

Using nested classes as associated types.

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Abstract

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1 Introduction

Associated types are a powerful form of generics, now integrated in both Scala and Rust. They are a new kind of member, like methods fields and nested classes. Associated types behave as 'virtual' types: they can be overridden, can be abstract and can have a default. However, the user has to specify those types and their concrete instantiations manually; that is, the user have to provide a complete mapping from all virtual type to concrete instantiation. When the number of associated types is small this poses no issue, but it hinders designs where the number of associated types is large. In this paper we examine the possibility of completing a partial mapping in a desirable way, so that the resulting mapping is sound and also robust with respect to code evolution.

The core of our design is to reuse the concept of nested classes instead of relying of a new kind of member for associated types. An operation, call Redirect, will redirect some nested classes in some external types. To simplify our formalization and to keep the focus on the core of our approach, we present our system on top of a simple Java like languages, with only final classes and interfaces, when code reuse is obtained by trait composition instead of conventional inheritance. We rely on a simple nominal type system, where subtyping is induced only by implementing interfaces; in our approach we can express generics without having a polymorphic type system. To simplify the treatment of state, we consider fields to be always instance private, and getters and setters to be automatically generated, together with a `static` method `of(..)` that would work as a standard constructor, taking the value of the fields and initializing the instance. In this way we can focus our presentation to just (static) methods, nested classes and implements relationships. Expanding our presentation to explicitly include visible fields, constructors and sub-classing would make it more complicated without adding any conceptual underpinning. In our proposed setting we could write:

```
String=...
SBox={String inner;
  method String inner(){..} //implicit
  static method SBox of(String inner){..} //implicit
myTtrait={
  Box={Elem inner} //implicit Box(Elem inner) and Elem inner()
  Elem={Elem concat(Elem that)}
  static method Box merge(Box b, Elem e){return Box.of(b.inner().concat(e));}
}
Result=myTrait<Box=SBox> //equivalent to trait<Box=SBox, Elem=String>
...Result.merge(SBox.of("hello "), "world");//hello world
```



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48 Here class **SBox** is just a container of **Strings**, and **myTrait** is code encoding **Boxes** of any kind
49 of **Elem** with a **concat** method. By instantiating **myTrait<Box=SBox>**, we can infer **Elem=String**,
50 and obtain the following flattened code, where **Box** and **Elem** has been removed, and their
51 occurrences are replaced with **SBox** and **String**.

```
52 Result={static method SBox merge(SBox b,String e){  
53     return SBox.of(b.inner().concat(e));}  
54 }
```

56 Note how **Result** is a new class that could have been written directly by the programmer,
57 there is no trace that it has been generated by **myTrait**. We will represent trait names with
58 lower-case names and class/interface names with upper-case names. Traits are just units of
59 code reuse, and do not induce nominal types.

60 We could have just written **Result=myTrait<Elem=String>**, obtaining

```
61 Result={  
62     Box={String inner}  
63     static method Box merge(Box b,String e){  
64         return Box.of(b.inner().concat(e));}  
65 }
```

67 Note how in this case, class **Result.Box** would exist. Thanks to our decision of using nested
68 classes as associated types, the decision of what classes need to be redirected is not made
69 when the trait is written, but depends on the specific redirect operation. Moreover, our
70 redirect is not just a way to show the type system that our code is correct, but it can change
71 the behaviour of code calling static methods from the redirected classes.

72 This example shows many of the characteristics of our approach:

- 73 ■ (A) We can redirect mutually recursive nested classes by redirecting them all at the
74 same time, and if a partial mapping is provided, the system is able to infer the complete
75 mapping.
- 76 ■ (B) **Box** and **Elem** are just normal nested classes inside of **myTrait**; indeed any nested
77 class can be redirected away. In case any of their (static) methods was implemented, the
78 implementation is just discarded. In most other approaches, abstract/associated/generic
79 types are special and have some restriction; for example, in Java/Scala static methods
80 and constructors can not be invoked on generic/associated types. With redirect, they are
81 just normal nested classes, so there are no special restrictions on how they can be used.
82 In our example, note how **merge** calls **Box.of(..)**.
- 83 ■ (C) While our example language is nominally typed, nested classes are redirected over
84 types satisfying the same structural shape. We will show how this offers some advantages
85 of both nominal and structural typing.

86 A variation of redirect, able to only redirect a single nested class, was already presented
87 in literature. While points (B) and (C) already apply to such redirect, we will show how
88 supporting (A) greatly improves their value.

89 The formal core of our work is in defining

- 90 ■ **ValidRedirect**, a computable predicate telling if a mapping respects the structural shapes
91 and nominal subtype relations.
- 92 ■ A formal definition of what properties a procedure expanding a partial mapping into a
93 complete one should respect.
- 94 ■ **ChoseRedirect**, an efficient algorithm respecting those properties.

95 We first formally define our core language, then we define our redirect operator and its
96 formal properties. Finally we motivate our model showing how many interesting examples of
97 generics and associated types can be encoded with redirect. Finally, as an extreme application,
98 we show how a whole library can be adapted to be injected in a different environment.

2 Language grammar and well formedness

$e ::= x \mid e.m(es) \mid T.m(es) \mid e.x \mid \text{new } T(es)$	expression	$T ::= \text{This}n.Cs$	types
$L ::= \{ \text{interface } Tz; Mz \mid \{ Tz; Mz; K \}$	code literal	$Tx ::= T x$	parameter
$M ::= \text{static? } T m(Txs) e? \mid \text{private? } C=E$	member	$D ::= id=E$	declaration
$K ::= \langle Txs \rangle?$	state	$id ::= C \mid t$	class/trait id
$E ::= L \mid t \mid E_1 <+ E_2 \mid E < Cs = T >$	Code Expr.	$v ::= \text{new } T(vs)$	value

We apply our ideas on a simplified object oriented language with nominal typing and (nested) interfaces and final classes. Instead of inheritance, code reuse is obtained by trait composition, thus the source code would be a sequence of top level declarations D followed by a main expression; a lower-case identifier t is a trait name, while an upper case identifier C is a class name. To simplify our terminology, instead of distinguishing between nested classes and nested interfaces, we will call *nested class* any member of a code literal named by a class identifier C . Thus, the term *class* may denote either an *interface class* (interface for short) or a *final class*.

In the context of nested classes, types are paths. Syntactically, we represent them as relative paths of form $\text{This}n.Cs$, where the number n identify the root of our path: $\text{This}0$ is the current class, $\text{This}1$ is the enclosing class, $\text{This}2$ is the enclosing enclosing class and so on. $\text{This}n.Cs$ refers to the class obtained by navigating throughout Cs starting from $\text{This}n$. Thus, $\text{This}0$ is just the type of the directly enclosing class. By using a larger than needed n , there could be multiple different types referring to the same class. Here we expect all types to be in the normalized form where the smallest possible n is used.

Code literals L serve the role of class/interface bodies; they contain the set of implemented interfaces Tz , the set of members Mz and their (optional) state. In the concrete syntax we will use **implements** in front of a non empty list of implemented interfaces and we will omit parenthesis around a non empty set of fields. A class member M can be a (private) nested class or a (static) method. Abstract methods are just methods without a body. Well formed interface methods can only be abstract and non-static. To facilitate code reuse, classes can have (static) abstract methods, code composition is expected to provide an implementation for those or, as we will see, redirect away the whole class. We could easily support private methods too, but to simplify our formalism we consider private only for nested classes. In a well formed code literal, in all types of form $\text{This}n.Cs.C.Cs'$, if C denotes a private nested class, then Cs is empty.

Expressions are used as body of (static) methods and for the main expression. They are variables x (including **this**) and conventional (static) method calls. Field access and **new** expressions are included but with restricted usage: well formed field accesses are of form **this**. x in method bodies and $v.x$ in the main expression, while well formed **new** expressions have to be of form **new This** $0(xs)$ in method bodies and of form v in the main expression. Those restrictions greatly simplify reasoning about code reuse, since they require different classes to only communicate by calling (static) methods. Supporting unrestricted fields and constructors would make the formalism much more involved without adding much of a conceptual difficulty. Values are of form **new** $T(vs)$.

For brevity, in the concrete syntax we assume a syntactic sugar declaring a static of method (that serve as a factory) and all fields getters; thus the order of the fields would induce the order of the factory arguments. In the core calculus we just assume such methods to be explicitly declared.

Finally, we examine the shape of a nested class: **private?** $C=E$. The right hand side is not just a code literal but a code composition expression E . In trait composition, the

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code expression will be reduced/flattened to a code literal L during compilation. Code expressions denote an algebra of code composition, starting from code literal L and trait names t , referring to a literal declared before by $t=E$. We consider two operators: conventional preferential sum $E_1 \leftarrow E_2$ and our novel redirect $E \leftarrow C_s = T$.

The compilation process consists in flattening all the E into L , starting from the innermost leftmost E . This means that sum and redirect work on LV s: a kind of L , where all the nested classes are of form $C=LV$. The execution happens after compilation and consist in the conventional execution of the main expression e in the context of the fully reduced declarations, where all trait composition has been flatted away. Thus, execution is very simple and standard and behaves like a variation of FJ with interfaces instead of inheritance, and where nested classes are just a way to hierarchically organize code names. On the other side, code composition in this setting is very interesting and powerful, where nested classes are much more than name organization: they support in a simple and intuitive way expressive code reuse patterns. To flatten an E we need to understand the behaviour of the two operators, and how to load the code of a trait: since it was written in another place, the syntactic representation of the types need to be updated. For each of those points we will first provide some informal explanation and then we will proceed formalizing the precise behaviour.

2.1 Redirect

Redirect takes a library literal and produce a modified version of it where some nested classes has been removed and all the types referencing such nested classes are now referring to an external type. It is easy to use this feature to encode a generic list:

```
list={
  Elem={}
  static This0 empty()= new This0(Empty.of())
  boolean isEmpty()= this.impl().isEmpty()
  Elem head()= this.impl.asCons().tail()
  This0 tail()=this.impl.asCons().tail()
  This0 cons(Elem e)=new This0(Cons.of(e, this.impl)
  private Impl={interface Bool isEmpty() Cons asCons()}
  private Empty={implements This1
    Bool isEmpty()=true Cons asCons()=../*error*/
    ()//() means no fields
  private Cons={implements This1
    Bool isEmpty()=false Cons asCons()=this
    Elem elem Impl tail }
  Impl impl
}
IntList=list<Elem=Int>
...
IntList.Empty.of().push(3).top()=4 //example usage
```

This would flatten into

```
list={/*as before*/
//IntList=list<Elem=Int>
IntList={
  //Elem={} no more nested class Elem
  static This0 empty()= new This0(Empty.of())
  boolean isEmpty()= this.impl().isEmpty()
  Int head()= this.impl.asCons().tail()
  This0 tail()=this.impl.asCons().tail()
  This0 cons(Int e)=new This0(Cons.of(e, this.impl)
  private Impl={interface Bool isEmpty() Cons asCons()}
  private Empty={/*as before*/}
```

```

198 private Cons={implements This1
199     Bool isEmpty()=false Cons asCons()=this
200     Int elem Impl tail }
201 Impl impl
202 }//everywhere there was "Elem", now there is "Int"
203

```

Redirect can be propagated in the same way generics parameters are propagate: For example, in Java one could write code as below,

```

206 class ShapeGroup<T extends Shape>{
207     List<T> shapes;
208     ..}
209 //alternative implementation
210 class ShapeGroup<T extends Shape,L extends List<T>>{
211     L shapes;
212     ..}
213

```

to denote a class containing a list of a certain kind of **Shapes**. In our approach, one could write the equivalent

```

217 shapeGroup={
218     Shape={implements Shape}
219     List=list<Elem=Shape>
220     List shapes
221     ..}
222

```

With redirect, `shapeGroup` follow both roles of the two Java examples; indeed there are two reasonable ways to reuse this code

Triangulation=`shapeGroup<Shape=Triangle>`, if we have a **Triangle** class and we would like the concrete list type used inside to be local to the **Triangulation**, or **Triangulation**=`shapeGroup<List=Triangles>`, if we have a preferred implementation for the list of triangles that is going to be used by our **Triangulation**. Those two versions would flatten as follow:

```

230 //Triangulation=shapeGroup<Shape=Triangle>
231 Triangulation={
232     List=/*list with Triangle instead of Elem*/
233     List shapes
234     ..}
235
236 //Triangulation=shapeGroup<List=Triangles>
237 //expands to shapeGroup<List=Triangles,Shape=Triangle>
238 Triangulation={
239     Triangles shapes
240     ..}
241

```

As you can see, with redirect we do not decide a priori what is generic and what is not in a class.

Redirect can not always succeed. For example, if we was to attempt `shapeGroup<List=Int>` the flattening process would fail with an error similar to a invalid generic instantiation. Subtype is a fundamental feature of object oriented programming. Our proposed redirect operator do not require the type of the target to perfectly match the structural type of the internal nested classes; structural subtyping is sufficient. This feature adds a lot of flexibility to our redirect, however completing the mapping (as happens in the example above) is a challenging and technically very interesting task when subtyping is took into account. This is strongly connected with ontology matching and will be discussed in the technical core of the paper later on.

2.2 Preferential sum and examples of sum and redirect working together

The sum of two traits is conceptually a trait with the sum of the traits members, and the union of the implemented interfaces. If the two traits both define a method with the same name, some resolution strategy is applied. In the symmetric sum¹ the two methods need to have the same signature and at least one of them need to be abstract. With preferential sum (sometimes called override), if they are both implemented, the left implementation is chosen. Since in our model we have nested classes, nested classes with the same name will be recursively composed.

We chose preferential sum since is simpler to use in short code examples.¹ Since the focus of the paper is the novel redirect operator, instead of the well known sum, we will handle summing state and interfaces in the simplest possible way: a class with state can only be summed with a class without state, and an interface can only be summed with another interface with identical methods signatures.

In literature it has been shown how trait composition with (recursively composed) nested classes can elegantly handle the expression problem and a range of similar design challenges. Here we will show some examples where sum and redirect cooperate to produce interesting code reuse patterns:

```
listComp=list<+{
  Elem:{ Int geq(Elem e)}// -1/0/1 for smaller, equals, greater
  static Elem max2(Elem e1, Elem e2)=if e1.geq(e2)>0 then e1, else e2
  Elem max(Elem candidate)=
    if This.isEmpty() then candidate
    else this.tail().max(This.max2(this.head(), candidate))
  Elem min(Elem candidate)=...
  This0 sort()=...
}
```

As you can see, we can *extends* our generic type while refining our generic argument: **Elem** of **listComp** now needs a **geq** method.

While this is also possible with conventional inheritance and F-Bound polymorphism, we think this solution is logically simpler than the equivalent Java

```
class ListComp<Elem extends Comparable<Elem>> extends LinkedList<Elem>{
  ../*body as before*/
}
```

Another interesting way to use sum is to modularize behaviour delegation: consider the following (not efficient for the sake of compactness) implementation of **set**, where the way to compare elements is not fixed:

```
set:{
  Elem:{}
  List=list<Elem=Elem>
  static This0 empty()= new This0(List.empty())
  Bool contains(Elem e)=../*uses eq and hash*/
  Int size()=..
  This add(Elem e)=...
  This remove(Elem e)=...
  Bool eq(Elem e1,Elem e2)//abstract
  Int hash(Elem e)//abstract
  List asList //to allow iteration
}
```

¹ symmetric sum is often presented in conjunction with a restrict operator that makes some methods abstract.

```

307 }
308 eqElem={
309   Elem={ Bool equals(Elem e)/*abstract*/}
310   Bool eq(Elem e1,Elem e2)=e1.equals(e2)
311 }
312 hashElem={
313   Elem={ Int hash(Elem e)/*abstract*/}
314   Int hash(Elem e)=e.hash()
315 }
316 Strings=(set<+eqElem<+eqHash)<Elem=String>
317 LongStrings=(set<+eqElem)<Elem=String> <+{
318   Int hash(String e)=e.size()
319 }//for very long strings, size is a faster hash
320

```

321 Note how $(\text{set}\langle +\text{eqElem}\langle +\text{eqHash}\rangle\langle \text{Elem}=\text{String}\rangle)$ is equivalent to $\text{set}\langle \text{Elem}=\text{String}\rangle\langle +\text{eqElem}\langle \text{Elem}=\text{String}\rangle\langle +\text{eqHash}\langle \text{Elem}=\text{String}\rangle\rangle$.

322 Consider now the signature `Bool equals(Elem e)`. This is different from the common signature `Bool equals(Object e)`. What is the best signature for `equals` is an open research question, where most approaches advise either the first or the second one. Our `eqElem`, as I wrote, can support both: `Strings` would be correctly defined both if `String.equals` signature has a `String` or an `Object` parameter. EXPAND on method subtyping.

327 2.3 Moving traits around in the program

328 It is not trivial to formalize the way types like `This1.A.B` have to be adapted so that when code is moved around in differed depths of nesting the refereed classes stay the same. To this aim we define a concept of program p , as a representation of the code as seen from a certain point inside of the source code.

329 The program p is the most interesting form of the grammar, used for virtually all reduction and typing rules. On the left of the `;` is a stack representing which (nested) declaration is currently being processed, the bottom (rightmost) DL represents the D of the source-program that is currently being processed. The right of the `;` represents the top-level declarations that have already been compiled, this is necessary to look up top-level classes and traits. That is, each of the $DL_0 \dots DL_n$ represents the outer nested level $0..n$, while the DVs component represent the already flattened portion of the program top level, that is the outer nested level $n + 1$.

330 $p ::= DLs; DVs$ program

331 $DL ::= id=L$ partially-evaluated-declaration

332 $DV ::= id=LV$ evaluated-declaration

333 $Mid ::= C \mid m$ member-id

334 Thus, for example in the program

```

342 A={}
343 t={ B={} } This1.A m(This0.B b)
344 C={D={E=t}}
345

```

346 the flattened version for `C.D.E` will be `{ B={} This3.A m(This0.B b)}`, where the path `This1.A` is now `This3.A` while the path `This0.B` stays the same. The program p in the observation point `E=t` is

```

350 A={}
351 t={ B={} } This1.A m(This0.B b)
352 C={D={E=t}};
353 C={D={E=t}},
354 D={E=t}
355

```

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357 To look up the value of a type in the program we will use the notation $p(T) = LV$, which is
 358 defined by the following:

$$(_; _, C = L, _)(\mathbf{This}0.C.Cs) := L(Cs)$$

$$359 \quad (id = L, DLS; DVs)(\mathbf{This}0.Cs) := L(Cs)$$

$$360 \quad (id = L, DLS; DVs)(\mathbf{This}n + 1.Cs) := DLS; DVs(\mathbf{This}n.Cs)$$

361 And a few simple auxiliary definitions:

$$Ts \in p := \forall T \in Ts \bullet p(T) \text{ is defined}$$

$$L(\emptyset) := L$$

$$362 \quad L(C.Cs) := L(Cs) \text{ where } L = \mathbf{interface?} \{ _; _, C = L, _; _ \}$$

$$L[C = E'] := \mathbf{interface?} \{ Tz; MVs C = E' Ms; K? \}$$

$$363 \quad \text{where } L = \mathbf{interface?} \{ Tz; MVs C = _ Ms; K? \}$$

364 To get the relative value of a trait, we define $p[T]$:

$$365 \quad (DLS; _, t = LV, _)[t] := LV[from \mathbf{This} \# DLS]$$

366

367 To get a the value of a literal, in a way that can be understand from the current location

368 $(\mathbf{This}0)$, we define:

$$369 \quad p[T] := p(T)[from T]$$

370

$$\mathcal{E}_V ::= \square \mid \mathcal{E}_V \leftarrow E \mid LV \leftarrow \mathcal{E}_V \mid \mathcal{E}_V \leftarrow Cs = T \quad \text{context of library-evaluation}$$

371

$$\mathcal{E}_v ::= \square \mid \mathcal{E}_v.m(es) \mid v.m(vs \mathcal{E}_v es) \mid T.m(vs \mathcal{E}_v es)$$

We have two top level reduction rules defining our language, of the form $Dse^{\sim\sim} > Ds'e$ which simply reduces the source-code. The first rule (*compile*) ‘compiles’ each top-level declaration (using a well-typed subset of already compiled top-level declarations), this reduces the defining expression. The second rule, (*main*) is executed once all the top-level declarations have compiled (i.e. are now fully evaluated class literals), it typechecks the top-level declarations and the main expression, and then proceeds to reduce it. In principle only one-typechecking is needed, but we repeat it to avoid declaring more rules.

```

379 Define Ds e --> Ds' e'
380 =====
381 DVs' |- Ok
382 empty; DVs'; id | E --> E'
383 (compile)----- DVs' subsetof DVs
384 DVs id = E Ds e --> DVs id = E' Ds e
385
386 DVs |- Ok
387 DVs |- e : T
388 DVs |- e --> e'
389 (main)----- for some type T
390 DVs e --> DVs e'

```

3 Compilation

Aside from the redirect operation itself, compilation is the most interesting part, it is defined by a reduction arrow $p; id | E \rightarrow E'$, the *id* represents the id of the type/trait that we are currently compiling, it is needed since it will be the name of *This0*, and we use that fact that that is equal to *This1.id* to compare types for equality. The (*CtxV*) rule is the standard context, the (*L*) rule propagates compilation inside of nested-classes, (*trait*) merely evaluates a trait reference to its defined body, (*sum*) and (*redirect*) perform our two meta-operations.

```

398 Define p; id | E --> E'
399 =====
400 p; id | E --> E'
401 (CtxV) -----
402 p; id | CtxV[E] --> CtxV[E']
403
404 id = L[C = E], p; C | E --> E'
405 (L) ----- // TODO use fresh C?
406 p; id | L[C = E] --> L[C = E']
407
408 (trait) -----
409 p; id | t -> p[t]
410
411 LV1 <+p' LV2 = LV3                                p' = C' = LV3, p
412 (sum) ----- for fresh C'
413 p; id | LV1 <+ LV2 --> LV3
414
415 // TODO: Inline and de-42 redirect formalism
416 (redirect) -----LV'=redirect(p, LV, Cs, P)
417 p; id | LV(Cs=P) -> LV'

```

4 The Sum operation

The sum operation is defined by the rule $L1 < +p L2 = L3$, it is unconventional as it assumes we already have the result ($L3$), and simply checks that it is indeed correct. We believe (but have not proved) that this rule is unambiguous, if $L1 < +p L2 = L3$ and $L1 < +p L2 = L3'$, then $L3 = L3'$ (since the order of members does not matter for Ls).

The main rule for summing of non-interfaces, sums the members, unions the implemented interfaces (and uses *minimize* to remove any duplicates), it also ensures that at most one of them has a constructor. For summing an interface with a interface/class we require that an interface cannot 'gain' members due to a sum. The actual L42 implementation is far less restrictive, but requires complicated rules to ensure soundness, due to problems that could arise if a summed nested-interface is implemented. Summing of traits/classes with state is a non-trivial problem and not the focus of our paper, there are many prior works on this topic, and our full L42 language simply uses ordinary methods to represent state, however this would take too much effort to explain here.

```

432 Define L1 <+p L2 = L3
433 =====
434 {Tz1; Mz1; K?1} <+p {Tz2; Mz2; K?2} = {Tz; Mz; K?}
435 Tz = p.minimize(Tz1 U Tz2)
436 Mz1 <+p Mz1 = Mz
437 {empty, K?1, K?2} = {empty, K?} //may be too sophisticated?
438
439 interface{Tz1; amtz,amtz';} <+p interface?{Tz2;amtz;} = interface {Tz;amtz,amtz';}
440 Tz = p.minimize(Tz1 U Tz2)
441 if interface? = interface then amtz'=empty

```

The rules for summing member are simple, we take two sets of members collect all the ones with unique names, and sum those with duplicates. To sum nested classes we merely sum their bodies, to sum two methods we require their signatures to be identical, if they both have bodies, the result has the body of the RHS, otherwise the result has the body (if present) of the LHS.

```

447 Define Mz <+p Mz' = Mz"
448 -----
449 M, Mz <+p M', Mz' = M <+p M', Mz <+p Mz
450 //note: only defined when M.Mid = M'.Mid
451
452 Mz <+p Mz' = Mz, Mz':
453 dom(Mz) disjoint dom(Mz')
454
455 Define M <+p M' = M"
456 -----
457 T' m(Txs') e? <+p T m(Txs) e = T m(Txs) e
458 T', Txs'.Ts =p Ts, Txs
459
460 T' m(Txs') e? <+p T m(Txs) = T m(Txs) e?
461 T', Txs'.Ts =p Ts, Txs
462
463 (C = L) <+p (C = L') = L <+p.push(C) L'

```

5 Type System

The type system is split into two parts: type checking programs and class literals, and the typechecking of expressions. The latter part is mostly conventional, it involves typing judgments of the form $p; Txs \vdash e : T$, with the usual program p and variable environment Txs (often called Γ in the literature). rule $(Dsok)$ type checks a sequence of top-level declarations by simply push each declaration onto a program and typecheck the resulting program. Rule pok typechecks a program by check the topmost class literal: we type check each of it's members (including all nested classes), check that it properly implements each interface it claims to, does something weird, and finanly check check that it's constructor only referenced existing types,

```
Define p |- Ok
```

```
=====
```

```
D1; Ds |- Ok ... Dn; Ds|- Ok
```

```
(Ds ok) ----- Ds = D1 ... Dn
```

```
Ds |- Ok
```

```
p |- M1 : Ok .... p |- Mn : Ok
```

```
p |- P1 : Implemented .... p |- Pn : Implemented
```

```
p |- implements(Pz; Ms) /*WTF?*/ if K? = K: p.exists(K.Txs.Ts)
```

```
(p ok) ----- p.top() = interface? {P1...Pn; M1, ..., Mn; K?}
```

```
p |- Ok
```

```
p.minimize(Pz) subseteq p.minimize(p.top().Pz)
```

```
amt1 _ in p.top().Ms ... amtn _ in p.top().Ms
```

```
(P implemented) ----- p[P] = interface {Pz; amt1 ... am
```

```
p |- P : Implemented
```

```
(amt-ok) ----- p.exists(T, Txs.Ts)
```

```
p |- T m(Tcs) : Ok
```

```
p; This0 this, Txs |- e : T
```

```
(mt-ok) ----- p.exists(T, Txs.Ts)
```

```
p |- T m(Tcs) e : Ok
```

```
C = L, p |- Ok
```

```
(cd-Ok) -----
```

```
p |- C = L : OK
```

Rule $(Pimplemented)$ checks that an interface is properly implemented by the program-top, we simply check that it declares that it implements every one of the interfaces super-interfaces and methods. Rules $(amt-ok)$ and $(mt-ok)$ are straightforward, they both check that types mensioned in the method signature exist, and ofcourse for the latter case, that the body respects this signature.

23:12 Using nested classes as associated types.

510 To typecheck a nested class declaration, we simply push it onto the program and typecheck
511 the top-of the program as before.

512 The expression typesystem is mostly straightforward and similar to feartherwiegth Java,
513 notable we we use $p[T]$ to look up information about types, as it properly ‘from’s paths, and
514 use a classes constructor definitions to determine the types of fields.

```
515 Define p; Txs |- e : T
516 =====
517 (var)
518 ----- T x in Txs
519 p; Txs |- x : T
520
521 (call)
522 p; Txs |- e0 : T0
523 ...
524 p; Txs |- en : Tn
525 ----- T' m(T1 x1 ... Tn xn) _ in p[T0].Ms
526 p; Txs |- e0.m(e1 ... en) : T'
527
528 (field)
529 p; Txs |- e : T
530 ----- p[T].K = constructor(_ T' x _)
531 p; Txs |- e.x : T'
532
533
534 (new)
535 p; Txs |- e1 : T1 ... p; Txs |- en : Tn
536 ----- p[T].K = constructor(T1 x1 ... Tn xn)
537 p; Txs |- new T(e1 ... en)
538
539
540 (sub)
541 p; Txs |- e : T
542 ----- T' in p[T].Pz
543 p; Txs |- e : T'
544
545
546 (equiv)
547 p; Txs |- e : T
548 ----- T =p T'
549 p; Txs |- e : T'
```

6 Graph example

551 We now consider an example where Redirect simplifies the code quite a lot: We have a **Node**
552 and **Edge** concepts for a graph. The **Node** have a list of **Edges**. A **isConnected** function takes
553 a list of **Nodes**. A **getConnected** function takes **Node** and return a set of **Nodes**.

```
554 graphUtils={
555   Edges:list<+{Node start() Node end()}
556
```

```

557 Node:{Edges connections()}
558 Nodes:set<Elem=Node> //note that we do not specify equals/hash
559 static Bool isConnected(Nodes nodes)=
560   if(nodes.size()==0) then true
561   else getConnected(nodes.asList().head()).size()==nodes.size()
562 static Nodes getConnected(Node node)=getConnected(node,Nodes.empty())
563 static Nodes getConnected(Node node,Nodes collected)=
564   if(collected.contains(node)) then collected
565   else connectEdges(node.connections(),collected.add(node))
566 static Nodes connectEdges(Edges e,Nodes collected)=
567   if( e.isEmpty()) then collected
568   else connectEdges(e.tail(),collected.add(e.head().end()))
569 }

```

We have shown the full code instead of omitting implementations to show that the code inside of an highly general code like the former is pretty conventional. Just declare nested classes as if they was the concrete desired types. Note how we can easily create a new Nodes@ by doing Nodes.empty().

Here we show how to instantiate graphUtils to a graph representing cities connected by streets, where the streets are annotated with their length, and Edges is a priority queue, to optimize finding the shortest path between cities.

```

578 Map:{
579   Street:{City start, City end, Int size}
580   City:{}
581   Streets:priorityQueue<Elem=Street><+{
582     Int geq(Street e1, Street e2)=e1.size()-e2.size()
583   }<+{
584     Streets:{}
585     City:{Streets connections, Int index} //index identify the node
586     Cities:set<Elem=City><+{
587       Bool eq(City e1, City e2) e1.index==e2.index
588       Int hash(City e) e.index
589     }
590     Cities cities
591     //more methods
592   }
593 }
594 MapUtils=graphUtils<Nodes=Map.Cities>
595 //infers Nodes.List, Node, Edges, Edge

```

In Appending 2 we will show our best attempt to encode this graph example in Java, Rust and Scala. In short, we discovered... - towel1:.. //Map: towel2:.. //Map: lib: T:towel1 f1 ... fn
MyProgram: T:towel2 Lib:lib[T=This0.T] ... -

7 extra

Features: Structural based generics embedded in a nominal type system. Code is Nominal, Reuse is Structural. Static methods support for generics, so generics are not just a trik to make the type system happy but actually change the behaviour Subsume associate types. After the fact generics; redirect is like mixins for generics Mapping is inferred-> very large maps are possible -> application to libraries

In literature, in addition to conventional Java style F-bound polymorphism, there is another way to obtain generics: to use associated types (to specify generic paramaters) and inheritance (to instantiate the paramaters). However, when parametrizing multiple types, the user to specify the full mapping. For example in Java interface A B m(); interface BString f(); class G<TA extends A<TB>, TB> //TA and TB explicitly listed String g(TA

612 a TB b) return a.m().f(); class MyA implements A<MyB>.. class MyB implements B ..
 613 G<MyA,MyB> //instantiation Also scala offers generics, and could encode the example in
 614 the same way, but Scala also offers associated types, allowing to write instead...

615 Rust also offers generics and associated types, but also support calling static methods
 616 over generic and associated types.

617 We provide here a foundational model for genericity that subsume the power of F-bound
 618 polymorphisms and associated types. Moreover, it allows for large sets of generic parameter
 619 instantiations to be inferred starting from a much smaller mapping. For example, in our
 620 system we could just write g= A= method B m() B= method String f() method String g(A a
 621 B b)=a.m().f() MyA= method MyB m()= new MyB(); .. MyB= method String f()="Hello";
 622 .. g<A=MyA> //instantiation. The mapping A=MyA, B=MyB

623 We model a minimal calculus with interfaces and final classes, where implementing an
 624 interface is the only way to induce subtyping. We will show how supporting subtyping
 625 constitute the core technical difficulty in our work, inducing ambiguity in the mappings.
 626 As you can see, we base our generic matches the structure of the type instead of respect-
 627 ing a subtype requirement as in F-bound polymorphisms. We can easily encode subtype
 628 requirements by using implements: Print=interface method String print(); g= A:implements
 629 Print method A printMe(A a1,A a2) if(a1.print().size()>a2.print.size())return a1; return a2;
 630 MyPrint=implements Print .. g<A=MyPrint> //instantiation g<A=Print> //works too

631 ————— example showing ordering need to strictly improve EI1: interface EA1: imple-
 632 ments EI1

633 EI2: interface EA2: implements EI2

634 EB: EA1 a1 EA1 a1

635 A1: A2: B: A1 a1 A2 a2 [B = EB] // A1 -> EI1, A2 -> EA2 a // A1 -> EA1, A2 ->

636 EI2 b // A1 -> EA1, A2 -> EA2 c

637 a <= b b <= a c <= a, b a <= c

638 hi Hi class

a ::= b c

639 a a hi Hi class q a a ::= b c

a ::= b c

640 } } [()]
 (TOP)

a \xrightarrow{b} c $\forall i < 3 a \vdash b : \text{OK}$

641
$$\frac{\forall i < 3 a \vdash b : \text{OK}}{1 + 2 \rightarrow 3} \begin{array}{l} a \\ b \\ c \end{array}$$