Dummy title

Authors omitted for double-bind review.
Unspecified Institution.

Abstract

Lorem ipsum dolor sit amet, consectetur adipiscing elit. Praesent convallis orci arcu, eu mollis dolor. Aliquam eleifend suscipit lacinia. Maecenas quam mi, porta ut lacinia sed, convallis ac dui. Lorem ipsum dolor sit amet, consectetur adipiscing elit. Suspendisse potenti.

2012 ACM Subject Classification Dummy classification

Keywords and phrases Dummy keyword

Digital Object Identifier 10.4230/LIPIcs.CVIT.2016.23

1 Introduction

`here` we examine and understand what it means for a mapping to be completed in a desirable way desarible means sound, but also maintenable

Associated types are a powerful form of generics, now integrated in both Scala and Rust. They are a new kind of member, like methods fields and nested classes. Associated types behave as 'virtual' types: they can be overridden, can be abstract and can have a default. However, the user has to specify those types and their concrete instantiations manually. We propose here a different design, where instead of relying on a new kind of member, we reuse the well known concept of nested classes. An operation, call Redirect, will redirect some nested classes in some external types. To simplify our formalization and to keep the focus on the core of our approach, we present our system on top of a simple Java like languages, with only final classes and interfaces, when code reuse is obtained by trait composition instead of conventional inheritance. For example, we could write:

```
String=...
SBox={String inner}
trait={
  Box={Elem inner}
  Elem={Elem concat(Elem that)}
  static method Box merge(Box b,Elem e){return new Box(b.inner.concat(e));}
  }
Result=trait<Box=SBox>//equivalent to trait<Box=SBox, Elem=String>
Result.merge(new SBox("hello "), "world");//hello world
```

Here class SBox is just a container of Strings, and trait is code encoding Boxes of any kind of Elem with a concat method. In our examples, we assume a constructor that is just initializing the fields is always present. We will also not consider any other kind of constructors. By instantiating trait<Box=SBox>, we can infer Elem=String, and obtain the flattened code

`{static method SBox merge(SBox b1,SBox b2){return new SBox(b1.inner.concat(b2.inner));}}`

where **`Box`** and **`Elem`** has been removed, and their occurrences are replaced with **`SBox`** and **`String`**. Note how **`Result`** is a new class that could have been written directly by the programmer. There is no trace that it has been generated by `trait`. Moreover, `trait` is just a unit of code reuse, and is not a nominal type.

This example show many of the characteristics of our approach:

- (A) We can redirect mutually recursive nested classes by redirecting them all at the same time, and if a partial mapping is provided, the system is able to infer the complete mapping.

- (B) `Box` and `Elem` are just normal nested classes inside of `trait`; indeed any nested class can be redirected away. In case any of their (static) methods was implemented, the implementation is just discarded. In most other approaches, abstract/associated/generic types are special and have some restriction; for example, in Java/Scala static methods and constructors can not be invoked on generic/associated types. With redirect, they are just normal nested classes, so there are no special restrictions on how they can be used. In our example, note how `merge` calls `new Box(..)`.
- (C) While our example language is nominally typed, nested classes are redirected over types satisfying the same structural shape. We will show how this offers some advantages of both nominal and structural typing.

A variation of redirect, able to only redirect a single nested class, was already presented in literature. While points (B) and (C) already applies to such redirect, we will show how supporting (A) greatly improve their value.

The formal core of our work is in defining

- `ValidRedirect`, a computable predicate telling if a mapping respect the structural shapes and nominal subtype relations.
- `ChoseRedirect`, an algorithm expanding a partial mapping into a complete one.
- And more importantly a formal definition of what properties we expect a good expanding procedure should respect, and we prove our `ChoseRedirect` respect those properties.

After formally defining our map expander, we show that such a feature can be very useful, by showing how may interesting examples of generics and associated types can be encoded with redirect, and as an extreme application, a whole library can be adapted to be injected in a different environment.

Features: Structural based generics embedded in a nominal type system. Code is Nominal, Reuse is Structural. Static methods support for generics, so generics are not just a trik to make the type system happy but actually change the behaviour Subsume associate types. After the fact generics; redirect is like mixins for generics Mapping is inferred-> very large maps are possible -> application to libraries

In literature, in addition to conventional Java style F-bound polymorphism, there is another way to obtain generics: to use associated types (to specify generic paramaters) and inheritence (to instantiate the paramaters). However, when parametrizing multiple types, the user to specify the full mapping. For example in Java interface A<B> B m(); inteface BString f(); class G<TA extends A<TB>, TB>//TA and TB explicitly listed String g(TA a TB b)return a.m().f(); class MyA implements A<MyB>.. class MyB implements B .. G<MyA,MyB>//instantiation Also scala offers genercs, and could encode the example in the same way, but Scala also offers associated types, allowing to write instead....

Rust also offers generics and associated types, but also support calling static methods over generic and associated types.

We provide here a fundational model for genericty that subsume the power of F-bound polimorphims and associated types. Moreover, it allows for large sets of generic parameter instantiations to be inferred starting from a much smaller mapping. For example, in our system we could just write g= A= method B m() B= method String f() method String g(A a B b)=a.m().f() MyA= method MyB m()= new MyB(); .. MyB= method String f()="Hello"; .. g<A=MyA>//instantiation. The mapping A=MyA,B=MyB

We model a minimal calculus with interfaces and final classes, where implementing an interface is the only way to induce subtyping. We will show how supporting subtyping constitute the core technical difficulty in our work, inducing ambiguity in the mappings.

As you can see, we base our generic matches the structor of the type instead of respecting a subtype requirement as in F-bound polymorphis. We can easily encode subtype requirements by using implements: Print=interface method String print(); g= A:implements Print method A printMe(A a1,A a2) if(a1.print().size()>a2.print.size())return a1; return a2; MyPrint=implements Print .. g<A=MyPrint> //instantiation g<A=Print> //works too

——— example showing ordering need to strictly improve EI1: interface EA1: implements EI1

EI2: interface EA2: implements EI2

EB: EA1 a1 EA1 a1

A1: A2: B: A1 a1 A2 a2 [B = EB] // A1 -> EI1, A2 -> EA2 a // A1 -> EA1, A2 -> EI2 b // A1 -> EA1, A2 -> EA2 c

a <=b b <=a c<= a,b a <= c

`hi` **`Hi`** `class`

$$aa\texttt{hi}\mathtt{\textbf{Hi}}\texttt{class}qaq \begin{array}{l} a ::= b \quad \text{c} \\ a ::= b \quad \text{c} \\ a ::= b \quad \text{c} \end{array}$$

`}}][()]`

$$\frac{\begin{array}{c}(\text{TOP})\\ a \underset{b}{\rightarrow} c \quad \forall i < 3a \vdash b : \text{OK} \\ \forall i < 3a \vdash b : \text{OK}\end{array}}{1 + 2 \rightarrow 3} \begin{array}{l} a \\ b \\ c \end{array}$$

2 Formal

$$
\begin{array}{rcll}
id & ::= & t \mid C & \\
T & ::= & \texttt{This}n.\,Cs & \\
CD & ::= & C\texttt{=}E & \text{class declaration} \\
CV & ::= & C\texttt{=}LV & \text{evaluated class declaration} \\
D & ::= & id\texttt{=}E & \text{declaration} \\
DL & ::= & id\texttt{=}L & \text{partially-evaluated-declaration} \\
DV & ::= & id\texttt{=}LV & \text{evaluated-declaration} \\
L & ::= & \texttt{interface}\,\texttt{\{}Tz\texttt{;}\ amtz\ \texttt{;}\ \texttt{\}} \mid \texttt{\{}Tz\texttt{;}\ Ms\ \texttt{;}\ K?\texttt{\}} & \text{literal} \\
LV & ::= & \texttt{interface}\,\texttt{\{}Tz\texttt{;}\ amtz\ \texttt{;}\ \texttt{\}} \mid \texttt{\{}Tz\texttt{;}\ MVs\ \texttt{;}\ K?\texttt{\}} & \text{literal value} \\
amt & ::= & T\ m\texttt{(}Txs\texttt{)} & \text{abstract method} \\
mt & ::= & T\ m\texttt{(}Txs\texttt{)}\ \ e? & \text{method} \\
Tx & ::= & T\ x & \text{paramater-declaration} \\
M & ::= & CD \mid mt & \text{member} \\
MV & ::= & CV \mid mt & \\
Mid & ::= & C \mid m & \text{member-id} \\
K & ::= & \texttt{constructor}\texttt{(}Txs\texttt{)} & \text{constructor} \\
e & ::= & x \mid e.\,m\texttt{(}es\texttt{)} \mid e.\,x \mid \texttt{new}\ \ T\texttt{(}es\texttt{)} & \text{expression} \\
E & ::= & L \mid t \mid E \texttt{<+}\ E \mid E\texttt{(}Cs\texttt{=}T\texttt{)} & \text{library-expression} \\
\mathcal{E}_V & ::= & \square \mid \mathcal{E}_V \texttt{<+}\ E \mid LV \texttt{<+}\ \mathcal{E}_V \mid \mathcal{E}_V\texttt{(}Cs\texttt{=}T\texttt{)} & \text{context of library-evaluation} \\
\mathcal{E}_v & ::= & \square \mid \mathcal{E}_v.\,m\texttt{(}es\texttt{)} \mid v.\,m\texttt{(}vs\ \mathcal{E}_v\ es\texttt{)} \mid \mathcal{E}_v.\,x \mid \texttt{new}\ \ T\texttt{(}vs\ \mathcal{E}_v\ es\texttt{)} & \\
v & ::= & \texttt{new}\ \ T\texttt{(}vs\texttt{)} & \\
p & ::= & DLs\texttt{;}\ DVs & \text{program} \\
S & ::= & Ds\ e & \text{source code}
\end{array}
$$

We use t and C to syntactically distinguish between trait and class names. A type (T) has an interesting syntax, see below for what it means. An E is a top-level class expression, which can contain class-literals, references to traits, and operations on them, namely our sum $E < +E$ and redirect $e(Cs = T)$. A declaration D is just an $id = E$, representing that id is declared to be the value of E, we also have CD, CV, DL, and DV that constrain the forms of the LHS and RHS of the declaration. A literal L has 4 components, an optional interface keyword, a list of implemented interfaces, a list of members, and an optional constructor. For simplicity, interfaces can only contain abstract-methods (amt) as members, and cannot have constructors. A member M, is either an (potentially abstract) methood mt or a nested class declaration (CD). A member value MV, is a member that has been fully compiled. An mid is an identifier, identifying a member. Constructors, K, contain a Txs indicating the type and names of fields. An e is normal fetherweight-java style expression, it has variables x, method calls $e.m(es)$, field accesses $e.x$ and object creation $newes$. $CtxV$ is the evalation context for class-expressions E, and $ctxv$ is the usuall one for e's.

An S represents what the top-level source-code form of our language is, it's just a sequence of declarations and a main expression. The most interesting form of the grammer is a p, it is a 'program', used as the context for many reductions and typing rules, on the LHS of the ; is a stack representing which (nested) declaration is currently being processed, the bottom

(rightmost) DL represents the D of the source-program that is currently being processed. Th RHS of the ; represents the top-level declarations that have allready been compiled, this is neccessary to look up top-level classes and traits.
To look up the value of a type in the program we will use the notation $p(T)$, which is defined by the following, but only if the RHS denotes an LV:

$$(;\_, C = L, \_)(\mathtt{This}0.C.Cs) \coloneqq L(Cs)$$
$$(id = L, p)(\mathtt{This}0.Cs) \coloneqq L(Cs)$$
$$(id = L, p)(\mathtt{This}n+1.Cs) \coloneqq p(\mathtt{This}n.Cs)$$

To get the relative value of a trait, we define $p[t]$:

$$(DLs; \_, t = LV, \_)[t] \coloneqq LV[\mathtt{This}\#DLs]$$

To get a the value of a literal, in a way that can be understand from the current location ($\mathtt{This}0$), we define:

$$p[T] \coloneqq p(T)[T]$$

And a few simple auxiliary definitions:

$$Ts \in p \coloneqq \forall T \in Ts \bullet p(T) \text{ is defined}$$
$$L(\emptyset) \coloneqq L$$
$$L(C.Cs) \coloneqq L(Cs) \text{ where } L = \mathtt{interface}?\,\{\_;\ \_, C = L, \_;\ \_\}$$
$$L[C = E'] \coloneqq \mathtt{interface}?\,\{Tz;\ MVs\ C = E'\ Ms;\ K?\}$$
$$\text{where } \mathrm{L} = \mathtt{interface}?\,\{\mathrm{Tz};\ MVs\ \mathrm{C} = \_\ Ms\ ;\ \mathrm{K}?\}$$

We have two-top level reduction rules defining our language, of the form $Dse^{``} > Ds'e$ which simply reduces the source-code. The first rule (*compile*) 'compiles' each top-level declaration (using a well-typed subset of allready compiled top-level declarations), this reduces the defining expresion. The second rule, (*main*) is executed once all the top-level declarations have compiled (i.e. are now fully evaluated class literals), it typechecks the top-level declarations and the main expression, and then procedes to reduce it. In principle only one-typechecking is needed, but we repeat it to avoid declaring more rules.

```
Define Ds e --> Ds' e'
================================================================
DVs' |- Ok
empty; DVs'; id | E --> E'
(compile)---------------------------------------- DVs' subsetof DVs
DVs id = E Ds e --> DVs id = E' Ds e

DVs |- Ok
DVs |- e : T
DVs |- e --> e'
(main)---------------------------------- for some type T
DVs e --> DVs e'
```

3 Compilation

Aside from the redirect operation itself, compilation is the most interesting part, it is defined by a reduction arrow $p; id| - E - - > E'$, the id represents the id of the type/trait that we are currently compiling, it is needed since it will be the name of $This0$, and we use that fact that that is equal to $This1.id$ to compare types for equality. The ($CtxV$) rule is the standard context, the (L) rule propegates compilation inside of nested-classes, ($trait$) merely evaluates a trait reference to it's defined body, (sum) and ($redirect$) perform our two meta-operations.

```
Define p; id |- E --> E'
=========================================================
p; id |- E --> E'
(CtxV) ---------------------------------------------
p; id |- CtxV[E] --> CtxV[E']

id = L[C = E], p; C |- E --> E'
(L) --------------------------------------------- // TODO use fresh C?
p; id |- L[C = E] ---> L[C = E']

(trait) -----------------------------------
p; id |- t -> p[t]

LV1 <+p' LV2 = LV3                  p' = C' = LV3, p
(sum) --------------------------------------- for fresh C'
p; id |- LV1 <+ LV2 --> LV3

// TODO: Inline and de-42 redirect formalism
(redirect) ------------------------------------LV'=redirect(p, LV, Cs, P)
p; id |- LV(Cs=P) -> LV'
```

4 The Sum operation

The sum operation is defined by the rule $L1 < +pL2 = L3$, it is unconventional as it assumes we allready have the result ($L3$), and simply checks that it is indead correct. We believe (but have not proved) that this rule is unambigouse, if $L1 < +pL2 = L3$ and $L1 < +pL2 = L3'$, then $L3 = L3'$ (since the order of members does not matter for Ls).

The main rule fir summong of non-interfaces, sums the members, unions the implemented interfaces (and uses *mininize* to remove any duplicates), it also ensures that at most one of them has a constructor. For summing an interface with a interface/class we require that an interface cannot 'gain' members due to a sum. The actually L42 implementation is far less restrictive, but requires complicated rules to ensure soudness, due to problems that could arise if a summed nested-interface is implemented. Summing of traits/classes with state is a non-trivial problem and not the focus of our paper, their are many prior works on this topic, and our full L42 language simply uses ordinary methods to represent state, however this would take too much effort to explain here.

```
Define L1 <+p L2 = L3
==========================================================================================
{Tz1; Mz1; K?1} <+p {Tz2; Mz2; K?2} = {Tz; Mz; K?}
Tz = p.minimize(Tz1 U Tz2)
Mz1 <+p Mz1 = Mz
{empty, K?1, K?2} = {empty, K?} //may be too sophisticated?

interface{Tz1; amtz,amtz';} <+p interface?{Tz2;amtz;} = interface {Tz;amtz,amtz';}
Tz = p.minimize(Tz1 U Tz2)
if interface? = interface then amtz'=empty
```

The rules for summing member are simple, we take two sets of members collect all the oness with unique names, and sum those with duplicates. To sum nested classes we merely sum their bodies, to sum two methods we require their signatures to be identical, if they both have bodies, the result has the body of the RHS, otherwise the result has the body (if present) of the LHS.

```
Define Mz <+p Mz' = Mz"
------------------------------------------
M, Mz <+p M', Mz' = M <+p M', Mz <+p Mz
//note: only defined when M.Mid = M'.Mid

Mz <+p Mz' = Mz, Mz':
dom(Mz) disjoint dom(Mz')

Define M <+p M' = M"
-----------------------------------------
T' m(Txs') e? <+p T m(Txs) e = T m(Txs) e
T', Txs'.Ts =p Ts, Txs

T' m(Txs') e? <+p T m(Txs) = T m(Txs) e?
T', Txs'.Ts =p Ts, Txs

(C = L) <+p (C = L') = L <+p.push(C) L'
```

5 Type System

The type system is split into two parts: type checking programs and class literals, and the typechecking of expressions. The latter part is mostly convential, it involves typing judgments of the form $p; Txs \vdash e : T$, with the usual program p and variable environement Txs (often called Γ in the literature). rule ($Dsok$) type checks a sequence of top-level declarations by simply push each declaration onto a program and typecheck the resulting program. Rule pok typechecks a program by check the topmost class literal: we type check each of it's members (including all nested classes), check that it properly implements each interface it claims to, does something weird, and finanly check check that it's constructor only referenced existing types,

```
Define p |- Ok
===========================================================

D1; Ds |- Ok ... Dn; Ds|- Ok
(Ds ok) ------------------------------ Ds = D1 ... Dn
Ds |- Ok

p |- M1 : Ok .... p |- Mn : Ok
p |- P1 : Implemented .... p |- Pn : Implemented
p |- implements(Pz; Ms) /*WTF?*/                   if K? = K: p.exists(K.Txs.Ts)
(p ok) ------------------------------------------- p.top() = interface? {P1...Pn; M1, ..., Mn
p |- Ok

p.minimize(Pz) subseteq p.minimize(p.top().Pz)
amt1 _ in p.top().Ms ... amtn _ in p.top().Ms
(P implemented) ----------------------------------------------- p[P] = interface {Pz; amt1 ..
p |- P : Implemented

(amt-ok) ------------------- p.exists(T, Txs.Ts)
p |- T m(Tcs) : Ok

p; This0 this, Txs |- e : T
(mt-ok) ------------------------------ p.exists(T, Txs.Ts)
p |- T m(Tcs) e : Ok

C = L, p |- Ok
(cd-Ok) -------------------
p |- C = L : OK
```

Rule ($Pimplemented$) checks that an interface is properly implemented by the programtop, we simply check that it declares that it implements every one of the interfaces superinterfaces and methods. Rules ($amt - ok$) and ($mt - ok$) are straightforward, they both check that types mensioned in the method signature exist, and ofcourse for the latter case, that the body respects this signature.

To typecheck a nested class declaration, we simply push it onto the program and typecheck the top-of the program as before.

The expression typesystem is mostly straightforward and similar to feartherwieght Java, notable we we use $p[T]$ to look up information about types, as it properly 'from's paths, and use a classes constructor definitions to determine the types of fields.

```
Define p; Txs |- e : T
=====================================
(var)
----------------------- T x in Txs
p;  Txs |- x : T

(call)
p; Txs |- e0 : T0
...
p; Txs |- en : Tn
-----------------------------------  T' m(T1 x1 ... Tn xn) _ in p[T0].Ms
p; Txs |- e0.m(e1 ... en) : T'

(field)
p; Txs |- e : T
---------------------------------------  p[T].K = constructor(_ T' x _)
p; Txs |- e.x : T'


(new)
p; Txs |- e1 : T1 ... p; Txs |- en : Tn
------------------------------------------- p[T].K = constructor(T1 x1 ... Tn xn)
p; Txs |- new T(e1 ... en)


(sub)
p; Txs |- e : T
-----------------------------------  T' in p[T].Pz
p; Txs |- e : T'


(equiv)
p; Txs |- e : T
-----------------------------------  T =p T'
p; Txs |- e : T'
```

– towel1:.. //Map: towel2:.. //Map: lib: T:towel1 f1 ... fn
MyProgram: T:towel2 Lib:lib[.T=This0.T] ... –

References