

# Using nested classes as associated types.

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## Abstract

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## 1 Introduction

Associated types are a powerful form of generics, now integrated in both Scala and Rust. They are a new kind of member, like methods fields and nested classes. Associated types behave as 'virtual' types: they can be overridden, can be abstract and can have a default. However, the user has to specify those types and their concrete instantiations manually; that is, the user have to provide a complete mapping from all virtual type to concrete instantiation. When the number of associated types is small this poses no issue, but it hinders designs where the number of associated types is large. In this paper we examine the possibility of completing a partial mapping in a desirable way, so that the resulting mapping is sound and also robust with respect to code evolution.

The core of our design is to reuse the concept of nested classes instead of relying of a new kind of member for associated types. An operation, call Redirect, will redirect some nested classes in some external types. To simplify our formalization and to keep the focus on the core of our approach, we present our system on top of a simple Java like languages, with only final classes and interfaces, when code reuse is obtained by trait composition instead of conventional inheritance. We rely on a simple nominal type system, where subtyping is induced only by implementing interfaces; in our approach we can express generics without having a polymorphic type system. To simplify the treatment of state, we consider fields to be always instance private, and getters and setters to be automatically generated, together with a `static` method `of(..)` that would work as a standard constructor, taking the value of the fields and initializing the instance. In this way we can focus our presentation to just (static) methods, nested classes and implements relationships. Expanding our presentation to explicitly include visible fields, constructors and sub-classing would make it more complicated without adding any conceptual underpinning. In our proposed setting we could write:

```
String=...
SBox={String inner;
  method String inner(){..} //implicit
  static method SBox of(String inner){..} //implicit
myTtrait={
  Box={Elem inner} //implicit Box(Elem inner) and Elem inner()
  Elem={Elem concat(Elem that)}
  static method Box merge(Box b, Elem e){return Box.of(b.inner().concat(e));}
}
Result=myTrait<Box=SBox> //equivalent to trait<Box=SBox, Elem=String>
...Result.merge(SBox.of("hello "), "world");//hello world
```



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## 23:2 Using nested classes as associated types.

48 Here class **SBox** is just a container of **Strings**, and **myTrait** is code encoding **Boxes** of any kind  
49 of **Elem** with a **concat** method. By instantiating **myTrait<Box=SBox>**, we can infer **Elem=String**,  
50 and obtain the following flattened code, where **Box** and **Elem** has been removed, and their  
51 occurrences are replaced with **SBox** and **String**.

```
52 Result={static method SBox merge(SBox b,String e){  
53   return SBox.of(b.inner().concat(e));}  
54  
55
```

56 Note how **Result** is a new class that could have been written directly by the programmer,  
57 there is no trace that it has been generated by **myTrait**. We will represent trait names with  
58 lower-case names and class/interface names with upper-case names. Traits are just units of  
59 code reuse, and do not induce nominal types.

60 We could have just written **Result=myTrait<Elem=String>**, obtaining

```
61 Result={  
62   Box={String inner}  
63   static method Box merge(Box b,String e){  
64     return Box.of(b.inner().concat(e));}  
65  
66
```

67 Note how in this case, class **Result.Box** would exists. Thanks to our decision of using nested  
68 classes as associated types, the decision of what classes need to be redirected is not made  
69 when the trait is written, but depends on the specific redirect operation. Moreover, our  
70 redirect is not just a way to show the type system that our code is correct, but it can change  
71 the behaviour of code calling static methods from the redirected classes.

72 This example show many of the characteristics of our approach:

- 73 ■ (A) We can redirect mutually recursive nested classes by redirecting them all at the  
74 same time, and if a partial mapping is provided, the system is able to infer the complete  
75 mapping.
- 76 ■ (B) **Box** and **Elem** are just normal nested classes inside of **myTrait**; indeed any nested  
77 class can be redirected away. In case any of their (static) methods was implemented, the  
78 implementation is just discarded. In most other approaches, abstract/associated/generic  
79 types are special and have some restriction; for example, in Java/Scala static methods  
80 and constructors can not be invoked on generic/associated types. With redirect, they are  
81 just normal nested classes, so there are no special restrictions on how they can be used.  
82 In our example, note how **merge** calls **Box.of(..)**.
- 83 ■ (C) While our example language is nominally typed, nested classes are redirected over  
84 types satisfying the same structural shape. We will show how this offers some advantages  
85 of both nominal and structural typing.

86 A variation of redirect, able to only redirect a single nested class, was already presented  
87 in literature. While points (B) and (C) already applies to such redirect, we will show how  
88 supporting (A) greatly improve their value.

89 The formal core of our work is in defining

- 90 ■ **ValidRedirect**, a computable predicate telling if a mapping respect the structural shapes  
91 and nominal subtype relations.
- 92 ■ A formal definition of what properties a procedure expanding a partial mapping into a  
93 complete one should respect.
- 94 ■ **ChoseRedirect**, an efficient algorithm respecting those properties.

95 We first formally define our core language, then we define our redirect operator and its  
96 formal properties. Finally we motivate our model showing how many interesting examples of  
97 generics and associated types can be encoded with redirect. Finally, as an extreme application,  
98 we show how a whole library can be adapted to be injected in a different environment.

## 2 Language grammar and well formedness

$a ::= b \quad c$

$a ::= b \quad c$

$a ::= b \quad c$

## 3 extra

Features: Structural based generics embedded in a nominal type system. Code is Nominal, Reuse is Structural. Static methods support for generics, so generics are not just a trik to make the type system happy but actually change the behaviour Subsume associate types. After the fact generics; redirect is like mixins for generics Mapping is inferred-> very large maps are possible -> application to libraries

In literature, in addition to conventional Java style F-bound polymorphism, there is another way to obtain generics: to use associated types (to specify generic paramaters) and inheritance (to instantiate the paramaters). However, when parametrizing multiple types, the user to specify the full mapping. For example in Java interface  $A<B> B \text{ m}()$ ; interface  $BString \text{ f}()$ ; class  $G<TA \text{ extends } A<TB>, TB> //TA \text{ and } TB \text{ explicitly listed } String \text{ g}(TA \text{ a } TB \text{ b}) \text{return a.m().f}()$ ; class  $MyA \text{ implements } A<MyB>..$  class  $MyB \text{ implements } B ..$   $G<MyA, MyB> //instantiation$  Also scala offers genercs, and could encode the example in the same way, but Scala also offers associated types, allowing to write instead....

Rust also offers generics and associated types, but also support calling static methods over generic and associated types.

We provide here a foundational model for genericity that subsume the power of F-bound polymorphisms and associated types. Moreover, it allows for large sets of generic parameter instantiations to be inferred starting from a much smaller mapping. For example, in our system we could just write  $g = A = \text{method } B \text{ m}() \quad B = \text{method } String \text{ f}() \quad \text{method } String \text{ g}(A \text{ a } B \text{ b}) = a.m().f() \quad MyA = \text{method } MyB \text{ m}() = \text{new } MyB(); .. \quad MyB = \text{method } String \text{ f}() = "Hello"; .. \quad g<A=MyA> //instantiation$ . The mapping  $A=MyA, B=MyB$

We model a minimal calculus with interfaces and final classes, where implementing an interface is the only way to induce subtyping. We will show how supporting subtyping constitute the core technical difficulty in our work, inducing ambiguity in the mappings. As you can see, we base our generic matches the structor of the type instead of respecting a subtype requirement as in F-bound polymorphis. We can easily encode subtype requirements by using implements:  $Print = \text{interface } \text{method } String \text{ print}(); \quad g = A: \text{implements } Print \text{ method } A \text{ printMe}(A \text{ a1}, A \text{ a2}) \text{ if}(a1.print().size() > a2.print.size()) \text{return } a1; \text{return } a2; \quad MyPrint = \text{implements } Print .. \quad g<A=MyPrint> //instantiation \quad g<A=Print> //works too$

————— example showing ordering need to strictly improve EI1: interface  $EA1$ : implements  $EI1$

$EI2$ : interface  $EA2$ : implements  $EI2$

$EB$ :  $EA1 \text{ a1 } EA1 \text{ a1}$

$A1: \quad A2: \quad B: A1 \text{ a1 } A2 \text{ a2 } [B = EB] // \quad A1 \rightarrow EI1, A2 \rightarrow EA2 \text{ a} // \quad A1 \rightarrow EA1, A2 \rightarrow EI2 \text{ b} // \quad A1 \rightarrow EA1, A2 \rightarrow EA2 \text{ c}$

$a \leq b \quad b \leq a \quad c \leq a, b \quad a \leq c$

**hi Hi class**

$a ::= b \quad c$

**aaHiHi class qa**  $a ::= b \quad c$

$a ::= b \quad c$

## 23:4 Using nested classes as associated types.

140  $\}}[(\text{TOP})]$   
 $a \xrightarrow{b} c \quad \forall i < 3a \vdash b : \text{OK}$   
141  $\frac{\forall i < 3a \vdash b : \text{OK}}{1 + 2 \rightarrow 3} \quad \begin{matrix} a \\ b \\ c \end{matrix}$

### 4 Formal

142  $id ::= t \mid C$   
 $T ::= \text{This}n. Cs$   
 $CD ::= C = E$  class declaration  
 $CV ::= C = LV$  evaluated class declaration  
 $D ::= id = E$  declaration  
 $DL ::= id = L$  partially-evaluated-declaration  
 $DV ::= id = LV$  evaluated-declaration  
 $L ::= \text{interface } \{Tz; amtz ; \} \mid \{Tz; Ms ; K?\}$  literal  
 $LV ::= \text{interface } \{Tz; amtz ; \} \mid \{Tz; MVs ; K?\}$  literal value  
 $amt ::= T m(Txs)$  abstract method  
 $mt ::= T m(Txs) e?$  method  
143  $Tx ::= T x$  paramater-declaration  
 $M ::= CD \mid mt$  member  
 $MV ::= CV \mid mt$   
 $Mid ::= C \mid m$  member-id  
 $K ::= \text{constructor}(TxS)$  constructor  
 $e ::= x \mid e.m(es) \mid e.x \mid \text{new } T(es)$  expression  
 $E ::= L \mid t \mid E <+ E \mid E(Cs = T)$  library-expression  
 $\mathcal{E}_V ::= \square \mid \mathcal{E}_V <+ E \mid LV <+ \mathcal{E}_V \mid \mathcal{E}_V(Cs = T)$  context of library-evaluation  
 $\mathcal{E}_v ::= \square \mid \mathcal{E}_v.m(es) \mid v.m(vs \mathcal{E}_v es) \mid \mathcal{E}_v.x \mid \text{new } T(vs \mathcal{E}_v es)$   
 $v ::= \text{new } T(vs)$   
 $p ::= DLs; DVs$  program  
 $S ::= Ds e$  source code

144 We use  $t$  and  $C$  to syntactically distinguish between trait and class names. A type ( $T$ )  
145 has an interesting syntax, see below for what it means. An  $E$  is a top-level class expression,  
146 which can contain class-literals, references to traits, and operations on them, namely our sum  
147  $E <+ E$  and redirect  $e(Cs = T)$ . A declaration  $D$  is just an  $id = E$ , representing that  $id$  is  
148 declared to be the value of  $E$ , we also have  $CD, CV, DL$ , and  $DV$  that constrain the forms  
149 of the LHS and RHS of the declaration. A literal  $L$  has 4 components, an optional interface  
150 keyword, a list of implemented interfaces, a list of members, and an optional constructor.  
151 For simplicity, interfaces can only contain abstract-methods ( $amt$ ) as members, and cannot  
152 have constructors. A member  $M$ , is either an (potentially abstract) method  $mt$  or a nested  
153 class declaration ( $CD$ ). A member value  $MV$ , is a member that has been fully compiled. An  
154  $mid$  is an identifier, identifying a member. Constructors,  $K$ , contain a  $Txs$  indicating the  
155 type and names of fields. An  $e$  is normal fetherweight-java style expression, it has variables

156  $x$ , method calls  $e.m(es)$ , field accesses  $e.x$  and object creation  $newes$ .  $CtxV$  is the evaluation  
 157 context for class-expressions  $E$ , and  $ctxv$  is the usual one for  $e$ 's.

158 An  $S$  represents what the top-level source-code form of our language is, it's just a sequence  
 159 of declarations and a main expression. The most interesting form of the grammar is a  $p$ , it is  
 160 a 'program', used as the context for many reductions and typing rules, on the LHS of the ;  
 161 is a stack representing which (nested) declaration is currently being processed, the bottom  
 162 (rightmost)  $DL$  represents the  $D$  of the source-program that is currently being processed.  
 163 The RHS of the ; represents the top-level declarations that have already been compiled, this  
 164 is necessary to look up top-level classes and traits.

165 To look up the value of a type in the program we will use the notation  $p(T)$ , which is defined  
 166 by the following, but only if the RHS denotes an  $LV$ :

$$\begin{aligned} 167 \quad & (; \_, C=L, \_)(\text{This0}.C.Cs) := L(Cs) \\ & (id=L, p)(\text{This0}.Cs) := L(Cs) \\ 168 \quad & (id=L, p)(\text{This}n+1.Cs) := p(\text{This}n.Cs) \end{aligned}$$

169 To get the relative value of a trait, we define  $p[t]$ :

$$170 \quad (DLs; \_, t=LV, \_)[t] := LV[\text{This}\#DLs]$$

171  
 172 To get the value of a literal, in a way that can be understood from the current location  
 173 ( $\text{This0}$ ), we define:

$$174 \quad p[T] := p(T)[T]$$

175  
 176 And a few simple auxiliary definitions:

$$\begin{aligned} & Ts \in p := \forall T \in Ts \bullet p(T) \text{ is defined} \\ & L(\emptyset) := L \\ 177 \quad & L(C.Cs) := L(Cs) \text{ where } L = \text{interface?} \{ \_, \_, C=L, \_, \_ \} \\ & L[C=E'] := \text{interface?} \{ Tz; MVs C=E' Ms; K? \} \\ 178 \quad & \text{where } L = \text{interface?} \{ Tz; MVs C=\_ Ms; K? \} \end{aligned}$$

## 23:6 Using nested classes as associated types.

We have two-top level reduction rules defining our language, of the form  $Dse^{\sim\sim} > Ds'e$  which simply reduces the source-code. The first rule (*compile*) ‘compiles’ each top-level declaration (using a well-typed subset of already compiled top-level declarations), this reduces the defining expression. The second rule, (*main*) is executed once all the top-level declarations have compiled (i.e. are now fully evaluated class literals), it typechecks the top-level declarations and the main expression, and then proceeds to reduce it. In principle only one-typechecking is needed, but we repeat it to avoid declaring more rules.

```

179 Define Ds e --> Ds' e'
180 =====
181 DVs' |- Ok
182 empty; DVs'; id | E --> E'
183 (compile)----- DVs' subsetof DVs
184 DVs id = E Ds e --> DVs id = E' Ds e
185
186 DVs |- Ok
187 DVs |- e : T
188 DVs |- e --> e'
189 (main)----- for some type T
190 DVs e --> DVs e'

```

### 5 Compilation

Aside from the redirect operation itself, compilation is the most interesting part, it is defined by a reduction arrow  $p; id | E \rightarrow E'$ , the *id* represents the id of the type/trait that we are currently compiling, it is needed since it will be the name of *This0*, and we use that fact that that is equal to *This1.id* to compare types for equality. The (*CtxV*) rule is the standard context, the (*L*) rule propagates compilation inside of nested-classes, (*trait*) merely evaluates a trait reference to its defined body, (*sum*) and (*redirect*) perform our two meta-operations.

```

205 Define p; id | E --> E'
206 =====
207 p; id | E --> E'
208 (CtxV) -----
209 p; id | CtxV[E] --> CtxV[E']
210
211 id = L[C = E], p; C | E --> E'
212 (L) ----- // TODO use fresh C?
213 p; id | L[C = E] --> L[C = E']
214
215 (trait) -----
216 p; id | t -> p[t]
217
218 LV1 <+p' LV2 = LV3 p' = C' = LV3, p
219 (sum) ----- for fresh C'
220 p; id | LV1 <+ LV2 --> LV3
221
222 // TODO: Inline and de-42 redirect formalism
223 (redirect) -----LV'=redirect(p, LV, Cs, P)
224 p; id | LV(Cs=P) -> LV'

```

## 6 The Sum operation

The sum operation is defined by the rule  $L1 < +p L2 = L3$ , it is unconventional as it assumes we already have the result ( $L3$ ), and simply checks that it is indeed correct. We believe (but have not proved) that this rule is unambiguous, if  $L1 < +p L2 = L3$  and  $L1 < +p L2 = L3'$ , then  $L3 = L3'$  (since the order of members does not matter for  $Ls$ ).

The main rule for summing of non-interfaces, sums the members, unions the implemented interfaces (and uses *minimize* to remove any duplicates), it also ensures that at most one of them has a constructor. For summing an interface with a interface/class we require that an interface cannot 'gain' members due to a sum. The actual L42 implementation is far less restrictive, but requires complicated rules to ensure soundness, due to problems that could arise if a summed nested-interface is implemented. Summing of traits/classes with state is a non-trivial problem and not the focus of our paper, there are many prior works on this topic, and our full L42 language simply uses ordinary methods to represent state, however this would take too much effort to explain here.

```
Define L1 <+p L2 = L3
```

```
=====
```

```
{Tz1; Mz1; K?1} <+p {Tz2; Mz2; K?2} = {Tz; Mz; K?}
```

```
Tz = p.minimize(Tz1 U Tz2)
```

```
Mz1 <+p Mz1 = Mz
```

```
{empty, K?1, K?2} = {empty, K?} //may be too sophisticated?
```

```
interface{Tz1; amtz,amtz';} <+p interface?{Tz2;amtz;} = interface {Tz;amtz,amtz';}
```

```
Tz = p.minimize(Tz1 U Tz2)
```

```
if interface? = interface then amtz'=empty
```

The rules for summing members are simple, we take two sets of members collect all the ones with unique names, and sum those with duplicates. To sum nested classes we merely sum their bodies, to sum two methods we require their signatures to be identical, if they both have bodies, the result has the body of the RHS, otherwise the result has the body (if present) of the LHS.

```
Define Mz <+p Mz' = Mz"
```

```
-----
```

```
M, Mz <+p M', Mz' = M <+p M', Mz <+p Mz
```

```
//note: only defined when M.Mid = M'.Mid
```

```
Mz <+p Mz' = Mz, Mz':
```

```
dom(Mz) disjoint dom(Mz')
```

```
Define M <+p M' = M"
```

```
-----
```

```
T' m(Txs') e? <+p T m(Txs) e = T m(Txs) e
```

```
T', Txs'.Ts =p Ts, Txs
```

```
T' m(Txs') e? <+p T m(Txs) = T m(Txs) e?
```

```
T', Txs'.Ts =p Ts, Txs
```

```
(C = L) <+p (C = L') = L <+p.push(C) L'
```

## 271 7 Type System

272 The type system is split into two parts: type checking programs and class literals, and the  
 273 typechecking of expressions. The latter part is mostly conventional, it involves typing judgments  
 274 of the form  $p; Txs \vdash e : T$ , with the usual program  $p$  and variable environment  $Txs$  (often  
 275 called  $\Gamma$  in the literature). rule  $(Dsok)$  type checks a sequence of top-level declarations by  
 276 simply push each declaration onto a program and typecheck the resulting program. Rule  $pok$   
 277 typechecks a program by check the topmost class literal: we type check each of it's members  
 278 (including all nested classes), check that it properly implements each interface it claims to,  
 279 does something weird, and finanly check check that it's constructor only referenced existing  
 280 types,

```

281
282
283 Define p |- Ok
284 =====
285
286 D1; Ds |- Ok ... Dn; Ds|- Ok
287 (Ds ok) ----- Ds = D1 ... Dn
288 Ds |- Ok
289
290 p |- M1 : Ok .... p |- Mn : Ok
291 p |- P1 : Implemented .... p |- Pn : Implemented
292 p |- implements(Pz; Ms) /*WTF?*/ if K? = K: p.exists(K.Txs.Ts)
293 (p ok) ----- p.top() = interface? {P1...Pn; M1, ..., Mn
294 p |- Ok
295
296 p.minimize(Pz) subseteq p.minimize(p.top().Pz)
297 amt1 _ in p.top().Ms ... amtn _ in p.top().Ms
298 (P implemented) ----- p[P] = interface {Pz; amt1 ..
299 p |- P : Implemented
300
301 (amt-ok) ----- p.exists(T, Txs.Ts)
302 p |- T m(Tcs) : Ok
303
304 p; This0 this, Txs |- e : T
305 (mt-ok) ----- p.exists(T, Txs.Ts)
306 p |- T m(Tcs) e : Ok
307
308 C = L, p |- Ok
309 (cd-Ok) -----
310 p |- C = L : OK
311

```

312 Rule  $(Pimplemented)$  checks that an interface is properly implemented by the program-  
 313 top, we simply check that it declares that it implements every one of the interfaces super-  
 314 interfaces and methods. Rules  $(amt - ok)$  and  $(mt - ok)$  are straightforward, they both  
 315 check that types mentioned in the method signature exist, and ofcourse for the latter case,  
 316 that the body respects this signature.



317 To typecheck a nested class declaration, we simply push it onto the program and typecheck  
 318 the top-of the program as before.

319 The expression typesystem is mostly straightforward and similar to feartherwiegth Java,  
 320 notable we we use  $p[T]$  to look up information about types, as it properly ‘from’s paths, and  
 321 use a classes constructor definitions to determine the types of fields.

```

322 Define p; Txs |- e : T
323 =====
324 (var)
325 ----- T x in Txs
326 p; Txs |- x : T
327
328 (call)
329 p; Txs |- e0 : T0
330 ...
331 p; Txs |- en : Tn
332 ----- T' m(T1 x1 ... Tn xn) _ in p[T0].Ms
333 p; Txs |- e0.m(e1 ... en) : T'
334
335 (field)
336 p; Txs |- e : T
337 ----- p[T].K = constructor(_ T' x _)
338 p; Txs |- e.x : T'
339
340
341 (new)
342 p; Txs |- e1 : T1 ... p; Txs |- en : Tn
343 ----- p[T].K = constructor(T1 x1 ... Tn xn)
344 p; Txs |- new T(e1 ... en)
345
346
347 (sub)
348 p; Txs |- e : T
349 ----- T' in p[T].Pz
350 p; Txs |- e : T'
351
352
353 (equiv)
354 p; Txs |- e : T
355 ----- T =p T'
356 p; Txs |- e : T'
357
358 - towel1:.. //Map: towel2:.. //Map: lib: T:towel1 f1 ... fn
359   MyProgram: T:towel2 Lib:lib[T=This0.T] ... -

```

359 ——— References ———