AUTHOR, OLDDEGREE

Evaluation of a Genetic Algorithm on generating critical Scenarios in a Traffic Simulation

Master's Thesis

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Dr. Some Body

Institute for Softwaretechnology
Head: Univ.-Prof. Dipl-Ing. Dr.techn. Some One

Graz, November 2013

Affidavit

I declare that I have authored this thesis independently, that I have not used other than the declared sources/resources, and that I have explicitly indicated all material which has been quoted either literally or by content from the sources used. The text document uploaded to TUGRAZonline is identical to the present master's thesis.

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Abstract

This is a placeholder for the abstract. It summarizes the whole thesis to give a very short overview. Usually, this the abstract is written when the whole thesis text is finished.

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1 Introduction

This Thesis will use a Genetic Algorithm in order to generate critical Driving Scenarios for testing ADAS/AD Functionality in vehicles. While generating these scenarios is the objective, the main task of the thesis will evolve around the implementation of the Genetic Algorithm as well as the Optimization of its Hyperparameter.

1.1 Research Questions

1.1.1 Research Question 1

Is a Genetic Algorithm suitable for generating critical driving scenarios compared to a random generation?

In this thesis,

1.1.2 Research Question 2

Can hypertuning improve the performance of a Genetic Algorithm?

1.1.3 Research Question 3

Can a hypertuned Genetic Algorithm generalize on different start scenarios?

1.1.4 Research Question 4

Is the usage of a Behavior Tree on the Ego vehicle improving the criticaality of resulting scenarios?

1.1.5 Research Question 5

Can rules help to improve the performance of a genetic algorithm?

1.2 Shortcomings

This Master Thesis started with the developement of the Traffic Manger and thus progress was closely linked. Without a working simulations, no genetic alogirthmis could be tested. Due to time and performance constraints, it is not possible to test a full driving stack like autoware, as well as other professional ADAS/AD functions. In this Thesis, internal functions like Time-To-Collision and Emergency Braking will be optimized. The learned information on e.g. optimal hyperparameter settings can then be applied in further steps to test these functions. This will however not be tackled by this thesis.

Performance is also a problem and will lead to many shortcuts that need to be taken. There is a hughe number of possible compations of hyperparamter, so only a handful can be tested. In further chapers, these shortcuts will be explained and their relevancy will be dicussed.

2 Foundations

2.1 Genetic Algorithm

Genetic Algorithms are a popular search algorithm that utilizes the principle of Darwin. They have been used successfully in various areas. Some of their strengths are .... However we will also look at shortcomings, which mainly evolve around performance. We will have a look at its History and then discussing the most important paramters.

> **Define a vocabulary**

The task of the Genetic Algorithm is to search for sequences of actions that will result in the most interesting Scenarios according to its cost function.

> **Usage of GA**

2.1.1 History

The GA was invented by....

2.1.2 Different Hyperparameter

Hyperparamter have a huge influence on the performance of a Genetic Algorihm. They have an impact on the "convergin" ... It has been shown, that there is no universal hyperparamter set and that it needs to be optimized on a per "problem" basis.

Num of generations

The Number of Generation defines the duration of a GA. As long as the algorihtm has not converged, ...? For my testing, using a generation size of 40 was almost always sufficient, and will thus mostly be used.

Pop Size

Pop size will set the number of Individuals of a GA per Generation. The higher the pop size, the bigger the less change of premature converging. It will however also lead to a longer convergin time.

Selection

Selection defines how which individuals are allowed to mate and move into the next generation.

pros and cons of roulette vs Tournament

tournament was chosen to be used for this works because of this paper (and also because of pros and cons list)

cite paper

Other ideas are evolve around having a flexible selection system debending on fitness

Crossover

Discuss all used crossover methods

Crossover is the mating process.

Mutation

Discuss individual mutation

Mutation is responsible for introducing new information into the gene pool.

Discuss all used mutation methods

4

Other

More to come....

2.2 Behavior Tree

A behavior tree is a decision tree.

insert a good introduction to BT

2.2.1 Usage for GA

Due to the fact, , that there is no full stack available for the EGO vehicle, a solution had to be found. In order to have the Genetic Algorithm controll only NPCs and not the EGO vehicle itselve, a behaviour tree is used. The behaviour tree is used to controll the EGO vehicle over the action interface provided by the Traffic Manager. This is the same as the Genetic Algorithm is doing.

insert ref to discussion

The behaviour tree will define which direction the EGO should take at junctions and it will realistically dodge obstacles intoduced by the Genetic Algorithm. The main goal of the BT is to make the EGO vehicle behave in a realistic way.

In a further chapter it will be dicussed if a GA with controll of the EGO (i.e. no BT will be used) lead to better cost.

While the aim of the GA is to find the most optimal solution, considering the vastness of the hyperspace, this is unlikely. Rather, we want to find the "best" local minimas. Considering the contex of Automotive testing, it is not so much of importance to find "the best fail of the ADAS/AD System", rather its important to find "all" fails.

2.3 Traffic Manager

The Genetic Algorithm will control the simulation of a custom developed Traffic Manager. This Traffic Manager was developed closely to fit the needs of the Genetic Algorithm. It, however is not part of this Thesis and will thus will only get a brief introduction. In general, it will simulate traffic starting from a predefined scenarios where the positions and types of Vehicles and Pedestrians are given (i.e. actors). It also allows for an Interface for aplying actions on all actors in the simulation, which will be discussed in section 2.3.1.

A simulation consists of multiple NPCs and exactly one EGO vehicle. While the NPCs are only controlled by the Traffic Manager (and dadurch also by its action interface), the ego vehicle can be either partly or even completly controlled by an ADAS/AD Function. This function can then be tested inside the simulation on errors.

2.3.1 Action Interface

To interface with the Traffic Manager, actions have to be used. An action will request a certain behaviour from an actor. If no action is set, the actor will behave in a normal manner inside the simulation. An action can be set to at any timestep (for this thesis, the simulation is running with 100 Hz) for any actor. Pedestrians and vehicles however have different actions.

The following list are now all actions provided by the traffic manager that were available for the genetic algorithm at the time of this master thesis.

- JunctionSelection
    - Parameters: Vehicle ID: int, Junction_selection_angle: float
    - Angle is set in radiant. Default value is 0. Vehicles will chose which direction to take at a junction based on this angle.

- LaneChange
    - Parameters: Vehicle ID: int, ...
    - Initiates a LaneChange based on its given parameters.

- AbortLaneChange

  - Parameters: Vehicle ID: int, ...
  - If a LaneChange is currently happening, it will get aborted.

- ModifyTargetVelocity

  - Parameters: Vehicle ID: int, ...
  - Modifies the interal Target Velocity of the Traffic Manager by a percentage. If it is for example 0, the vehicle will stop.

- TurnHeading

  - Parameters: Pedestrian ID: int, ...
  - The pedestrian will turn 180 degrees and walk in the oposite direction

- CrossRoad

  - Parameters: Pedestrian ID: int, ...
  - The pedestrian will cross the road immediately.

- CrossAtCrosswalk

  - Parameters: Pedestrian ID: int, ...
  - The pedestrian will cross the road at the next crosswalk.

2.3.2 Graphics

During the simulation, usually no graphics engine is used in order to save performance. In order to visualize the results, two options can be chosen. The more lightweight Esmini, as well as Carla, which is using Unreal Engine to render realistic graphics.

3 Implementation

This chapter will explain

All these actions are accessed by the Genetic Algorithm to maximize a given Cost Function.

3.1 Map and Starting Scenario

The map is Town10 from Carla. It was chosen, because 1. its roads are self contained, 2. its not too big, yet still complex and 3. its supported by Carla and thus visualization looks better.

The Starting Scenario defines the number and type of all actors as well as their position. It needs to be created manually. Changing the scenario will have a great impact on the Genetic Algorithms performance. For time and complexity reasons, it was thus decided to first stick with one scenario and do all hyperparameter testing there. And finally test the performance for a handfull different scenarios.

3.2 Genetic Algorithm

For implementing the Genetic Algorithm, DEAP was chosen. It is a popular tool for accademia .

explain why pygad was NOT chosen

cite

cite 3 examples

dejong talks about dynamic param and why its not good

3.2.1 Encoding

When implementing a Genetic Algorithm, it is necessary to implement a Encoding that fits to the problem.

cite what makes an encoding good: eg. simplicity,...

Gene

Genes are the building blocks of a GA.

Chromosome

Each Individual has 1 chomosome which consits of a list of genes. Starting out, 2 different encodings came to mind, in both cases, the genes position in the chromosome defined the time an action is set.

generate images

Encoding 1 has the idea that each gene stands for 1 time step. Because multiple actors exist in the simulation, a gene thus needs to be a list of actions. This list always has the length of the number of all actors. This means that crossover can only move all actions of a timestep at once, modifing between actions of the same timestep can only be done using mutation.

Encoding 2 has not only the time step encoded in the position, also the actor ID is encoded. This makes a chromosome now much longer than in the previous encoding, whith the eqatuion beeing: number of timesteps * number of actors. Now crossover has more possibilities.

In the chapter 5 these two chromosome types will be compared.

3.2.2 Rules

Often, actions are not possible if specific requirements are not met. The obvious example is that it is not possible to perform the action Abort-LaneChange if there is no current LaneChange happening. LaneChange during a LaneChange is not possible as well. Also Pedestrians can not CrossRoad shortly in a Row. The hypothesis is that implementing Rules that

dont allow for these behaviours will reduce the searchspace and will thus make GA converge quicker.

be carefull, lanechange after lanechange or crossroad after crossroad might be possible if prev did not happen. Good to explain

3.2.3 Cost Function

Cost function is a bit difficult, as we are only using interal values. No ADAS/AD system is tested and we thus have to work with what we got. Currently 3 different cost functions are tested

Oracles

While not implemented here, Oracles are needed in order to get a list of good scenarios.

3.3 Behavior Tree

The Behavior Tree will controll the ego vehicle

setJunctionSelection(Step)

o → ->

?
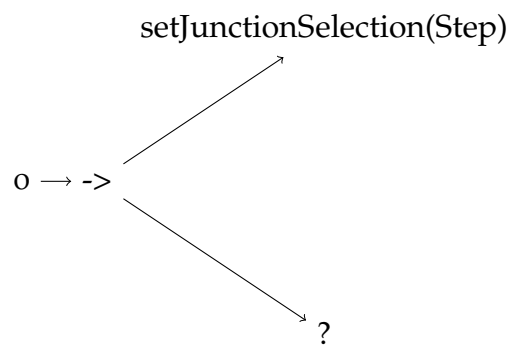
Figure 3.1: Used Behaviour Tree

4 Hyperparameter Tuning

In this chapter, we will incrementally move to an optimized Genetic Algorithm

4.1 No Free Lunch Theorem

No Free Lunch Theorem: The best hyperparameter settings of a Genetic Algorithm are very problem specific. K. De Jong, 2007, Dao, Abhary, and Marian, 2016 _____ More ref

4.2 Start Scenario

4.3 Population

The number of Individuals is of high importance to a genetic algorithm, as has been explained in section 2.1. Especially considering the limed processing resources available, a suitable population size has to be found. On one hand, a population that is too low might result in less diverse runs of the genetic algorithm, on the other hand, if population is too high, the simulations will become too costly. Considering these points, the first step of the hyper parameter tuning was to find a suitable population size. In the next chapter 4.4, we will aim to improve the hyperparamter using a more robust approach.

In order to test for the best population size, the other hyperparameters have to be assumed using an educated guess. While reviewing the literature,

trends of general settings for genetic algorithms can be found. However Mills, Filliben, and Haines, 2015 highlight the inconsistencies between findings, stating to have "uncovered conflicting opinions and evidence regarding key GA control parameters".

However Grefenstette, 1986 suggests, that "while it is possible to optimize GA control parameters, very good performance can be obtained with a range of GA control parameter settings." This is also complimented by findings from K. De Jong, 2007: "The key insight from such studies is the robustness of EAs with respect to their parameter settings. Getting "in the ball park" is generally sufficient for good EA performance. Stated another way, the EA parameter "sweet spot" is reasonably large and easy to find [18]. As a consequence most EAs today come with a default set of static parameter values that have been found to be quite robust in practice."

Chosing the right selection method is complicated as well, as discuees by K. De Jong, 2007: "One source of difficulty here is that selection pressure is not as easy to "parameterize" as population size. We have a number of families of selection procedures (e.g, tournament selection, truncation selection, fitness-proportional selection, etc.) to choose from and a considerable body of literature analyzing their differences (see, for example, [19] or [15]), but deciding which family to choose or even which member of a parameterized family is still quite difficult, particularly because of the interacting effects with population size [13]."

Looking at the literature might lead to hyperparameters are used that at least sufficient enough, to get an idea which range for population size is suitable. We will now look at different concrete hyperparameter suggestions from the literature.

4.3.1 Suggested hyperparameter from the literature

In an often cited thesis by K. A. De Jong, 1975, the following parameters have been suggested: GA(50, 0.6, 0.001, 1.0, 7, E) These suggested parameters have been used successfully by various different genetic algorithms Grefenstette, 1986.

Use best values also from : Using genetic algorithms for automating automated lane-keeping system testing

Talk about rules (e.g. 1/n for mut rate...) - look at: Parameter selection in genetic algorithms

14

An extensive study by Mills, Filliben, and Haines, 2015 which that took over "over 60 numerical optimization problems." into consideration found that "the most effective level settings found for each factor: population size = 200, selection method = SUS, elite selection percentage = 8%, reboot proportion = 0.4, number of crossover points = 3, mutation rate = adaptive and precision scaling = 1/2 as fine as specified by the user."

Grefenstette, 1986 claim that GA(30, 0.95, 0.01, 1.0, 1, E) and GA(80, 0.45, 0.01, 0.9, 1, P) produced the best results. They also advised against, a mutation rate of over 0.05, suggesting poor performance. Using a low mutation rate is also suggested by Whitley, 1994 and Jinghui Zhong et al., 2005. On the other hand, Boyabatli and Sabuncuoglu, 2004 state, that "Controversial to existing literature on GA, our computational results reveal that in the case of a dominant set of decision variable the crossover operator does not have a significant impact on the performance measures, whereas high mutation rates are more suitable for GA applications." Other paper also find a relatively high mutation rate useful. Almanee et al., 2021 uses genetic algorithms in a similar domain as this thesis. There, a Population of 50, crossover of 0.8 and mut of 0.2 was used. These used params are the same as the default params from deap (pop = 50 CXPB, MUTPB, NGEN = 0.5, 0.2, 4).

cite
https://deap.readthed

Srinivas and Patnaik, 1994 state, that for a higher population, cross : 0.6, mut: 0.001 and pop: 100 is a good starting point, while a lower population needs higher crossover and mutation rates like this cross: 0.9, mut: 0.01, pop: 30

These next three paper use ANOVA analysis to come a conclusion. Fazal et al., 2005 recommend: Migration direction: Forward Population size: 50 Fitness scaling function: Rank Selection function: Tournament Elite count: 5 Crossover fraction: 0.5 Crossover function: Scattered

Dao, Abhary, and Marian, 2016 suggests these values after anova: Migdirection: forwards pop size: 200 fitness scaling: rank selection: roulette elite count: 1 Crossover prop: 0.7 MutationFunc: Gaussian Crossover FUnc: two point hybrid function: none

Assistant Professor, Amity University, Jaipur, Rajasthan, India et al., 2019 use these values after anova: Direction: Forward Pop: 200 Fitness Scaling

Function: linar Shift selection: Roulette elite count: 10 Crossover: 0.4 Mutation: Constraint Dependent Crossover function: Heuristi Hybrid Function: None

4.3.2 results

This now leads to a difficult decision in choosing the right parameters. Based on the extensive research, we will compare population size of 32, 48, 64 and 96. We will compare the different crossover rates: 0.8 and 0.6. For mutation, 0.01 and 0.2 will be discussed. Further we will use tournament selection with 2 and 4. Each run will be executed 5 times to get rid of randomness and to make the results more robuts. We will run each simulation for 40 Generations.

Comparison of Population Size - mean(standard deviation)					
Settings	Code	32	48	64	96
C: 0.6, M: 0.01, TS: 2	A	3051 (74)	3016 (85)	2851(132)	2871 (57)
C: 0.6, M: 0.01, TS: 4	B	3111 (79)	3021(110)	3079(103)	2937(129)
C: 0.6, M: 0.2, TS: 2	C	3062(128)	3010 (55)	3002 (76)	2831(110)
C: 0.6, M: 0.2, TS: 4	D	3020 (44)	2967 (37)	2891(181)	2850 (90)
C: 0.8, M: 0.01, TS: 2	E	3063(105)	2892(222)	2971(108)	2916(158)
C: 0.8, M: 0.01, TS: 4	F	3052(109)	3049 (96)	3054 (68)	2897(117)
C: 0.8, M: 0.2, TS: 2	G	3099(127)	2940(111)	2959 (96)	2869(131)
C: 0.8, M: 0.2, TS: 4	H	3058 (49)	3005 (84)	2794(173)	2809(105)

Figure 4.1: List Settings per Population Size

In figure 4.3.2, the results per population are plotted. The line is corresponds to the mean, while the bars show the spread (min to max) of all 5 repetitions.
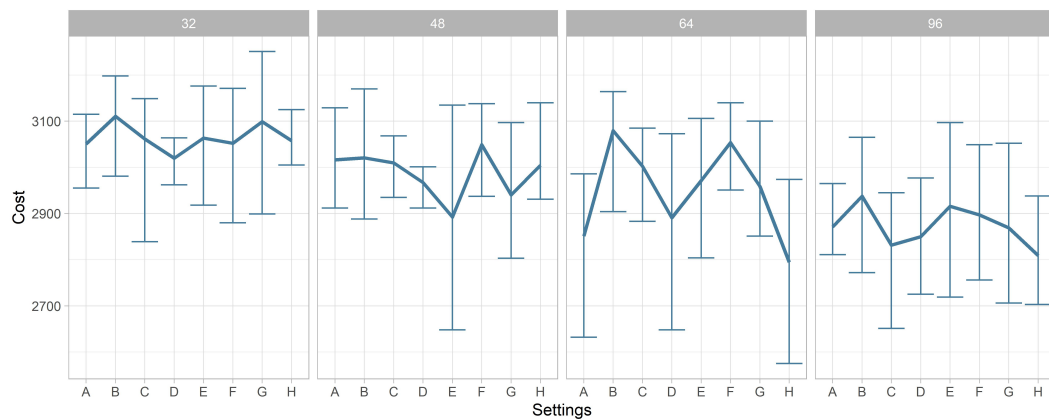
Figure 4.2: mean and error bars per population

A high spread can be seen when looking at small population sizes. Considering these findings, a population size of 96 was chosen. While such a high value will result in a performance impact, it is important to keep the variation low.

4.4 Design of Experiment

"Design of experiments is also called statistically designed experiments. The purpose of the experiment and data analysis is to find the causeand-effect relationship between the output and experimental factors in a process."Yang and El-Haik, 2009

"In a DOE project, each experimental factor will be changed at least once; that is, each factor will have at least two settings."Yang and El-Haik, 2009

"If the range of variable is too small, then we may miss lots of useful information. If the range is too large, then the extreme values might give infeasible experimental runs."Yang and El-Haik, 2009

" DOE data analysis can identify significant and insignificant factors by using analysis of variance. Ranking of relative importance of factor effects and interactions. Analysis of variance (ANOVA) can identify the relative

importance of each factor by giving a numerical score. DOE data analysis can also provide graphical presentations of the mathematical relationship between experimental factors and output, in the form of main-effects charts and interaction charts. "Yang and El-Haik, 2009

In order to tune the hyperparameter of the genetic algorithm, various different strategies can be used. Using automated hyperparamter tuning approaches like "Grid Search", "Bayesian Optimization, "Simmulated Annealing or "Hyperband" might lead to good results with minimal effort (tuning hyperparameter of these search algorithms is still needed), however they require a high number of runs, which is not feasable.

find references

Following the conclusion from the previous section 4.3, a population size of 96 will be used. Executing one run for 30 generations currently takes around 3:50 hours. Although two different workstations were available, the time required to execute the needed number of runs for these automated tests would exceed the available time budged. This is without considering a minimum required number of repetitions to remove randomness in the results.

A different approach called "design of experiment" (DOE), also known as factorial design (Roy, 1990). Each design of experiment has factors, of which each consists of at least two settings, with the actual number of settings being called "levels" (Yang and El-Haik, 2009). Design of experiment needs manual expertise to define which factors are possibly of importance and which settings each factor should have, this is a drawback compared to automatic hyperparameter tuning. Afterwards, main effects and interactions can be calculated to find the best settings per factor. Using ANOVA (Analysis of Variance) it is possible to identify the significance of each main effect and interaction. More details on these analysis tools will be provided in section 4.4.3.

"Most industrial experiments involve two or more experimental factors. In this case, factorial designs are the most frequently used designs. By a factorial design, we mean that all combinations of factor levels will be tested in the experiment."Yang and El-Haik, 2009

In a factorial designs, each possible combination of factor levels needs to be tested. Looking at the proposed factors in table 4.4.1, we would require

1024 runs .

"Techniques such as fractional (or partial) factorial experiments are used to simplify the experiment. Fractional factorial experiments investigate only a fraction of all possible combinations. This approach saves considerable time and money but requires rigorous mathematical treatment, both in the design of the experiment and in the analysis of the results." Roy, 1990

> generated by minitab (or https://datatab.net/st calculator/design-of-experiments)

> Is this really the case? What about combinatorial testing?

4.4.1 Taguchi Design

Various improvements to Design of experiment have been but forward by Dr. Genichi Taguchi, such as reducing the influence of uncontrollable (noise) factors on processes and products and reducing variability. Some of these methods evolve around Signal-to-noise (S/N) analysis and utilizing cost functions to "express predicted improvements from DOE results in terms of expected cost saving" (Roy, 1990). This master thesis will not discuss all of this proposed considerations, for more detail Roy, 1990 as well as Yang and El-Haik, 2009 is highly recommended.

" There are many similarities between "regular" experimental design and Taguchi's experimental design. However, in a Taguchi experiment, only the main effects and two-factor interactions are considered. Higher-order interactions are assumed to be nonexistent. In addition, experimenters are asked to identify which interactions might be significant before conducting the experiment, through their knowledge of the subject matter. "Yang and El-Haik, 2009

This masters thesis will mainly utilizes Taguchis orthogonal arrays (OAs), "which represent the smallest fractional factorials and are used for most common experiment designs." (Roy, 1990). This means, that only a fraction of combinations needs to be tested which drastically improves performance. Each row of these matrices contains the factors of one experiment, while the columns correspond the factors Hamzaçebi, 2021.

"Taguchis proposed various different orthogonal arrays which need to be selected based on the individual needs." Hamzaçebi, 2021.

An othogonal array has multiple properties

> Definition orthogonal array

Using these orthogonal arrays instead of full factorial experiments will lead to needing a much smaller amount of simulation runs (in our case only 16 compared to 1024), while the latter "might not provide appreciably more useful information" Roy, 1990.

"Generally speaking, OA experiments work well when there is minimal interaction among factors; that is, the factor influences on the measured quality objectives are independent of each other and are linear. In other words, when the outcome is directly proportional to the linear combination of individual factor main effects, OA design identifies the optimum condition and estimates performance at this condition accurately. If, however, the factors interact with each other and influence the outcome, there is still a good chance that the optimum condition will be identified accurately, but the estimate of performance at the optimum can be significantly off. The degree of inaccuracy in performance estimates will depend on the degree of complexity of interactions among all the factors."Roy, 1990.

cons of taguchi arrays: no higher level interactions, Levels are treated as being discrete

"During many years of applications of factorial design, people have found that higher-order interaction effects (i.e., interaction effects involving three or more factors) are very seldom significant. In most experimental case studies, only some main effects and two-factor interactions are significant."Yang and El-Haik, 2009

"In summary, for full factorial experiments, as the number of factors k increases, the number of runs will increase at an exponential rate that leads to extremely lengthy and costly experiments. On the other hand, as k increases, most of data obtained in the full factorial are used to estimate higher-order interactions, which are most likely to be insignificant."Yang and El-Haik, 2009

"The values of the factors should be as far away from either side of the current working condition as possible."Roy, 1990.

"After these two steps, the total degrees of freedom of the experimental factors should be determined in the Taguchi experimental design. The degrees of freedom are the relative amount of data needed in order to estimate all the effects to be studied."Yang and El-Haik, 2009

Taguchis proposed various different orthogonal arrays which need to be selected based on the individual needs. When choosing a suitable taguchi

ortogonal arrays, we need to take various factors into account, which can make the process tricky. According to Yang and El-Haik, 2009, we will have to follow a three step procedure:

1. Calculate the total degree of freedom (DOF).
2. Following two rules, standard orthogonal array should be selected:

   a) Total DOF need to be smaller than the number of runs provided by the orthogonal array.
   b) All required factor level combinations need to be accommodated by the orthogonal array.

3. Factors have to be assigned using these rules:

   a) In case the factor level does not fit into the orthogonal array, methods such as column merging and dummy level can be used to modify the original array.
   b) Using the linear graph and interaction table, interactions can be defined.
   c) In case some columns are not assigned, its possible to keep these columns empty.

For this genetic algorithm, 7 factors (3 Factors of Level 4 and 4 Factors of Level 2) have been selected. Which factors to choose and with which level was done based on experience gained on section 4.3. In table 4.4.1, every factor with correspondig levels has been listed,

Factors	Code	Level 1	Level 2	Level 3	Level 4
CrossoverType	A	one point	two point	uniform 0.1	uniform 0.5
CrossoverProp	B	0.2	0.5	0.8	0.9
MutationProp	C	0.01	0.1	0.3	0.5
ChromosomeType	D	Time	Time+NPC	-	-
GeneType	E	int	dict	-	-
TournamentSize	F	2	4	-	-
IndMutationProp	G	0.1	0.5	-	-

Figure 4.3: List of Hyperparamters (Factors) matched to a Code and defined settings (Levels)

Using this table, we will now find the best standart orthogonal array in section 4.4.2. Before doing so, it is important to state, that taguchi allows to test for possible (pre determined) two-level interactions (Yang and El-Haik, 2009). Analysing interactions comes at a cost of Degrees of freedom. If we look at the table, an interaction between ChromosomeType and GeneType might be of interest. Using the power of hindsight, we know, that a second two factor interaction is possible within our chosen array, thus we will have a look at the interaction between Tournament Size and IndMutationPropability.

4.4.2 Selection of a suitable standart orthogonal array

The total degree of freedom can be quickly calculated using the rules provided by Yang and El-Haik, 2009:

1. 1 DOF is always used for the overall mean.
2. Each factor has a DOF of NumberOfLevels - 1.
3. Two-factor interactions use this equation to calculate DOF: $(n_{factor1} - 1)(n_{factor2} - 1)$ where n = number of levels.

This leads to the following calculation for the needed 3 Factors of Level 4 and 4 Factors of Level 2 as well as the two interactions between ChromosomeType-GeneType and TournamentSize-IndMutationProp:

$$
\begin{aligned}
DOF &= 1 + 3 * (3 - 1) + 4 * (2 - 1) + 2 * (2 - 1) * (2 - 1) \\
&= 13
\end{aligned}
\tag{4.1}
$$

A L_{16} array seems suitable to accommodate the required 13 DOF, which can be seen in 4.4.2.

NO.	$L_{16}(2^{15})$														
	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
2	1	1	1	1	1	1	1	2	2	2	2	2	2	2	2
3	1	1	1	2	2	2	2	1	1	1	1	2	2	2	2
4	1	1	1	2	2	2	2	2	2	2	2	1	1	1	1
5	1	2	1	1	1	2	2	1	1	2	2	1	1	2	2
6	1	2	2	1	1	2	2	2	2	1	1	2	2	1	1
7	1	2	2	2	2	1	1	1	1	2	2	2	2	1	1
8	1	2	2	2	2	1	1	2	2	1	1	1	1	2	2
9	2	1	2	1	2	1	2	1	2	1	2	1	2	1	2
10	2	1	2	1	2	1	2	2	1	2	1	2	1	2	1
11	2	1	2	2	1	2	1	1	2	1	2	2	1	2	1
12	2	1	2	2	1	2	1	2	1	2	1	1	2	1	2
13	2	2	1	1	2	2	1	1	2	2	1	1	2	2	1
14	2	2	1	1	2	2	1	2	1	1	2	2	1	1	2
15	2	2	1	2	1	1	2	1	2	2	1	2	1	1	2
16	2	2	1	2	1	1	2	2	1	1	2	1	2	2	1

Figure 4.4: $L_{16}(2^{15})$ Taguchi ortohogonal array taken from Roy, 1990

This graph now needs to be fitted to the needed factors. 4 Level Factors need more space which will be generated using column merging, while interactions need to be assigned as well. For this, either an interaction table or linear graphs of this L_{16} array can be used (Roy, 1990, NazanDanacıoğlu, 2005). The linear graph approach is straight forward and will be selected. While there are multiple linear graphs for L_{16} array, the following graph has the best fit for the requirements from table 4.4.1. If no graph with the perfect fit is found, theses graphs can be modified as well, as described by NazanDanacıoğlu, 2005

"In each of Taguchi's orthogonal arrays, there are one or more accompanying linear graphs. A linear graph is used to illustrate the interaction relationships in the orthogonal array."Yang and El-Haik, 2009
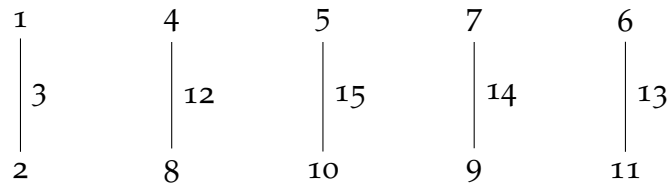
Figure 4.5: Linear Graph of $L_{16}(2^{15})$ taken from Yang and El-Haik, 2009

In a taguchi linear graph, the nodes as well as the ?Lines? both represent collumns in the orthogonal array. An interaction between to columns that are represented as nodes "comes out to" to the connecting line column Taguchi et al., 2005. This is usefull for both analyzing interactions between columns as well as combining (mergin) interacting columns in case a higher factor is needed.

Column Merging A, B and C are both 4 level factors. The currently selected orthogonal only fits 2 level factors. Using column merging, it is possible to extend columns to fit into the given requirements.

"A four-level column is easily prepared from three two-level columns that are part of an interacting group of columns."Roy, 1990

"Steps 1. From the linear graph for L8, select a set of three interacting columns (Figure 5-9). Example: columns 1, 2, and 3. 2. Select any two columns. Suppose 1 and 2 are selected. 3. Combine the two columns row by row, by following the rules of Table 5-19, to get a combined column such as shown in Table 5-17. Replace the original columns 1, 2, and 3 by the new column that has just been prepared."Roy, 1990

"The first three columns of an L8 can be combined to produce a four-level column following the procedure previously described. Step 1. Start with an original L8 and select a set of three interacting columns, say 1, 2, and 3. Step 2. Ignore column 3 (Table 5-21). Step 3. Combine column 1 and 2 into a new column. Follow the procedure as shown by Tables 5-22 and 5-23. Step 4. Assign the four-level factor to this new column and the others to the remaining original two-level columns, as shown in Tables 5-24 and 5-25."Roy, 1990

"The column merging method merges several low-level columns into a high-level column."Yang and El-Haik, 2009

OLD COLUMN			NEW COLUMN
1	1	->	1
1	2	->	2
2	1	->	3
2	2	->	4

Figure 4.6: Rules taken from Roy, 1990

Assigning Interactions An interaction between DE is might be possible. As we still have some unused space in the graph, we will also look at the interaction of FG.
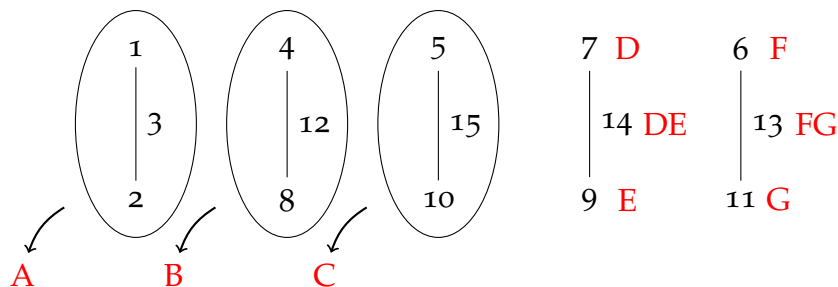
Go over notes from paper and explain this

Figure 4.7: Modified Linear Graph to fit our needs

Combining columns 1 2 3 to A, 4 8 12 to B and 5 10 15 to C using rules defined by table 4.6 is done in 4.8.

NO.	1 2 ~~3~~	4 8 ~~12~~	5 10 ~~15~~
1	~~1 1~~ > 1	~~1 1~~ > 1	~~1 1~~ > 1
2	~~1 1~~ > 1	~~1~~ 2 > 2	~~1~~ 2 > 2
3	~~1 1~~ > 1	~~2 1~~ > 3	~~2 1~~ > 3
4	~~1 1~~ > 1	~~2 2~~ > 4	~~2 2~~ > 4
5	~~1~~ 2 > 2	~~1 1~~ > 1	~~1~~ 2 > 2
6	~~1~~ 2 > 2	~~1~~ 2 > 2	~~1 1~~ > 1
7	~~1~~ 2 > 2	~~2 1~~ > 3	~~2 2~~ > 4
8	~~1~~ 2 > 2	~~2 2~~ > 4	~~2 1~~ > 3
9	~~2 1~~ > 3	~~1 1~~ > 1	~~2 1~~ > 3
10	~~2 1~~ > 3	~~1~~ 2 > 2	~~2 2~~ > 4
11	~~2 1~~ > 3	~~2 1~~ > 3	~~1 1~~ > 1
12	~~2 2~~ > 3	~~2 2~~ > 4	~~1~~ 2 > 2
13	~~2 2~~ > 4	~~1 1~~ > 1	~~2 2~~ > 4
14	~~2 2~~ > 4	~~1~~ 2 > 2	~~2 1~~ > 3
15	~~2 2~~ > 4	~~2 1~~ > 3	~~1~~ 2 > 2
16	~~2 2~~ > 4	~~2 2~~ > 4	~~1 1~~ > 1

Figure 4.8: Building 4 Level columns from 2 Level columns

Removing the old and inserting the new columns in the table and transcoding 7 to D, 9 to E, 14 to DE, 6 to F, 11 to G and 13 to FG results in the final table 4.9. This A-G combinations table will subsequently be used as settings for simulations.

NO.	A	B	C	D	E	F	G	FG	DE
1	1	1	1	1	1	1	1	1	1
2	1	2	2	1	2	1	2	2	2
3	1	3	3	2	1	2	1	2	2
4	1	4	4	2	2	2	2	1	1
5	2	1	2	2	1	2	2	1	2
6	2	2	1	2	2	2	1	2	1
7	2	3	4	1	1	1	2	2	1
8	2	4	3	1	2	1	1	1	2
9	3	1	3	2	2	1	2	2	1
10	3	2	4	2	1	1	1	1	2
11	3	3	1	1	2	2	2	1	2
12	3	4	2	1	1	2	1	2	1
13	4	1	4	1	2	2	1	2	2
14	4	2	3	1	1	2	2	1	1
15	4	3	2	2	2	1	1	1	1
16	4	4	1	2	1	1	2	2	2

Figure 4.9: Final version of used Taguchi orthogonal array

4.4.3 Analysing the results

This now can be used for running all the needed testcases (the interaction columns can be ignored until the evaluation). Simply exchange all levels in the table with the corresponding setting from table 4.4.1. We will repeat every setting 8 times. These are the results:

NO.	rep1	rep2	rep3	rep4	rep5	rep6	rep7	rep8
1	3124	3110	3025	3077	3068	2925	3106	3105
2	2694	2980	3025	2996	3037	2921	3068	2900
3	2638	2711	2624	2856	2623	2832	2904	2778
4	2735	2805	2851	2965	2876	2703	2848	2858
5	3074	2955	3045	3080	3120	2971	2895	2798
6	2974	2979	2929	2941	2952	2936	3139	2953
7	3108	3099	3049	3020	3092	3057	3090	2895
8	2840	2931	2921	2921	2957	2997	2889	2895
9	3007	2995	2983	3009	2847	2996	2734	2927
10	2916	2828	3013	2787	2818	2926	3034	2822
11	3007	2879	3090	3033	2906	2981	3109	3104
12	2946	3016	2790	2917	2904	2983	2898	2606
13	2378	2712	2906	2800	2912	2795	2860	2834
14	2895	2760	2750	2849	2542	2997	2965	2991
15	2842	3065	3050	2779	2862	2923	2955	2892
16	3065	2834	2643	3056	3051	3011	2828	2963

Figure 4.10: List of results

Main-effects and interaction chart

Main-effects or main-effect

Identifing the optimal conditions is done by analyzing the main effects per factor. Using them, it is possible to predict the factors, that lead to the best result Roy, 1990.

According to Yang and El-Haik, 2009, "The main-effects chart is a plot of average responses at different levels of a factor versus the factor levels" and the calculation" of main-effect charts and iteration charts are the same as those of classical experimental data analysis".

For every factor, sum up the mean of the results per level, then divide by the number of runs per level. This is the calculation for D:

Insert calculation for d

The resulting main-effect charts can be seen here:

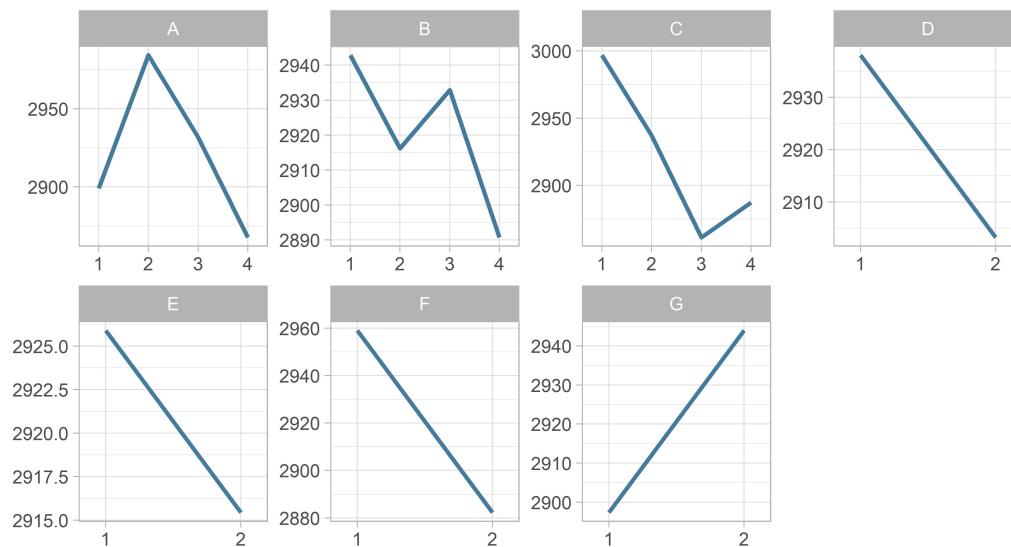**Explain interactiona an main effects using example from results**

Figure 4.11: Main Effects

Similarly, the interactions are calculated like this:

Insert example calculation of interaction

"To determine whether the interaction is present, a proper interpretation of the results is necessary. The general approach is to separate the influence of an interacting member from the influences of the others. In this example, A × C and B × C are the interactions with C common to both."Roy, 1990.
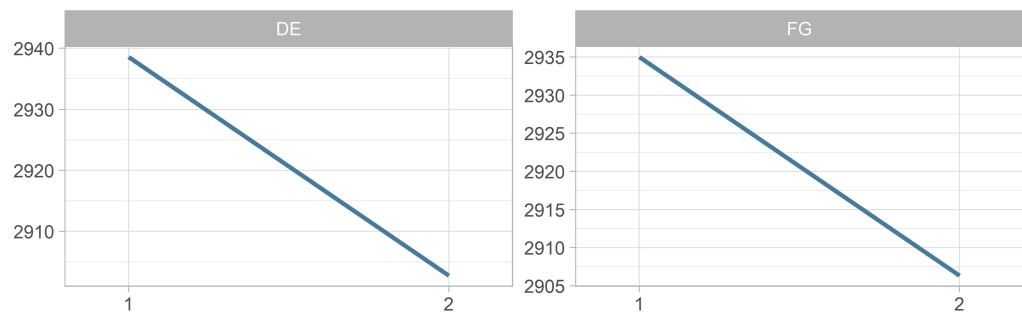
The resulting interaction charts can be seen here:

29

Figure 4.12: Interactions Effects

"The steps involved are described below. The A1C1 is first found from the results that contain both A1 and C1. Note that A1C1 is not the same as the average value in level 1 of Table 5-16(a) for interaction A × C assigned to column 3 of Table 5-13. This value is (A × C)1. In this analysis, interaction columns, that is, columns 3 and 6, are not used. Instead, the columns of Table 5-13 that represent the individual factors are used. Examination of column 1 shows that A1 is contained in rows (trial runs) 1, 2, 3, and 4, but C1 is in trial runs 1, 2, 5, and 6. Comparing the two, the rows that contain both A1 and C1 are 1 and 2. Therefore, A1C1 comes from the results of trial runs 1 and 2."Roy, 1990.

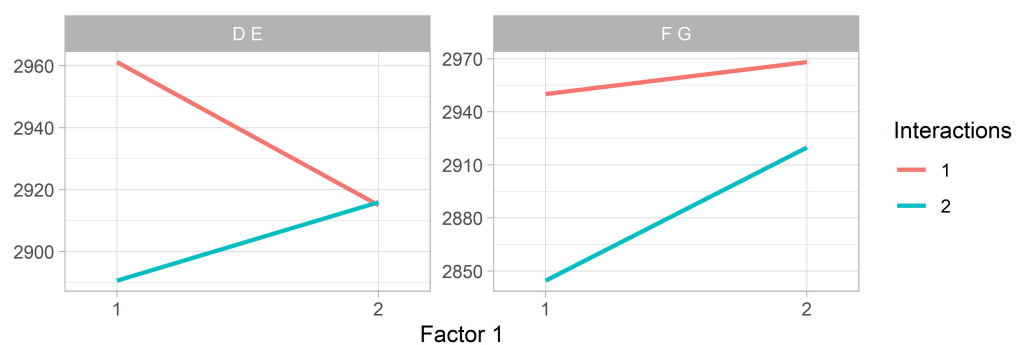In order the see, if interactions are existing, we need a Test of interactions.

Figure 4.13: Test of interactions

"Figure 5-2(a) shows an interaction between the two factors because the lines cross. Figure 5-2(b) shows no interaction because the lines are parallel. If the lines are not parallel, the factors may interact, albeit weakly. .... the input for this interaction plot comes from the experimental results, and the degree of presence of interaction is calculated as the magnitude of the angle between the lines" Roy, 1990.

"if there is no interaction, the optimal setting can be determined by looking at one factor at a time. If there are interactions, then we have to look at the interaction chart. For the problem above, since AB interaction is significant, we have to find optimal by studying the AB interaction. From the interaction chart, if the vibration level is "the smaller, the better," then A at low level and B at high level will give the lowest possible vibrations."Yang and El-Haik, 2009

ANOVA

Due to our number of repetitions, the number of DOF increases according to the following equation (taken from Roy, 1990):

"There is actually no difference between analysis of variance of classical DOE and Taguchi DOE."Yang and El-Haik, 2009

"Identify which main effects and interactions have significant effects on variation of data."Yang and El-Haik, 2009

"In analysis of variance, mean squares are used in the F test to see if the corresponding effect is statistically significant."Yang and El-Haik, 2009 "F ratio is a better measure for relative performance"Yang and El-Haik, 2009

". The most commonly used criterion is to compare the p value with 0.05, or 5%, if p value is less than 0.05, then that effect is significant."Yang and El-Haik, 2009

"The variance ratio, commonly called the F statistic, is the ratio of variance due to the effect of a factor and variance due to the error term. (The F statistic is named after Sir Ronald A. Fisher.) This ratio is used to measure the significance of the factor under investigation with respect to the variance of all of the factors included in the error term. The F value obtained in

the analysis is compared with a value from standard F-tables for a given statistical level of significance." Roy, 1990.

"Because the partial experiment is only a selected set of the full factorial combinations, the analysis of the partial experiment must include an analysis of confidence to qualify the results. Fortunately, there is a standard statistical technique called analysis of variance (ANOVA) that is routinely used to provide a measure of confidence. The technique does not directly analyze the data but rather determines the variability (variance) of the data. Confidence is measured from the variance"Roy, 1990

$$
\begin{aligned}
DOF &= totalNumberOfResults - 1 \\
&= numberOfTrials * numberOfRepetitions - 1 \qquad (4.2) \\
&= 16 * 8 - 1 = 127
\end{aligned}
$$

Calculating ANOVA can be done using R:

Cite book from Gabriel

```
# pivot the results, so that the table has 8 times the ro
taguchi.combined_pivoted <- taguchi.combined %>% pivot_lo

# run anova analysis
anova <- aov(results ~ factor(A) + factor(B) + factor(C)
summary(anova)
```

"The process of disregarding an individual factor's contribution and then subsequently adjusting the contributions of the other factors is known as pooling. Generally, only factors that are believed to be insignificant are pooled. Whether a factor is significant or not is found by the test of significance." Roy, 1990

"Procedures for Pooling When the contribution of a factor is small, as for factor B in the above example, the sum of squares for that factor is combined with the error, Se. This process of disregarding the contribution of a selected factor and subsequently adjusting the contributions of the other factor is known as pooling. Pooling is usually accomplished by starting with the smallest sum of squares and continuing with the ones having successively larger effects. Pooling is recommended when a factor is determined to be

insignificant by performing a test of significance against the error term at a desired confidence level. A general guideline for when to pool is obtained by comparing the error DOF with the total factor DOF. Taguchi recommends pooling factors until the error DOF is approximately half the total DOF of the experiment ([9], pp. 293-295). Approaching the matter technically, one could test for significance and pool all factor influences below the 90% confidence level"Roy, 1990

"No matter the effect on the results, insignificant factors should always be pooled."Roy, 1990

"Note that as small factor effects are pooled, the percentage contributions and the confidence level of the remaining factors decrease (PC = 5.71 versus PC = 6.02). By pooling, the error term is increased and, in comparison, the other factors appear less influential. The greater the number of factors pooled, the worse the unpooled factor effects look. Then we must consider why column effects are pooled."Roy, 1990

"A sure way to determine if a factor or interaction effect should be pooled is to perform a test of significance (1 – confidence level). But what level of confidence do you work with? No clear guidelines are established. Generally, factors are pooled if they do not pass the test of significance at the confidence level assumed for the experiment. A factor is considered significant if its experimental F-ratio exceeds the standard table value at a confidence level. A common practice is to subjectively assume a confidence level between 85% and 99%, with 90% or 95% being a popular selection. Consider factor C in Example 6-5, which has 5.7% influence (19.267 F-ratio). When tested for significance, this factor shows more than 99% confidence level and thus should not be pooled."Roy, 1990

After pooling, we can run anova again:

```
anova <- aov(results ~ factor(A) + factor(B) + factor(C) + factor(
summary(anova)
```

This will result in the following table:

Column	DF	Sum Sq	Mean Sq	F value	p value
1	A	3	1000	1000	1000
2	B	3	1000	1000	1000
3	C	3	1000	1000	1000
4	D	1	1000	1000	1000
5	E	1	1000	1000	1000
6	F	1	1000	1000	1000
7	G	1	1000	1000	1000
8	DxE	1	1000	1000	1000
9	FxG	1	1000	1000	1000
Residuals			1000	1000	1000

Figure 4.14: ANOVA results

We can also look at the percentage contribution of each factor, using the formular gathered by Yang and El-Haik, 2009:

$$SS_T = SS_A + SS_B + SS_C + ... + SS_e rror \tag{4.3}$$

$$contribution_A = SS_A/SS_T * 100 \tag{4.4}$$

Import already generated chart

Best factor level selection and optimal performance level prediction (Take from yang_design_2009, so reformulate) "Further analysis for the significance of this influence is made possible by the ANOVA table in Table 5-16(b), which shows that the interaction A × C (column 3) is 5.26%, compared to the individual main effects of butter (B) 64.76% and flour (D) 18.4%, and so on."Roy, 1990.

"To reexamine the optimum condition determined only from the factors A2, C1, B2, D1, and E1, we see from Figure 5-6 that AC 11has a higher value than AC 21. Thus, based on the interaction analysis, the optimum condition must include levels A1 and C1. The new optimum conditions become A1

B2 C1 D1 E1. However, the performance at the new optimum should be compared with the original optimum before the final determination of the interaction effects."Roy, 1990. This means, that If an interaction exist, we 1. look at the best main effect combination 2. check if the interactions align with this combination -> look at Test of interactions 3. if not, combute Y_{opt}... -> look at page 88 from Roy, 1990. You use the interaction effects only for combuting Yopt (altough it is also possible to calc it without...)

"For the purpose of analysis, interactions are treated as any other factors; however, their presence is ignored for the preliminary determination of the optimum condition. The relative significance of interactions is obtained from an ANOVA study."Roy, 1990

"The performance at the optimum condition is estimated only from the significant factors. This practice keeps the predicted performance conservative. Therefore, the pooled factors are not included in the estimate."Roy, 1990

If we only look at main effects, we would select: A4, B4, C3, D2, E2, F2, G1 However we select A4, B4, C3, D2, E1, F2, G1 because of important interaction DE. E on the other hand is not significant.

We can also optimum performance when 1. using only main effects or 2. using main effects with applied interaction. Folrumar provided by Roy, 1990.

Better bars

$$Y_{opt} = \bar{T} + (\bar{A}_4 - \bar{T}) + (\bar{B}_4 - \bar{T}) + (\bar{C}_3 - \bar{T}) + (\bar{D}_2 - \bar{T}) + (\bar{E}_2 - \bar{T}) + (\bar{F}_2 - \bar{T}) + (\bar{G}_1 - \bar{T})$$
$$= 2693.984$$

(4.5)

$$Y_{opt} = \bar{T} + (\bar{A}_4 - \bar{T}) + (\bar{B}_4 - \bar{T}) + (\bar{C}_3 - \bar{T}) + (\bar{D}_2 - \bar{T}) + (\bar{E}_1 - \bar{T}) + ([\bar{DxE}]_2 - \bar{T}) + (\bar{F}_2 - \bar{T}) + (\bar{G}_1$$
$$= 2686.547$$

(4.6)

SN -> proposed by taguchi. "A common approach to analyze such results is to use the average of the trial results for the optimum condition. Unfortunately, average alone does not capture complete information about the variability present."Roy, 1990

"Repetition permits determination of a variance index called the signal-to-noise (S/N) ratio. The greater this value, the smaller the product variance around the target value"Roy, 1990

TODO: Somehow argument, that having less variablity is only to an extend important. It is always possible to restart a simulation, if the variability is not too large, it is important that the results have a good mean overall. Less variability is in producing products much more important.

"Advantage of S/N Ratio Over Average To analyze the results of experiments involving multiple runs, use of the S/N ratio over standard analysis (use average of results) is preferred. Analysis using the S/N ratio will offer the following advantages: 1. It provides a guidance to selection of the optimum level based on the least variation around the target and also on the average value closest to the target. 2. It offers objective comparison of two sets of experimental data with respect to variation around the target and the deviation of the average from the target value. Because S/N represents results transformed into a logarithmic scale that linearizes any nonlinear behavior, if present, the assumption of linearity for prediction of optimum performance is validated."Roy, 1990

"On the other hand, for set A, the spread around its average is smaller, but the average itself is quite far from the target. Which one of the two is better? Based on average value, the product shown by observation B appears to be better. Based on consistency, product A is better. How can one credit A for less variation? How does one compare the distances of the averages from the target? Surely, comparing the averages is one method. Use of the S/N ratio offers an objective way to look at the two characteristics together."Roy, 1990

Not usefull for our purposes... Because df is reduced, run anova without interactions (or maybe without bad main effects). Fazit: S N was tried, however resulting anova showed that no factor was significant. Thus is was not further investigated.

"Effect of S/N Ratio on the Analysis Use of the S/N ratio of the results, instead of the average values, introduces some minor changes in the analysis. 1. Degrees of freedom of the entire experiment is reduced. DOF with S/N ratio = number of trial conditions - 1 (that is, number of repetitions is

reduced to 1). Recall that the DOF in the case of the standard analysis is: DOF = (number of trials × number of repetitions) - 1 The S/N ratio calculation is based on data from all observations of a trial condition. The set of S/N ratios can then be considered as trial results without repetitions. Hence the DOF, in the case of S/N, is the number of trials - 1. The rest of the analysis follows the standard procedure."Roy, 1990

5 Evaluation

in this chapter, we evaluate and compare various different settings

5.1 Comparison with random and default ga Values

Compare with Boxplot...

Different Algorithms: 1. Optimized GA 2. Best GA setting from Population 3. Random

5.2 Generalization on different start scenarios

scenario 1: default : 9v 5p scenario 2: 9v 5p scenario 3: 5v 3p scenario 4: 18v 10p

6 Conclusion

6.1 Test

Altough lots of shortcommings Results look very vielversprechend. This thesis hopes to have emphasised that this approach has lots of advanatages

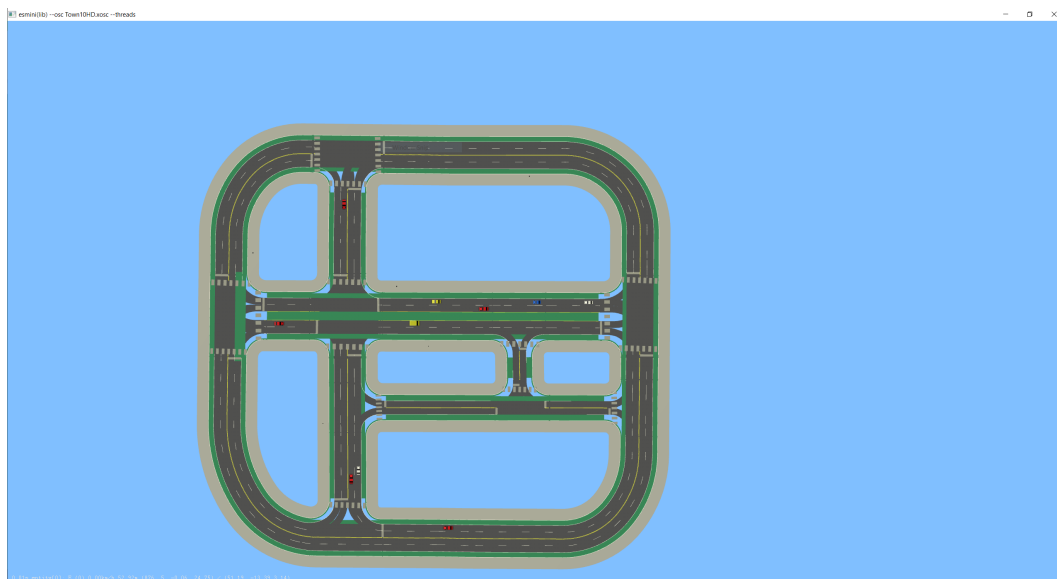# Appendix

Appendix A.

Figure 1: Start scenario 1

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