

Iteratively Composing Statically Verified Traits

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Object oriented languages supporting static verification (SV) usually extend the syntax for method declarations to support *contracts* in the form of pre and post-conditions [5]. Correctness is defined only for code annotated with such contracts.

We say that a method is *correct*, if whenever its precondition holds on entry, the precondition of every directly invoked method holds, and the postcondition of the method holds when the method returns. Automated SV typically works by asking an automated theorem prover to verify that each method is correct individually, by assuming the correctness of every other method [1]. This process can be very slow and can produce unexpected results: since SV is undecidable correct code may not pass SV. Many SV approaches are not resilient to [some] standard refactoring techniques like method inlining. Sometimes SV even *times out, making it harder to use such refactoring techniques. [terminate for a time-out, exacerbating the impact of transformations like method inlining.]*

Metaprogramming is often used to programmatically generate faster specialised code when some parameters are known in advance, this is particularly useful where the specialisation mechanism is too complicated for a generic compiler to automatically derive [6] We could use metaprogramming to generate code together with contracts, and then once the metaprogramming has been run, *[ensure the correctness of] SV* the resulting code *[by applying SV.]*. [Isaac: You don't 'apply static verification', rather you 'statically verify', you could also 'use a static verifier'.] However, the resulting code could be much larger than the input to the metaprogramming, and so it could take a long time to SV. Moreover, one of the [main] many goals of metaprogramming is to make it easier [easy] to generate [many specialized] specialised versions of the same [functionality] code. [Isaac: A 'version of functionality' doesn't really make sense, a 'version of code' does, we could also use 'function/method'.] The aim of our work is to [apply] SV only [to the code manually wrote by the programmer] code written directly, and not code produced by metaprogramming; instead, we [and to] ensure that the result of metaprogramming is [instead] correct by construction.

Here we use the disciplined form of metaprogramming introduced by Servetto & Zucca [9], which is based on trait composition and adaptation [8]. Here a *Trait* is a unit of code: a set of method declarations. *Such methods can be abstract and be [Those methods can be abstract, and they can]* be mutually recursive by using the implicit parameter *this*.

As in [9] we require that all the traits are well-typed before they are used. *[Moreover, in our proposed approach we] we extend this by allowing [annotating] methods to be annotated with pre/post-conditions, and ensuring that traits are correct in terms of such contracts [we require that all traits are also correct]. Traits* directly written in the source code are *SVed [proven correct by SV]*, while traits resulting from metaprogramming are *ensured* correct by *only providing trait operations that preserve correctness [construction]*. [Isaac: SV proves correctness (that's the whole point), so no need to say 'proven correct by SV'. It was not clear how we 'ensure correctness by construction', so I fixed that.] *[Crucially] In particular*, we extend the checking performed by the traditional trait composition (+) operator, to also check the compatibility of contracts *[composition and adaptation of Traits to also check that contracts are composed correctly; thus ensuring the correctness*

of the result]. [Isaac: we only extend the + operator here, so I've made that explicit.] [Isaac: The above paragraph of changes are trying to make it more clear what our contribution is, but even then it's not good enough].

Our metaprogramming approach does not allow generating [generate] code from scratch (such as by generating ASTs), rather the language provides a specific set of primitive composition and adaption operators which preserve correctness. [; rather code is only generated by composing and adapting traits. Each composition/adaptation step is guaranteed to produce well typed and correct code; thus also the result of metaprogramming is well typed and correct.] [Isaac: I reworded it to make it sound like you are forced to use our safe operators, and can't subvert the system, since this makes our 'guarantees' meaningful.] Note that generated code may not be able to pass a particular SVer, since theorem provers are not complete. [Isaac: In principle, since our code is correct, it should be able to pass some form of 'static verification', however that doesn't mean it will base every 'static verifier'.]

SV handles **extends** and **implements** by verifying that every time a method is implemented/overridden, the Liskov substitution principle [4] is satisfied by checking that the [new contract] contract of the override/implementation implies the contract of the overridden/implemented method [overridden one]. [Isaac: In your version, it was not clear what contracts you were referring to.] In this way, there is no need to re-verify inherited code in the context of the derived class. This concept is easily adapted to handle trait composition, which simply provides another way to implement an **abstract** method. When traits are composed, it is sufficient to match the contracts of the few composed methods to ensure the whole result is correct.

In our examples we will use the notation **@requires**(*predicate*) to specify a precondition, and **@ensures**(*predicate*) to specify a postcondition; where *predicate* is a boolean expression in terms of the parameters of the method (including **this**), and for the **@ensures** case, the **result** of the method. Suppose we want to implement an efficient exponentiation function, we could use recursion and the common technique of 'repeated squaring':

```
1 @requires(exp > 0)
2 @ensures(result == x**exp) // Here x**y means x to the power of y
3 Int pow(Int x, Int exp) {
4     if (exp == 1) return x;
5     if (exp % 2 == 0) return pow(x*x, exp/2); // exp is even
6     return x*pow(x, exp-1); } // exp is odd
```

If the exponent is known at compile time, unfolding the recursion produces even more efficient code:

```
7 @ensures(result == x**7) Int pow7(Int x) {
8     Int x2 = x*x; // x**2
9     Int x4 = x2*x2; // x**4
10    return x*x2*x4; } // Since 7 = 1 + 2 + 4
```

Now we show how the technique of *Iterative Composition* (introduced in [9] and enriched by [our contract composition check] the contract compatibility check we propose performing in trait composition) [Isaac: We never call 'a contract composition check', so it's not clear what you are talking about, since I already mentioned a 'contract compatibility check above', I'm referencing it here] can be used to write a metaprogram that given an exponent, produces code like the above. Iterative Composition is a metacircular metaprogramming technique relying on *compile-time execution* (as defined by [10]), [Isaac: I'm not sure what 'as [10]' was meant to mean, correct me if my guess was wrong.] [thus a metaprogram is just a function or a method wrote in the target programming language that is executed during compilation.] , in our context this means that arbitrary expressions can be used as the RHS of a class declaration, during compilation such expressions will be evaluated to produce a **Trait**, which provides the body of the class. In this way metaprograms can be represented as otherwise normal functions/methods that return a **Trait**, without requiring the use of any additional 'meta language'. [Isaac: Major rewording, as your version didn't explain anything, in particular it was not clear what you meant by 'during

```

compilation'].
11 Trait base=class { //induction base case: pow(x) == x**1
12   @ensures(result>0) Int exp(){return 1;}
13   @ensures(result==x**exp()) Int pow(Int x){return x;}
14 }
15 Trait even=class { //if _pow(x)== x**_exp(), pow(x) == x**(2*_exp())
16   @ensures(result>0) Int _exp();
17   @ensures(result==2*_exp()) Int exp(){return 2*_exp();}
18   @ensures(result==x**_exp()) Int _pow(Int x);
19   @ensures(result==x**exp()) Int pow(Int x){return _pow(x*x);}
20 }
21 Trait odd=class { //if _pow(x)== x**_exp(), pow(x) == x**(1+_exp())
22   @ensures(result>0) Int _exp();
23   @ensures(result==1+_exp()) Int exp(){return 1+_exp();}
24   @ensures(result==x**_exp()) Int _pow(Int x);
25   @ensures(result==x**exp()) Int pow(Int x){return x*_pow(x);}
26 }
27 //‘compose’ performs a step of iterative composition
28 Trait compose(Trait current, Trait next){
29   current = current[rename exp->_exp, pow->_pow];
30   return (current+next)[hide _exp, _pow];}
31 @requires(exp>0) //the entry point for our metaprogramming
32 Trait generate(Int exp) {
33   if (exp==1) return base;
34   if (exp%2==0) return compose(generate(exp/2), even);
35   return compose(generate(exp-1), odd);
36 };
37 class Pow7: generate(7) //generate(7) is executed at compile time
38 //the body of class Pow7 is the result of generate(7)
39 /*example usage:*/new Pow7().pow(3)==2187 //Compute 3**7

```

[Isaac: I added a paragraph break here, so this is correctly indented with respect to the code above.] The traits `base`, `even`, and `odd` are the basic building blocks we will use to compute our result. They will be compiled, typechecked and SVed before the method `generate(exp)` can run. As you can see in line 37, a class body can be an expression in the language itself. At compile time such an expression will be run and the resulting `Trait` will be used as the body of the class. For example, we could write `class Pow1: base`; this would generate a class such that `new Pow1().pow(x)==x**1`. The other two traits have abstract methods; implementations for `_pow(x)` and `_exp()` must be provided. However, given the contract of `pow(x)`, and the fact that `even` and `odd` have both been SVed, if we supply method bodies respecting these contracts, we will get *correct* code, without the need for further SV. Many works in literature allow adapting traits by renaming or hiding methods [9, 7, 3]. Hiding a method may also trigger inlining if the method body is simple enough or used only once. Since all occurrences of names are consistently renamed, **renaming and hiding preserve code correctness**.

The `compose` method starts by renaming the `exp` and `pow` methods of `current` so that they satisfy the contracts in `next` (which will be `even` or `odd`). The `+` operator is the main way to compose traits [8, 2]. The result of `+` will contain all the methods from both operands.

Crucially, it is possible to sum traits where a method is declared in both operands; in this case at least

one of the two competing methods needs to be abstract, and the signatures of the two competing methods need to be *compatible*. To make sure that the traditional `+` operator also handles contracts, we need to require that the contract annotations of the two competing methods are *compatible*. For the sake of our example, we can just require them to be syntactically identical. Relaxing this constraint is an important future work. Thanks to this constraint **the sum operator also preserves code correctness**.

The sum is executed when the method `compose` runs, if the matched contracts are not identical an exception will be raised. A leaked exception during compile-time metaprogramming would become a compile-time error. Our approach is very similar to [9], and does not guarantee the success of the code generation process, rather it guarantees that if it succeeds, correct code is generated.

Finally the `_pow(x)` and `_exp()` method are hidden, so that the structural shape of the result is the same as `base`'s. As you can see, `Traits` are first class values and can be manipulated with a set of primitive operators that preserve code correctness and well-typedness. In this way, by inductive reasoning, we can start from the base case and then recursively compose even and odd until we get the desired code. Note how the code of `generate(exp)` follows the same scheme of the code of `pow(x, exp)` in line 1.

To understand our example better, imagine executing the code of `generate(7)` while keeping `compose` in symbolic form. We would get the following (where `c` is short for `compose`):

```
generate(7) == c(generate(6), odd) == ...
            == c(c(c(c(base, even), odd), even), odd)
```

As `base` represents `pow1(x)`; `c(base, even)` represents `pow2(x)`. Then `c(/*pow2(x)*/, odd)` represents `pow3(x)`, `c(/*pow3(x)*/, even)` represents `pow6(x)`, and finally, `c(/*pow6(x)*/, odd)` represents `pow7(x)`. The code of each `_pow` method is only executed once for each top-level `pow` call, so the `hide` operator can inline them. Thus, the result could be identical to the manually optimized code in line 7.

Our approach, as presented in this [extend abstract \[short paper\]](#), only guarantees that [code resulting from metaprogramming \[the resulting code\]](#) follows its own contracts, it does not [\[statically\]](#) ensure what [those contracts may be \[contracts it would have\]](#). As future work, we are investigating how [the resulting contracts can be ensured to have a particular meaning \[to ensure the contract content of the result\]](#). [Isaac: 'Ensure the contract content' does not mean what you want it to, rather it means that you are ensuring what the contract says, which we do do! You could say 'ensure the contract has a specific content'.] To do so, we need to [allow assertions on the contracts of Traits to be used within pre/post conditions \[extends the language of pre/post conditions to allow assertions on the contracts of Trait code\]](#). [Isaac: 'extend the language' makes it sound like pre/post conditions are written in a separate language! whereas in this paper we don't really care about that.]

For example we could allow post conditions like [\[the post condition\]](#) `@ensures(result.methName.ensures == predicate)` to mean that the resulting Trait has [\[requires the result to be a Trait with\]](#) a method called `methName`, whose `@ensures` clause is syntactically identical to [\[the given predicate, while\]](#) `predicate; whilst [` `@ensures(result.methName.ensures <=> predicate)` rely on conventional SV to check that such `@ensures` clause is equivalent to the given predicate.] `@ensures(result.methName.ensures ==> predicate)` would SV that `methName`'s `@ensures` clause logically implies `predicate`. [Isaac: An implication check (`=>`) is likely to be much more useful than an equivalence check.] With [\[those two instruments\]](#) these two features we could annotate the method `generate` in line 32 above as:

```
42 @requires(exp>0)
43 @ensures(result.exp().ensures ==> (result==exp))
44 @ensures(result.pow(x).ensures == (result==x**exp()))
45 Trait generate(Int exp) {...}
```

[Isaac: Why in the world did you set the above code to number starting at 32?, to make things more readable, I deleted that, so that the numbering is consistent with the previous listings. I have also added parenthesis to the code above, and changed `<->` to `==>`.]

In this way, we could [apply SV to the] SV the generate[(exp)] method [and prove it correct once and for all]. However, we fear such SV will be too complex or impractical.

We could instead automatically check the above postconditions after each call to generate. If generate is used to define a class (such as Pow7 above), we will guarantee that such class has the correct contracts, before it is used. Thus such runtime checking is sufficient to ensure the correctness of code produced by metaprogramming, before such code is used, however it is not sufficient to ensure the correctness of the metaprogram itself. [In this case we could defer those difficult/novel predicates to run-time checks, without losing much safety: Iterative Composition execute metaprogramming code at compile time, thus even run-time verification of metaprograms would happen at compile time. This consideration could result in a crucial design decision: code performing metaprogramming does not need to be verified by SV to produce code annotated with the desired contracts; it may be sufficient to apply some type of runtime verification during compile-time execution.] [Isaac: I did a major rewording since we actually have multiple compile-times and run-times, so your version is confusing, hopefully my version makes the point more clear.]

In conclusion, by leveraging over conventional OO SV techniques, we have extended the Iterative Composition form of metaprogramming with a simple contract compatibility check, to statically ensure the correctness of code produced by such metaprogramming. In particular, our approach does not require SV of the result of metaprogramming, but only requires SVing code present directly in source code. [Isaac: I'm worried about my use of statically here, as it might be misconstrued as meaning before the metaprogramming is executed, what I mean to say is before the resulting code is executed.] [In conclusion, static verification of metaprogramming is an exciting new area of research; attacking the problem by reusing conventional object oriented static verification techniques coupled with trait composition, extended to also check contract compatibility.] [Isaac: We are not doing 'static verification of metaprogramming'! How is this a 'new area of research', it might not be a popular one, but people have done it before, what they haven't dealt with is your SPECIFIC form of meta-programming. In addition, we have not presented how the research is 'exciting', finally we are not 'attacking the problem', rather we have already 'attacked the problem', since that's what this paper has done.]

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