charge of an electron

$r$  distance or ~~between~~ between two objects  
or radius.

$\lambda$  wave length.

$f$  or  $\nu$  (nu) frequency.

$\beta = v/c$

$\gamma = \frac{1}{\sqrt{1-v^2/c^2}} = \frac{1}{\sqrt{1-\beta^2}}$  (gamma)

$k$  used in 2 ways.  
 $k$  ~~at charge~~ constant in electrostatic force law  
 similar to  $G$  in concept.  
 or wave number  $1/\lambda$ .

$J = mvr =$  angular momentum.

$\theta$  angle. theta.



# Ch 1.

## Coordinates:

①. constellations

brightest to dimmest  $\alpha, \beta, \gamma, \delta$   
countries / circles

Celestial sphere      fixed stars.

north } celestial pole  
south }

zenith.  
meridian

~~the~~ great circle  
connecting zenith  
to poles.

Celestial equator.

longitude      latitude

right ascension      declination

Sun  $\rightarrow$  ecliptic.

Zero right ascension intersection of  
equator / ecliptic.

② Time.

mean solar day.

meridian crossing to meridian crossing.  
average over one year

sidereal day

same but with a particular star.

$\approx 23 \text{ hr } 56 \text{ min } 4 \text{ sec}$  (solar time).

right ascension = sidereal time.

year: sidereal yr. sun obscures same star.

365.2564 in solar days.

precession of earth axis.

wobbles celestial sphere not ecliptic.

$\Rightarrow$  intersection of ecliptic / celestial eq. moves around  
 $360^\circ$  every 26,000 yrs

tropical yr.      vernal eq.      to vernal eq.  
365.2422 days

julius ~~caesar~~ Caesar      365  $\frac{1}{4}$ .

by Pope Gregory XIII      1582.

vernal equinox off by 10 days.  
adds 10 day and.

Only centuries divisible by 400 leap yrs.

$\Rightarrow$  1700 1800 1900 not leap years  
2000 is.

Gregorian year      365, 2425.

also occasional adjustments for wobbles.

ex. 1 extra second was added at end  
of this last yr 1982



## Ch 2.

Newtons laws.

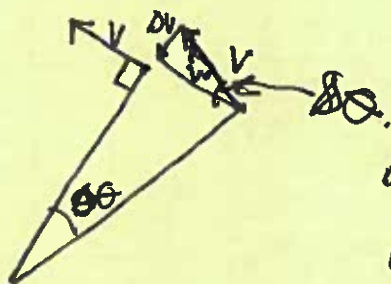
①. principle of inertia concept of mass.

②.  $F = ma$

$$F = \frac{dp}{dt}$$

$$p = mv$$

$$a = \frac{dv}{dt} = \dot{v}$$



$$dv = v d\theta$$

$$\frac{dv}{dt} = v \frac{d\theta}{dt} \Rightarrow v \frac{d\theta}{dt}$$

$$v = r \frac{d\theta}{dt} \Rightarrow \frac{v}{r} = \frac{d\theta}{dt}$$

Centrifugal  
acceleration.

$$a = \frac{dv}{dt} = v \frac{d\theta}{dt} = \frac{v^2}{r}$$

light. Electro magnetic wave

changing electric field cause changing magnetic field  
& vice versa.

①. Speed of propagation in vacuum  $= c = 3 \times 10^8 \text{ m/s}$

②. Wave length.

$$f \lambda = c \quad \text{or} \quad \nu \lambda = c.$$

③. Polarization. transverse wave.

direction of E field  $\perp$  to B field  
 $\perp$  to direction of motion.

carries energy.  
energy density  $= \frac{1}{2\epsilon_0} (\vec{E} \cdot \vec{E} + \vec{B} \cdot \vec{B})$

flux. = Poynting's vector

$$\vec{f} = \frac{c}{4\pi} (\vec{E} \times \vec{B})$$

for light  $\langle E \rangle_t = \langle B \rangle_t$

$$\Rightarrow \frac{c}{4\pi} E B = \frac{c}{8\pi} (E^2 + B^2) = c \times \text{energy dens.}$$

Source are charges i.e. charged particles.  
~~force~~ Electrons / protons.

$$\vec{F}_q = q \left( \vec{E} + \frac{\vec{v}}{c} \times \vec{B} \right)$$

Lorentz force.

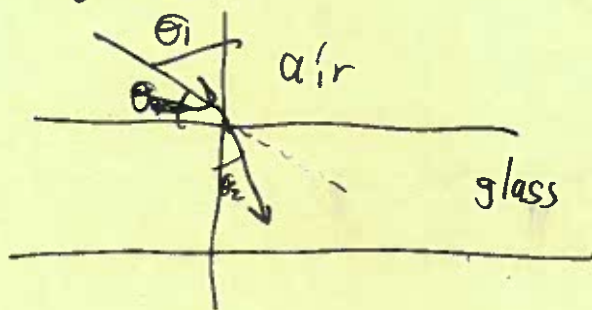
↑  
cross product. Right hand rule.

force  $\perp$  to  $\vec{v}$  and  $\vec{B}$ .

$\Rightarrow$  particle goes in a circle.

interaction with material (telescopes/spectrum analyzers)

refraction.



Snell's law

$$\frac{\sin \theta_1}{\sin \theta_2} = \frac{n_2}{n_1}$$

$n$  = index of refraction

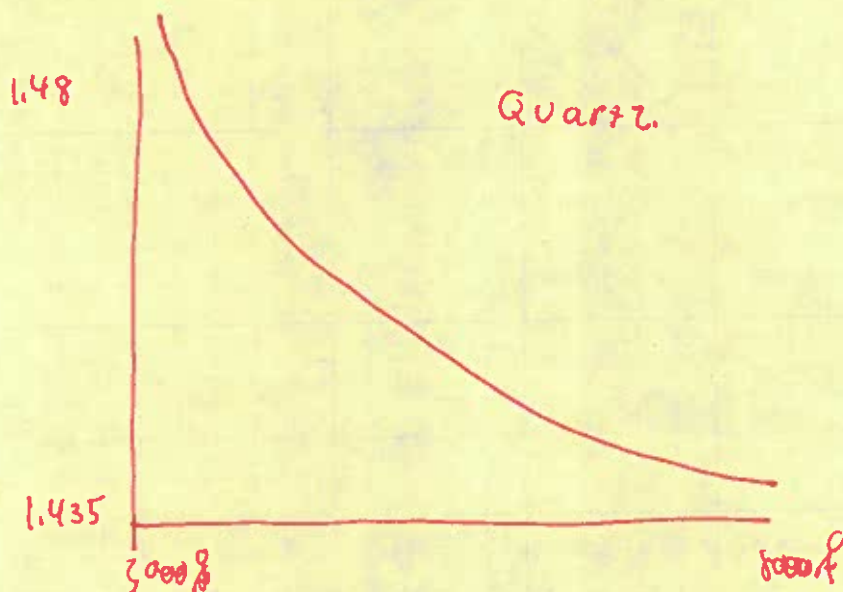
air = vac = 1

water ~~glass~~ = 1.3333

glass 1.5  $\Rightarrow$  2.

diamond 2.4.

The index of refraction of materials typically depends on wavelength.



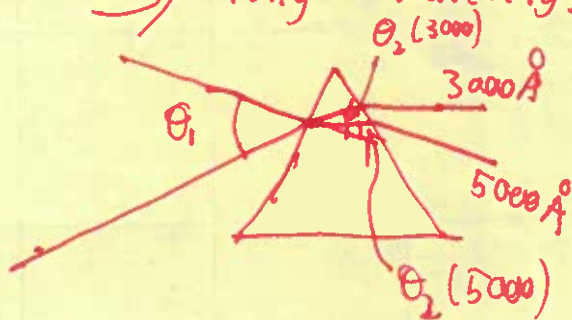
So at the interface of air (<sup>medium 1</sup> = vacuum) and Glass (medium 2)

$$\frac{\sin \theta_1}{\sin \theta_2(\lambda)} = n_2(\lambda)$$

$$\text{or } \frac{\sin \theta_2(\lambda)}{\sin \theta_1} = \frac{1}{n_2(\lambda)}$$

note  $n(3000 \text{ Å}) > n(5000 \text{ Å})$

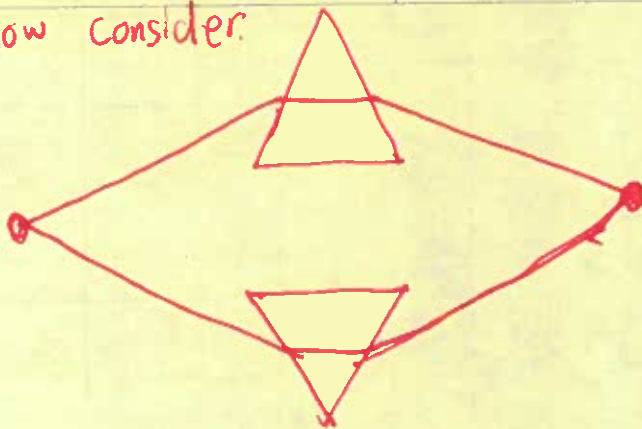
⇒ long wavelengths bend less.



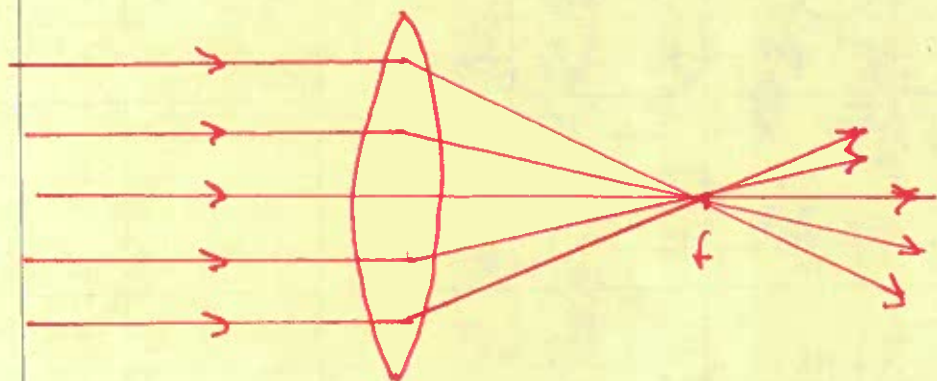
i.e. refraction can be used to disperse the light spectrum into a rainbow.



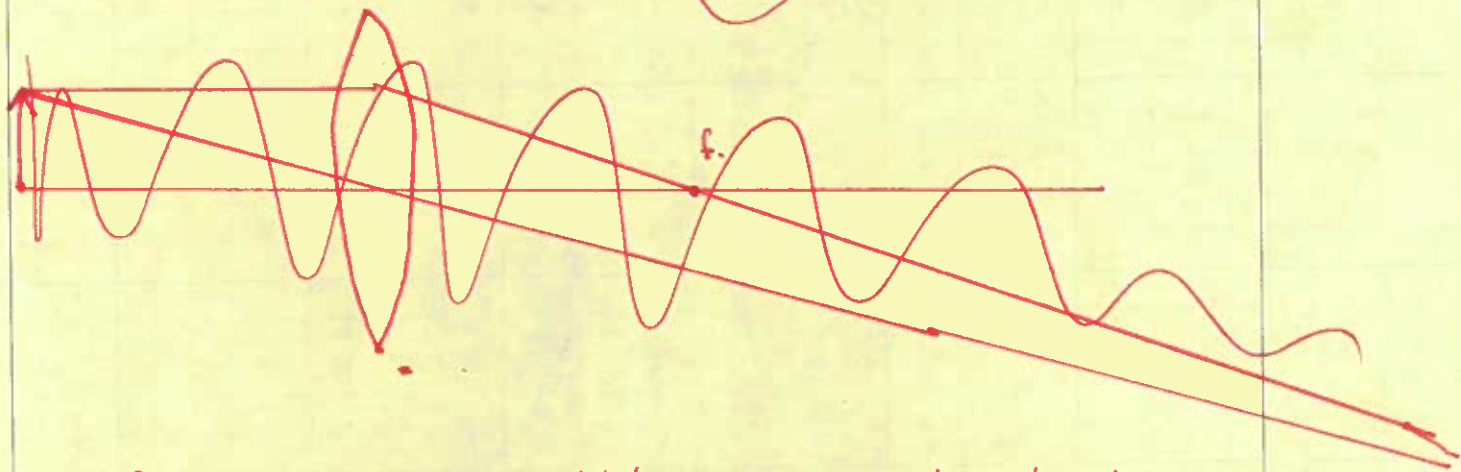
now consider



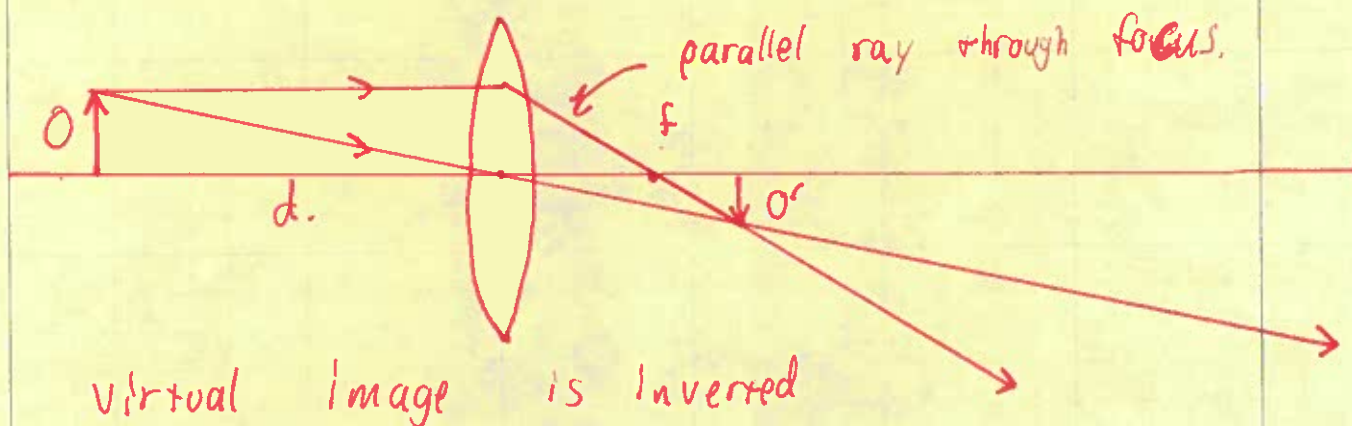
lens. (ray tracing).



parallel light is all converged on the focus.  
consider an object.



note: the ray which passes through the center of the lens is undeflected.



matrix technique of lens systems.

a ray of light is written as a 2 component vector.

$$\begin{pmatrix} x \\ x' \end{pmatrix} \quad \text{where } x' \equiv \frac{dx}{dz} = \text{slope.}$$

the position of the ray after a distance  $L$  is.

$$x(L) = x + x' \cdot L.$$

~~can be so~~ the slope is still  $x' \Rightarrow x'(L) = x'$

this can be written as.

$$\begin{pmatrix} x(L) \\ x'(L) \end{pmatrix} = \begin{pmatrix} 1 & L \\ 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ x' \end{pmatrix}$$

with the matrix being the drift matrix.

the effect of a thin lens is

$$x(\text{after lens}) = x(\text{before lens}) \quad \text{infinitely thin.}$$

$$x'(\text{after}) = \frac{x(\text{before})}{-f} + x'(\text{before})$$

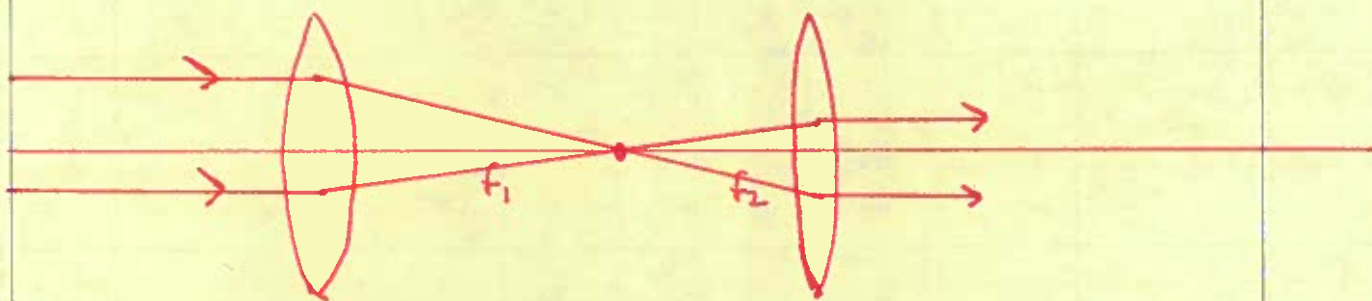
(6)

where  $f$  is the focal length.

thus, a lens has the effect.

$$\begin{pmatrix} x \\ x' \end{pmatrix}_{\text{after}} = \begin{pmatrix} 1 & 0 \\ -\frac{1}{f} & 1 \end{pmatrix} \begin{pmatrix} x \\ x' \end{pmatrix}_{\text{before}}$$

the matrix being the focussing matrix.  
consider a compound system



if  $f_1 \gg f_2$  then the parallel light is concentrated ie an infinitely far away object appears brighter to the eye

in matrix notation this would become.

$$\begin{aligned} & \begin{matrix} \text{lens 2} & \text{drift} & \text{lens 1} \end{matrix} \\ & \begin{pmatrix} 1 & 0 \\ -\frac{1}{f_2} & 1 \end{pmatrix} \begin{pmatrix} 1 & f_1+f_2 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 \\ -\frac{1}{f_1} & 1 \end{pmatrix} \begin{pmatrix} x \\ 0 \end{pmatrix} \\ & \begin{pmatrix} 1 & 0 \\ -\frac{1}{f_2} & 1 \end{pmatrix} \begin{pmatrix} 1 - \frac{f_1+f_2}{f_1} & f_1+f_2 \\ -\frac{1}{f_1} & 1 \end{pmatrix} \begin{pmatrix} x \\ 0 \end{pmatrix} \\ & \begin{pmatrix} 1 - \frac{f_1+f_2}{f_1} & f_1+f_2 \\ \frac{f_1+f_2}{f_1 f_2} - \frac{1}{f_1} - \frac{1}{f_2} & 1 - \frac{f_1+f_2}{f_2} \end{pmatrix} \begin{pmatrix} x \\ 0 \end{pmatrix} \\ & \begin{pmatrix} 1 - \frac{f_1+f_2}{f_1} & f_1+f_2 \\ 0 & 1 - \frac{f_1+f_2}{f_2} \end{pmatrix} \begin{pmatrix} x \\ 0 \end{pmatrix} \end{aligned}$$



The significance of the lower left element being zero is that the outgoing ray's direction is independent of its incoming position hence parallel light coming in is parallel light going out though direction may be changed (comment on beam lines / accelerators Quads = lens)

Telescopes can also be made with mirrors like the one we used last night. This is much more common because it is vastly less expensive.

A parabola has the property that it focus' ~~light~~ parallel light at the parabolic focus. This is well illustrated in the book so I won't harp on it. As far as the matrix approach is concerned mirrors can be treated like lens'. There are a variety of standard reflecting telescope configurations.

Prime  
newtonian  
Cassegrain (like the one we used)  
Coudé

Two important features of telescopes

①. Signal.

The brightness focussed onto your eye or a camera is proportional to the area of the telescope. ie  $B \propto D^2$ .

②. resolution

$$\begin{aligned}\theta_{\text{diff. limit}} &= 1.22 \lambda / D \quad (\text{in radians}) \\ &= 206265 \cdot 1.22 \lambda / D \quad (\text{in seconds of arc})\end{aligned}$$

⑧.

The shorter the wavelength the better the resolution therefore two very close stars will be blurred into one object in the red but resolvable in the blue

The largest optical telescope is in the Soviet Union with a diameter of 6 meters. The largest in the West is on Mt. Palomar Calif and is 200 in ( $\sim 5$  m.)

the resolution of this device at say  $5000 \text{ \AA}$

$$\theta_{\min} = 2.063 \times 10^5 \cdot 1.22 * \frac{5 \times 10^{-7} \text{ m}}{5}$$

$$= .025 \text{ sec of arc.}$$

This cannot be achieved due to atmospheric distortions and the air limits it to

$$\theta_{\text{seeing}} \sim .25 \text{ sec of arc.}$$

on Mauna Kea Hawaii 14,000 ft.!

$$\theta_{\text{seeing}} \sim .1 \text{ sec of arc.}$$

the space telescope (2.4 m.) which will be above the atmosphere will achieve its theoretical resolution and because it is above the water vapor can be run in the Ultra Violet

$$\lambda \sim 1000 \rightarrow 2000 \text{ \AA}$$

9

## Aperture Synthesis radio telescopes

telescopes can be made to run at radio wavelengths using metallic parabolic reflectors. The signals can be added electronically preserving the phase information to create the interference pattern which corresponds to focussing, hence.



two telescopes of diameter  $D$  separated by a length  $L$  can have a resolution,

$$\theta = 2.063 \times 10^5 \cdot 1.22 \cdot \lambda / L$$

and a signal  $\propto D^2$

VLA very large array in NM. has 75 25 m dishes spread out on rail road track 15 miles long laid out in a Y

At optical wavelengths the frequencies are far too high to play this game but large ~~mirrors~~ telescopes can be made using multiple mirrors to gather more signal.

What can be done is.

moving mirror  
speckle interferometry

$1/r^2$



## Ch 3.

forces.

There are four known forces in nature

the gravitational force  $10^{-40}$ the weak nuclear force  $10^{-10}$ 

the electro magnetic force 1

the strong nuclear force 100

To date ~~the~~ two of these forces (the weak nuclear and electromagnetic forces) have been unified into a single mathematical description. Gravity is described geometrically by general relativity and the strong nuclear force is currently best described by a theory something like electromagnetism but with some major differences

① the force mediators (like the EM photon) are "charged." (Non Abelian).

② there are three charges instead of one in EM.

Gravity is the force we will mainly be concerned with it has the form,

$$\vec{F}_g = -G \frac{M_1 M_2}{r_{12}^3} (\vec{r}_1 - \vec{r}_2)$$

$$G = 6.67 \times 10^{-11} \text{ m}^3/\text{kg sec}^2$$

$$6.67 \times 10^{-8} \text{ cm}^3/\text{gm sec}^2.$$

mechanics has led to certain understandings of the universe among them that there exist certain physical quantities whose values do not change in time. ~~among them~~. These conserved quantities in fact are fundamentally tied to the invariance properties of the universe.

Conserved quantity	invariance
① Energy	laws of physics are constant in time
② momentum	laws of physics are independent of absolute position
③ Angular momentum	laws of physics are independent of rotations.

The assigned problem 3.1 is to explicitly show that for gravitation Energy is conserved