Automatic Test Grader Using Image Processing And Machine Learning Techniques



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I would like to acknowledge my skripsie leader, JA du Preez, parents and the engineering class of 2017 for their kind contributing to this thesis.

Declaration

I, the undersigned, hereby declare that t	the work contained in this final year
project is my own original work and that	I have not previously in its entirety
or in part submitted it at any university	y for a degree.
Signature	Date

Check of dit reg is??

ECSA Exit Level Outcomes Reference

Outcome	Reference				
	Sections	Pages			
1. Problem solving: Demonstrate competence to	All	All			
identify, assess, formulate and solve convergent					
and divergent engineering problems creatively and					
innovatively.					
5. Engineering methods, skills and tools, includ-	2, 3, 4, 5, 6 & 7	10 - 62			
ing information technology: Demonstrate com-					
petence to use appropriate engineering methods,					
skills and tools, including those based on informa-					
tion technology.					
6. Professional and technical communication:	All	All			
Demonstrate competence to communicate effec-					
tively, both orally and in writing, with engineering					
audiences and the community at large.					
9. Independent learning ability: Demonstrate	2, 3, 4 & 5	10 - 37			
competence to engage in independent learning					
through well developed learning skills.					
10. Engineering professionalism: Demonstrate	8.3 & 8.4	66 - 67			
critical awareness of the need to act professionally					
and ethically and to exercise judgment and take					
responsibility within own limits of competence.					

Abstract

English abstract here.

Opsomming

Afrikaanse opsomming hier. Alle dokumente moet beide Afrikaans en Engelse opsommings bevat.

Contents

ECSA Outcomes Reference												
A	Abstract											
O	Opsomming											
Li	st of	Figur	es			x						
Li	st of	Table	·s			xi						
N	omer	ıclatur	re			xii						
1	Intr	oduct	ion			1						
	1.1	Proble	em background			1						
	1.2	Proble	em statement			2						
	1.3	Projec	ct scope and assumptions			2						
	1.4	Projec	ct objectives			4						
	1.5	Resea	rch methodology			4						
	1.6	Graph	nical overview of system			5						
		1.6.1	System overview			5						
		1.6.2	Graphical representation			5						
2	Literature Study											
	2.1	Existi	ng systems			7						
		2.1.1	Standard OMR techniques			7						
	2.2	Additional techniques										
		2.2.1	Contour detection			9						
		2.2.2	Character recognition			10						

	2.3	Concl	usion: System requirements	10									
3	Ima	ige Pro	ocessing	11									
	3.1	Orient	tation Detection	11									
		3.1.1	Initial filtering and orientation detection	12									
		3.1.2	Radon Transform	14									
		3.1.3	Finding the template	14									
	3.2	Bubbl	e detection and processing	17									
	3.3	Data 1	processing and grading	18									
	3.4	Conclusion											
4	Ma	chine l	earning approach	19									
	4.1	Chara	cter recognition using a neural network	19									
		4.1.1	Introduction	19									
		4.1.2	Neural Network Basics	20									
			4.1.2.1 The artificial neuron	20									
			4.1.2.2 Getting a output from the network	21									
			4.1.2.3 Training of neural network	22									
		4.1.3	Preprocessing on image	22									
	4.2	Proba	bilistic Graphical Models	26									
		4.2.1	Structure of the graph	26									
		4.2.2	Determining the intended digit	27									
		4.2.3	Training the model	28									
		4.2.4	Student number identification	28									
	4.3	Concl	usion	28									
5	Ana	alysis o	of results	30									
	5.1	Future	e improvements	30									
6	Sun	nmary	and conclusions	31									
	6.1	Project summary											
	6.2	How t	his final year project benefits society	31									
	6.3	What	the student learned	31									
	6.4	Concl	usion: Summary and conclusions	31									

CONTENTS

Re	eferences	32
\mathbf{A}	Graphical overview of system as a whole	33
В	Mathematical derivation of system as a whole	34
\mathbf{C}	Implementation/Algorithms	35
	C.1 Deep Convolutional Neural Network	35
D	Validation and results	36
${f E}$	Project plan	37

List of Figures

1.1	Automatic grading template 1	3
1.2	System overview	6
2.1	Standard OMR template, VijayaForm (2017)	8
2.2	Example answer from student	10
3.1	Reduced contours in image	13
3.2	Radon transform applied on a 2 dimensional area, Edoras (2017) \dots	15
3.3	Detection of template in image and estimation of bubble locations	16
3.4	Result in rotation after applying radon transform	17
4.1	Basic structure of an neural network, Karpathy (2017)	20
4.2	Example image used as input to the neural network, $\overline{\text{Tensorflow}}$ (2017) .	21
4.3	Image scanned for character areas	23
4.4	The found box is then normalized to rectangular shape	24
4.5	a Randon transform then gets applied	24
4.6	An clustering algorithm is used to find the main cluster in the remaining	
	image	25
4.7	Area of found cluster	25
4.8	Final translation and normalization of image	26
4.9	Graphical setup of digit generation	27
4.10	Column representing one digit	28
E.1	Project plan for the final year project	38

List of Tables

Nomenclature

ANN Artificial neural network

DCNN Deep convolutional neural network

OCR Optical character recognition

OMR Optical mark recognition

PGM Probabilistic graphical model

Chapter 1

Introduction

As modern technology and machine learning techniques advances, it is important for the educational sector to also continuously advance their learning environment. This allows for a ever improving learning experience in and outside the classroom.

1.1 Problem background

In the recent years the Applied Mathematics Department of Stellenbosch Engineering, started observing a decrease of accuracy in grading of tutorial tests, done by a teaching assistants or demi. Students complain on a regular basis about correct answers being marked wrong or even that their answers were totally ignored. To address this problem the Applied Mathematics department proposes to automate the process of grading these tutorial tests.

The head of the department wants a system that can analyze and grade tests written on a specific template. These answer sheets will be handed out for the students to fill in their respective answers. The answer sheets are then scanned-in to create a digital copy. The system is tasked with automatically grading all these digital copies and transferring the graded results to a database.

The department will send weekly scanned in sheets, which needs to be graded and the results then sent back to them. This will be done in parallel with the development and expansion of the test grading software. For these reasons an agile development mythology will be used with a weekly validation test, as the system gets used.

1.2 Problem statement

Given the problem background and stakeholders discussed in the previous section the problem to be solved can be formulated as

Develop and **implement** a automatic test grading system that will reduce marking time and increasing accuracy on the grading of Applied Mathematics tutorial tests, written by students.

1.3 Project scope and assumptions

Initial discussions with the department head revealed that a specific answer sheet template can be used. This allows the custom image processing software to more accurately determine what the student filled in. The template will consist of bubbles that can be colored in as well as blocks for handwritten digits, as can be seen in Figure 1.1. This template is constructed by the Applied Mathematics Department. Thus the focus of this thesis will be on processing that scanned in document written on the specific template. Too use the template the student must fill in their student number and answers in the blocks above each category. They are also required to fill in the bubble underneath each digit, corresponding to that specific digit. Additionally n bubble next to each question is provided if a negative sign is required.

Any additional assumptions will be specified at the appropriate times throughout the thesis. Two more templates will also be implemented in later chapters, which will allow for multiple choice questions.

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Figure 1.1: Automatic grading template 1.

1.4 Project objectives

The problem as stated in section ??, will be addressed by pursuing the following objectives:

- 1. Do a literature study on the topics of Image Processing, Computer Vision and Character Recognition.
- 2. Develop a software application to enable a user to grade a large number (approximately 1000) scanned in student tests automatically.
- 3. Do a weekly validation experiment with the software, by grading tutorial test for the department. The results is then used as the student's grade for that test.
- 4. Use an agile development mythology to improving the software in parallel with the grading of weekly tests.
- 5. Add additional software to allow grading of new *templates* and to increase the speed and accuracy of the software.

The objectives will be covered in different chapters in the report. Note that each objective (1–5) built on the objective(s) previously listed.

The software must also ease the use of the template for students while also providing precise and useful feedback. To do this every graded result will also include feedback on what answers the student got wrong and what the correct answers were. To increase ease of use, software will be developed that provides the luxury to students to only writing down their student numbers. Thus time does not get wasted filling in the student number bubbles. This result is achieved in Chapter 4.2.4.

1.5 Research methodology

To complete the objectives listed in Section 1.4, a agile development mythology will be used. The methodology followed comprises of five different phases:

- 1. Identify a new feature or update that needs to be implemented into the software package.
- 2. Do a study on the existing methods to implement this new software.

- 3. Implement and integrate the new software with the currently knowledge of the solution.
- 4. Test the software and observe if it is working as planned.
- 5. If the software is not working as planned recurs steps 2-4 until the new software is working.
- 6. Backup the new working software using Git or another backup utility.

The structure and graphical overview of the software, is presented next. (Vra prof of my wiskude reg is oor hoe die PGM stelsel werk.)

1.6 Graphical overview of system

For a detailed derivation of the entire system, refer to Appendix B.

1.6.1 System overview

When thinking about the system(for template 1), from a philosophical sense, it can be represented by 6 information nodes. The student has certain information he/she wants to portray on the paper. This includes the 4 answers and student number he/she wants to write down. Thus those 5 nodes gives rise to the image, representing the last node. This has to be represented in a probabilistic way. This is, because the process of writing answers down and scanning the test sheet in is going to produce a different image every time a test is written, even though the same answers are intended. This graphical model is illustrated in Figure 1.2. The unnamed blocks indicate that information processing happens in these steps. For a more detailed visual overview of the system, please refer to Appendix A.

1.6.2 Graphical representation

For this thesis a graphical approach is followed in representing the software developed. A graphical model in essence allows software to be represented as information (represented by circles) and relationships (represented by directed arrows). The directions of the arrows represents what information causes other information to be created (From

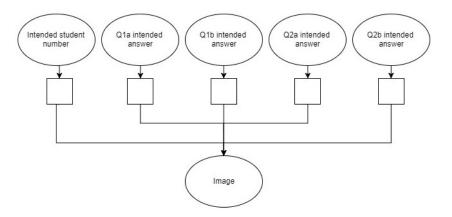


Figure 1.2: System overview.

parent to offspring). This can again be seen in Figure 1.2. This allows intuitive reasoning about how the system should operate. An observation is always made in the form of an image and then the system is tasked with predicting what the written answers are. Due to the probabilistic nature of the system a probabilistic component is also needed in this graphical models. Thus a probabilistic graphical modeling(PGM) is used.

A PGM is in essence the same as a general graphical model. The only difference is that now the information and relationships between information bubbles are probabilistic and not always certain as with general logic graphical models.

A literature study will be presented next on methods currently used by existing automatic test grading systems. This will describe in the next chapter.

Chapter 2

Literature Study

In the previous chapter the problem statement and objectives of this thesis was laid out. Further a brief system overview was also provided. This chapter will provide information about already excising systems and the techniques they use in doing image processing and character recognition on images. There will also be looked at already excising libraries to aid in the implementation of these techniques.

2.1 Existing systems

The types of systems used to grade test automatically are commonly known as a Optical Mark Recognition (OMR) systems. OMR systems are used to extracted answers from filled in forms, using a special template, seen in Figure 2.1. These templates are normally used when fast and accurate grading of tests are needed, where test only have specific answer choices. OCR systems are thus excellent for the grading multiple choice type questions. The drawback of most of these systems are that they normally only grade color-in bubbles and do not interpret characters on the page.

2.1.1 Standard OMR techniques

As can be seen in Figure 2.1, there is normally specific reference blocks on a OMR template. These blocks are included to allow the computer vision and image processing algorithms find the orientation of the image more easily.

In an OMR system there are normally two phases to marking an test, as stated in Ivetic & Dragan (2003). The first step is to determine the region within where the

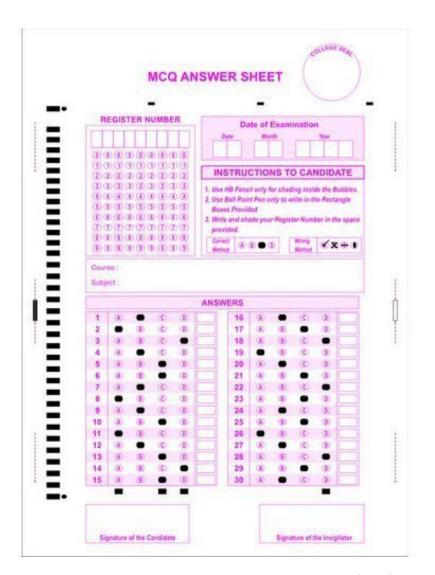


Figure 2.1: Standard OMR template, VijayaForm (2017)

answers are located in the image. In this process the system finds the orientation of the template in the image and thus can approximate the location of the bubbles. Normally some preprocessing on a blank template is done beforehand too aid in locating the bubbles. Once the bubbles are found their locations gets stored and processed. The final step is then to calculate the average pixel concentration in the bubbles and estimate weather they have been filled in.

2.2 Additional techniques

The above method allows for grading of tests using a simple OMR system. For the test grader used for the Applied Mathematics tests, there is needed to go beyond such a basic system. In standard OCR, when a student makes a mistake, he/she needs to erase the existing answer and write a new answer in. This can be time consuming for a template with 8 bubble row choices per answer. This also increases the probability that the student will make a mistake in the process. Addressing this problem it is determined that two additional options needs to be made available. Firstly the student is allowed to cross out answers instead of totally erasing them. An example of this can be seen in Figure 2.2. Then secondly the system needs to be accurate enough to determine the student's student number only by filling in the character blocks above the bubbles. This requirement will be addressed by using a PGM in Section 4.2.4. Using optical character recognition (OCR), the bubble information and character information can thus be cross-referenced in an intelligence way and will be implemented in Section 4.2.

2.2.1 Contour detection

To determine if an answer in a bubble is truly colored in and not just crossed out, contour detection is needed. This means that the contour around the bubble needs to be detected and used in analysis. In python this can be implemented using the freely available OpenCV library, as referenced in Rosebrock (2016). OpenCV is an image processing library has has highly optimized techniques to find contours in a given image. With this information each bubble can be assessed not only by the pixels inside it, but also its shape. (Verander die image dalk na een wat 'n contour om het)

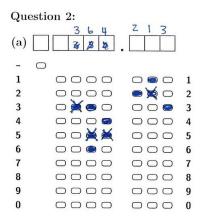


Figure 2.2: Example answer from student

2.2.2 Character recognition

To further increase the accuracy of the system, Optical Character Recognition (OCR) software will also be need and applied on the characters blocks, present on the templates. Researched shows that one preferred way of doing OCR is using TensorFlow. This method is described in Google (2017). TensorFlow is also a python library, but allows the build of instructions to be implemented in efficient c++ code. For this test grader, TensorFlow will be used to setup a convolutional neural network. This network will read an image, containing the digit, and predict the probability of each digit.

2.3 Conclusion: System requirements

In conclusion it can be seen that the system will need to incorporate a combination of image processing(OMR) on the bubbles and character recognition on the digits, handwritten by the students. Combined this evidence an more accurate result can be estimate, while also improving the convenience for students writing these test.

Chapter 3

Image Processing

The previous chapter focused on already existing methods of grading tests automatically. It was found that most systems only use image processing, without a machine learning component, to grade these test. In this chapter the core techniques behind processing these answer sheets, using image processing, will be described. By using only these image processing techniques a reasonably accurate system can already be constructed.

For further improvements in accuracy two machine learning approaches will be investigate and implemented. These approaches will be discussed in Chapter 4.

3.1 Orientation Detection

As mentioned in Section 2.1.1 there are two main steps in OMR grading. The first challenge with grading a scanned in answer sheet, is finding the orientation of the template in the image. This can be done by finding five values, including the rotation, offset(xOff,yOff) and a reference point(xRef,yRef). In Chapter 2 it was determined that the common way to find this orientation is to include specific reference blocks as markers on the page. A disadvantage with this method is that if their is to little markers on the page, the student might accidentally write over them or write something that resembles a marker and confuse the system. The template also looks less attractive if there is many markers. To compensate for this the markers that will be chose, are already present on the template paper. They are the two longest horizontal lines as well as the two vertical lines on the comment box. Together these lines have enough

information to determine the rotation, offset and size of the template. The reason these lines are chosen as references, are due to the fact that a Radon transform can easily be applied to determine where they are, as seen in Section 3.1.2. But before the orientation of the image can be determined it is a good idea to quickly check if the image might be upside down. This is done to make it easier to find the orientation afterwards. To do this some initial image filtering will be required and will be discussed next.

3.1.1 Initial filtering and orientation detection

To check if and image is upside down the software first needs to find relevant contours on the page. The contours are then filtered out if it does not loosely match the characteristics of a bubble or character block. This is done in 5 steps:

- 1. Threshold the image by making all the pixel values either white(lower that the mean) or black(higher that the mean)
- 2. Do contour analysis on the image to find all the contours, using the python library OpenCV.
- 3. Filter through the contour array to filter out all contours that are not approximately the size and aspect ratios desired.
- 4. Save these contours for later use.
- 5. Determine if more contours lie above the middle of the image (This is true if the image is the right way around). Rotate the image by 180° otherwise.

It is important to note that there are still unwanted contours in the list, but for now this list will be sufficient. Once the list is found the software counts the number of contour centerpoints below and above the image center. Figure 3.1 shows the resulting contours found in the image. As can be seen in the figure more bubbles should be below the horizontal center line, for the image to be the right side up. The next step will now be to determine the coordinates of the answers the student wrote down. To do this the template must first be found in the image. This will now be done in Section 3.1.2.

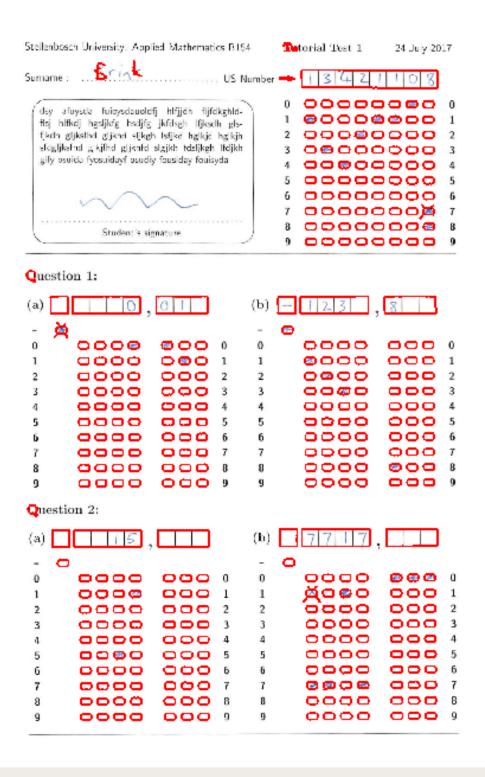


Figure 3.1: Reduced contours in image.

3.1.2 Radon Transform

The Radon transform is an integral transform that converts an 2 dimensional image into a 1 dimensional array. An example of this transform can be seen in Figure 3.2. This transform is always done over a chosen axis. In this case we will chose the horizontal axis to sum over. By counting up all the pixel values, each in the range 0.0 to 1.0,that corresponds to the same horizontal row a single sum value is calculated. By repeating this process for each row an resulting 1 dimensional array is created. This array provides information about the total pixel concentration on each horizontal line. In the case of the test grader, this can be used to identify where the lines on the pages are, by looking at the maximum values. By slightly rotating the axis over which the Radon transform is calculated new arrays can be calculated. Black lines will cause big values to appear on the Radon transform, when summing parallel with that line. After the correct angle is found the image gets rotated to correct for this angle offset.

3.1.3 Finding the template

Once the image is rotate correctly the two maximum values of the radon transform will indicate the two horizontal lines in the template. Using those two lines the relative size of the template in the image and y-offset value can be determined. The last step is thus to determine the x-offset value of the template. To do this a vertical Radon transform is applied to detect the two vertical lines of the comment box. This will provide the last x-offset value needed to find the template inside the image as well as additional size evidence to confirm the previously calculated size estimate. Once the template is found the bubble values and digit blocks can be determined, using reference location. These reference locations were calculated in preprocessing done on an empty template. Figure 3.3 illustrates the final estimation of all the bubbles in the template. The estimated bubble centers are colored red, while the green points represent the centers of all the remaining contours. (Stel dalk beter en duideliker)

In Figure 3.4 The final rotation after applying consecutive Radon transforms can be seen

In the next step a contour will be assigned to each bubble and then stored.

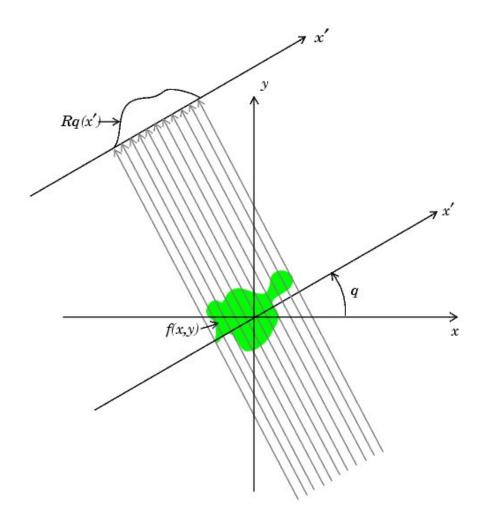


Figure 3.2: Radon transform applied on a 2 dimensional area, Edoras (2017)

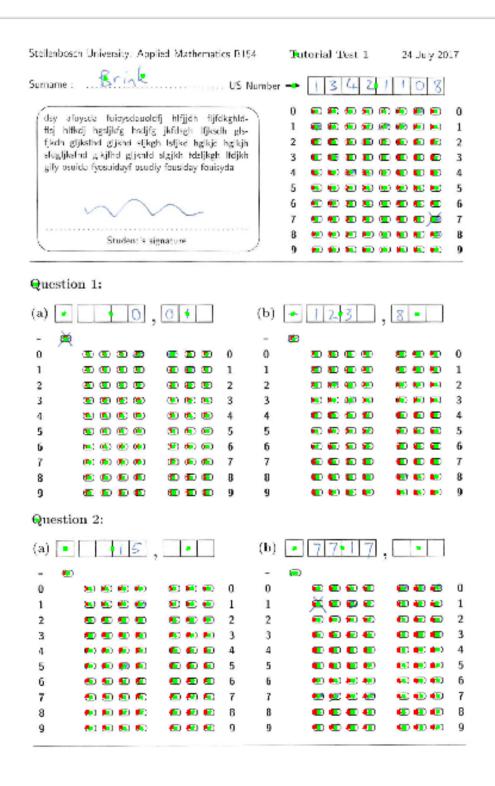


Figure 3.3: Detection of template in image and estimation of bubble locations.

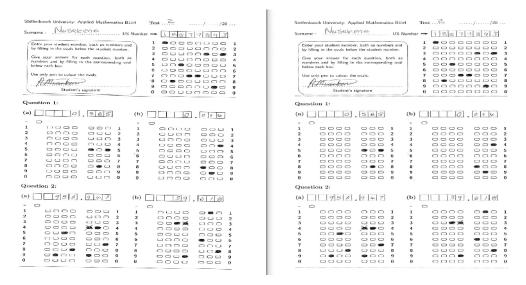


Figure 3.4: Result in rotation after applying radon transform.

3.2 Bubble detection and processing

To find the location of each bubble in the image, the system simply takes the contour closest to the estimated bubble location. This can be done in an efficient manner by sorting the contours by there locations. Searching through the contours now becomes linear and of complexity O(n), where n is the number of bubbles. This means that the processing time to find these bubbles is linearly related to the number of bubbles in the template image. Next the data in each contour needs to be processed and stored. The first type of evidence is calculating the average pixel intensity inside the contours. If this value is high the bubble is most likely colored in or crossed out. The advantage of using the closest contour as the bubble's estimated location, over conventional methods now becomes apparent. In conventional methods an estimated area is calculated where the bubble is most likely to be located. This becomes problamatic if the system needs to know if the bubble has been crossed out, as only data about pixel intensities are present. Using contour analysis information about the shape of the bubble entry is also provided. Thus by drawing the smallest possible block around the contour, that still covers every value inside the contour, an area can be calculated. This area will become large when a answer is crossed out, due to the lines stretching outside the initial bubble. By inspecting the area value, the system can successfully determine if the bubble is filled-in and crossed out.

3.3 Data processing and grading

The previous section now allows each bubble to be classified into 3 categories namely, empty, completely filled-in and crossed out. An additional category of partially filled-in will also be introduced, as it aids grading of tests where students write lightly. An algorithm to determine what bubble was chosen can now be described as follows:

- 1. Count the number of completely filled-in answers in each column. Store the position of that entry for later use.
- 2. If there are no completely filled-in answers, count the amount of partially filled-in answers and override the previous values.
- 3. If the previous result is 0, set the output value for that column to 0.
- 4. If step 2 or 3 presents a value greater that 1, save the answer sheet to a clashlist to be evaluated manually once the automatic grading of the test are completed.

3.4 Conclusion

This chapter provided an overview of a basic automatic test grading system using image processing and computer vision. The system can achieve acceptable results using only these techniques.

The following chapter will focus on applying additional machine learning techniques to further improve the accuracy of grading these test. Two new test templates will also be introduced. (maak seker jy het daaroor gepraat).

Chapter 4

Machine learning approach

The previous chapter briefly described the basic workings of the optical mark recognition (OCR) system inside the automatic test grader. There is still one critical piece of information that has not been observed in the system. This information is the characters that the student writes into the designated boxes.

This next chapter will provide two machine learning approaches to significantly improve the accuracy of the system over the previous standalone basic system. Firstly an approach to locate and classify hand written characters, provided by the students, using a deep convolutional neural network(DCNN), will be described. A more accurate method in determining the true digit represented by the bubble and character evidence, using a probabilistic graphical model(PGM), will also be implemented. This PGM method will then allow for an integrated probabilistic approach to determine the true student number using the bubble as well as character evidence. It will be determined that the PGM is accurate enough to determine the student number by only using the character recognition information provided.

For a more detailed explanation on the DCNN used in this thesis, refer to Appendix C.1.

4.1 Character recognition using a neural network

4.1.1 Introduction

An neural network is a powerful machine learning tool for approximating complex functions. The basic architecture of a neural network can be seen in Figure 4.1. The

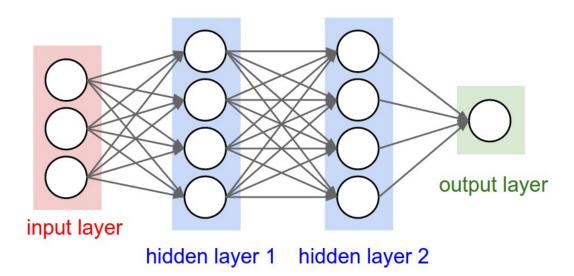


Figure 4.1: Basic structure of an neural network, Karpathy (2017)

structure of an feed-forward neural network consist of an input, hidden and output layer, as described in Nielsen (2015). A artificial neural network(ANN) is a simplified approximation of how neurons in the brain works. Each neuron in the network acts as a small processing unit. The final output can thus be collected by reading the value at the output layer after it has been passed each layer of the network.

For this thesis a neural network will be trained to predict what digit, from 0 to 9, is most likely present in a image. Figure 4.2 illustrates the input of of the neural network using and 14 by 14 example image. For this thesis a 28 by 28 greyscalled image will be used as input. Thus if each pixel represents one value, ranging from 0.0 to 1.0, there is total of 748 input values.

4.1.2 Neural Network Basics

4.1.2.1 The artificial neuron

The neuron unit takes in decimal values as input. The first step is then to calculate the weighted sum of these inputs, as shown in, Equation 4.1. Where c is the number of inputs. x_i and w_i respectively are the input and weight values at index i.

$$z = \sum_{i=0}^{c} x_i * w_i \tag{4.1}$$

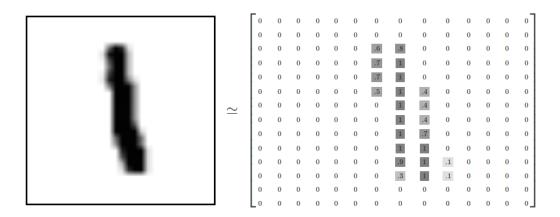


Figure 4.2: Example image used as input to the neural network, Tensorflow (2017)

The summed value then gets normalize using an sigmoid function, seen in Equation 4.2.

$$Out(z) = \frac{1}{1 + e^{-z}} \tag{4.2}$$

This artificial neuron thus basically takes in a weighted input and produces a normalized out. By adjusting the weights, certain inputs will excite and others inhibit the output of the neuron more. This process thus allows different functions to be approximated by changing these weights. If a network of these neurons gets place together, shown in Figure 4.1, complex functions can be trained onto the network. These weights variables thus needs to be tuned to specific values, to allow the network to best categorize digits given an image. The process of calculating values for these weights will be covered in Section sec:trainNN.

4.1.2.2 Getting a output from the network

After the 748 input values have been assigned to the network inputs, each of the network's coulombs can be calculated one at a time. The first coulomb in the hidden layer will thus use the 748 input values and produce a normalize output for each of the neurons in that coulomb. This is done using using the previously mentioned equations 4.1 and 4.2. Once the first column's outputs are calculated the next column can be calculated. This process is repeated until all the columns are calculated in the hidden

layer. The output layer is then calculated using the same method. For the character recognition in the test grader, 10 output neurons will be used, corresponding to the probability of the 10 digits being present. The values observed on the output neurons, gets normalized and used as the probability of each digit being present, using Equation 4.3. Where prob(i) is the probability of digit i being the character in the image. The value $Out(z_i)$ us the output of the output neuron at index i.

$$prob(i) = \frac{Out(z_i)}{\sum_{k=0}^{10} Out(z_k)}$$

$$(4.3)$$

4.1.2.3 Training of neural network

To train a neural network the MNIST dataset will be used. This is a database that has a labeled training set of 60,000 images, and a labeled test set of 10,000 images. The neural network will be trained using the training set. The basic idea behind the training method used in a neural network will be described in the following steps. For a more detailed description refer to Appendix C.

- 1. Calculate the network's output for each of the training images used in this training round.
- 2. Get the error margin of the network, using a formula that compares the true label of the training image, with the estimated label of the network.
- Calculate the value with which each weight should be changed to reduce the error margin. One method of doing this is using the gradient decent with back propagation algorithms.
- 4. Repeat steps 1-3 until a time or accuracy criteria is met.

4.1.3 Preprocessing on image

For the neural network to be able to classify digits from a 28 by 28 image, those subimages must first be found inside the test image. To do this Image processing is required. This is done in 6 steps as seen below: (Kry images by items om beter te lyk)

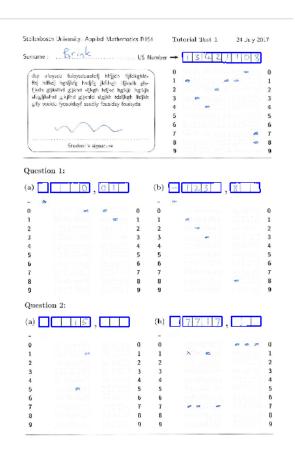


Figure 4.3: Image scanned for character areas.

- 1. Find the contour closest to the expected location of the block, calculated in Section 3.1.3. This is ilustrated in Figure 4.3. The bubbles have already been filter out of the image in a previous process.
- 2. Transform the image to become fully rectangle using OpenCv's four_point_transform method. This method applies a four point perspective transform on the image to reshape it into a rectangular form. An example of the final product can be seen in Figure 4.4.
- 3. Do a horizontal and vertical Radon transform, Section 3.1.2, to find and remove the dark box lines on the image, as seen in Figure 4.5.
- 4. Use the values received from the Radon transform to segment the image into the different boxes.

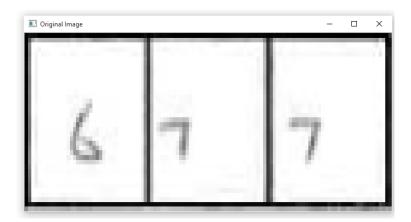


Figure 4.4: The found box is then normalized to rectangular shape.

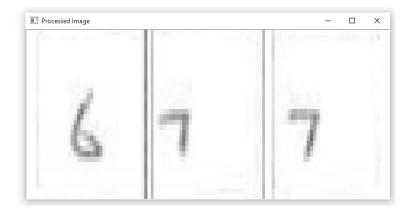


Figure 4.5: a Randon transform then gets applied.



Figure 4.6: An clustering algorithm is used to find the main cluster in the remaining image.



Figure 4.7: Area of found cluster.

- 5. Using a custom segmentation algorithm, find the pixels most likely to belong to the digit, as seen in Figure 4.6.
- 6. Locate the area the pixels are located in, as seen in Figure 4.7
- 7. Now calculate the center of the pixels, recenter and normalize the image area, as seen in Figure 4.8
- 8. Finally reshape the image into an 28 by 28 greyscalled image to be processed by the neural network.

Each box on the image can now be classified by the neural network and saved. The new character recognition evidence can now be used in combination with the bubble evidence to make a significantly more accurate estimate for the intended answers from the student. The next step is thus to combine all these individual evidence, in a intelligence way, to make a accurate prediction. A method to achieve this result will be covered in the next section.



Figure 4.8: Final translation and normalization of image.

4.2 Probabilistic Graphical Models

The final step in determining the students answers is to probabilistic determining the most likely answers, given all the evidence presented. To do this a probabilistic graphical model(PGM) will be developed.

4.2.1 Structure of the graph

a Probabilistic graphical model(PGM) is a probabilistic graph containing random variables, where the graph expresses the conditional independence structure between these variables. The type of PGM used for this project is a Bayesian network. A Bayesian network models a set of random variables and their conditional dependencies via a directed acyclic graph (DAG). As seen in Figure 4.9, arrows are used to indicate which variables are conditionally dependent on another.

The figure should be interpreted in the direction which information flows. Originally a student has a certain digit that he/she wants to portray on the page. This is given by the 'Digit user intended bubble'. There are 10 possible digits to consider and thus the bubble has 10 possible states. The intended digit gives rise to the intended bubbles and character that the student wants to write down. The student might sometimes mistakenly think that the first bubble represents 0 and thus even if the intended digit is 0 the intended bubble might be 1. Thus, this must also be done in a probabilistic manner to compensate for this uncertainty. The intended bubbles and character then produces evidence, as seen in Figure 4.9.

When looking at Figure 4.10, it is observed that there are 11 evidence areas to consider. They are the 10 bubbles and the character block. The process of writing

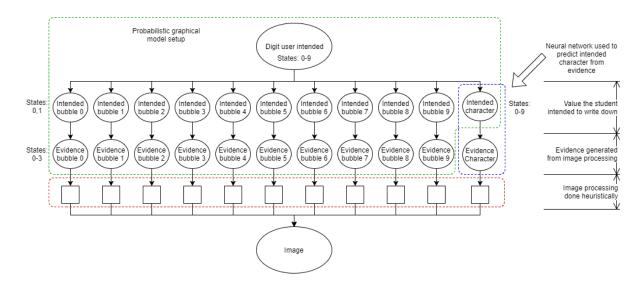


Figure 4.9: Graphical setup of digit generation.

down this digit introduces so noise into the system, due to the fact the student is not always going to write down the digit in exactly the same way. Thus the evidence is also probabilistically linked to the 'intended bubble' and 'intended character' parent distribution. This evidence then gets written down on the paper and is what ultimately influences how the image looks. Each of the bubbles can take one of 4 states as evidence. These states are blank, crossed-out, partially colored in and fully colored in. The character block evidence is an 28 by 28 greyscale image. Thus it can have 28*28*256 possible states, where 256 is the possible pixel intensities of each pixel. This value with true range 0 to 256, gets converted into a normalized value between 0.0 and 1.0 when the neural network needs to process it.

4.2.2 Determining the intended digit

After the model is constructed the intended digit needs to be estimated, given the image. Thiss can be done by reasoning from the bottom(image evidence) upwards to the intended digit. The first step is to process the image that produces the evidence using of image processing. Producing the bubble evidence from the image is described in Chapter 3. In 4.1.3, the process to extract the character evidence from the image was also described. Using the neural network the probability of intended character can be determined. After these steps have been completed the intended digit can be



Figure 4.10: Column representing one digit.

determined using the PGM, shown in Figure Figure 4.9. Thus is done by first setting the evidence node to the values calculated when image processing were done on them. The 'intended character' node then gets set to priors calculated through the use of the neural network. After this is done inference is done on the PGM and the resulting probability of each digit is calculated for the 'intended digit node'.

4.2.3 Training the model

This subsection still needs to be completed.

As seen in Figure 4.9,the PGM will include the bubble evidence as well as a prior probability that the neural network provides as evidence. Once these values are assigned, the PGM model will infer the intended digit using the probability distribution specified. To do this the conditional probabilities of the PGM, must first be determined from data. This is done by simple.. to be continued.

4.2.4 Student number identification

To be continued..

4.3 Conclusion

This chapter looked at two machine learning techniques to improve the accuracy with with the system infers the answers written on each scanned test sheet. A method was shown, using a neural network, to estimate the probability of each digit given only the character box as input. Additionally a approach was discussed, using a PGM, to allow

the system to make a final prediction of what the student intended to write down given the bubble and character boxes as evidence.

The following chapter will cover the validation and results of the system from weekly grading done for the Applied mathematics department.

Chapter 5

Analysis of results

This still needs to be written up.

Document the accuracy of the system before and after the machine learning components have been added. Compare the results.

5.1 Future improvements

Increase speed of test. Use the Radon transform to locate circles. Then do image processing only on that areas. No need for contour finding on the whole image.

Chapter 6

Summary and conclusions

This section still needs to be written up.

6.1 Project summary

6.2 How this final year project benefits society

Must say something here. Also say something about ethics, how you realised that your work may have an impact on the environment (or not), etc.

6.3 What the student learned

During the execution of this project, the student learned that time management is important, because ... Also, using LATEX is of cardinal importance to professionally typeset a report.

6.4 Conclusion: Summary and conclusions

This chapter provided a summary of the objectives, methodology and results of the final year project....

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Appendix A

Graphical overview of system as a whole

This is a graphical overview of the entire system.

Appendix B

Mathematical derivation of system as a whole

This appendix introduces and contains a probabilistic mathematical derivation that describes the overall workings of this system.

Appendix C

${\bf Implementation/Algorithms}$

Algorithms used in this project.

C.1 Deep Convolutional Neural Network

Appendix D

Validation and results

Validation and results of this system.

Appendix E

Project plan

The final year project plan is shown in Figure E.1. This idea of this Gantt chart plan was to give the student an indication of the progress of the final year project. It was last updated as a final adjustment to the project report.

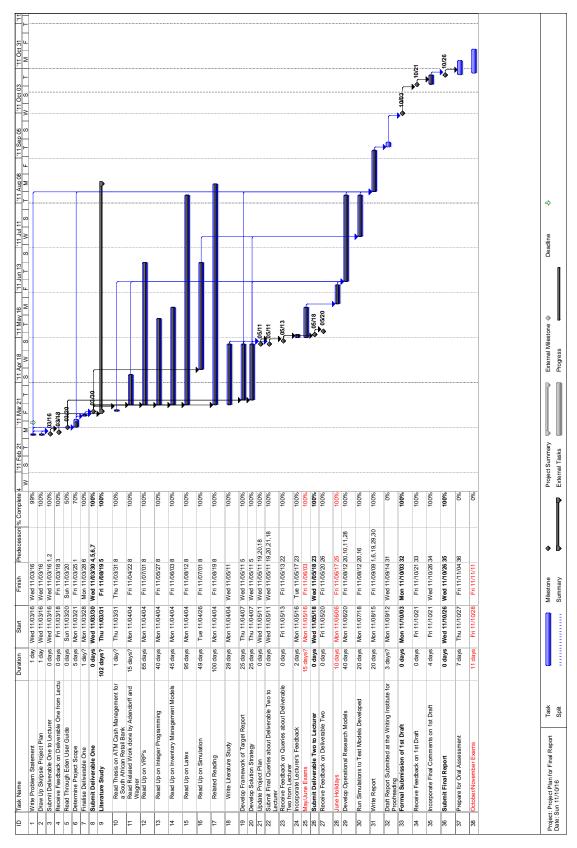


Figure E.1: Project plan for the final year project.