Yield Curve Premia

Brooks & Moskowitz (2017)

Gustavo Amarante

Carry, momentum and value provide rich description of bond return premia

- Subsume information from the yield curve's first three principal components, macroeconomic data and Cochrane and Piazzesi (2005, CP) factor
- Describes both the cross-section and time-series of yield curve premia across different countries
- Provide new economic intuition for what drives bond return premia
- Connects to return predictability in other asset classes, suggesting a unifying asset pricing framework

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- International Bond Data and Yield Curves
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Outline: International Bond Data and Yield Curves

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International Bond Data and Yield Curves

Zero Coupon Yields

- Australia, Germany, Canada, Japan, Sweden, UK and US.
- Maturities from 1 to 30 years
- Sources:
 - Wright (2011): From Dec 1971 to May 2009
 - Reuters (DSFI): From June 2009 to Mar 2016

Portfolios

- Level: 10-year
- Slope: Long 10-year, Short 2-year, duration neutral
- Butterfly: Long 5-year, short equal-duration weighted average of 2- and 10-year

Synthetic Returns

Quarterly annualized log returns in excess of the 3-month yield.

Principal Components

• Computed using the full sample





Returns



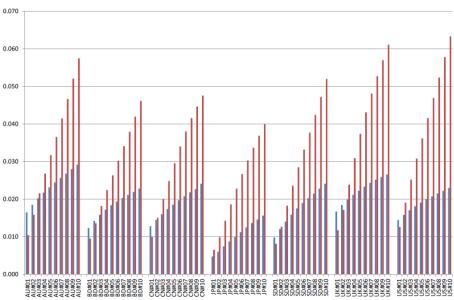
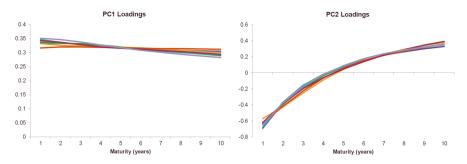
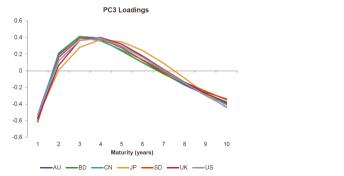


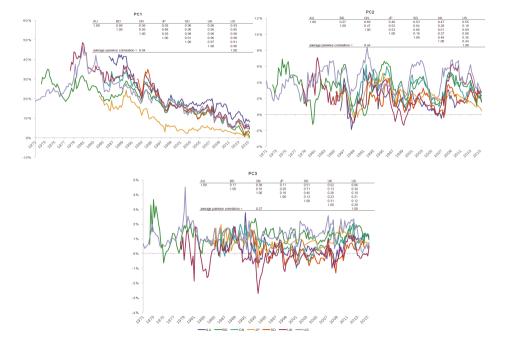
Table I: First Three Principal Components of Yields and Level, Slope, and Curvature Portfolios Across Countries

Panel A reports the fraction of the covariance matrix of yields across 1 to 10 year maturity zero coupon bonds in each country explained by each of the first three principal components, as well as the total amount of covariation explained by all three principal components. Panel B reports the correlation between the first principal component, PC1, and the yield on the "level" portfolio (10-year bond) for each country, the correlation between the second principal component, PC2, and the yield on the "slope" portfolio (10-year minus 2-year bond) in each country, and the correlation between the third principal component, PC3, and the yield on the curvature or butterfly portfolio (5-year minus an average of 10- and 2-year bonds) in each country.

AU	BD	CN	JP	SD	UK	US	Avg.					
	Pan	el A: Perce	ent of Cova	ariation Ca	ptured by I	PCs						
97.6%	95.4%	96.7%	96.6%	97.8%	96.7%	96.8%	96.8%					
1.9%	3.8%	2.5%	2.9%	1.6%	2.7%	2.7%	2.6%					
0.4%	0.5%	0.4%	0.4%	0.4%	0.4%	0.4%	0.4%					
99.9%	99.7%	99.7%	99.9%	99.9%	99.8%	99.9%	99.8%					
Panel B: Correlation between PC and Level, Slope, and Butterfly Portfolios												
1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00					
0.98	0.96	0.92	0.98	0.98	0.91	0.84	0.94					
0.81	0.73	0.73	0.89	0.96	0.98	0.84	0.85					
	97.6% 1.9% 0.4% 99.9% Panel 1.00 0.98	Pan 97.6% 95.4% 1.9% 3.8% 0.4% 0.5% 99.9% 99.7% Panel B: Correlat 1.00 1.00 0.98 0.96	Panel A: Perconstruction 97.6% 95.4% 96.7% 1.9% 3.8% 2.5% 0.4% 0.5% 0.4% 99.9% 99.7% 99.7% Panel B: Correlation between 1.00 1.00 1.00 0.98 0.96 0.92	Panel A: Percent of Cova 97.6% 95.4% 96.7% 96.6% 1.9% 3.8% 2.5% 2.9% 0.4% 0.5% 0.4% 0.4% 99.9% 99.7% 99.7% 99.9% Panel B: Correlation between PC and 1.00 1.00 1.00 1.00 0.98 0.96 0.92 0.98	Panel A: Percent of Covariation Car 97.6% 95.4% 96.7% 96.6% 97.8% 1.9% 3.8% 2.5% 2.9% 1.6% 0.4% 0.5% 0.4% 0.4% 0.4% 99.9% 99.7% 99.7% 99.9% 99.9% Panel B: Correlation between PC and Level, Slope 1.00 1.00 1.00 1.00 0.98 0.96 0.92 0.98 0.98	Panel A: Percent of Covariation Captured by I 97.6% 95.4% 96.7% 96.6% 97.8% 96.7% 1.9% 3.8% 2.5% 2.9% 1.6% 2.7% 0.4% 0.5% 0.4% 0.4% 0.4% 0.4% 99.9% 99.7% 99.9% 99.9% 99.8% Panel B: Correlation between PC and Level, Slope, and But 1.00 1.00 1.00 1.00 1.00 0.98 0.96 0.92 0.98 0.98 0.91	Panel A: Percent of Covariation Captured by PCs 97.6% 95.4% 96.7% 96.6% 97.8% 96.7% 96.8% 1.9% 3.8% 2.5% 2.9% 1.6% 2.7% 2.7% 0.4% 0.5% 0.4% 0.4% 0.4% 0.4% 0.4% 99.9% 99.7% 99.9% 99.9% 99.8% 99.9% Panel B: Correlation between PC and Level, Slope, and Butterfly Port 1.00 1.00 1.00 1.00 1.00 0.98 0.96 0.92 0.98 0.98 0.91 0.84					







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Cross Section of the Level Portfolio Returns

$$\textit{rx}_{t+1}^{\textit{Level}} = \textit{B'PC}_t + \textit{S'}\left[\textit{Carry}_t \; \textit{Mom}_t \; \textit{Val}_t\right] + \textit{TimeFE} + \varepsilon_{t+1}$$

$$ext{Carry}_t = y_t^{10y} - y_t^{3m} \ ext{Mom}_t = ret_{t-12,t-1}^{10y} \ ext{Val}_t = y_t^{10y} - ext{E}_t \left(\pi_{t+1,t+10}
ight)$$

Cross Section of the Level Portfolio Returns

					Panel A:	Excess retu	ırns of cou	ntry levels				
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)
PC1	0.089					0.039	0.075	0.111	0.029	0.063	0.099	0.055
	(2.63)					(1.05)	(2.37)	(3.01)	(0.85)	(1.65)	(2.79)	(1.49)
PC2	0.254					0.226	0.286	0.015	0.250	0.031	0.024	0.027
	(2.42)					(2.17)	(2.70)	(0.08)	(2.44)	(0.18)	(0.15)	(0.16)
PC3	-0.066					-0.044	-0.084	-0.228	-0.062	-0.174	-0.258	-0.207
	(-0.31)					(-0.21)	(-0.43)	(-0.90)	(-0.32)	(-0.71)	(-1.15)	(-0.93
Carry	, ,			0.246	0.304		, ,	0.333	, ,	0.279	0.367	0.318
				(2.11)	(2.64)			(1.75)		(1.55)	(1.93)	(1.70)
Mom			-0.001		-0.021		-0.013		-0.019		-0.015	-0.019
			(-0.03)		(-0.98)		(-0.63)		(-0.92)		(-0.74)	(-0.91
Val		0.525			0.498	0.439			0.466	0.380		0.401
		(3.56)			(3.72)	(2.61)			(3.12)	(2.45)		(2.88)
R ² after F.E.	3.2%	3.7%	0.0%	1.0%	5.3%	5.1%	3.2%	3.9%	5.4%	5.6%	4.1%	6.1%
p -value of nest	ed F-test v	ersus (1)				(0.000)	(0.499)	(0.000)	(0.000)	(0.000)	(0.001)	(0.000)

Cross Section of the Slope Portfolio Returns

$$\textit{rx}_{t+1}^{\textit{Slope}} = \textit{B'PC}_t + \textit{S'}\left[\textit{Carry}_t \; \textit{Mom}_t \; \textit{Val}_t\right] + \textit{TimeFE} + \varepsilon_{t+1}$$

$$\begin{aligned} & \textit{Carry}_{t} = \frac{D}{10} \left(y_{t}^{10y} - y_{t}^{3m} \right) - \frac{D}{2} \left(y_{t}^{2y} - y_{t}^{3m} \right) \\ & \textit{Mom}_{t} = \frac{D}{10} \left(\textit{ret}_{t-12,t-1}^{10y} \right) - \frac{D}{2} \left(\textit{ret}_{t-12,t-1}^{2y} \right) \\ & \textit{Val}_{t} = \left(y_{t}^{10y} - \textit{E}_{t} \left(\pi_{t+1,t+10} \right) \right) - \left(y_{t}^{2y} - \textit{E}_{t} \left(\pi_{t+1,t+2} \right) \right) \end{aligned}$$

Cross Section of the Slope Portfolio Returns

					Panel B:	Excess retu	rns of cou	ntry slopes	5			
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)
PC1	0.026					0.077	0.029	-0.014	0.068	0.019	-0.004	0.019
	(0.87)					(2.35)	(0.93)	(-0.49)	(2.11)	(0.64)	(-0.14)	(0.62)
PC2	0.205					-0.634	0.172	0.354	-0.574	-0.072	0.227	-0.109
	(1.89)					(-3.00)	(1.36)	(3.37)	(-2.79)	(-0.33)	(1.91)	(-0.49
PC3	0.069					-0.370	0.061	0.265	-0.310	0.003	0.169	-0.018
	(0.26)					(-1.38)	(0.22)	(1.11)	(-1.14)	(0.01)	(0.68)	(-0.07)
Carry	, ,			0.265	0.277		` /	0.292	, ,	0.259	0.307	0.269
-				(5.52)	(6.21)			(6.07)		(5.49)	(6.10)	(5.51)
Mom			-0.027		-0.036		-0.009		0.004		-0.053	-0.036
			(-1.18)		(-1.54)		(-0.37)		(0.15)		(-2.17)	(-1.49
Val		0.620			0.533	1.828	` ′		1.712	0.843		0.756
		(2.86)			(2.43)	(3.73)			(3.56)	(1.79)		(1.60)
R ² after F.E.	0.9%	1.9%	0.3%	9.5%	10.4%	3.7%	0.9%	11.7%	3.3%	11.2%	11.7%	10.4%
p -value of nest	$\operatorname{ed} F$ -test v	ersus (1)				(0.000)	(0.938)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000

Cross Section of the Butterfly Portfolio Returns

$$rx_{t+1}^{Fly} = B'PC_t + S'[Carry_t Mom_t Val_t] + TimeFE + \varepsilon_{t+1}$$

$$\begin{aligned} & \textit{Carry}_t = \frac{D}{5} \left(y_t^{5y} - y_t^{3m} \right) - \frac{1}{2} \sum_{n \in \{2,10\}} \frac{D}{n} \left(y_t^{ny} - y_t^{3m} \right) \\ & \textit{Mom}_t = \frac{D}{5} \left(\textit{ret}_{t-12,t-1}^{5y} \right) - \frac{1}{2} \sum_{n \in \{2,10\}} \frac{D}{n} \left(\textit{ret}_{t-12,t-1}^{ny} \right) \\ & \textit{Val}_t = \left(y_t^{5y} - E_t \left(\pi_{t+1,t+5} \right) \right) - \frac{1}{2} \sum_{n \in \{2,10\}} \left(y_t^{ny} - E_t \left(\pi_{t+1,t+n} \right) \right) \end{aligned}$$

Cross Section of the Butterfly Portfolio Returns

				Panel	C: Exces	s returns o	f country k	outterfly sp	oreads			
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)
PC1	0.003					-0.001	0.005	-0.005	-0.002	-0.006	0.000	-0.003
	(0.35)					(-0.11)	(0.55)	(-0.51)	(-0.26)	(-0.69)	(-0.02)	(-0.39)
PC2	0.042					-0.056	0.047	0.024	-0.052	-0.072	0.018	-0.051
	(1.03)					(-1.30)	(1.13)	(0.63)	(-1.17)	(-1.69)	(0.47)	(-1.12
PC3	0.414					-0.025	0.381	0.353	-0.025	-0.068	0.250	-0.031
	(3.02)					(-0.20)	(2.99)	(3.00)	(-0.19)	(-0.59)	(2.75)	(-0.25)
Carry				0.336	0.320			0.298		0.280	0.378	0.319
-				(3.63)	(3.07)			(4.10)		(3.62)	(4.02)	(3.12)
Mom			-0.061		-0.033		-0.029		0.042		-0.088	-0.026
			(-1.66)		(-0.91)		(-0.99)		(1.41)		(-2.47)	(-0.63
Val		2.973			2.207	3.096			3.316	2.922		2.417
		(4.29)			(4.78)	(4.55)			(4.87)	(4.61)		(3.49)
R ² after F.E.	6.3%	11.4%	1.2%	7.6%	16.1%	11.8%	6.5%	11.9%	11.7%	16.5%	14.4%	16.5%
p -value of nest	ed F-test v	ersus (1)				(0.000)	(0.082)	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)

Time Variation in Yield Curve Premia

The same study is done using country fixed effects:

$$rx_{t+1}^{portfolio} = B'PC_t + S'[Carry_t Mom_t Val_t] + CountryFE + \varepsilon_{t+1}$$

- Results are roughly the same:
 - Time variation in country level returns appears to be related to the first two PCs, but even more strongly related to carry and value, which subsumes pricing information from the PCs.
 - Factors that drive the cross-section of expected yield curve returns also capture time-variation in expected returns

Outline: Spanned and Unspenned Sources of Returns

- International Bond Data and Yield Curves
- Cross-Section and Time-Series of Yield Curve Premia
- Spanned and Unspenned Sources of Returns
 - How Are Styles Related to Yield Principal Components?
 - Are Styles Related to Information in Past Yields?
 - Unspanned Macro Factors
 - Cochrane and Piazzesi Factor
- Tradeable Bond Portfolios

The style characteristics capture cross-sectional and time-series pricing information from the PCs (which fully characterize the yield curve) and have **additional** predictive power.

What is the nature of this additional information?

How Are Styles Related to Yield Principal Components?

Factor PC1 PC2 PC3 R2 PC1 PC2 PC3 R2 Paul A: Level of yield curve PC3			Time Fixe	ed Effects			Country Fi	xed Effects	
Carry	Factor	PC1			R^2	PC1			R^2
Carry Carr				Par	nel A: Leve	el of yield c	nve		
Mom -0.12 1.36 1.16 8.9% -0.30 2.41 -0.71 14.9% Val (-2.06) (7.09) (3.89) (-3.54) (6.84) (-0.78) (-0.78) Val 0.10 0.06 -0.03 17.7% 0.14 0.24 0.84 44.9% Farel B: Slope of yield curve Farel B: Slope of yield curve Carry 0.14 -0.51 -0.66 6.8% 0.05 -0.33 -3.57 29.4% Mom 0.08 -2.27 -1.78 25.5% 0.00 -3.13 -4.23 40.7% Val -0.03 0.45 0.25 82.8% -0.03 0.55 0.17 96.3% Val -0.03 0.45 0.25 82.8% -0.03 0.55 0.17 96.3% Val -0.03 0.05 0.21 5.2% 0.01 0.12 -0.37 10.3% Carry 0.03 0.06 0.21 5.2%	Carry	-0.07	0.72	0.48	59.3%	-0.05	0.80	1.13	75.1%
Val		(-6.17)	(28.24)	(7.47)		(-10.97)	(35.98)	(10.71)	
Val	Mom	-0.12	1.36	1.16	8.9%	-0.30	2.41	-0.71	14.9%
Carry 0.14 -0.51 -0.66 6.8% 0.05 -0.33 -3.57 29.4%		(-2.06)	(7.09)	(3.89)		(-3.54)	(6.84)	(-0.78)	
Carry 0.14 -0.51 -0.66 6.8% 0.05 -0.33 -3.57 29.4% (2.96) (-4.43) (-2.27) 0.05 -0.05 -0.33 -3.57 29.4% (3.96) (-4.43) (-2.27) 0.05 -0.00 -3.13 -4.23 40.7% (1.82) (-12.46) (-5.75) 0.00 -3.13 -4.23 40.7% (1.82) (-12.46) (-5.75) 0.00 -14.26) (-8.13) (-13.57) (58.47) (15.50) 0.05 (-14.26) (-14.26) 0.03 0.45 0.25 82.8% 0.03 0.55 0.17 96.3% (1.357) (58.47) (15.50) (-36.71) (167.71) (13.63) (1.50) 0.05 (-2.34) (2.17) (2.65) 0.01 0.12 -0.37 10.3% (1.354) 0.00 0.03 0.26 83.8% 0.00 0.03 0.245 (1.316) 0.3% (1.348) 0.36 0.36 0.36 0.36 0.36 0.36 0.36 0.36	Val	0.10	0.06	-0.03	17.7%	0.14	0.24	0.84	44.9%
Carry 0.14 -0.51 -0.66 6.8% 0.05 -0.33 -3.57 29.4% Mom 0.08 -2.27 -1.78 25.5% 0.00 -3.13 -4.23 40.7% Val -0.30 0.45 0.25 82.8% -0.03 0.55 0.17 96.3% Val -1.357 (58.47) (15.50) -6.3671) (167.71) (13.63) Carry 0.03 0.06 0.21 5.2% 0.01 0.12 -0.37 10.3% (2.34) (2.17) (2.65) -(2.48) (4.90) (-3.11) Mom 0.04 -0.07 -0.78 7.4% -0.01 0.13 -2.45 40.8% Val 0.00 0.03 0.14 55.2% 0.00 0.03 0.25 83.6% 0.00 0.03 0.25 83.6% 0.00 0.03 0.25 83.6% 0.00 0.03 0.25 83.6% 0.00 0.03 0.245 (17.78) Val 0.00 0.03 0.05 0.21 5.2% 0.01 0.12 -0.37 10.3% 0.05 0.05 0.05 0.05 0.05 0.05 0.05 0.0		(8.16)	(1.73)	(-0.55)		(11.87)	(6.12)	(5.71)	
Mom				Par	nel B: Slop	e of yield c	nve		
Mom 0.08 -2.27 -1.78 25.5% 0.00 -3.13 -4.23 40.7% Val (1.82) (-12.46) (-5.75) (0.05) (-14.26) (-81.3) Val -0.03 0.45 0.25 82.8% -0.03 0.55 0.17 96.3% Panel C: Curvature of yield curve Carry 0.03 0.06 0.21 5.2% 0.01 0.12 -0.37 10.3% Carry 0.03 0.06 0.21 5.2% 0.01 0.12 -0.37 10.3% Mom 0.04 -0.07 -0.78 7.4% -0.01 0.13 -2.45 40.8% Val 0.00 0.03 0.14 55.2% 0.00 0.03 0.245 (:1.77.8)	Carry	0.14	-0.51	-0.66	6.8%	0.05	-0.33	-3.57	29.4%
Val		(2.96)	(-4.43)	(-2.27)		(2.57)	(-3.52)	(-8.06)	
Val	Mom	0.08	-2.27	-1.78	25.5%	0.00	-3.13	-4.23	40.7%
Carry 0.03 0.06 0.21 5.2% 0.01 0.12 -0.37 10.3% Mom 0.04 -0.07 -0.78 7.4% -0.01 0.13 -2.45 40.8% (2.48) (1.10) (-6.38) (-1.39) (2.45) (-1.78) (2.45) (-1.78) (2.48) (-1.10) (-6.38) (-1.39) (2.45) (-1.78) (-1.78) (2.48) (-1.00) 0.03 0.14 55.2% 0.00 0.03 0.22 83.6% (3.57) (58.47) (15.77) (13.63) (13.67) (13.63) (3.67) (13.67) (13.67) (13.63) (13.67) (13.67) (13.63) (4.90) (-2.45) (-2.45) (-2.45) (-1.78) (-2.45) (-1.78)		(1.82)	(-12.46)	(-5.75)		(0.05)	(-14.26)	(-8.13)	
Carry 0.03 0.06 0.21 5.2% 0.01 0.12 -0.37 10.3% (2.34) (2.17) (2.65) (2.48) (4.90) (-3.11) (4.90) (2.48) (4.90) (-3.11) (4.90) (2.48) (4.90) (-3.12) (2.48) (4.90) (-3.13) (2.48) (4.10) (-6.38) (-1.39) (2.45) (-1.78) (2.48) (-1.10) (-6.38) (-1.39) (2.45) (-1.78) (2.48) (-1.90) (0.03) 0.22 (83.6%)	Val	-0.03	0.45	0.25	82.8%	-0.03	0.55	0.17	96.3%
Carry 0.03 0.06 0.21 5.2% 0.01 0.12 -0.37 10.3% (2.34) (2.17) (2.65) (2.48) (4.90) (-3.11) (Mom 0.04 -0.07 -0.78 7.4% -0.01 0.13 -2.45 40.8% (2.48) (4.10) (-6.38) (-1.39) (2.45) (-1.78) (2.45) (0.00 0.03 0.14 55.2% 0.00 0.03 0.22 83.6%		(-13.57)	(58.47)	(15.50)		(-36.71)	(167.71)	(13.63)	
(2.34) (2.17) (2.65) (2.48) (4.90) (-3.11) (2.48) (4.90) (-3.11) (2.48) (4.90) (-3.11) (2.48) (-1.10) (-6.38) (-1.39) (2.45) (-1.78) (2.45) (2.45) (-1.78) (2.45) (2.45) (-1.78) (2.45) (2.45) (-1.78) (2.45)				Panel	C: Curvat	ure of yield	curve		
Mom 0.04 -0.07 -0.78 7.4% -0.01 0.13 -2.45 40.8% (2.48) (-1.10) (-6.38) (-1.39) (2.45) (-17.78) Val 0.00 0.03 0.14 55.2% 0.00 0.03 0.22 83.6%	Carry	0.03	0.06	0.21	5.2%	0.01	0.12	-0.37	10.3%
Mom 0.04 -0.07 -0.78 7.4% -0.01 0.13 -2.45 40.8% (2.48) (-1.10) (-6.38) (-1.39) (2.45) (-1.78) (17.78) (Val 0.00 0.03 0.14 55.2% 0.00 0.03 0.22 83.6%		(2.34)	(2.17)	(2.65)		(2.48)	(4.90)	(-3.11)	
Val 0.00 0.03 0.14 55.2% 0.00 0.03 0.22 83.6%	Mom	0.04			7.4%	-0.01	0.13		40.8%
Val 0.00 0.03 0.14 (55.2%) 0.00 0.03 0.22 83.6%		(2.48)	(-1.10)	(-6.38)		(-1.39)	(2.45)	(-17.78)	
(0.11) (10.21) (26.74) (13.85) (12.57) (37.45)	Val	0.00	0.03	0.14	55.2%	0.00	0.03	0.22	83.6%
		(0.11)	(10.21)	(26.74)		(13.85)	(12.57)	(37.45)	

Styles are related to the PCs but are not fully captured by them and add incremental explanatory power for returns.

One possible explanation is that the PCs indicate how yields are today, but not how rates have **recently changed** or how they compare to a **fundamental anchor**.

Are Styles Related to Information in Past Yields?

		Panel A	: PCs from	ı lagged yi	eld curves			Panel	B: Moving	averge of	PCs from	lagged yield	curves
	Level P	ortfolios	Slope P	ortfolios	Curvature	Portfolios		Level P	ortfolios	Slope P	ortfolios	Curvature	Portfolios
PC1	0.22 (2.59)	0.30 (1.34)	0.11 (1.40)	0.23 (2.98)	0.03 (1.23)	0.05 (2.20)	PC1	0.40 (2.82)	0.47 (2.69)	0.23 (1.58)	0.34 (2.46)	-0.01 (-0.12)	0.02 (0.44)
$PC1_{t-l}$	-0.12 (-1.40)	-0.17 (-0.75)	-0.14 (-1.64)	-0.19 (-2.19)	-0.01 (-0.26)	-0.02 (-0.98)	$PC1_{MA(Iyear)}$	-0.23 (-1.37)	-0.23 (-1.21)	-0.21 (-1.30)	-0.23 (-1.52)	0.05 (0.97)	0.03 (0.66)
PC1 _{t-5}	-0.04 (-0.82)	-0.09 (-1.69)	0.02 (0.36)	0.00 (0.06)	-0.04 (-2.17)	-0.04 (-2.58)	PC1 _{MA(5year)}	-0.12 (-1.64)	-0.21 (-2.76)	-0.04 (-0.79)	-0.06 (-1.26)	-0.06 (-2.51)	-0.07 (-3.14)
PC2	0.29 (1.85)	-0.05 (-0.23)	0.34 (2.39)	-0.39 (-1.03)	0.01 (0.26)	-0.11 (-2.07)	PC2	-0.06 (-0.21)	-0.30 (-1.04)	0.62	-0.31 (-0.78)	0.06 (0.65)	-0.11 (-1.11)
PC2 _{t-1}	0.06 (0.39)	0.01 (0.03)	-0.14 (-1.18)	0.13 (0.45)	0.04 (0.88)	0.09 (1.83)	$PC2_{MA(Iyear)}$	0.57	0.41 (1.42)	-0.45 (-1.32)	-0.16 (-0.41)	-0.06 (-0.52)	0.04 (0.36)
PC2 _{t-5}	0.01 (0.05)	0.03	-0.05 (-0.55)	0.04 (0.37)	0.02 (0.52)	0.04 (1.25)	$PC2_{MA(5year)}$	-0.17 (-1.32)	-0.13 (-0.98)	0.09	0.27 (1.68)	0.03 (0.65)	0.07 (1.59)
PC3	-0.001 (-0.002)	-0.32 (-1.06)	-0.31 (-0.92)	-0.46 (-1.43)	(3.55)	-0.05 (-0.45)	PC3	-0.447 (-0.925)	-0.74 (-1.55)	-0.23 (-0.32)	-0.36 (-0.54)	0.82	0.25 (1.36)
PC3 _{t-l}	0.06 (0.23)	0.15 (0.58)	0.35	0.30 (1.29)	-0.08 (-1.05)	0.04 (0.32)	PC3 _{MA(Iyear)}	0.40 (0.73)	0.33	0.01 (0.02)	-0.07 (-0.11)	-0.44 (-2.21)	-0.28 (-1.49)
PC3 _{t-5}	0.04	0.22	0.49	0.46	-0.04 (-0.49)	-0.01 (-0.18)	PC3 _{MA(5year)}	0.25	0.60	0.93	0.84	-0.15 (-1.43)	-0.03 (-0.30)
Сапту		0.49		0.22 (2.64)		0.35	Сапу		0.48		0.21 (2.98)		0.32
Mom		0.03 (0.42)		-0.02 (-0.38)		0.01 (0.16)	Mom		0.03 (0.95)		-0.01 (-0.24)		0.02 (0.58)
Val		0.40 (2.40)		1.35		2.61 (4.48)	Val		0.41 (2.51)		1.58		2.40 (3.95)
R ² p-value	4.3%	7.8% (0.089)	3.2%	9.0% (0.003)	7.3%	16.7% (0.000)	R ² p-value	5.9%	9.5% (0.000)	3.2%	9.4% (0.003)	9.6%	17.5% (0.000)

Styles maintain their predictive power even in the presence of lagged yield information.

Carry and Value remain statistically significant and with similar magnitudes as estimated before.

Other Unspanned Factors

Macroeconomic Data

- Source: Consensus Economics (starting in 1990)
- Expected inflation
- Expected output growth (industrial production)

Cochrane-Piazzesi Factor

- Tent-shaped linear combination of forward rates
- Can predict returns across maturities
- Not spanned by the first three principal components of the yield curve

Panel A: Level Panel B: Slope Panel C: Curvature (2) (2) (2) (3) -0.050 -0.100 0.004 0.067 -0.032 -0.033 -0.014 Growth -0.010 0.010 (-0.14)(-0.75)(-1.48)(0.18)(0.08)(1.18)(-1.61)(-1.60)(-0.62)-0.260 -0.071 -0.010 0.022 Inflation -0.0350.018 -0.019 -0.0040.068 (-0.40)(-2.74)(-1.32)(0.24)(-0.20)(-0.11)(0.77)(-0.16)(2.54)PC1 0.140 0.083 0.024 0.013 0.002 -0.017 (3.82)(2.06)(0.69)(0.38)(0.17)(-1.69)PC2 0.244 -0.012 0.190 -0.055 0.046 -0.059 (2.34)(-0.07)(1.75)(-0.25)(-1.30)PC3 -0.058 -0.245 0.079 0.021 0.416 -0.071

0.01%

(0.30)

0.82%

(0.065)

vs (1)

(0.08)

0.279

(5.48)

-0.038

(-1.58)

0.645

(1.41)

10.67%

(0.000)

vs (2)

Macro factors have no predictive power at explaining slope and curvature returns with or without the PCs.

Carry and Value continue to capture significant positive return premia

0.04%

(-0.27)

4.32%

(0.000)

vs (1)

(-1.07)

0.367

(1.94)

-0.021

(-1.02)

0.357

(2.35)

6.57%

(0.000)

vs (2)

Macro Factors

Carry

Mom

Val

R2

p-value of nested F-test

0.58%

(2.99)

6.69%

(0.000)

vs (1)

(-0.57)

0.313

(3.04)

-0.025 (-0.62)

2.710

(3.87)

17.30%

(0.000)

vs (2)

Cochrane-Piazzesi Factor

Dependent variable = 10-year bond excess return, rx_{t+1} (10)

CP	1.53	1.82	0.90	1.69	1.27	0.71	0.52
	(5.22)	(2.09)	(1.04)	(1.83)	(1.29)	(1.37)	(0.48)
PC1		-0.08	-0.16	-0.09	0.03		-0.14
		(-0.55)	(-1.11)	(-0.62)	(0.20)		(-0.73)
PC2		-0.26	0.71	0.27	-0.38		1.24
		(-0.23)	(0.62)	(0.22)	(-0.34)		(1.03)
PC3		-0.45	0.53	-0.05	-0.30		1.01
		(-0.29)	(0.32)	(-0.03)	(-0.19)		(0.58)
Val			1.30			0.95	1.36
			(2.70)			(2.05)	(2.49)
Mom				-0.17		-0.16	-0.19
				(-2.30)		(-2.38)	(-2.68)
Carry					0.95	1.34	0.37
					(1.25)	(1.91)	(0.41)
Intercept	-1.98%	-1.39%	-1.63%	-0.88%	-1.63%	-1.60%	-0.96%
_	(-1.48)	(-0.67)	(-0.78)	(-0.42)	(-0.78)	(-1.03)	(-0.45)
R^2	12.25%	12.50%	16.21%	16.51%	13.03%	19.23%	20.18%

A simple value metric prices bonds better the CP factor or PCs.

Outline: Tradeable Bond Portfolios

- International Bond Data and Yield Curves
- Cross-Section and Time-Series of Yield Curve Premis
- Spanned and Unspenned Sources of Returns
- Tradeable Bond Portfolios
 - Style Performance
 - Style Factors in Other Asset Classes

Tradeable Bond Portfolios

Style Performance

Tradeable Bond Universe

- Source: JP Morgan Government Bond Index (GBI)
- Country-Maturity Partitions: 1-5 years, 5-10 years and 10-30 years.

Country Porfolios

- Level: Equal-Duration across the partitions
- Slope: Level-neutral, duration-weighted
- Butterfly: Zero-duration, minimal slope exposure

Combined Portfolio

- Same definitions of carry, momentum and value as before
- Countries are ranked by the style and weighted as

$$w_t = \frac{rank (style) - avg (rank)}{std (rank)}$$

 Multi-style/single-dimension and single-style/multi-dimension, scaled to have equal vol contributions to a 10% vol portfolio (in sample)

			Panel	D: Multi-di	mension return	s			
	Value	Momentum	Carry	Multi-style		PC1	PC2	PC3	Combo
Average	6.14%	2.11%	8.07%	9.67%		-0.29%	1.90%	0.13%	0.73%
Stdev	6.5%	6.2%	7.4%	7.3%		5.3%	5.4%	6.9%	5.7%
t-stat	4.4	1.6	5.0	6.1		-0.2	1.6	0.1	0.6
Sharpe	0.95	0.34	1.09	1.32		-0.05	0.35	0.02	0.13
Correl to market	0.08	0.17	0.15	0.22		0.03	0.25	0.07	0.17
Alpha to market	5.65%	1.03%	6.95%	8.05%		-0.45%	0.52%	-0.37%	-0.24%
t-stat	3.8	0.7	4.2	5.0		-0.4	0.4	-0.2	-0.2
Info ratio	0.87	0.17	0.95	1.13		-0.08	0.10	-0.05	-0.04
Skewness	1.34	0.03	1.62	2.71		-0.48	0.67	0.35	-1.19
Kurtosis	7.3	3.5	14.2	21.7		5.5	4.9	11.1	13.9
Autocorrelation	-0.05	0.01	0.03	0.02		-0.10	-0.17	-0.06	-0.19
Beta to PC1	0.21	-0.27	-0.32	-0.22	Beta to Carry	-0.34	-0.05	0.25	-0.16
	(3.89)	(-4.57)	(-5.50)	(-3.69)		(-5.68)	(-0.76)	(3.88)	(-2.75)
Beta to PC2	0.39	-0.02	0.08	0.22	Beta to Mom	-0.13	0.08	-0.21	-0.15
	(7.11)	(-0.28)	(1.42)	(3.76)		(-2.07)	(1.33)	(-3.24)	(-2.52)
Beta to PC3	0.23	-0.18	0.24	0.17	Beta to Val	0.29	0.45	0.16	0.45
	(4.33)	(-3.08)	(4.19)	(2.87)		(4.79)	(7.20)	(2.44)	(7.65)
Alpha to PCs	8.20%	3.35%	10.38%	12.29%	Alpha to Styles	0.84%	-0.53%	-3.26%	-0.77%
	(4.38)	(1.62)	(5.14)	(5.95)		(0.40)	(-0.25)	(-1.49)	(-0.38)

Tradeable Bond universe Style Factors in Other Asset Classes

Style factors provide a direct connection to asset pricing factors used in other asset classes. The efficacy and consistency of the concepts of carry, momentum and value in pricing an array of diverse assets suggests a unifying framework for pricing assets generally.

<u> </u>		Panel	A: Value			
	EQ value	FX value	Com value	Mkt-rf	Alpha	Marginal R ²
Level value	0.28	0.23	-0.01	0.46	0.33%	13.0%
	(4.69)	(3.96)	(-0.09)	(2.38)	(1.87)	
Slope value	-0.03	0.05	-0.02	-0.15	0.38%	0.3%
	(-0.42)	(0.74)	(-0.31)	(-0.73)	(2.01)	
Butterfly value	0.06	-0.09	0.00	0.20	0.61%	1.1%
	(0.95)	(-1.34)	(0.07)	(0.97)	(3.19)	
Multi-dimension value	0.16	0.10	-0.01	0.26	0.68%	3.5%
	(2.55)	(1.61)	(-0.17)	(1.28)	(3.62)	
		Panel B: I	Momentum			
	EQ mom	FX mom	Com mom	Mkt-rf	Alpha	Marginal R ²
Level mom	0.12	0.21	0.18	0.28	0.10%	10.9%
	(1.91)	(3.34)	(3.00)	(1.43)	(0.56)	
Slope mom	0.00	0.06	0.04	0.59	0.04%	0.5%
	(-0.06)	(88.0)	(0.63)	(2.85)	(0.21)	
Butterfly mom	0.01	-0.08	0.03	0.19	-0.01%	0.8%
	(0.13)	(-1.29)	(0.48)	(0.93)	(-0.04)	
Multi-dimension mom	0.07	0.10	0.13	0.57	0.07%	3.8%
	(1.04)	(1.51)	(2.18)	(2.81)	(0.39)	
		Panel	C: Carry			
	EQ carry	FX carry	Com carry	Mkt-rf	Alpha	Marginal R ²
Level carry	0.15	0.30	-0.06	0.30	0.29%	12.5%
Lever carry	(2.57)	(5.11)	(-0.97)	(1.48)	(1.56)	(0.00)
Clare same	0.11	0.08	(-0.97) -0.05	0.40	0.44%	2.2%
Slope carry						
D. H	(1.71)	(1.34)	(-0.79)	(1.90)	(2.31)	(0.13)
Butterfly carry	-0.02	-0.01	0.11	0.38	0.82%	1.2%
8 A - (4) - (1) 1	(-0.35)	(-0.14)	(1.69)	(1.76)	(4.25)	(0.40)
Multi-dimension carry	0.11	0.17	0.00	0.48	0.70%	4.3%
	(1.73)	(2.75)	(-0.00)	(2.32)	(3.69)	(0.01)

Tradeable Bond universe

Style Factors in Other Asset Classes

_	EQVOL	FIVOL	GBI	HY	OTR	SPX	Alpha	R ²
Level multi-style	-0.02	0.69	0.95	0.10	-1.41	0.10	0.58%	5.4%
	(-0.06)	(0.60)	(4.05)	(1.14)	(-0.58)	(1.91)	(2.87)	
Slope multi-style	0.32	2.17	0.59	0.10	3.01	0.02	0.27%	4.6%
	(0.83)	(1.84)	(2.48)	(1.08)	(1.21)	(0.32)	(1.28)	
Butterfly multi-style	-0.05	0.33	0.87	0.33	-2.06	-0.07	0.81%	6.9%
	(-0.12)	(0.29)	(3.73)	(3.79)	(-0.85)	(-1.30)	(3.99)	
Multi-dimension value	0.23	0.09	0.48	0.13	-3.02	0.07	0.63%	6.0%
	(0.63)	(80.0)	(2.08)	(1.48)	(-1.26)	(1.38)	(3.16)	
Multi-dimension mom	-0.05	1.11	0.56	0.01	-0.77	0.00	0.15%	0.5%
	(-0.14)	(0.97)	(2.42)	(0.09)	(-0.32)	(0.09)	(0.72)	
Multi-dimension carry	0.06	1.60	0.91	0.28	3.03	-0.03	0.58%	8.2%
•	(0.15)	(1.41)	(3.92)	(3.28)	(1.26)	(-0.58)	(2.88)	
Multi-dimension, multi-style	0.12	1.46	1.10	0.24	-0.21	0.02	0.76%	7.8%
,	(0.31)	(1.28)	(4.78)	(2.79)	(-0.09)	(0.44)	(3.79)	

Conclusions

These simple style factors:

- do significantly better job explaining yield curve returns than a combination of traditional yield factors and other unspanned factors.
- provide economic intuition for what drives yield curve premia.
- offer an enticing and direct link to return predictability from other asset classes.