

Using nested classes as associated types.

Authors omitted for double-bind review.

Unspecified Institution.

Abstract

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1 Introduction

Associated types are a powerful form of generics, now integrated in both Scala and Rust. They are a new kind of member, like methods, fields and nested classes. Associated types behave as ‘virtual’ types: they can be overridden, can be abstract and can have a default. However, the user has to specify those types and their concrete instantiations manually; that is, the user have to provide a complete mapping from all virtual type to concrete instantiation. When the number of associated types is small this poses no issue, but it hinders designs where the number of associated types is large. In this paper we examine the possibility of completing a partial mapping in a desirable way, so that the resulting mapping is sound and also robust with respect to code evolution.

The core of our design is to reuse the concept of nested classes instead of relying of a new kind of member for associated types. An operation, called Redirect, will redirect some nested classes in some external types. To simplify our formalization and to keep the focus on the core of our approach, we present our system on top of a simple Java like languages, with only final classes and interfaces, when code reuse is obtained by trait composition instead of conventional inheritance. As in many trait languages, we support **This** to refer to the current class. It is needed so that a method inside of a trait can refer to its eventual type. We rely on a simple nominal type system, where subtyping is induced only by implementing interfaces; in our approach we can express generics without having a polymorphic type system. To simplify the treatment of state, we consider fields and constructors to be always private. In our code examples we assume standard getters and setters to be automatically declared, together with a **static** method `of(..)` that would contain a standard constructor call, taking the value of the fields and initializing the instance. In this way we can focus our presentation to just (static) methods, nested classes and implements relationships. Expanding our presentation to explicitly include visible fields, constructors and sub-classing would make it more complicated without adding any conceptual underpinning. In our proposed setting we could write:

```
String=...
SBox={String inner;
  method String inner()=this.inner//implicit
  static method This of(String inner)=new This(inner)//implicit
myTtrait={
  Box={Elem inner}//implicit This of(Elem inner) and Elem inner()
  Elem={This concat(This that)}
  static method Box merge(Box b,Elem e){return Box.of(b.inner().concat(e));}
}
```



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```
47 Result=myTrait<Box=SBox>//equivalent to trait<Box=SBox, Elem=String>
48 ...Result.merge(SBox.of("hello "), "world");//hello world
```

Here class **SBox** is just a container of **Strings**, and **myTrait** is code encoding **Boxes** of any kind of **Elem** with a **concat** method. By instantiating **myTrait<Box=SBox>**, we can infer **Elem=String**, and obtain the following flattened code, where **Box** and **Elem** has been removed, and their occurrences are replaced with **SBox** and **String**.

```
54 Result={static method SBox merge(SBox b,String e){
55     return SBox.of(b.inner().concat(e));}}
56
```

Note how **Result** is a new class that could have been written directly by the programmer, there is no trace that it has been generated by **myTrait**. We will represent trait names with lower-case names and class/interface names with upper-case names. Traits are just units of code reuse, and do not induce nominal types.

Redirect could be applied in other ways; **Result2=myTrait<Elem=String>** for example would flatten into:

```
64 Result2={
65     Box={String inner}
66     static method Box merge(Box b,String e){
67         return Box.of(b.inner().concat(e));}}
68
```

Note how in this case, class **Result.Box** would exist. Thanks to our decision of using nested classes as associated types, the decision of what classes need to be redirected is not made when the trait is written, but depends on the specific redirect operation. Moreover, our redirect is not just a way to show the type system that our code is correct, but it can change the behaviour of code calling static methods from the redirected classes.

This example show many of the characteristics of our approach:

- (A) We can redirect mutually recursive nested classes by redirecting them all at the same time, and if a partial mapping is provided, the system is able to infer the complete mapping.
- (B) **Box** and **Elem** are just normal nested classes inside of **myTrait**; indeed any nested class can be redirected away. In case any of their (static) methods was implemented, the implementation is just discarded. In case they had fields, they are discarded too. In most other approaches, abstract/associated/generic types are special and have some restrictions; for example, in Java/Scala static methods and constructors can not be invoked on generic/associated types. With redirect, they are just normal nested classes, so there are no special restrictions on how they can be used. In our example, note how **merge** calls **Box.of(...)**.
- (C) While our example language is nominally typed, nested classes are redirected over types satisfying the same structural shape. We will show how this offers some advantages of both nominal and structural typing.

A variation of redirect, able to only redirect a single nested class, was already presented in literature. While points (B) and (C) already applies to such redirect, we will show how supporting (A) greatly improve their value.

The formal core of our work is in defining

- **ValidRedirect**, a computable predicate telling if a mapping respect the structural shapes and nominal subtype relations.
- **BestRedirect**, a formal definition of what properties a procedure expanding a partial mapping into a complete one should respect.
- **ChoseRedirect**, an efficient algorithm respecting those properties.

Before diving in the formal details, we show an example motivating that expanding the redirect map is not trivial when subtyping is taken into consideration. Consider an interface **ColorPoint** implementing **Point** and **Root**, **Left**, **Right** and **Merge** forming a diamond interface implementation, where method **m** return type is refined in **Right**, and thus stay refined in **Merge**:

```

104 Point=interface{ ...}
105 ColorPoint=interface{ implements Point ...}
106 Root=interface{Point m()}
107 Left={interface implements EA Point m()}
108 Right={interface implements EA ColorPoint m()}
109 Merge={implements Left, Right ColorPoint m()}
110 C={ Merge bind()}
111

```

Trait **t** contains **Target** with a method returning a **Result**, that implements an interface **I** with a method returning a **ColorPoint**. We include an abstract method **show** reporting in its signature **Target**, **Result** and **I**, so we can see where are they redirected to.

```

116 t={
117   I=interface{ColorPoint m()}
118   Result=interface{implements I ColorPoint m()}
119   Target={Result bind()}
120   Target show(Result r, I i)
121 }
122 Res=t<Target=C>
123

```

The big question is, what is the complete mapping inferred from **t<Target=C>**? Naively, if **Target=C**, since both **Target** and **C** have a method **bind**, we could connect their result types: **Result=Merge**. This is not acceptable, since **Result** is an interface while **Merge** is not, and more (possibly private) members inside **t** may be currently implementing **Result**, even if such members are not present now, it would be reasonable if they were added in the future, and we want our inferred map to be stable to such additions. Note however that is safe to redirect result to any interface implemented by **Merge**. Thus we have three possibilities: **Left**, **Right** and indirectly **Root**. The only possibility is **Result=Right**, since the method **m** need to return a **ColorPoint**. However, **Result** implements **I**, so also **I** need to be redirected, but to what? all possible supertypes of **Right** are a possible option, so in this case **Root** and **Right** itself. The only option here is **Right**, again method **m** need to return a **ColorPoint**. Thus, the final mapping is **Target=C, Result=Right, I=Right** and the flattening result would be **Res={C show(Right r, Right i)}**. Subtyping is a fundamental feature of object oriented programming. Our proposed redirect operator do not require the type of the target to perfectly match the structural type of the internal nested classes; structural subtyping is sufficient. This feature adds a lot of flexibility to our redirect, however completing the mapping (as happens in the example above) is a challenging and technically very interesting task when subtyping is taken into account. This is strongly connected with ontology matching and will be discussed in the technical core of the paper later on.

We first formally define our core language, then we define our redirect operator and its formal properties. Finally we motivate our model showing how many interesting examples of generics and associated types can be encoded with redirect. Finally, as an extreme application, we show how a whole library can be adapted to be injected in a different environment.

2 Language grammar and well formedness

We apply our ideas on a simplified object oriented language with nominal typing and (nested) interfaces and final classes. Code reuse is obtained by trait composition, thus the source code

would be a sequence of top level declarations D followed by a main expression; a lower-case identifier t is a trait name, while an upper case identifier C is a class name. To simplify our terminology, instead of distinguishing between nested classes and nested interfaces, we will call *nested class* any member of a code literal named by a class identifier C . Thus, the term *class* may denote either an *interface class* (interface for short) or a *final class*.

$e ::= x \mid e.m(es) \mid T.m(es) \mid e.x \mid \text{new } T(es)$	expression	$T ::= \text{This}_n.Cs$	types
$L ::= \{ \text{interface } Tz; Mz \mid \{ Tz; Mz; K \}$	code literal	$Tx ::= T x$	parameter
$M ::= \text{static? } T m(Txs) e? \mid \text{private? } C=E$	member	$D ::= id=E$	declaration
$K ::= (Txz)?$	state	$id ::= C \mid t$	class/trait id
$E ::= L \mid t \mid E_1 <+ E_2 \mid E < R$	Code Expr.	$v ::= \text{new } T(vs)$	value
$R ::= Cs_1 = T_1 \dots Cs_n = T_n$	redirect map	$LV ::= \dots$	

In the context of nested classes, types are paths. Syntactically, we represent them as relative paths of form $\text{This}_n.Cs$, where the number n identify the root of our path: This_0 is the current class, This_1 is the enclosing class, This_2 is the enclosing enclosing class and so on. $\text{This}_n.Cs$ refers to the class obtained by navigating throughout Cs starting from This_n . By using a larger then needed n , there could be multiple different types referring to the same class. We require all types to be in the form where the smallest possible n is used.

Code literals L serve the role of class/trait bodies; they contain the set of implemented interfaces Tz , the set of members Mz and their (optional) state. In the concrete syntax we will use **implements** in front of a non empty list of implemented interfaces and we will omit parenthesis around a non empty set of fields. To simplify our formalism, we delegate some sanity checks to well formedness: all the fields in the state K have different names; no two methods or nested classes with the same name (m or C) are declared in a code literal, and no nested class is named This_n for any number n ; in any method headers, all parameters have different names, and no parameter is named **this**.

A class member M can be a (private) nested class or a (static) method. Abstract methods are just methods without a body. Well formed interface methods can only be abstract and non-static. To facilitate code reuse, classes can have (static) abstract methods; code composition is expected to provide an implementation for those or, as we will see, redirect away the whole class. We could easily support private methods too, but to simplify our formalism we consider private only for nested classes. In a well formed code literal, in all types of form $\text{This}_n.Cs.C.Cs'$, if C denotes a private nested class, then Cs is empty. We assume a form of alpha-reaming for private nested classes, that will consistently rename all the paths of form $\text{This}_n.C.Cs'$, where $\text{This}_n.C$ refer to such private nested class. The trivial definition of such alpha rename is given in appendix.

Expressions are used as body of (static) methods and for the main expression. They are variables x (including **this**) and conventional (static) method calls. Field access and **new** expressions are included but with restricted usage: well formed field accesses are of form **this**. x in method bodies and $v.x$ in the main expression, while well formed **new** expressions have to be of form **new This0(xs)** in method bodies and of form v in the main expression. Those restrictions greatly simplify reasoning about code reuse, since they require different classes to only communicate by calling (static) methods. Supporting unrestricted fields and constructors would make the formalism much more involved without adding much of a conceptual underpinning. Values are of form **new** $T(vs)$.

For brevity, in the concrete syntax we assume a syntactic sugar declaring a static of method (that serve as a factory) and all fields getters; thus the order of the fields would induce the order of the factory arguments. In the core calculus we just assume such methods

193 to be explicitly declared.

194 Finally, we examine the shape of a nested class: `private? C=E`. The right hand side
 195 is not just a code literal but a code composition expression E . In trait composition, the
 196 code expression will be reduced/flattened to a code literal L during compilation. Code
 197 expressions denote an algebra of code composition, starting from code literal L and trait
 198 names t , referring to a literal declared before by $t=E$. We consider two operators: conventional
 199 preferential sum $E_1 \leftarrow E_2$ and our novel redirect $E \leftarrow Cs = T$.

200 2.1 Compilation process/flattening

201 The compilation process consists in flattening all the E into L , starting from the innermost
 202 leftmost E . This means that sum and redirect work on LV s: a kind of L , where all the
 203 nested classes are of form `private? C=LV`. The execution happens after compilation and
 204 consist in the conventional execution of the main expression e in the context of the fully
 205 reduced declarations, where all trait composition has been flattened away. Thus, execution
 206 is very simple and standard and behaves like a variation of FJ with interfaces instead of
 207 inheritance, and where nested classes are just a way to hierarchically organize code names.
 208 On the other side, code composition in this setting is very interesting and powerful, where
 209 nested classes are much more than name organization: they support in a simple and intuitive
 210 way expressive code reuse patterns. To flatten an E we need to understand the behaviour of
 211 the two operators, and how to load the code of a trait: since it was written in another place,
 212 the syntactic representation of the types need to be updated. For each of those points we
 213 will first provide some informal explanation and then we will proceed formalizing the precise
 214 behaviour.

215 2.1.1 Redirect

216 Redirect takes a library literal and produce a modified version of it where some nested classes
 217 has been removed and all the types referencing such nested classes are now referring to an
 218 external type. It is easy to use this feature to encode a generic list:

```
219 list={
220   Elem={}
221   static This0 empty()= new This0(Empty.of())
222   boolean isEmpty()= this.impl().isEmpty()
223   Elem head()= this.impl.asCons().tail()
224   This0 tail()=this.impl.asCons().tail()
225   This0 cons(Elem e)=new This0(Cons.of(e, this.impl)
226   private Impl={interface Bool isEmpty() Cons asCons()}
227   private Empty={implements This1
228     Bool isEmpty()=true Cons asCons()=../*error*/
229     ()}//() means no fields
230   private Cons={implements This1
231     Bool isEmpty()=false Cons asCons()=this
232     Elem elem Impl tail }
233   Impl impl
234 }
235
236 IntList=list<Elem=Int>
237 ...
238 IntList.Empty.of().push(3).top()=4 //example usage
239
```

240 This would flatten into

```
241 list=/*as before*/
242 //IntList=list<Elem=Int>
243 IntList={
244   //Elem={} no more nested class Elem
245
```

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```
246 static This0 empty()= new This0(Empty.of())
247 boolean isEmpty()= this.impl().isEmpty()
248 Int head()= this.impl.asCons().tail()
249 This0 tail()=this.impl.asCons().tail()
250 This0 cons(Int e)=new This0(Cons.of(e, this.impl)
251 private Impl={interface Bool isEmpty() Cons asCons()}
252 private Empty={/*as before*/}
253 private Cons={implements This1
254     Bool isEmpty()=false Cons asCons()=this
255     Int elem Impl tail }
256 Impl impl
257 }//everywhere there was "Elem", now there is "Int"
```

259 Redirect can be propagated in the same way generics parameters are propagate: For
260 example, in Java one could write code as below,

```
261 class ShapeGroup<T extends Shape>{
262     List<T> shapes;
263     ..}
264 //alternative implementation
265 class ShapeGroup<T extends Shape,L extends List<T>>{
266     L shapes;
267     ..}
268
```

270 to denote a class containing a list of a certain kind of **Shapes**. In our approach, one could
271 write the equivalent

```
272 shapeGroup={
273     MyShape={implements Shape}
274     List=list<Elem=MyShape>
275     List shapes
276     ..}
277
```

279 With redirect, shapeGroup follow both roles of the two Java examples; indeed there are two
280 reasonable ways to reuse this code

281 **Triangulation**=shapeGroup<MyShape=Triangle>, if we have a **Triangle** class and we would
282 like the concrete list type used inside to be local to the **Triangulation**,
283 or **Triangulation**=shapeGroup<List=Triangles>, if we have a preferred implementation for
284 the list of triangles that is going to be used by our **Triangulation**. Those two versions would
285 flatten as follow:

```
286 //Triangulation=shapeGroup<MyShape=Triangle>
287 Triangulation={
288     List=/*list with Triangle instead of Elem*/
289     List shapes
290     ..}
291
292 //Triangulation=shapeGroup<List=Triangles>
293 //expands to shapeGroup<List=Triangles,MyShape=Triangle>
294 Triangulation={
295     Triangles shapes
296     ..}
297
```

299 As you can see, with redirect we do not decide a priori what is generic and what is not.

300 Redirect can not always succeed. For example, if we was to attempt shapeGroup<List=Int>
301 the flattening process would fail with an error similar to a invalid generic instantiation.

302 2.1.2 Preferential sum; sum and redirect working together

303 The sum of two traits is conceptually a trait with the sum of the traits members, and the
304 union of the implemented interfaces. If the two traits both define a method with the same

name, some resolution strategy is applied. In the symmetric sum[] the two methods need to have the same signature and at least one of them need to be abstract. With preferential sum (sometimes called override), if they are both implemented, the right implementation is chosen and the left one is discarded. Since in our model we have nested classes, nested classes with the same name will be recursively composed.

We chose preferential sum since is simpler to use in short code examples.¹ Since the focus of the paper is the novel redirect operator, instead of the well known sum, we will handle summing state and interfaces in the simplest possible way: a class with state can only be summed with a class without state, and an interface can only be summed with another interface with identical methods signatures.

In literature it has been shown how trait composition with (recursively composed) nested classes can elegantly handle the expression problem and a range of similar design challenges. Here we will show some examples where sum and redirect cooperate to produce interesting code reuse patterns:

```

319 listComp=list<+{
320   Elem:{ Int geq(This e)}// -1/0/1 for smaller, equals, greater
321   static Elem max2(Elem e1, Elem e2)=if e1.geq(e2)>0 then e1, else e2
322   Elem max(Elem candidate)=
323     if This.isEmpty() then candidate
324     else this.tail().max(This.max2(this.head(), candidate))
325   Elem min(Elem candidate)=...
326   This0 sort()=...
327 }
328

```

As you can see, we can *extends* our generic type while refining our generic argument: **Elem** of **listComp** now needs a **geq** method.

While this is also possible with conventional inheritance and F-Bound polymorphism, we think this solution is logically simpler than the equivalent Java

```

334 class ListComp<Elem extends Comparable<Elem>> extends LinkedList<Elem>{
335   ../*body as before*/
336 }
337

```

Another interesting way to use sum is to modularize behaviour delegation: consider the following (not efficient for the sake of compactness) implementation of **set**, where the way to compare elements is not fixed:

```

342 set:{
343   Elem:{
344     List=list<Elem=Elem>
345     static This0 empty()= new This0(List.empty())
346     Bool contains(Elem e)=../*uses eq and hash*/
347     Int size()=..
348     This add(Elem e)=...
349     This remove(Elem e)=...
350     Bool eq(Elem e1,Elem e2)//abstract
351     Int hash(Elem e)//abstract
352     List asList //to allow iteration
353   }
354   eqElem={
355     Elem={ Bool equals(Elem e)//abstract*/}
356     Bool eq(Elem e1,Elem e2)=e1.equals(e2)
357   }
358   hashElem={
359

```

¹ symmetric sum is often presented in conjunction with a restrict operator that makes some methods abstract.


```

360   Elem={ Int hash(Elem e)/*abstract*/
361         Int hash(Elem e)=e.hash()
362         }
363   Strings=(set<+eqElem<+eqHash)<Elem=String>
364   LongStrings=(set<+eqElem)<Elem=String> <+{
365     Int hash(String e)=e.size()
366   }//for very long strings, size is a faster hash

```

Note how `(set<+eqElem<+eqHash)<Elem=String>` is equivalent to `set<Elem=String> <+eqElem<Elem=String> <+eqHash<Elem=String>`.

Consider the signature `Bool equals(Elem e)`. This is different from the common signature `Bool equals(Object e)`. What is the best signature for `equals` is an open research question, where most approaches advise either the first or the second one. Our `eqElem`, as written, can support both: `Strings` would be correctly define both if `String.equals` signature has a `String` or an `Object` parameter. EXPAND on method subtyping.

2.2 Moving traits around in the program

It is not trivial to formalize the way types like `This1.A.B` have to be adapted so that when code is moved around in different depths of nesting the refereed classes stay the same. This is needed during flattening, when a trait t is reused, but also during reduction, when a method body is inlined in the main expression, and during typing, where a method body is typed depending on the signature of other methods in the system.

To this aim we define a concept of program $p ::= Ds; DVz$ where $DV ::= id=LV$; as a representation of the code as seen from a certain point inside of the source code. It is the most interesting form of the grammar, used for virtually all reduction and typing rules. On the left of the ‘;’ is a stack representing which (nested) declaration is currently being processed, the bottom of the stack (rightmost) D represents the top level declaration of the source-program that is currently being processed, while the other elements of the stack are nested classes nested inside of each other. The right of the ‘;’ represents the top-level declarations that have already been compiled, this is necessary to look up top-level classes and traits. Summarizing, each of the $D_0 \dots D_n$ represents the outer nested level $0..n$, while the DVs component represent the already flattened portion of the program top level, that is the outer nested level $n + 1$. Thus, for example in the program

```

392   A={()}
393   t={ B={()}   This1.A m(This0.B b)}
394   C={D={E=t}}
395   H=t<B=A>
396

```

the flattened body of `C.D.E` will be `{ B={()} This3.A m(This0.B b)}`, where the path `This1.A` is now `This3.A` while the path `This0.B` stays the same: types defined internally will stay untouched. The program p in the observation point `E=t` is

```

401   A={()}
402   t={ B={()}   This1.A m(This0.B b)}
403   C={D={E=t}};
404   C={D={E=t}}; //this means, we entered in C
405   D={E=t} //this means, we entered in D
406

```

In order to fetch the code literals corresponding to t , we define notation $p[t]$ ($=\{ B={()} This3.A m(This0.B b)\}$). Such notation transforms the types so that they keep referring to the same nested classes. We also rely on the notation $p[T]$, to extract just methods and the list of implemented interfaces, in a form were they are useful for direct comparison with T . for example, if the program contains `{B={} This0 m(This0.B x)}` in position `This2.A`,

$p[\text{This2.A}]$ would be $\{\text{This2.A } m(\text{This2.A.B } x)\}$. We also use notation $L[C = E]$ to update the code expression in C to E , and $p.\min(T) = T'$ to minimize types to the required form when the n is as small as possible. For space reasons, those notations are defined in the appendix. Moreover, also type system and the reduction of the main program are in appendix. They are very straight forward: thanks to flattening, they are a simple nominal type system and reduction over a FJ-like language, with no generics or special method dispatch rules.

3 Flattening

Flattening is defined by reduction arrow $Ds \Rightarrow Ds'$, where eventually Ds' is going to reach form DVs and $p; id \vdash E \Rightarrow E'$, where eventually E' is going to reach form LV . The id represents the identifier of the type/trait that we are currently compiling, it is needed since it will be the name of This_0 , and we use to the fact that refers to the same nested class as $\text{This}_1.id$. Rule (TOP) selects the leftmost $id=E$ where E is not of form LV and DVz : a well typed subset of the preceeding declarations. E is flattened in the context of such DVz , thus by rule (TRAIT) DVz must contain all the trait names used in E . In the judgement $p; id \vdash E \Rightarrow E'$ id is only used in order to grow the program p in rule (L-ENTER), and p itself is only needed for (REDIRECT). The (CTXV) rule is the standard context, the (L-ENTER) rule propagates compilation inside of nested-classes, (TRAIT) merely evaluates a trait reference to it's defined body, finally (SUM) and (REDIRECT) perform our two meta-operations by propagating to corresponding auxiliary definitions. We will present those two rules in the two sections below. Note how we require their input to be already in the *minimized* form, that is, all the T uses the shortest way to refer to their corresponding nested class. This prevents the programmer from expressing some difficult cases. Consider for example using two different ways to refer to A , redirect A and then adding it back:

```

B = ...
X = { A: {}      Void m(This1.X.A p1, This0.A p2)} <A=B> <+ {A: {}>
//should flattening redirect only p2 or also p1
X = { A: {}      Void m(??? p1, This1.B p2)}

```

The complete L42 language solves those issues, but here we present a simplified version.

3.1 Sum

Rule (SUM) just delegate the work on the auxiliary notation defined below:

Def: $L_1 \lt+ L_2 = \text{interface? } \{Tz_1 \cup Tz_2; Mz \lt+ Mz', Mz_1, Mz_2; K?\}$

$L_1 = \text{interface? } \{Tz_1; Mz, Mz_1; K?_1\}$ $L_2 = \text{interface? } \{Tz_2; Mz', Mz_2; K?_2\}$
 $\{empty, K?_1, K?_2\} = \{empty, K?\}$

if $\text{interface?} = \text{interface}$ then $m\text{dom}(L_1) = m\text{dom}(L_2)$

Def: $Tm(Txs)e? \lt+ Tm(Txs)e = Tm(Txs)e$

Def: $Tm(Txs)e? \lt+ Tm(Txs) = Tm(Txs)e?$

Def: $(C=L) \lt+ (C=L') = C = L \lt+ L,$

As usual in definitions of sum operators, the implemented interfaces is the union of the interfaces of L_1 and L_2 , the members with the same domain are recursively composed while the members with disjoint domains are directly included. Since method and nested class identifiers must be unique in a well formed L and $M_1 \lt+ M_2$ being defined only if the identifier is the same, our definition forces $\text{dom}(Mz) = \text{dom}(Mz')$ and $\text{dom}(Mz_1)$ disjoint $\text{dom}(Mz_2)$. For simplicity here we require at most one class to have a state; if both have no state, the result will have no state, otherwise the result will have the only present state (the set $\{empty, K?\}$ mathematically express this requirement in a compact way); we also

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allow summing only interfaces with interfaces and final classes with final classes. When two interfaces are composed both sides must define the same methods. This is because other nested classes inside L_1 may be implementing such interface, and adding methods to such interface would require those classes to somehow add an implementation for those methods too. In literature there are expressive ways to soundly handle merging different state, composing interfaces with final classes and adding methods to interfaces, but they are out of scope in this work.

Member composition $M_1 \leftarrow M_2$ uses the implementation from the right hand side, if available, otherwise if the right hand side is abstract, the body is taken from the left side. Composing nested classes, not how they can not be **private**; it is possible to sum two literals only if their private nested classes have different private names. This constraint can always be obtained by alpha-renaming them.

3.2 Redirect

Rule (REDIRECT) is the centre of our interest for this work. As for sum we check that the LV is in minimized form. Moreover, to have a single data structure p' where all the types correctly points to the corresponding nested classes, we add the L to the top of our current program. Notation R/id is defined as

$Cs_0 = \text{This}_n.C.Cs = Cs_0 = \text{This}_{n+1}.C.Cs$, where either $C \neq id$ or $n > 0$

In addition of adding 1 to all the types provided in the redirect map, since they were relative to p and not p' , it also checks that R actually refers to types external of LV , by preventing types of form $\text{This}_0.id.$.

Notation $p.\text{redirectSet}(R)$ computes the set of nested classes that need to be redirected if R is redirected. This is information dependent just from LV (the top of the program) and the domain of R . RedirectSet is easily computable.

$$\begin{aligned} \text{dom}(R) &\subseteq p.\text{redirectSet}(R) \\ \text{internals}(\text{reachables}(p[\text{This}_0.Cs])) &\subseteq p.\text{redirectSet}(R) \quad \text{with } Cs \in p.\text{redirectSet}(R) \\ \text{reachables}(\text{interface? } \{Tz; Mz; K?\}) &= Tz, \text{reachables}(Mz) \\ \text{reachables}(\text{static? } T_0m(T_1x_1 \dots T_nx_n)e?) &= T_0 \dots T_n \\ \text{internals}(Tz) &= \{Cs \mid \text{This}_0.Cs \in Tz\} \end{aligned}$$

The intuition behind redirectSet is that if the signature of a nested class mentions another nested class, they must be redirected together. Consider the following simple example:

```

481 t={A={B size()} B={} ...}
482
483 Res=t<A=String>
484

```

If we were to redirect **A**, we would need to redirect also **B**: the type **B** is nested inside **t**, thus **String** would not be able to reach it. The only reasonable solution is to redirect **A** and **B** together.

For our redirection (and $p'.\text{bestRedirection}()$) to be well defined, we need to check that $p.\text{redirectable}(Cs)$. This is again a check local to the LV (the top of the program) and is also easily computable.

$$\begin{aligned} \text{redirectable}(p, Cs) &\text{iff} \\ &\text{empty} \notin Cs \\ &\text{if } Cs \in Cs \text{ then } \text{This}_0.Cs \in \text{dom}(p) \\ &\text{if } Cs \in Cs \text{ and } C \in \text{dom}(p(\text{This}_0.Cs)) \text{ then } Cs.C \in Cs \\ &\text{if } Cs.C \in Cs \text{ then } p(\text{This}_0.Cs) = \text{interface? } \{ _ ; C=L _ ; _ \} \end{aligned}$$

That is, the empty path is not redirectable, every nested class of a redirect path must be redirected away, and all paths must traverse only non-private C .

■ **Figure 1** Flattening

Def: $Ds \Rightarrow Ds'$ and $p; id \vdash E \Rightarrow E'$, where $\mathcal{E}_V ::= \square \mid \mathcal{E}_V <+ E \mid LV <+ \mathcal{E}_V \mid \mathcal{E}_V < Cs = T >$
(TOP)

$$\begin{array}{c}
 DVz \subseteq DVs \\
 DVz \vdash \mathbf{Ok} \\
 \hline
 empty; DVz; id \vdash E \Rightarrow E' \\
 \hline
 DVs \text{ id}=EDs \Rightarrow DVs \text{ id}=E'Ds
 \end{array}
 \quad
 \begin{array}{c}
 (L\text{-ENTER}) \\
 \hline
 p.\mathbf{push}(id=L[C=E]); C \vdash E \Rightarrow E' \\
 \hline
 p; id \vdash L[C=E] \Rightarrow L[C=E']
 \end{array}
 \quad
 \begin{array}{c}
 (TRAIT) \\
 \hline
 p; id \vdash t \Rightarrow p[t]
 \end{array}$$

$$\begin{array}{c}
 (REDIRECT) \\
 \hline
 LV = p.\mathbf{min}(id=LV) \\
 p' = p.\mathbf{push}(id=LV) \\
 Csz = p'.\mathbf{redirectSet}(R/id) \\
 p'.\mathbf{redirectable}(Csz) \\
 R' = p'.\mathbf{bestRedirection}(R/id) \\
 \hline
 p; id \vdash LV <+ LV_2 \Rightarrow LV \quad p; id \vdash LV <R> \Rightarrow R'(LV.\mathbf{remove}(Csz))
 \end{array}$$

$$\begin{array}{c}
 (SUM) \\
 \hline
 LV_i = p.\mathbf{min}(id=LV_i) \\
 LV_1 <+ LV_2 = LV \\
 \hline
 p; id \vdash LV_1 <+ LV_2 \Rightarrow LV
 \end{array}$$

Finally, $p.\mathbf{bestRedirection}(R)$, given a p and an R that are valid input for redirection as defined above can denote the best complete map, mapping any element of Csz into a suitable type in p . This is the centerpiece of our formal framework and his definition will be the main topic of the next section.

Given the complete mapping R' , to produce the flattened result we first remove all the elements of Csz from LV , and then we apply R' as a rename, renaming all internal paths $Cs \in Csz$ to the corresponding external type $R'(Cs)$. Those two notations are formally defined as following:

$$\begin{aligned}
 LV.\mathbf{remove}(Cs_1 \dots Cs_n) &= LV.\mathbf{remove}(Cs_1) \dots \mathbf{remove}(Cs_n) \\
 LV[C.s.C = _].\mathbf{remove}(Cs.C) &= LV \text{ where } Cs.C \notin \text{dom}(LV) \\
 R(L) &= R_{empty}(L) \\
 R_{Cs}(\mathbf{interface?} \{Tz; Mz; K?\}) &= \mathbf{interface?} \{R_{Cs}(Tz); R_{Cs}(Mz); R_{Cs}(K?)\} \\
 R_{Cs}(C=L) &= C=R_{Cs.C}(L) \\
 R_{Cs}(M), R_{Cs}(e), R_{Cs}(K) &\quad \text{simply propagate on the structure until } T \text{ is reached} \\
 R_{C_1 \dots C_n}(T) &= \mathbf{This}_{n+k+1}.Cs' \quad \text{where } T.\mathbf{from}(\mathbf{This}_0.C_1 \dots C_n) = \mathbf{This}_0.Cs, R(Cs) = \mathbf{This}_k.Cs' \\
 \text{otherwise } R_{Cs}(T) &= T
 \end{aligned}$$

The second clause of $\mathbf{remove}(r)$ requires the Cs to be ordered in such a way where the inner-most nested classes are removed first. Rename must keep track of the explored Cs in order to distinguish internal paths that need to be renamed, and the mapped type need to look out of the whole explored Cs and the top level code literal (thus $n + k + 1$).

4 BestRedirect

Best redirection balance three aspects:

- **Validity:** the selected redirect map must be valid. This means that if the mapping is applied to well typed code (as in the rule (REDIRECT)) then the result is still well typed.
- **Stability:** this means that changing little details on the code base (as for example adding a new nested class) do not change the selected map.
- **Specificity:** when multiple options are available, the most specific is chosen.

To better divide the various aspect, we will use functions of form $(p, R) \rightarrow Rz$, producing valid mappings for any program p and starting map R . All of those functions will respect

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516 **possibleRedirections**. Rule REDIRECT ensures **possibleRedirections** for the input mapping,
 517 here we check that is also verified for the complete mapping.

$$\begin{array}{c}
 \frac{R' \in \text{possibleRedirections}(p, R) \text{ if} \\
 \quad R \subseteq R' \\
 \quad \text{dom}(R') = \text{redirectSet}(p, R) \\
 \quad (p, R') \in \text{validProblems}}{
 \begin{array}{c}
 518 (p, Cs_1 = T_1 \dots Cs_n = T_n) \in \text{validProblems} \text{ iff } \forall i \in 1..n : \\
 \quad p.\text{minimize}(T_i) = T_i \\
 \quad T_i \text{ not of form } \text{This}_0. _ \\
 \quad p \vdash p[T] : \text{OK} \\
 \quad \text{redirectable}(p, \text{redirectSet}(p, R))
 \end{array}
 }
 \end{array}$$

519 One of those functions is the most complete: **validRedirections**. It is based on the
 520 judgement $p \vdash T \subseteq L$ to be read as: under the program p , the type T is structurally a
 521 subtype of the literal L . Some more auxiliary notation is used: the obvious **isInterface** and
 522 the more interesting **superClasses** and method subtyping $p \vdash M \leq M'$. In **superClasses** we
 523 add T so that F-Bound polymorphism may work as expected, so that is possible to redirect
 524 **{implements Foo}** not only to any class implementing **Foo** but also to **Foo** itself. Method
 525 subtyping is given in the expressive form where the return type can be more specific, and the
 526 parameter types can be more general. PUT LATER? However, the type system of the language
 527 is more restrictive when it comes to refine an interface method, allowing only return type
 528 refinement. This is not just to align our calculus with existing languages like Java/C# and
 529 C++, but is required to make reasoning about parameter types influential while expanding
 530 redirect mappings. END PUT LATER

$$\begin{array}{c}
 \frac{R' \in \text{validRedirections}(p, R) \text{ iff} \\
 \quad R' \in \text{possibleRedirections}(p, R) \\
 \quad \forall Cs \in \text{dom}(R') \quad p \vdash p[R'(Cs)] : R'(Cs) \subseteq R'(p[Cs]) : Cs}{
 \begin{array}{c}
 p \vdash P \subseteq \text{interface? } \{Tz; Mz; _ \} \text{ iff} \\
 \quad Tz \subseteq \text{superClasses}(p, P) \\
 \quad \forall m \in \text{dom}(Mz) : p \vdash p[P](m) \leq Mz(m) \\
 531 \quad \text{if } \text{interface?} = \text{interface} \text{ then } \forall m \in \text{dom}(p[P]) \quad p \vdash Mz(m) \leq p[P](m) \\
 \quad \text{if } \text{interface}(p[P]) \text{ then } \text{staticTm}(Txs) _ \notin Mz \text{ else } \text{interface?} = \text{empty} \\
 \text{isInterface}(L) \text{ iff } L = \{ \text{interface } _ ; _ \} \\
 \text{superClasses}(p, T) = \{T\} \cup \text{superClasses}(T_1) \cup \dots \cup \text{superClasses}(T_n) \\
 \quad \text{with } p[T] = \text{interface? } \{T_1 \dots T_n; _ ; _ \} \\
 p \vdash \text{static? } T'_0 m(T_1 x_1 \dots T_n x_n) _ \leq \text{static? } T_0 m(T'_1 x'_1 \dots T'_n x'_n) _ \\
 \quad \text{with } T_0 \in \text{superClasses}(p, T'_0) \dots T_n \in \text{superClasses}(p, T'_n)
 \end{array}
 }
 \end{array}$$

532 Note how **validRedirections**, while mathematically sound, is incredibly hard to compute:
 533 while it is easy to check if a certain $R' \in \text{validRedirections}(p, R)$, finding naively all such
 534 R' would require examining every possible permutation. In particular, subtyping allows for
 535 redirections to be conceptually took out of thin-air. Consider the following example:

```

536 I=interface {...}
537 A= {method A m(I x)}
538 C={implements I ...}
539 t={B: {} T: {method T m(B x)}}
540 Res=t<T=A>
541

```

543 Clearly, selecting **C** as a candidate to complete the map is a valid choice but is also an
 544 arbitrary choice that should not be made while automatically completing the mapping. What
 545 if type **D**={implements I ...} was introduced while maintaining the program? the completed
 546 redirect map may change unpredictably. To avoid those issues, we define the concept of

547 Similar programs:

548 $DLs; DVz DVz' \in \text{similarPrograms}(DLs; DVz)$

549 Note how we just add new declarations at the outermost level. We will later prove that
 550 this is sufficient to ensure that adding/removing unrelated classes anywhere in the program
 551 would still not change the selected completed mapping. Finally, we have all the pieces to
 552 define **bestRedirection**: the objective of our quest is finally here for us puny readers to be
 553 understood.

$$\begin{array}{l} \text{bestRedirection}(p, R) = \text{stableMostSpecific}(p, R, \text{validRedirections}) \\ \text{stableMostSpecific}(p, R, f) = R_0 \text{ iff } \forall p' \in \text{similarPrograms}(p) \\ R_0 \in f(p', R) \text{ and } \forall R_1 \in f(p', R) \text{ moreSpecific}(p, R_0, R_1) \\ \text{moreSpecific}(p, Cs_1 = T_1 \dots Cs_n = T_n, Cs_1 = T'_1 \dots Cs_n = T'_n) \\ T_1 \in \text{superClasses}(p', T'_1) \dots T_n \in \text{superClasses}(p', T'_n) \end{array}$$

554 The best redirection is a valid redirection that is the most specific across all similar
 555 programs. While **bestRedirection** in the current form is not practically computable, it
 556 is clear from the formulation a good stepping stone to obtain a computable algorithm
 557 would be to replace **validRedirections** with an computable algorithm producing a subset of
 558 **validRedirections** and behaving identically for all the **similarPrograms**.

560 5 Appendix?

561 $\mathcal{E}_V ::= \square \mid \mathcal{E}_V \leftarrow E \mid LV \leftarrow \mathcal{E}_V \mid \mathcal{E}_V \leftarrow Cs = T >$ context of library-evaluation
 $\mathcal{E}_v ::= \square \mid \mathcal{E}_v.m(es) \mid v.m(vs \mathcal{E}_v es) \mid T.m(vs \mathcal{E}_v es)$

562 6 Type System

563 The type system is split into two parts: type checking programs and class literals, and the
 564 typechecking of expressions. The latter part is mostly conventional, it involves typing judgments
 565 of the form $p; Txs \vdash e : T$, with the usual program p and variable environment Txs (often
 566 called Γ in the literature). rule (*Dsok*) type checks a sequence of top-level declarations by
 567 simply push each declaration onto a program and typecheck the resulting program. Rule *pok*
 568 typechecks a program by check the topmost class literal: we type check each of it's members
 569 (including all nested classes), check that it properly implements each interface it claims to,
 570 does something weird, and finanly check check that it's constructor only referenced existing
 571 types,

572

573

574 Define $p \mid - \text{Ok}$

575 =====

576

577 $D1; Ds \mid - \text{Ok} \dots Dn; Ds \mid - \text{Ok}$

578 $(Ds \text{ ok}) \text{ ----- } Ds = D1 \dots Dn$

579 $Ds \mid - \text{Ok}$

580

581 $p \mid - M1 : \text{Ok} \dots p \mid - Mn : \text{Ok}$

582 $p \mid - P1 : \text{Implemented} \dots p \mid - Pn : \text{Implemented}$

583 $p \mid - \text{implements}(Pz; Ms) \text{ /*WTF?*/}$ if $K? = K: p.\text{exists}(K.Txs.Ts)$

584 $(p \text{ ok}) \text{ ----- } p.\text{top}() = \text{interface? } \{P1 \dots Pn; M1, \dots, Mn; K?$

585 $p \mid - \text{Ok}$

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```

586
587 p.minimize(Pz) subseq p.minimize(p.top().Pz)
588 amt1 _ in p.top().Ms ... amtn _ in p.top().Ms
589 (P implemented) ----- p[P] = interface {Pz; amt1 ..
590 p |- P : Implemented
591
592 (amt-ok) ----- p.exists(T, Txs.Ts)
593 p |- T m(Tcs) : Ok
594
595 p; This0 this, Txs |- e : T
596 (mt-ok) ----- p.exists(T, Txs.Ts)
597 p |- T m(Tcs) e : Ok
598
599 C = L, p |- Ok
600 (cd-Ok) -----
601 p |- C = L : OK
602

```

603 Rule (*Pimplemented*) checks that an interface is properly implemented by the program-
604 top, we simply check that it declares that it implements every one of the interfaces super-
605 interfaces and methods. Rules (*amt - ok*) and (*mt - ok*) are straightforward, they both
606 check that types mentioned in the method signature exist, and ofcourse for the latter case,
607 that the body respects this signature.

608 To typecheck a nested class declaration, we simply push it onto the program and typecheck
609 the top-of the program as before.

610 The expression typesystem is mostly straightforward and similar to feartherwiegth Java,
611 notable we use $p[T]$ to look up information about types, as it properly ‘from’s paths, and
612 use a classes constructor definitions to determine the types of fields.

```

613 Define p; Txs |- e : T
614 =====
615 (var)
616 ----- T x in Txs
617 p; Txs |- x : T
618
619 (call)
620 p; Txs |- e0 : T0
621 ...
622 p; Txs |- en : Tn
623 ----- T' m(T1 x1 ... Tn xn) _ in p[T0].Ms
624 p; Txs |- e0.m(e1 ... en) : T'
625
626 (field)
627 p; Txs |- e : T
628 ----- p[T].K = constructor(_ T' x _)
629 p; Txs |- e.x : T'
630
631
632 (new)

```

```

633 p; Txs |- e1 : T1 ... p; Txs |- en : Tn
634 ----- p[T].K = constructor(T1 x1 ... Tn xn)
635 p; Txs |- new T(e1 ... en)
636
637
638 (sub)
639 p; Txs |- e : T
640 ----- T' in p[T].Pz
641 p; Txs |- e : T'
642
643
644 (equiv)
645 p; Txs |- e : T
646 ----- T =p T'
647 p; Txs |- e : T'

```

7 Graph example

We now consider an example where Redirect simplifies the code quite a lot: We have a **Node** and **Edge** concepts for a graph. The **Node** have a list of **Edges**. A **isConnected** function takes a list of **Nodes**. A **getConnected** function takes **Node** and return a set of **Nodes**.

```

652 graphUtils={
653   Edges:list<+{Node start() Node end()}
654   Node:{Edges connections()}
655   Nodes:set<Elem=Node> //note that we do not specify equals/hash
656   static Bool isConnected(Nodes nodes)=
657     if(nodes.size()==0) then true
658     else getConnected(nodes.asList().head()).size()==nodes.size()
659   static Nodes getConnected(Node node)=getConnected(node,Nodes.empty())
660   static Nodes getConnected(Node node,Nodes collected)=
661     if(collected.contains(node)) then collected
662     else connectEdges(node.connections(),collected.add(node))
663   static Nodes connectEdges(Edges e,Nodes collected)=
664     if( e.isEmpty()) then collected
665     else connectEdges(e.tail(),collected.add(e.head().end()))
666 }
667
668

```

We have shown the full code instead of omitting implementations to show that the code inside of an highly general code like the former is pretty conventional. Just declare nested classes as if they was the concrete desired types. Note how we can easily create a new **Nodes**@ by doing **Nodes.empty()**.

Here we show how to instantiate **graphUtils** to a graph representing cities connected by streets, where the streets are annotated with their length, and **Edges** is a priority queue, to optimize finding the shortest path between cities.

```

676 Map:{
677   Street:{City start, City end, Int size}
678   City:{}
679   Streets:priorityQueue<Elem=Street><+{
680     Int geq(Street e1, Street e2)=e1.size()-e2.size()
681   }><+{
682     Streets:{}
683     City:{Streets connections, Int index} //index identify the node
684     Cities:set<Elem=City><+{
685       Bool eq(City e1, City e2) e1.index==e2.index
686       Int hash(City e) e.index
687     }
688   }
689 }

```


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```

688     }
689     Cities cities
690     //more methods
691 }
692 MapUtils=graphUtils<Nodes=Map.Cities>
693 //infers Nodes.List, Node, Edges, Edge
694

```

695 In Appending 2 we will show our best attempt to encode this graph example in Java,
696 Rust and Scala. In short, we discovered...

697 FROM and minimize that will go in the appendix:

698 To fetch a trait form a program, we will use notation $p(t) = LV$, to fetch a class we will
699 use $p(T)$.

700 To look up the definition of a class in the program we will use the notation $p(T) = LV$,
701 which is defined by the following:

$$\begin{aligned}
 (DLs; DVs).push(id=L) &:= id=L, DLs; DVs \\
 (; _, C=L, _)(\text{This}_0.C.Cs) &:= L(Cs) \\
 p.push(_=L)(\text{This}_0.Cs) &:= L(Cs) \\
 p.push(_)(\text{This}_{n+1}.Cs) &:= p(\text{This}_n.Cs) \\
 LV(\emptyset) &:= LV \\
 \text{interface? } \{ _; _, C=L_0, _; _ \} (C.Cs) &:= L_0(Cs)
 \end{aligned}$$

702 where $L = a$

703 This notation just fetch the referred LV without any modification. To adapt the paths
704 we define $T_0.\text{from}(T_1, j)$, $L.\text{from}(T, j)$ and $p.\text{minimize}(T)$ as following:

$$\begin{aligned}
 \text{This}_n.Cs.\text{from}(T, j) &:= \text{This}_n.Cs \quad \text{with } n < j \\
 \text{This}_{n+j}.Cs.\text{from}(\text{This}_m.C_1 \dots C_{k,j}) &:= \text{This}_{m+j}.C_1 \dots C_{k-n} \quad \text{with } n \leq k \\
 \text{This}_{n+j}.Cs.\text{from}(\text{This}_m.C_1 \dots C_{k,j}) &:= \text{This}_{m+j+n-k}.C_1 \dots C_{k-n}Cs \quad \text{with } n > k \\
 \{ \text{interface? } Tz; Mz; K \}.\text{from}(T, j-1) &:= \{ \text{interface? } Tz.\text{from}(T, j); Mz.\text{from}(T, j); K.\text{from}(T, j) \} \\
 p.\text{minimize}(T) &:= T' \dots
 \end{aligned}$$

706 Finally, we we combine those to notation for the most common task of getting the value of a
707 literal, in a way that can be understand from the current location: $p[t]$ and $p[T]$:

$$\begin{aligned}
 (DL_1 \dots DL_n; _, t=LV, _)[t] &:= LV.\text{from}(\text{This}_n) \\
 p[T] &:= p.\text{minimize}(p(T).\text{from}(T))
 \end{aligned}$$

```

712
713 - towel1:.. //Map: towel2:.. //Map: lib: T:towel1 f1 ... fn
714   MyProgram: T:towel2 Lib:lib[T=This0.T] ... -

```

8 extra

716 Features: Structural based generics embedded in a nominal type system. Code is Nominal,
717 Reuse is Structural. Static methods support for generics, so generics are not just a trik to
718 make the type system happy but actually change the behaviour Subsume associate types.
719 After the fact generics; redirect is like mixins for generics Mapping is inferred-> very large
720 maps are possible -> application to libraries

721 In literature, in addition to conventional Java style F-bound polymorphism, there is
722 another way to obtain generics: to use associated types (to specify generic paramaters) and
723 inheritance (to instantiate the paramaters). However, when parametrizing multiple types,

the user to specify the full mapping. For example in Java interface A B m(); interface BString f(); class G<TA extends A<TB>, TB> //TA and TB explicitly listed String g(TA a TB b) return a.m().f(); class MyA implements A<MyB>.. class MyB implements B .. G<MyA,MyB> //instantiation Also scala offers generics, and could encode the example in the same way, but Scala also offers associated types, allowing to write instead....

Rust also offers generics and associated types, but also support calling static methods over generic and associated types.

We provide here a foundational model for genericity that subsume the power of F-bound polymorphisms and associated types. Moreover, it allows for large sets of generic parameter instantiations to be inferred starting from a much smaller mapping. For example, in our system we could just write $g = \lambda A. \lambda m. \lambda B. \lambda f. \lambda g. \lambda a. \lambda b. a.m().f()$ $MyA = \lambda m. \lambda B. \lambda f. \lambda g. \lambda a. \lambda b. a.m().f()$ $MyB = \lambda f. \lambda g. \lambda a. \lambda b. \text{"Hello"}$.. $g < A = MyA, B = MyB >$ //instantiation. The mapping $A = MyA, B = MyB$

We model a minimal calculus with interfaces and final classes, where implementing an interface is the only way to induce subtyping. We will show how supporting subtyping constitute the core technical difficulty in our work, inducing ambiguity in the mappings. As you can see, we base our generic matches the structure of the type instead of respecting a subtype requirement as in F-bound polymorphisms. We can easily encode subtype requirements by using implements: $Print = \text{interface } \lambda f. \lambda g. \lambda a. \lambda b. a.f()$ $g = \lambda A. \lambda f. \lambda g. \lambda a. \lambda b. a.f()$ $Print$ $method A printMe(A a1, A a2) \text{ if } (a1.print().size() > a2.print().size()) \text{ return } a1; \text{ return } a2;$ $MyPrint = \text{implements } Print$.. $g < A = MyPrint >$ //instantiation $g < A = Print >$ //works too

————— example showing ordering need to strictly improve EI1: interface EA1: implements EI1

EI2: interface EA2: implements EI2

EB: EA1 a1 EA1 a1

A1: A2: B: A1 a1 A2 a2 [B = EB] // A1 -> EI1, A2 -> EA2 a // A1 -> EA1, A2 -> EI2 b // A1 -> EA1, A2 -> EA2 c

$a \leq b \quad b \leq a \quad c \leq a, b \quad a \leq c$

hi Hi class

$a ::= b \quad c$

aaHiHi class qa q $a ::= b \quad c$

$a ::= b \quad c$

}} [()]
(TOP)

$a \xrightarrow{b} c \quad \forall i < 3 \quad a \vdash b : \text{OK}$

$\frac{\forall i < 3 \quad a \vdash b : \text{OK}}{1 + 2 \rightarrow 3} \quad \begin{matrix} a \\ b \\ c \end{matrix}$