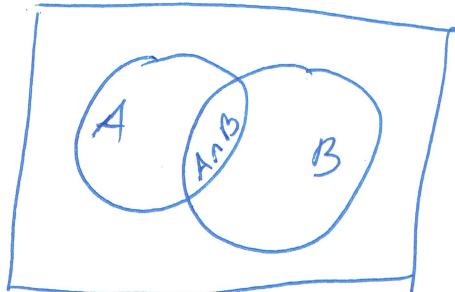


- 1) a) $A \cup B$
 b) $A \cap B$
 c) $A \setminus B$
 d) $(A \setminus B) \cup (B \setminus A)$
 e) $A' \cap B'$

2) $P(A') = \frac{1}{3}$ $\left\{ \begin{array}{l} P(A) = \frac{2}{3} \\ P(A \cap B) = \frac{1}{6} \\ P(A \cup B) = \frac{2}{3} \end{array} \right.$ $\left\{ \begin{array}{l} P(B) = \frac{1}{4} \\ P(B') = \frac{3}{4} \end{array} \right.$



$$P(A \setminus B) = P(A) - P(A \cap B) = \frac{2}{3} - \frac{1}{6} = \frac{8}{12} - \frac{3}{12} = \frac{5}{12}$$

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$\frac{2}{3} = \frac{2}{3} + P(B) - \frac{1}{6}$$

$$\frac{1}{6} = P(B)$$

$$P(A \cap B') = P(A \setminus B) = \frac{2}{3} - \frac{1}{6} = \frac{8}{12} - \frac{3}{12} = \frac{5}{12}$$

$$P(B \setminus A) = \frac{1}{4} - \frac{1}{6} = 0$$

3)

3)

$$(A1) \quad \forall A \in \mathcal{F} \quad P(A) \geq 0$$

$$(A2) \quad P(\Omega) = 1$$

$$(A3) \quad A_1, A_2, \dots \quad A_i \cap A_j = \emptyset \\ \text{dla } i \neq j$$

$$P: \mathcal{F} \rightarrow \mathbb{R}$$

$$\Omega = N = \{1, 2, 3, \dots\}$$

$$\text{a)} \quad P(\{\omega_n\}) = \frac{1}{\sqrt{n}}, \quad n \in N$$

$$\{\omega_n\} = \omega_n$$

A1 +

$$P(\{1\}) = 1$$

$$P(\{2\}) = \frac{1}{\sqrt{2}}$$

$$P(\{1 \cup 2\}) = 1 + \frac{1}{\sqrt{2}} > 1$$

A2 -

$$\text{b)} \quad P(\{\omega_n\}) = c \cdot (-1)^{n+5} \quad (\forall n \text{ oddneq } c \in \mathbb{R}, n \in \mathbb{N})$$

$$c=0 : \forall n \quad P(\{\omega_n\}) = 0 \Rightarrow P(\Omega) = 0 \quad \text{A2 -}$$

c) $P(\{n\}) = c/n^2$ dla $c \in \mathbb{R}$ i $n \in \mathbb{N}$

c) 70

$$P(\Omega) = 1 = P\left(\bigcup_{n=1}^{\infty} \{n\}\right) = \sum_{n=1}^{\infty} P(\{n\}) = \sum_{n=1}^{\infty} \frac{c}{n^2} = c \sum_{n=1}^{\infty} \frac{1}{n^2}$$

$$\textcircled{5} \quad \binom{49}{6} = \frac{49!}{(49-6)!6!} = \frac{49 \cdot 48 \cdot 47 \cdot 46 \cdot 45 \cdot 44}{1 \cdot 2 \cdot 3 \cdot 4 \cdot 5 \cdot 6} = \\ = 13\ 983\ 816$$

$$P = \frac{1}{13\ 983\ 816}$$

\textcircled{6} 6 BIAŁYCH
2 CZARNYCH $\sum 8$

A - 3 BIAŁE i 1 CZARNA

$$\bar{\Omega} = \binom{8}{4} = \frac{8!}{4!4!} = \frac{5 \cdot 4 \cdot 3 \cdot 2}{4 \cdot 3 \cdot 2 \cdot 1} \cdot \frac{8!}{1 \cdot 1 \cdot 1} = 70$$

$$\bar{A} = \binom{6}{3} \binom{2}{1} = \frac{6!}{3!3!} \cdot \frac{2!}{1!1!} = \frac{3! \cdot 2!}{3!2!} \cdot \frac{2 \cdot 1}{1} = 20 \cdot 2 = 40$$

$$P(A) = \frac{A}{\bar{\Omega}} = \frac{40}{70} = \frac{4}{7}$$

19) A - BDWIEZ OSOBY UNODUJE SIE U TYM SWIEM DNIU
B - RÓLNE DNI (KAIOS V INNYMI DNIAMI)

$$\Omega = 100\% = P(A) + P(B)$$

$$\Omega = (365)^{365}$$

~~$$B = \frac{365!}{(365-30)! 365^{30}}$$~~

~~$$B = \frac{365!}{(365-30)! 365^{30}} = \frac{365!}{(335)! 365^{30}}$$~~

$$\text{dla } m = 30$$

$$B = \frac{365!}{(365-30)! 365^{30}} = \frac{365!}{(335)! 365^{30}} \approx 0,2937$$

$$A = 1 - 0,2937 = 0,7063$$

$$\text{dla } m = 40$$

$$B = \frac{365!}{(365-40)! 365^{40}} = \frac{365!}{(325)! 365^{40}} \approx 0,1088$$

$$A = 1 - 0,1088 = 0,8912$$

$$8) \Omega = \{(x_1; x_2; x_3 \dots; x_{10}) : x_i \in \{0; 1\}, i=1, \dots, 10\}$$

/ |
OBERK RESULT

$$\Omega = 2^{10} = 1024$$

$$\bar{A} = 1$$

$$P(A) = \frac{1}{1024}$$

$$9) \Omega = \{x_1; x_2; x_3 ; x_i \in \{1, 2, 3\}, i=1, 2, 3\}$$

$x_i \rightarrow$ wynik i RWTU

$$\bar{\Omega} = 6^3 = 216$$

a) $A \rightarrow 2A$ (A jestem BRADEM INNA LICZBA)

OGRZĄ

$$\bar{A} = 6 \cdot 5 \cdot 4 =$$

$$P(A) = \frac{6 \cdot 5 \cdot 4 \cdot 1}{6 \cdot 5 \cdot 4 \cdot 3 \cdot 3} = \frac{1}{9}$$

b) B - 2 AUSZE TA SĄCA
LICZBA OGRZĄ

$$\bar{B} = 6 \cdot 1 \cdot 1 = 6$$

$$P(B) = \frac{6 \cdot 1 \cdot 1}{6 \cdot 6} = \frac{1}{36}$$

$$\overline{L}_1 = 6'$$

$$I_2 = \cancel{6.736}$$

$$S_3 = 6 \cdot \cancel{6}$$

A - WYPADEK 1x 6

$\downarrow_B = \text{WYP4DK4} \quad 2 + 6$

$$c = -9 - 3 + 6k$$

$$\text{Ans} \quad P(A) = \frac{5}{6} \quad P(A') = 1 - \frac{5}{6} = \frac{1}{6}$$

$$P(A) = 1 - \frac{5^6}{6^6} \approx 0.333333333$$

~~R(B)~~ =

$$P(B) = \frac{5^{12}}{6^{12}} + \frac{\binom{12}{1} \cdot 5^{11}}{6^{12}} = \frac{5^{12}}{6^{12}} + \frac{12 \cdot 5^{11}}{6^{12}}$$

$$P(B) = 1 - \left(\frac{\cancel{42} 5^{12}}{6^{12}} + \frac{12 \cdot 5^{11}}{6^{12}} \right) =$$

≈ 0,38

$$(4) = \frac{5^{18}}{6^{18}} + \binom{18}{1} \cdot \frac{5^{17}}{6^{18}} + \binom{18}{2} \cdot \frac{5^{16}}{6^{18}} = \frac{5^{18}}{6^{18}} + 18 \frac{5^{17}}{6^{18}} +$$

$$+153 \frac{5^{16}}{6^{18}} \approx 0,0376 + 0,1352 + 0,2299$$

$$= 0,9026$$

$$P(C) = 1 - 0.502C \equiv P_{50\%}$$

$$\textcircled{11} \quad \bar{\Omega} = 10^6$$

A - WYSŁYŚĆ WYSIADĄ NA 10

~~A - WYSŁYŚĆ WYSIADĄ NA 10~~

~~A - WYSŁYŚĆ WYSIADĄ NA 10~~

$$P(A) = \frac{9^6}{10^6}$$

$$P(A) = 1 - \frac{9^6}{10^6} \approx 0.4686$$

$$P(B) = \frac{10}{10^6}$$

$$P(A) = \frac{10}{10^6} = \frac{1}{10^5}$$

$$P(A) = \frac{10}{10^6} = 10 \cdot \frac{10^{-6}}{10^6}$$

$$P(A) = \frac{\binom{10}{2}}{10^6} = \frac{10 \cdot 9}{10^6} :$$

$$\textcircled{12} \quad \Delta = 10!$$

A - DUT LEVY I PRAVY KAZDÝ

~~10!~~

$$A = 2^5 \cdot (5!)^2$$

$$P(A) = \cancel{\frac{2^5 \cdot (5!)^2}{10!}}$$

B - PARÉ

$$B = 2^5 \cdot 5!$$

$$P(B) = \frac{2^5 \cdot 5!}{10!}$$

~~BEC~~

C - SVOJKÉ PŘÍZ

$$\cancel{C} \quad C = 5^2$$

$$P(C) = \frac{5^2}{10!}$$

$$\textcircled{B} \quad \bar{\Delta} = 10! \quad A - \text{POMIĘDZY} \quad 2 \times 3 \quad \text{SŁ} \leftarrow \text{CYPRE}$$

~~2~~
 2 ~~xx~~ ~~xx~~ 3 ~~xx~~ ~~xx~~ ~~x~~
~~x~~ 2 ~~xx~~ ~~xx~~ 3 ~~xx~~ ~~x~~
 x ~~2~~ ~~xx~~ ~~xx~~ 3 ~~x~~ ~~x~~
 x ~~xx~~ 2 ~~xx~~ ~~x~~ 3 ~~x~~
 x ~~xx~~ ~~x~~ 2 ~~xx~~ ~~x~~ 3

$$A = 5 \cdot \cancel{2!} \cdot 2! \cdot 8!$$

$$P(A) = \frac{5 \cdot 2! \cdot 8!}{10!}$$

B - 0, 1, 2 STOSUA KOTO SIĘBIE

~~012~~
~~012~~ ~~xx~~ ~~xx~~ ~~xx~~ ~~x~~ ~~x~~
~~x~~ ~~012~~ ~~xx~~ ~~xx~~ ~~xx~~ ~~x~~ ~~x~~
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 x ~~xx~~ ~~x~~ ~~x~~ ~~012~~ ~~x~~
 x ~~xx~~ ~~x~~ ~~x~~ ~~x~~ ~~012~~

$$B = 8 \cdot 3! \cdot 4!$$

$$P(B) = \frac{\cancel{3!} \cdot \cancel{8} \cdot 8 \cdot 3! \cdot 7!}{10!}$$

15) $\bar{x} = 10!$ A - PARZYSTĘ NA MIEJSCU PARZYSTY.

$$+ 2 + 4 \dots 18 +$$

$$A = 9! \cdot 10!$$

$$P(A) = \frac{9! \cdot 10!}{19!}$$

(15) 1, 1, 1, 1, M, P, P, S, S, S, S

4-1 A - MISSISSIPPI

$$1 - m \stackrel{=}{\rightarrow} A = 1$$

2 - P

4-5

$$\bar{D} = \frac{n!}{4! \cdot 1 \cdot 2! \cdot 5!}$$

$$P(A) = \frac{1}{m!} \underbrace{\frac{1}{n! \cdot 1 \cdot 2 \cdots n}}$$

~~16~~ - 8!

A - ~~2ADNA~~ ~~021EC~~ ~~VIE~~ ~~5701~~ ~~6060~~ ~~SLIBB~~

$$A = \begin{pmatrix} 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 & 1 \end{pmatrix} \cdot \begin{pmatrix} 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 & 1 \end{pmatrix}^T$$

$$16) \underline{\underline{D}} = 8!$$

*) A - IĄONE Dwie ORGANOZYNKI NIE STOJA OBOK SIĘ SIEBIE

D

A

D → ORGANIZYUNKI

↑

C → CHŁOPIEC

DCDCDCDC
COCDCDCD + PERMUTACJE

$$\textcircled{1} \quad A = \cancel{A} \cdot 4! \cdot 4!$$

$$P(A) = \frac{2 \cdot 4! \cdot 4!}{8!}$$

~~D~~

$$\textcircled{2) } \quad \underline{\underline{D}} = 7!$$

B - IĄONE Dwie ORGANOZYNKI NIE STOJĄ OBOK SIĘ SIEBIE

$$\textcircled{3) } \quad B = 4! \cdot 4!$$

$$P(B) = \frac{4! \cdot 4!}{7!}$$

$$\textcircled{17} \quad \bar{\Delta} = 99$$

A - PODZIELNA PRZ 2

B - PODzielna PRZ 3

$$\bar{A} = 49$$

$$\bar{B} = 33$$

$$\overline{A \cap B} = 16$$

$$P(A) = \frac{49 + 33 - 16}{99}$$

\textcircled{18}



$$\bar{\Delta} = 4!$$

A - CO NADNIĘS 1 LIST DOBRY

B_i - LIST "i" DOBRY

$$A = B_1 \cup B_2 \cup B_3 \cup B_4$$

$$P(A) = \sum_{i=1}^n P(B_i) - \sum_{1 \leq i < j \leq 4} P(B_i \cap B_j) + \sum_{1 \leq i < j < k \leq 4} P(B_i \cap B_j \cap B_k) - P(B_1 \cap B_2 \cap B_3 \cap B_4)$$

$$P(B_i) = \frac{3!}{4!} \rightarrow i = 1, 2, 3, 4$$

$$P(B_i \cap B_j) = \frac{2!}{4!} \rightarrow i \neq j \Rightarrow i, j = 1, 2, 3, 4$$

$$P(B_i \cap B_j \cap B_k) = \frac{1}{4!} \rightarrow i \neq j \neq k, i, j, k = 1, 2, 3, 4$$

$$P(B_1 \cap B_2 \cap B_3 \cap B_4) = \frac{1}{4!}$$

$$P(A) = 4 \cdot \frac{3!}{4!} - \binom{4}{2} \frac{2!}{4!} + \binom{4}{3} \frac{1}{4!} - \frac{1}{4!} =$$

~

$$P(A) = P(B_1 \cup B_2 \cup \dots \cup B_n) = n \cdot \frac{(n-1)!}{n!} - \binom{n}{2} \frac{(n-2)!}{n!} +$$

$$+ \binom{n}{3} \frac{n-3!}{n!} + \dots + (-1)^{n+1} \frac{1}{n!} = 1 - \frac{1}{2!} + \frac{1}{3!} + \dots + (-1)^{n+1} \frac{1}{n!}$$

$$\textcircled{19} \quad \bar{\lambda} = \cancel{3^{10}}$$

A - TEONA SŁUFLA DŁA PUSTA

A' - TYLKO W DWOICH POŁOSIACH \hookrightarrow TYLKO U TEONIEJ; TYLKO DŁUGA

~~$\bar{\lambda} = \cancel{3^{10}}$~~

$$\bar{\lambda} = 2^{10}$$

~~$P(A) = 1 - \cancel{\frac{2}{3}^{10}} - \cancel{1 - \frac{1}{3^{10}}}$~~

$$P(A) = \binom{3}{1} \cdot \frac{2^{10}}{3^{10}} - 3 \frac{1}{3^{10}}$$

~~$\cancel{2^{10} - 3^{10}}$~~

$$\textcircled{P} \quad \Omega = \{\underset{\omega_1}{\underset{\parallel}{O}}, \underset{\omega_2}{\underset{\parallel}{RO}}, \underset{\omega_3}{\underset{\parallel}{RRO}}, \underset{\omega_4}{\underset{\parallel}{RRRO}}, \dots\}$$

$$\omega_i = \underbrace{R \dots R}_{i-1} O \rightarrow i = 1, 2, \dots$$

$$P(A) = \sum_{i: \omega_i \in A} P(\{\omega_i\})$$

$$A = \{ \underset{\omega_3}{\underset{\parallel}{RRO}} \} - \text{DOKŁADNIĘ 3 RZUTY}$$

$$P(A) = P(\{\omega_3\}) = \left(\frac{1}{2}\right)^3 = \frac{1}{8}$$

$$B = \{ \underset{\omega_4}{\underset{\parallel}{RRR O}}, \underset{\omega_5}{\underset{\parallel}{RERR O}}, \dots \} \leftarrow \text{UJĘCIE } n, i \text{ 3}$$

$$P(B) = P(\{\omega_4\}) + P(\{\omega_5\}) + \dots$$

$$P(\{\omega_1\}) = P(\{O\}) = \frac{1}{2}$$

$$P(\{\omega_2\}) = P(\{RO\}) = \frac{1}{4} = \left(\frac{1}{2}\right)^2$$

$$P(\{\omega_3\}) = P(\{RRO\}) = \frac{1}{8} = \left(\frac{1}{2}\right)^3$$

$$P(\{\omega_k\}) = \left(\frac{1}{2}\right)^k \rightarrow k = 1, 2, 3$$

$$\textcircled{20} \quad B' = \{\omega_1; \omega_2; \omega_3\}$$

$$P(B) = 1 - P(B') =$$

$$= 1 - \frac{1}{2} - \frac{1}{4} - \frac{1}{8} = \textcircled{1} 125$$

$C \rightarrow$ WYKONANIE PRZESTRZENI UOGÓŁ

$$C = \{\omega_2; \omega_4; \dots; \omega_{2n}\}$$

$$P(C) = P(\{\omega_2\}) + P(\{\omega_4\}) + \dots + P(\{\omega_{2n}\}) =$$

$$= \sum_{n=1}^{\infty} P(\{\omega_{2n}\}) = \sum_{n=1}^{\infty} \left(\frac{1}{2}\right)^{2n} = \sum_{n=1}^{\infty} \left(\frac{1}{4}\right)^n =$$

$$= \frac{\frac{1}{4}}{1 - \frac{1}{4}} = \frac{\frac{1}{4}}{\frac{3}{4}} = \frac{1}{4} \cdot \frac{4}{3} = \frac{1}{3}$$

$$\textcircled{21} \quad D = \{1, 2, 3, 4, 5, 6, 11, 12, 13, \dots\}$$

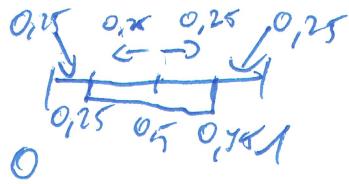
" 1 4 4 1 1 1
 ω₇ ω₁ ω₁ ω₁ ω₁ ω₂

~~$$D = \{1, 2, 3, 4, 5\}$$~~

~~$$D = \{1, 2, 3, 4, 5\}$$~~

" 1 1 1
 ω₂ ω₂ ω₂

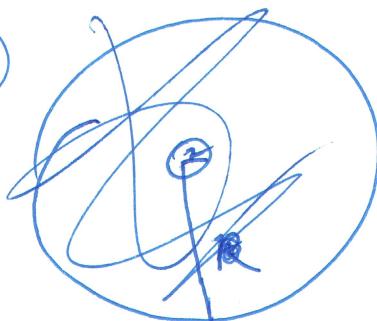
(22)



$$0,25 + 0,25 = 0,5$$

$$\rho = \frac{1}{2}$$

(23)



$$\pi = r=1$$

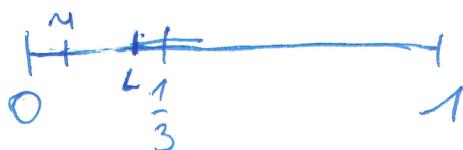
~~$$A = \pi r^2 = 1$$~~

~~$$D = \pi r^2$$~~

~~$$A = \pi r^2$$~~

~~$$RAC \quad P(A) = \frac{\pi r^2}{\pi R^2} = \frac{r^2}{R^2}$$~~

(24)



(25)



$$A = \{E\}$$

~~A = NIS U FIS~~

~~$$1^2 + \pi(0,5)^2 = r^2 + 0,25\pi$$~~

$$P(A) = 1 - 1 + 0,25\pi$$

$$P(A) = 0,25\pi$$

~~(27)~~
$$D = 3$$

$$A = 2$$

$$P(A) = \frac{2}{3}$$

~~(28)~~
$$P(A) = 0,7$$

~~$$P(A \cap B) = 0,9$$~~

$$P(A') = 0,3$$

$$P(C) = 0,3 \cdot 0,9 = 0,27$$

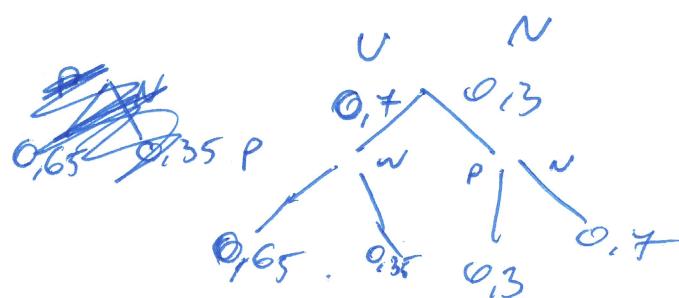
~~(29)~~
$$P(A) = 0,5 \quad D \rightarrow 2 \text{ JEDEN}$$

$$P(B) = 0,001$$

$$P(C) = 0,8$$

$$P(D) = 0,5 \cdot 0,001 \cdot 0,8 = 0,0004$$

(30)



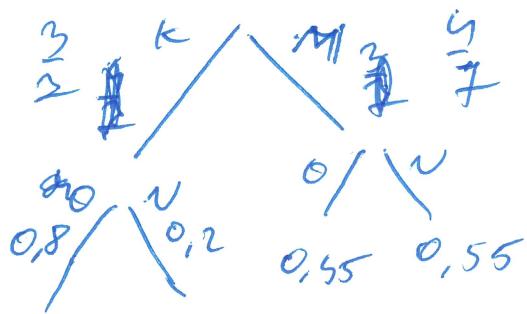
$$P = 0,65 \cdot 0,7 + 0,3 \cdot 0,3$$

$$P = 0,455 + 0,09 = 0,545$$

$$31) -2 = 2000 + 1500 = 3500$$

$$P(K) = \frac{2000}{3500} = \frac{4}{7} \quad \text{D} \rightarrow 24\% 12,8\%$$

$$P(M) = \frac{1500}{3500} = \frac{3}{7}$$



$$P = \frac{4}{7} \cdot 0,8 + \frac{3}{7} \cdot 0,55 =$$

$$= 0,6$$

K - JEST NA KARTE

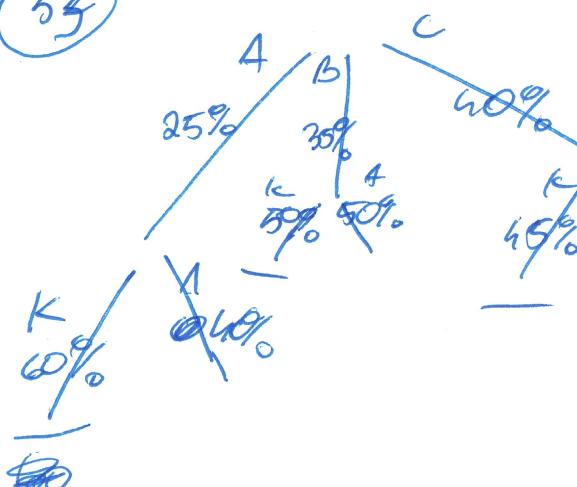
A - SIEĆ A

B - - a - B

C - - i - C

$$PCA = 0,25$$

$$P(K) = P(K|A)PCA + P(K|B)PCB + P(K|C)PCC =$$



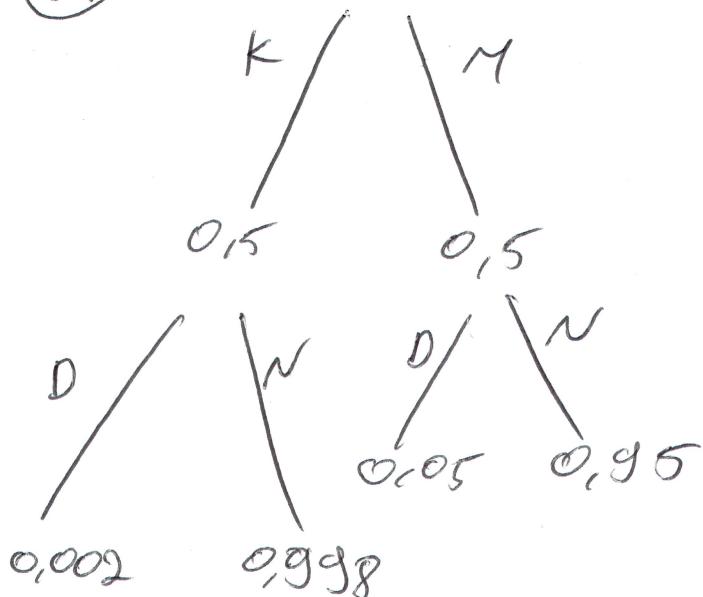
~~$$D = 0,6 \cdot 0,25 + 0,5 \cdot 0,35 + 0,4 \cdot 0,6 = 0,505$$~~

~~$$= 0,45 + 0,15 + 0,18 = 0,78$$~~

$$= 0,6 \cdot 0,25 + 0,5 \cdot 0,35 + 0,4 \cdot 0,6 = 0,505$$

$$P(A|K) = \frac{P(K|A)P(A)}{P(K)} = \frac{0,6 \cdot 0,25}{0,505} \approx 0,295$$

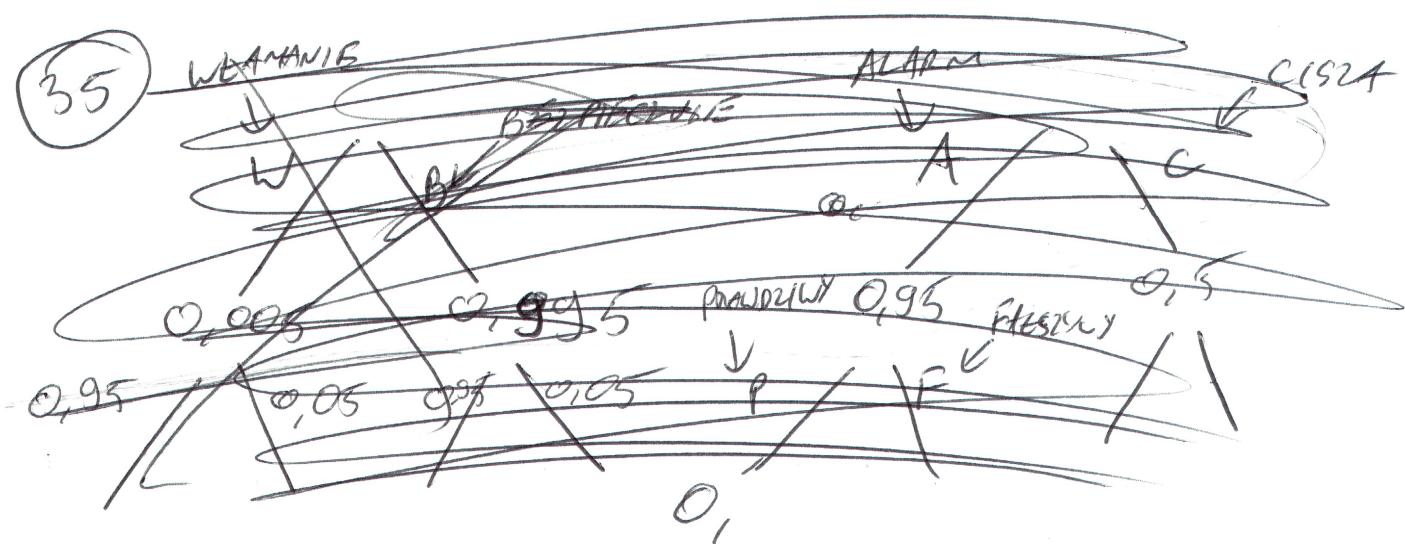
34



$$\begin{aligned}
 P(D) &= P(D|K) \cdot P(K) + \\
 &\quad P(D|M) \cdot P(M) = \\
 &= 0,002 \cdot 0,5 + 0,05 \cdot 0,5 = \\
 &= 0,001 + 0,025 = \\
 &= 0,026
 \end{aligned}$$

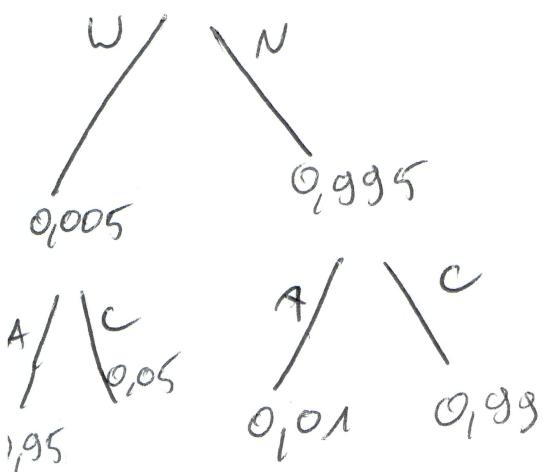
$$P(M|D) = \frac{P(D|M) \cdot P(M)}{P(D)} = \frac{0,025}{\cancel{0,001}} \approx \cancel{0,025} \approx 0,961$$

35



35

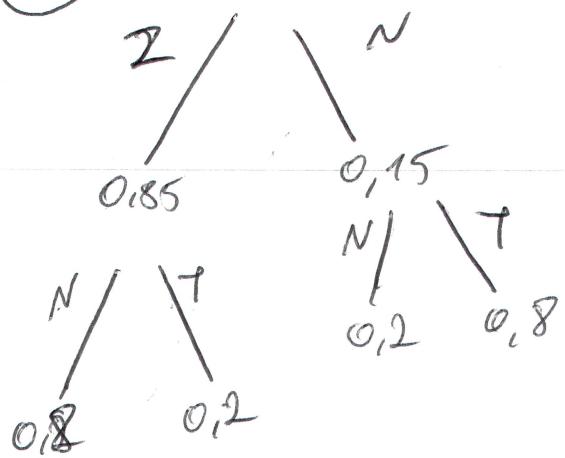
$$P(W|A) = ?$$



$$\begin{aligned} P(A) &= P(A|W) \cdot P(W) + P(A|N) \cdot P(N) = \\ &= 0,95 \cdot 0,005 + 0,01 \cdot 0,995 = \\ &= 0,00475 + 0,00995 = \\ &= \cancel{0,0575} \quad 0,0147 \end{aligned}$$

$$P(W|A) = \frac{P(A|W)P(W)}{P(A)} = \frac{\frac{0,00475}{\cancel{0,0575}}}{0,0147} \approx 0,32$$

(36)

 $P(N|T)$ 

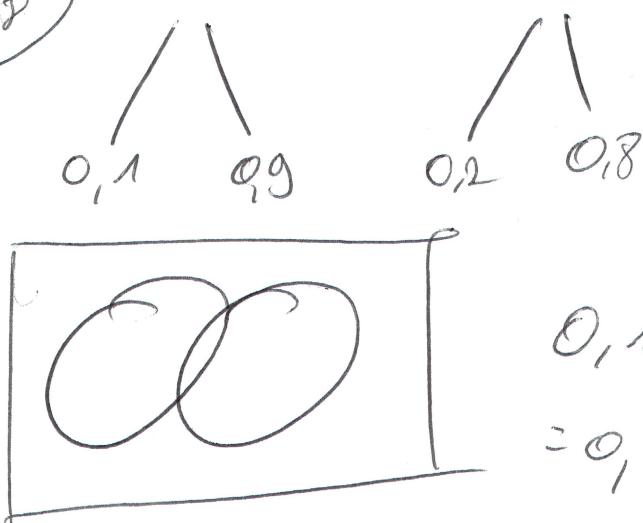
$$P(T) = 0,8 \cdot 0,15 + 0,2 \cdot 0,85 = \\ = 0,12 + 0,17 = 0,29$$

$$P(N|T) = \frac{P(T|N) P(N)}{P(T)} =$$

$$= \frac{0,8 \cdot 0,15}{0,29} = \frac{0,12}{0,29} \approx 0,41$$

~~(37)~~ ~~Skizze~~

(38)



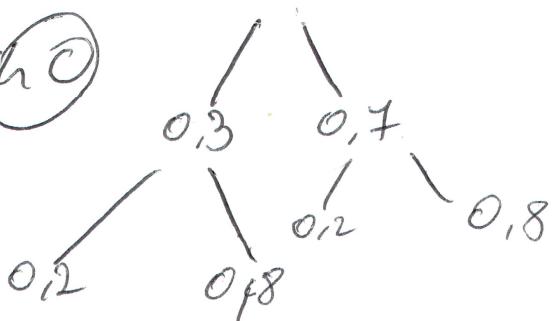
$$0,1 + 0,2 - 0,1 \cdot 0,2 = \\ = 0,3 - 0,02 = 0,28$$

(39)

$$3 \cdot \frac{1}{3} - \binom{3}{2} \frac{1}{3} \cdot \frac{1}{3} + \frac{1}{3} \cdot \frac{1}{3} \cdot \frac{1}{3} = \frac{7}{9}$$

(40)

$$0,7 \cdot 0,8 = 0,56$$



(4)

A_i - działa $\rightarrow i = 1, 2$

$A_1 \cup A_2 \rightarrow$ niezależne

$$P(A_1) = P(A_2) = 0,9 \quad \cancel{P(A'_1) = 0,1}$$

$$P(A'_1 \cap A'_2) = ? \quad P(A'_2) = 0,1$$

$$P(A'_1 \cap A'_2) = 0,1 \cdot 0,1 = 0,01$$

(5)

$A_i \rightarrow$ w i zdaniach wypada określona litera
 $i = 1, 2, 3$

$$\Omega = \{ \text{OOO}, \text{OOR}, \text{ORO}, \text{ROO}, \text{RRO}, \text{RRR}, \text{QRR}, \text{RQR}, \text{ORR} \}$$

$$A_1 = \{ \text{ORR}, \text{OOO}, \text{ORO}, \text{OOR} \}$$

$$A_2 = \{ \text{OOO}, \text{ROR}, \text{OOR}, \text{ROO} \}$$

$$A_3 = \{ \text{OOO}, \text{RRO}, \text{ORO}, \text{ROR} \}$$

$$\frac{1}{8} P(A_1 \cap A_2) = P(A_1) \cancel{P(A_2)} = \frac{1}{4}$$

$$\frac{1}{4} = \frac{2}{8} = P(A_1 \cap A_3) = P(A_1) P(A_3) = \frac{1}{4}$$

$$\frac{1}{4} = \frac{2}{8} = P(A_2 \cap A_3) = P(A_2) P(A_3) = \frac{1}{4}$$

$$\frac{1}{8} = P(A_1 \cap A_2 \cap A_3) = P(A_1)P(A_2)P(A_3) = \frac{1}{8}$$

$$P(A_1) = P(A_2) = P(A_3) = \frac{1}{8} = \frac{1}{2}$$

43)

$$\Omega = \{1, 2, 3, 4\}$$

$$C = \frac{1}{3}$$

$$B = \frac{1}{3}$$

$$2 = 4 \frac{1}{3}$$

~~P(C)~~

$$\frac{1}{4} = P(C \cap B) \stackrel{?}{=} P(C)P(B) = \frac{1}{3} \cdot \frac{1}{3} = \frac{1}{9} = 0,111$$

~~P(B)~~

NIE SA NIEZALEŻNIE

$$P(C) = \frac{\frac{1}{3}}{4} = 0,33$$

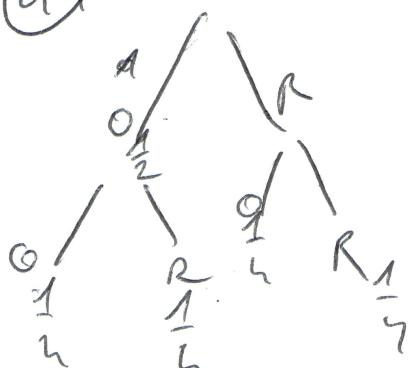
$$P(B) = 0,33$$

$$P(2) = 0,33$$

44)

$$\frac{1}{8} : A = \left\{ \begin{array}{l} \text{xx}, \text{xy} \\ \text{ox}, \text{oy} \end{array} \right\}$$

xx; xo; ox; ro
oo; xo; or; rr



$$B = \left\{ \begin{array}{l} \text{xx}, \text{xy} \\ \text{ox}, \text{oy} \end{array} \right\}$$

$$C = \left\{ \begin{array}{l} \text{xx}, \text{ro} \\ \text{oy}, \text{rr} \end{array} \right\}$$

$$D = P(A \cap B) \stackrel{?}{=} P(A)P(B) = \frac{1}{8} \cdot \frac{1}{8} = \frac{1}{64}$$

↑

NIE SA NIEZALEŻNIE
PONIĘWIĘ JESTEŚ NIE
WYPOŁCZ W PIERWSZEJ TURZE OR I OO
WYPOŁCZ W PIERWSZEJ TURZE OR I OO

$$\frac{1}{4} - \frac{2}{8} = P(A_1 \cap A_2) = P(A_1) P(A_2) = \frac{1}{4}$$

$$\frac{1}{4} = \frac{2}{8} = P(A_1 \cap A_3) = P(A_1) P(A_3) = \frac{1}{4}$$

$$\frac{1}{4} = \frac{2}{8} = P(A_2 \cap A_3) = P(A_2) P(A_3) = \frac{1}{4}$$

$$\frac{1}{8} = P(A_1 \cap A_2 \cap A_3) = P(A_1) P(A_2) P(A_3) = \frac{1}{8}$$

$$P(A_1) = P(A_2) = P(A_3) = \frac{1}{8} = \frac{1}{2}$$

Zatem $A_1, A_2 \cap A_3$ są niezależne

(45)



$$S = A \cap B \cap C$$

$$\begin{aligned} P(S) &= P(A \cap B \cap C) = \\ &= P(A) P(B) P(C) \\ &= p^3 = 0,9^3 = 0,729 \end{aligned}$$

A - "obiekty powstające A"

B - " " = B

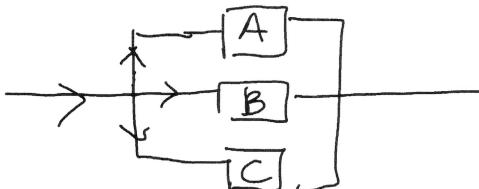
C - " " = C

$$P(A) = P(B) = P(C) = p = 0,9$$

A, B, C - niezależne

S - "powstanie sygnału
po ujęciu po
powielaczówka"

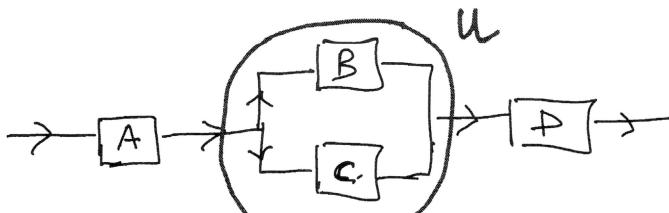
(b)



$$S = A \cup B \cup C$$

$$\begin{aligned} P(S) &= P(A \cup B \cup C) = 1 - P(A^c \cap B^c \cap C^c) = \\ &= 1 - \underbrace{P(A)}_{1-P(A)} \underbrace{P(B)}_{1-P(B)} \underbrace{P(C)}_{1-P(C)} \\ &= 1 - (1-p)(1-p)(1-p) = 1 - (1-p)^3 \\ &= 1 - 0,1^3 = 0,989 \end{aligned}$$

(c)

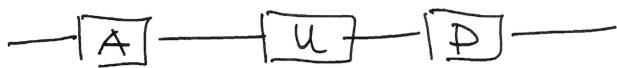


A, B, C, D - niezależne

$$P(A) = P(B) =$$

$$- P(C) = P(D) =$$

$$= n - n^2$$

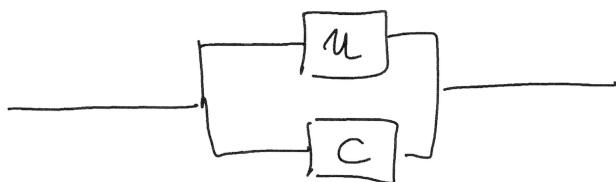
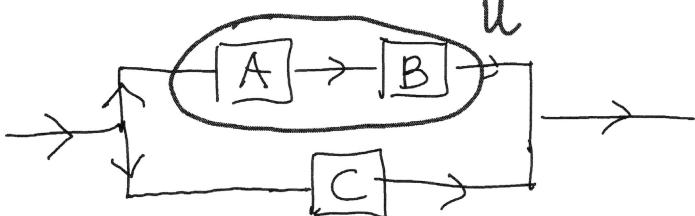


$$\begin{aligned} P(S) &= P(A \cap u \cap D) = \\ &= \underbrace{P(A)}_P \underbrace{P(u)}_P \underbrace{P(D)}_P \end{aligned}$$

$$\begin{aligned} P(u) &= P(B \cup C) = 1 - P(B^c \cap C^c) = \\ &= 1 - \underbrace{P(B^c)}_{1-p} \underbrace{P(C^c)}_{1-p} \\ &= 1 - (1-p)^2 \end{aligned}$$

$$\begin{aligned} P(S) &= p^2 [1 - (1-p)^2] = 0,8^2 [1 - 0,1^2] = \\ &= 0,8 \cdot 0,99 = 0,8019 \end{aligned}$$

(d)



$$\begin{aligned} P(S) &= P(u \cup C) = 1 - P(u^c \cap C^c) = \\ &= 1 - P(u^c) P(C^c) = \\ &= 1 - [1 - P(u)] (1-p) \end{aligned}$$

$$P(u) = P(A \cap B) = P(A) P(B) = p^2$$

$$P(S) = 1 - (1-p^2)(1-p) =$$

$$= 1 - 0,19 \cdot 0,1 = 0,881$$

Koloekwium 1 → 7/11/2020

45 min → 2 potome rafsc'

Inspeera ↔ 14¹⁵ - 15

3 krotnie zedawie ~ 30 min
+ 10 min

Ⓐ --- → = =