Using Capabilities for Strict Runtime Invariant Checking

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Abstract

In this paper we use pre-existing language support for both reference and object capabilities to enable sound runtime verification of representation invariants. Our invariant protocol is stricter than the other protocols, since it guarantees that invariants hold for all objects involved in execution. Any language already offering appropriate support for reference and object capabilities can support our invariant protocol with minimal added complexity. In our protocol, invariants are simply specified as methods whose execution is statically guaranteed to be deterministic and to not access any externally mutable state. We formalise our approach and prove that our protocol is sound, in the context of a language supporting mutation, dynamic dispatch, exceptions, and non-deterministic I/O. We present case studies showing that our system requires a lighter annotation burden compared to Spec#, and performs orders of magnitude less runtime invariant checks compared to the 'visible state semantics' protocols of D and Eiffel. [Isaac: When we said "widlely" used, we mean visible state semantics is, not the D and Eiffel languages]

Keywords: reference capabilities, object capabilities, runtime verification, class invariants

1. Introduction

Representation invariants (sometimes called class invariants, object invariants, or type refinements) are a useful concept when reasoning about software correctness, particularly with Object Oriented (OO) languages. Such invariants are predicates on the state of an object and its reachable object graph (ROG). They can be presented as documentation, checked as part of static verification, or, as we do in this paper, monitored for violations using runtime verification. In our system, a class specifies its invariant by defining a method called invariant() that returns a boolean. We say that an object's invariant holds when its invariant() method would return true. In a purely functional setting, sound runtime checking is trivial: the runtime simply needs to check the invariant each time a value/object is created (or in the case of refinement types, converted to such a type).

In an impure setting, like most OO languages, operations on data structures are often implemented as complex sequences of mutations, where the invariant is temporarily broken. To support this behaviour, most invariant protocols present in the literature allow invariants to be broken and observed broken. The two main forms of invariant protocols are visible state semantics [2] and the Pack-Unpack/Boogie methodology [3]. In visible state semantics, invariants can be broken when a method on the object is active (that is, currently executing). Some interpretations of the visible state are more permissive, requiring the invariants of receivers to hold only before and after every public method call, and after constructors. In the pack-unpack approach, objects are either in a 'packed' or 'unpacked' state, the invariant of 'packed' objects must hold, whereas

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¹We do this (as in Dafny [1]) to minimise the special treatment of invariants, whereas other approaches often treat invariants as a special annotation with its own syntax.

unpacked objects can be broken. To complicate matters further, OO languages often permit rampant aliasing of mutable state, thus any mutation may inadvertently break the invariant of an arbitrary object.

In this paper we propose a much stricter invariant protocol: at all times, the invariant of every object involved in execution must hold; thus they can be broken when the object is not (currently) involved in execution. An object is *involved in execution* when it is in the reachable object graph of any of the objects mentioned in the method call, field access, or field update that is about to be reduced; we state this more formally later in the paper.

Our strict protocol supports easier reasoning: an object can never be observed broken. However at first glance it may look overly restrictive, preventing useful program behaviour. Consider the iconic example of a Range class, with a min and max value, where the invariant requires that min<max:

```
class Range{
   private field min; private field max;
   method invariant(){ return min<max; }
   method set(min, max){
     if(min>=max){ throw new Error(/**/); }
     this.min = min;
   this.max = max;
}
```

In this example we omit types to focus on the runtime semantics. The code of set does not violate visible state semantics: this.min = min may temporarily break the invariant of this, however it will be fixed after executing this.max = max. Visible state allows such temporary breaking of invariants since we are inside a method on this, and by the time it returns, the invariant will be re-established. However, if min is \geq this.max, set will violate our stricter approach. The execution of this.min = min will break the invariant of this and this.max = max would then involve a broken object. If we were to inject a call Do.stuff(this); between the two field updates, arbitrary user code could observe a broken object; adding such a call is however allowed by visible state semantics.

In this paper, we illustrate the *box pattern*, where we can provide a modified Range class with the desired client interface, while respecting the principles of our strict protocol:

```
class BoxRange{//no invariant in BoxRange
    field min; field max;
    BoxRange(min, max){ this.set(min, max); }
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    method Void set(min, max){
       if (min>=max) { throw new Error(/**/); }
       this.min = min;
       this.max = max;
    }
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  }
  class Range{
    private field box; //box contains a BoxRange
    Range(min, max){ this.box = new BoxRange(min, max); }
    method invariant(){ return this.box.min < this.box.max; }</pre>
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    method set(min, max){ return this.box.set(min, max); }
  }
```

The code of Range.set(min,max) does not violate our protocol. The call to BoxRange.set(min,max) works in a context where the Range object is unreachable, and thus not involved in execution. That is, the Range object is not in the reachable object graph of the receiver or the parameters of BoxRange.set(min,max). Thus Range.set(min,max) can temporarily break the Range's invariant. By using the box field as an extra level of indirection, we restrict the set of objects involved in execution while the state of the object Range is modified.² With appropriate type annotations, the code of Range and BoxRange is accepted as correct by our system: no matter how Range objects are used, a broken Range object will never be involved in execution.

²Due to its simplicity and versatility, we do not claim this pattern to be a contribution of our work, as we expect others

Contributions

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Invariant protocols allow for objects to make necessary changes that might make their invariant temporarily broken. In visible state semantics any object that has an active method call anywhere on the call stacks is potentially invalid; arguably not a very useful guarantee as observed by Gopinathan et al.'s work. [5] Approaches such as pack/unpack [3] represent potentially invalid objects in the type system; this encumbers the type system and the syntax with features whose only purpose is to distinguish objects with broken invariants. The core insight behind our work is that we can use a small number of decorator-like design patterns to avoid exposing those potentially invalid objects in the first place, thus avoiding the need for representing them at the type level.

In this paper, we discuss how to combine runtime checks and capabilities to soundly enforce our strict invariant protocol. Our sound solution only requires that all code is well-typed. Our approach works in the presence of mutation, I/O, non-determinism, and exceptions, all under an open world assumption.

We formalise and prove our approach sound, and have fully implemented our protocol in $L42^3$, and used it to run our various case studies. It is important to note that unlike most prior work, we soundly handle catching of invariant failures and I/O.

The remainder of this paper proceeds as follows:

- Section 2 explains background information necessary to understand our approach
- Section 3 fully explains our novel invariant protocol, and our novel field type for mutable data
- Section 4 demonstrates why the soundness of our protocol depends on the properties of the L42 (and similar) type systems
- Section 5 formalises our runtime invariant checking, and what it means it to soundly enforce our invariant protocol
- Section 6 contains many case studies, showing that our protocol is more succinct than the pack/unpack approach and much more efficient then the visible state semantic
- Section 7 show how our approach does not hamper expressiveness, by showing programming patterns that can be used to perform batch mutation operations with a single invariant check, and how the state of a 'broken' object can be safely passed around
- Section 8 summarises how we have implemented our protocol in L42
- Section 9 presents related work, and Section 10 concludes
- ullet Appendix A formally specifies the properties a type system needs to guarantee, and proves the formalism in Section 5 sound
- Appendix B presents a simple L42-inspired type system and proves that it satisfies the requirements in Section Appendix A

to have used it before. We have however not been able to find it referenced with a specific name in the literature, though technically speaking, it is a simplification of the Decorator pattern, but with a different goal. While in very specific situations the overhead of creating such additional box object may be unacceptable, we designed our work for environments where such fine performance differences are negligible. Also note that many VMs and compilers can optimize away wrapper objects in many circumstances. [4] This is even more applicable in languages with inlined structs, like C++ or C#.

³Our implementation is implemented by checking that a given class conforms to our protocol, and injecting invariant checks in the appropriate places. An anonymised version of L42, supporting the protocol described in this paper, together with the full code of our case studies, is available at http://l42.is/InvariantArtifact.zip.

2. Background on Reference and Object Capabilities

Reasoning about imperative OO programs is a non-trivial task, made particularly difficult by mutation, aliasing, dynamic dispatch, I/O, and exceptions. There are many ways to perform such reasoning; instead of using automated theorem proving, it is becoming more popular to verify aliasing and immutability properties using a type system. For example, three languages: L42 [6, 7, 8, 9], Pony [10, 11], and the language of Gordon et al. [12] use reference capabilities⁴ and object capabilities to statically ensure deterministic parallelism and the absence of data races. While studying those languages, we discovered an elegant way to enforce invariants: we use capabilities to restrict how/when the result of invariant methods changes; this is done by restricting I/O, and how mutation through aliases can affect the state seen by invariants.

That is, our work shows that reference and object capabilities are very usueful also outside of the context of safe parallelism.

Reference Capabilities

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Reference capabilities, as used in this paper, are a type system feature that allows reasoning about aliasing and mutation. A more recent design for them has emerged that radically improves their usability; three different research languages are being independently developed relying on this new design: the language of Gordon et al., Pony, and L42. These projects are quite large: several million lines of code are written in Gordon et al.'s language and are used by a large private Microsoft project; Pony and L42 have large libraries and are active open source projects. In particular the reference capabilities of these languages are used to provide automatic and correct parallelism [12, 10, 11, 7].

Reference capabilities are a well known mechanism [13, 14, 15, 10, 9, 12] that allow statically reasoning about the mutability and aliasing properties of objects. Here we refer to the interpretation of [12], that introduced the concept of recovery/promotion. This concept is the basis for L42, Pony, and Gordon *et al.*'s type systems [12, 7, 6, 10, 11]. With slightly different names and semantics, those languages all support the following reference capabilities for object references:

- Mutable (mut): the referenced object can be mutated and shared/aliased without restriction; as in most imperative languages without reference capabilities.
- Immutable (imm): the referenced object cannot mutate, not even through other aliases. An object with any imm aliases is an *immutable object*. Any other object is a *mutable object*. All objects are born mutable and may later become immutable. Thus, an object can be classified as *mutable* even if it has no fields that can be updated or mutated.
- Readonly (read): the referenced object cannot be mutated by such references, but there may also be mutable aliases to the same object, thus mutation can be observed. Readonly references can refer to both mutable and immutable objects, as read types are supertypes of both their imm and mut variants.
- Encapsulated (capsule): every mutable object in the reachable object graph of a capsule reference (including itself) is only reachable through that reference. Immutable objects in the reachable object graph of a capsule reference are not constrained, and can be freely referred to without passing through that reference.

That is, there are only two kinds of objects: mutable and immutable, but there are more kinds of reference capabilities. In L42 only mut and imm references can be saved on the heap; that is, capsule and read references only exists on the stack.

Reference capabilities are different to field or variable qualifiers like Java's final: reference capabilities apply to references, whereas final applies to fields themselves. Unlike a variable/field of a read type, a final variable/field cannot be reassigned, it always refers to the same object, however the variable/field can

 $^{^4}$ reference capabilities are called $\it Type\ Modifiers$ in former works on L42.

still be used to mutate the referenced object. On the other hand, an object cannot be mutated through a read reference, however a read variable can still be reassigned.⁵

Reference capabilities are applied to all types. This includes types in the receiver and parameters of methods. A mut method is a method where this is typed mut; An imm method is a method where this is typed imm, and so on for all the other reference capabilities.

Consider the following example usage of mut, imm, and read, where we can observe a change in rp caused by a mutation inside mp.

```
mut Point mp = new Point(1, 2);
mp.x = 3; // ok

imm Point ip = new Point(1, 2);
//ip.x = 3; // type error
read Point rp = mp;
//rp.x = 3; // type error
mp.x = 5; // ok, now we can observe rp.x == 5
ip = new Point(3, 5); // ok, ip is not final
```

Reference capabilities influence the access to the whole reachable object graph; not just the referenced object itself, as in the full/deep interpretation of type modifiers [16, 17]:

- A mut field accessed from a read reference produces a read reference; thus a read reference cannot be used to mutate the reachable object graph of the referenced object.
- Any field accessed from an imm reference produces an imm reference; thus all the objects in the reachable object graph of an immutable object are also immutable.

A common misconception of this line of work is that a mut field will always refer to a mutable object. Classes declare reference capabilities for their methods and field types, but what kinds of object is stored in a field also depends on the kind of the object: a mut field of a mutable object will contain a mutable object; but a mut field of an immutable object will contain an immutable object. This is different with respect to work prior to Gordon et al.'s [12], where the declaration fully determines what values can be stored. In those other approaches, any contextual information must be explicitly passed through the type system, for example, with a generic reference capability parameter.

Another common misconception is the belief that capsule fields and capsule local variables always hold capsule references, i.e. the referenced object cannot be reached except via that field/variable. How capsule local variables are handled differs widely in the literature:

In L42, a capsule local variable always holds a capsule reference: this is ensured by allowing them to be read only once (similar to linear and affine types [18]). Pony and Gordon et al. follow a more complicated approach: capsule variables can be accessed multiple times, however in those cases the result will not be a capsule reference but another kind of reference, that can be promoted to capsule, but only under certain conditions. Pony and Gordon also provide destructive reads, where the variable's old value is returned as capsule.

Like capsule variables, how capsule fields are handled differs widely in the literature, however they must always be initialised and updated with capsule references. In order for access to a capsule field to safely produce a capsule reference, Gordon et al. only allows them to be read destructively (i.e. by replacing the field's old value with a new one, such as null). In contrast, Pony does not guarantee that capsule fields contain a capsule reference at all times, as it provides non-destructive reads.

Pony's capsule fields are useful for safe parallelism, but not invariant checking; while Gordon et al.'s cannot be read non-destructively.

The formal model of L42 [19] does not contains capsule fields. The L42 concrete language interprets the syntax for capsule fields as private mut fields with some extra restrictions, including being initialized an upudated only with capsule references. Those encapsulated fields allows to model various forms of ownership

⁵In C, this is similar to the difference between A* const (like final) and const A* (like read), where const A* const is like final read.

and parallelism. ⁶ In Section 3 we present a novel kind of "rep" field. These, like capsule fields, can only be initialised/updated with capsule references, however alias to it can be created in restricted ways. Unlike capsule fields, which are usually designed for safe parallelism, these rep fields are specifically useful for invariant checking; we added support for them to L42, and believe they could be easily added to Pony and Gordon et al.'s language.

Promotion and Recovery

Many different techniques and type systems handle the reference capabilities above [16, 20, 21, 12, 6]. The main progress in the last few years is with the flexibility of such type systems: where the programmer should use imm when representing immutable data and mut nearly everywhere else. The system will be able to transparently promote/recover [12, 10, 6] the reference capability, adapting them to their use context. To see a glimpse of this flexibility, consider the following:

```
mut Circle mc = new Circle(new Point(0, 0), 7);
s capsule Circle cc = new Circle(new Point(0, 0), 7);
imm Circle ic = new Circle(new Point(0, 0), 7);
```

Here mc, cc, and ic are all syntactically initialised with the same exact expression. All new expressions return a mut [10, 19], so mc is well typed. The declarations of cc and ic are also well typed, since any expression (not just new expressions) of a mut type that has no mut or read free variables can be implicitly promoted to capsule or imm. This requires the absence of read and mut global/static variables, as in L42, Pony, and Gordon et al.'s language. L42 also allows such expression to use read free variables as well as mut variables as if they were read. For this to be sound, L42 does not allow read fields. This is the main improvement on the flexibility of reference capabilities in recent literature [7, 6, 12, 10, 11]. From a usability perspective, this improvement means that these reference capabilities are opt-in: a programmer can write many classes simply using mut types and be free to have rampant aliasing. Then, at a later stage, another programmer may still be able to encapsulate instances of those data structures into an imm or capsule reference.

For example, immagine a program where most objects belong to classes designed in a simple minded imperative style: without worrying about ownership, aliasing and encapsulation and with most methods requiring mutation. Thanks to the flexibility discussed above, those objects can still take advantage of our invariant protocol; we just need to apply our Box pattern around those.

Exceptions

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In most languages exceptions may be thrown at any point. Combined with mutation this complicates reasoning about the state of programs after exceptions are caught: if an exception was thrown while mutating an object, what state is that object in? Does its invariant hold? The concept of strong exception safety [22, 8] simplifies reasoning: if a try-catch block caught an exception, the state visible before execution of the try block is unchanged, and the exception object does not expose any object that was being mutated; this prevents exposing objects whose invariant was left broken in the middle of mutations.

L42 enforces strong exception safety for unchecked exceptions using reference capabilities ⁷ in the following way: ⁸

- Only imm objects may be thrown as unchecked exceptions.
- Code inside a try block that captures unchecked exceptions is typed as if all variables declared outside of the block are final and all those of a mut type were read. With such restrictions those try-catches can not rely on side effects to produce a result. In L42 try-catch is an expression, so the try can produce a result without the need of updating local variables. In a language where the try-catch is a statement, the try can still produce a result; for example using the return keywork.

⁶It may seem surprising that those weaker forms of encapsulation are still sufficient to ensure safe parallelism. The detailed way L42 parallelism works is unrelated to the presented work. Please see the tutorial on Forty2.is (specifically, section 5 and 6) for more information on parallelism in L42.

⁷This is needed to support safe parallelism. Pony takes a drastic approach and not support exceptions. We are not aware of how Gordon *et al.* handles exceptions, however to have sound unobservable parallelism it must have some restrictions.

⁸Formal proof that these restriction are sufficient is in the work of Lagorio and Servetto [8].

This strategy does not restrict when exceptions can be *thrown*, but only restricts when unchecked exceptions can be *caught*. Strong exception safety allows us to throw invariant failures as unchecked exceptions: if an object's reachable object graph was mutated into a broken state within a **try**, when the invariant failure is caught, the mutated object will be unreachable/garbage-collectable. This works since strong exception safety guarantees that no object mutated within a **try** is visible when it catches an unchecked exception.⁹

Similarly to Java, L42 distinguishes between checked and unchecked exceptions, and **try-catch**es over checked exceptions impose no limits on object mutation during the **try**. That is, strong exception safety is only enforced for unchecked exceptions.

Object Capabilities

Object capabilities, which L42, Pony, and Gordon et al.'s work have, are a widely used [23, 24, 25, 26] programming technique where access rights to resources are encoded as references to objects. When this style is respected, code unable to reach a reference to such an object cannot use its associated resource. Here, as in Gordon et al.'s work, we enforce the object capabilities pattern with reference capabilities in order to reason about determinism and I/O. To properly enforce this, the object capabilities style needs to be respected while implementing the primitives of the standard library, and when performing foreign function calls that could be non-deterministic, such as operations that read from files or generate random numbers. Such operations would not be provided by static methods, but instead by instance methods of classes whose instantiation is kept under control by carefully designing their implementation.

For example, in Java, System.in is a capability object that provides access to the standard input resource. However, since it is globally accessible it completely prevents reasoning about determinism. In contrast, if Java were to respect the object capability style, the main method could take a System parameter, as in

```
public static void main(System s){... s.in().read() ...}
```

Calling methods on that System instance would be the only way to perform I/O; moreover, the only System instance would be the one created by the runtime system before calling main(s). This design has been explored by Joe-E [27].

Object capabilities are typically not part of the type system nor do they require runtime checks or special support beyond that provided by a memory safe language.

However, L42 has no predefined standard library, but many can be defined by the community. Thus, the only way to perform I/O operations is via foreign function calls. Since enforcing the object capabilities pattern can not be done via a unique standard library, the type system of L42 directly enforces the object capabilities pattern as follows:

- Foreign methods (which have not been whitelisted as deterministic) and methods whose names start with #\$ are capability operations.
- Classes containing capability operations are *capability classes*.
- Constructors of capability classes are also *capability operations*.
- Capability operations can only be called by other capability operations or mut/capsule methods of capability classes.
- In L42 there is no main method, rather it has several main expressions; such expressions can also call capability operations, thus they can instantiate object capabilities and pass them around to the rest of the program.

3. Our Invariant Protocol

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All classes contain a read method Bool invariant() {..}, if no invariant() method is explicitly present, a trivial one returning true is assumed.

 $^{^9}$ Transactions are another way of enforcing strong exception safety, but they require specialised and costly run time support.

Our protocol guarantees that the whole reachable object graph of any object involved in execution (formally, in a redex) is *valid*: if you can use an object, *manually* calling invariant() on it is guaranteed to return **true** in a finite number of steps. ¹⁰

As the invariant() is used to determine whether **this** is broken, it may receive a broken **this**; however this will only occur for calls to invariant() inserted by our approach. User written calls to invariant() are guaranteed to receive a valid **this**.

We restrict invariant() methods so that they represent a predicate over the receiver's imm and rep fields. To ensure that invariant() methods do not expose a potentially broken this to the other objects, we require that all occurrences of this 11 in the invariant()'s body are the receiver of a field access (this.f) of an imm/rep field, or the receivers of a method call (this.m(..)) of a final (non-virtual) method that in turn satisfies these restrictions. No other uses of this are allowed, such as as the right hand side of a variable declaration, or an argument to a method. An equivalent alternative design could instead rely on static invariant(..) methods taking each imm/rep field as an imm/read parameter.

Invariants can only refer to immutable and encapsulated state. Thus while we can easily verify that a doubly linked list of immutable elements is correctly linked up, we can not do the same for a doubly linked lists of mutable elements. We do not make it harder to correctly implement such data structures, but the invariant() method is unable to access the list's nodes, since they may contain mut references to shared/unencapsulated objects. There is a line of work [28] striving to allow invariants over other forms of state. We have not tried to integrate such solutions into our work, as we believe it would make our system more complex and ad hoc, probably requiring numerous specialised kinds of reference capabilities. Thus we have traded some expressive power in order to preserve safety and simplicity.

Purity

L42's enforcement of reference and object capabilities statically guarantees that any method with only read or imm parameters (including the receiver) is pure; we define pure as being deterministic and not mutating existing memory. This holds because (1) the reachable object graph of the parameters (including this) is only accessible as read (or imm), thus it cannot be mutated (2) if a capability object is in the reachable object graph of any of the arguments (including the receiver), then it can only be accessed as read, preventing calling any non-deterministic (capability) methods; (3) no other pre-existing objects are accessible (as L42 does not have global variables). In particular, this means that our invariant() methods are pure, since their only parameter (the receiver) is read.

Rep Fields

Former work on L42 discusses "depending on how we expose the owned data, we can closely model both owners-as-dominators[...] and owners-as-qualifiers[...]" [19], and "lent getter[s], a third variant" [19].

Those informal considerations have then influenced the L42 language design, bringing to the creation of syntactic sugar and programming patterns to represent various kinds of capsule fields aimed to model various forms of ownership. Under the hood, all those forms of capsule fields are just private mut fields with some extra restrictions. Describing in the details those restrictions would be outside of the scope of this paper.

Here we present a novel kind of encapsulated field, that we call a rep field. As for the various kinds of L42 capsule fields, our new kind of field is also just a private mut fields with extra restrictions, enforcing the following key property: the reachable object graph of a rep field o.f can only be mutated under the control of a mut method of o, and during such mutation, o itself cannot be seen. This is similar to owner-as-modifier [29, 30], where we could consider an object to be the 'owner' of all the mutable objects in the reachable object graph of its rep fields, but with the extra restriction that the owner is unobservable during mutation of those objects.

More preciselly, if a reference to an object in the reachable object graph of a **rep** field o.f is involved in execution as **mut**, then: (1) no reference to o is involved in execution, (2) a call to a **mut** method for o is

 $^{^{-10}}$ We will show later how we satisfy this constraint without solving the halting problem or requiring all invariant() methods to be total.

¹¹Some languages allow the this receiver to be implicit. For clarity in this work we require this to be always used explicit.

present in a previous stack frame, and (3) mutable references to the reachable object graph of o.f are not leaked out of such method execution, either as return values, exception values, or stored in the reachable object graph of any parameter or any other field of the method's receiver.

To show how our **rep** fields ensure these properties, we first define some terminology: x.f is a *field access*, x.f=e is a *field update*, 12 a **mut** method with a field access on a **rep** field of **this** is a *rep mutator*. 13 Note that a method performing a field *update* of a **rep** field (instead of a field access) is not called a rep mutator, but it is just a normal method performing a field update. Rep mutators handle the more subtle case where the fields of an object with invariant are not updated, but a mutation deep within their reachable object graph may potentially break the invariant.

The following rules define our novel rep fields:

- A rep field can only be initialised/updated using the result of an expression with capsule type.
- A rep field access will return a:
 - mut reference, when accessed on this within a rep mutator,
 - read reference, when accessed on any other mut receiver,
 - imm if the receiver is imm, read if the receiver is read, or capsule if the receiver is capsule. This last case is safe since a capsule receiver object will then be garbage collectable, so we do not need to preserve its invariant.
- A rep mutator must:

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- use this exactly once: to access the rep field,
- have no mut or read parameters (except the mut receiver),
- not have a **mut** return type,
- not throw any checked exceptions¹⁴.

The above rules ensure that rep mutators control the mutation of the reachable object graph of c.f and only a rep mutator on c.f as c.f as

In contrast, L42's pre-existing **capsule** fields do not have our rep mutator restrictions, in particular, other objects can mutate them, although storing references to them on the heap is highly restricted. These properties are also *weaker* than those of **capsule** *references*: we do not need to prevent arbitrary **read** aliases to the reachable object graph of a **rep** field, and we do allow arbitrary **mut** aliases to exist during the execution of a rep mutator. In particular, our rules allow unrestricted read only access to our **rep** fields.

 $^{^{12}\}mathrm{Thus}$ a field update <code>x.f=e</code> is not a field access followed by an assignment.

¹³We could relax our protocol, so that a mut method that reads a rep field it is not considered a rep mutator if the method only needs to use the field value as read. This relaxation would be merely for convenience; it does not change expressivity as one can write a getter of form read method read C m(){return this.f;} for a rep C f field, and then call this.m() on a mut this.

¹⁴To allow rep mutators to leak checked exceptions, we would need to check the invariant when such exceptions are leaked. However, this would make the runtime semantics of checked exceptions inconsistent with unchecked ones.

¹⁵That is, rep mutators pretend that **this** is linear by requiring it to be used exactly once to read the **rep**. By burying the only current access point to the **rep** field we can read it as **mut** and update it. The restrictions on parameter types and return types ensure that such reference goes out of scope, the only remaining reference allowing mutation is in the **rep** field again. This is similar to the idea of the Focus operation [?] and View-point adaptation [52]

Runtime Monitoring

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The language runtime will automatically perform calls to invariant(), if such a call returns false, an unchecked exception will be thrown. Such calls are performed at the following points:

- After a constructor call, on the newly created object.
- After a field update, on the receiver.
- After a rep mutator method returns, on the receiver of the method ¹⁶.

In Section 5, we show that these checks, together with our aforementioned restrictions, are sufficient to ensure our guarantee that the invariants of all objects involved in execution hold.

70 Traditional Constructors and Subclassing

L42 constructors directly initialise all the fields using the parameters, and L42 does not provide traditional subclassing. This works naturally with our invariant protocol. We can support traditional constructors as in Pony and Gordon et al.'s language, by requiring that constructors only use this as the receiver of a field initialisation. Subclassing can be supported by forcing that a subclass invariant method implicitly starts with a check that super.invariant() returns true. We would also perform invariant checks at the end of new expressions, as happens in [31], and not at the end of super(...) constructor calls.

4. Essential Language Features

Our invariant protocol relies on many different features and requirements. In this section we will show examples of using our system, and how relaxing any of our requirements would break the soundness of our protocol. In our examples and in L42, the reference capability imm is the default, and so it can be omitted. Many verification approaches take advantage of the separation between primitive/value types and objects, since the former are immutable and do not support reference equality. However, our approach works in a pure OO setting without such a distinction. Hence we write all type names in BoldTitleCase to emphasise this. To save space, we omit the bodies of constructors that simply initialise fields with the values of the constructor's parameters, but we show their signature in order to show any annotations.

First we consider Person: it has a single immutable (and non final) field name.

```
class Person {
  read method Bool invariant() { return !name.isEmpty(); }
  private String name;//the default reference capability imm is applied here
  read method String name() { return this.name; }
  mut method Void name(String name) { this.name = name; }
  Person(String name) { this.name = name; }
```

The name field is not final: Persons can change state during their lifetime. The reachable object graphs of all of a Person's fields are immutable, but Persons themselves may be mutable. We enforce Person's invariant by generating checks on the result of calling this.invariant(): immediately after each field update, and at the end of the constructor. Such checks are generated/injected, and not directly written by the programmer.

```
class Person { .. // Same as before
    mut method String name(String name) {
        this.name = name; // check after field update
        if (!this.invariant()) { throw new Error(...); }
    }
    Person(String name) {
        this.name = name; // check at end of constructor
        if (!this.invariant()) { throw new Error(...); }
```

¹⁶The invariant is not checked if the call was terminated via an an unchecked exception, since strong exception safety guarantees the object will be unreachable.

```
}
}
```

We now show how if we were to relax (as in Rust), or even eliminate (as in Java), the support for reference and object capabilities, or strong exception safety, the above checks would not be sufficient to enforce our invariant protocol.

Unrestricted Access to Capability Objects?

Allowing invariant() methods to (indirectly) perform non-deterministic operations by creating new capability objects or mutating existing ones would break our guarantee that (manually) calling invariant() always returns true. Consider this use of person; where myPerson.invariant() may randomly return false:

```
class EvilString extends String {//INVALID EXAMPLE
    @Override read method Bool isEmpty() { return new Random().bool(); }
}//Creates a new object capability out of thin air
...
method mut Person createPersons(String name) {
    // we can not be sure that name is not an EvilString
    mut Person schrodinger = new Person(name); // exception here?
    assert schrodinger.invariant(); // will this fail?
...}
```

Despite the code for Person.invariant() intuitively looking correct and deterministic (!name.isEmpty()), the above call to it is not. Obviously this breaks any reasoning and would make our protocol unsound. In particular, note how in the presence of dynamic class loading, we have no way of knowing what the type of name could be. Since our system allows non-determinism only through object capabilities, and restricts their creation, the above example is prevented.

Moreover, since our system allows non-determinism only through **mut** methods on object capabilities, even if an object has a **rep** field referring to a "file" object, it would be unable to read such file during an invariant, since a **mut** reference would be required, but only a **read** reference would be available.

Allowing Internal Mutation Through Back Doors?

Rust [32] and Javari [13] allow interior mutability: the reachable object graph of an 'immutable' object can be mutated through back doors. Such back doors would allow invariant() methods to store and read information about previous calls. The example class MagicCounter breaks determinism by remotely breaking the invariant of person without any interaction with the person object itself:

```
class MagicCounter {//INVALID EXAMPLE
    Int counter = 0;
    method Int incr(){return unsafe{counter++}; /*using internal mutability*/}}
class NastyS extends String {..
    MagicCounter c = new MagicCounter(0); //can be 'imm' since it is 'unsafe'
    @Override read method Bool isEmpty(){return this.c.incr()!=2;}}
...
    NastyS name = new NastyS(); //type system believe name's ROG is immutable
Person person = new Person(name); // person is valid, counter=1
    name.incr(); // counter == 2, person is now broken
    person.invariant(); // returns false, counter == 3
    person.invariant(); // returns false, counter == 4
```

Such back doors are usually motivated by performance reasons, however in [12] they discuss how a few trusted language primitives can be used to perform caching and other needed optimisations, without the need for back doors.

No Strong Exception Safety?

The ability to catch and recover from invariant failures allows programs to take corrective actions. Since we represent invariant failures by throwing unchecked exceptions, programs can recover from them with a conventional try-catch. Due to the guarantees of strong exception safety, any object that has been mutated during a try block is now unreachable, as happens in alias burying [18]. This property ensures that an

object whose invariant fails will be unreachable after the invariant failure has been captured. If instead we were to not enforce strong exception safety, an invalid object could be made reachable. The following code is ill-typed since we try to mutate bob in a **try-catch** block that captures all unchecked exceptions; thus also including invariant failures:

```
mut Person bob = new Person("Bob");//INVALID EXAMPLE
// Catch and ignore invariant failure:
try { bob.name(""); } catch (Error t) { }// bob mutated
assert bob.invariant(); // fails!
```

The following variant is instead well typed, since bob is now declared inside of the **try** and it is guaranteed to be garbage collectable after the **try** is completed.

```
try { mut Person bob = new Person("Bob"); bob.name(""); }
catch (Error t) { }
```

Note how soundly catching exceptions like stack overflows or out of memory cannot be allowed in invariant() methods, since they are not deterministically thrown. L42 allows catching them only as a capability operation, which thus can't be used inside an invariant.

Relaxing restrictions on rep fields?

Rep fields allow expressing invariants over mutable object graphs. Consider managing the shipment of items, where there is a maximum combined weight:

```
class ShippingList {
    rep Items items;
    read method Bool invariant(){ return this.items.weight()<=300; }
    ShippingList(capsule Items items) {
        this.items = items;
        if (!this.invariant()){ throw Error(...); }//injected check
    }
    mut method Void addItem(Item item) {
        this.items.add(item);
        if (!this.invariant()){ throw Error(...); }//injected check
}</pre>
```

We inject calls to invariant() at the end of the constructor and the addItem(item) method. This is safe since the items field is declared **rep**. Relaxing our system to allow a **mut** reference capability for the items field and the corresponding constructor parameter would make the above checks insufficient: it would be possible for external code with no knowledge of the **ShippingList** to mutate its items. In order to write correct library code in mainstream languages like Java and C++, defensive cloning [33] is needed. For performance reasons, this is hardly done in practice and is a continuous source of bugs and unexpected behaviour.

```
mut Items items = ...; //INVALID EXAMPLE
mut ShippingList 1 = new ShippingList(items); // 1 is valid
items.addItem(new HeavyItem()); // 1 is now invalid!
```

If we were to allow x.items to be seen as **mut**, where x is not **this**, then even if the **ShippingList** has full control of items at initialisation time, such control may be lost later, and code unaware of the **ShippingList** could break it:

```
//INVALID EXAMPLE: 1.items can be exposed as mut
mut ShippingList l = new ShippingList(new Items()); // l is ok
mut Items evilAlias = l.items; // here l loses control
evilAlias.addItem(new HeavyItem()); // now l is invalid!
```

Relaxing our requirements for rep mutators would break our protocol: if rep mutators could have a mut return type the following would be accepted:

```
os //INVALID EXAMPLE: rep mutator expose(c) return type is mut
mut method mut Items expose(C c) {return c.foo(this.items);}
```

Depending on dynamic dispatch, c.foo() may just be the identity function, thus we would get in the same

situation as the former example.

Allowing this to be used more than once would allow the following code, where this may be reachable from f, thus f.hi() may observe an object that does not satisfying its invariant:

```
mut method Void multiThis(C c) {//INVALID EXAMPLE: two 'this'
  read Foo f = c.foo(this);
  this.items.add(new HeavyItem());
  f.hi(); }//'this' could be observed here if it is in ROG(f)
```

In order to ensure that a second reference to **this** is not reachable through arguments to such methods, we only allow **imm** and **capsule** parameters. Accepting a **read** parameter, as in the example below, would cause the same problems as before, where f may contain a reference to **this**:

```
mut method Void addHeavy(read Foo f) {//INVALID EXAMPLE
    this.items.add(new HeavyItem());
f.hi(); }//'this' could be observed here if it is in ROG(f)
...
mut ShippingList 1 = new ShippingList(new Items());
read Foo f = new Foo(1);
l.addHeavy(f); // We pass another reference to 'l' through f
```

5. Formal Language Model

To model our system we need to formalise an imperative OO language with exceptions, object capabilities, and type system support for reference capabilities and strong exception safety. Formal models of the runtime semantics of such languages are simple, but defining and proving the correctness of such a type system is quite complex, and indeed many such papers exist that have already done this [7, 6, 12, 10, 8]. Thus we parametrise our language formalism, and assume we already have an expressive and sound type system enforcing the properties we need, so that we can separate our novel invariant protocol, from the non-novel reference capabilities. We clearly list in Appendix A the requirements we make on such a type system, so that any language satisfying them can soundly support our invariant protocol. In Appendix B we show an example type system, a restricted subset of L42, and prove that it satisfies our requirements. Conceptually our approach can parametrically be applied to any type system supporting these requirements, for example you could extend our type system with additional promotions or generic. To keep our small step reduction semantics as conventional as possible, we base our formalism on Featherweight Java [34, 35, Chapter 19], which is a turing complete [36] minimalistic subset of Java. As such, we model an OO language where receivers are always specified explicitly, and the receivers of field accesses and updates in method bodies are always this; that is, all fields are instance-private. Constructor declarations are not present explicitly, instead we assume they are all of the form $C(T_1 x_1, ..., T_n x_n)$ {this. $f_1 = x_1$;...;this. $f_n = x_n$ }, for appropriate types $T_1, ..., T_n$. Note that we do not model variable updates or traditional subclassing, since this would make the proofs more involved without adding any additional insight.

Notational Conventions

We use the following notational conventions:

- Class, method, parameter, and field names are denoted by C, m, x, and f, respectively.
- We use "vs" and "ls" as metavariables denoting a sequence of form $v_1, ..., v_n$ and $l_1, ..., l_n$, similarly with other metavariables ending in "s".
- We use "_" to stand for any single piece of syntax.
- Memory locations are denoted by l.
- We assume an implicit program/class table; we use the notation C.m to get the method declaration for m within class C, similarly we use C.f to get the declaration of field f, and C.i to get the declaration of the ith field.

- Memory, denoted by $\sigma: l \to C\{ls\}$, is a finite map from locations, l, to annotated tuples, $C\{ls\}$, representing objects; here C is the class name and ls are the field values. We use the notation C_l^{σ} to get the class name of l, $\sigma[l.f = l']$ to update a field of l, $\sigma[l.f]$ to access one, and $\sigma \setminus l$ to delete l (this is only used in our proofs since our small step reduction does not need to delete individual locations). The notation σ, σ' combines the two memories, and requires that $dom(\sigma)$ is disjoint from $dom(\sigma')$.
- We assume a typing judgment of form σ ; $\Gamma \vdash e : T$, this says that the expression e has type T, where the classes of any locations are stored in σ and the types of variables are stored in the environment $\Gamma : x \to T$.

To encode object capabilities and I/O, we assume a special location c of class Cap. This location can be used in the main expression and would refer to an object with methods that behave non-deterministically, such methods would model operations such as file reading/writing. In order to simplify our proof, we assume that:

• Cap has no fields,

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- instances of Cap cannot be created with a new expression,
- Cap's invariant() method is defined to have a body of 'new True()', and
- mut methods on Cap, unlike all other methods, can have the same method name declared multiple times. To enable a typesystem to be sound, we require that methods with the same name have identical signatures. Such methods will model I/O, for example reading a byte from a file could be modelled by having several different mut method Int readByte() implementations, each of which returns a different byte value, a call to such a method will then non-deterministically reduce to one of these values.
- We only model a single Cap capability class for simplicity, as modelling user-definable capability classes as described in 2 is unnecessary for the soundness of our invariant protocol.

We encode booleans as ordinary objects, in particular we assume:

- There is a Bool interface, a "boolean" value is any instance of this interface.
- There is a True class that implements Bool, an instance of this class represents "true".
- The True class has no fields, so it can be created with new True().
- The True class has a trivial invariant (i.e. its body is new True()).
- Any other implementation of Bool, such as a False class, represent "false".

Other than the invariant method of True, we impose no requirements on the methods of the Bool interface or its classes, in particular, they could be used to provide logical operations.¹⁷

For simplicity, we do not formalise actual exception objects, rather we have expressions which are "error"s, these correspond to expressions which are currently 'throwing' an unchecked exception; in this way there is no value associated with an error. Our L42 implementation instead allows arbitrary imm values to be thrown as (unchecked) exceptions, formalising exceptions in such way would not cause any interesting variation of our proofs.

Grammar

The grammar is defined in Figure 1.

¹⁷In particular, **if** statements can be supported using Church encoding: we would have a **Bool.if** method of form **read method** T **if** (T **ifTrue**, T **ifFalse**), for an appropriate type T. The body of **True.if** will then be **ifTrue**, and the body of **False.if** will be **ifFalse**. In this way, x.**if** (t, t) will return t if t is "true" and t if it is "false".

```
:= x \mid \text{new } C(es) \mid \text{this.} f \mid \text{this.} f = e \mid e.m(es)
                                                                                                                                                                                               expression
                  e \operatorname{as} \mu \mid \operatorname{try} \{e\} \operatorname{catch} \{e'\}
              v \mid v.f \mid v.f = e \mid \text{try}^{\sigma}\{e\} \text{ catch } \{e'\} \mid \text{M}(l; e; e')
                                                                                                                                                                             runtime expression
                                                                                                                                                                                                         value
\mathcal{E}_v ::= \Box \mid \text{new } C(vs, \mathcal{E}_v, es) \mid v.f = \mathcal{E}_v \mid \mathcal{E}_v.m(es) \mid v.m(vs, \mathcal{E}_v, es)
                                                                                                                                                                              evaluation context
             \mid \mathcal{E}_v \text{ as } \mu \mid \mathsf{try}^{\sigma} \{ \mathcal{E}_v \} \text{ catch } \{e\} \mid \mathtt{M}(l; \mathcal{E}_v; e) \mid \mathtt{M}(l; v; \mathcal{E}_v) \mid
          := \Box \mid \text{new } C(es, \mathcal{E}, es') \mid \mathcal{E}.f \mid \mathcal{E}.f = e \mid e.f = \mathcal{E} \mid \mathcal{E}.m(es)
                                                                                                                                                                                             full context
               | e.m(es, \mathcal{E}, es') | \mathcal{E} as \mu | \text{try } \{\mathcal{E}\} catch \{e\} | \text{try } \{e\} catch \{\mathcal{E}\}
                  \mathsf{try}^{\sigma}\{\mathcal{E}\}\ \mathsf{catch}\ \{e\}\ |\ \mathsf{try}^{\sigma}\{e\}\ \mathsf{catch}\ \{\mathcal{E}\}\ |\ \mathsf{M}(l;\mathcal{E};e)\ |\ \mathsf{M}(l;e;\mathcal{E})
CD ::= \operatorname{class} C \operatorname{implements} \operatorname{Cs} \{Fs; Ms\} \mid \operatorname{interface} \operatorname{C} \operatorname{implements} \operatorname{Cs} \{As\}
                                                                                                                                                                                  class declaration
          := \kappa C f
                                                                                                                                                                                                           field
          := \mu \operatorname{method} T m(T_1 x_1, ..., T_n x_n)
A
                                                                                                                                                                                  abstract method
         := \mu \operatorname{method} T m (T_1 x_1, ..., T_n x_n) e
M
                                                                                                                                                                                                    method
T
          := \mu C
                                                                                                                                                                                                           type
          ::= mut | imm | read | capsule
\mu
                                                                                                                                                                            reference capability
         ∷= mut | imm | rep
                                                                                                                                                                                                field kind
         ::= \mathcal{E}_v[\overset{}{\mathsf{new}} \ C^{'}(vs,\square,vs')] \mid \mathcal{E}_v[\square.f] \mid \mathcal{E}_v[\square.f=v] \mid \mathcal{E}_v[v.f=\square] \\ \mid \mathcal{E}_v[\square.m(vs)] \mid \mathcal{E}_v[v.m(vs,\square,vs')] \mid \mathcal{E}_v[\square \operatorname{as} \mu] 
                                                                                                                                                                                        redex context
```

Figure 1: Grammar

We use μ for our reference capabilities, and κ for field kinds. We don't model the pre existing L42 capsule fields, but instead model our novel rep fields, which can only be initialised/updated with capsule values. If capsule fields where added, they would not make our invariant protocol more interesting, as long as they do not provide a backdoor to create improper capsule references.

We use v, of form μl , to keep track of the reference capabilities in the runtime, as it allows multiple references to the same location to co-exist with different reference capabilities; however μ 's are not stored in memory. The reduction rules do not change behaviour based on these μ 's, they are merely used by our proofs to keep track of the guarantees enforced by the typesystem.

Our expressions (e), include variables (x), object creations (new C(es)), field accesses (this. f and v.f), field updates (this. f = e and v.f = e), method calls (e.m(es)), and values (v). Note that these are sufficient to model standard constructs, for example a sequencing ";" operator could be simulated by a method which simply returns its last argument. The expressions with this will only occur in method bodies, at runtime this will be substituted for a μl .

The three other expressions are:

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- as expressions (e as μ), these evaluate e and change the reference capability of the result to μ. This is important for our proofs in Appendix A, were we require the typesystem to ensure certain properties for all references with a given μ. The typesystem is then responsible for rejecting any as expression that could violate this. For example, a mut las read could be used to prevent l from being used for further mutation, and a mut las capsule (if accepted by the typesystem) will guarantee that l is properly encapsulated. These as expressions are merely a proof device, they do not effect the runtime behaviour, and as in L42, they could simply be inferred by the typesystem when it would be sound to do so.
- Monitor expressions (M(l; e; e')) represent our runtime injected invariant checks. The location l refers to the object whose invariant is being checked, e represents the behaviour of the expression, and e' is the invariant check, which will initially be read l.invariant(). The body of the monitor, e, is evaluated first, then the invariant check in e' is evaluated. If e' evaluates to an imm True (i.e. an imm reference to an instance of True), then the whole monitor expression will return the value of e, otherwise if it evaluates to a reference to a non-True value (i.e. an imm reference to an instance of a class other than True), the monitor expression is an error, and evaluation will proceed with the nearest enclosing catch block, if any.

• try-catch expressions (try {e} catch {e'}), which as in many other expression based languages 18, evaluate e, and if successful, return its result, otherwise if e is an error, evaluation will reduce to e'. During reduction, try-catch expressions will be annotated as try^σ{e} catch {e'}, where σ is the state of the memory before the body of the try block begins execution. This annotation has no effect on the runtime, but is used by the proofs to model strong exception safety: objects in σ are not mutated by the body of the try. Note that as mentioned before, this strong limitation is only needed for unchecked exceptions, in particular, invariant failures. Our calculus only models unchecked exceptions/errors, however L42 also supports checked exceptions, and try-catches over them impose no limits on object mutation during the try. This is safe since checked exceptions can not leak out of invariant methods or ref mutators: in both cases our protocol requires their throws clause to be empty.

We say that an e is an error if it represents an uncaught invariant failure, i.e. a runtime-injected invariant check that has failed and is not enclosed in a **try** block:

 $error(\sigma, e)$ iff:

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- $e = \mathcal{E}_v[\mathbf{M}(l; v; \mathbf{imm} l')]$
- $C_{l'}^{\sigma} \neq \mathtt{True}$
- \mathcal{E}_v is not of form $\mathcal{E}_v'[\mathsf{try}^{\sigma'}\{\mathcal{E}_v''\}\ \mathsf{catch}\ \{_\}]$

This ensures that the body of a **try** block will only be an *error* if there is no inner **try**—**catch** that should catch it instead.

Locations (l), annotated tries ($try^{\sigma}\{e\}$ catch $\{e'\}$), and monitors M(l; e; e') are runtime expressions: they are not written by the programmer, instead they are introduced internally by our reduction rules.

We provide several expression contexts, \mathcal{E}_v , and \mathcal{E}_v . The standard evaluation context [35, Chapter 19], \mathcal{E}_v , represents the left-to-right evaluation order, an \mathcal{E}_v is like an e, but with a hole (\square) in place of a sub-expression, but all the expression to the left of the hole must already be fully evaluated. This is used to model the standard left to right evaluation order: the hole denotes the location of the next sub-expression that will be evaluated. We use the notation $\mathcal{E}_v[e]$ to fill in the hole, i.e. $\mathcal{E}_v[e]$ returns \mathcal{E}_v but with the single occurrence of \square replaced by e. For example, if $\mathcal{E}_v = \square .m()$ then $\mathcal{E}_v[new C()] = new C().m()$.

The full expression context, \mathcal{E} , is like an \mathcal{E}_v , but nothing needs to have been evaluated yet, i.e. the hole can occur in place of any sub-expression. The context \mathcal{E}_r is also like an \mathcal{E}_v , but instead has a hole in an argument to a redex (i.e. an expression that is about to be reduced). This captures our previously informal notion: a value v is involved in execution if we have an $\mathcal{E}_r[v]$. For example, if $\mathcal{E}_r = \mathcal{E}_v[\text{new } C(v_1, \square, v_3)]$, then $\mathcal{E}_r[v_2] = \mathcal{E}_v[\text{new } C(v_1, v_2, v_3)]$, i.e. we are about to perform an operation (creating a new object) that is involving the value v_2 .

The rest of our grammar is standard and follows Java, except that types (T) contain a reference capability (μ) , and fields (F) contain a field kind (κ) .

Reference Capability Operations

We define the following properties of our reference capabilities and field kinds:

- $\mu \leq \mu'$ indicates that a reference of capability μ can be be used whenever μ' is expected. This defines a partial order:
 - $\begin{array}{ll} \ \mu \leq \mu, \ {\rm for \ any} \ \mu \\ \ {\rm imm} \leq {\rm read} \\ \ {\rm mut} \leq {\rm read} \\ \ {\rm capsule} \leq {\rm mut}, \ {\rm capsule} \leq {\rm imm}, \ {\rm and} \ {\rm capsule} \leq {\rm read} \end{array}$
- $\widetilde{\kappa}$ denotes the reference capability that a field with kind κ requires when initialised/updated:
 - $-\widetilde{\text{rep}} = \text{capsule}$ $-\widetilde{\kappa} = \kappa$, otherwise (in which case κ is also of form μ)

¹⁸This differs from *statement* based languages like Java, were a **try-catch**, does not return a value. The expression-based form can be translated to a call to a method whose body is "try {return e;} catch (Throwable t) {return e';}".

• μ :: κ denotes the reference capability that is returned when accessing a field with kind κ , on a receiver with capability μ :

```
- imm::\kappa = \mu::imm = imm

- read::\kappa = read, if \kappa \neq imm

- mut::rep = mut::mut = mut

- capsule::rep = capsule::mut = capsule
```

The \leq notation and $\tilde{\kappa}$ notations are used later in Appendix A and Appendix B.

Well-Formedness Criteria

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We additionally restrict the grammar with the following well-formedness criteria:

• invariant() methods must follow the requirements of Section 3, except that for simplicity method calls on this are not allowed.¹⁹ This means that for every non-interface class C, C.invariant = readmethod imm Bool invariant() e, where e can only use this as the receiver of an imm or rep field access. Formally, this means that forall \mathcal{E} where $e = \mathcal{E}[\text{this}]$, we have:

```
-\mathcal{E} = \mathcal{E}'[\Box.f], \text{ for some } \mathcal{E}'-C.f = \kappa_- f-\kappa \in \{\text{imm, rep}\}
```

• Rep mutators must also follow the requirements in Section 3, Such methods must not use this, except for the single access to the rep field, and they must not have mut or read parameters, or a mut return type. Formally, this means that for any C, m, and f, if $C.f = \text{rep}_f$ and $C.m = \text{mut method } \mu' - m(\mu_1 - \dots - \mu_n - \dots) \mathcal{E}[\text{this.} f]$:

```
\begin{array}{l} -\text{ this }\notin\mathcal{E}\\ -\ \mu_1\notin\{\text{mut},\text{read}\},\ \dots,\ \mu_n\notin\{\text{mut},\text{read}\}\\ -\ \mu'\neq\text{mut} \end{array}
```

- We require that the method bodies do not contain runtime expressions. Formally, for all C_0 and m with $C_0.m = _method_m(_, _, _) e$, e contains no l, $M(_; _; _)$, or $try^{\sigma'}\{_\}$ catch $\{_\}$ expressions.
- We also assume some general sanity requirements: every C mentioned in the program or in any well typed expression has a single corresponding class/interface definition; the Cs in an implements are all names of interfaces; the C in a new C(es) expression denotes a class; the implements relationship is acyclic; the fields of a class have unique names; methods within a class/interface (other than mut methods in Cap) have unique names; and parameters of a method have unique names and are not named this.
- For simplicity of the type-system and associated proof, we require that every method in the (indirect) super-interfaces of a class be implemented with exactly the same signature, i.e. if we have a class C implements $_{-}$ { $_{-}$; Ms}, and interface C' implements $_{-}$ {As}, where C' is reachable through the implements clauses starting from C, then for all μ method T $m(T_1 x_1, _{-}, T_n x_n) \in As$, there is some e with μ method T $m(T_1 x_1, _{-}, T_n x_n)$ $e \in Ms$.

A typesystem, such as our example one in Appendix B, may impose additional restrictions on method bodies, for example that they are well typed. Our typesystem requirements in Appendix A however only refer to the main expression, and hence only the methods that could actually be called need to be restricted.

Reduction Rules

Our reduction rules are defined in Figure 2. We use the function $fresh(\sigma)$ to return an arbitrary l such that $l \notin dom(\sigma)$. The rules use \mathcal{E}_v to ensure that the sub-expression to be reduced is the left-most unevaluated one:

¹⁹Such method calls could be inlined or rewritten to take the field values themselves as parameters.

```
(\text{NEW}) \ \sigma | \mathcal{E}_v[\text{new } C(\_l_1, \_, \_l_n)] \to \sigma, l_0 \mapsto C\{l_1, \_, l_n\}| \mathcal{E}_v[\texttt{M}(l_0; \texttt{mut } l_0; \texttt{read } l_0.\texttt{invariant}())], \text{ where: } l_0 = fresh(\sigma) \text{ and } C \neq \texttt{True}
(\text{NEW TRUE}) \ \sigma | \mathcal{E}_v[\texttt{new True}()] \to \sigma, l_0 \mapsto \texttt{True}\{\}| \mathcal{E}_v[\texttt{mut } l_0], \text{ where: } l_0 = fresh(\sigma)
(\text{ACCESS}) \ \sigma | \mathcal{E}_v[\mu l, f] \to \sigma | \mathcal{E}_v[\mu' l'], \text{ where: } C_l^\sigma f = \kappa_-f, \mu' = \mu :: \kappa, \text{ and } l' = \sigma[l, f]
(\text{UPDATE}) \ \sigma | \mathcal{E}_v[\_l, f = \_l'] \to \sigma[l, f = l']| \mathcal{E}_v[\texttt{M}(l; \texttt{mut } l; \texttt{read } l.\texttt{invariant}())]
(\text{CALL}) \ \sigma | \mathcal{E}_v[\_l, m(\_l_1, \_, \_l_n]) \to \sigma | \mathcal{E}_v[\texttt{e}[\texttt{this} := \mu_0 l_0, x_1 := \mu_1 l_1, \_, x_n := \mu_n l_n] \text{ as } \mu'], \text{ where: } C_0^\sigma m = \mu_0 \text{ method } \mu' = m(\mu_1 - x_1, \_, \mu_n - x_n) e \text{ if } \mu_0 = \text{mut then } \#(f, \mathcal{E}) \text{ with } C_0^\sigma f = \texttt{rep} - f \text{ and } e = \mathcal{E}[\texttt{this}.f]
(\text{CALL MUTATOR}) \ \sigma | \mathcal{E}_v[\_l, m(\_l, -, \_l_n)] \to \sigma | \mathcal{E}_v[\texttt{M}(l_0; e; \texttt{read } l_0.\texttt{invariant}())], \text{ where: } C_{l_0}^\sigma m = \text{mut method } \mu' = m(\mu_1 - x_1, \_, \mu_n - x_n) \mathcal{E}[\texttt{this}.f]
C_{l_0}^\sigma f = \texttt{rep} - f e = \mathcal{E}[\texttt{this}.f][\texttt{this} := \text{mut } l_0, x_1 := \mu_1 l_1, \_, x_n := \mu_n l_n] \text{ as } \mu'
(\text{AS}) \ \sigma | \mathcal{E}_v[\_l \text{ as } \mu] \to \sigma | \mathcal{E}_v[\mu l]
(\text{TRY ENTER)} \ \sigma | \mathcal{E}_v[\texttt{try}^\sigma \{e\} \text{ catch } \{e'\}] \to \sigma | \mathcal{E}_v[v]
(\text{TRY ERROR)} \ \sigma | \mathcal{E}_v[\texttt{try}^\sigma \{e\} \text{ catch } \{e'\}] \to \sigma | \mathcal{E}_v[e'], \text{ where } error(\sigma, e)
(\text{MONITOR EXIT)} \ \sigma | \mathcal{E}_v[\texttt{M}(l; v; \texttt{imm} l')] \to \sigma | \mathcal{E}_v[v], \text{ where } C_l^\sigma = \texttt{True}
```

Figure 2: Reduction rules

• NEW/NEW TRUE creates a new object. NEW is used when creating a non-True object, it returns a monitor expression that will check the new object's invariant, and if that succeeds, return a mut reference to the object. NEW TRUE is for creating an instance of True, it simply returns a mut reference to the new object, without checking its invariant. The separate NEW TRUE rule is needed as the invariant of True is itself defined to perform new True(), so using the NEW rule would cause an infinite recursion. This is sound since manually calling invariant on True will return a True reference. Note that although we do not define what fresh actually returns, since it is a function these reduction rules are deterministic: l_0 is uniquely defined for any given σ .

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- ACCESS looks up the value of a field in the memory and returns it, annotated with the appropriate reference capability (see above for the definition of $\mu::\kappa$).
- UPDATE updates the value of a field, returning a monitor that re-checks the invariant of the receiver, and if successful, will return the receiver of the update as mut. Note that this does not check that the receiver of the field update has an appropriate reference capability, it is the responsibility of the type-system to ensure that this rule is only applied to a mut or capsule receiver. For soundness, we return a mut reference even when the receiver is capsule. Promotion can then be used to convert the result to a capsule, provided the new field value is appropriately encapsulated.
- CALL/CALL MUTATOR looks for a corresponding method definition in the receiver's class, and reduces to its body with parameters appropriately substituted. The parameters are substituted with the reference capabilities of the method's signature, not the capabilities at the call-site, this is used by the proofs to show that further reductions will respect the capabilities in the method signature. We wrap the body of the method call in a as expression to ensure that the returned μ is actually as the method signature specified; for example, a method declared as returning a read might actually return a mut, but the as expressions will soundly change it to a read, thus preventing it from being used for mutation. As with as expressions in general, the type system is required to ensure that this will not break our reference capability guarantees in Appendix A. The CALL MUTATOR rule is like CALL, but is used when the method is a rep mutator (a mut method that accesses a rep field): it additionally wraps the method body in a monitor expression that will re-check the invariant of the receiver once the body of the method has finished reducing. Note that as Cap has no rep fields and can have multiple definitions of the same method, the CALL rule allows for non-determinism, but only if the receiver is of class Cap and the method is a mut method.
- As simply changes the reference capability to the one indicated. Note that our requirements on the type-system, given in Appendix A, ensure that inappropriate promotions (e.g. imm to mut) will be ill-typed.
- TRY ENTER will annotate a try-catch with the current memory state, before any reduction occurs within the try part. In Appendix A, we require the type system to ensure strong exception safety: that the objects in the saved σ are never modified. Note that the grammar for \mathcal{E}_v prevents the body of an unannotated try block from being reduced, thus ensuring that this rule is applied first.
- TRY OK simply returns the body of a **try** block once it has successfully reduced to a value. TRY ERROR on the other hand reduces to the body of the **catch** block if its **try** block is an *error* (an invariant failure that is *not* enclosed by an inner **try** block). Note that the grammar for \mathcal{E}_v prevents the body of a **catch** block from being reduced, instead TRY ERROR must be applied first; this ensures that the body of a **catch** is only reduced if the **try** part has reduced to an *error*.
- MONITOR EXIT reduces a successful invariant check to the body of the monitor. If the invariant check on the other hand has failed, i.e. has returned a non-True reference, it will be an *error*, and TRY ERROR will proceed to the nearest enclosing catch block.

Note that as with most OO languages, an expression e can always be reduced, unless: e is already a value, e contains an uncaught invariant failure, or e attempts to perform an ill-defined operation (e.g. calling

a method that doesn't exist). The latter case can be prevented by any standard sound OO typesystem. However, invalid use of reference capabilities (e.g. having both an imm and mut reference to the same location) does not cause reduction to get stuck, instead, in Appendix A we explicitly require that the typesystem prevents such things from happening, which our example type system in ?? proves to be the case.

Note that the monitor expressions are only a proof device, they need not be implemented directly as presented. For example, in L42 they are implemented by statically injecting calls to invariant() at the end of setters (for imm and rep fields), factory methods, and rep mutators; this works as L42 follows the uniform access principle, so it does not have primitive expression forms for field updates and constructors, rather they are uniformly represented as method calls.

Statement of Soundness

We define a deterministic reduction arrow to mean that exactly one reduction is possible:

$$\sigma|e \Rightarrow \sigma'|e'$$
 iff $\sigma|e \rightarrow \sigma'|e'$, and $\forall \sigma'', e'', \sigma|e \rightarrow \sigma''|e''$, implies $\sigma''|e'' = \sigma'|e'$

We say that an object is valid when calling its invariant() method would deterministically produce an imm True in a finite number of steps, i.e. assuming the typesystem is sound, this means it does not evaluate to a non-True reference, fail to terminate, or produce an error. We also require that evaluating invariant() preserves existing memory, however new objects can be freely created and mutated:

 $valid(\sigma, l)$ iff $\sigma | \mathbf{read} \ l$.invariant() $\Rightarrow^+ \sigma, \sigma' | \mathbf{imm} \ l$ where $C_l^{\sigma, \sigma'} = \mathbf{True}$. To allow the invariant() method to be called on an invalid object, and access fields on such an objects, we define the set of trusted execution steps as the call to invariant() itself, and any field accesses inside its evaluation:

 $trusted(\mathcal{E}_r, l)$ iff, either:

- $\mathcal{E}_r = \mathcal{E}_v[M(l; _; \Box.invariant())],$ or
- $\mathcal{E}_r = \mathcal{E}_v[\mathbf{M}(l; \underline{\cdot}; \mathcal{E}_v'[\Box .f])].$

The idea being that the \mathcal{E}_r is like an \mathcal{E}_v but it has a hole where a reference can be, thus $trusted(\mathcal{E}_r, l)$ holds when the very next reduction we are about to perform is μl -invariant() or $\mu l \cdot f$. As we discuss in our proof of Soundness, any such $\mu l.f$ expression came from the body of the invariant() method itself, since lcan not occur in the ROG of any of its fields mentioned in the invariant() method.²⁰

We define a validState as one that was obtained by any number of reductions from a well typed initial main expression and memory:

 $validState(\sigma, e)$ iff $c \mapsto \texttt{Cap}\{\}|e_0 \to^* \sigma|e$, for some e_0 such that:

- $c \mapsto \operatorname{Cap}\{\}; \emptyset \vdash e_0 : T, \text{ for some } T$
- e_0 contains no M(_; _; _), try $^{\sigma'}$ {_} catch {_}}, or _as μ expressions
- $\bullet \ \forall \mu \, l \in e_0, \, \mu \, l = \mathtt{mut} \, c$

By restricting which initial expressions are well-typed, the type-system (such as the one presented in Appendix B) can ensure the required properties of our reference-capabilities (see Appendix A); any standard OO type system can also be used to reject expressions that might try to perform an ill-defined reduction (like reading a field that does not exist). The initial expression cannot contain any runtime expressions, except for mut references to the single pre-existing Cap object. Note that as Cap has no fields and this is not of form l, field accesses/updates in the initial main expression can never be reduced. To make the type system and proofs presented in Appendix B simpler, we require that c can only be initially referenced as mut and that there are no as expressions in e_0 . This restriction does not effect expressivity, as you can pass c to a method whose parameters have the desired reference capability, and whose body contains the desired as expressions.

Finally, we define what it means to soundly enforce our invariant protocol:

Theorem 1 (Soundness).

If $validState(\sigma, \mathcal{E}_r[-l])$, then either $valid(\sigma, l)$ or $trusted(\mathcal{E}_r, l)$.

²⁰Invariants only see imm and rep fields (as read), neither of which can alias the current object.

Except for the injected invariant checks (and fields they directly access), any redex in the execution of a well typed program takes as input only valid objects. In particular, no method call (other than *injected* invariant checks themselves) can see an object which is being checked for validity.

This is a very strong statement because $valid(\sigma, l)$ requires the invariant of l to deterministically terminate. Our setting does ensure termination of the invariant of any l that is now within a redex (as opposed to an l that is on the heap, or is being monitored). This works because non terminating **invariant()** methods would cause the monitor expression to never terminate. Thus, an l with a non terminating **invariant()** is never involved in an untrusted redex. This works as invariants are deterministic computations that depend only on the state reachable from l. In particular, if l is in a redex, a monitor expression must have terminated after the object instantiation and after any updates to the state of l.

6. Case Studies

To perform compelling case studies, we used our system on many examples, including one designed to be a worst case scenario for our approach. We also replicate many examples originally proposed by other papers, so that not all the code examples come from us.

6.1. An interactive GUI

We start by presenting our GUI example; a program that interacts with the real world using I/O. It demonstrates how to verify invariants over cyclic mutable object graphs. Our example is particularly relevant since, as with most GUI frameworks, it uses the *composite* programming pattern; arguably one of the most fundamental patterns in OO.

Our case study involves a GUI with containers (SafeMovables) and Buttons. The SafeMovable class has an invariant to ensure that its children are graphically contained within it and do not overlap. The Buttons move their SafeMovable when pressed. We have a Widget interface, which provides methods to get Widgets' size and position as well as children (a list of Widgets). Both SafeMovables and Buttons implement Widget. Crucially, since the children of SafeMovable are stored in a list of Widgets it can contain other SafeMovables, and all queries to their size and position are dynamically dispatched. Such queries are also used in SafeMovable's invariant. Here we show a simplified version²¹, where SafeMovable has just one Button and certain sizes and positions are fixed. Note that Widgets is a class representing a mutable list of mut Widgets.

```
class SafeMovable implements Widget {
     rep Box box; Int width = 300; Int height = 300;
835
     @Override read method Int left() { return this.box.l; }
     @Override read method Int top() { return this.box.t; }
     @Override read method Int width() { return this.width; }
     @Override read method Int height() { return this.height; }
     @Override read method read Widgets children() { return this.box.c; }
     @Override mut method Void dispatch(Event e) {
       for (Widget w:this.box.c) { w.dispatch(e); }
     read method Bool invariant() {../* presented later */..}
     SafeMovable(capsule Widgets c) { this.box = makeBox(c); }
845
     static method capsule Box makeBox(capsule Widgets c) {
       mut Box b = new Box(5, 5, c);
       b.c.add(new Button(0, 0, 10, 10, new MoveAction(b));
       return b; // mut b is soundly promoted to capsule
     }
   }
   class Box { Int 1; Int t; mut Widgets c; Box(Int 1, Int t, mut Widgets c) {..} }
   class MoveAction implements Action {
```

 $^{^{21}}$ The full version, written in L42, which uses a different syntax, is available in our artifact at http://l42.is/InvariantArtifact.zip

```
mut Box outer;
MoveAction(mut Box outer) { this.outer = outer; }
mut method Void process(Event e) { this.outer.l += 1; }
}
... //main expression
//#$ is a capability operation making a Gui object
Gui.#$().display(new SafeMovable(...));
```

As you can see, Boxes encapsulate the state of the SafeMovables that can change over time: left, top, and children. Also note how the reachable object graph of Box is cyclic: since the MoveActions inside Buttons need a reference to the containing Box in order to move it. Even though the children of SafeMovables are fully encapsulated, we can still easily dispatch events to them using dispatch(e). Once a Button receives an Event with a matching ID, it will call its Action's process(e) method.

Our example shows how to encode interactive GUI programs, where widgets may circularly reference other widgets. In order to perform this case study we had to first implement a simple GUI Library in L42. This library uses object capabilities to draw the widgets on screen, as well as fetch and dispatch events. Importantly, neither our application, nor the underlying GUI library requires back doors, into either reference or object capabilities.

The Invariant

SafeMovable is the only class in our GUI that has an invariant, our system automatically checks it in two places: the end of its constructor and the end of its dispatch(e) method (which is a rep mutator). There are no other checks inserted since we never do a direct field update on a SafeMovable. The code for the invariant is just a couple of simple nested loops:²²

```
read method Bool invariant() {
  for(Widget w1 : this.box.c) {
    if(!this.inside(w1)) { return false; }
    for(Widget w2 : this.box.c) {
       if(w1!=w2 && SafeMovable.overlap(w1, w2)){ return false; }
    }
  }
  return true;
}
```

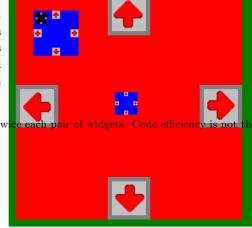
Here SafeMovable.overlap is a static method that simply checks that the bounds of the widgets don't overlap. The call to this.inside(w1) similarly checks that the widget is not outside the bounds of this; this instance method call is allowed as inside(w) only uses this to access its imm and rep fields.

Our Experiment

As shown in the figure below, counting both SafeMovables and Buttons, our main method creates 21 widgets: a top level (green) SafeMovable without buttons, containing 4 (red, blue, and black) SafeMovables with 4 (gray) buttons each. When a button is pressed it moves the containing SafeMovable a small amount in the corresponding direction. This set up is not overly complicated, the maximum nesting level of Widgets is 5. Our main method automatically presses each of the 16 buttons once. In L42, using our invariant protocol, this resulted in 77 calls to SafeMovable's invariant.

5 Comparison With Visible State Semantics

As an experiment, we set our implementation to generate invariant checks following the visible state semantics approaches of D and Eiffel [37, 38], where the invariant of the receiver is instead checked at the start and end of *every* public (in D) and qualified²³ (in Eiffel) method call. In our SafeMovable class,



 $^{^{22}}$ We could make the code sigtly more efficient by avoiding comparing tw priority here.

²³That is, the receiver is not **this**.

all methods are public, and all calls (outside the invariant) are qualified, thus this difference is irrelevant. Neither protocol performs invariant checks on field accesses or updates, however due to the 'uniform access principle' [38], Eiffel allows fields to directly implement methods, allowing the width and height fields to directly implement Widget's width() and height() methods. On the other hand in D, one would have to write getter methods, which would perform invariant checks. When we ran our test case following the D approach, the invariant() method was

called 52,734,053 times, whereas the Eiffel approach 'only' called it 14,816,207 times;²⁴in comparison our invariant protocol only performed 77 calls. The number of checks is exponential in the depth of the GUI: the invariant of a SafeMovable will call the width(), height(), left(), and top() methods of its children, which may themselves be SafeMovables, and hence such calls may invoke further invariant checks. Note that width() and height() are simply getters for fields, whereas the other two are non-trivial methods. Concluding, we have shown that when an invariant check queries other objects with invariants the visible state semantics may cause an exponential explosion in the number of checks.

Spec# Comparison

We also encoded our example in Spec#²⁵; that relies on pack/unpack; also called inhale/exhale or the Boogie methodology. In pack/unpack, an object's invariant is checked only by the explicit pack operations. In order for this to be sound, some form of aliasing and/or mutation control is necessary. Spec# uses a theorem prover, together with source code annotations. Spec# can be used for full static verification, but it conveniently allows invariant checks to be performed at runtime, whilst statically verifying aliasing, purity and other similar standard properties. This allows us to closely compare our approach with Spec#.

As the back-end of the L42 GUI library is written in Java, we did not port it to Spec#, rather we just simulated it, and don't actually display a GUI in Spec#. We ran our code through the Spec# verifier (powered by Boogie [39]), which only gave us 2 warnings²⁶, because the invariant of SafeMovable was not known to hold at the end of its constructor and dispatch(e) method. Thus, like our system, Spec# checks the invariant at those two points at runtime. Thus the code is equivalently verified in both Spec# and L42; in particular it performed exactly the same number (77) of runtime invariant checks.

While the same numbers of checks are performed, we do not have the same guarantee provided by our approach: Spec#/Boogie does not soundly handle the non-deterministic impact of I/O, thus it does not properly prevent us from writing unsound invariants that may be non-deterministic. We also encoded our GUI in Microsoft Code Contracts [40], whose unsound heuristic also calls the invariant 77 times. However Code Contract does not enforce the encapsulation of children(), thus this approach is even less sound than Spec#.

Note how both our L42 and Spec# code required us to use the box pattern for our SafeMovable, due to the cyclic object graph caused by the Actions of Buttons needing to change their enclosing SafeMovable's position. We found it quite difficult to encode the GUI in Spec#, due to its unintuitive and rigid ownership discipline. In particular we needed to use many more annotations, which were larger and had greater variety. The following table shows the annotation burden, for the *program* that defines and displays the SafeMovables and our GUI; as well as the *library* which defines Buttons, Widget, and event handling. We only count constructs Spec# adds over C# as annotations, we also do not count annotations related to array bounds or null checks:

 $^{^{24}}$ This difference is caused by Eiffel treating getters specially, and skipping invariant checks when calling a getter. Thus, even ignoring getter methods, the visible state semantic would still run 14 millions of invariant checks.

 $^{^{25}}$ We compiled Spec# using the latest available source (from 19/9/2014). The verifier available online at rise4fun.com/SpecSharp behaves differently.

²⁶We used assume statements, equivalent to Java's assert, to dynamically check array bounds. This aligns the code with L42, which also performs such checks at runtime.

	$\operatorname{Spec} \#$	$\operatorname{Spec} \#$	L42	L42
	program	library	program	library
Total number of annotations	40	19	19	18
Tokens (except .,;(){}[] and whitespace)	106	34	19	18
Characters (with minimal whitespace)	619	207	74	60

To encode the GUI example in L42, the only annotations we needed were the 3 reference capabilities: mut, read, and capsule (rep fields in the actual L42 language use the capsule keywords to minimise language complexity); Our Spec# code requires purity, immutability, ownership, method pre/post-conditions and method modification annotations. In addition, it requires the use of 4 different ownership functions including explicit ownership assignments. In total we used 18 different kinds of annotations in Spec#. The table presents token and character counts to compare against Spec#'s annotations, which can be quite long and involved, whereas ours are just single keywords. Consider for example the Spec# pre-condition on SafeMovable's constructor:

```
requires Owner.Same(Owner.ElementProxy(children), children);
```

The Spec# code also required us to deviate from the code style shown in our simplified version: we could not write a usable children() method in Widget that returns a list of children, instead we had to write children_count() and children(int i) methods; we also needed to create a trivial class with a [Pure] constructor (since Object's one is not marked as such). In contrast, the only indirection we had to do in L42 was creating Boxes by using an additional variable in a nested scope. This is needed to delineate scopes for promotions. Based on these results, we believe our system is significantly simpler and easier to use in comparision with Spec#, that is more verbose but supports a wider range of verification applications.

6.2. A Comparison of a Simple Example in Spec#

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Suppose we have a Cage class which contains a Hamster; the Cage will move its Hamster along a path. We would like to ensure that the Hamster does not deviate from the path. We can express this as the invariant of Cage: the position of the Cage's Hamster must be within the path (stored as a field of Cage). This example is interesting since it relies on Lists and Points that are not designed with Hamster/Cages in mind.

```
class Point { Double x; Double y; Point(Double x, Double y) {..}
     @Override read method Bool equals(read Object that) {
       if (!(that instanceof Point)) { return false; }
       Point p = (Point)that;
       return this.x == p.x && this.y == p.y;
970
   }
   class Hamster { Point pos; Hamster(Point pos) {..} }//pos is imm by default
   class Cage {
     rep Hamster h;
     List < Point > path; //path is imm by default
     Cage(capsule Hamster h, List<Point> path) {..}
     read method Bool invariant() { return this.path.contains(this.h.pos); }
     mut method Void move() {
       Int index = 1 + this.path.indexOf(this.pos()));
980
       this.moveTo(this.path.get(index % this.path.size())); }
     read method Point pos() { return this.h.pos; }
     mut method Void moveTo(Point p) { this.h.pos = p; }
```

The invariant() method on Cage simply verifies that the pos of this.h is within the this.path list. This is accepted by our invariant protocol since path is an imm field (hence deeply immutable) and h is a rep field (hence fully encapsulated). The path.contains call is accepted by our type system as it only needs read access: it merely needs to be able to access each element of the list and call Point's equal method, which takes a read receiver and parameter. The move method actually moves the hamster along the path, but to ensure that our restrictions on rep fields are respected we forwarded some of the behaviour to separate

methods: pos() which returns the position of h and moveTo(p) which updates the position of h. The pos method is needed since move() is a **mut** method, and so any direct **this**.h access would cause it to be a rep mutator, which would make the program erroneous as move() uses **this** multiple times. Similarly, we need the moveTo(p) method to modify the reachable object graph of the h field, this must be done within a rep mutator that uses **this** only once.

As our path and h fields are never themselves updated, the only point where the reachable object graph of our Cage can mutate is in the moveTo(p) rep mutator, thus our invariant protocol will insert runtime invariant checks only here and at the end of the constructor.

Note: since only Cage has an invariant, only the code of Cage needs to be handled carefully; allowing the code for Point and Hamster to be unremarkable. Thus our verification approach is more self contained and modular. This contrasts with Spec#: all code involved in verification needs to be designed with verification in mind [41].

Comparison with Spec#

We now show our hamster example in the system most similar to ours, Spec#:

```
// Note: assume everything is 'public'
   class Point { double x; double y; Point(double x, double y) {..}
      [Pure] bool Equal(double x, double y) { return x == this.x && y == this.y; } }
   class Hamster{[Peer] Point pos; Hamster([Captured] Point pos){...} }
   class Cage {
      [Rep] Hamster h; [Rep, ElementsRep] List<Point> path;
1010
     Cage([Captured] Hamster h, [Captured] List<Point> path)
       requires Owner.Same(Owner.ElementProxy(path), path); {
         this.h = h; this.path = path; base(); }
     invariant exists {int i in (0 : this.path.Count);
       this.path[i].Equal(this.h.pos.x, this.h.pos.y) };
1015
      void Move() {
       while(i<path.Count && !path[i].Equal(h.pos.x,h.pos.y)){ i++; }</pre>
        expose(this) { this.h.pos = this.path[i%this.path.Count]; }
     }
```

In both this and our original version, we designed Point and Hamster in a general way, and not solely to be used by classes with an invariant: thus Point is not an immutable class.

The Spec# approach uses ownership: the Rep attribute on the h and path fields means its value is owned by the enclosing Cage, similarly the ElementsRep attribute on the path field means its elements are owned by the Cage. Conversely, in the Hamster class, the Peer annotation on the pos field means its value is owned by the owner of the enclosing Hamster, thus if a Cage owns a Hamster, it also owns the Hamster's pos. The Captured annotations on the constructor parameters of Cage and Hamster means that the passed in values must be un-owned and the body of the constructor may modify their owners (the owner is automatically updated when the parameter is assigned to a Rep or Peer field).

Though we don't want either pos or path to ever mutate, Spec# currently has no way of enforcing that an *instance* of a non-immutable class is itself immutable.²⁷ In Spec#, an invariant() can only access fields on owned or immutable objects, thus necessitating our use of the Peer and Rep annotations on the pos and path fields.

Note that this prevents multiple Cages from sharing the same point instance in their path. Had we made Point an immutable class, we would get no such restriction. A similar problem applies to our pos field: the pos of Hamsters in different Cages cannot be the same Point instance. Note how if we consider being in the

²⁷There is a paper [42] that describes a simple solution to this problem: assign ownership of the object to a special predefined 'freezer' object, which never gives up mutation permission. However, this does not appear to have been implemented. This would provide similar flexibility to the reference capabilities system we use, which allows an initially mutable object to be promoted to immutable.

reachable object graph of an object's rep fields as being 'owned' by the object, our rep fields behave like Rep fields; similarly, mut fields that are in the reachable object graph of a rep field behave like Peer fields.

The expose(this) block is needed, since in Spec# in order to modify a field of an object (like this.h.pos), we must first "expose" its owner (the Cage). During an expose block, Spec# will not assume the invariant of the exposed object, but will ensure it is re-established at the end of the block. This is similar to our concept of rep mutators (like our moveTo method above), however it is supported by adding an extra syntactic construct (the expose block), which we avoid.

Finally, note the custom Equal(x,y) method on Point: this is needed since we can't overload the usual Object.Equals(other) method because it is marked as Reads(ReadsAttribute.Reads.Nothing), which requires the method not read any fields, even those of its receiver. We resorted to making our own Equal(x,y) method. Since it is called in Cage's invariant, Spec# requires it to be annotated as Pure, this requires that it can only read fields of objects owned by the receiver of the method, so a method [Pure] bool Equal(Point that) can read the fields of this, but not the fields of that. Of course this would make the method unusable in Cage since the Points we are comparing equality against do not own each other. As such, the simplest solution is to just pass the fields of the other point to the method. Sadly this mean we can no longer use List's Contains(elem) and IndexOf(elem) methods, rather we have to expand out their code manually.

Even with all the above annotations, we needed special care in creating Cages:

```
List<Point> pl = new List<Point>{new Point(0,0), new Point(0,1)};
Owner.AssignSame(pl, Owner.ElementProxy(pl));
Cage c = new Cage(new Hamster(new Point(0, 0)), pl);
```

In Spec# objects start their life as un-owned, so each **new** instruction above returns an unowned object. However when the **Points** are placed inside the pl list, Spec# loses track of this. Thus the **AssignSame** call is needed to mark the elements of pl as still being unowned (since pl itself is unowned). Contrast this with our system which requires no such operation; we can simply write:

```
 \textbf{Cage} \  \  \textbf{c=new} \  \  \textbf{Cage} \  \, (\textbf{new} \  \, \textbf{Point} \  \, (\textbf{0} \, , \textbf{0})) \, , \\ \textbf{List.of} \  \, (\textbf{new} \  \, \textbf{Point} \  \, (\textbf{0} \, , \textbf{0}) \, , \\ \textbf{new} \  \, \textbf{Point} \  \, (\textbf{0} \, , \textbf{1}))) \, ; \\ \textbf{constant} \  \, (\textbf{new} \  \, \textbf{Point} \  \, (\textbf{0} \, , \textbf{0}) \, , \\ \textbf{new} \  \, \textbf{Point} \  \, (\textbf{0} \, , \textbf{0}) \, , \\ \textbf{new} \  \, \textbf{Point} \  \, (\textbf{0} \, , \textbf{0}) \, , \\ \textbf{new} \  \, \textbf{Point} \  \, (\textbf{0} \, , \textbf{0}) \, , \\ \textbf{new} \  \, \textbf{Point} \  \, (\textbf{0} \, , \textbf{0}) \, , \\ \textbf{new} \  \, \textbf{Point} \  \, (\textbf{0} \, , \textbf{0}) \, , \\ \textbf{new} \  \, \textbf{Point} \  \, (\textbf{0} \, , \textbf{0}) \, , \\ \textbf{new} \  \, \textbf{Point} \  \, (\textbf{0} \, , \textbf{0}) \, , \\ \textbf{new} \  \, \textbf{Point} \  \, (\textbf{0} \, , \textbf{0}) \, , \\ \textbf{new} \  \, \textbf{Point} \  \, (\textbf{0} \, , \textbf{0}) \, , \\ \textbf{new} \  \, \textbf{Point} \  \, (\textbf{0} \, , \textbf{0}) \, , \\ \textbf{new} \  \, \textbf{Point} \  \, (\textbf{0} \, , \textbf{0}) \, , \\ \textbf{new} \  \, \textbf{Point} \  \, (\textbf{0} \, , \textbf{0}) \, , \\ \textbf{new} \  \, \textbf{Point} \  \, (\textbf{0} \, , \textbf{0}) \, , \\ \textbf{new} \  \, \textbf{Point} \  \, (\textbf{0} \, , \textbf{0}) \, , \\ \textbf{new} \  \, \textbf{Point} \  \, (\textbf{0} \, , \textbf{0}) \, , \\ \textbf{new} \  \, \textbf{Point} \  \, (\textbf{0} \, , \textbf{0}) \, , \\ \textbf{new} \  \, \textbf{Point} \  \, (\textbf{0} \, , \textbf{0}) \, , \\ \textbf{new} \  \, \textbf{Point} \  \, (\textbf{0} \, , \textbf{0}) \, , \\ \textbf{new} \  \, \textbf{Point} \  \, (\textbf{0} \, , \textbf{0}) \, , \\ \textbf{new} \  \, \textbf{new} \  \, \textbf{new} \  \, \textbf{new} \, . \\ \textbf{new} \  \, \textbf{new} \  \, \textbf{new} \, \textbf{new} \, . \\ \textbf{new} \  \, \textbf{new} \  \, \textbf{new} \, \textbf{new} \, \textbf{new} \, . \\ \textbf{new} \  \, \textbf{new} \, \textbf{n
```

In Spec#, we had to add 10 different annotations, of 8 different kinds, some of which are quite involved. In comparison, our approach requires only 8 simple keywords of 3 different kinds. However, we needed to write separate pos() and moveTo(p) methods.

6.3. A Worst Case for the Number of Invariant Checks

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The following test case was designed to produce a worst case in the number of invariant checks. We have a Family that (indirectly) contains a list of parents and children. The parents and children are of type Person. Both Family and Person have an invariant, the invariant of Family depends on its contained Persons.

```
class Person {
     final String name;
     Int daysLived;
     final Int birthday;
     Person(String name, Int daysLived, Int birthday) { .. }
     mut method Void processDay(Int dayOfYear) {
        this.daysLived += 1;
        if(this.birthday == dayOfYear) {Console.print("Happy birthday "+this.name + "!");}
     read method Bool invariant() {
        return !this.name.equals("") && this.daysLived >= 0
1080
            && this.birthday >= 0 && this.birthday < 365;
    class Family {
     static class Box {
        mut List < Person > parents;
        mut List < Person > children;
        Box(mut List<Person> parents, mut List<Person> children){..}
```

```
mut method Void processDay(Int dayOfYear) {
          for(Person c : this.children) { c.processDay(dayOfYear); }
1090
          for(Person p : this.parents) { p.processDay(dayOfYear); }
     rep Box box;
     Family(capsule List < Person > ps, capsule List < Person > cs) { this.box = new Box(ps,cs); }
1095
     mut method Void processDay(Int dayOfYear) { this.box.processDay(dayOfYear); }
     mut method Void addChild(capsule Person child) { this.box.children.add(child); }
     read method Bool invariant() {
        for (Person p : this.box.parents) {
          for (Person c : this.box.children) {
1100
            if (p.daysLived <= c.daysLived) { return false; }</pre>
        }
        return true;
     }
   }
```

Note how we created a Box class to hold the parents and children. Thanks to this pattern, the invariant only needs to hold at the end of Family.processDay(dayOfYear), after all the parents and children have been updated. Thus processDay(dayOfYear) is atomic: it updates all its contained Persons together. Had we instead made the parents and children rep fields of Family, the invariant would be required to also hold between modifying the two lists. This could cause semantic problems if, for example, a child was updated before their parent.

We have a simple test case that calls processDay(dayOfYear) on a Family $1,095 \ (3 \times 365)$ times.

The idea is that everything we do with the Family is a mutation; the fam.processDay calls also mutate the contained Persons.

This is a worst case scenario for our approach compared to visible state semantics since it reduces our advantages: our approach avoids invariant checks when objects are not mutated but in this example most operations are mutations; similarly, our approach prevents the exponential explosion of nested invariant checks when deep object graphs are involved, but in this example the object graph of fam is very shallow.

We ran this test case using several different languages: L42 (using our protocol) performs 4,000 checks, D and Eiffel perform 7,995, and finally, Spec# performs only 1,104.

Our protocol performs a single invariant check at the end of each constructor, processDay(dayOfYear) and addChild(child) call (for both Person and Family).

The visible state semantics of both D and Eiffel perform additional invariant checks at the beginning of each call to processDay(dayOfYear) and addChild(child).

The results for Spec# are very interesting, since it performs fewer checks than L42. This is the case since processDay(dayOfYear) in Person just does a simple field update, which in Spec# do not invoke runtime invariant checks. Instead, Spec# tries to statically verify that the update cannot break the invariant; if it

is unable to verify this, it requires that the update be wrapped in an **expose** block, which will perform a runtime invariant check.

Spec# relies on the absence of arithmetic overflow, and performs runtime checks to ensure this²⁸, as such the verifier concludes that the field increment in processDay(dayOfYear) cannot break the invariant. Spec# is able to avoid some invariant checks in this case by relying on all arithmetic operations performing runtime overflow checks; whereas integer arithmetic in L42 has the common wrap around semantics.

The annotations we had to add in the Spec# version²⁹ were similar to our previous examples, however since the fields of Person all have immutable classes/types, we only needed to add the invariant itself. In order to implement the addChild(child) method we were forced to do a shallow clone of the new child (this also caused a couple of extra runtime invariant checks). Unlike L42 however, we did not need to create a box to hold the parents and children fields, instead we wrapped the body of the Family.processDay(dayOfYear) method in an expose (this) block. In total we needed 16 annotations, worth a total of 45 tokens, this is slightly worse than the code following our approach that we showed above, which has 14 annotations and 14 tokens.

6.4. Encoding Examples from Spec# Papers

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There are many published papers about the pack/unpack methodology used by Spec#. To compare against their expressiveness we will consider the three main ones that introduced their methodology and extensions:

- Verification of Object-Oriented Programs with Invariants [3]: this paper introduces their methodology. In their examples section (pages 41–47), they show how their methodology would work in a class hierarchy with Reader and ArrayReader classes. The former represents something that reads characters, whereas the latter is a concrete implementation that reads from an owned array. They extend this further with a Lexer that owns a Reader, which it uses to read characters and parse them into tokens. They also show an example of a FileList class that owns an array of file names, and a DirFileList class that extends it with a stronger invariant. All of these examples can be represented in L42³⁰. The most interesting considerations are as follow:
 - Their ArrayReader class has a relinquishReader() method that 'unpacks' the ArrayReader and returns its owned array. The returned array can then be freely mutated and passed around by other code. However, afterwards the ArrayReader will be 'invalid', and so one can only call methods on it that do not require its invariant to hold. However, it may later be 'packed' again (after its invariant is checked). In contrast, our approach requires the invariant of all usable objects to hold. We can still relinquish the array, but at the cost of making the ArrayReader forever unreachable. This can be done by declaring relinquishReader() as a capsule method, this works since our type modifier system guarantees that the receiver of such a method is not aliased, and hence cannot be used again. Note that Spec# itself cannot represent the relinquishReader() method at all, since it does not provide explicit pack and unpack operations, rather its expose statement performs both an unpack and a pack, thus we cannot unpack an ArrayReader without repacking it in the same method.
 - Their DirFileList example inherits from a FileList, which has an invariant and a final method, this is something their approach was specifically designed to handle. As L42 does not have traditional subclassing, we are unable to express this concept fully, but L42 does have code reuse via trait composition, in which case DirFileList can include the methods from FileList, and they will automatically enforce the invariant of DirFileList.

 $^{^{28}}$ Runtime checks are enabled by a compilation option; when they fail, unchecked exceptions are thrown.

 $^{^{29} \}mathrm{The}$ Spec# code is in the artifact.

- Object Invariants in Dynamic Contexts [43]: this paper shows how one can specify an invariant for a doubly linked list of ints (here int is an immutable value type). Unlike our protocol however, it allows the invariant of Node to refer to sibling Nodes which are not owned/encapsulated by itself, but rather the enclosing List. Our protocol can verify such a linked list³¹ (since its elements are immutable), however we have to specify the invariant inside the List class. We do not see this as a problem, as the Node type is only supposed to be used as part of a List, thus this restriction does not impact users of List.
- Friends Need a Bit More: Maintaining Invariants Over Shared State [28]: this paper shows how one can verify invariants over interacting objects, where neither owns/contains the others. They have multiple examples which utilise the 'subject/observer' pattern, where a 'subject' has some state that an 'observer' wants to keep track of. In their Subject/View example, Views are created with references to Subjects, and copies of their state. When a Subject's state is modified, it calls a method on its attached Views, notifying them of this update. The invariant is that a View's copy of its Subject's state is up to date. Their Master/Clock example is similar, a Clock contains a reference to a Master, and saves a copy of the Master's time. The Master has a Tick method that increases its time, but unlike the Subject/View example, the Clock is not notified. The invariant is that the Clock's time is never ahead of its Master's. Our protocol is unable to verify these interactions, because the interacting objects are not immutable or encapsulated by each other.

7. Patterns

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In this section we show programming patterns that allow various kinds of invariants. Our goal is not to verify existing code or patterns, but to create a simple system that allows soundly verifying the correctness of data structures. In particular, as we show, in order to use our approach to ensure invariants, one has to program in an uncommon and very defensive style.

The SubInvariant Pattern

We showed how the box pattern can be used to write invariants over cyclic mutable object graphs, the latter also shows how a complex mutation can be done in an 'atomic' way, with a single invariant check. However the box pattern is much more powerful.

Suppose we want to pass a temporarily 'broken' object to other code as well as perform multiple field updates with a single invariant check. Instead of adding new features to the language, like an <code>invalid</code> modifier (denoting an object whose invariant does not need to hold), and an <code>expose</code> statement like Spec#, we can use a 'box' class and a rep mutator to the same effect:

```
interface Person{ mut method Bool accept(read Account a,read Transaction t); }
   interface Transaction{ mut method List<Transfer> compute(); }
   //Here List<T> represents a list of immutable Ts.
   class Transfer{ Int money;
     method Void execute(mut AccountBox that){// Gain some money, or lose some money
1220
       if(this.money>0){ that.income+=money; }
       else{ that.expenses -= money; }
     }
   }
   class AccountBox{
1225
     UInt income=0; UInt expenses=0;
     read method Bool subInvariant(){ return this.income >= this.expenses; }
     //An 'AccountBox' is like a 'potentially invalid Account':
      //we may observe income >= expenses
   }
1230
```

 $^{^{31}}$ Our protocol allows for encoding this example, but to express the invariant we would need to use reference equality, which the L42 language does not support.

```
class Account{
    rep AccountBox box; mut Person holder;
    read method Bool invariant(){ return this.box.subInvariant(); }

    // 'h' could be aliased elsewhere in the program

Account(mut Person h){ this.holder=h; this.box=new AccountBox(); }
    mut method Void transfer(mut Transaction ts){
        if(this.holder.accept(this, ts)){ this.transferInner(ts.compute()); }
    }

// rep mutator, like an 'expose(this)' statement
private mut method Void transferInner(List<Transfer> ts){
        mut AccountBox b = this.box;
        for (Transfer t : ts) { t.execute(b); }
}// check the invariant here
}
```

The idea here is that transfer(ts) will first check to see if the account holder wishes to accept the transaction, it will then compute the full transaction (which could cache the result and/or do some I/O), and then execute each transfer in the transaction. We specifically want to allow an individual Transfer to raise the expenses field by more than the income, however we don't want an entire Transaction to do this. Our rep mutator (transferInner) allows this by behaving like a Spec# expose block: during its body (the for loop) we don't know or care if this.invariant() is true, but at the end it will be checked. For this to make sense, we make Transfer.execute take an AccountBox instead of an Account: it cannot assume that the invariant of Account holds, and it is allowed to modify the fields of that without needing to check it. Though rep mutators can be used to perform batch operations like the above, they can only take immutable and capsule objects. This means that they can perform no non-deterministic I/O (due to our object capabilities system), and other externally accessible objects (such as a mut Transaction) cannot be mutated during such a batch operation.

As you can see, adding support for features like **invalid** and **expose** is unnecessary, and would likely require making the type system significantly more complicated as well as burdening the language with more core syntactic forms.

In particular, the above code demonstrates that our system can:

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- Have useful objects that are not entirely encapsulated: the **Person** holder is a **mut** field; this is fine since it is not mentioned in the invariant() method.
- Wrap normal methods over rep mutators: transfer is not a rep mutator, so it can use this multiple times and take a mut parameter.
- Perform multiple state updates with only a single invariant check: the loop in transferInner(ts) can perform multiple field updates of income and expenses, however the invariant() will only be checked at the end of the loop.
- Temporarily break an invariant: it is fine if during the for loop, expenses > income, provided that this is fixed before the end of the loop.
- Pass the state of an 'invalid' object around, in a safe manner: an AccountBox contains the state of Account, but not the invariant method. Note how programmers can use conventional private types to control how such 'invalid' versions of objects are exposed in the public API, for example by declaring AccountBox as a private nested class). In contrast, if invalid was a type system feature than any user defined type would intrisically expose the existence of both variants in the public API.

Under our strict invariant protocol, the invariant holds for all reachable objects. The sub invariant pattern allows to control when an object is required to be valid. Instead, other protocols strive to allow the invariant to be observed broken in controlled conditions defined by the protocol itself.

The sub invariant pattern offers interesting guarantees: any object 'a' with a subInvariant() method that is checked by the invariant() method of an object 'b' will respect its subInvariant() in all contexts where 'b' is involved in execution. This is because whenever 'b' is involved in execution, its invariant holds.

Moreover, a's subInvariant() can be observed as **false** only if a rep mutator of 'b' is currently active (that is, being executed), or b is now garbage collectable. Thus, even when there is no reachable reference to b in the current stack frame, if no rep mutator on b is active, a's subInvariant() will hold.

In the former example, this means that if you can refer to an Account, you can be sure that its income >= expenses; if you have an AccountBox then you can be sure that either income >= expenses or a rep mutator of the corresponding Account object is currently active. This closely resembles some visible state semantic protocols, aiming to ensure that either an object's invariant holds, or one of its methods is currently active.

Another interesting and natural application of the sub invariant pattern would be to support a version of the GUI such that, when a Widget's position is updated, the Widget can in turn update the coordinates of its parent Widgets, in order to re-establish their subInvariants. This would also make the GUI follow the versions of the composite pattern were objects have references to their 'parent' nodes. The main idea is to define an interface HasSubInvariant, that denotes Widgets with a subInvariant() method. Then, WidgetWithInvariant is a decorator over a Widget; the invariant method of a WidgetWithInvariant checks the subInvariant() of each contained widget.

We define SafeMovable as a Widget and HasSubInvariant. Since subInvariant() methods don't have the restrictions of invariant methods, it allows SafeMovable to be significantly simpler than the version shown before in Section 6.1.

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```
interface HasSubInvariant{ read method Bool subInvariant(); }
    class SafeMovable implements Widget, HasSubInvariant {
      Int width = 300; Int height = 300;
1300
     Int left; Int top; // Here we do not use a box, thus all the state
                          // is in SafeMovable.
     mut Widgets c;
     mut Widget parent;//We add a parent field
      @Override read method Int left(){ return this.left; }
      @Override read method Int top(){ return this.top; }
1305
      @Override read method Int width(){ return this.width; }
      @Override read method Int height(){ return this.height; }
      @Override read method read Widgets children() { return this.c; }
      @Override mut method Void dispatch(Event e){
        for(mut Widget w :this.c){ w.dispatch(e); }
1310
     @Override read method Bool subInvariant() { /*same of original GUI*/ }
      SafeMovable(mut Widget parent, mut Widgets c){
                           //SafeMovable no longer has an invariant,
        this.c=c;
        this.left=5;
                           //so we impose no restrictions on its constructor
1315
        this.top=5;
        this.parent=parent;
        c.add(new Button(0,0,10,10,new MoveAction(this));
   }
1320
    class MoveAction implements Action{
     mut SafeMovable o:
     MoveAction(mut SafeMovable o){ this.o = o; }
     mut method Void process(Event e){
        this.o.left+=1;
1325
        Widget p = this.o.parent;
        ... // mutate p to re-establish its subInvariant
   }
   class WidgetWithInvariant implements Widget{
1330
     rep Widget w;
      @Override read method Int left(){ return this.w.left; }
      @Override read method Int top(){ return this.w.top; }
```

```
@Override read method Int width(){ return this.w.width; }
      @Override read method Int height() { return this.w.height; }
1335
      @Override read method read Widgets children(){ return this.w.c; }
      @Override mut method Void dispatch(Event e){ w.dispatch(e); }
      @Override read method Bool invariant(){ return wInvariant(w); }
      static method Bool wInvariant(read Widget w){
        for(read Widget wi:w.children()){ if(!wInvariant(wi)){ return false; } }
1340
        //Check that the subInvariant of all of w's descendants holds
        if(!(w instanceof HasSubInvariant)){ return true; }
        HasSubInvariant si = (HasSubInvariant)w;
        return si.subInvariant();
1345
     WidgetWithInvariant(capsule Widget w){ this.w = w; }
   }
    ... // main expression
   //#$ is a capability operation making a Gui object
   mut Widget top=new WidgetWithInvariant(new SafeMovable(...))
   Gui.#$().display(top);
```

In this way, the method WidgetWithInvariant.dispatch() is the only rep mutator, hence the only invariant checks will be at the end of WidgetWithInvariant's constructor and dispatch methods.

Importantly, this allows the graph of widgets to be cyclic and for each to freely mutate each other, even if such mutations (temporarily) violate their subInvariant's. In this way a widget can access its parent (whose subInvariant() may not hold) in order to re-establish it. Note that this trade off is logically unavoidable: in order to manipulate a parent in order to fix it, the parent must be reachable, but by mutating a Widget's position, its parent may become invalid. Thus if Widgets were to encode their validity in their invariant() methods they could not have access to their parents. Instead, by encoding their validity in a subInvariant() method, they can access invalid widgets, but this comes at a cost: the programmer must reason as to when Widgets are valid, as we described above.

The Transform Pattern

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Recall the GUI case study from Section 6.1, where we had a Widget interface and a SafeMovable (with an invariant) that implements Widget. Suppose we want to allow Widgets to be scaled, we could add mut setters for width(), height(), left(), and top() in the Widget interface. However, if we also wish to scale its children we have a problem, since Widget.children() returns a read Widgets, which does not allow mutation. We could of course add a mut method zoom(w) to the Widget interface, however this does not scale if more operations are desired. If instead Widget.children returned a mut Widgets, it would be difficult for Widget implementations, such as SafeMovable, to mention their children() in their invariant(). A simple and practical solution would be to define a transform(t) method in Widget, and a Transformer interface like so:

```
interface Transformer <T> { capsule method Void apply(mut T elem); }
interface Widget { ...
    mut method Void top(Int that); // setter for immutable data
    // transformer for possibly encapsulated data
    mut method read Void transform(capsule Transformer < Widgets > t);
}
class SafeMovable implements Widget { ...
    // A well typed rep mutator
    mut method Void transform(capsule Transformer < Widgets > t) {t.apply(this.box.c);}}
The transform method offers an expressive power similar to mut getters, but prevents Widgets from leaking out. With a Transformer, a zoom(w) function could be simply written as:
    static method Void zoom(mut Widget w) {
        w.transform(ws -> { for (wi : ws) { zoom(wi); } });
        w.width(w.width() / 2); ...; w.top(w.top() / 2);
}
```

In the context of reference capabilities, <code>capsule</code> lambdas/closures will only be allowed to capture <code>imm</code> and <code>capsule</code> local variables. Note that the <code>Transformer</code> parameter to transform is <code>capsule</code> and the method <code>Trasformer.apply</code> takes a <code>capsule</code> receiver. In particular, this means that transform will be able to call the lambda at most once, and that those lambdas cannot be saved and passed to multiple calls to transform. However, we could instead make transform take an <code>imm Transformer</code>, and make <code>Transformer.apply</code> be an <code>imm</code> method, this would allow those lambdas to be freely copied and called multiple times, however they would only be able to capture <code>imm</code> local variables.

That is, a lambda is a normal object instantiated from an interface with a single abstract method. Reference capabilities of both the created object and the provided method must be consider when deciding what local variables can be captured. For simplicity in this work we only consider three cases: When creating an imm object by specifying an imm method, only imm local variables can be captured in the lambda closure. When creating a capsule object by specifying a capsule method, only imm and capsule local variables can be captured. When creating a mut object by specifying a mut method, only imm and mut local variables can be captured.

Using Patterns Together: A general and flexible Graph class

Here we rely on all the patterns shown above to encode a general library for **Graphs** of **Nodes**. Users of this library can define personalised kinds of nodes, with their own personalised sub invariant. The library will ensure that no matter how the library is used, for any accessible **Graph**, each user defined sub invariant of its **Nodes** holds. Note that those sub invariants are not restricted to the local state of a node; since they can explore the state of all reachable nodes, they may even depend upon the whole graph.

The Nodes are guaranteed to be encapsulated by the Graph, however they can be arbitrarily modified by user defined transformations using the Transform Pattern.

```
interface Transform <T>{ capsule method read T apply(mut Nodes nodes); }
1410
    interface Node {
     read method Bool subInvariant(read Nodes nodes)
      mut method mut Nodes directConnections()
   class Nodes{//just an ordered set of nodes
     mut method Void add(mut Node n){..}
     read method Int indexOf(read Node n){..}
     mut method Void remove(read Node n){..}
     mut method mut Node get(Int index){..}
1420 }
    class Graph{
     rep Nodes nodes; //box pattern
     Graph(capsule Nodes nodes){..}
     read method read Nodes getNodes(){ return this.nodes; }
      <T> mut method read T transform(capsule Transform<T> t){
1425
       mut Nodes ns=this.nodes;//rep mutator with a single use of 'this'
        return t.apply(ns);//single call of the capsule lambda
     read method Bool invariant(){
        for(read Node n: this.nodes){if(!n.subInvariant(this.nodes)){return false;}}
1430
        return true;
     }
```

We now show how our **Graph** library allows the invariant of the various **Nodes** to be customised by the library user, and arbitrary transformations can be performed on the **Graphs**. This is a generalisation of the example proposed by [44](section 4.2) as one of the hardest problems when it comes to enforcing invariants.

Note how there are only a minimal set of operations defined in the above code, others can be freely defined by the user code, as demonstrated below:

```
class MyNode{
     mut Nodes directConnections;
1440
      mut method mut Nodes directConnections(){ return this.directConnections; }
     MyNode(mut Nodes directConnections){..}
      read method Bool subInvariant(read Nodes nodes){
        /* any user defined condition on this or nodes */}
      capsule method read MyNode addToGraph(mut Graph g){..}
1445
     read method Void connectWith (read Node other, mut Graph g) {..}
   }
   mut Graph g = new Graph(new Nodes());
   read MyNode n1 = new MyNode(new Nodes())).addToGraph(g);
   read MyNode n2 = new MyNode(new Nodes())).addToGraph(g);
    //lets connect our two nodes
   n1.connectWith(n2,g);
```

Here we define a MyNode class, where the subInvariant(nodes) can express any property over this and nodes, such as properties over their direct connections, or any other reachable node.

We can define methods in MyNode to add our nodes to graphs and to connect them with other nodes. Note that the method addToGraph(g) is marked as capsule: this ensures that the node is not in any other graph. In contrast, the method connectWith(other, g) is marked as read, even though it is clearly intend to modify the reachable object graph of this. It works by recovering a mut reference to this from the mut Graph.

These methods can be implemented like this:

```
read method Void connectWith(read Node other, mut Graph g){
      Int i1=g.getNodes().indexOf(this);
      Int i2=g.getNodes().indexOf(other);
      if(i1==-1 \mid | i2==-1)\{throw /*error nodes not in g*/;\}
      g.transform(ns->{
1465
        mut Node n1=ns.get(i1);
        mut Node n2=ns.get(i2);
        n1.directConnections().add(n2);
   }
1470
    capsule method read MyNode addToGraph(mut Graph g){
      return g.transform(ns->{
      mut MyNode n1=this;//single usage of capsule 'this'
      ns.add(n1);
      });
1475
   }
```

As you can see, both methods rely on the transform pattern.

These transformation operations are very general since they can access the mut Nodes of the Graph and any rep or imm data from outside. Note how the body of the capsule lambda in connectWith(other,g), can not capture the read this or the read other, but we get their (immutable) indexes and recover the concrete objects from the mut Nodes ns object. In this way, we also obtain more useful mut references to those nodes. On the other hand, note how in addToGraph(g) we use the reference to the capsule this within the lambda, this allows the lambda to be safely typed as capsule, since there can be no other aliases to this, and the this variable cannot be used again in the method.

8. Integration in L42

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In the last version of L42, invariants have been integrated with caching and automatic parallelism; it would be out of this article's scope to explain in detail this integration, but the overall idea is that an invariant is seen as a Void @Cache.Now method. The language ensures that @Cache.Now methods are recomputed whenever their result may change; any exceptions are propagated immediately, and are not cached. The type-system requires that any method that could alter the result of a Cache.Now method

(except via a field update) must be marked with <code>@Cache.Clear</code> and respect our rep mutator restrictions. L42 requires an explicit <code>@Cache.Clear</code> so as to make it clear in the code that such methods has special type-system restrictions. This is more general than invariant checking however, as <code>Cache.Now</code> methods can return a meaningful result, and not simply success or exception. L42 also supports other kinds of cached methods, which get computed in parallel when an instance of the corresponding class is created, or when their result may be altered.

L42 libraries rely on a very expressive form of metaprogramming to generate a lot of boilerplate/redundant code. In L42 many tasks can be either manually performed by writing code directly, or partially automated by code generation. L42 allows writing class methods (similar to a static method in Java) with appropriate parameters instead of invariants method and rep mutators. The bodies of such methods don't have special restrictions as they cannot see this, instead the meta-programming generates appropriate instance methods, conforming to our restrictions, which call the user provided class methods.

Our restrictions are also checked by the type system, so even if the user manually writes these methods, instead of relying on the metaprogramming, they still cannot break our invariant protocol.

To make this work more accessible to programmers familiar with Java/C#, we have shown our examples in a more Java-like syntax. Here you can see our ShippingList example from Section 4 in the full L42 Syntax:

```
ShippingList = Data:{
    capsule Items items

@Cache.Now
    class method Void invariant(read Items items) =
        X[items.weight()<=300Num]
    @Cache.Clear
    class method Void addItem(mut Items items,Item item) =
        items.add(item)
}</pre>
```

In this example, the Data decorator generates a factory method, a mut method Void addItem(Item item) and a lot of other utility methods, including equality and conversion to string. In particular, note how the current concrete 42 syntax uses the keyword capsule to represent varius kinds of restrictions over fields. The language relies on the presence of annotations or other specific methods to decide what restrictions to apply. In this case, the presence of the @Cache.Now annotation clarifies that the field capsule Items items is actually a rep field as discussed in our work. The @Cache.Now annotation causes the invariant method to be automatically computed, and recomputed every time a @Cache.Clear method is called. The X[...] notation used in invariant is an assert statement: it throws an unchecked exception if it's argument is false. Please refer to Forty2.is for more information.

9. Related Work

Reference Capabilities

We rely on a combination of reference capabilities supported by at least three languages/lines of research: L42 [6, 7, 8, 9], Pony [10, 11], and Gordon et al. [12]. They all support full/deep interpretation (see page 5), without back doors. Former works [45, 46, 47, 48, 49] (which eventually enabled the work of Gordon et al.) do not consider promotion and infers uniqueness/isolation/immutability only when starting from references that have been tracked with restrictive annotations along their whole lifetime. Other approaches like Javari [13, 50] and Rust [32] provide back doors, which are not easily verifiable as being used properly.

Ownership [51, 16, 52] is a popular form of aliasing control often used as a building block for static verification [53, 41]. However, ownership does not require the whole reachable object graph of an object to be 'owned'. This complicates restricting the data accessible by invariants.

Object Capabilities

In the literature, object capabilities are used to provide a wide range of guarantees, and many variations are present. Object capabilities, in conjunction with reference capabilities, are able to enforce purity of code in a modular way, without requiring the use of effects or monads. L42 and Gordon *et al.* use object capabilities

simply to reason about I/O and non-determinism. This approach is best exemplified by Joe-E [27], which is a self-contained and minimalistic language using object capabilities (but not reference capabilities) over a subset of Java in order to reason about determinism. However, in order for Joe-E to be a subset of Java, they leverage a simplified model of immutability: immutable classes must be final and have only final fields that refer to immutable classes. In Joe-E, every method that only takes instances of immutable classes is pure. Thus their model would not allow the verification of purity for invariant methods of mutable objects. In contrast our model has a more fine grained representation of mutability: it is reference-based instead of class-based. Thanks to this crucial difference, in our work every method taking only read or imm references as receivers and parameters is pure, regardless of their class type. In particular, we allow the parameter of such a method to be mutated later on by other code.

Invariant protocols

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Invariants are a fundamental part of the design by contract methodology. Invariant protocols differ wildly and can be unsound or complicated, particularly due to re-entrancy and aliasing [43, 54, 55].

While invariant protocols all check and assume the invariant of an object after its construction, they handle invariants differently across object lifetimes. Popular approaches include:

- The invariants of objects in a *steady* state are known to hold: that is when execution is not inside any of the objects' public methods [5]. Invariants need to be constantly maintained between calls to public methods.
- The invariant of the receiver before a public method call and at the end of every public method body needs to be ensured. The invariant of the receiver at the beginning of a public method body and after a public method call can be assumed [56, 54]. Some approaches ensure the invariant of the receiver of the *calling* method, rather than the *called* method [57]. JML [58] relaxes these requirements for helper methods, whose semantics are the same as if they were inlined.
- The same as above, but only for the bodies of 'selectively exported' (i.e. not instance-private) methods, and only for 'qualified' (i.e. not this) calls [55].
- The invariant of an object is assumed only when a contract requires the object be 'packed'. It is checked after an explicit 'pack' operation, and objects can later be 'unpacked' [3].

These different protocols can be deceivingly similar. Note that all those approaches fail our strict requirements and allow for broken objects to be observed. Some approaches like JML suggest verifying a simpler approach (that method calls preserve the invariant of the *receiver*) but assume a stronger one (the invariant of *every* object, except **this**, holds).

Security and Scalability

Our approach allows verifying an object's invariant independently of the execution context. This is in contrast to the main strategy of static verification: to verify a method, the system assumes the contracts of other methods, and the content of those contracts is the starting point for their proof. Thus, static verification proceeds like a mathematical proof: a program is valid if it is all correct, but a single error invalidates all claims. This makes it hard to perform verification on large programs, or when independently maintained third party libraries are involved. Static verification has more flexible and fine-grained annotations and often relies on a fragile theorem prover as a backend.

To soundly verify code embedded in an untrusted environment, as in gradual typing [59, 60], it is possible to consider a verified core and a runtime verified boundary. One can see our approach as an extremely modularized version of such a system: every class is its own verified core, and the rest of the code could have Byzantine behaviour. Our proofs show that every class that compiles/type checks is soundly handled by our protocol, independently of the behaviour of code that uses such a class or any other surrounding code.

Our approach works both in a library setting and with the open world assumption. Consider for example the work of Parkinson [61]: he verified a property of the Subject/Observer pattern. However, the proof relies on (any override of) the Subject.register(Observer) method respecting its contract. Such assumption is unrealistic in a real-world system with dynamic class loading, and could trivially be broken by a user-defined

EvilSubject: checking contracts at load time is impractical and is not done by any verification systems we know of.

Static Verification

AutoProof [62] is a static verifier for Eiffel that also follows the Boogie methodology, but extends it with semantic collaboration where objects keep track of their invariants' dependencies using ghost state.

Dafny [1] is a language where all code is statically verified. It supports invariants with its {:autocontracts} annotation, which treats a class's Valid() function as the invariant and injects pre and post-conditions following visible state semantics. However it requires objects to be newly allocated (or cloned) before another object's invariant may depend on it. Dafny is also generally highly restrictive with its rules for mutation and object construction, it also does not provide any means of performing non-deterministic I/O.

Spec# [63] is a language built on top of C#. It adds various annotations such as method contracts and class invariants. It primarily follows the Boogie methodology [64] where (implicit) annotations are used to specify and modify the owner of objects and whether their invariants are required to hold. Invariants can be ownership based [3], where an invariant only depends on objects it owns; or visibility based [28, 65], where an invariant may depend on objects it doesn't own, provided that the class of such objects know about this dependence. Unlike our approach, Spec# does not restrict the aliases that may exist for an object, rather it restricts object mutation: an object cannot be modified if the invariant of its owner is required to hold. This allows invariants to query owned mutable objects whose reachable object graph is not fully encapsulated. However as we showed in Section 6.1, it can become much more difficult to work with and requires significant annotation, since merely having an alias to an object is insufficient to modify it or call its methods. Spec# also works with existing .NET libraries by annotating them with contracts, however such annotations are not verified. Spec#, like our approach, does perform runtime checks for invariants and throws unchecked exceptions on failure. However Spec# does not allow soundly recovering from an invariant failure, since catching unchecked exceptions in Spec# is intentionally unsound. [66]

Specification languages

Using a specification language based on the mathematical metalanguage and different from the programming language's semantics may seem attractive, since it can express uncomputable concepts, has no mutation or non-determinism, and is often easier to formally reason about. However, a study [67] discovered that developers expect specification languages to follow the semantics of the underlying language, including short-circuit semantics and arithmetic exceptions; thus for example 1/0 | | 2>1 should not hold, while 2>1 | | 1/0 should, thanks to short circuiting. This study was influential enough to convince JML to change its interpretation of logical expressions accordingly [68]. Dafny [1] uses a hybrid approach: it has mostly the same language for both specification and execution. Specification ('ghost') contexts can use uncomputable constructs such as universal quantification over infinite sets, whereas runtime contexts allow mutation, object allocation and print statements. The semantics of shared constructs (such as short circuiting logic operators) is the same in both contexts. Most runtime verification systems, such as ours, use a metacircular approach: specifications are simply code in the underlying language. Since specifications are checked at runtime, they are unable to verify uncomputable contracts.

Ensuring determinism in a non-functional language is challenging. Spec# recognizes the need for purity/determinism when method calls are allowed in contracts [69] 'There are three main current approaches: a) forbid the use of functions in specifications, b) allow only provably pure functions, or c) allow programmers free use of functions. The first approach is not scalable, the second overly restrictive and the third unsound'. They recognize that many tools unsoundly use option (c), such as AsmL [70]. Spec# aims to follow (b) but only considers non-determinism caused by memory mutation, and allows other non deterministic operations, such as I/O and random number generation. In Spec# the following verifies: [Pure] bool uncertain() {return new Random().Next() % 2 == 0;}

And so assert uncertain() == uncertain(); also verifies, but randomly fails with an exception at runtime. As you can see, failing to handle non-determinism jeopardises reasoning. A simpler and more restrictive solution to these problems is to restrict 'pure' functions so that they can only read final fields and call other pure functions. This is the approach used by [71]. One advantage of their approach is that invariants (which must be 'pure') can read from a chain of final fields, even when they are contained in otherwise mutable

objects. However their approach completely prevents invariants from mutating newly allocated objects, thus greatly restricting how computations can be performed.

Runtime Verification Tools

By looking to a survey by Voigt et al. [72] and the extensive MOP project [73], it seems that most runtime verification (RV) tools empower users to implement the kind of monitoring they see fit for their specific problem at hand. This means that users are responsible for deciding, designing, and encoding both the logical properties and the instrumentation criteria [73]. In the context of class invariants, this means the user defines the invariant protocol and the soundness of such protocol is not checked by the tool.

In practice, this means that the logic, instrumentation, and implementation end up connected: a specific instrumentation strategy is only good to test certain logic properties in certain applications. No guarantee is given that the implemented instrumentation strategy is able to support the required logic in the monitored application. Some of these tools are designed to support class invariants: for example InvTS [74] lets you write Python conditions that are verified on a set of Python objects, but the programmer needs to be able to predict which objects are in need of being checked and to use a simple domain specific language to target them. Hence if a programmer makes a mistake while using this domain specific language, invariant checking will not be triggered. Some tools are intentionally unsound and just perform invariant checking following some heuristic that is expected to catch most failures: such as jmlrac [56] and Microsoft Code Contracts [75].

Many works attempt to move out of the 'RV tool' philosophy to ensure RV monitors work as expected, as for example the study of contracts as refinements of types [76]. However, such work is only interested in pre and post-conditions, not invariants.

Our invariant protocol is much stricter than visible state semantics, and keeps the invariant under tight control. Gopinathan et al.'s. [5] approach keeps a similar level of control: relying on powerful aspect-oriented support, they detect any field update in the whole reachable object graph of any object, and check all the invariants that such update may have violated. We agree with their criticism of visible state semantics, where methods still have to assume that any object may be broken; in such case calling any public method would trigger an error, but while the object is just passed around (and for example stored in collections), the broken state will not be detected; Gopinathan et al. says "there are many instances where o's invariant is violated by the programmer inadvertently changing the state of p when o is in a steady state. Typically, o and p are objects exposed by the API, and the programmer (who is the user of the API), unaware of the dependency between o and p, calls a method of p in such a way that o's invariant is violated. The fact that the violation occurred is detected much later, when a method of o is called again, and it is difficult to determine exactly where such violations occur."

However, their approach addresses neither exceptions nor non-determinism caused by I/O, so their soundess guarantee does not scale to programs using such features.

Their approach is very computationally intensive, but we think it is powerful enough that it could even be used to roll back the very field update that caused the invariant to fail, making the object valid again. We considered a rollback approach for our work, however rolling back a single field update is likely to be completely unexpected, rather we should roll back more meaningful operations, similarly to what happens with transactional memory, and so is likely to be very hard to support efficiently. Using reference capabilities to enforce strong exception safety is a much simpler alternative, providing the same level of safety, albeit being more restrictive.

Chaperones and impersonators [77] lifts the techniques of gradual typing [78, 59, 60] to work on general purpose predicates, where values can be wrapped to ensure an invariant holds. This technique is very powerful and can be used to enforce pre and post-conditions by wrapping function arguments and return values. This technique however does not monitor the effects of aliasing, as such they may notice if a contract has been broken, but not when or why. In addition, due to the difficulty of performing static analysis in weakly typed languages, they need to inject runtime checking code around every user-facing operation.

10. Conclusion

In this paper we (1) identified the essential language features that support representation invariants in object-oriented verification; (2) presented a full formalism for our approach with capabilities that is proved to soundly guarantee that all objects involved in execution are valid; (3) conducted extensive case studies showing that we require many order of magnitude less runtime checking than *visible state semantics* and three times less annotation burden than an equivalent version in Spec#. We hope that as a result of this work, the software verification community will make more use of the advanced general purpose language features, such as capabilities, appearing in modern languages to achieve its goals.

Our approach follows the principles of offensive programming [79] where no attempt to fix or recover an invalid object is performed. Failures (unchecked exceptions) are raised close to their cause: at the end of constructors creating invalid objects and immediately after field updates and instance methods that invalidate their receivers.

Our work builds on a specific form of reference and object capabilities, whose popularity is growing, and we expect future languages to support some variations of these. Crucially, any language already designed with such a support can also support our invariant protocol with minimal added complexity.

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Appendix A. Invariant Protocol Proof and Type System Requirements

As previously discussed, we provide a set of requirements that the type system needs to ensure, and prove the soundness of our invariant protocol over these, in this way we are parametric over the concrete typesystem. In Appendix B, we present an example typesystem and prove that it satisfies these requirements.

Auxiliary Definitions

To express our type system assumptions, we first need some auxiliary definitions.

First, we inductively define the set of objects in the reachable object graph (ROG) of a location l:

- $l' \in ROG(\sigma, l)$ iff:
- $\exists f \text{ such that } l' \in ROG(\sigma, \sigma[l.f])$

We define the mROG of an l to be the locations reachable from l by traversing through any number of mut and rep fields:

 $l' \in mROG(\sigma, l)$ iff:

• l' = l, or

• l' = l, or

• $\exists f \text{ such that } C_l^{\sigma}.f = \kappa f, \kappa \in \{\text{mut, rep}\}, \text{ and } l' \in mROG(\sigma, \sigma[l.f])$

Thus the mROG of l are the objects that could be mutated via a reference to l.

We define what it means for an l to be reachable from an expression or context:

- $reachable(\sigma, e, l)$ iff $\exists l' \in e$ such that $l \in ROG(\sigma, l')$
- $reachable(\sigma, \mathcal{E}, l)$ iff $\exists l' \in \mathcal{E}$ such that $l \in ROG(\sigma, l')$

We now define what it means for an object to be *immutable*: it is in the *ROG* of an **imm** reference or a reachable **imm** field:

 $immutable(\sigma, e, l)$ iff $\exists l'$ such that:

- $\operatorname{imm} l' \in e$, and $l \in ROG(\sigma, l')$, or
- $reachable(\sigma, e, l'), C_{l'}^{\sigma} f = imm_{-}f$, and $l \in ROG(\sigma, \sigma[l'.f])$, for some f

Now we can define what it means for an l to be $mutatable^{32}$ by an expression e: something reachable from l can also be reached by using a **mut** or **capsule** reference in e, and traversing through any number of **mut** or **rep** fields:

 $mutatable(\sigma, e, l)$ iff $\exists l', l''$ such that:

- $l' \in ROG(\sigma, l)$
- $\mu l'' \in e \text{ with } \mu \in \{\text{mut}, \text{capsule}\}\$

 $^{^{32}}$ We use the term mutatable and not 'mutable' as an object might be neither mutatable nor immutable, e.g. if there are only read references to it.

• $l' \in mROG(\sigma, l'')$

The idea is that e could mutate something reachable from l: by using l'' to get a **mut** reference to l', and then performing a field update on it; the new field value for l' would then be observable through l. In particular, we will require the typesystem to ensure that e can only mutate state observable from l if l is mutatable.

Finally, we model the *encapsulated* property of capsule references:

encapsulated (σ, \mathcal{E}, l) iff $\forall l' \in ROG(\sigma, l)$, if $mutatable(\sigma, \mathcal{E}[\texttt{capsule}\ l], l')$, then not $reachable(\sigma, \mathcal{E}, l')$. That is, a location l found in a context \mathcal{E} is encapsulated if all mutatable objects in its ROG would be unreachable with that single use of l removed. That single use of l is the connection preventing those mutatable objects from being garbage collectable.

Type System Requirements

As we do not have a concrete type system, we need to assume some properties about the expressions that it admits. Rather than requiring each expression during reduction to be well-typed, we instead let the type-system impose restrictions on method bodies, and type-check the initial expression, we then require properties on all future memories and expressions (i.e. validStates). In Appendix B we show such a type-system and prove it satisfies these requirements, but these requirements do not hold for arbitrary well-typed $\sigma|e$ pairs, only for validStates. This allows the type-system to be simpler, in particular, as the initial main expression can only have \mathtt{mut} references to c (an object with no fields(), the type-system need not check that the heap structure and reference capabilities in the main expressions are consistent.

First we require that fields and methods are only given values with the correct reference capabilities, i.e. the field initialisers of **new** expressions, the right hand sides of update expressions, and the receiver and parameters of method calls have the capabilities required by the field declarations/method signatures:

Requirement 1 (Type Consistency).

- 1. If $validState(\mathcal{E}[\text{new } C(\mu_1, ..., \mu_n]))$, then:
 - there is a class C implements _ {Fs;_}
 - $Fs = \kappa_1 \ldots \kappa_n \ldots$
 - $\mu_1 \leq \widetilde{\kappa}_1, ..., \mu_n \leq \widetilde{\kappa}_n$
- 2. If $validState(\mathcal{E}[_l.f = \mu_l])$, then:
 - $C_l^{\sigma}.f = \kappa f$
 - $\mu \leq \widetilde{\kappa}$

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- 3. If $validState(\mathcal{E}[\mu_0 l.m(\mu_1 , ..., \mu_n]))$, then:
 - $C_l^{\sigma}.m = \mu_0' \text{ method } m(\mu_1', -, -, \mu_n', -)$
 - $\mu_0 \le \mu'_0, ..., \mu_n \le \mu'_n$

This requirement also ensure that objects are created with the appropriate number of fields, and that fields and methods that are accessed/updated/called actually exist.

Now we define formal properties about our reference capabilities, thus giving them meaning. First we require that an *immutable* object can not also be *mutatable*: i.e. if an object is reachable from an *imm* reference or field, then no part of its ROG can be reached by starting at a mut or capsule reference, and then traversing through mut and rep fields:

Requirement 2 (Imm Consistency).

If $validState(\sigma, \mathcal{E}[e])$ and $immutable(\sigma, e, l)$, then not $mutatable(\sigma, e, l)$.

Thus e cannot use field accesses to obtain a mut or capsule reference to anything reachable from an *immutable* l. Note that this does not prevent *promotion* from a mut to an imm: an as expression can change a reference from mut to imm, provided that in the new state there are no longer any mut references to the ROG of l. Note that from the definition of mutatable and immutable, it follows that if l is immutable in any e, then it is immutable in $\mathcal{E}[e]$, and not mutatable in any $e' \in \mathcal{E}[e]$.

We require that if something was not *mutatable*, it remains that way:

Requirement 3 (Mut Consistency).

If $validState(\sigma, \mathcal{E}[e])$, not $mutatable(\sigma, e, l)$, and $\sigma|e \to^* \sigma'|e'$, then not $mutatable(\sigma', e', l)$.

Note that this holds even if l is mutatable through \mathcal{E} , thus an **as** expression cannot change a **read** or **imm** reference to **mut**, as the associated location will not be mutatable within the body of the **as** expression, even if there are **mut** references to the same object outside the **as**.

We require that any capsule reference is encapsulated, i.e. that no mutatable part of its ROG is reachable through any other reference:

Requirement 4 (Capsule Consistency).

If $validState(\sigma, \mathcal{E}[\mathtt{capsule}\,l])$, then $encapsulated(\sigma, \mathcal{E}, l)$.

As all objects are created as mut, the only way to actually get a capsule reference is via an as expression. As our reduction rules impose no constraints on such expressions, the type-system must ensure that it only accepts a as capsule expression if it is guaranteed to return an encapsulated reference. Note that a specific typesystem's idea of "capsuleness" may in fact be stronger then encapsulated, but encapsulated is sufficient for our invariant protocol.

We require that field updates are only performed on mut/capsule receivers:

Requirement 5 (Mut Update).

If $validState(\mathcal{E}[\mu_{--}=])$, then $\mu \leq mut$.

Finally we require strong exception safety: the body of a **try** block does not mutate objects that existed before the enclosing **try-catch** began executing and are reachable outside the **try** block:

Requirement 6 (Strong Exception Safety).

If $validState(\sigma', \mathcal{E}_v[\mathsf{try}^\sigma\{e\} \mathsf{catch} \{e'\}])$, then $\forall l \in dom(\sigma)$, if $reachable(\sigma, \mathcal{E}_v[e'], l)$, then $\sigma(l) = \sigma'(l)$.

Note that this strong requirement *only* needs to hold because our try-catch can catch invariant failures: in L42, try-catch's that catch *checked* exceptions do not need this restriction. Note that as our reduction rules never modify the body of a catch, it follows that if $validState(\sigma', \mathcal{E}_v[try^{\sigma}_{-}] catch \{e\}])$, then for any $l \in dom(\sigma')$, if $l \notin dom(\sigma)$, then l is not reachable in $\mathcal{E}_v[e]$.

Usefull Lemmas

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First we prove a few useful lemmas about the properties of references in our language.

We show that a sub-expression can mutate an object only if it is *mutatable*:

Lemma 1 (Non Mutating).

If $validState(\sigma, \mathcal{E}[e])$, $l \in dom(\sigma)$, not $mutatable(\sigma, e, l)$, and $\sigma|e \to^* \sigma'|e'$, then $\sigma'(l) = \sigma(l)$.

Proof. By Mut Consistency, l never becomes mutatable, and so we never obtain a mut or capsule reference to it, thus by Mut Update, we never update the fields of l, and there are no reduction rules that remove from

By the definition of *validState* and the reduction rules themselves, we can show that the main expression and heap never contain dangling references:

Lemma 2 (No Dangling).

If $validState(\sigma, e)$ then:

- $\forall l \in e, l \in dom(\sigma)$
- $\forall l \in dom(\sigma)$, if $\sigma(l) = C\{ls\}$ then $\{ls\} \subseteq dom(\sigma)$

Proof. The proof is by definition of validState, and induction on the number of reductions since the initial memory and main-expression. In the base case, by definition of validState, the only l in the main-expression and memory is c, which is defined in the memory. In the inductive case, each reduction rule only introduces ls into the memory or main-expression that were either already there, or in the case of NEW/NEW TRUE, that are simultaneously added to the dom of the memory. As a simple corollary of this, we have that if $l \in dom(\sigma)$, then $ROG(\sigma, l) \subseteq dom(\sigma)$, similarly with mROG.

Similarly, we show that once an l becomes un-reachable, it remains that way:

Lemma 3 (Lost Forever).

If $validState(\sigma, \mathcal{E}[e])$, and $\sigma|e \to^* \sigma'|e'$, then $\forall l \in dom(\sigma)$, if not $reachable(\sigma, e, l)$, then not $reachable(\sigma', e', l)$.

Proof. The proof follows from induction on the number of reductions, and the fact that each reduction either does not introduce an l into the main expression or heap, or only introduces ls that were already reachable (in the case of UPDATE and ACCESS), or only introduces an $l \notin dom(\sigma)$ (in the case of NEW/NEW TRUE)

We can use our object capability discipline (described in Section 5) to prove that the **invariant()** method is deterministic and does not mutate existing memory:

Lemma 4 (Determinism).

If $validState(\sigma, \mathcal{E}[\texttt{read}\,l.\texttt{invariant()}])$ and $\sigma[\texttt{read}\,l.\texttt{invariant()}] \to^n \sigma'[e']$, for some $n \geq 0$, then:

- $\sigma \subset \sigma'$
- $\sigma | \mathbf{read} \, l.$ invariant() $\Rightarrow^n \sigma' | e'$

Proof. As the only reference in read l.invariant() is read l, it follows from the definition of mutatable, that there is no l' with $mutatable(\sigma, read l.invariant(), <math>l'$), thus by Mutatatable Update we have that for all $l \in dom(\sigma)$, $\sigma(l) = \sigma(l')$, i.e. $\sigma \subseteq \sigma'$

We show the second part by induction on n: if n=0, then no reduction was performed, $e'=\mathsf{read}\,l.\mathsf{invariant}()$, and it trivially holds that $\sigma|\mathsf{read}\,l.\mathsf{invariant}() \Rightarrow^0 \sigma|\mathsf{read}\,l.\mathsf{invariant}()$. In the inductive case, we have some σ'' and e'' with $\sigma|\mathsf{read}\,l.\mathsf{invariant}() \to^{n-1} \sigma''|e'' \to \sigma'|e'$, and assume our inductive hypothesis that $\sigma|\mathsf{read}\,l.\mathsf{invariant}() \Rightarrow^{n-1} \sigma''|e''$. As c is not $\mathit{mutatable}$ in $\mathsf{read}\,l.\mathsf{invariant}()$, by Mut Consistency, $\mathsf{mut}\,c \notin e''$ and $\mathsf{capsule}\,c \notin e''$. Since, by definition, there are never any other instances of Cap, it follows from Type Consistency that the reduction $\sigma''|e'' \to \sigma'|e'$ was not due to CALL/CALL MUTATOR reducing a call to a mut method of Cap. As all other methods are uniquely defined, the reduction must have been deterministic, i.e. $\sigma''|e'' \to \sigma'|e'$, and so by the inductive hypothesis, we have $\sigma|\mathsf{read}\,l.\mathsf{invariant}() \Rightarrow^n \sigma''|e''$.

Rep Field Soundness

[Isaac: Re-read everything from this point!] Now we define and prove important properties about our novel rep fields. We first start with a few core auxiliary definitions. To simplify the notation, we define the repFields of an l to be the set of rep field names for l:

```
repFields(\sigma, l) = \{f \text{ where } C_l^{\sigma}.f = rep_{-}f\}
```

We say that an l and f is *circular* if l is reachable from l.f:

 $circular(\sigma, l, f)$ iff $l \in ROG(\sigma, \sigma[l.f])$.

We say that an l is repCircular if any its rep fields are circular:

 $\exists f \in repFields(\sigma, l) \text{ such that } circular(\sigma, l, f).$

We say that an l and f is confined if l.f is not mutatable without passing through l:

 $confined(\sigma, l, f)$ iff not $mutatable(\sigma \setminus l, e, \sigma[l.f])$. We say that an l is repConfined if each of its rep fields are confined:

 $\forall f \in repFields(\sigma, l) \text{ we have } confined(\sigma, l, f).$

We say that an l is repMutating if we are in a monitor for l which must have been introduced by CALL MUTATOR:

```
repMutating(\sigma, e, l) iff e = \mathcal{E}[M(l; e'; \bot)], with e' \neq mut l.
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Finally we say that l is headNotObservable if we are in a monitor introduced for a call to a rep mutator, and l is not reachable from inside this monitor, except perhaps through a single **rep** field access:

 $headNotObservable(\sigma, e, l)$ iff $e = \mathcal{E}_v[M(l; e'; _)]$, and either:

- not $reachable(\sigma, e', l)$, or
- $e' = \mathcal{E}[\mathtt{mut} \ l.f], f \in repFields(\sigma, l), \text{ and not } reachable(\sigma, \mathcal{E}, l)$

Now we formally state the core properties of our rep fields (informally described in Section 3):

Theorem 2 (Rep Field Soundness).

If $validState(\sigma, e)$ then $\forall l$ with $reachable(\sigma, e, l)$, we have:

- not $repCircular(\sigma, l, f)$, and
- one of the following holds:

- $repConfined(\sigma, l)$ and not $repMutating(\sigma, e, l)$, or

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- headNotObservable(σ , e, l). That is, for every reachable object l: l is not reachable through any of its rep fields, and either we are in a rep mutator for l and l is not observable (except perhaps through a single rep field access), or we are not repMutating l, and each of ls rep fields are confined. Proof. By validState we have $c \mapsto \text{Cap}\{\}|e_0 \to^m \sigma|e$, so we proceed by induction on m, the number of reductions. The base case when m=0 is trivial, since Cap has no rep fields and the initial main expression e_0 cannot contain monitors.

 $e_0, ..., e_{m-1}$, where $\sigma_0|e_0$ is a valid initial memory and expression. Our inductive hypothesis is then that the conclusion of our theorem holds for each $\sigma_i|e_i$, for $i \in [0, m-1]$. We then proceed by cases on the reduction rule applied, and prove the theorems conclusion for $\sigma|e$:

- 1. (NEW/NEW TRUE) $\sigma'|\mathcal{E}_v[\text{new }C(\mu_1 l_1,...,\mu_n l_n)] \stackrel{\rightarrow}{\to} \sigma|\mathcal{E}_v[e'],$
 - where $\sigma = \sigma', l_0 \mapsto C\{l_1, ..., l_n\}$; by Type Cosnsistency, we have class C implements $\{\kappa_1 f_1, ..., \kappa_n f_n\}$.
 - (a) We have that l_0 is not repCircular: by No Dangling, we have that $\forall l' \in dom(\sigma'), ROG(\sigma', l') \subseteq$ $dom(\sigma')$. By our notational conventions for ",", it follows that $l_0 \notin dom(\sigma')$. Now consider each $i \in [1, n]$, since the pre-existing σ' was not modified, it follows that $ROG(\sigma', l_i) =$ $ROG(\sigma, \sigma[l_0.f_i])$. By No Dangling we have that $ROG(\sigma, \sigma[l_0.f_i]) \subseteq dom(\sigma)$, and so $l_0 \notin ROG(\sigma, \sigma[l_0.f_i])$, thus each $l_0.f_i$ is not *circular*.
 - (b) Ever reachable $l' \neq l_0$ is not repCircular: Since reduction didn't modify the fields of any preexisting l', by the inductive hypothesis, we have that l' is still not repCircular.
 - (c) The new l_0 is repConfined and not repMutating:
 - ullet Consider each $i \in [1,n]$ with $\kappa_i = {\tt rep}.$ By Type Consistency and Capsule Consistency, l_i was encapsulated and so $ROG(\sigma', l_i)$ cannot be mutatable from \mathcal{E}_v . Thus, we don't have $mutatable(\sigma \setminus l_0, \mathcal{E}_v[e'], l_i)$, and so each of l_0 s rep fields is confined.
 - We trivially have that l_0 is not repMutating since $l_0 \notin dom(\sigma')$, by No Dangling, there can't be any monitor expressions for it in \mathcal{E}_v .
 - (d) Every reachable $l' \neq l_0$ that was repConfined and not repMutating still is:
 - Suppose we have made it so that for some $f' \in repFields(\sigma', l'), l'.f'$ is no longer confined. Since we didn't modify the ROG of l' nor the ROG of any other pre-existing l'', we must have that $\sigma'[l'.f']$ is now mutatable through $l_0.f_i$, for some $i \in [1, n]$. This requires that l_i is an initialiser for a mut or rep field, which by Type Consistency means that $\mu_i \leq \text{mut}$. But then $\sigma'[l',f']$ was already mutatable through $\mu_i l_i$, so l',f' can't have already been confined, a contradiction.
 - We can't have caused l' to be repMutating since we haven't introduced any monitor expressions, nor modified any existing ones.
 - (e) Every reachable $l' \neq l_0$ is headNotObservable: by No Dangling, $l' \in dom(\sigma')$, so by Lost Forever, l'must have already been reachable. Thus, by the inductive hypothesis, l' must be headNotObservable, but we haven't removed any monitor expression or field accesses (because the arguments to the constructor are all fully reduced values), thus l' is still headNotObservable.
- 2. (ACCESS) $\sigma | \mathcal{E}_v[\mu l.f] \to \sigma | \mathcal{E}_v[\mu :: \kappa \sigma[l.f]]$, where $C_l^{\sigma}.f = \kappa f$:
 - (a) No reachable l' is rep Circular: this holds by the inductive hypothesis and the fact that we haven't mutated memory.
 - (b) If l is reachable and it was repConfined and not repMutating, than it still is:
 - If $\kappa \neq \text{rep}$, then we can't have broken confined for any $f' \in repFields(\sigma, l)$, since by definition of repConfined, $\sigma[l.f']$ can't have been mutatable through $\sigma[l.f]$.
 - If $\kappa = \text{rep}$, since l' was not repMutating, this field access can't have been inside a rep mutator (or else we would be inside a monitor). As fields are instance private, we have $\mu \neq \text{mut}$, or else the field access would have come from a rep mutator.
 - If $\mu = \text{capsule}$, then by Capsule Consistency and repCircular, l is not reachable from $\mathcal{E}_v[\mu :: \kappa \sigma[l.f]]$, so it is irrelevant if l is no longer repConfined. Otherwise, since $\mu \notin \{Kwcapsule, mut\}$, we have $\mu::\kappa \nleq \text{mut}$, so l.f is still confined. By the above case for $\kappa \neq \text{rep}$, every other $f' \in repFields(\sigma, l)$ is confined.

- We can't have made l' repMutating since we have introduced any monitor expressions.
- (c) If l was repMutating or not repConfined, than it is headNotObservable: by the inductive hypothesis, l was headNotObservable before this reduction, thus $\mathcal{E}_v = \mathcal{E}_v'[\mathtt{M}(l; \mathcal{E}_v''; \lrcorner)]$. As l is clearly reachable in $\mathcal{E}_v''[\mu l.f]$, by definition of headNotObservable we must have that l is not reachable from \mathcal{E}_v'' , and $\kappa = \mathbf{rep}$. By repCircular, l is not in the ROG of $\sigma[l.f]$, and so l is not reachable from $\mathcal{E}_v''[\mu :: \kappa \sigma[l.f]]$, and so it is still headNotObservable.
- (d) Every reachable $l' \neq l$ that was repConfined and not repMutating, still is:
 - Since this reduction doesn't modify memory, and $\mu::\kappa \leq \text{mut}$ only if $\mu \leq \text{mut}$, we can't have made the ROG of any rep field f' of l' mutatable without going through l', so repConfined is preserved.
 - As in the NEW/NEW TRUE case above, we can't have made *repMutating* hold as we haven't introduced any monitor expressions.
- (f) Every reachable $l' \neq l$ that was repMutating or not repConfined is headNotObservable: as this reduction doesn't create any new objects, by No Dangling and Lost Forever, anything reachable was already reachable, thus by the inductive hypothesis, l' must have been headNotObservable. but we haven't removed any monitor expression or field accesses on l', thus l' must still be headNotObservable.
- 3. (UPDATE) $\sigma'|\mathcal{E}_v[\mu l.f = \mu' l'] \rightarrow \sigma'[l.f = l']|\mathcal{E}_v[M(l; \text{mut } l; \text{read } l.\text{invariant()})]$:
 - (a) For each $f' \in repFields(\sigma, l)$, l.f' is still not repCircular:

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- if f' = f, then by Type Consistency and Capsule Consistency, $encapsulated(\sigma', \mathcal{E}_v[\mu l. f = \Box], l')$. Hence l is not reachable from l', and so after the update, l.f' cannot be circular.
- otherwise, by the inductive hypothesis, l.f' was not repCircular, so $l \notin ROG(\sigma', \sigma'[l.f'])$, and so this update couldn't have change the ROG of l.f', and so it is still repCircular.
- (b) For every reachable $l'' \neq l$, and $f' \in repFields(\sigma, l'')$, l''.f' is still not circular:
 - By the inductive hypothesis, l''.f' was not *circular*.
 - If l'' was repConfined, by Mut Update, $\mu \leq \text{mut}$. By repConfined, the ROG of $\sigma'[l''.f']$ is not mutatable, except through a field access on l'', but this rule doesn't perform a field access, so since $l'' \neq l$, we must have that $l \notin ROG(\sigma', \sigma'[l''.f'])$. Since we can't have modified the ROG of $\sigma'[l''.f']$, l''.f' is still not circular.
 - Otherwise, by the inductive hypothesis, l'' was headNotObservable, and so $l'' \notin ROG(\sigma', l')$, so we can't have added l'' to the ROG of anything, thus l''.f' is still not circular.
- (c) Any $reachable\ l''$ that was repConfined and not repMutating still is:
 - Suppose l'' = l and $f \in repFields(\sigma', l)$, by Type Consistency and Capsule Consistency, l' is encapsulated, thus l' is not mutatable from \mathcal{E}_v , and l is not reachable from l'. Hence l' is still encapsulated, and so l.f is still confined.
 - Now consider any $f' \in repFields(\sigma', l'')$, with $l''.f' \neq l.f$; by the above, l is not repCircular and so $l \notin ROG(\sigma', \sigma'[l''.f'])$. If f was a **mut** or **rep** field, by Type Consistency, $\mu' \leq \text{mut}$, so by repConfined, $l' \notin ROG(\sigma', \sigma'[l''.f'])$; thus we can't have made $ROG(\sigma', \sigma'[l''.f'])$ mutatable through l.f; so $\sigma'[l''.f']$ can't now be mutatable through **mut** l. By Mut Consitency, we couldn't have have made $\sigma'[l''.f']$ mutatable some other way, so l'' is still repConfined.
 - As in the above cases for NEW/NEW TRUE, l'' is still not repMutating as we haven't introduced any monitor expressions.

- (d) Every reachable l' that was repMutating or not repConfined is headNotObservable: similarly to the above case for ACCESS, as this reduction doesn't create any new objects, by by No Dangling and Lost Forever, anything reachable was already reachable, thus by the inductive hypothesis, l' must have been headNotObservable. but we haven't removed any monitor expression or field accesses, thus l' must still be headNotObservable.
- 4. (CALL/CALL MUTATOR) $\sigma | \mathcal{E}_v[\mu_0 \, l_0.m(\mu_1 \, l_1, ..., \mu_n \, l_n)] \rightarrow \sigma | \mathcal{E}_v[e]$

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- (a) Every reachable l' is not repCircular: as this rule doesn't mutate memory, by the inductive hypothesis, every reachable l' is still not repCircular.
- (b) If \hat{l}_0 was repConfined and not repMutating, it either still is, or is now headNotObservable:
 - As we haven't modified memory, and by our well-formedness rules on method bodies, we haven't introduce any new ls into the main-expression, we must have that l_0 is still repConfined.
 - Suppose the rule applied was CALL, by our well-formedness rules for method bodies, e doesn't contain a monitor. Moreover, by the CALL rule, e is not a rep mutator, if $e = \mathcal{E}[\mu' l_0.f]$, for some $f \in repFields(\sigma, l_0)$, we must have that m was not a mut method. Since fields are instance-private, we must have $\mu' \nleq mut$, and by our well-formedness rules on method bodies, e doesn't contain any monitors, thus we can't have caused l_0 to be repMutating.
 - Otherwise, the rule applied was CALL MUTATOR, and m is a rep mutator, so $e = M(l_0; e'; read l_0.invariant())$ By our rules for rep mutators, m must be a mut method with only imm and capsule parameters, thus by Type Consistency, $\mu_0 \leq \text{mut}$, and for each $i \in [1, n]$, $\mu_i \in \{\text{imm}, \text{capsule}\}$. By Imm Consistency and Capsule Consistency, l_0 can't be reachable from any l_i . Since rep mutators use this only once, to access a rep field, $e' = \mathcal{E}[\text{mut} l_0.f]$, for some $f \in repFields(\sigma, l_0)$. By our rules for rep mutators, $l_0 \notin \mathcal{E}$, and l_0 is not reachable from any l_i , and by our well-formedness rules for method bodies, there are no other l_i in \mathcal{E} , thus we have that l_0 is not reachable from any \mathcal{E} , thus headNotObservable now holds for l.
- (c) Every $l' \neq l_0$ that was repConfined and not repMutating, still is:
 - By the above, since we haven't modified memory or introduced any new ls, l' must still be repConfined.
 - Since $l' \neq l_0$ and fields are instance-private, we must have that there is no $\mu' l' \cdot f \in e$. Moreover, by our well-formedness rules on method bodies, and the CALL/CALL MUTATOR rules, the only monitor that could be in e is a monitor on l_0 , thus we can't have made l' repMutating.
- (d) Every reachable l' that was repMutating or not repConfined is headNotObservable: as in the UPDATE case above, by the inductive hypothesis, l' must have been headNotObservable, as we haven't removed any monitor expressions or field accesses, l' is still headNotObservable.
- 5. (TRY ERROR) $\sigma | \mathcal{E}_v[\mathsf{try}^{\sigma'}\{e\} \mathsf{catch} \{e'\}] \to \sigma | \mathcal{E}_v[e']$, where $error(\sigma, e)$
 - (a) Every reachable l is not repCircular: as in the CALL/CALL MUTATOR case above, since this rule doesn't mutate memory, by the inductive hypothesis, every reachable l is still not repCircular.
 - (b) Every reachable l that was repConfined and not repMutating still is: by Mut Consistency and the fact that we haven't modified memory, l must still be repConfined. Since we haven't introduced any monitor expressions or field accesses, l cannot now be repMutating.
 - (c) If l is still reachable, and was repMutating or not repConfined then it is now repConfined and not repMutating:
 - By definition of *error*, we have $e = \mathcal{E}_{v}'[M(l; v; v')]$.
 - If the monitor was introduced by NEW or UPDATE, then v = mut l. And so headNotObservable can't have held for l since l = l', and v was not the receiver of a field access. Thus by the inductive hypothesis, l must have been repConfined and not repMutating, a contradiction.
 - By definition of *validState* and our well-formedness rules on method bodies, we must have that monitor must introduced by CALL MUTATOR, due to a call to a rep mutator on l.³³

 $^{^{33}}$ A type-system will likely prevent this case from happening, as this would require calling a **mut** method on l, but l is reachable outside the **try** block. However, if the typesystem can prove that said **mut** method will not actually mutate l, this would not violate our requirements. Thus we still need to ensure that Rep Field Soundness holds in this case.

- From our reduction rules, it follows that we were previously in a state $\sigma_i|e_i$, where $i \in [1, m-1]$, e_i is of form $\mathcal{E}_v''[e'']$, and the next state was obtained by said application of the CALL MUTATOR rule to e''.
- Moreover, it follows that $\mathcal{E}_v'' = \mathcal{E}_v[\mathsf{try}^{\sigma'}\{\mathcal{E}_v'\}\ \mathsf{catch}\ \{e'\}]$, as no reduction rules modify the \mathcal{E}_v .
- We must not have had that l was headNotObservable, since e'' would contain l as the receiver of a method call. Thus, by our inductive hypothesis, in state i, l was repConfined and not repMutating.
- By Strong Exception Safety and No Dangling, every l' reachable from $\mathcal{E}_v[e']$ has not been mutated, i.e. $\sigma(l') = \sigma_i(l') = \sigma'(l)$.
- Since nothing reachable has been mutated, it follows that l is still repConfined.
- By validState and our well-formedness rules on method bodies, it follows that e' contains no monitor expressions.
- Moreover, since l was not repMutating in $\mathcal{E}_v[\mathsf{try}^{\sigma'}\{\mathcal{E}_v'[e'']\}\ \mathsf{catch}\ \{e'\}]$, and e' contains no monitors, l it follows that l is not repMutating in $\mathcal{E}_v[e']$.
- (d) Every reachable $l'' \neq l$ that was repMutating or not repConfined is headNotObservable: as in the above case for UPDATE, by the inductive hypothesis, l'' must have been headNotObservable, as we haven't removed any monitor expressions on l'', or any field accesses, l'' is still headNotObservable.
- 6. (MONITOR EXIT) $\sigma |\mathcal{E}_v[\mathbf{M}(l; \mu l';])| \rightarrow \sigma |\mathcal{E}_v[\mu l']|$

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- (a) Every reachable l'' is not repCircular: as in the CALL/CALL MUTATOR case above, since this rule doesn't mutate memory, by the inductive hypothesis, every reachable l'' is still not repCircular.
- (b) Every reachable l'' that was repConfined and not repMutating still is: as in the TRY ERROR case above, by Mut Consistency and the fact that we haven't modified memory, l'' must still be repConfined. Since we haven't introduced any monitor expressions or field accesses, l'' cannot now be repMutating.
- (c) If l is still reachable, and l was repMutating or not repConfined then it is now repConfined and not repMutating:
 - If the monitor was introduced by NEW or UPDATE, then $\mu l' = \text{mut } l$. And so headNotObservable can't have held for l since l = l', and v was not the receiver of a field access. Thus by the inductive hypothesis, l must have been repConfined and not repMutating, a contradiction.
 - By definition of validState and our well-formedness rules on method bodies, we must have that monitor must introduced by CALL MUTATOR, due to a call to a rep mutator on l.
 - From our reduction rules, it follows that we were previously in a state $\sigma_i|e_i$, where $i \in [1, m-1]$, e_i is of form $\mathcal{E}_v'[e']$, and the next state was obtained by said application of the CALL MUTATOR rule to e'.
 - Moreover, it follows that $\mathcal{E}_{v}' = \mathcal{E}_{v}$, as no reduction rules modify the \mathcal{E}_{v} .
 - We must not have had that l was headNotObservable, since e' would contain l as the receiver of a method call. Thus, by our inductive hypothesis, in state i, l was repConfined and not repMutating.
 - As with the above case for try error, by the inductive hypothesis, *l* must have been *headNotObservable*, and so the monitor must have been introduced by CALL MUTATOR.
 - Thus, we were previously in a state $\sigma_i|e_i$ where $i \in [1, m-1]$, e_i is of form $\mathcal{E}_v[e']$, and the next state was obtained by said application of the CALL MUTATOR rule to e'.
 - Thus, by the inductive hypothesis, in state i, l must have been repConfined and not repMutating.
 - Because l was not repMutating in $\sigma_i | \mathcal{E}_v[e']$, and $\mu l'$ contains no monitors, l is not repMutating in $\mathcal{E}_v[\mu l']$.
 - Since a rep mutator cannot have any **mut** parameters, by Type Consistency and Non Mutating, the body of the method can only modify things *mutatable* through *l*, or a **capsule** parameter.

- By Type Consistency, and Capsule Consistency, every capsule parameter is *encapsulated*, and so anything mutated through such a parameter must have been un *reachable* outside the call.
- Thus, for all $l' \in dom(\sigma_i)$, if $reachable(\sigma_i, \mathcal{E}_v, l')$ and $l' \notin mROG(\sigma_i, l)$, then $\sigma(l) = \sigma_i(l)$.
- If $\mu = \text{capsule}$, then by Capsule Consistency, not part of the mROG of any rep field of l can be in the ROG of l' (or else l would have to be unreachable), so we can't have made such a field mutatable.
- If $\mu \neq \text{capsule}$, then since a rep mutator cannot have a mut return type, and our CALL MUTATOR rule wraps the method body in a as expression, we must have that $\mu \not\leq \text{mut}$. Thus $\mu \in \{\text{read, imm}\}$, and so by l is not mutatable through $\mu l'$.
- As l was repConfined in $\sigma_i | \mathcal{E}_v[e']$, and we haven't modified anything reachable through $\sigma \setminus l$, nor have we made the ROG of l mutatable through $\mu l'$, it follows that l is also repConfined in $\mathcal{E}_v[\mu l']$.
- (d) Every reachable $l'' \neq l$ that was repMutating or not repConfined is headNotObservable: as in the UPDATE case above, by the inductive hypothesis, l'' must have been headNotObservable, as we haven't removed any monitor expressions on l'', or any field accesses, l'' is still headNotObservable.
- 7. (AS, TRY ENTER, and TRY OK) these are trivial, since as in the above cases:
 - (a) Every $reachable\ l$ is not repCircular: as in the CALL/CALL MUTATOR case above, since these rules don't mutate memory, by the inductive hypothesis, every $reachable\ l$ is still not repCircular.
 - (b) Every reachable l that was repConfined and not repMutating still is: as in the TRY ERROR case above, by Mut Consistency and the fact that these rules don't modified memory, l must still be repConfined. Since this rules don't introduce any monitor expressions or field accesses, l cannot now be repMutating.
 - (c) Every reachable l that was repMutating or not repConfined is headNotObservable: as in the UPDATE case above, by the inductive hypothesis, l must have been headNotObservable, as these rules don't remove any monitor expressions or field accesses, l'' is still headNotObservable.

Stronger Soundness

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It is hard to prove Soundness directly, so we first define a stronger property, called Stronger Soundness.

We say that an object is *monitored* if execution is currently inside of a monitor for that object, and the monitored expression e_1 does not contain a reference to l as a proper sub-expression:

monitored(e, l) iff $e = \mathcal{E}_v[\mathbf{M}(l; e'; _)]$ and $l \in e'$ only if $e' = _l$.

A monitored object is associated with an expression that cannot observe it, but may reference its internal representation directly. In this way, we can safely modify its representation before checking its invariant. The idea is that at the start the object will be valid and e' will reference l; but during reduction, l will be used to modify the object, but not observe it; only after that moment, the object may become invalid.

Stronger Soundness says that starting from a well-typed and well-formed $\sigma_0|e_0$, and performing any number of reductions, every reachable object is either valid or monitored:

Theorem 3 (Stronger Soundness).

If $validState(\sigma, e)$ then $\forall l$, if $reachable(\sigma, e, l)$, then $valid(\sigma, l)$ or monitored(e, l).

Proof. As with the above proof of Rep Field Soundness, we will prove this inductively on the number of reductions. By validState we have $c \mapsto \operatorname{Cap}\{\}|e_0 \to^m \sigma|e$, The base case when m=0 is trivial, from our requirements for the Cap class, $\sigma|\operatorname{read} c.\operatorname{invariant}() \to \sigma|\operatorname{new} \operatorname{True}() \to \sigma, l \mapsto \operatorname{True}\{\}|l$, for some l, thus by Determinism, it follows that c (the only thing in the memory) is valid.

In the inductive case, where m > 0, we have $\sigma_0|e_0 \to ... \to \sigma_{m-1}|e_{m-1} \to \sigma|e$, for some $\sigma_0, ..., \sigma_{m-1}$ and $e_0, ..., e_{m-1}$, where $\sigma_0|e_0$ is a valid initial memory and expression. Our inductive hypothesis is then that that everything reachable from the previous validState is valid or monitored. We then proceed by cases on the reduction rule that gets us to $\sigma|e$:

- 1. (NEW) $\sigma'|\mathcal{E}_v[\text{new }C(_l_1,_,_l_n)] \rightarrow \sigma', l_0 \mapsto C\{l_1,_,l_n\}|\mathcal{E}_v[\text{M}(l_0;\text{mut }l_0;\text{read }l_0.\text{invariant())}]$:
 - Clearly the newly created object, l, is monitored.

- This rule does not modify pre-existing memory, introduce pre-existing ls into the main expression, nor remove monitors on other ls, by the inductive hypothesis, every $l' \neq l_0$ is still valid (due to Determinism), or monitored.
- 2. (NEW TRUE) $\sigma' | \mathcal{E}_v[\text{new True}()] \rightarrow \sigma', l_0 \mapsto \text{True}\{\} | \mathcal{E}_v[\text{mut } l_0]$:
 - The True class is required to have an invariant of **new True()**, so as with c in the base case above, we have that l_0 is valid.
 - As in the above case for NEW, since we didn't modify pre-existing memory, introduce pre-existing ls into the main expression, nor remove monitors, by the inductive hypothesis, every $l' \neq l_0$ is still valid or monitored.
- 3. (UPDATE) $\sigma'|\mathcal{E}_v[\mu l.f = v] \to \sigma|\mathcal{E}_v[e']$, where e' = M(l; mut l; read l.invariant()):
 - Clearly l is now monitored.

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• Consider any other l', where $l \in ROG(\sigma', l')$ and l' was valid; now suppose we just made l' in valid. By our well-formedness criteria, invariant() can only accesses imm and rep fields, thus by Non Mutating, and Determinism, we must have that l was in the ROG of $\sigma'[l'.f']$, for some $f' \in repFields(\sigma', l')$.

Since $l \neq l'$, l' can't have been repConfined. Thus, by Rep Field Soundness, l' was headNotObservable, and so $\mathcal{E}_v[\mu l. f = v]$ is of form $\mathcal{E}_v'[\mathsf{M}(l'; e''; e''')]$:

- As the ROG of l' has just been mutated, and since e''' must have started off as read l'''.invariant(), if follows from Determinism, that we cannot currently be inside e'''.
- Thus, $\mathcal{E}_v = \mathcal{E}_v'[M(l'; \mathcal{E}_v''; e''')]$, where $\mathcal{E}_v''[\mu l.f = v] = e''$.
- Suppose that l' was not reachable in e'', then clearly $l' \notin e''$, since $l' \neq l$, it follows that $l' \notin \mathcal{E}_{v''}[e']$, and so l' is monitored.
- Otherwise, by definition of headNotObservable, we have that $e'' = \mathcal{E}[\mathtt{mut}\, l'.f'']$ for some $f'' \in repFields(\sigma', l')$, and where l' is not reachable in \mathcal{E} .
- By the proof for the TRY ERROR case of Rep Field Soundness, the monitor must have come from a call to a rep mutator, in a state where l' was repConfined. Thus, we were previously in a state $\sigma_i|e_i$, for some $i\in[0,m-1]$, immediately after a CALL MUTATOR; moreover, e_i is of form $\mathcal{E}_v'[\mathsf{M}(l';e_i';\omega)]$, immediately after a CALL MUTATOR, where e_i' is of form $\mathcal{E}'[\mathsf{mut}\,l'.f''']$.
- By Rep Field Soundness, l' is not reachable through $\sigma'[l'.f''']$,. By the proof for the CALL/CALL MUTATOR case of Rep Field Soundness, we have that l' is not reachable through \mathcal{E}' . Thus, by Lost Forever, once $\mathtt{mut}\,l'.f'''$ has been reduced, l' must be $\mathtt{un}\,reachable$, and it follows that $\mathtt{mut}\,l'.f''' = \mathtt{mut}\,l'.f'''$
- By Mut Update, l is mutatable in the current state, thus by Mut Consistency, we have that it was also mutatable when CALL MUTATOR rule was applied. But we have that l' was repConfined, so since $l \in ROG(\sigma', \sigma'[l'.f'])$, we have that l can only be mutatable through l'.
- By Lost Forever, the only way we could have obtain a reference to l was by reducing mut l'.f'', but we haven't done that yet, a contradiction.
- Every other valid l', where $l \notin ROG(\sigma', l')$ is still valid by Determinism.
- As in the above case, since we don't remove any monitors, any other l' that was monitored, is still monitored.
- 4. (TRY ERROR) $\sigma | \mathcal{E}_v[\mathsf{try}^{\sigma'}\{e\} \mathsf{catch} \{e'\}] \to \sigma | \mathcal{E}_v[e'], \text{ where } error(\sigma, e) = \mathcal{E}_v'[\mathsf{M}(l; _; _)]$:
 - As with the case for TRY ERROR in the proof of Rep Field Soundnes, we were previously in a state $\sigma_i|e_i$, where $e_i = \mathcal{E}_v[\mathtt{try}^{\sigma'}\{_\}\ \mathtt{catch}\ \{_\}]$, and $\sigma_i = \sigma'$.
 - By definition of error, we have that l is not valid in σ . [Isaac: Because monitors always start of ass invariant calls]
 - Suppose l is still reachable in $\sigma | \mathcal{E}_v[e']$, by Strong Exception Safety, we have $l \in dom(\sigma')$. Thus by the inductive hypothesis, we have that l was valid or monitored in the state $\sigma' | e_i$.

- If *l* was *monitored*, then by *validState* and our well-formedness rules on method bodies, said monitor must have been introduced by the NEW, UPDATE, or CALL MUTATOR reduction rules.
- The NEW and UPDATE rules monitor a value, which cannot reduce to a try-catch, so the monitor must have been introduced by CALL MUTATOR.[Isaac: No new bullet point]
- But by our well-formedness rules on rep mutators, the body of the called method cannot mention l except to read a field, as shown in the case for UPDATE above, l will be unreachable once the field access has been reduced, which by Lost Forever is a contradiction, as l is reachable through e.
- Thus, l can't have been monitored in $\sigma'|e_i$, so it must have been valid.
- Also by Strong Exception Safety, we have that nothing reachable from l could have been modified, that is $\forall l' \in ROG(\sigma', l)$, we have $\sigma'(l') = \sigma(l')$. By Lost Forever, and our reduction rules, any memory location not reachable from a call read l-invariant() cannot affect its reduction.
- Thus, by Determinism, and the fact that l was valid in σ , we have that l is still valid, a contradiction.
- Thus, l cannot be reachable, so the fact that it is in valid is irrelevant.
- As in the above case for NEW, since we didn't modify any memory, or remove any other monitors, by the inductive hypothesis every $l' \neq l$ is still valid or monitored.
- 5. (MONITOR EXIT) $\sigma | \mathcal{E}_v[\mathbf{M}(l; v; \mathbf{imm} l')] \to \sigma | \mathcal{E}_v[v]$, where $C_{l'}^{\sigma} = \mathbf{True}$:
 - By *validState* and our well-formedness requirements on method bodies, the monitor expression must have been introduced by UPDATE, CALL MUTATOR, or NEW. In each case the third expression started off as **read** *l.***invariant()**, and it has now (eventually) been reduced to **imm** *l'*, thus by Determinism *l* is *valid*.
 - As in the above case for NEW, since we didn't modify any memory, or remove any other monitors, by the inductive hypothesis every reachable $l' \neq l$ is still valid or monitored.
- 6. (ACCESS, CALL/CALL MUTATOR, AS, TRY ENTER, and TRY OK) these are trivial:
 - As in the above case for NEW, since these rules don't modify memory or remove monitors, by the inductive hypothesis, every *reachable l* is still *valid* or *monitored*.

Proof of Soundness

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[Isaac: I haven't checked the proofs here for correctness yet, I need a break...] First we need to prove that an object is not reachable from one of its imm fields; if it were, invariant() could access such a field and observe a potentially broken object:

Lemma 5 (Imm Not Circular).

If $validState(\sigma, e), \forall f, l$, if $reachable(\sigma, e, l), C_l^{\sigma}.f = imm_{-}f$, then $l \notin ROG(\sigma, \sigma[l.f])$.

Proof. The proof is by induction; obviously the property holds in the initial $\sigma|e$, since $\sigma=c\mapsto \operatorname{Cap}\{\}$. Now suppose it holds in a $\operatorname{validState}(\sigma',e')$ where $\sigma'|e'\to\sigma|e$:

- 1. Consider any pre-existing reachable l and f with $C_l^{\sigma'}.f = \underline{\mathsf{imm}}_-f$, by Imm Consistency and Non Mutating, the only way $ROG(\sigma, \sigma[l.f])$ could have changed is if $e' = \mathcal{E}_v[\mu \, l.f = \mu' \, l']$, where $\mu \leq \mathtt{mut}$, i.e. we just applied the UPDATE rule. By Type Consistency, $\mu' \leq \underline{\mathsf{imm}}$, so by Imm Consistency, $l \notin ROG(\sigma, l')$. Since $l' = \sigma[l.f]$, we now have $l \notin ROG(\sigma, \sigma[l.f])$.
- 2. The only rules that make an l reachable are NEW/NEW TRUE. So consider $e = \mathcal{E}_v[\text{new } C(_l_1, _, _l_n)]$, and each i with $C.i = \text{imm}_f$. But each of $l_1, _, l_n$ existed in the previous state and $l \notin dom(\sigma')$; so by validState and our reduction rules, $l \notin ROG(\sigma', l_i) = ROG(\sigma, \sigma[l.f])$.

Note that the above only applies to imm fields: imm references to cyclic objects can be created by promoting a mut reference, however the cycle must pass through a field declared as read or mut, but such fields cannot be referenced in the invariant method.

We can now finally prove the soundness of our invariant protocol:

Theorem 4 (Soundness). If $validState(\sigma, \mathcal{E}_r[_l])$, then either $valid(\sigma, l)$ or $trusted(\mathcal{E}_r, l)$.

Proof. Suppose $validState(\sigma, e)$, and $e = \mathcal{E}_r[-l]$. Suppose l is not valid; since l is reachable, by Stronger Soundness, monitored(e, l), $e = \mathcal{E}[M(l; e_1; e_2)]$, and either:

- $\mathcal{E}_r = \mathcal{E}[M(l; \mathcal{E}'; e_2)]$, that is l was found inside of e_1 , but by definition of \mathcal{E}_r , we can't have $e_1 = \mu l$, this contradicts the definition of monitored, or
- $\mathcal{E}_r = \mathcal{E}[\mathsf{M}(l; e_1; \mathcal{E}')]$, and thus l was found inside e_2 . By our reduction rules, all monitor expressions start with $e_2 = \mathtt{read}\,l.\mathtt{invariant}()$; if this has yet to be reduced, then $\mathcal{E}' = \mathcal{E}''[\Box.\mathtt{invariant}()]$, thus $trusted(\mathcal{E}_r, l)$. By our well-formedness rules for $\mathtt{invariant}()$, the next reduction step will be a CALL, e_2 will only contain l as the receiver of a field access; so if we just performed said CALL, $\mathcal{E}' = \mathcal{E}''[\Box.f]$: hence $trusted(\mathcal{E}_r, l)$. Otherwise, by Imm Not Circular, Rep Field Soundness, and $trusted(\mathcal{E}_r, l)$ was introduced by the CALL to $trusted(\mathcal{E}_r, l)$, and so $trusted(\mathcal{E}_r, l)$.

Thus either l is valid or $trusted(\mathcal{E}_r, l)$.

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Appendix B. Typesystem and Proof of Requirements

Appendix C. Safe Parallelism in 42, without destructive reads

This section discuss the relation between our work and the 42 support for safe unobservable parallelism. From its inception, the work on 42 tried to build a system supporting flexible, elegant and soundly unobservable parallelism without the need of relying on destructive reads. 42 uses the same kind of reference and object capabilities used by Pony and Gordon, but while they allow for *true* isolated fields with destructive reads, 42 avoids them. That is: in Pony/Gordon we can easy define a class boxing a capsule references as follows

```
class Box{ //pseudocode for clarity
   iso Foo foo;//isolated field
   Box(iso Foo foo){this.foo=foo;}//initialized with an iso reference
   mut method iso Foo getFoo(){return this.foo;}//destructive read here
   }//the getter mutates the box (destructive read) and returns the stored iso reference
   //usage
  iso Foo myFoo = ..
   mut Box box = new Box(myFoo);//the type system ensures this is the only usage of 'myFoo'
   //box is now a mut object and can be freely passed around and aliased
  iso Foo foo1 = box.getFoo();//this foo1 can now be used for parallelism
  iso Foo foo2 = box.getFoo();//either foo2==null or exception is thrown here
```

42 does not support destructive reads. Thus, there is no way to declare method getFoo(). This also means that after putting encapsulated data into a field of any kind, it is not possible to extract the data back as encapsulated. Indeed, if 42 where to somehow allow the initialization of foo1 we would then have two ways to reach the 'encapsulated' data, thus breaking the encapsulation guarantee. Thus, the 42 research has explored various ways to access those fields, that are initialized with encapsulated data but can not soundly release the data as capsule. From a research perspective, it was interesting to discover many different access patterns that allowed to preserve some encapsulation properties but not others. On the other side, it is worth of notice that exploring those different kind of encapsulated data does not impact the way capsule references are threated when passed around as method parameters or saved in local variables, nor their parallemism properties.

Indeed, in 42, as in Pony or Gordon, we can make fork-join where the parallel branches only use capsule variables. The difference is that in 42 those variables will not be able to come from reading encapsulated fields of mut objects. Note that this is because, as a research question, the 42 developers are trying to understand how far they can go without resorting to destructive reads. They could easely add a primitive datatype working as a consumable mutable box storing a true capsule. Such a primitive data type would behave exactly like the Box type above. Then, a 42 user could chose to use those boxes to recover all the expressive power (and risks) of destructive reads. Doing so would however make it much harder to claim that 42 supports expressive automatic parallelism without the need of destructive reads, since destructive reads would now be avaible on demand.

Parallel patterns in 42

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The current version of 42 relies on the annotation <code>@Cache.ForkJoin</code> and the <code>Data</code> decorator to activate varius forms of (unobservable) automatic parallelism. We show those forms below. Of course, the invariant protocol described in this paper does work also in the context of <code>@Cache.ForkJoin</code>, thus it is impossible to observe a broken invariant, even when using parallelism. This is a direct result of the fact that parallelism in 42 is unobservable: the semantic of parallel code is equivalent to the semantic of the corresponding sequential code, only the performance change.

$Non\text{-}Mutable\ computation$

This is the simplest 42 parallel pattern. Consider the following code in 42:

```
Example = Data:{
    @Cache.ForkJoin class method

2460    capsule D foo(capsule A a, capsule B b, imm C c, read D d) = (
        mut A a0=a.op(d)
        mut B b0=b.op(c)
        mut C c0=c.op(d)
        a0.and(b0).and(c0)
    }
}
```

The initialization expressions for a0, b0, and c0 are run in parallel, and the final expression is run only when all of the initialization expressions are completed. The method itself can take any kind of parameters, and they can all be used in the final expression, but the initialization expressions need to fit one of the recognized safe parallel patterns. In non-mutable computation only read,capsule and imm parameters can be used in the initialization expressions. The name non-mutable computation comes from the fact that, even if the capsules can indeed be mutated, nothing that is visible outside of the fork-join can be mutated while the fork-join is open; thus parallelism is unobservable.

More in general, @Cache.ForkJoin works only on methods whose body is exactly a round parenthesis block, with some local variable initialization expressions and a conclusive expression. Thus, fork-join methods will follow this specific syntactic pattern:

```
@Cache.ForkJoin \mu method T_0 m(T_1x_1,...,T_nx_n) = ( T_0' \quad x_0 = e_0 \\ ... \\ T_k' \quad x_k = e_k \\ e \\ )
```

where the varius expressions $e_0...e_k$ are executed in parallel, and the final expression e is executed after all of $e_0...e_k$. Different forms of parallelism impose different requirements on the free variables that expressions $e_0...e_k$ can use.

Some readers find suprising that in the *non-mutable computation* pattern read references can be freely used, since there can be mut references to those same objects. However, those mut references are all unreachable from inside our fork-join. This is because the whole mutROG of all the capsule rerefences is encapsulated and other mut references are not allowed.

This form of parallelism is the only one proposed by Gordon; it is very expressive in their setting with destructive reads, but it is quite limited in 42. However 42 offers other forms of parallelism, as shown below.

Single-Mutable computation

In this pattern, a single initialization expression can use any kind of parameter, while the other ones can not use mut, lent (a variation of mut present in 42) or read parameters. This pattern allows the single initialization expression that can use mut to recursively explore a complex mutable data structure and to update immutable elements arbitrarily nested inside of it. Consider for example this code computing in parallel new immutable string values for all of the entries in a mutable list:

```
UpdateList = Data:{
      class method S map(S that) = that++that//could be any user defined code
      class method Void of (mut S.List that) = this.of (current=0I, data=that)
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      class method Void of(I current, mut S.List data) = (
        if current < data.size()</pre>
          this.of(current=current,elem=data.val(current),data=data)
        )
      @Cache.ForkJoin class method Void of (I current, S elem, mut S.List data) = (
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        S newElem=this.map(elem)
        this.of(current=current+1I,data=data)
        data.set(current, val=newElem)
      }
2510
    //usage
    mut S.List data = S.List[S"a";S"b";S"c";S"d";S"e";]
    UpdateList.of(data)
   Debug(data)//["aa"; "bb"; "cc"; "dd"; "ee"]
```

As you can see, we do not need to copy the whole list. We can update the elements in place one by one. If the operation map(that) is complex enough, running it in parallel could be beneficial. You can equivalently read this code either as a fork join or as sending the computation this.map(elem) to be run on a separate worker, while the computation this.of(current=current+1I,data=data) is executed on the current thread. Indeed, to implement a fork join it is always more efficient to run the last branch in the current thread. As you can see, it is trivial to adapt that code to explore other kinds of collections, like for example a binary tree. The visit of the tree will be performed recursively but sequentially in the current thread, and workers will be spowned at all recursive layers and their results will be composed at the end of the recursion.

Those two forms of parallelism where already possible on the 42 model before our work on invariants and our rep fields. We think that it is pretty impressive that this kind of parallelism can be obtained without destructive reads. Building on top of our the rep fields and on the concept of rep mutators, a new form of parallel fork-join computation was recently added: This-Mutable computation.

This-Mutable computation

In this pattern, the this variable is considered specially. The method must be declared mut, and the initialization expressions can not use mut, lent or read parameters. However, the mut parameter this can be used to directly call rep mutator methods (marked by @Cache.Clear in the 42 syntax). Since a rep mutator can mutate the reachable object graph of a rep field, and the mutROG from different rep fields is disjoint, different initialization expressions must use rep mutators updating different rep fields. In this way, 42 can express parallel computation processing arbitrary complex mutable objects inside well encapsulated data structures. Consider the following example, where instances of Foo could be arbitrarily complex; containing complex (possibly circular) graphs of mutable objects.

```
class method Void rightOp(mut Tree right, I a, S b) = right.op(a=a,b=b)
    Leaf = Data:{[Tree]
      capsule Foo label
      @Cache.Clear
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      class method Void op(mut Foo label, I a, S b) = label.op(a=a,b=b)
    //usage
    mut Tree top = Node(
      left=Node(
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        left=Leaf(label=..)
        right=Leaf(label=..)
      right = Node (
        left=Leaf(label=..)
2565
        right=Leaf(label=..)
      )
    top.op(a=15I b=S"hello")
```

This pattern relies on the fact that using **rep** fields we can define arbitrary complex data structures composed of disjointed mutable object graphs. Note that **read** aliases to parts of the data structure can be visible outside. This is safe since we can not access them when the forkjoin is open. The declarations can not use **read** parameters.

Non fork-join parallelism in 42

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42 also supports eager caching using the annotation @Cache.Eager. This form of parallelism is limited to start only from fully immutable data. This annotation can be used only on no args methods of objects that are born immutable. Parallel workers are used to eagerly compute the result of those methods and cache the result in the object. This form of parallelism allows to express computation in a very declarative style, but it does not interact with capsule references, our rep fields or rep mutators, so an in-dept discussion of @Cache.Eager is out of scope.

Parallelism in older versions of the 42 type system

42 has been undergoing many changes across the years. The earlier version of the 42 type system was based on [??], where you could see many more modifiers, including fresh and baloon. In that version fresh is similar to the current 42 capsule references and baloon is similar to one of the various kinds of capsule fields available in 42 before our work on rep fields. That work was then summarized in a short 6 pages paper [??], that refers to both fresh and baloon as baloon; using the different context (reference, local variable, field) to make change the meaning of the single keword baloon, to cover both roles of fresh and baloon in [..]. Even in those earlier works there was no way to recover a fresh from a baloon, and a baloon was basically a kind of encapsulated reference that allowed other restricted kinds of references (external and external readonly) to point inside of it. Looking back to those earlier work it is clear to us that the current 42 type system is much more minimal and elegant. Those works suggested interesting forms of parallelism where the type system could cooperate with a few efficent run time pointer equality checks to decide what to run in parallel. Such a direction has not been explored further and it is not currently present in modern versions of 42.