Using nested classes as associated types.

- 2 Authors omitted for double-bind review.
- 3 Unspecified Institution.

- Abstract

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1 Introduction

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Associated types are a powerful form of generics, now integrated in both Scala and Rust.

They are a new kind of member, like methods fields and nested classes. Associated types behave as 'virtual' types: they can be overridden, can be abstract and can have a default. However, the user has to specify those types and their concrete instantiations manually; that is, the user have to provide a complete mapping from all virtual type to concrete instantiation. When the number of associated types is small this poses no issue, but it hinders designs where the number of associated types is large. In this paper we examine the possibility of completing a partial mapping in a desirable way, so that the resulting mapping is sound and also robust with respect to code evolution.

The core of our design is to reuse the concept of nested classes instead of relying of a new kind of member for associated types. An operation, call Redirect, will redirect some nested classes in some external types. To simplify our formalization and to keep the focus on the core of our approach, we present our system on top of a simple Java like languages, with only final classes and interfaces, when code reuse is obtained by trait composition instead of conventional inheritance. We rely on a simple nominal type system, where subtyping is induced only by implementing interfaces; in our approach we can express generics without having a polymorphic type system. To simplify the treatment of state, we consider fields to be always instance private, and getters and setters to be automatically generated, together with a static method of(...) that would work as a standard constructor, taking the value of the fields and initializing the instance. In this way we can focus our presentation to just (static) methods, nested classes and implements relationships. Expanding our presentation to explicitly include visible fields, constructors and sub-classing would make it more complicated without adding any conceptual underpinning. In our proposed setting we could write:

```
String= ...
   SBox={String inner;
37
     method String inner(){..}//implicit
38
     static method SBox of(String inner){..}}//implicit
39
40
     Box={Elem inner}//implicit Box(Elem inner) and Elem inner()
41
42
     Elem={Elem concat(Elem that)}
     static method Box merge(Box b, Elem e){return Box.of(b.inner().concat(e));}
43
  Result=myTrait <Box=SBox>//equivalent to trait <Box=SBox, Elem=String>
45
     ...Result.merge(SBox.of("hello "), "world");//hello world
```

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Here class SBox is just a container of Strings, and myTrait is code encoding Boxes of any kind of Elem with a concat method. By instantiating myTrait<Box=SBox>, we can infer Elem=String, and obtain the following flattened code, where Box and Elem has been removed, and their occurrences are replaced with SBox and String.

```
Result={static method SBox merge(SBox b,String e){
     return SBox.of(b.inner().concat(e));}}
55
```

Note how Result is a new class that could have been written directly by the programmer, there is no trace that it has been generated by myTrait. We will represent trait names with lower-case names and class/interface names with upper-case names. Traits are just units of code reuse, and do not induce nominal types.

We could have just written Result=myTrait<Elem=String>, obtaining

```
Result={
     Box={String inner}
63
     static method Box merge(Box b,String e){
       return Box.of(b.inner().concat(e));}}
65
```

Note how in this case, class Result.Box would exists. Thanks to our decision of using nested classes as associated types, the decision of what classes need to be redirected is not made when the trait is written, but depends on the specific redirect operation. Moreover, our redirect is not just a way to show the type system that our code is correct, but it can change the behaviour of code calling static methods from the redirected classes.

This example show many of the characteristics of our approach:

- (A) We can redirect mutually recursive nested classes by redirecting them all at the same time, and if a partial mapping is provided, the system is able to infer the complete mapping.
- (B) Box and Elem are just normal nested classes inside of myTrait; indeed any nested class can be redirected away. In case any of their (static) methods was implemented, the implementation is just discarded. In most other approaches, abstract/associated/generic types are special and have some restriction; for example, in Java/Scala static methods and constructors can not be invoked on generic/associated types. With redirect, they are just normal nested classes, so there are no special restrictions on how they can be used. In our example, note how merge calls Box.of(..).
- (C) While our example language is nominally typed, nested classes are redirected over types satisfying the same structural shape. We will show how this offers some advantages of both nominal and structural typing.

A variation of redirect, able to only redirect a single nested class, was already presented in literature. While points (B) and (C) already applies to such redirect, we will show how supporting (A) greatly improve their value.

The formal core of our work is in defining

- ValidRedirect, a computable predicate telling if a mapping respect the structural shapes and nominal subtype relations.
- A formal definition of what properties a procedure expanding a partial mapping into a 92 complete one should respect.
 - **ChoseRedirect**, an efficient algorithm respecting those properties.

We first formally define our core language, then we define our redirect operator and its formal properties. Finally we motivate our model showing how many interesting examples of generics and associated types can be encoded with redirect. Finally, as an extreme application, we show how a whole library can be adapted to be injected in a different environment.

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2 Language grammar and well formedness

```
e := x \mid e.m(es) \mid T.m(es) \mid e.x \mid new T(es)
                                                                          T ::= \mathtt{This}\, n.\, Cs
                                                          expression
                                                                                                         types
L := \{ \text{ interface } Tz; Ms \} \mid \{ Tz; Mz ; K \} \}
                                                         code literal Tx := Tx
                                                                                                   parameter
M ::= static? T m(Txs) e? | private? C = E
                                                                          D := id = E
                                                             member
                                                                                                  declaration
K ::= (Txz)?
                                                                        id ::= C \mid t
                                                                 state
                                                                                               class/trait id
E := L \mid t \mid E_1 \iff E_2 \mid E \iff Cs = T \implies
                                                         Code Expr.
                                                                          v := new T(vs)
```

We apply our ideas on a simplified object oriented language with nominal typing and (nested) interfaces and final classes. Instead of inheritance, code reuse is obtained by trait composition, thus the source code would be a sequence of top level declarations D followed by a main expression; a lower-case identifier t is a trait name, while an upper case identifier C is a class name. To simplify our terminology, instead of distinguishing between nested classes and nested interfaces, we will call nested class any member of a code literal named by a class identifier C. Thus, the term class may denote either an interface class (interface for short) or a final class.

In the context of nested classes, types are paths. Syntactically, we represent them as relative paths of form $\mathtt{Thisn}.Cs$, where the number n identify the root of our path: $\mathtt{This0}$ is the current class, $\mathtt{This1}$ is the enclosing class, $\mathtt{This2}$ is the enclosing enclosing class and so on. $\mathtt{Thisn}.Cs$ refers to the class obtained by navigating throughout Cs starting from \mathtt{Thisn} . Thus, $\mathtt{This0}$ is just the type of the directly enclosing class. By using a larger then needed n, there could be multiple different types referring to the same class. Here we expect all types to be in the normalized form where the smallest possible n is used.

Code literals L serve the role of class/interface bodies; they contain the set of implemented interfaces Tz, the set of members Mz and their (optional) state. In the concrete syntax we will use **implements** in front of a non empty list of implemented interfaces and we will omit parenthesis around a non empty set of fields. A class member M can be a (private) nested class or a (static) method. Abstract methods are just methods without a body. Well formed interface methods can only be abstract and non-static. To facilitate code reuse, classes can have (static) abstract methods, code composition is expected to provide an implementation for those or, as we will see, redirect away the whole class. We could easily support private methods too, but to simplify our formalism we consider private only for nested classes. In a well formed code literal, in all types of form Thisn.Cs.C.Cs', if C denotes a private nested class, then Cs is empty.

Expressions are used as body of (static) methods and for the main expression. They are variables x (including this) and conventional (static) method calls. Field access and new expressions are included but with restricted usage: well formed field accesses are of form this.x in method bodies and v.x in the main expression, while well formed new expressions have to be of form new ThisO(xs) in method bodies and of form v in the main expression. Those restrictions greatly simply reasoning about code reuse, since they require different classes to only communicate by calling (static) methods. Supporting unrestricted fields and constructors would make the formalism much more involved without adding much of a conceptual difficulty. Values are of form new T(vs).

For brevity, in the concrete syntax we assume a syntactic sugar declaring a static of method (that serve as a factory) and all fields getters; thus the order of the fields would induce the order of the factory arguments. In the core calculus we just assume such methods to be explicitly declared.

Finally, we examine the shape of a nested class: private? C=E. The right hand side is not just a code literal but a code composition expression E. In trait composition, the

code expression will be reduced/flattened to a code literal L during compilation. Code expressions denote an algebra of code composition, starting from code literal L and trait names t, referring to a literal declared before by t=E. We consider two operators: conventional preferential sum $E_1 \leftrightarrow E_2$ and our novel redirect E < Cs = T >.

The compilation process consists in flattening all the E into L, starting from the innermost leftmost E. This means that sum and redirect work on LVs: a kind of L, where all the nested classes are of form C=LV. The execution happens after compilation and consist in the conventional execution of the main expression e in the context of the fully reduced declarations, where all trait composition has been flatted away. Thus, execution is very simple and standard and behaves like a variation of FJ[] with interfaces instead of inheritance, and where nested classes are just a way to hierarchically organize code names. On the other side, code composition in this setting is very interesting and powerful, where nested classes are much more than name organization: they support in a simple and intuitive way expressive code reuse patterns. To flatten an E we need to understand the behaviour of the two operators, and how to load the code of a trait: since it was written in another place, the syntactic representation of the types need to be updated. For each of those points we will first provide some informal explanation and then we will proceed formalizing the precise behaviour.

2.1 Redirect

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Redirect takes a library literal and produce a modified version of it where some nested classes has been removed and all the types referencing such nested classes are now referring to an external type. It is easy to use this feature to encode a generic list:

```
list={
165
      Elem={}
166
      static This0 empty() = new This0(Empty.of())
167
168
      boolean isEmpty() = this.impl().isEmpty()
      Elem head() = this.impl.asCons().tail()
169
      This0 tail()=this.impl.asCons().tail()
170
      ThisO cons(Elem e) = new ThisO(Cons.of(e,
                                                 this.impl)
171
      private Impl={interface
                                  Bool isEmpty()
                                                   Cons asCons()}
172
      private Empty={implements This1
173
        Bool isEmpty()=true Cons asCons()=../*error*/
174
        ()}//() means no fields
175
      private Cons={implements This1
176
        Bool isEmpty()=false
                               Cons asCons()=this
177
        Elem elem Impl tail }
178
179
      Impl impl
180
181
   IntList=list<Elem=Int>
182
   IntList.Empty.of().push(3).top()==4 //example usage
183
```

This would flatten into

```
list={/*as before*/
187
   //IntList=list<Elem=Int>
188
189
   IntList={
      //Elem={} no more nested class Elem
190
      static This0 empty() = new This0(Empty.of())
191
      boolean isEmpty() = this.impl().isEmpty()
192
     Int head() = this.impl.asCons().tail()
193
      ThisO tail()=this.impl.asCons().tail()
194
      ThisO cons(Int e)=new ThisO(Cons.of(e,
                                               this.impl)
195
     private Impl={interface
                                Bool isEmpty() Cons asCons()}
196
     private Empty={/*as before*/}
```

```
private Cons={implements This1
Bool isEmpty()=false Cons asCons()=this
Int elem Impl tail }
Impl impl
}//everywhere there was "Elem", now there is "Int"
```

Redirect can be propagated in the same way generics parameters are propagate: For example, in Java one could write code as below,

```
206
207 class ShapeGroup<T extends Shape>{
208  List<T> shapes;
209   ...}
210  //alternative implementation
211 class ShapeGroup<T extends Shape,L extends List<T>>{
212  L shapes;
213  ...}
```

to denote a class containing a list of a certain kind of **Shape**s. In our approach, one could write the equivalent

```
217
218 shapeGroup={
219 Shape={implements Shape}
220 List=list<Elem=Shape>
221 List shapes
222 ...}
```

With redirect, shapeGroup follow both roles of the two Java examples; indeed there are two reasonable ways to reuse this code

Triangolation=shapeGroup<Shape=Triangle>, if we have a Triangle class and we would like the concrete list type used inside to be local to the Triangolation, or Triangolation=shapeGroup<List=Triangles>; if we have a preferred implementation for the list of triangles that is going to be used by our Triangolation. Those two versions would flatten as follow:

```
230
    //Triangolation=shapeGroup<Shape=Triangle>
231
232
   Triangolation={
      List=/*list with Triangle instead of Elem*/
233
234
      List shapes
235
236
    //Triangolation=shapeGroup<List=Triangles>
237
    //exapands to shapeGroup <List=Triangles,Shape=Triangle>
238
   Triangolation={
239
      Triangles shapes
240
241
```

As you can see, with redirect we do not decide a priori what is generic and what is not in a class.

Redirect can not always succeed. For example, if we was to attempt <code>shapeGroup<List=Int></code> the flattening process would fail with an error similar to a invalid generic instantiation. Subtype is a fundamental feature of object oriented programming. Our proposed redirect operator do not require the type of the target to perfectly match the structural type of the internal nested classes; structural subtyping is sufficient. This feature adds a lot of flexibility to our redirect, however completing the mapping (as happens in the example above) is a challenging and technically very interesting task when subtyping is took into account. This is strongly connected with ontology matching and will be discussed in the technical core of the paper later on.

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2.2 Preferential sum and examples of sum and redirect working together

The sum of two traits is conceptually a trait with the sum of the traits members, and the union of the implemented interfaces. If the two traits both define a method with the same name, some resolution strategy is applied. In the symmetric sum[] the two methods need to have the same signature and at least one of them need to be abstract. With preferential sum (sometimes called override), if they are both implemented, the left implementation is chosen. Since in our model we have nested classes, nested classes with the same name will be recursively composed.

We chose preferential sum since is simpler to use in short code examples. ¹ Since the focus of the paper is the novel redirect operator, instead of the well known sum, we will handle summing state and interfaces in the simplest possible way: a class with state can only be summed with a class without state, and an interface can only be summed with another interface with identical methods signatures.

In literature it has been shown how trait composition with (recursively composed) nested classes can elegantly handle the expression problem and a range of similar design challenges. Here we will show some examples where sum and redirect cooperate to produce interesting code reuse patterns:

```
272
273
   listComp=list<+{
      Elem:{ Int geq(Elem e)}//-1/0/1 for smaller, equals, greater
274
      static Elem max2(Elem e1, Elem e2)=if e1.geq(e2)>0 then e1, else e2
275
      Elem max(Elem candidate)=
276
        if This.isEmpty() then candidate
277
        else this.tail().max(This.max2(this.head(),candidate))
278
279
      Elem min(Elem candidate) = . . .
280
      This0 sort()=...
381
```

As you can see, we can *extends* our generic type while refining our generic argument: **Elem** of listComp now needs a geq method.

While this is also possible with conventional inheritance and F-Bound polymorphism, we think this solution is logically simpler then the equivalent Java

```
class ListComp<Elem extends Comparable<Elem>> extends LinkedList<Elem>{
    ../*body as before*/
}
```

Another interesting way to use sum is to modularize behaviour delegation: consider the following (not efficient for the sake of compactness) implementation of set, where the way to compare elements is not fixed:

```
295
296
   set:{
      Elem:{}
297
298
      List=list < Elem = Elem >
      static This0 empty() = new This0(List.empty())
299
      Bool contains (Elem e) = ... /*uses eq and hash*/
300
      Int size()=..
301
      This add(Elem e)=...
302
      This remove(Elem e)=...
303
      Bool eq(Elem e1,Elem e2)//abstract
      Int hash(Elem e)//abstract
305
306
      List asList //to allow iteration
```

symmetric sum is often presented in conjunction with a restrict operator that makes some methods abstract.

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```
307
    eqElem={
308
      Elem={ Bool equals(Elem e)/*abstract*/}
309
      Bool eq(Elem e1, Elem e2) = e1. equals(e2)
310
311
    hashElem={
312
      Elem={ Int hash(Elem e) /*abstract*/}
313
      Int hash(Elem e) = e.hash()
314
315
    Strings=(set<+eqElem<+eqHash)<Elem=String>
316
    LongStrings=(set<+eqElem)<Elem=String> <+{</pre>
317
      Int hash(String e)=e.size()
318
      }//for very long strings, size is a faster hash
318
```

Note how (set<+eqElem<+eqHash)<Elem=String> is equivalent to set<Elem=String> <+eqElem<Elem=String> <+eqHash<Elem=Consider now the signature Bool equals(Elem e). This is different from the common signature Bool equals(Object e). What is the best signature for equals is an open research question, where most approaches advise either the first or the second one. Our eqElem, as is wrote, can support both: Strings would be correctly define both if String.equals signature has a String or an Object parameter.EXPAND on method subtyping.

We now consider an example where Redirect simplifies the code quite a lot: We have a **Node** and **Edge** concepts for a graph. The **Node** have a list of **Edges**. A isConnected function takes a list of **Nodes**. A getConnected function takes **Node** and return a set of **Nodes**.

```
graphUtils={
331
      Edges:list<+{Node start() Node end()}</pre>
332
      Node: {Edges connections()}
333
      Nodes: set < Elem = Node > // note that we do not specify equals / hash
334
      static Bool isConnected(Nodes nodes)=
335
        if(nodes.size()=0) then true
336
        else getConnected(nodes.asList().head()).size() == nodes.size()
337
      static Nodes getConnected(Node node) = getConnected(node, Nodes.empty())
      static Nodes getConnected(Node node, Nodes collected)=
339
        if(collected.contains(node)) then collected
340
341
        else connectEdges(node.connections(),collected.add(node))
342
      static Nodes connectEdges(Edges e, Nodes collected)=
        if( e.isEmpty()) then collected
343
        else connectEdges(e.tail(),collected.add(e.head().end()))
344
345
```

We have shown the full code instead of omitting implementations to show that the code inside of an highly general code like the former is pretty conventional. Just declare nested classes as if they was the concrete desired types. Note how we can easly create a new Nodes@ by doing Nodes.empty().

Here we show how to instantiate graphUtils to a graph representing cities connected by streets, where the streets are annotated with their length, and Edges is a priority queue, to optimize finding the shortest path between cities.

```
Map: {
355
      Street:{City start,City end, Int size}
356
357
      Citv:{}
      Streets:priorityQueue <Elem=Street><+{</pre>
358
359
        Int geq(Street e1,Street e2)=e1.size()-e2.size()}
360
361
      Streets:{}
      City: {Streets connections, Int index} // index identify the node
362
      Cities:set<Elem=City><+{
363
        Bool eq(City e1,City e2) e1.index==e2.index
364
        Int hash(City e) e.index
365
366
367
      Cities cities
```

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```
//more methods
}

MapUtils=graphUtils < Nodes = Map. Cities >
//infers Nodes. List, Node, Edges, Edge
```

In Appending 2 we will show our best attempt to encode this graph example in Java, Rust and Scala. In short, we discovered...

2.3 Moving traits around in the program

It is not trivial to formalize the way types like This1.A.B have to be adapted so that when code is moved around in differed depths of nesting the refereed classes stay the same. To this aim we define a concept of program p, as a representation of the code as seen from a certain point inside of the source code. Each of the $DV_0 \dots DV_n$ represents the outer nested level 0..n, while the DLs component represent the program top level, that is the outer nested level n+1

```
p := DLs; \ DVs program DL := id = L partially-evaluated-declaration DV := id = LV evaluated-declaration Mid := C \mid m member-id Thus, for example in the program
```

384 385 **A**={()} 386 **t**={ **B**={()} This1.**A** m(This0.**B** b)} 387 **C**={**D**={**E**=t}}

the flattened version for C will be $C=\{D=\{E=\{B=\{()\}\}\}\}$, where the path This1.A is now This3.A while the path This0.B stays the same. The program p in the observation point D=t is

```
392
393 A={()}
394 t={ B={()} This1.A m(This0.B b)}
395 C={D={E=t}};
396 C={D={E=t}},
D={E=t}
```

We will use p as a function, so we will writep(T) and p(T.m) we define now From, $\mathcal{E}_V := \Box \mid \mathcal{E}_V \prec + \mid LV \prec + \mid \mathcal{E}_V \mid \mathcal{E}_V \prec Cs = T >$ context of library-evaluation $\mathcal{E}_v := \Box \mid \mathcal{E}_v \cdot m(es) \mid v \cdot m(vs \mid \mathcal{E}_v \mid es) \mid T \cdot m(vs \mid \mathcal{E}_v \mid es)$

We use t and C to syntactically distinguish between trait and class names. An E is a top-level class expression, which can contain class-literals, references to traits, and operations on them, namely our sum E < +E and redirect e(Cs = T). A declaration D is just an id = E, representing that id is declared to be the value of E, we also have CD, CV, DL, and DV that constrain the forms of the LHS and RHS of the declaration. A literal E has 4 components, an optional interface keyword, a list of implemented interfaces, a list of members, and an optional constructor. For simplicity, interfaces can only contain abstract-methods (amt) as members, and cannot have constructors. A member E0, is either an (potentially abstract) method E1 method E2 member that has been fully compiled. An E3 midentifier, identifying a member. Constructors, E3, contain a E4 member E5 indicating the type and names of fields. An E5 is normal fetherweight-java style expression, it has variables E3, method calls E4. E5, field accesses E5, and E6 we shall one for E6.

```
An S represents what the top-level source-code form of our language is, it's just a sequence
415
    of declarations and a main expression. The most interesting form of the grammer is a p, it is
416
    a 'program', used as the context for many reductions and typing rules, on the LHS of the;
417
    is a stack representing which (nested) declaration is currently being processed, the bottom
    (rightmost) DL represents the D of the source-program that is currently being processed.
419
    Th RHS of the; represents the top-level declarations that have allready been compiled, this
420
    is neccessary to look up top-level classes and traits.
421
    To look up the value of a type in the program we will use the notation p(T), which is defined
422
    by the following, but only if the RHS denotes an LV:
        (;\underline{\phantom{C}},C=L,\underline{\phantom{C}})(\mathtt{This}0.C.Cs)\coloneqq L(Cs)
                (id = L, p)(\mathtt{This} 0.Cs) \coloneqq L(Cs)
424
           (id = L, p)(\mathtt{This}\, n + 1.Cs) \coloneqq p(\mathtt{This}\, n.Cs)
425
    To get the relative value of a trait, we define p[t]:
        (DLs; \_, t = LV, \_)[t] \coloneqq LV[\mathtt{This} \# DLs]
427
428
    To get a the value of a literal, in a way that can be understand from the current location
429
    (This 0), we define:
430
        p[T] := p(T)[T]
431
432
    And a few simple auxiliary definitions:
433
           Ts \in p := \forall T \in Ts \bullet p(T) is defined
             L(\emptyset) := L
        L(C.Cs) := L(Cs) where L = interface? \{\_; \_, C = L, \_; \_\}
434
         L[C = E'] := interface? \{Tz; MVs C = E' Ms; K?\}
           where L = interface? {Tz; MVs C = Ms; K?}
```

We have two-top level reduction rules defining our language, of the form $Dse^{\sim} > Ds'e$ which simply reduces the source-code. The first rule (compile) 'compiles' each top-level declaration (using a well-typed subset of allready compiled top-level declarations), this reduces the defining expresion. The second rule, (main) is executed once all the top-level declarations have compiled (i.e. are now fully evaluated class literals), it typechecks the top-level declarations and the main expression, and then procedes to reduce it. In principle only one-typechecking is needed, but we repeat it to avoid declaring more rules.

```
Define Ds e --> Ds' e'
  ______
  DVs' |- Ok
445
  empty; DVs'; id | E --> E'
  (compile)----- DVs' subsetof DVs
  DVs id = E Ds e --> DVs id = E' Ds e
448
  DVs |- Ok
450
  DVs |- e : T
  DVs |- e --> e'
                ----- for some type T
  (main)-----
453
  DVs e --> DVs e'
```

3 Compilation

Aside from the redirect operation itself, compilation is the most interesting part, it is defined by a reduction arrow p; id | -E - > E', the id represents the id of the type/trait that we are currently compiling, it is needed since it will be the name of This0, and we use that fact that that is equal to This1.id to compare types for equality. The (CtxV) rule is the standard context, the (L) rule propegates compilation inside of nested-classes, (trait) merely evaluates a trait reference to it's defined body, (sum) and (redirect) perform our two meta-operations.

```
Define p; id |- E --> E'
  ______
  p; id |- E --> E'
  (CtxV) -----
  p; id |- CtxV[E] --> CtxV[E']
466
  id = L[C = E], p; C \vdash E \longrightarrow E'
  (L) ----- // TODO use fresh C?
469
  p; id |-L[C = E] ---> L[C = E']
471
  (trait) -----
  p; id |- t -> p[t]
473
474
                           p' = C' = LV3, p
  LV1 <+p' LV2 = LV3
  (sum) ----- for fresh C'
476
  p; id |- LV1 <+ LV2 --> LV3
477
  // TODO: Inline and de-42 redirect formalism
479
  (redirect) -----LV'=redirect(p, LV, Cs, P)
  p; id |- LV(Cs=P) -> LV'
```

4 The Sum operation

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The sum operation is defined by the rule L1 < +pL2 = L3, it is unconventional as it assumes we allready have the result (L3), and simply checks that it is indead correct. We believe (but have not proved) that this rule is unambigouse, if L1 < +pL2 = L3 and L1 < +pL2 = L3', then L3 = L3' (since the order of members does not matter for Ls).

The main rule fir summong of non-interfaces, sums the members, unions the implemented interfaces (and uses mininize to remove any duplicates), it also ensures that at most one of them has a constructor. For summing an interface with a interface/class we require that an interface cannot 'gain' members due to a sum. The actually L42 implementation is far less restrictive, but requires complicated rules to ensure soudness, due to problems that could arise if a summed nested-interface is implemented. Summing of traits/classes with state is a non-trivial problem and not the focus of our paper, their are many prior works on this topic, and our full L42 language simply uses ordinary methods to represent state, however this would take too much effort to explain here.

```
Define L1 <+p L2 = L3
   ______
497
  \{Tz1; Mz1; K?1\} <+p \{Tz2; Mz2; K?2\} = \{Tz; Mz; K?\}
498
   Tz = p.minimize(Tz1 U Tz2)
   Mz1 < +p Mz1 = Mz
500
   {empty, K?1, K?2} = {empty, K?} //may be too sophisticated?
501
502
   interface{Tz1; amtz,amtz';} <+p interface?{Tz2;amtz;} = interface {Tz;amtz,amtz';}</pre>
503
   Tz = p.minimize(Tz1 U Tz2)
504
   if interface? = interface then amtz'=empty
```

The rules for summing member are simple, we take two sets of members collect all the oness with unique names, and sum those with duplicates. To sum nested classes we merely sum their bodies, to sum two methods we require their signatures to be identical, if they both have bodies, the result has the body of the RHS, otherwise the result has the body (if present) of the LHS.

```
Define Mz <+p Mz' = Mz"
511
   _____
512
   M, Mz <+p M', Mz' = M <+p M', Mz <+p Mz
513
   //note: only defined when M.Mid = M'.Mid
514
515
   Mz <+p Mz' = Mz, Mz':
   dom(Mz) disjoint dom(Mz')
517
518
   Define M <+p M' = M"
   T' m(Txs') e? <+p T m(Txs) e = T m(Txs) e
521
   T', Txs'.Ts =p Ts, Txs
522
523
   T' m(Txs') e? <+p T m(Txs) = T m(Txs) e?
524
   T', Txs'.Ts =p Ts, Txs
525
   (C = L) \leftarrow (C = L') = L \leftarrow (C) L'
```

5 Type System

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The type system is split into two parts: type checking programs and class literals, and the typechecking of expressions. The latter part is mostly convential, it involves typing judgments of the form $p; Txs \vdash e : T$, with the usual program p and variable environement Txs (often called Γ in the literature). rule (Dsok) type checks a sequence of top-level declarations by simply push each declaration onto a program and typecheck the resulting program. Rule pok typechecks a program by check the topmost class literal: we type check each of it's members (including all nested classes), check that it properly implements each interface it claims to, does something weird, and finanly check check that it's constructor only referenced existing types,

```
539
  Define p |- Ok
540
  ______
542
  D1; Ds |- Ok ... Dn; Ds|- Ok
  (Ds ok) ----- Ds = D1 ... Dn
  Ds |- Ok
545
  p \mid -M1 : Ok \dots p \mid -Mn : Ok
  p |- P1 : Implemented .... p |- Pn : Implemented
  p |- implements(Pz; Ms) /*WTF?*/
                                            if K? = K: p.exists(K.Txs.Ts)
  (p ok) ----- p.top() = interface? {P1...Pn; M1, ..., Mn
  p |- 0k
552
  p.minimize(Pz) subseteq p.minimize(p.top().Pz)
  amt1 _ in p.top().Ms ... amtn _ in p.top().Ms
  (P implemented) ------ p[P] = interface {Pz; amt1 ...
555
  p |- P : Implemented
556
  (amt-ok) ----- p.exists(T, Txs.Ts)
  p \mid - T m(Tcs) : Ok
559
560
  p; ThisO this, Txs |- e : T
  (mt-ok) ----- p.exists(T, Txs.Ts)
  p |- T m(Tcs) e : Ok
563
  C = L, p \mid -Ok
565
  (cd-0k) -----
  p \mid - C = L : OK
```

Rule (Pimplemented) checks that an interface is properly implemented by the programtop, we simply check that it declares that it implements every one of the interfaces superinterfaces and methods. Rules (amt - ok) and (mt - ok) are straightforward, they both check that types mensioned in the method signature exist, and ofcourse for the latter case, that the body respects this signature.

To typecheck a nested class declaration, we simply push it onto the program and typecheck the top-of the program as before.

The expression typesystem is mostly straightforward and similar to feartherwieght Java, notable we we use p[T] to look up information about types, as it properly 'from's paths, and use a classes constructor definitions to determine the types of fields.

```
Define p; Txs |- e : T
   (var)
581
   ----- T x in Txs
   p; Txs |- x : T
583
584
   (call)
585
  p; Txs |- e0 : T0
586
  p; Txs |- en : Tn
588
  ----- T' m(T1 x1 ... Tn xn) _ in p[T0].Ms
   p; Txs |- e0.m(e1 ... en) : T'
591
   (field)
592
   p; Txs |- e : T
593
                     ----- p[T].K = constructor(_ T' x _)
594
  p; Txs |- e.x : T'
596
597
   (new)
   p; Txs |- e1 : T1 ... p; Txs |- en : Tn
599
  ----- p[T].K = constructor(T1 x1 ... Tn xn)
  p; Txs |- new T(e1 ... en)
601
602
   (sub)
604
  p; Txs |- e : T
605
  ----- T' in p[T].Pz
  p; Txs |- e : T'
607
608
609
   (equiv)
610
  p; Txs |- e : T
  ----- T =p T'
612
  p; Txs |- e : T'
  - towel1:.. //Map: towel2:.. //Map: lib: T:towel1 f1 ... fn
614
     MyProgram: T:towel2 Lib:lib[.T=This0.T] ... -
615
```

6 extra

Features: Structural based generics embedded in a nominal type system. Code is Nominal, Reuse is Structural. Static methods support for generics, so generics are not just a trik to

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make the type system happy but actually change the behaviour Subsume associate types. After the fact generics; redirect is like mixins for generics Mapping is inferred-> very large maps are possible -> application to libraries

In literature, in addition to conventional Java style F-bound polymorphism, there is another way to obtain generics: to use associated types (to specify generic paramaters) and inheritence (to instantiate the paramaters). However, when parametrizing multiple types, the user to specify the full mapping. For example in Java interface A B m(); inteface BString f(); class G<TA extends A<TB>, TB>//TA and TB explicitly listed String g(TA a TB b)return a.m().f(); class MyA implements A<MyB>.. class MyB implements B .. G<MyA,MyB>//instantiation Also scala offers genercs, and could encode the example in the same way, but Scala also offers associated types, allowing to write instead....

Rust also offers generics and associated types, but also support calling static methods over generic and associated types.

We provide here a fundational model for genericty that subsume the power of F-bound polimorphims and associated types. Moreover, it allows for large sets of generic parameter instantiations to be inferred starting from a much smaller mapping. For example, in our system we could just write g=A= method B m() B= method B f() method B f() method B f() method B f() method B f()="Hello"; B g(A and B b)=a.m().f() MyA= method MyB m()= new MyB(); ... MyB= method B f()="Hello"; ... B g(A=MyA)=//instantiation. The mapping A=MyA,B=MyB

We model a minimal calculus with interfaces and final classes, where implementing an interface is the only way to induce subtyping. We will show how supporting subtyping constitute the core technical difficulty in our work, inducing ambiguity in the mappings. As you can see, we base our generic matches the structor of the type instead of respecting a subtype requirement as in F-bound polymorphis. We can easily encode subtype requirements by using implements: Print=interface method String print(); g= A:implements Print method A printMe(A a1,A a2) if(a1.print().size()>a2.print.size())return a1; return a2; MyPrint=implements Print .. g<A=MyPrint> //instantiation g<A=Print> //works too

example showing ordering need to strictly improve EI1: interface EA1: implements EI1

```
ments En
```

EI2: interface EA2: implements EI2

EB: EA1 a1 EA1 a1

A1: A2: B: A1 a1 A2 a2 [B = EB] // A1 -> EI1, A2 -> EA2 a // A1 -> EA1, A2 -> EI2 b // A1 -> EA1, A2 -> EA2 c

```
a \le b \le a \le a, b \le c
```

hi Hi class

$$a := b$$
 c

aahi**Hi**class $qaq \ a \coloneqq b$

$$a := b$$
 c

655 }}][()] (TOP)

$$a \xrightarrow{b} c \quad \forall i < 3a \vdash b : OK$$

$$\frac{\forall i < 3a \vdash b : OK}{1+2 \to 3} \qquad b$$