

Towards an accurate brain tractography using diffusion weighted imaging

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1 Introduction

Diffusion MRI (dMRI) is the only non-invasive method that provides information about the neural tracts found in white matter and the cortex. dMRI acquires one or more T2-weighted reference images, and a collection of diffusion-weighted images that attenuate the T2 signal according to the amount of diffusion along prescribed gradient directions [29]. The information is not complete and the tracts cannot be reconstructed in full detail [21]. However, some spatial structures and patterns can be visualised. These are usually represented as trajectories [57] or connectivity maps [9]. The unique new area that aims to reconstruct the neural tracts from diffusion data is called diffusion tractography. Other types of tractography are based in staining using for example luxol-fast blue [38] but these can only be used with *in vitro* brains and they lack ease of repeatability.

The field of diffusion tractography is less than ten years old. It started with Mori's first tractography algorithm FACT[41] in 1999 and it is still a highly active field of research and development. We believe however that the resolution and accuracy of tractography today is weakened by the following problems:

1. Poor acquisition schemes not specifically designed for tractography.
2. Over-simplistic local fiber direction modelling.
3. Lack of gold standard phantoms and validation techniques for dMRI.
4. Lack of robust and efficient tractography algorithms.

The goal of this thesis is to investigate possible solutions or improvements of existing solutions for all four problems. However, we focus more on problems 2 and 4. We want to be able to increase the resolution of tractography by taking into account global properties of the brain. We believe that by using whole brain discrete optimisation and Bayesian inference we will be able to remove many artifacts and ghosts, see section 8. In order to decide which is the best way to go forward and plan our research strategy we had to study and test many different algorithms and approaches (see sections 4 and 6) and gather datasets obtained at the MRC-CBU (see Fig. 1 and 2) and elsewhere. Furthermore, we developed a new software library in Python which is able to visualise and interact with 3D/4D datasets, open medical files, calculate tensors, draw trajectories, and many other features, see section 5. We proposed and tested a new acquisition protocol that will hopefully replace the current default dMRI protocol in use at MRC-CBU, for more details see 7.

1.1 Terminology

Diffusion imaging has many specialist terms, and one source of confusion has been lack of clarity in the meaning of these terms. To start, we will use the term "diffusion weighted imaging" (DWI) to refer to any MRI image acquisition that is weighted to be sensitive to diffusion.

One major source of confusion is that terms are often used to refer both the type of *acquisition* used to acquire the data, and to the subsequent *analysis* of the data. The most egregious example is the term "diffusion tensor imaging" (DTI). Used in a technical sense, the term refers to a very simple analysis model for the per-voxel diffusion direction profiles - a single diffusion tensor (SDT). However, it is also used to refer to all diffusion weighted imaging, or to a particular type of acquisition with a small number of diffusion gradient directions (of which more below). We will avoid the term DTI in this paper, and humbly suggest that it will reduce confusion if others do the same.

Tractography is the process of spatially integrating local estimates of fiber directions throughout the brain. Tractography gives only an estimation of the real tracts. Consequently, when we use the term tract we will generally mean a tract or track estimated or computed using some algorithm, i.e. a trajectory, except if it is stated we are referring to an actual real tract. The terms tract and fiber are considered here equivalent.

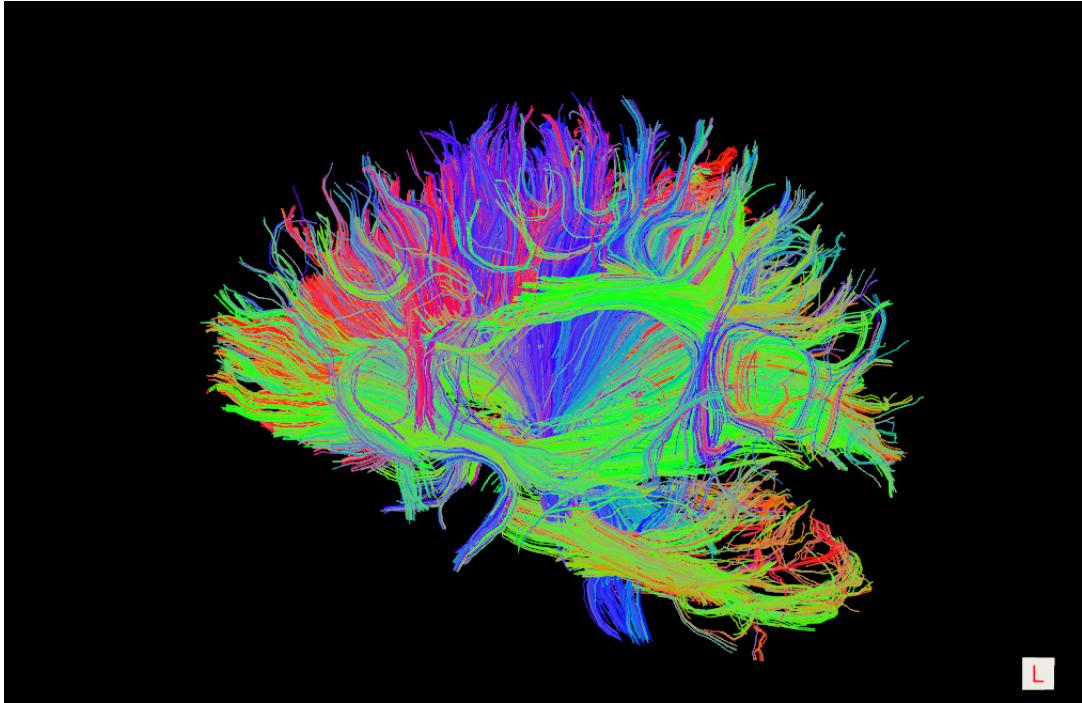


Figure 1: The dMRI dataset were obtained at MRC-CBU and analyzed with DTK & TrackVis using the deterministic algorithm FACT. All tracts less than 26 mm were removed in length. See sections 4 and 7 for discussion and Fig.1 for comparison.

2 Diffusion Weighted Imaging signal

2.1 What is diffusion?

Molecular diffusion is a process that is taking place all the time in fluids and accounts for a number of interesting phenomena; the dMRI signal measures the history of the random (Brownian) displacements of spin-labelled hydrogen protons (spins) resolved in the direction of a magnetic field gradient. Though the actual probability displacement function of the protons is unaffected by the presence or variation in the magnetic field, the cumulative phase change in the spins reflects the changes in the position-dependent spin frequency induced by the field gradient. Components of the motion along the direction of the gradient induce such changes. The signal change due to cumulative dephasing is greatest when this coincides with a direction that allows greater random displacements, e.g. because of the orientation of a microstructure within which the proton is moving. It is this link between the directional dependence of the dMRI signal and the orientations of the supposed underlying brain fibres that provides the unique insights of diffusion tractography.

Anisotropy is one of the terms that are very common in diffusion terminology. Anisotropy means that the average displacement of the particles is greater along a preferred direction. On the other hand, isotropy means that the particles are equally likely to move in any direction. It is anisotropy, i.e. directional dependence of diffusion that is the basis of dMRI. In dMRI the protons will move more along the directions of the axons and less perpendicular to that direction. For a biological interpretation of the signal measured with dMRI see[7], [60] and [29].

2.2 Diffusion Maths

Bloch and Torrey[55] established differential equations governing MR diffusion in non-isotropic magnetic fields by analogy with Fick's Laws[24] for the spontaneous dispersion along concentration gradients of inhomogeneous substances. Callagan[14] also showed how these bulk properties could be derived by statistical methods from the collective spin histories of individual protons. When a molecule is at position x_0 , we cannot say where it will

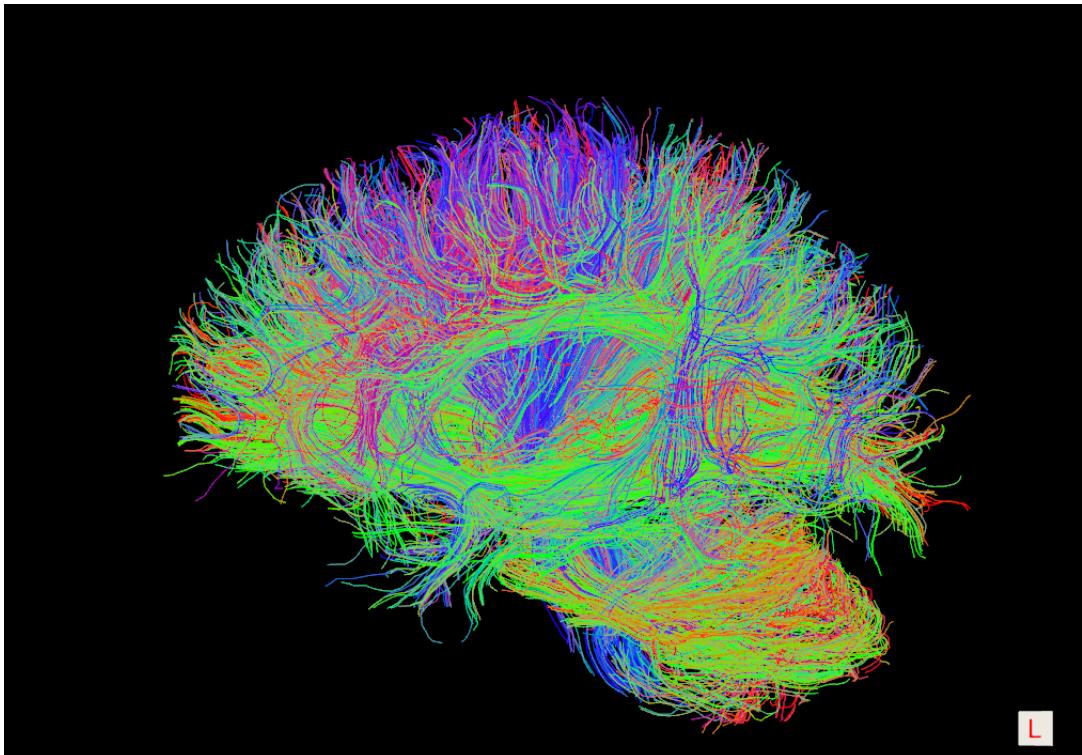


Figure 2: Derived from the same dataset as in Fig. 1 but here the deterministic algorithm R-K was used with the same 26 mm threshold. By comparing these two figures it is obvious that R-K generated thousands more tracts than FACT. So, which one is the best? The need for validation of existing tractography and the removal of ghost tracks is crucial for obtaining meaningful data. However, this is a very difficult problem for which we hope to spend our time investigating possible solutions and inventing new more accurate tractography algorithms.

be after time t , we can only model a distribution of possible locations. This motion is described by a propagator $P(x; x_0, t)$ which defines the probability of being in x after a time t , starting at x_0 .

Since the primary interest of dMRI is the way that the signal depends on the direction of underlying fiber orientations., it is the orientation information in this propagator that is potentially of interest. The orientation distribution function (ODF) expresses the probability of a spin displacing into a differential solid angle about a possible fibre direction u . This is used in order to model and visualise the directional information in diffusion propagator and in simple words it just projects the diffusion function on to the sphere by integrating over the radial coordinate of the diffusion function. The ODF representation symbolised below with f sacrifices all the radial information but retains the relevant directional information:

$$f(\mathbf{u}) = \int_0^\infty P(\rho\mathbf{u}) d\rho \quad (1)$$

where \mathbf{u} is a unit normal vector and ρ is the radial coordinate in the diffusion space. Stejskal and Tanner [53] showed that the spin echo magnitude $S(\mathbf{q}, t)$ from a PGSE experiment (see 2.3) is directly related with the diffusion propagator by the following Fourier relation

$$S(\mathbf{q}, t) = S_0 \int P(\mathbf{R}, t) e^{i\mathbf{q}^T \mathbf{R}} d\mathbf{R} \quad (2)$$

where S_0 is the signal in the absence of the applied diffusion gradient, \mathbf{R} is the relative spin displacement $\mathbf{x} - \mathbf{x}_0$ at diffusion time t , \mathbf{q} is the spin displacement wave vector. With the inverse Fourier transform we can reconstruct the diffusion propagator P by measuring the signal in a number of different directions and gradient magnitudes. Q-space imaging (QSI) and Diffusion Spectrum Imaging (DSI) are the best known methods which try to reconstruct the full diffusion propagator in that way.

Assuming that the diffusion propagator is given by a 3-dimensional Gaussian distribution we can write

$$P(\mathbf{R}, t) = \frac{1}{\sqrt{4\pi t^3 |\mathbf{D}|}} \exp\left(-\frac{\mathbf{R}^T \mathbf{D}^{-1} \mathbf{R}}{4t}\right) \quad (3)$$

where \mathbf{D} is known as the diffusion tensor. This tensor is a 3D symmetric matrix that can be completely described by a centred ellipsoid with axes (eigenvalues) $\lambda_1, \lambda_2, \lambda_3$. Fractional Anisotropy (FA) is a very common metric in diffusion imaging which is used to characterise the presence or absence of a preferred direction for diffusion. It is calculated from the eigenvalues.

$$FA = \frac{1}{\sqrt{2}} \frac{\sqrt{(\lambda_1 - \lambda_2)^2 + (\lambda_2 - \lambda_3)^2 + (\lambda_3 - \lambda_1)^2}}{\sqrt{\lambda_1^2 + \lambda_2^2 + \lambda_3^2}} \quad (4)$$

If FA is equal to 1 that means very anisotropic (infinitely prolonged ellipsoid) and if FA is equal to 0 that means completely isotropic (sphere). FA is used in clinical studies to diagnose diseases like stroke and cancer and assess the progress of therapy [37].

Whenever we are using FA volumes we assume that the propagator of the spin displacements in every voxel will be a 3D Gaussian distribution. This assumption is used in most of diffusion related literature. Unfortunately, in reality things are much more complicated; inside our brain the axons are semi-permeable (restriction), the water molecules interact with many different elements in the complex intra fibre fluid, the fibres might cross, kiss, divert or bend inside a voxel. Therefore, assuming a Gaussian distribution is a non-trivial approximation. For alternatives see 3.4.

2.3 Acquisition sequences in use

The best known method for generating diffusion-weighted images is called Pulsed Gradient Spin Echo method (PGSE), also known as the Stejskal and Tanner method [53]. This has 90-180 degrees spin echo pair of RF pulses with one gradient before the second pulse and one equal gradient after the second pulse (see [39], p329), see Fig. 3. The refocusing is perfect only when the spins do not move between the two pulses. The diffusion weighted contrast acts like inverse T_2 weighting i.e. tissues with mobile water molecules give lower signal than more solid tissues with smaller mobility. Eddy currents caused by the onset and offset of the gradients are

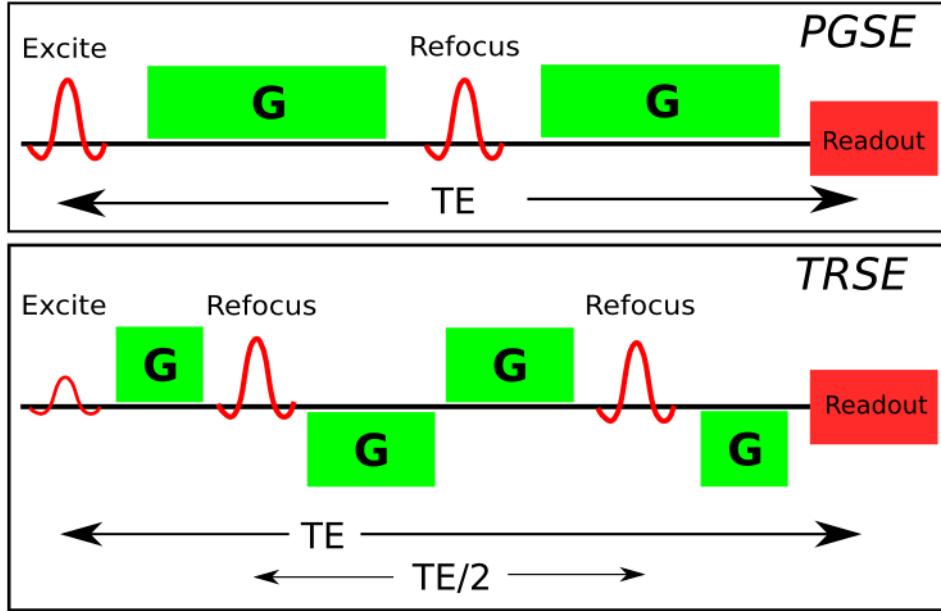


Figure 3: PGSE and TRSE

a problem with PGSE and most systems (including Siemens) use twice-refocused spin echo sequences [49] to reduce these artifacts. Every time the magnetic field gradients switch they generate currents that generate other smaller magnetic fields which disturb the spins. The TRSE sequence is an improvement on the PGSE. The improvement is made using another refocusing pulse surrounded by the inverse mirror of the previous diffusion gradients (see Fig. 3). By adjusting the timing of the diffusion gradients, eddy currents can be nulled or greatly reduced. This sequence improves the image quality without loss of scanning efficiency i.e. TR duration and it is the standard in most modern MRI scanners.

2.4 What is a b-value?

The b-value b or *diffusion weighting* is a function of the strength, duration and temporal spacing and timing parameters of the specific paradigm. This function is derived from the Bloch-Torrey equations[14]. In the case of the classical Stejskal-Tanner pulsed gradient spin-echo (PGSE) sequence, at the time of readout

$$b = \gamma^2 G^2 \delta^2 \left(\Delta - \frac{\delta}{3} \right),$$

where γ is the gyromagnetic ratio, δ denotes the pulse width, G is the gradient amplitude and Δ the centre to centre spacing. γ is a constant, but we can change the other three parameters and in that way control the b-value.

Under the Brownian motion assumption the signal strength is described by the equation $S(b) = S(0)\exp(-bD)$ where D is the diffusion coefficient that we wish to measure and b the crucial experimental parameter diffusion weighting parameter or b-value which summarises the diffusion sensitising gradient history. Although the PGSE is useful for expository clarity, in reality more complicated but related sequences such as the twice-refocused spin-echo (TRSE) [28, 49] sequence and subsequent refinements such as TRASE [3] are employed as a means of removing the distortion effects from eddy currents resulting from the initial and final ramps of the gradient pulses. The important point is that we can control the size of the b-values by changing the strength and timings of the gradient pulses and that depending on the b-value, we can expect different amount of signal loss. A further important simplifying assumption made is that the function $S(b)$ is described by a single exponential term (mono-exponential). In fact there is evidence that this assumption may break down at higher b-values. The units of D are mm^2/sec (for water at $37^\circ D \approx 3 \cdot 10^{-3} m^2/sec$), and of b are sec/mm^2 , typically in the range $0\text{--}5,000 sec/mm^2$ though some DW-MRI acquisition paradigms can call for very much larger values e.g. $12,000 sec/mm^2$.

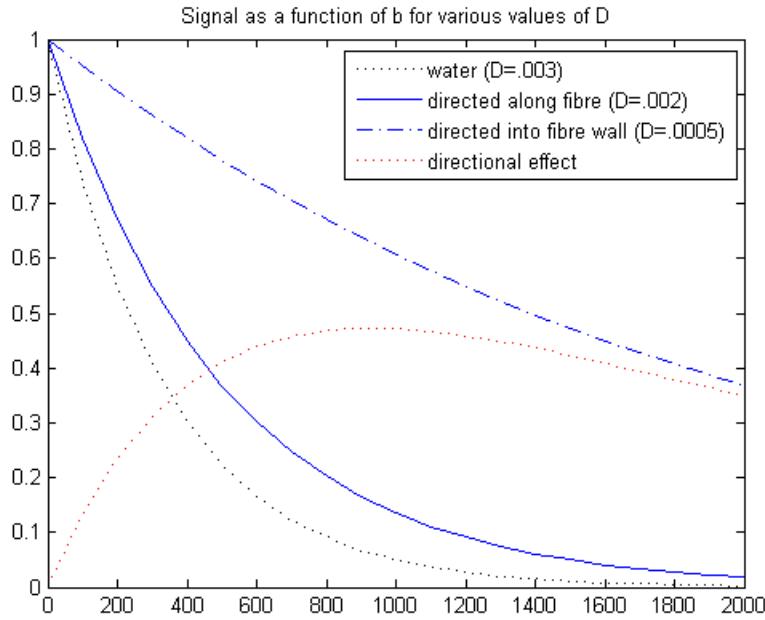


Figure 4: Signal as a function of b for various values of D

2.5 What is DWI?

Diffusion Weighted Imaging (DWI) is MRI imaging designed to be sensitive to diffusion. With this imaging technique we attempt to delineate the axonal organisation of the brain. A diffusion weighted image is a volume of voxels gathered by applying only one gradient direction to our sequence. Therefore, the signal in every voxel should be low if there is greater mobility of water molecules along the specified gradient direction and it should be high if there is less movement in the same direction. Therefore if inside a voxel there is an underlying fibre that is parallel to this direction we should expect a lower value otherwise if the fibre is not parallel or near parallel or if there is no underlying fibre we should expect a higher value.

The directional dependence of the DWI signal is the cornerstone of diffusion based tractography. Signal from a specific voxel will be higher in directions where diffusivity is high, e.g. along the direction of a putative bundle of fibres, and lower into the walls of the constituent fibres. Figure 5 and 6 show how signal for an anisotropic Gaussian diffusion would change with gradient direction.

3 Q-space methods

3.1 What is q-space?

Q-space is the space of one or more 3D spin displacement wave vectors \mathbf{q} as shown in equation 2. This vector is related to the applied magnetic gradient \mathbf{g} by the formula $\mathbf{q} = (2\pi)^{-1}\gamma\delta\mathbf{g}$. Every single vector \mathbf{q} has the same orientation of the direction of diffusion gradient \mathbf{g} and length proportional to the strength of the gradient g . Every single point in q-space corresponds to a 3D volume of the brain for a specific gradient direction and strength. Therefore if for example we have programmed the scanner to apply 60 gradient directions then our data should have 60 diffusion volumes with each volume obtained for a specific gradient. A Diffusion Weighted Image (DWI) is the volume acquired from only one direction gradient. Hence, in the previous example we would gather 60 DWI volumes. An alternative way to see \mathbf{q} is in mathematical terms as the combination of parameters which produces a Fourier transform relationship between the diffusion signal and the probability displacement distribution. In these terms (see Callaghan [14]) \mathbf{q} is the reciprocal of the probability displacement vector \mathbf{R} , just as in conventional MRI \mathbf{k} space is the reciprocal parametrisation of the brain space vector \mathbf{v} .

Another way to represent dMRI is the following. We can combine all the DWIs together creating a new

Signal as a function of direction for a gaussian diffusion function
with a horizontal principal direction and two values of b

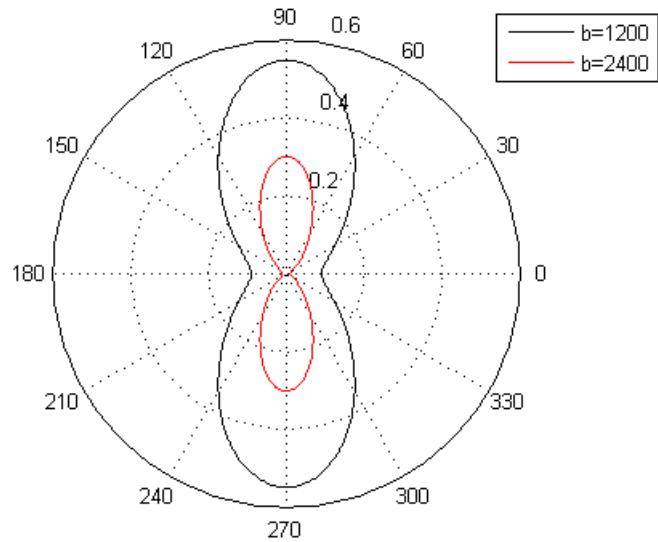


Figure 5: Directional dependence of signal for two b-values.

-Log(signal as a function of direction for a gaussian diffusion function
with a horizontal principal direction and two values of b

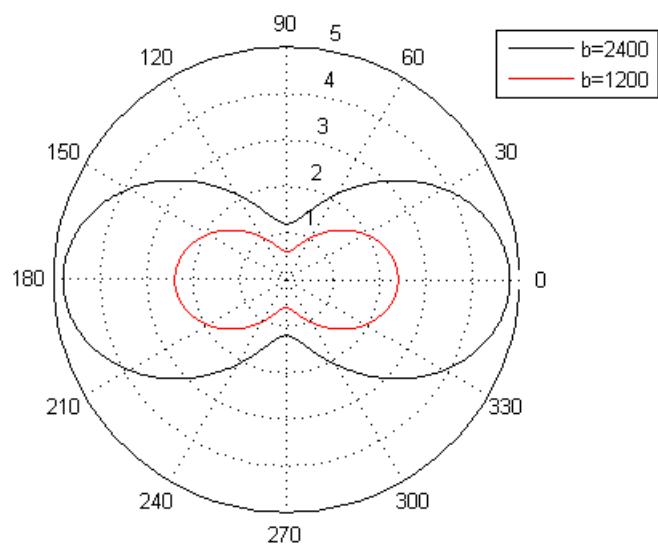


Figure 6: Minus log(signal) of the above.

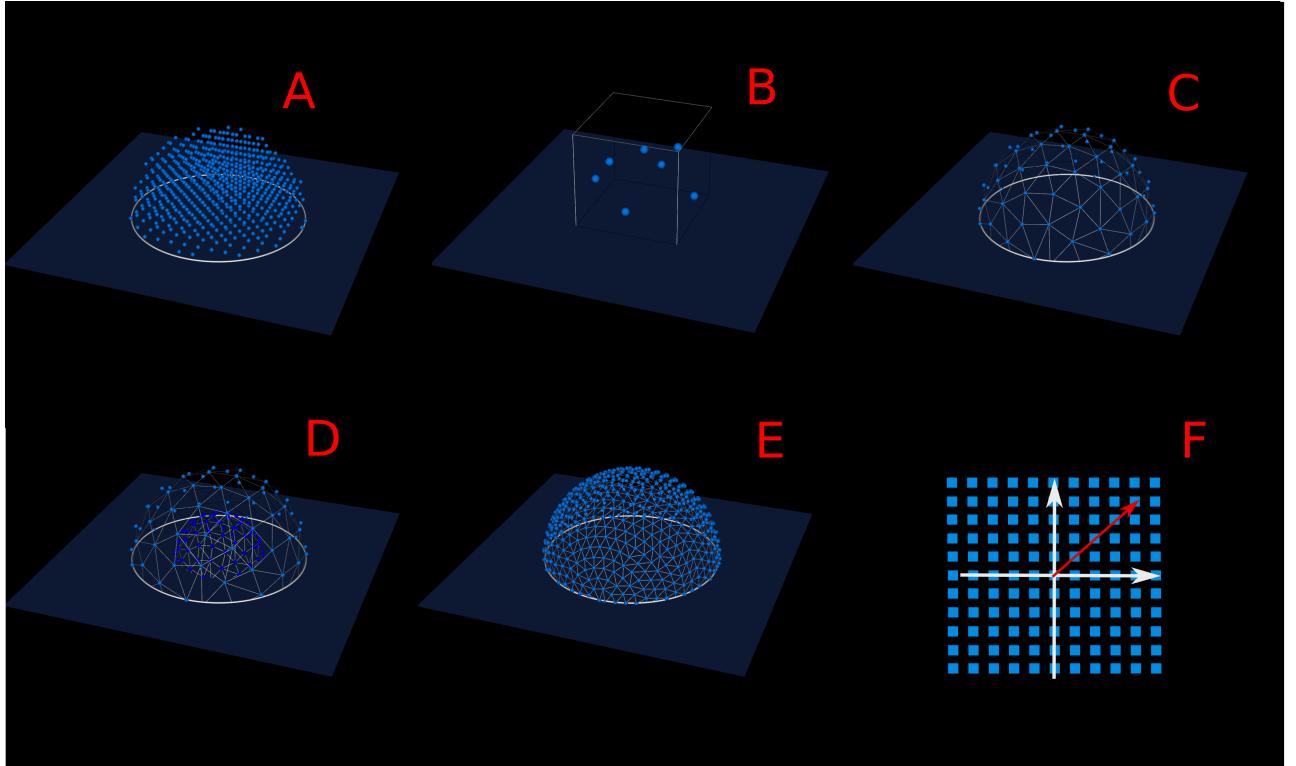


Figure 7: A: DSI 604 directions, B: DTI using only 7 directions, C: HARDI 65 directions, D: HARDI with 2 shells of 65 directions in each shell, E: QBI 515 directions, F: QSI simplified 2D example showing that the full q-space is needed for the reconstruction of the propagator.

multidimensional image where each voxel corresponds to a profile of diffusion signals measured in all the chosen gradient directions \mathbf{g} . This is the only known way to represent all different acquisition methods with the same structure and we are planning to use it as the basis for our novel tractography algorithm (see section 8).

3.2 Acquisition methods and defining terms

In our introduction, we promised to be as clear as possible about the terms we use. One problem in diffusion imaging is that names for techniques often refer both to a particular type of imaging acquisition, and to the subsequent analysis model. All dMRI acquisition methods acquire data in q-space, but the methods can be categorised by their sampling pattern in q-space.

We refer to a method as a *q-space shell* method if it is an acquisition method collecting a series of points in q-space that can be thought of as being on a curved surface, typically a sphere. Examples include techniques referred to as HARDI (High Angular Diffusion Imaging), Q-ball Imaging and HYDI (Hybrid Diffusion Imaging). A q-space shell method might involve a collection of a single shell (Fig. 7C,E), e.g. QBI or multiple shells (Fig. 7D) e.g. EQBI. In clinical settings where we can only use a few directions (less than 60 with minimum 6) the only way is to use the SDT model (Fig. 7B).

A *q-space volume* method is an acquisition method that is more easily thought of as collecting points distributed through a volume in q-space. The characteristic example is DSI (Fig. 7A). and QSI(Fig. 7F).

4 Deterministic vs Probabilistic Tracking

The number of different tractography algorithms for diffusion MRI data that have been introduced during recent years is enormous and it would be impossible to discuss them all here. There are two main families of

local tracking algorithm: deterministic and probabilistic. We will begin by describing here the simplest or most popular deterministic approaches and then we will concentrate to the probabilistic approaches. A tractographic algorithm belongs to the probabilistic domain if the fibre model that is being used incorporates uncertainty i.e. errors in estimating the orientation of the fibre at every voxel. If it does not assume any uncertainty along the path of the track then it is deterministic. All tractography algorithms are based in local estimates of diffusion direction. For more information about different models of local estimates see [6],[4], [11],[35].

One of the simplest and first deterministic methods is called Fibre Assignment by Continuous Tracking (FACT) [41]. The FACT algorithm starts through the input of an arbitrary point in the volume and then tracks in both directions e.g. forward and backwards. The interesting part with these tracking methods is how they decide when to stop tracking. FACT is using a single threshold variable $R = \sum_i^s \sum_j^s |\mathbf{e}_i \cdot \mathbf{e}_j| / s(s - 1)$ where s is the

number of neighbouring voxels and \mathbf{e} is the eigenvector corresponding to the largest eigenvalue in each point. The simplest case for defining a neighbourhood of a voxel is to use all 26 other adjacent (touching) voxels. Now, lets think of how R will behave in different neighbours. When adjacent fibres are aligned strongly R will increase as the absolute value of the dot product grows bigger as the normalised vectors become more co-linear. On the other side, R will grow shorter in regions without continuity in fibre direction, where $R = 0$ in perfect isotropic conditions. In voxels with R less than a prespecified threshold e.g. 0.8 the tracks will stop being followed and FACT will terminate. An important problem with FACT is that it fails to track axons leaving major pathways where it tracks only one of the branches.

Another popular deterministic approach very much inspired by the field of fluid dynamics was introduced by Basser [5] assuming again a continuous vector field but now the tract is generated by the solution of a system of differential equations subject to an initial condition, the position of the seed point. The solution of the system of ordinary differential equations (ODE) is given by an iterative method called 4thorder Runge-Kutta scheme. (Other schemes are possible.) Here the authors propose that a fibre can be represented by a 3D curve \mathbf{r} parametrised by the arc length s of the track. The iterative solution of this equation $d\mathbf{r}/ds = \mathbf{e}$ generates the trajectory of the underlying fibre also known as streamline.

Basser's method again is very sensitive in local noise and smoothing. However, it is very straightforward and fast. Wedeen et al.[57] showed that one could derive the local orientation field of vectors \mathbf{e} from the local maxima of the ODF calculated in each voxel. In that way we could visualise crossing distributions and depict crossing fibres. The results in [57] show that, using Fourier reconstruction or Funk-Radon analysis on q-space shells, we can generate much richer estimates of axonal architecture than SDT models i.e. many more fibres of complex or simple configuration. This investigation suggests that diffusion MRI with sufficient signal to noise ratio (SNR) could make tractography a mathematically well-posed problem. However, we need many hours of scanning to reach the necessary resolution.

Other deterministic approaches can be found here [36], [18]. A recent deterministic algorithm called Tensorlines[58] shares the problems of the other deterministic algorithms by failing in relatively sharp turns and Meyer's Loop. In summary, the deterministic algorithms generate paths by making a series of discrete locally optimum decisions. These are fast, simple and easy to interpret. Usually, we depict them using streamlines. A streamline is a curve that is always tangent to the velocity vector of the flow. The disadvantages of deterministic algorithms are that a pathway either exists or not (no uncertainty) and that they do not explore the entire space of likely white matter tracts. In other words, local thresholding makes our tractography vulnerable to small noise aberrations.

Probabilistic tractography is meant to deal with this problem and generate tracks even in regions that tracking is unclear. This is possible by assuming that uncertainty exists concerning the orientation of the fibre at each point of the track. We will try to illustrate the difference between the two approaches using a simplified 2D example shown in Fig. 8 (i,ii). Generalising afterwards in 3D is straightforward.

Let's imagine that we have a 2D slice where in each pixel we have calculated a vector showing the primary direction for that specific pixel. This vector \mathbf{e} could have been calculated from the tensor as the primer eigenvector or as a primer direction of a different model e.g. the maximum point of the ODF. Lets now think that we want to find the best path from seed A to seed Z. When using deterministic tractography we are using only the local direction information in every pixel therefore in a direction field as this of Fig. 8(i) we will have to use only one track and this is the diagonal pathway with yellow colour. However there are other possible tracts as well in this diagram e.g rather than taking the diagonal go first up north from A and then right.

Probabilistic tractography aims to identify all the possible tracts by assigning to each one of them a weight. All the weights of all the tracts together sum to 1. This is possible by generating samples from a probability

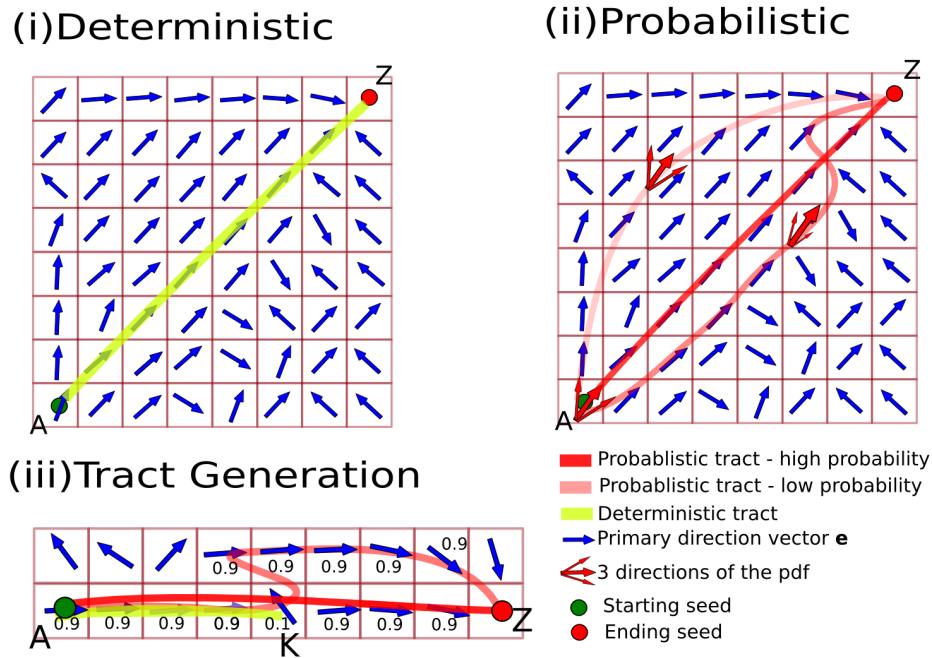


Figure 8: A simplified example showing in (i) & (ii) the same dataset but in (i) the yellow line shows the result of deterministic tractography which is given by a single trajectory and in (ii) is given by connectivity matrix depicting with red the probability of different pathways throughout the hole slice. Here only 3 possible pathways are depicted for the ease of understanding. Finally, in (iii) an example is given where it shows that probabilistic tractography weights more closer connections. However it can tract further deep than deterministic tractography. See section 4 for more.

distribution for every pixel. In this toy example shown in Fig. 8(ii) the orientation of the blue vectors can be represented by a single parameter, angle ω . ω here is a random variable that takes values from a probability distribution function (pdf). Now we have many possible directions to move next but with different probabilities. The weights of all directions again sum to 1. After this explanation we can identify in Fig.8(ii) that the most likely tract is again the diagonal (with deep red) but there are other pathways (with lighter red) that are less likely. In the same diagram we show with 3 combined red arrows some of the many directions that are possible in each point. However, some are more certain than others.

Let's try now to understand how a tract is valued as more probable than others. In 8(iii) we have drawn a very simple image with only two pixel rows and we are assuming that the probability of moving along the primary direction (shown with blue arrow) is 0.9 and there is only a secondary direction given by 0.1 (1-0.9) i.e. we assume for ease of understanding here only 2 directions. We can see that there is a discontinuity in position K. In that point an Euler based deterministic approach would have to stop at K (see yellow line). The probabilistic method will continue tracking and it will generate two tracts that both reach the target. To probability of each tract is calculated by multiplying the probability of a specific direction of each point. Therefore, the shorter and dark red path will have $p_s = 0.9^7 \times 0.1$ and the longer and lighter red path will have $p_l = 0.9^{10}$. It is obvious that $p_s > p_l$ and that the darker red path is more likely to exist according to this method.

This method of multiplying the probabilities at each voxel along the paths has been proposed by many [25],[2], [12], [26],[30],[46] and used in many software packages as well as Parker's PICO[44] in Camino , Behrens' FDT [10, 8, 9] in FSL, and others.

Although the probabilistic methods are able to identify many known tracts, they miss several large tracts such as the visual pathways LGN-MT and callosal MT. The visual pathways are useful frameworks for algorithmic development and testing because they diverge and bend significantly. The current methods have the advantages that they expand the track search space beyond deterministic algorithms and that they can easily expand with complex models supporting crossings (usually not more than 2 crossings). However, they don't compute an accurate probability of brain connections. The phraseology "Connection probabilities" or "estimation of global connectivity" or "the probability of the existence of a connection through the data field, between any two distant points" found in [10] can be very misleading because someone might believe that they represent the actual connectivity profile of the subject. For example we are certain (with probability 1) that LGN (lateral geniculate nucleus) is connected to V1 and V2 (primary visual cortex) in a healthy brain however the estimated connection probability in FDT is much less than 1. In addition, current probabilistic algorithms fail to identify pathways even when they are known to exist or in a few cases they generate pathways even when they do not exist [11, 32, 51]. For example no connections between left MT+ and the posterior portion of Corpus Callosum were found in PiCo [44] or FDT although it is well established that they do exist.

In 2008 Sherbondy[52] in order to try to deal with the problems explained in the previous paragraph implemented in ConTrack an algorithm that separates the pathway sampling and scoring steps. In that way the scoring does not depend any more one whether we are tracking from seed A to seed B or from B to A therefore, it assumes symmetry when the other probabilistic methods do not. At the same time Sherbondy's method assumes independence between different tracts i.e. path $A \rightarrow B$ is independent from $A \rightarrow C$ or $K \rightarrow L$. This is not happening in most other methods where the pathways depend on other pathways starting from the same seed. So, ConTrack is designed to estimate connections that are known to exist. The disadvantage of Sherbondy's method is that it needs a lot of user interaction to add the known tracks and the user needs to be a specialist in white matter anatomy otherwise the results might be biased. The same problem exists with the waypoint masks used in the latest versions of FDT. Finally, a small summary of the comparative strengths of deterministic vs. probabilistic tractography is given in Table 1. For noise related problems e.g. motion and eddy correction and possible solutions see [30, 5],[33],[27],[61],[1],[33],[59] and for methodology and ideas comparing across subjects see [34],[42],[34],[37],[22],[20],[43], [23], [19].

5 Software

We write our software in Python with embedded C/C++ modules for speed if necessary. We choose Python because it is open source, multiplatform, free, it has a very simple object oriented syntax and many interfaces with GUIs, scientific computing libraries and other languages. We also hope that some of our code will be used in a future version of Nipy. We coined the name Tractarian (TRN) for this python project but there are many functions and files that are useful not only for tractography but generally for machine learning, scientific

	Deterministic	Probabilistic
Voxel Noise Resistance	More	Less
Non-existing Tracts	Yes	Yes
Execution Time	Fast	Slow
Memory Size	Less	More
Biased on Tract Length	No	Yes

Table 1: Deterministic vs Probabilistic Tractography

TRN Modules	Main Features
lights.py	3D/4D visualisation using VTK & GUI using wxWindows
diffusion.py	Calculate Tensors & FA
eyes.py	OpenGL & Fast Tractography visualisation
form.py	File Reading & Writing
art.py	Machine Learning & Artificial Intelligence
external.py	Wrappers for external tools e.g. DTK, mri_convert.

Table 2: Summary of the developed features in TRN.

visualisation and medical imaging. TRN consists of the following modules diffusion.py, art.py, lights.py, form.py, eyes.py and external.py. See Table 2 for a summary of their features.

In more detail lights module is using underneath the Visualisation Toolkit (VTK) library provides simple commands to generate cones, tori, cubes, points, point clouds(dots), spheres, lines, poly-lines, trajectories, labels, arrows, planes, axes, splines, surfaces, volumes, record snapshot, record video, wireframe surfaces and spherical grids with evenly distributed points. For some results see Fig. 9A,B,C and Fig.7A-E. Lights enable as well two types of multithreaded interaction a. a graphical user interface using wxWindows and the 3d interaction that enables the user to translate the volumes and other primitives.

The diffusion module calculates at the moment the SDT (tensorfitssimple) and generates FA results. The future version of diffusion will be able to generate probabilistic tracts. The eyes module is an alternative visualisation module that enables very fast tractography representation and interaction. Imagine that the datasets we have contain hundreds of thousands of trajectories. To be able to depict them and interact with them in a user friendly speed is a difficult problem, see Fig. 9D.

The form module loads and writes many different types of files. For example Nifti, Analyze, Dicom, files with diffusion gradient directions (bvecs) and b-values (bvals), DTK tractography files e.g. trk files and also reads Excel files. It has also the possibility to compress and decompress files.

The art module is related with the development and testing of new artificial intelligence or machine learning algorithms and the use of existing ones. At the moment art uses the Modular Toolkit (MDP) e.g. to generate FastICA and Scipy for optimisation & integration methods.

Finally, the external module is used mainly as an alternative of bash scripting calling different external tools. For example it can generate tractography using DTK, convert files using mri_convert, find files, list directories etc. In the near future we plan to wrap FSL, Camino and Freesurfer commands.

There are many specific very interesting details about the software and the algorithms that we used that cannot be added in this short report. However we are planning to write a small wiki for other people to start using them in the MRC-CBU. Dr. Hampshire is already keen on using lights for his own visualisation problems.

6 Applying Fractional Anisotropy to a clinical dataset

During our journey on understanding the underlying theory behind dMRI methods we had to spend a lot of time trying to figure out the merits and deficits of the classical SDT approaches using Fractional Anisotropy (FA) volumes (presented in 2.2). In the next paragraph we present some interesting results we had during this investigation.

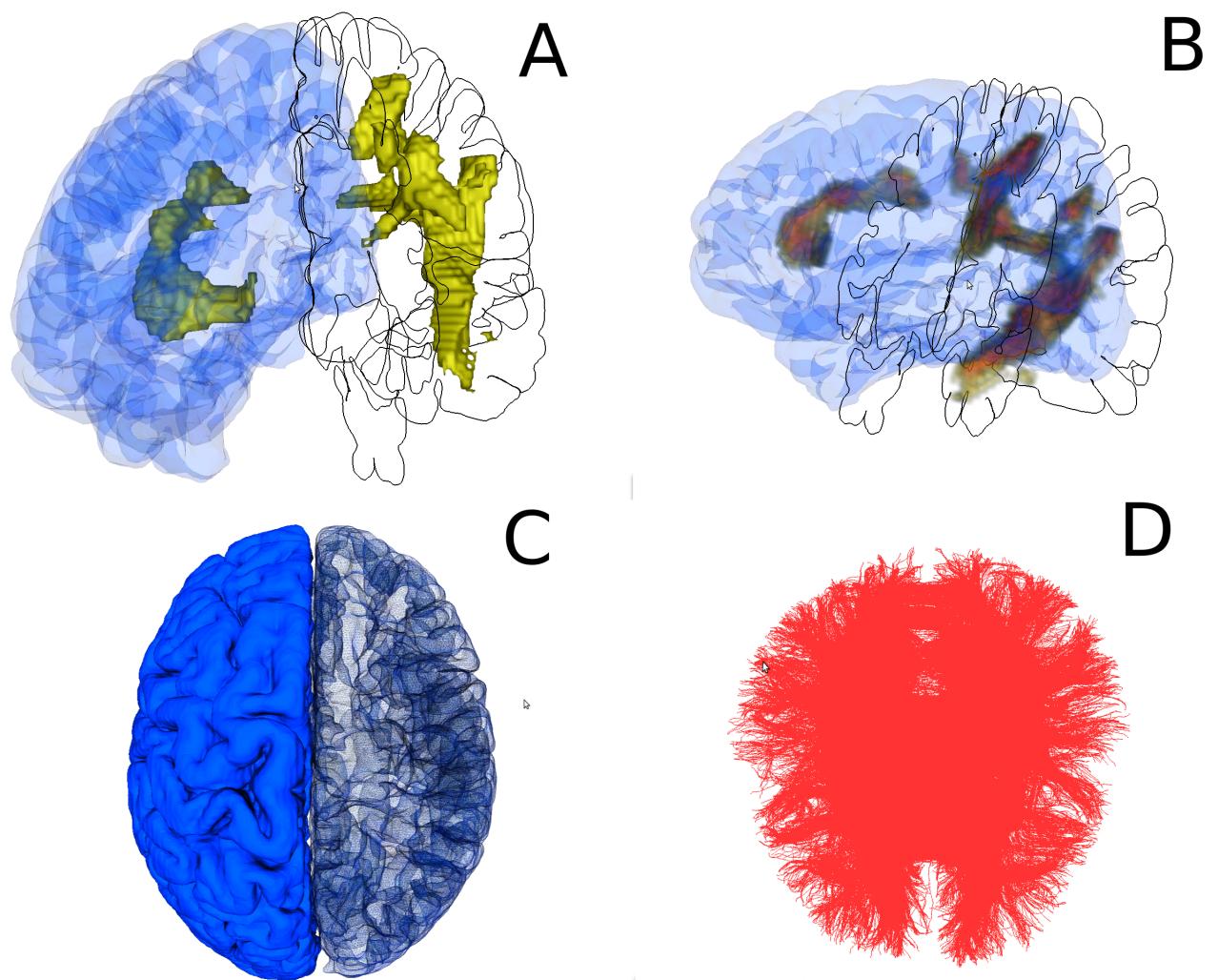


Figure 9: A, B, C are produced by TRN lights & D is generated using TRN eyes. dataset where loaded using TRN form. A,B & C show results found from the Trichotillomania experiment and D depicts fibre tracks without any orientation colour coding.

6.1 Trichotillomania

Trichotillomania is a disease with the symptom of impulsive hair pulling. It is also a disease that very little imaging data have been published. Chamberlain et al. [17] showed grey matter abnormalities in anterior congulate cortex and pre SMA. In collaboration with Adam Hampshire from MRC-CBU we tried to confirm and extend this result using diffusion imaging. The quality of the datasets was not good enough to generate tractography but they were good enough to calculate and analyse fractional anisotropy (FA) images. We found 3 clusters of lowered FA in the trichotillomania group compared with controls. A white matter cluster under the preSMA and ACC, mostly in the right hemisphere, another white matter cluster under the left hemisphere in the hand area of the pre motor cortex and a large cluster in left hemisphere that spread from underneath the pre motor cortex. These results are planned to be published at the Journal of American Psychiatry. My contributions was mainly on planning the diffusion analysis and visualising the datasets using our new software TRN. In the beginning we tried to use FSL for all the analysis however we had better results when combined FSL, SPM & CAMBA. This was inspired by a previous work of Chamberlain et al. with an OCD study[40].

The dataset included 20 patients with trichotillomania and 20 matched controls. Data collected at the MRIS in Addenbrooks on the 1.5 T GE Signa scanner using 25 gradient directions and one volume with $b=0$. MPRAGE was also collected. More information about the acquisition protocol and parameters can be found here[40].

Eddy correction and calculations of FA maps carried out in FSL/FDT and followed the standard on line directions. Then, for each participant, the b_0 was co-registered with the MPRAGE and this transform was applied to the FA maps. The MPRAGE was co-registered and normalised to the MNI template in SPM5 and these parameters were applied to the FA maps. The FA maps were now in the same space as the MNI template in SPM5. A spatial smooth was applied to the FA maps in SPM 5 using an 8mm Gaussian kernel. Group level analysis were carried out in CAMBA using cluster level correction. A white matter mask was obtained (from Sam Chamberlains previous OCD study). This white matter mask was defined by binarising the Statistical Parametric Mapping a priori white matter template to a binary mask, i.e., thresholding each voxel at 50% white matter to define white matter regions for analysis. FA maps were then compared cross group and within the white matter mask using a threshold of $p < 1$ false positive and two tailed cluster analysis.

For the visualisation of the results we used Freesurfer to extract the cortical surface from the MNI template. Then we used our own TRN software for the visualisation. The cortical surface was plotted using surface and contour rendering and the FA clusters were plotted inside the cortical surface using volumetric rendering. See Fig. 9A. For more information about how this visualisation was possible look section 5. We are now under the process with Dr. Adam Hampshire of making this graphical process automated so we can use it in all our following analyses that combine volumetric with surface data. The difficult part usually to achieve this is how to register these two datasets together. However, this is high too technical and complicated for this report.

We are running a larger cohort during Autumn 2009 with higher resolution sequence and we will also be collecting functional fMRI data in this patient group for the first time. We plan to identify functional differences and generate beautiful and hopefully meaningful tracts that will confirm our FA results.

7 Tractography Results

Here we discuss about some very motivating results we have obtained using our new tractography optimised acquisitions.

7.1 HARDI Experiments in CBU

The default Siemens diffusion acquisition protocol that we are using in CBU uses a rectangular voxel size of $1.8 \times 1.8 \times 2.5\text{ mm}$. We found that this creates problems with many different tractography software e.g. DSI Studio developed by Fang-Cheng Yeh. Tractography algorithms prefer cubic voxel size because that simplifies the modelling, clustering and interpolation of the tracts. This change would simplify as well our free model ideas described in section 8. Furthermore, we were planning to test the accuracy of tractography using acquisitions with different b -values. After some fruitful discussions with Dr. Guy Williams and Dr. Christian Schwarzbaumer we decided to run 4 acquisition schemes using 2 subjects and some fruits. All acquisitions were held in our own MRC-CBU's Siemens Trio scanner.

Acquisition	b-value	directions	repetitions
1A	1000	64	1
2A	3000	64	1
3A	5000	64	1
4A	5000	12	5

Table 3: Summary of the different acquisitions.

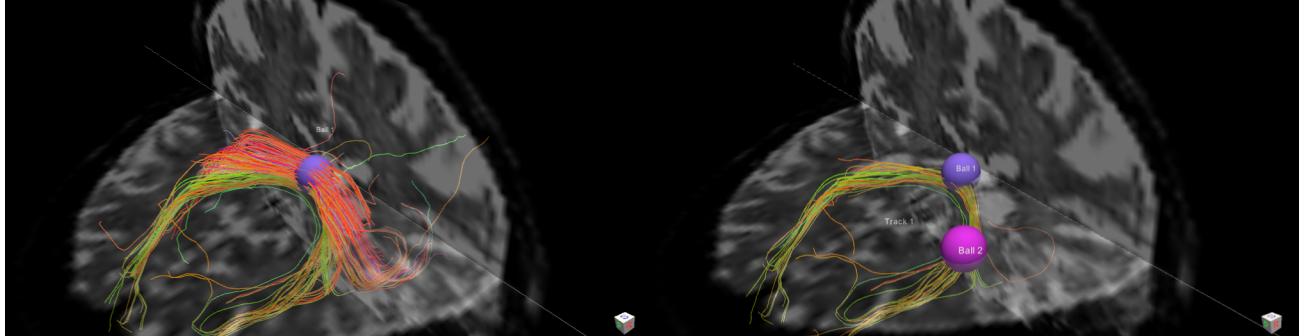


Figure 10: Left: Using one spherical ROI in TrackVis, Right: Using 2 spherical ROIs.

The first acquisition (1A) was using the following parameters: voxel size $2.0 \times 2.0 \times 2.0 \text{ mm}$, 64 directions, slice thickness 2.0 mm , TR=9200 ms, TE=93 ms, FoV read 256 mm and b-value = 1000 s/mm^2 . One more volume was acquired with b-value = 0 s/mm^2 . The total duration of the experiment was 10 minutes and 27 seconds.

The second acquisition (2A) was exactly the same with the previous one but using b-value = 3000 s/mm^2 , TR=10600 ms and TE= 114 ms. The total duration was 12 min and 27 sec.

The third acquisition (3A) was the same with the previous two but using b-value = 5000 s/mm^2 , TR=11500 ms and TE = 127 ms. The total duration was 13 min and 4 sec.

All the first three acquisitions were using 64 directions but the fourth one (4A) was using 12 directions with b-value 5000 s/mm^2 and the following parameters: TR=11500 ms, TE=127 ms, Averages=5. Table 3 summarises their main differences.

Unfortunately, the scanner failed to run 3A and 4A because of overheating problems. We believe that it is very important to gather data with high b-values because in that way we will be able to use algorithms that provide very detailed tractography e.g. QBI [56], EQBI [15] and DSI[57]. We are expecting technical experts from Siemens to solve this problem very soon hopefully during the summer. Furthermore, we scanned some fruits and vegetables with fibre structure e.g. a mango and a pineapple but the signal was too weak to be useful for tractography validation.

However, from 1A and 2A we gathered tracts using software and got the beautiful and inspiring results shown in Fig. 1,1,10 and 11.

8 Future Plan

Second Year

- First priority at the moment is to start implementing our idea for obtaining more information from the actual diffusion signals in each voxel (model free approach avoiding the tensor, multi-tensor and ODF approaches) and use it in a global fashion to denoise our data. We know that in a voxel we can have a nearly infinite number of configurations and patterns. However we believe that with a multidimensional histogram analysis and dimensionality reduction we can find some basic patterns. For a simplified 2D example look Fig.12. In summary, what we will try to do is a local voxel-based clustering of the signal configurations. In order to reduce the configuration search space we are planning to try first linear dimensionality reduction e.g. PCA and nonlinear dimensionality reduction e.g. Isomap [54] or FastICA[31]. We would like then to cluster the different configurations in discrete patterns as shown in Fig. 12.

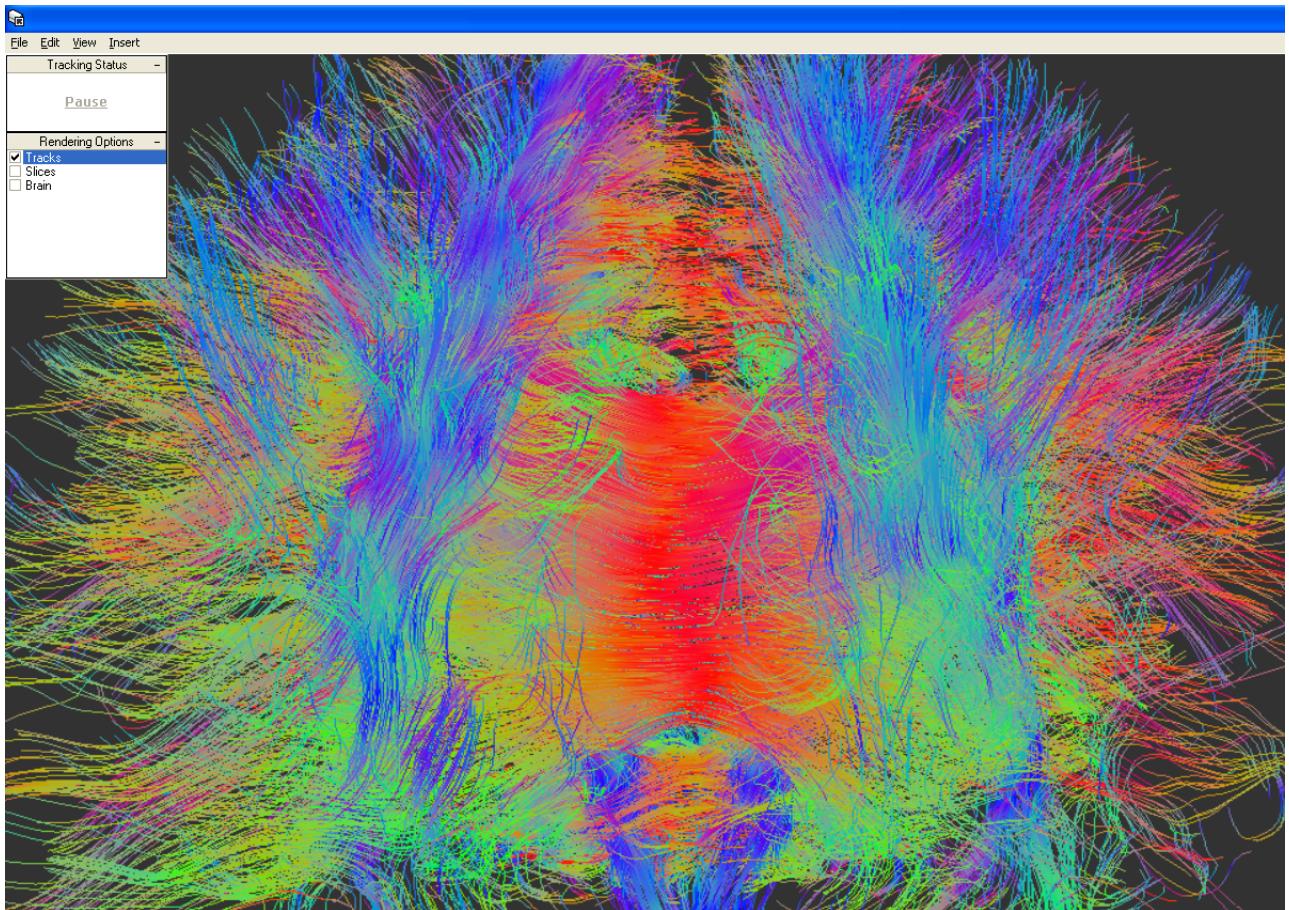


Figure 11: DSI Studio created this result only after changing the acquisition protocol used in CBU. DSI Studio is calculating this deterministic tractography using Runge-Kutta (RK). The colour coding shows the different orientations from the FA image.

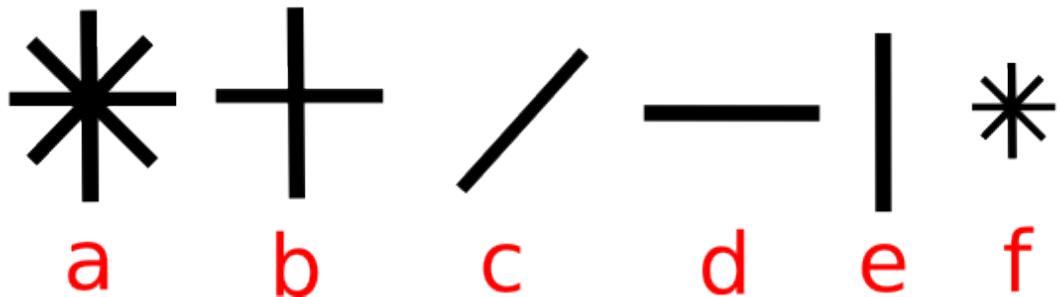


Figure 12: 2D simplified example of some patterns than can be found in a voxel: a) multiple fibre crossing, b) simple fibre crossing, c) diagonal fibre, d) horizontal, e) vertical fibre, f) multiple crossing. The difference in size between f and a means that f is more likely to be an actual crossing because the signal is very low in every direction. Low signal in dMRI means higher directional and less isotropy. Therefore, a is more isotropic than f i.e. f is more likely to be a fiber crossing than a. This is a fact not used at the moment in any other tractography methods.

It is important here to note that every configuration is not deterministic but probabilistic enabling for the possibility of errors. Error correction and denoising will be used in a neighbourhood level simultaneously in the hole brain data using discrete optimisation. The discrete optimisation algorithm that we are planning to use is based on the seminal work of Vladimir Kolmogorov[13] in Max-Flow.

Alternative: If the discrete optimisation idea does not show good results we will try to implement and extend the work of Özarslan and Pickalov[48] on fast reconstruction of the diffusion propagator or use compressed sensing[16] that had great success in computerised tomography (CT). The mathematics of CT have many similarities with these of dMRI therefore there is huge potential for algorithmic sharing.

2. After the denoising of our datasets we will try to implement probabilistic tracts which embed prior knowledge in a Bayesian fashion. For example in normal healthy brains there will always be an actual optic radiation underlying our datasets. Could we use this information in a Bayesian way? This idea was inspired by the work of Sherbondy et al[52] explained in section 8. We are also planning to compare the results against many other well known deterministic and probabilistic algorithms e.g. FACT, RK, FSL/FDT and Camino.
3. We are currently writing a review paper in collaboration with Dr. Williams, Dr. Brett, Dr. Nimmo-smith and Dr. Melie-García entitled “Finding connections with diffusion weighted imaging”. We hope that we will be able to finish this paper by the end of September. We are already half way through. The paper is planned to be published at the Journal of Cognitive Neuroscience and the target audience is psychologists not mathematicians or engineers who would like to understand the basics of graph and network theory for dMRI connectivity analysis. Hopefully, this paper will finish before the end of September 2009.
4. We would like to implement a theoretical acquisition model called Exact QBI [15] in the MRC-CBU Siemens scanner which will give us very detailed diffusion data very close to the resolution of DSI. This will be the first time that this model is implemented in a real scanner. However this acquisition depends on multi-shell data with very high b-values up to 10000 and we are waiting from Siemens for an answer if this is eligible in our scanner.

Alternative: There is a high possibility to drop this experiment from taking place at the MRC-CBU and try it at the WBIC where they have a small ball system which enables experiments with enormous gradient switches but unfortunately cannot be used with humans.

Final year

1. In the final year we will concentrate more on finding tracts that are similar across different subjects. Similarity parameters could be the length, curvature, thickness, torsion, distribution of thickness and others. In that way we hope to find solid landmarks that we can use to effectively co-register the subjects using tractography information and not classic FA as in FSL/TBSS.

2. We are also planning to acquire some synthetic or biological phantoms to validate our algorithms. For example Perrin et al. studied a complex phantom made from crossing hemodialysis fibres [47]. We share already some diffusion software phantoms (depicting DNA helices) obtained from UCLA. Unfortunately, global standard validation tools for dMRI are not available widely and this is a problem that we are trying to investigate. Roebroeck et al.[50] used a biological phantom, the optic chiasm in vitro which probably provides the best tissue-based crossing fibre.
3. We would like to combine tractography with surface reconstruction software e.g. Freesurfer and try to use the information from tractography to segment/parcellate the cortex in meaningful areas. Similar work was already published by Berhens[9] and Perrin[45]. We would like to extend these works using our registration described in 1.
4. Finally write the thesis, publish our results and make our software publicly available.

9 Conclusion

This is the first PhD course in MRC-CBU that is concentrated in diffusion MRI. Most of the time until this day was spent on understanding the theory, using the existing tools and making links and collaborations with other researchers who are more proficient in the field e.g. Dr. Williams on diffusion acquisitions and Dr. Melie-Garcia on connectivity analysis and graph theory. We had also progress developing our own software library in Python named TRN. TRN at the moment is able to calculate simple tensors, read and convert many different medical files, generate very complex graphics e.g. 4D density plots and many more options as described in section 5. We also analysed diffusion datasets using many different tools e.g. TrackVis, DTK, FSL, CAMBA, DSI Studio, Brain Visa, SPM and generated cortical surfaces using Freesurfer. We were happy to see lower FA with patients suffering from trichotillomania (see 6.1) and also generate extensive tractography implementing a new protocol with a cubic voxel size (see Fig 1, 2, 11) which hopefully will replace the default Siemens protocol used in CBU. Our primary concentration for the future is to investigate and implement a more meaningful tractography using machine learning and discrete optimisation. For this project we collaborate with two researchers from Computer Vision Group, Toshiba Research Laboratory in Cambridge, Dr. Vogiatzis and Dr. Hernández.

Finally, we envision tractography to become in the future the gold standard for registration of different brain modalities as today is the structural MRI and the Tailarach space. We also believe that diffusion tractography has a great potential to become a non-invasive navigation tool for surgical planning. However, current tractography is difficult to validate and visualise and can generate ghosts and artifacts. We are hoping to contribute the maximum towards the solution of these problems in the time left in this course.

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11 Appendix

11.1 TBSS

In collaboration with Dr. Boszic we tried to use FSL/TBSS to co-register many subjects together, define the mask in the mean FA image and then using TBSS de-project go back to the native diffusion space and do

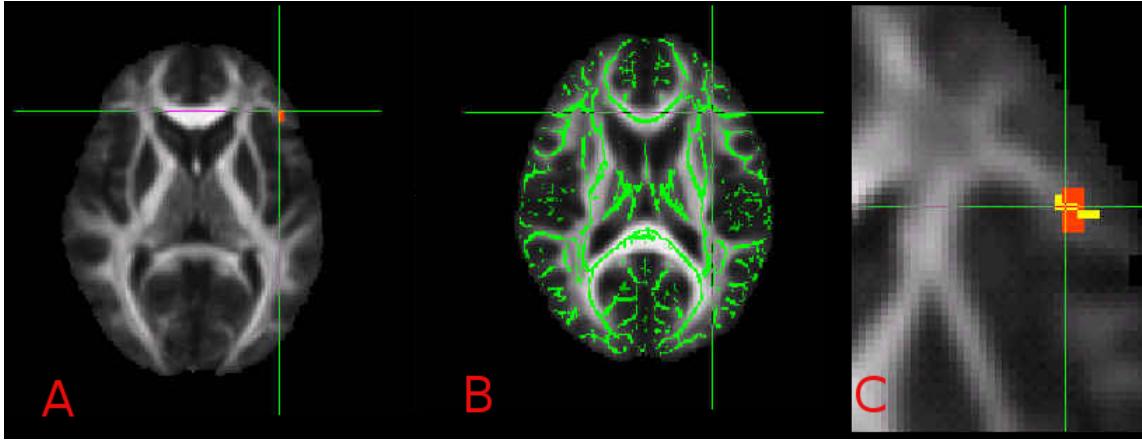


Figure 13: A: FA slice and seed, B: TBSS skeleton, C: After de-projection the masks were broken or very much de-morphed.

tractography there. We tried this idea because it is very time consuming to define seeds in every single subject it could take many weeks and it can be very biased. So, this automation idea could have reduced our analysis time dramatically. Unfortunately, the nonlinear nature of TBSS and the high dependence on the skeleton was not able to de-project the masks efficiently i.e. many masks were broken. We hope that in future versions of TBSS this will be resolved.

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