

# Calculus

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# 1 Derivatives

## 1.1 Definition

If the derivative is defined to be  $y = f(x)$ , then its derivative is  $f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$ .

Equivalent notations for the derivative of  $y = f(x)$  are:

$$f'(x) = y' = \frac{df}{dx} = \frac{dy}{dx} = \frac{d}{dx}(f(x)) = Df(x)$$

Equivalent notations for the the derivative of  $y = f(x)$  evaluated at  $x = a$  are:

$$f'(a) = y' \Big|_{x=a} = \frac{df}{dx} \Big|_{x=a} = \frac{dy}{dx} \Big|_{x=a} = Df(a)$$

## 1.2 Properties

The following properties hold where  $f(x)$  and  $g(x)$  are differential functions and  $c$  and  $n$  are any real numbers.

1.  $(cf)' = cf'(x)$
2.  $(f \pm g)' = f'(x) \pm g'(x)$
3.  $(fg)' = f'g + fg'$
4.  $\left(\frac{f}{g}\right)' = \frac{f'g - fg'}{g^2}$
5.  $\frac{d}{dx}(c) = 0$
6.  $\frac{d}{dx}(x^n) = nx^{n-1}$
7.  $\frac{d}{dx}(f(g(x))) = f'(g(x))g'(x)$

## 1.3 Common Derivatives

$$\frac{d}{dx}(x) = 1$$

$$\frac{d}{dx}(\sin x) = \cos x$$

$$\frac{d}{dx}(\cos x) = -\sin x$$

$$\frac{d}{dx}(\tan x) = \sec^2 x$$

$$\frac{d}{dx}(\sec x) = \sec x \tan x$$

$$\frac{d}{dx}(\csc x) = -\csc x \cot x$$

$$\frac{d}{dx}(\cot x) = -\csc^2 x$$

$$\frac{d}{dx}(\sin^{-1} x) = \frac{1}{\sqrt{1-x^2}}$$

$$\frac{d}{dx}(\cos^{-1} x) = -\frac{1}{\sqrt{1-x^2}}$$

$$\frac{d}{dx}(\tan^{-1} x) = \frac{1}{1+x^2}$$

$$\frac{d}{dx}(a^x) = a^x \ln(a)$$

$$\frac{d}{dx}(e^x) = e^x$$

$$(\ln(x))' = \frac{1}{x}, x > 0$$

$$\frac{d}{dx}(\ln|x|) = \frac{1}{x}, x \neq 0$$

$$\frac{d}{dx}(\log_a(x)) = \frac{1}{x \ln a}, x > 0$$