

-Syntax Analysis-Predictive Parser

FIRST

To compute $\text{FIRST}(X)$ for all grammar symbols X , apply the following rules until no more terminals or ϵ can be added to any FIRST set.

1. If X is a terminal, then $\text{FIRST}(X) = \{X\}$.
2. If X is a nonterminal and $X \rightarrow Y_1 Y_2 \cdots Y_k$ is a production for some $k \geq 1$, then place a in $\text{FIRST}(X)$ if for some i , a is in $\text{FIRST}(Y_i)$, and ϵ is in all of $\text{FIRST}(Y_1), \dots, \text{FIRST}(Y_{i-1})$; that is, $Y_1 \cdots Y_{i-1} \xRightarrow{*} \epsilon$. If ϵ is in $\text{FIRST}(Y_j)$ for all $j = 1, 2, \dots, k$, then add ϵ to $\text{FIRST}(X)$. For example, everything in $\text{FIRST}(Y_1)$ is surely in $\text{FIRST}(X)$. If Y_1 does not derive ϵ , then we add nothing more to $\text{FIRST}(X)$, but if $Y_1 \xRightarrow{*} \epsilon$, then we add $\text{FIRST}(Y_2)$, and so on.
3. If $X \rightarrow \epsilon$ is a production, then add ϵ to $\text{FIRST}(X)$.

FOLLOW

To compute FOLLOW(A) for all nonterminals A , apply the following rules until nothing can be added to any FOLLOW set.

1. Place $\$$ in FOLLOW(S), where S is the start symbol, and $\$$ is the input right endmarker.
2. If there is a production $A \rightarrow \alpha B \beta$, then everything in FIRST(β) except ϵ is in FOLLOW(B).
3. If there is a production $A \rightarrow \alpha B$, or a production $A \rightarrow \alpha B \beta$, where FIRST(β) contains ϵ , then everything in FOLLOW(A) is in FOLLOW(B).

Predictive Parser or LL(1) parser

- Is a top-down parser
- Given a **grammar G** and an **input string** to be tested.....
- Start from the root or start variable S
- Construct the tree in top-down fashion (leaves at the bottom)

PREDICTIVE PARSER

- Remove left recursion (if any) from the grammar $A \rightarrow Da$ (in G) $D \rightarrow A$
- Construct **parsing table** from given grammar
- **Table showing sequence of moves** for the given input string & parsing table

Step 1: Remove left recursion (if any) from the grammar: Check if for any variable A , $A \xRightarrow{+} A\alpha$

$$\begin{array}{ll} E & \rightarrow T E' \\ E' & \rightarrow + T E' \mid \epsilon \\ T & \rightarrow F T' \\ T' & \rightarrow * F T' \mid \epsilon \\ F & \rightarrow (E) \mid \mathbf{id} \end{array} \quad (4.28)$$

FIRST(R.H.S) and FOLLOW(Non-Term)

Q: G

$$\begin{aligned}
 E &\rightarrow TE' & \dots \dots \text{FIRST}(TE') &= \{[, id\} \\
 E' &\rightarrow +TE' & \dots \dots \text{FIRST}(+TE') &= \{+\} \\
 E' &\rightarrow \epsilon & \dots \dots \text{FIRST}(\epsilon) &= \{\epsilon\} \quad \therefore \text{Nothing} \\
 T &\rightarrow FT' & \dots \dots \text{FIRST}(FT') &= \{[, id\} \\
 T' &\rightarrow *FT' & \dots \dots \text{FIRST}(*FT') &= \{*\} \\
 T' &\rightarrow \epsilon & \dots \dots \text{FIRST}(\epsilon) &= \{\epsilon\} \\
 F &\rightarrow (E) & \dots \dots \text{FIRST}(\underline{(E)}) &= \{(\} \\
 F &\rightarrow id & \dots \dots \text{FIRST}(id) &= \{id\}
 \end{aligned}$$

$$\begin{aligned}
 \text{FOLLOW}(E) &= \{ \$, \} \checkmark \\
 \text{FOLLOW}(E') &= \text{FOLLOW}(E) \\
 &= \{ \$, \} \checkmark \\
 \text{FOLLOW}(T) &= \text{FIRST}(E') \\
 &= \{ +, \$, \} \\
 \text{FOLLOW}(T') &= \text{FOLLOW}(T) \\
 &= \{ +, \$, \} \\
 \text{FOLLOW}(P) &= \text{FIRST}(T') \\
 &= \{ *, +, \$, \} \\
 \text{term} &= \{ +, *, [,], id, \$ \} \\
 \text{N.T} &= \{ E, E', T, T', F \}
 \end{aligned}$$

Step 2: Construct parsing table from given grammar

Algorithm 4.31: Construction of a predictive parsing table.

INPUT: Grammar G .

OUTPUT: Parsing table M .

METHOD: For each production $A \rightarrow \alpha$ of the grammar, do the following:

1. For each terminal a in $\text{FIRST}(\alpha)$, add $A \rightarrow \alpha$ to $M[A, a]$.
2. If ϵ is in $\text{FIRST}(\alpha)$, then for each terminal b in $\text{FOLLOW}(A)$, add $A \rightarrow \alpha$ to $M[A, b]$. If ϵ is in $\text{FIRST}(\alpha)$ and $\$$ is in $\text{FOLLOW}(A)$, add $A \rightarrow \alpha$ to $M[A, \$]$ as well.

If, after performing the above, there is no production at all in $M[A, a]$, then set $M[A, a]$ to **error** (which we normally represent by an empty entry in the table). \square

Example 4.32: For the expression grammar (4.28), Algorithm 4.31 produces the parsing table in Fig. 4.17. Blanks are error entries; nonblanks indicate a production with which to expand a nonterminal.

NON - TERMINAL	INPUT SYMBOL					
	id	+	*	()	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
F	$F \rightarrow \text{id}$			$F \rightarrow (E)$		

Figure 4.17: Parsing table M for Example 4.32

Step 3: Sequence of moves for input $\text{id} + \text{id} * \text{id}$

MATCHED	STACK	INPUT	ACTION
	$E\$$	$\text{id} + \text{id} * \text{id}\$$	
	$TE'\$$	$\text{id} + \text{id} * \text{id}\$$	output $E \rightarrow TE'$
	$FT'E'\$$	$\text{id} + \text{id} * \text{id}\$$	output $T \rightarrow FT'$
	$\text{id } T'E'\$$	$\text{id} + \text{id} * \text{id}\$$	output $F \rightarrow \text{id}$
id	$T'E'\$$	$+ \text{id} * \text{id}\$$	match id
id	$E'\$$	$+ \text{id} * \text{id}\$$	output $T' \rightarrow \epsilon$
id	$+ TE'\$$	$+ \text{id} * \text{id}\$$	output $E' \rightarrow + TE'$
$\text{id} +$	$TE'\$$	$\text{id} * \text{id}\$$	match $+$
$\text{id} +$	$FT'E'\$$	$\text{id} * \text{id}\$$	output $T \rightarrow FT'$
$\text{id} +$	$\text{id } T'E'\$$	$\text{id} * \text{id}\$$	output $F \rightarrow \text{id}$
$\text{id} + \text{id}$	$T'E'\$$	$* \text{id}\$$	match id
$\text{id} + \text{id}$	$* FT'E'\$$	$* \text{id}\$$	output $T' \rightarrow * FT'$
$\text{id} + \text{id} *$	$FT'E'\$$	$\text{id}\$$	match $*$
$\text{id} + \text{id} *$	$\text{id } T'E'\$$	$\text{id}\$$	output $F \rightarrow \text{id}$
$\text{id} + \text{id} * \text{id}$	$T'E'\$$	$\$$	match id
$\text{id} + \text{id} * \text{id}$	$E'\$$	$\$$	output $T' \rightarrow \epsilon$
$\text{id} + \text{id} * \text{id}$	$\$$	$\$$	output $E' \rightarrow \epsilon$

Figure 4.21: Moves made by a predictive parser on input $\text{id} + \text{id} * \text{id}$

- Outcome of Syntax Analysis stage: $(\$, \$) : \text{YES/accept}$ (NO SYNTAX ERROR in $\text{id} + \text{id} * \text{id}$)

Some tips for LL(1) parser (Predictive parser)...

- While making the PARSING TABLE (Step 2) follow the rules.....
- For all productions $LHS \rightarrow RHS$, {go for the $FIRST(RHS)$; if $FIRST$ contains epsilon go for $FOLLOW(LHS)$ }; Write this production in appropriate cell number. [Repeat for all productions in the input grammar]
- While making SEQUENCE OF MOVES TABLE (Step 3) follow the rules.....
- 3 columns: STACK, INPUT, ACTION; refer to PARSING TABLE for each ACTION
- Explain ACTION in detail, eg. “Refer to cell no. (F, id) and substitute F by id”
- Replacement done on the top of the stack (leftmost position on the stack)
- Declare MATCH!! if top of stack matches and cancels out with leftmost symbol of input string
- Repeat till you get (\$, \$) in (STACK, INPUT) for NO SYNTAX ERROR IN INPUT!