

Technische Universität München

BGCE Project: CAD – Integrated Topology Optimization

BGCE Final Milestone Meeting

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S. Reiz, B. R  th, E. Wannerberg, A. Yurova

February 29, 2016



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6.1 Peters' scheme

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7. Summary & Outlook

CAD issues

Problem:

- The Engineer designer pendulum

Desired:

⇒ One click optimization

CAD issues

Problem:

- The Engineer designer pendulum
- Top-Opt algorithms are a one way street

Desired:

- ⇒ One click optimization
- ⇒ A full circle optimization process

CAD issues

Problem:

- The Engineer designer pendulum
- Top-Opt algorithms are a one way street
- Exotic input file types

Desired:

- ⇒ One click optimization
- ⇒ A full circle optimization process
- ⇒ Standardized input files

What they get

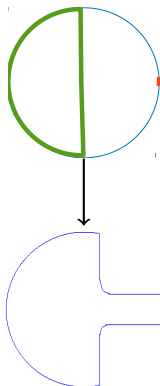
- One-step solution process
- Full 3-D optimization via Finite Elements
- Production-ready output geometry

DEMO

Scalability and Performance

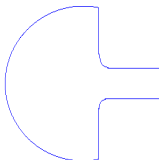
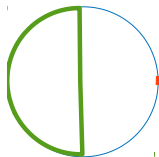
Overview: Workflow

What the user sees



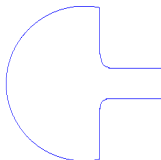
Overview: Workflow

CAD design including specification of loads and fixtures



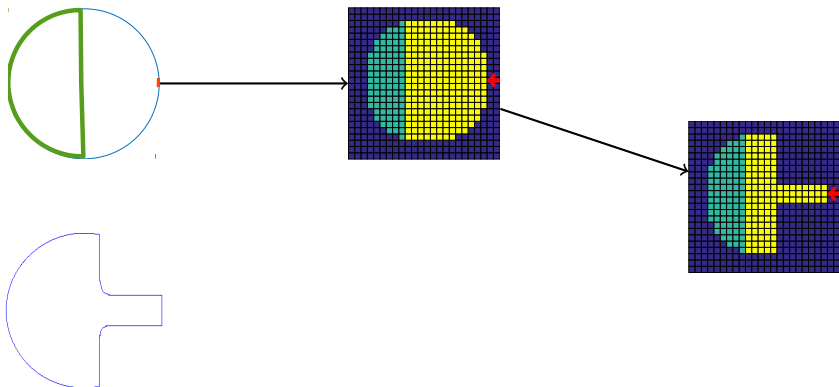
Overview: Workflow

Voxelized topology



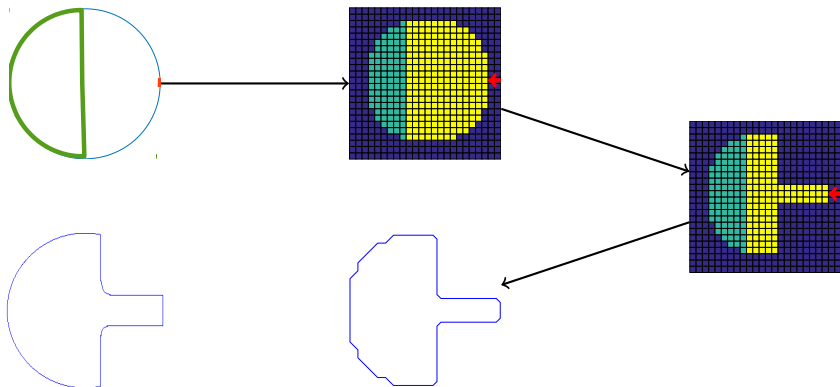
Overview: Workflow

Optimized topology



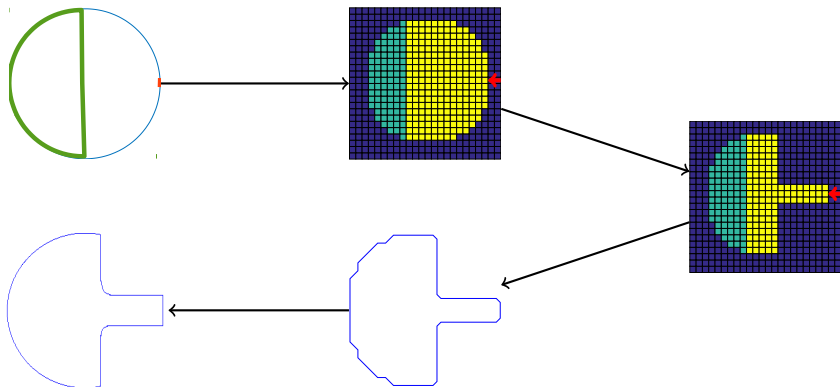
Overview: Workflow

Surface extraction



Overview: Workflow

Fit B-Spline surface



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Status

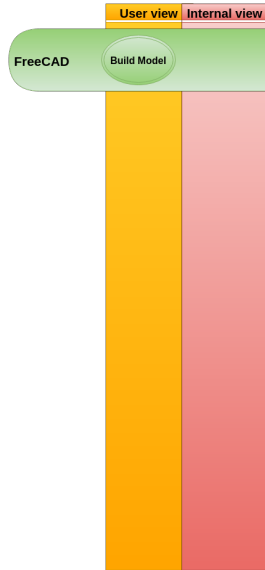
Last milestone

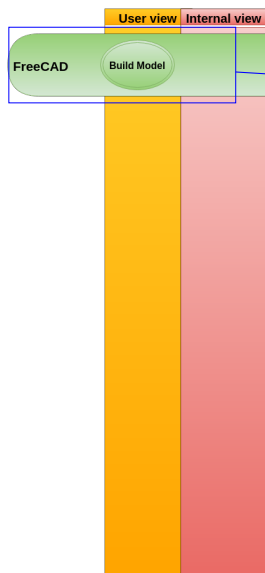
- ✓ Manual voxelization using CVMLCPP
- ✓ "Hard coded" script for ToPy input
- ✓ Topology optimized geometry using ToPy
- ✗ Recognition of boundary conditions

Today

- ✓ Voxelization with OpenCascade
- ✓ Extraction of loads, fixtures and active elements through colouring
- ✓ Automatic "one click" pipeline to surface reconstruction

User view	Internal view





- Model geometry in your favorite CAD tool
- Colour faces for boundary conditions
 - Red** Fixture
 - Green** Active
 - RGB** RGB value in $[0 \leq R < 255, 0 \leq G < 255, 0 \leq B < 255]$ for load vector
- Save model as STEP with Colours and IGES with Colours

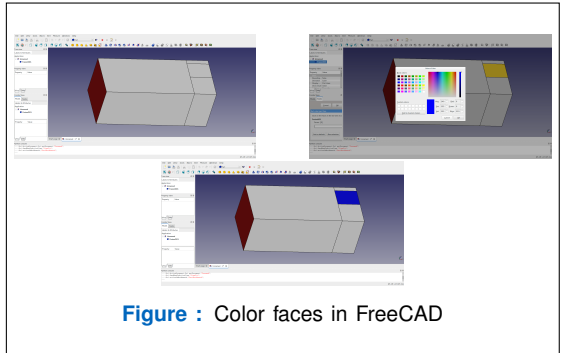
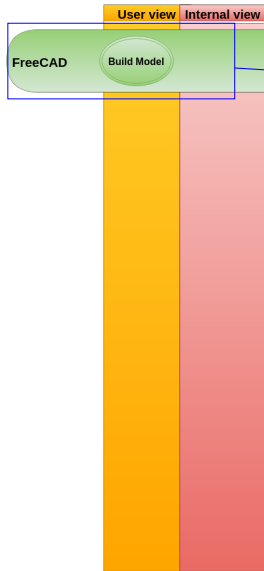
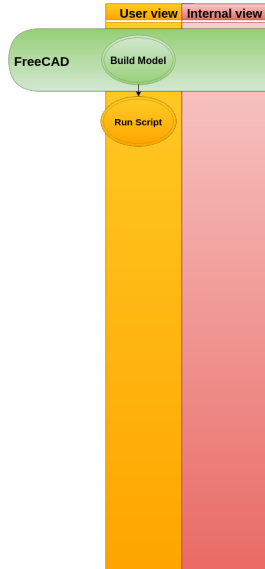
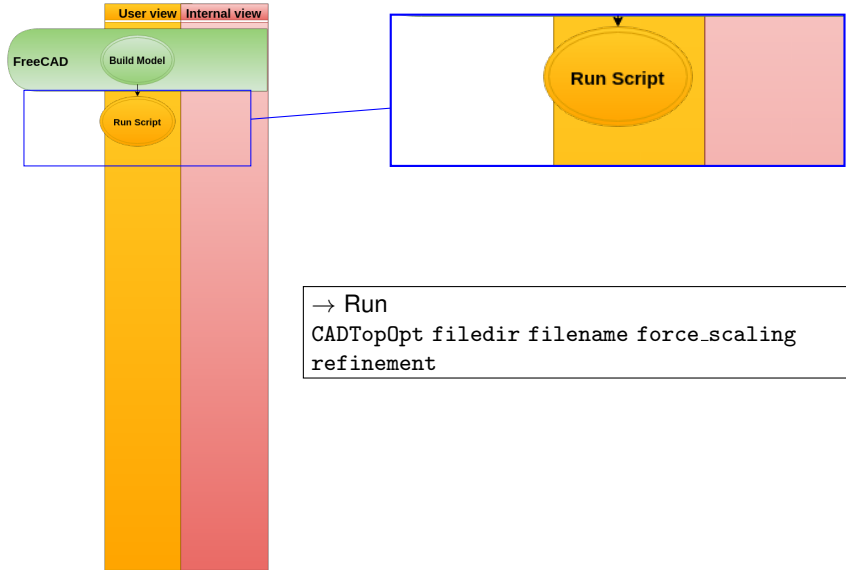
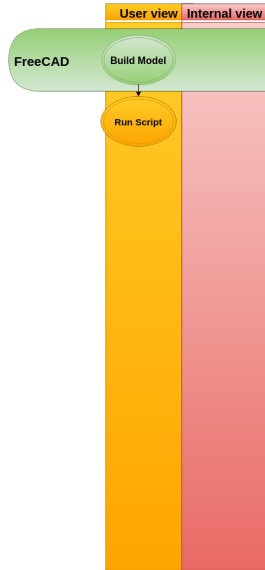
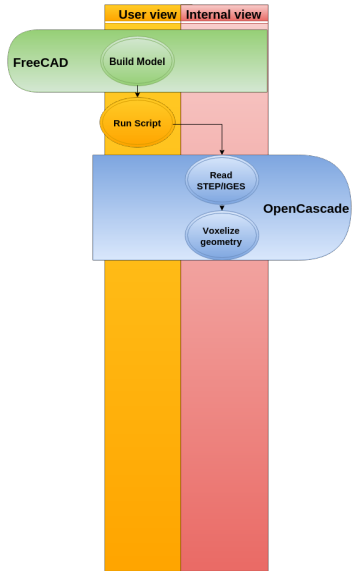


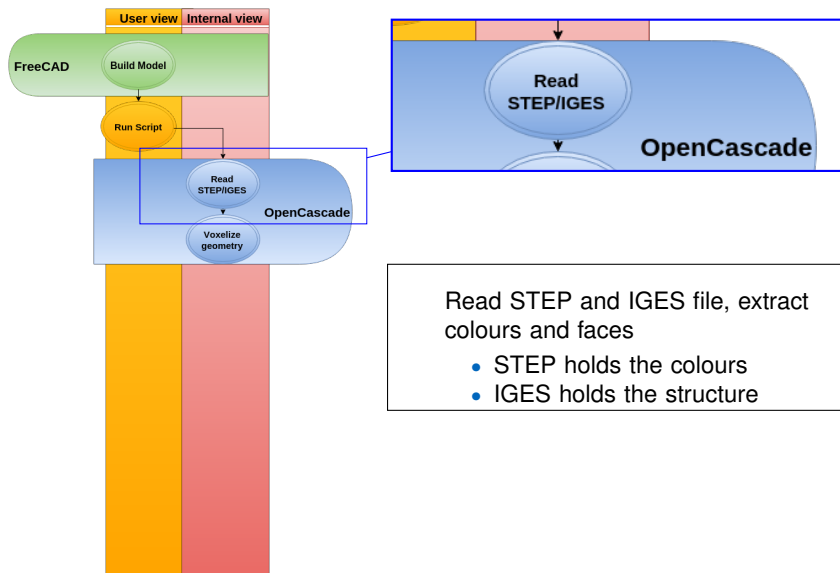
Figure : Color faces in FreeCAD

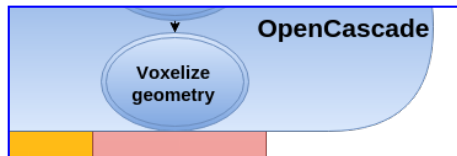
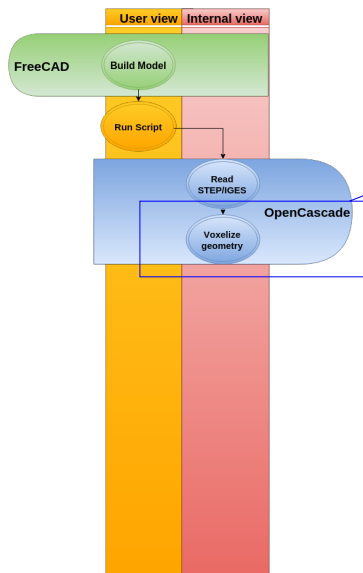












Voxelize faces using OpenCascade

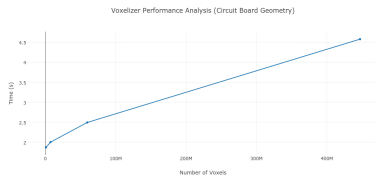
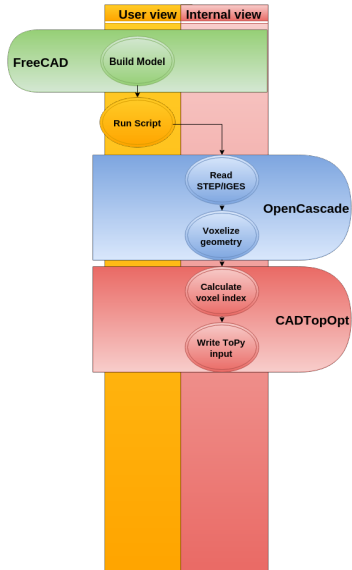
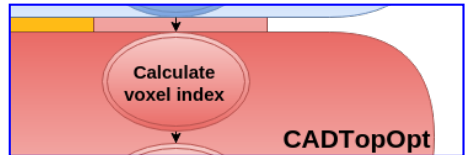
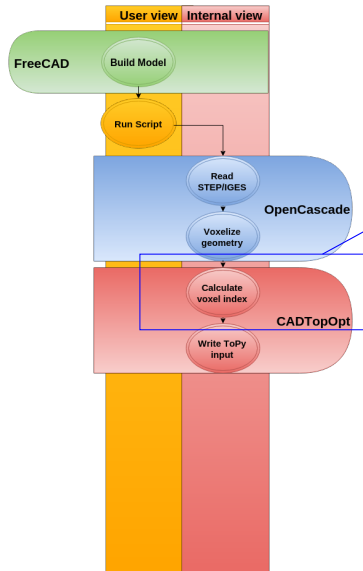


Figure : Scaling of voxelizer



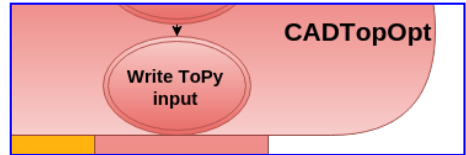


Different indexing for elements and nodes in ToPy

```
# =====
# === Discretisation of the design domain ===
# =====
# 2D: Y      3D: Y
# |          |
# +---X      +---X
#
#           Z
#
# 1---5---9
# | 1 | 5 |
# 2---6---10
# | 2 | 6 |
# 3---7---11
# | 3 | 7 |
# 4---8---12
#
```

Figure : Indexing in ToPy [1]

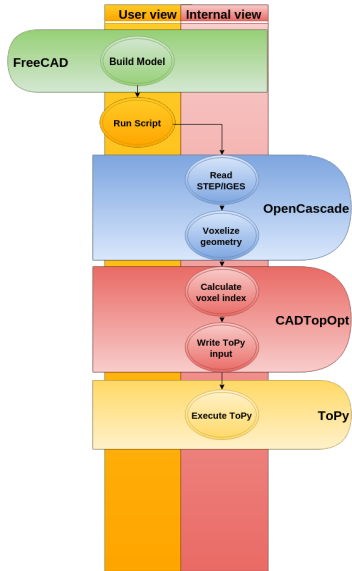
5.1. Internal structure

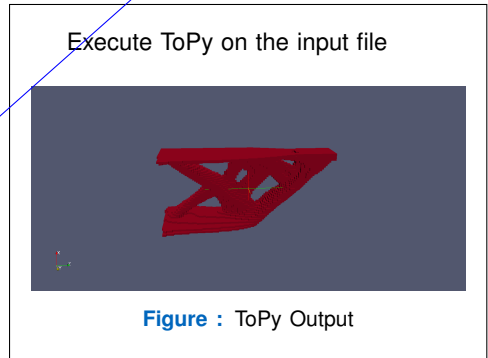
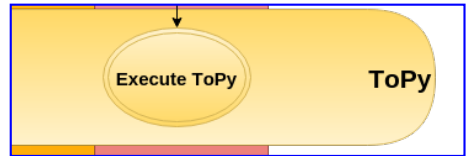
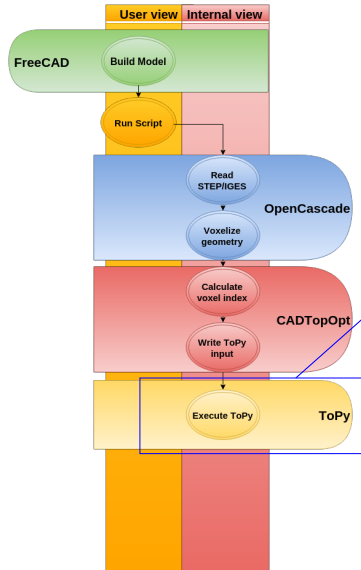


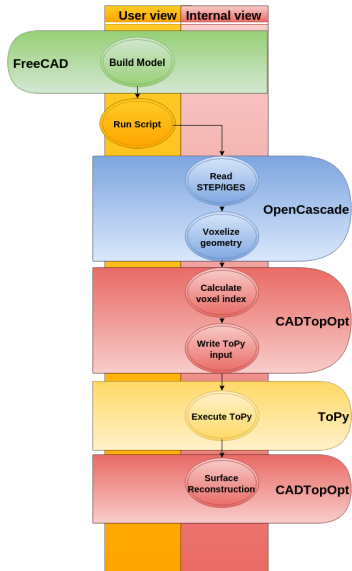
Each voxel index is specifically written

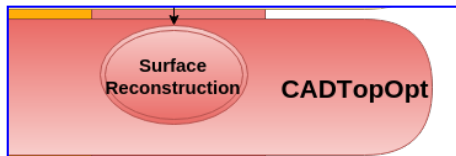
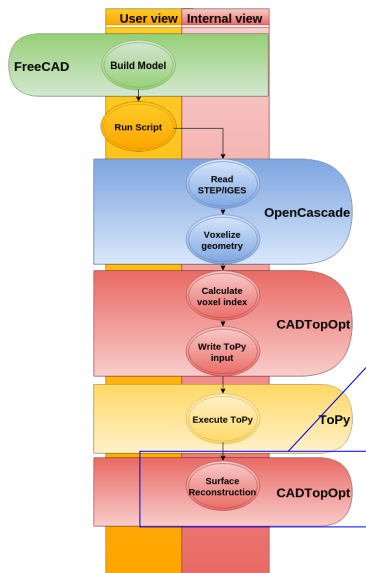
[illegible]

Figure : Script for ToPy









Run dual contouring algorithm

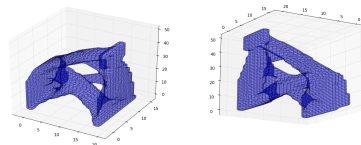
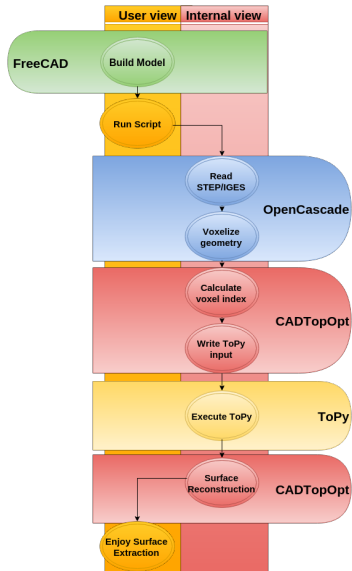
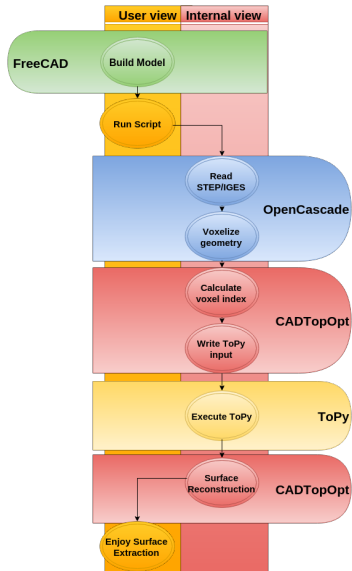
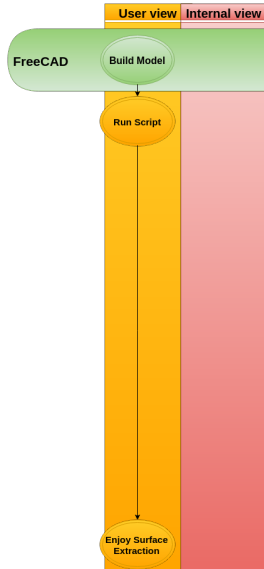


Figure : Surface extraction for Cantilever





But what does the user see?



But what does the user see?

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 - 6.1 Peters' scheme
 - 6.2 Fitting pipeline
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Status

Last milestone

- 🕒 Surface reconstruction with the VTK Toolbox

Today

- ✓ Extraction of voxel data from Topy
- ✓ 3D Dual Contouring implementation
- ✓ Coarsening and non-manifold edge treatment
- ✓ Projection of datapoints onto quads and respective parametrization
- 🕒 Interface to NURBS

From Voxel to Mesh Geometry

- Extract isosurface from voxel information
- Algorithms: Marching Cubes, Dual Contouring, Extended Models
- Problems with VTK's Marching Cube implementation

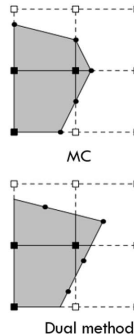
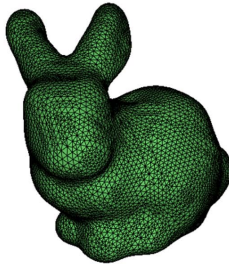
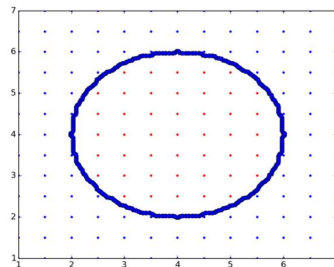
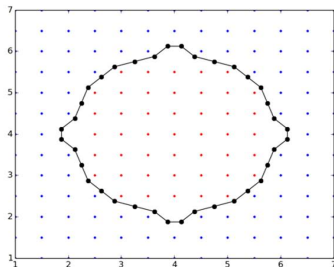


Figure : From [4],[5]

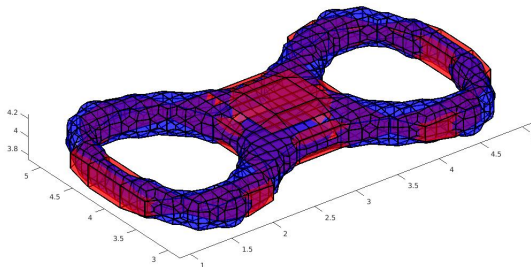
Dual Contouring

- Python implementation — Use of powerful libraries, including VTK
- Output: Closed surface made out of *quads*
- Coarsening is needed for surface fitting algorithms



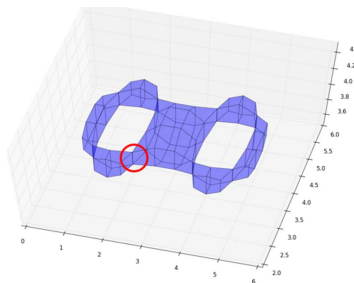
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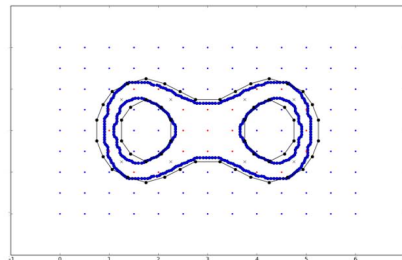
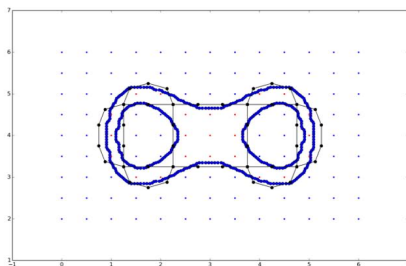
Dual Contouring — Problems

- **Non-manifold edges** appear
- One edge can only belong to two quads for the surface to be closed
- Special treatments in the implementation to avoid them



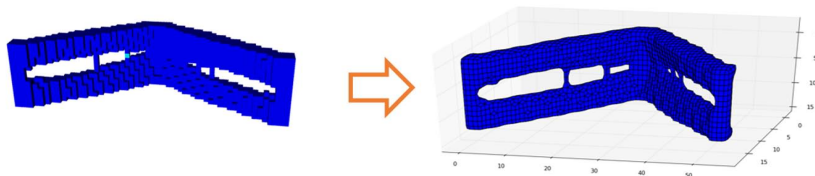
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Dual Contouring — Input

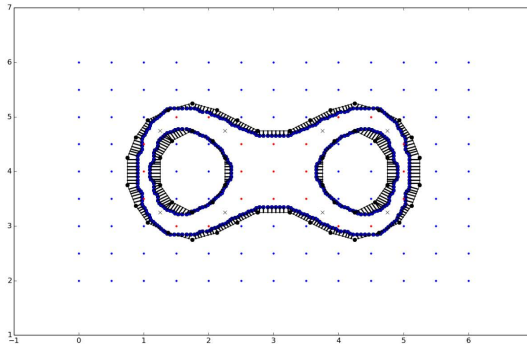
- Interface between Topology Optimization and Surface Extraction
- Special implementation to use voxel data from ToPy as input



Demo

Projection and Parametrization

- Points from finer grid are projected to quads of the coarser grid
- Parameters u and v are found for each quad
- This information is needed for the algorithms in the last part of the pipeline



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B-Spline

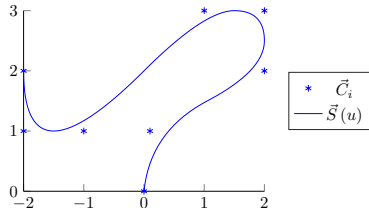
$$\vec{S}(u, v) = \sum_{i,j=1}^{n,m} \vec{C}_{i,j} N_i^p(u) N_j^p(v),$$

where p – degree of the B-Spline surface and n, m – number of control points in each direction.

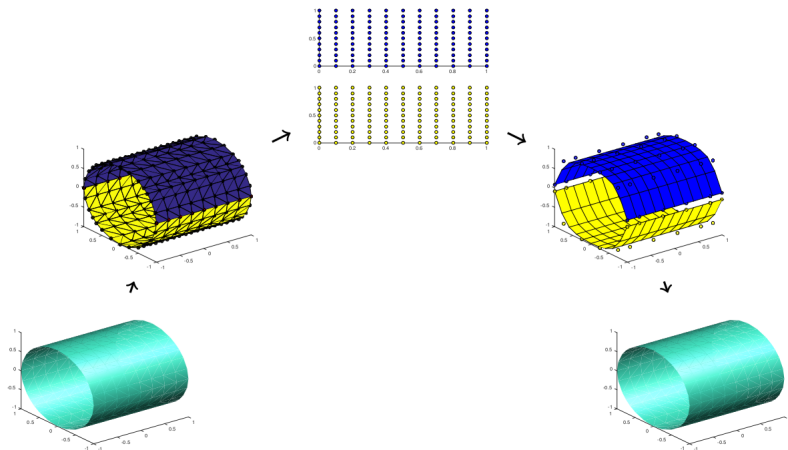
B-Splines

- offer great flexibility for handling arbitrary shapes
- are CAD-standard

Engineers are working with CAD



B-Spline Fitting Pipeline [2]



Status

Last milestone

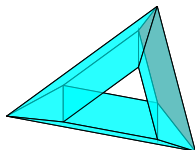
- ✗ Automatic patch selection
- ✗ Parametrization of obtained patches
- ✓ B-spline fitting using least squares
- 🕒 Smooth connection of patches
- ✗ Conversion back to CAD

Today

- ✓ Automatic patch selection – moved to the surface extraction part
- ✓ Parametrization of obtained patches – moved to the surface extraction part
- ✓ B-spline fitting using least squares – modified
- ✓ Smooth connection of patches
- ✗ Conversion back to CAD

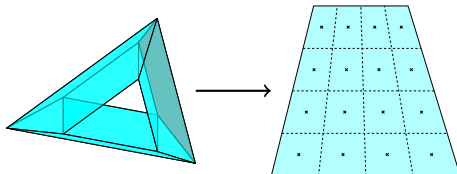
Long way to smoothness – Peter's scheme

Control mesh



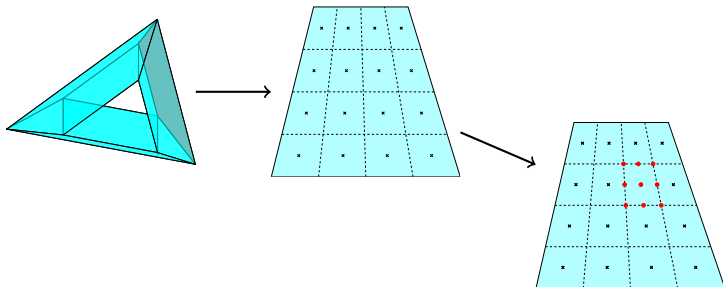
Long way to smoothness – Peter's scheme

Refined control mesh



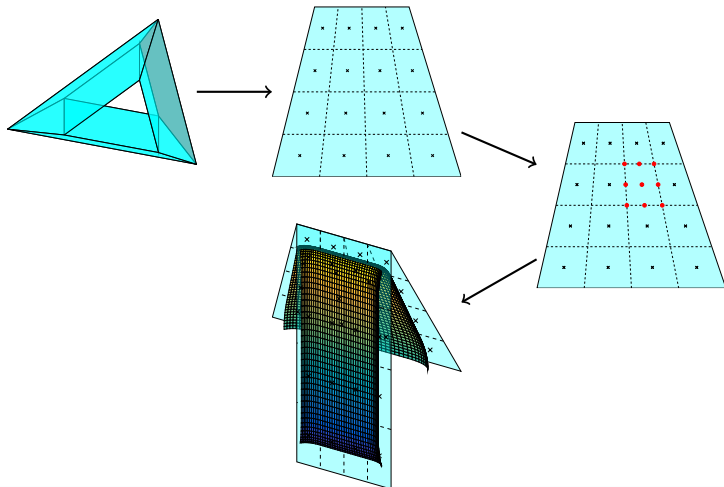
Long way to smoothness – Peter's scheme

Bezier control points



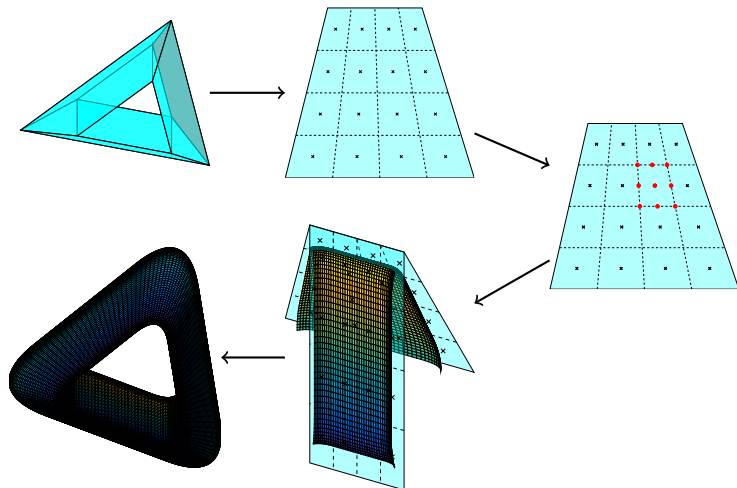
Long way to smoothness – Peter's scheme

B-Spline patch



Long way to smoothness – Peter's scheme

Peters' surface



Long way to smoothness

Main ideas

- Use the mesh obtained from Dual Contouring as a *control mesh*
- Modify the fitting step to take advantage of the **Peters' scheme**

$$\downarrow$$
$$E_{dist}(V_x) = \sum_{i=1}^N \| P_i - y_i V_x \|_2^2 \rightarrow \min,$$

y_i - coefficients obtained from the Peters' scheme theory.

Long way to smoothness

Main ideas

- Use the mesh obtained from Dual Contouring as a *control mesh*
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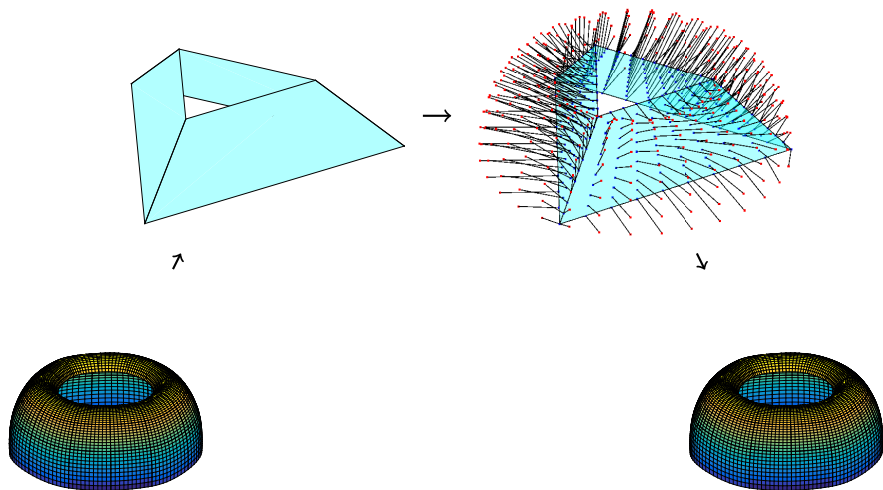
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What is achieved?

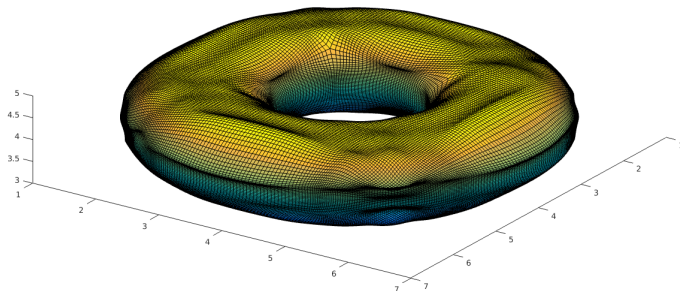
- Smoothness of the fitted surface is now guaranteed by construction
- Fitting of more complex shapes achieved

Improved pipeline[3]



Possible optimizations

- Introduction of the *fairness functional* in order to deal with more complex shapes
- Implementation of the *adaptive refinement* in order to control a maximum error tolerance
- Implementation of the *parameter correction* for the improved pipeline



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What is done? What is next?

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 - ✓ Pipeline from CAD model to optimized voxel model
 - ✓ User input of boundary conditions
 - ⌚ Support for complex geometries
 - ✗ GUI for user interaction

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 - ⌚ Interfaces
 - ✗ Adaptive and topology safe Dual Contouring

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 - ✓ B-spline fitting using least squares
 - ✓ Smooth connection of patches using Peters' scheme
 - ✗ Conversion back to CAD

Remaining questions

Python

- ⊖ First part of the pipeline is in C++
- ⊕ Second part of the pipeline is now in Python
- ⊕ Easy to port from the original MATLAB prototypes

C++

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- ⊖ Cumbersome to implement

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ToPy Problem

- ⊕ Current implementation is using ToPy

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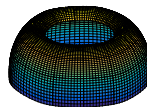
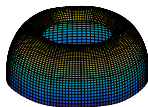
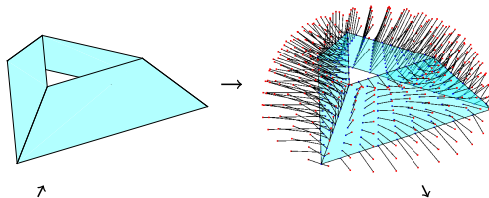
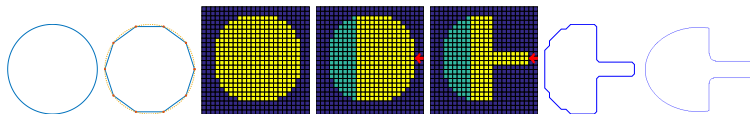
C++

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- ⊖ Second part of the pipeline is now in Python
- ⊖ Cumbersome to implement

ToPy Problem

- ⊕ Current implementation is using ToPy
- ⊖ ToPy is not available any more!

Thank you for your attention!



Literature

1. **William Hunter.** "Predominantly solid-void three-dimensional topology optimisation using open source software"
2. **Gerrit Becker, Michael Schäfer, Antony Jameson.** "An advanced NURBS fitting procedure for post-processing of grid-based shape optimizations"
3. **Matthias Eck, Hugues Hoppe.** "Automatic Reconstruction of B-Spline Surfaces of Arbitrary Topological Type"
4. **Greg Turk, Marc Levoy** "Stanford Bunny"
5. **Tao Ju, Frank Losasso, Scott Schaefer, Joe Warren.** "Dual contouring of hermite data"

Projection and Parametrization on arbitrary quads

1. find least squares plane approximating quad

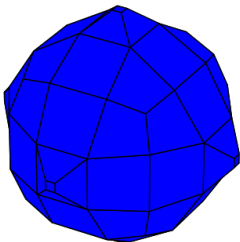


Figure : DC sphere

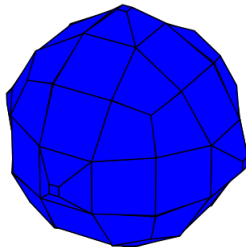
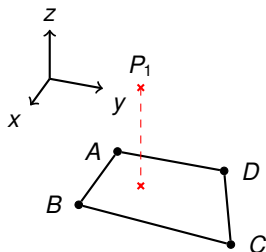


Figure : with plane quads

Projection and Parametrization on arbitrary quads

1. find least squares plane approximating quad
2. projection of datapoint onto plane



Coordinate transformation

system with basis

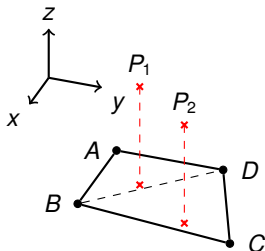
$$B_{BAD} = \begin{pmatrix} \vec{n} & \vec{AB} & \vec{AD} \end{pmatrix}$$

yields

$$(B_{BAD})^{-1} P_1 = \begin{pmatrix} d & u & v \end{pmatrix}^T$$

Projection and Parametrization on arbitrary quads

1. find least squares plane approximating quad
2. projection of datapoint onto plane
3. find corresponding parameters $[u, v] \in [0, 1]^2$



Problem:

- ✓ for $P_1: (u, v) = (0.5, 0.4)$
- ✗ for $P_2: (u, v) = (1, 1)$

Solution:

1. if we get $u + v > 1$
2. use B_{BCD} instead of B_{BAD}
3. set $u = 1 - u, v = 1 - v$