ICPC Templates For HKing

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Contents

1 Graph

1.1 Dinic

```
const int inf = 0x3f3f3f3f;
const int N = 205;
const int M = 1205;
struct Edge{
   int v,f,nxt;
};
struct Dicnic{
   int src,sink;
   int g[N],en;
   Edge e[M*2];
   int level[N];
   void _addEdge(int u,int v,int f){
      e[en].v=v;
      e[en].f=f;
      e[en].nxt=g[u];
      g[u]=en++;
   }
   void addEdge(int u,int v,int f){
      _addEdge(u,v,f);
      _addEdge(v,u,0);
   }
   void init(){
      en=0;
      memset(g,-1,sizeof(g));
   }
   int q[N],front,rear;
   bool bfs(){
      memset(level,0,sizeof(level));
      level[src]=1;
      front=0; rear=1;
      q[0]=src;
      while(front<rear){
         int u=q[front++];
         if(u==sink)return 1;
         for(int i=g[u];i!=-1;i=e[i].nxt){
            int v=e[i].v,f=e[i].f;
            if(!level[v]&&f){
               level[v]=level[u]+1;
               q[rear++]=v;
            }
         }
      }
      return 0;
   }
   int dfs(int u,int delta){
      if(u==sink || delta==0)return delta;
      int ret=0;
      for(int i=g[u];i!=-1;i=e[i].nxt){
         int v=e[i].v, f=e[i].f;
         if(level[v]==level[u]+1&&f){
            int minf=min(delta-ret,f);
            f=dfs(v,minf);
            e[i].f-=f;
            e[i^1].f+=f;
            delta-=f;
            ret+=f;
            if(ret==delta)return ret;
         }
      }
      return ret;
   }
   int maxflow(int _src,int _sink){
      src=_src;
      sink=_sink;
      int ret=0;
      while(bfs())ret+=dfs(src,inf);
      return ret;
   }
}dicnic_solver;
```

1.2 KM

```
// eg: soj 1013
const int N = 105;
const int inf = 1000000000;
struct KM{
   int w[N][N],x[N],y[N];
   int px[N],py[N],sy[N],sk[N],pr[N];
   int lx,ly,n;
   void adjust(int v){
      sy[v]=py[v];
      if(px[sy[v]]!=-2)adjust(px[sy[v]]);
   }
   int solve(int _n,int _w[][N]){
      n=_n;
      memcpy(w,_w,sizeof(w));
      return km();
   }
   bool find(int v){
      for(int i=0;i<n;++i)if(py[i]==-1){
         if(sk[i]>x[v]+y[i]-w[v][i]){
            sk[i]=x[v]+y[i]-w[v][i];
            pr[i]=v;
         }
         if(x[v]+y[i]==w[v][i]){
            py[i]=v;
            if(sy[i]==-1){
               adjust(i);
               return 1;
            }
            if(px[sy[i]]!=-1)continue;
            px[sy[i]]=i;
            if(find(sy[i]))return 1;
        }
    }
    return 0;
}
int km(){
    int i,j,m;
    for(i=0;i<n;++i){
        sy[i]=-1;
        y[i]=0;
    }
    for(i=0;i<n;++i){
        x[i]=0;
        for(j=0;j<n;++j){
            x[i]=max(x[i],w[i][j]);
        }
    }
    bool f;
    for(i=0;i<n;++i){
        for(j=0;j<n;++j){
            px[j]=py[j]=-1;
            sk[j]=inf;
        }
        px[i]=-2;
        if(find(i))continue;
        f=0;
        while(!f){
            m=inf;
            for(j=0;j<n;++j)if(py[j]==-1)m=min(m,sk[j]);
            for(j=0;j<n;++j){
                if(px[j]!=-1)x[j]-=m;
                if(py[j]!=-1)y[j]+=m;else sk[j]-=m;
            }
            for(j=0;j<n;++j)if(py[j]==-1&&!sk[j]){
                py[j]=pr[j];
                if(sy[j]==-1){
                    adjust(j);
                    f=1;
                    break;
                }
                px[sy[j]]=j;
                if(find(sy[j])){
                    f=1;
                    break;
                }
            }
        }
    }
    int ans=0;
    for(i=0;i<n;++i)ans+=w[sy[i]][i];
```

```
      return ans;
   }
}km_solver;
```

1.3 Mixed Euler Circuit

```
// eg: soj 1066
const int N = 205;
int degree[N],n;
void init(){
   dicnic_solver.init();
   int m,a,b,c;
   scanf("%d%d",&n,&m);
   memset(degree,0,sizeof(degree));
   while(m--){
      // c=0,a<->b; c=1,a->b
      scanf("%d%d%d",&a,&b,&c);
      a--; b--;
      degree[a]--;
      degree[b]++;
      if(!c)dicnic_solver.addEdge(a,b,1);
   }
}
bool work(){
   int ans=0;
   for(int i=0;i<n;++i)if(degree[i]&1)return 0;
   for(int i=0;i<n;++i){
      if(degree[i]<0){
         dicnic_solver.addEdge(n,i,-degree[i]/2);
         ans-=degree[i]/2;
      }else if(degree[i]>0){
         dicnic_solver.addEdge(i,n+1,degree[i]/2);
      }
   }
   return dicnic_solver.maxflow(n,n+1)>=ans;
}
void solve(){
   puts(work()?"possible":"impossible");
}
int main(){
   int t;
   scanf("%d",&t);
   while(t--){
      init();
      solve();
   }
   return 0;
}
```

2 Tree

2.1 Divide And Conquer Tree

```
//hdu 4812 D Tree
#include <iostream>
#include <cstdio>
#include <cstring>
#include <vector>
#pragma comment(linker,"/STACK:102400000,102400000")
using namespace std;
const int maxn = 1e5 + 10;
const int md = 1e6 +3;
int N,K;
vector<int > edge[maxn];
void add_edge(int from,int to) {
  edge[from].push_back(to);
}
void init() {
  for(int i = 1;i <= N;i ++) edge[i].clear();
}
int vi[maxn];
int vis[maxn];
int root;
int mi;
int son[maxn];
int hash[md + 10];
int vers[md + 10];
int verc;
pair<int , int > ans;
int fastpow(int x,int y) {
  int ret = 1 ,mul = x;
  while(y) {
    if(y & 1 ) ret = 1LL * mul * ret % md;
    mul = 1LL * mul* mul % md;
    y >>= 1;
  }
  return ret;
}
int comm[md + 10];
void inv1() {
  for(int i = 0;i < md;i ++) {
    comm[i] = fastpow(i,md - 2);
  }
}
int inv(int t) {
  return comm[t];
}
void getroot(int t,int sz) {
  vis[t] = true;
  son[t] = 1;
  int mx = 0;
  for(int i = 0;i < edge[t].size();i ++) {
    int nxt = edge[t][i];
    if(!vis[nxt]) {
      getroot(nxt,sz);
      son[t] += son[nxt];
      mx = max(mx,son[nxt]);
    }
  }
  mx = max(mx,sz - son[t]);
  if(mx <= mi) {
    root = t;
    mi = mx;
  }
  vis[t] = false;
}
void dfs(int t,int mul,int ri) {
  vis[t] = true;
  //query
  mul =1LL * mul * vi[t] % md;
  if(1LL * mul * ri % md == K) {
    pair<int ,int > tmp = pair<int ,int > (min(root,t),max(root,t));
    if(tmp < ans) ans = tmp;
  }
  int q = 1LL* inv(1LL * mul * ri % md) * K % md;
  if(vers[q] == verc && hash[q]!= 0 ) {
    pair<int ,int > tmp = pair<int ,int > (min(t,hash[q]),max(t,hash[q]));
    if(tmp < ans) ans = tmp;
  }
  son[t] = 1;
  for(int i = 0;i < edge[t].size();i ++) {
    int nxt = edge[t][i];
    if(!vis[nxt]) {
      dfs(nxt,mul,ri);
      son[t] += son[nxt];
    }
  }
  //set
  if(vers[mul] != verc ) {
    vers[mul] = verc;
    hash[mul] = t;
  }
  hash[mul] = min(hash[mul],t);
  vis[t] = false;
}
void work(int t,int sz) {
  mi = sz;
  getroot(t,sz);
  // dfs
  int rt = root;
  vis[rt] =true;
  verc ++;
  for(int i = 0;i < edge[root].size();i ++) {
    int nxt = edge[rt][i];
    if(!vis[nxt]) {
      dfs(nxt,1,vi[rt] % md);
    }
  }
  for(int i = 0;i < edge[rt].size();i ++) {
    int nxt = edge[rt][i];
    if(!vis[nxt]) {
      work(nxt,son[rt]);
    }
  }
}
int main() {
  inv1();
  verc = 0;
  while(scanf("%d%d",&N,&K) != EOF) {
    init();
    for(int i = 1;i <= N;i ++) {
      scanf("%d",&vi[i]);
    }
    for(int i = 0;i < N - 1;i ++) {
      int u,v;
      scanf("%d%d",&u,&v);
      add_edge(u,v);
      add_edge(v,u);
    }
    memset(vis,0,sizeof(vis));
    ans = pair<int ,int > (N+1,N+1);
    work(1,N);
    if(ans.first == N+1 && ans.second == N + 1) {
      puts("No solution");
    } else {
      printf("%d %d\n",ans.first,ans.second);
    }
  }
}
```

2.2 Link Tree

```
//HDU 3966
//operation1 path c1 to c2 plus k
//operation2 path c1 to c2 minus k
#include <iostream>
#include <cstdio>
#include <algorithm>
#include <vector>
#include <cstring>
#pragma comment(linker, "/STACK:1024000000,1024000000")
using namespace std;
#define lc (o<<1)
#define rc (o<<1|1)
int N,M,P;
```

```cpp
const int maxn = 100010;
vector<int > edge[maxn];
int ai[maxn];
void add_edge(int from,int to) {
  edge[from].push_back(to);
}
void init() {
  for(int i = 1;i <= N;i ++) edge[i].clear();
}
int son[maxn]; // size of children
int fa[maxn];
int wn[maxn]; //index in segment
int wcnt;
int vis[maxn];
int dep[maxn]; // depth
int top[maxn]; // link fa
//Tree link
void dfs1(int t,int d) {
  vis[t] = true;
  dep[t] = d;
  son[t] = 1;
  for(int i = 0;i < edge[t].size();i ++) {
    int nxt = edge[t][i];
    if(!vis[nxt]) {
      fa[nxt] = t;
      dfs1(nxt,d + 1);
      son[t] += nxt;
    }
  }
  vis[t] = false;
}
void dfs2(int t) {
  vis[t] = true;
  wn[t] = wcnt ++;
  bool first = true;
  int index = -1;
  for(int i = 0;i < edge[t].size();i ++) {
    int nxt = edge[t][i];
    if(!vis[nxt]) {
      if(first) {
        first =false;
        index = nxt;
      }
      if(son[nxt] > son[index]) {
        index= nxt;
      }
    }
  }
  if(!first ) {
    top[index] = top[t];
    dfs2(index);
    for(int i = 0;i < edge[t].size();i ++) {
      int nxt = edge[t][i];
      if(!vis[nxt] && nxt != index) {
        top[nxt] = nxt;
        dfs2(nxt);
      }
    }
  }
  vis[t] = false;
}
//segment tree
int addv[maxn << 2];
void add(int o,int l,int r,int y1,int y2,int v) {
  if(y1 <= l && r <= y2) {
    addv[o] += v;
  } else {
    int m = (l + r) >> 1;
    if(y1 <= m) add(lc,l,m,y1,y2,v);
    if(m < y2) add(rc,m+1,r,y1,y2,v);
  }
}
void query(int o,int l,int r,int x,int & ans) {
  if(l == r && r == x) {
    ans += addv[o];
  } else {
    int m = (l + r ) >> 1;
    ans += addv[o];
    if(x <= m ) {
      query(lc,l,m,x,ans);
    } else {
      query(rc,m+1,r,x,ans);
    }
  }
}
void init_seg() {
  memset(addv,0,sizeof(addv));
}
char buff[5];
int main() {
  while(~scanf("%d%d%d",&N,&M,&P) ) {
    init();
    for(int i = 1;i <= N;i ++) {
      scanf("%d",&ai[i]);
    }
    for(int i = 0;i < M;i ++) {
      int u,v;
      scanf("%d%d",&u,&v);
      add_edge(u,v);
      add_edge(v,u);
    }
    dfs1(1,1);
    wcnt = 0;
    top[1] = 1;
    dfs2(1);
    init_seg();
  while(P --) {
    scanf("%s",buff);
    if(buff[0] == 'I' || buff[0] == 'D') {
      int c1,c2,k;
      scanf("%d%d%d",&c1,&c2,&k);
      if(buff[0] == 'D') k = - k;
      /// query path
      while(top[c1] != top[c2]) {
        int f1 = top[c1];
        int f2 = top[c2];
        if(dep[f1] < dep[f2]) {
          swap(f1,f2);
          swap(c1,c2);
        }
        add(1,0,N - 1,wn[f1],wn[c1],k);
        c1 = fa[f1];
      }
      if(dep[c1] < dep[c2]) {
        swap(c1,c2);
      }
      add(1,0,N - 1,wn[c2],wn[c1],k);
    } else if(buff[0] == 'Q') {
      int d;
      scanf("%d",&d);
      int ans = 0;
      query(1,0,N-1,wn[d],ans);
      ans += ai[d];
      printf("%d\n",ans);
    }
  }
 }
}
```

2.3 Segment Tree

```
//HDU 4578
//segment plus mul power sum
#include <cstdio>
#include <algorithm>
using namespace std;
#define lc (o<<1)
#define rc (o<<1|1)
const int maxn = 100010;
const int md = 10007;
int sumv1[maxn<<2], sumv2[maxn<<2], sumv3[maxn<<2];
int addv[maxn<<2], setv[maxn<<2], timv[maxn<<2];
void pushdown(int o) {
  if (setv[o] >= 0) {
    setv[lc] = setv[rc] = setv[o];
    addv[lc] = addv[rc] = 0;
    timv[lc] = timv[rc] = 1;
    setv[o] = -1;
  }
  if (timv[o] != 1) {
    addv[lc] *= timv[o];
    addv[lc] %= md;
    addv[rc] *= timv[o];
    addv[rc] %= md;
    timv[lc] *= timv[o];
    timv[lc] %= md;
    timv[rc] *= timv[o];
    timv[rc] %= md;
    timv[o] = 1;
  }
  if (addv[o] > 0) {
    addv[lc] += addv[o];
    addv[lc] %= md;
    addv[rc] += addv[o];
    addv[rc] %= md;
    addv[o] = 0;
  }
}
void maintain(int o,int l,int r) {
  if (l == r) {
    if (setv[o] != -1) {
      sumv1[o] = setv[o];
      setv[o] = -1;
    }
    if (timv[o] != 1) {
      sumv1[o] *= timv[o];
      timv[o] = 1;
      sumv1[o] %= md;
    }
    if (addv[o] > 0) {
      sumv1[o] += addv[o];
      sumv1[o] %= md;
      addv[o] = 0;
    }
    sumv2[o] = sumv1[o] * sumv1[o] % md;
    sumv3[o] = sumv1[o] * sumv2[o] % md;
  } else {
    sumv1[o] = (sumv1[lc] + sumv1[rc]) % md;
    sumv2[o] = (sumv2[lc] + sumv2[rc]) % md;
    sumv3[o] = (sumv3[lc] + sumv3[rc]) % md;
    if (setv[o] != -1) {
      sumv1[o] = setv[o] * (r - l +1) % md;
      sumv2[o] = setv[o] * setv[o] % md * (r - l + 1) % md;
      sumv3[o] = setv[o] * setv[o] % md * setv[o] % md * (r - l + 1) % md;
    }
    if (timv[o] != 1) {
      sumv1[o] *= timv[o];
      sumv1[o] %= md;
      sumv2[o] *= timv[o] * timv[o] % md;
      sumv2[o] %= md;
      sumv3[o] *= timv[o] * timv[o] % md * timv[o] % md;
      sumv3[o] %= md;
    }
    if (addv[o] > 0) {
      int tmp1 = sumv1[o];
      sumv1[o] += addv[o] * (r - l + 1) % md;
      sumv1[o] %= md;
      int tmp2 = sumv2[o];
      int tmp3 = sumv3[o];
      sumv2[o] = (tmp2 + 2*tmp1%md * addv[o]%md + addv[o] * addv[o] %md* (r -
          l +1)%md) % md;
      sumv3[o] = tmp3 + 3 * tmp2%md * addv[o] % md + 3 * tmp1 % md *
          addv[o]%md * addv[o] % md + addv[o] * addv[o] % md * addv[o] % md *
          (r - l + 1) %md;
      sumv3[o] %= md;
    }
  }
}
void setq(int o,int l,int r,int y1,int y2,int v) {
  if (y1 <= l && r <= y2) {
    setv[o] = v;
    addv[o] = 0;
    timv[o] = 1;
  } else {
    pushdown(o);
    int m = (l + r) >> 1;
    if (y1 <= m) setq(lc,l,m,y1,y2,v);
    else maintain(lc,l,m);
    if (m < y2) setq(rc,m+1,r,y1,y2,v);
    else maintain(rc,m+1,r);
  }
  maintain(o,l,r);
}
void addq(int o,int l,int r,int y1,int y2,int v) {
  if (y1 <= l && r <= y2) {
    addv[o] += v;
    addv[o] %= md;
  } else {
    pushdown(o);
    int m = (l +r) >> 1;
    if (y1 <= m ) addq(lc,l,m,y1,y2,v);
    else maintain(lc,l,m);
    if (m < y2) addq(rc,m+1,r,y1,y2,v);
    else maintain(rc,m+1,r);
  }
  maintain(o,l,r);
}
void timq(int o,int l,int r,int y1,int y2,int v) {
  if (y1 <= l && r <= y2) {
    timv[o] *= v;
    timv[o] %= md;
    addv[o] *= v;
    addv[o] %= md;
  } else {
    pushdown(o);
    int m = (l + r) >> 1;
    if (y1 <= m) timq(lc,l,m,y1,y2,v);
    else maintain(lc,l,m);
    if (m < y2) timq(rc,m+1,r,y1,y2,v);
    else maintain(rc,m+1,r);
  }
  maintain(o,l,r);
}
int ans1, ans2, ans3;
void query(int o,int l,int r,int y1,int y2,int add,int ti) {
  if (setv[o] > 0) {
    add = ti * addv[o] % md + add;
    ti = ti * timv[o] % md;
    int len = min(r,y2) - max(y1,l) + 1;
    int tmp1 = setv[o] * len % md * ti % md;
    int tmp2 = setv[o] * setv[o] % md * len % md * ti%md * ti %md;
    int tmp3 = setv[o] * setv[o] % md * setv[o] % md * len % md *ti %md* ti %
        md* ti % md;
    int _sum1 = tmp1 + add * len % md;
    _sum1 %= md;
    int _sum2 = (tmp2 + 2* tmp1 * add % md + add * add % md * len % md) % md;
    int _sum3 = (tmp3 + 3 * tmp2 * add % md + 3 * tmp1 * add % md * add % md
        + len * add % md * add % md *add % md) % md;
    ans1 = (ans1 + _sum1) % md;
    ans2 = (ans2 + _sum2) % md;
    ans3 = (ans3 + _sum3) % md;
    return ;
  }
  if (y1 <= l && r <= y2) {
    int tmp1 = sumv1[o] * ti % md;
    int tmp2 = sumv2[o] * ti % md * ti % md;
    int tmp3 = sumv3[o] * ti % md * ti % md * ti % md;
    int _sum = tmp1 + add * (r - l + 1) % md;
    int _sum2 = tmp2 + 2* tmp1 * add % md + add * add % md * (r - l + 1) % md;
    int _sum3 = tmp3 + 3 * tmp2 % md * add % md + 3 * tmp1 % md * add % md *
        add % md + add * add % md * add % md * (r- l + 1) % md;
    _sum %= md;
    _sum2 %= md;
    _sum3 %= md;
    ans1 = (ans1 + _sum) % md;
    ans2 = (ans2 + _sum2) % md;
    ans3 = (ans3 + _sum3) % md;

  } else {
    int m = (l +r ) >> 1;
    if (y1 <= m) query(lc,l,m,y1,y2,(ti * addv[o] % md + add) % md,ti *
        timv[o] % md);
    if (m < y2) query(rc,m+1,r,y1,y2,(ti * addv[o] % md + add) % md,ti *
        timv[o] % md);
  }
}
```

```
void init(int o,int l,int r) {
  setv[o] = -1;
  timv[o] = 1;
  addv[o] = 0;
  sumv1[o] = sumv2[o] = sumv3[o] = 0;
  if (l == r) {
  } else {
    int m = (l + r) >> 1;
    init(lc,l,m);
    init(rc,m+1,r);
  }
}
int main() {
  int N,M;
  while (scanf("%d%d",&N,&M)==2 && N && M) {
    init(1,1,N);
    while (M --) {
      int cmd,x,y,c;
      scanf("%d%d%d%d",&cmd,&x,&y,&c);
      if(cmd == 1) {
        c %= md;
        addq(1,1,N,x,y,c);
      } else if(cmd == 2) {
        c %= md;
        timq(1,1,N,x,y,c);
      } else if(cmd == 3) {
        c %= md;
        setq(1,1,N,x,y,c);
      } else if(cmd == 4) {
        ans1 = ans2 = ans3 = 0;
        query(1,1,N,x,y,0,1);
        if(c == 1) {
          printf("%d\n",ans1);
        } else if(c == 2){
          printf("%d\n",ans2);
        } else if(c == 3) {
          printf("%d\n",ans3);
        }
      }
    }
  }
}
```

2.4 Splay Tree

```
#include <cstdio>
#include <iostream>
using namespace std;
struct Node {
  Node* ch[2];
  int v, s, flip;
  void maintain() {
    s = 1 + ch[0]->s + ch[1]->s;
  }
  void pushdown() {
    if (flip) {
      flip = 0;
      swap(ch[0], ch[1]);
      ch[0]->flip ^= 1;
      ch[1]->flip ^= 1;
    }
  }
  int cmp(int k) const {
    int d = k - ch[0]->s;
    if (d == 1) return -1;
    return d <= 0 ? 0 : 1;
  }
};
Node* null = new Node();
void rotate(Node* &o, int d) {
  Node* k = o->ch[d^1];
  o->ch[d^1] = k->ch[d];
  k->ch[d] = o;
  o->maintain();
  k->maintain();
  o = k;
}
void splay(Node* &o, int k) {
  o->pushdown();
  int d = o->cmp(k);
  if (d == 1) k -= o->ch[0]->s + 1;
  if (d != -1) {
    Node* p = o->ch[d];
    p->pushdown();
    int d2 = p->cmp(k);
    int k2 = (d2 == 0) ? k : k - p->ch[0]->s - 1;
    if (d2 != -1) {
      splay(p->ch[d2], k2);
      if (d == d2) {
        rotate(o, d^1);
      } else {
        rotate(o->ch[d], d);
      }
    }
    rotate(o, d^1);
  }
}
Node* merge(Node* left, Node* right) { // make sure left != null
  splay(left, left->s);
  left->ch[1] = right;
  left->maintain();
  return left;
}
void split(Node* o, int k, Node* &left, Node* &right) { // make sure 1 <= k
```

```
    <= o->s
  splay(o, k);
  left = o;
  right = o->ch[1];
  o->ch[1] = null;
  left->maintain();
}
const int maxn = 300000 + 10;
struct SS {
  int n;
  Node seq[maxn];
  Node* root;
  Node* build(int sz) {
    if (!sz) return null;
    Node* L = build(sz/2);
    Node* o = &seq[++n];
    o->v = n-1;
    o->flip = 0;
    o->ch[0] = L;
    o->ch[1] = build(sz - sz/2 - 1);
    o->maintain();
    return o;
  }
  void init(int sz) {
    n = 0;
    null->s = null->flip = 0;
    root = build(sz);
  }
  void print(Node *o) {
    if (o != null) {
      o->pushdown();
      print(o->ch[0]);
      if (o->v) {
        if (o->v != 1) putchar(' ');
        printf("%d", o->v);
      }
      print(o->ch[1]);
    }
  }
} ss;
int n, m, a, b, c;
char op[10];
int main() {
  while (scanf("%d%d",&n,&m) == 2 && n != -1 && m != -1) {
    ss.init(n+1);
    Node *t1, *t2, *t3;
    while(m--){
      scanf("%s",op);
      if(op[0]=='C'){ // split [a,b], put it after c
        scanf("%d%d%d",&a,&b,&c);
        split(ss.root, b+1, t1, t2);
        split(t1, a, t1, t3);
        ss.root = merge(t1, t2);
        split(ss.root, c+1, t1, t2);
        ss.root = merge(merge(t1, t3), t2);
      } else { // flip [a,b]
        scanf("%d%d",&a,&b);
        split(ss.root, b+1, t1, t3);
        split(t1, a, t1, t2);
        t2->flip ^= 1;
        ss.root = merge(merge(t1, t2), t3);
      }
    }
    ss.print(ss.root);
    puts("\n");
  }
}
```

2.5 Treap

```
struct Node {
  Node *ch[2]; // 0-left 1-right
  int r, v, s; // rank, val, #node
  Node(int v): v(v) {
    ch[0] = ch[1] = NULL;
    r = rand();
    s = 1;
  }
  int cmp(int x) const {
    if (x == v) return -1;
    return x < v ? 0 : 1;
  }
  void maintain() { // maintain #node
    s = 1;
    if (ch[0] != NULL) s += ch[0]->s;
    if (ch[1] != NULL) s += ch[1]->s;
  }
};
void rotate(Node* &o, int d) {
  Node* k = o->ch[d^1];
  o->ch[d^1] = k->ch[d];
  k->ch[d] = o;
  o->maintain();
  k->maintain();
  o = k;
}
void insert(Node* &o, int x) {
  if (o == NULL) {
    o = new Node(x);
  } else {
    int d = o->cmp(x);
    if (d != -1) { // same ele won't be inserted
      insert(o->ch[d], x);
      if (o->ch[d]->r > o->r) rotate(o, d^1);
    }
  }
  o->maintain();
}
void remove(Node* &o, int x) {
  if (o == NULL) return ; // ele to be removed not exist
  int d = o->cmp(x);
  if (d == -1) {
    Node* ret = o;
    if (o->ch[0] != NULL && o->ch[1] != NULL) {
      int d2 = (o->ch[0]->r > o->ch[1]->r ? 1 : 0);
      rotate(o, d2);
      remove(o->ch[d2], x);
    } else {
      if (o->ch[0] == NULL) o = o->ch[1];
      else o = o->ch[0];
      delete ret;
    }
  } else {
    remove(o->ch[d], x);
  }
  if (o) o->maintain();
}
int find(Node* o, int x) {
  while (o != NULL) {
    int d = o->cmp(x);
    if (d == -1) return 1;
    else o = o->ch[d];
  }
  return 0;
}
int kth_big(Node* o, int k) {
  if (o == NULL || k <= 0 || k > o->s) return 0;
  int s = o->ch[1] == NULL ? 0 : o->ch[1]->s;
  if (k == s+1) return o->v;
  else if (k <= s) return kth_big(o->ch[1], k);
  else return kth_big(o->ch[0], k-s-1);
}
int kth_small(Node* o, int k) {
  if (o == NULL || k <= 0 || k > o->s) return 0;
  int s = o->ch[0] == NULL ? 0 : o->ch[0]->s;
  if (k == s) return o->v;
  else if (k < s) return kth_small(o->ch[0], k);
  else return kth_small(o->ch[1], k-s-1);
}
void merge(Node* &src, Node* &dest) {
  if (src == NULL) return ;
  merge(src->ch[0], dest);
  merge(src->ch[1], dest);
  insert(dest, src->v);
  delete src;
  src = NULL;
}
```

```cpp
void clear(Node* &o) {
  if (o == NULL) return ;
  clear(o->ch[0]);
  clear(o->ch[1]);
  delete o;
  o = NULL;
}
```

3 Geometry

3.1 Basic Struct and Algorithm

```cpp
struct Point {
  double x, y;
  Point(double x=0, double y=0):x(x),y(y){}
};

typedef Point Vector;

Vector operator + (const Vector &A, const Vector &B) { return
    Vector(A.x+B.x, A.y+B.y); }
Vector operator - (const Point &A, const Point &B) { return Vector(A.x-B.x,
    A.y-B.y); }
Vector operator * (const Vector &A, double p) { return Vector(A.x*p, A.y*p);
    }
double Dot(const Vector &A, const Vector &B) { return A.x*B.x + A.y*B.y; }
double Cross(const Vector &A, const Vector &B) { return A.x*B.y - A.y*B.x; }
double Length(const Vector &A) { return sqrt(Dot(A, A)); }
Vector Normal(const Vector &A) { double L = Length(A); return Vector(-A.y/L,
    A.x/L); }

struct Line {
  Point P;
  Vector v;
  double ang;
  Line() {}
  Line(Point P, Vector v):P(P),v(v){ ang = atan2(v.y, v.x); }
  bool operator < (const Line &L) const {
    return ang < L.ang;
  }
};

// if $p$ is on the left side of $L$
bool OnLeft(const Line &L, const Point &p) {
  return Cross(L.v, p-L.P) > 0;
}

// intersection of line $a$ and $b$
Point GetLineIntersection(const Line &a, const Line &b) {
  Vector u = a.P-b.P;
  double t = Cross(b.v, u) / Cross(a.v, b.v);
  return a.P+a.v*t;
}
```

3.2 Polygon Area

```
double PolygonArea(vector<Point> p) {
  int n = p.size();
  double area = 0;
  for(int i = 1; i < n-1; i++)
    area += Cross(p[i]-p[0], p[i+1]-p[0]);
  return area/2;
}
```

3.3 Half Plane Intersection

```
const double eps = 1e-6;
// intersection of areas (leftside of lines)
vector<Point> HalfplaneIntersection(vector<Line> L) {
  int n = L.size();
  sort(L.begin(), L.end());
  int first, last;
  vector<Point> p(n);
  vector<Line> q(n);
  vector<Point> ans;
  q[first=last=0] = L[0];
  for(int i = 1; i < n; i++) {
    while(first < last && !OnLeft(L[i], p[last-1])) last--;
    while(first < last && !OnLeft(L[i], p[first])) first++;
    q[++last] = L[i];
    if(fabs(Cross(q[last].v, q[last-1].v)) < eps) {
      last--;
      if(OnLeft(q[last], L[i].P)) q[last] = L[i];
    }
    if(first < last) p[last-1] = GetLineIntersection(q[last-1], q[last]);
  }
  while(first < last && !OnLeft(q[first], p[last-1])) last--;
  if(last - first <= 1) return ans;
  p[last] = GetLineIntersection(q[last], q[first]);
  for(int i = first; i <= last; i++) ans.push_back(p[i]);
  return ans;
}
```

4 Math

4.1 China Remainder Theory

```
// china remainder theory, no matter whether gcd(m[i],m[j])=1
LL CRT(const vector<LL>&m, const vector<LL> &b){
 bool flag = false;
 LL x, y, i, d, result, a1, m1, a2, m2, Size = m.size();
 m1 = m[0], a1 = b[0];
 for(int i = 1; i < Size; i++){
   m2 = m[i], a2 = b[i];
   d = exgcd(m1, m2, x, y);
   if ((a2 - a1) % d != 0) flag = true;
   result = (mul_mod(x, (a2 - a1) / d, m2) % m2 + m2) % m2;
   LL tmp = m1;
   m1 = m1 / d * m2;
   a1 = (a1 + mul_mod(tmp, result, m1)) % m1;
   a1 = (a1 % m1 + m1) % m1;
 }
 if (flag) return -1;
 else return a1;
}
```

4.2 Decompose

```
// eg: poj 3471
const int maxn = 10000000;
const int maxp = 700000; // about maxn/log(maxn)
struct Factor{ // factor as p^num
  int p, num;
};
struct DeComposer {
  DeComposer() { gen_primes(); }
  bool vis[maxn+5];
  int pn, prime[maxp];
  void sieve() {
    int m = (int)sqrt(maxn+0.5);
    memset(vis,0,sizeof(vis));
    for(int i=2;i<=m;++i)if(!vis[i])
      for(int j=i*i;j<=maxn;j+=i)vis[j]=1;
  }
  void gen_primes() {
    sieve();
    pn = 0;
    for (int i = 2; i <= maxn; ++ i) {
      if (!vis[i]) prime[pn++] = i;
    }
  }
  int fcn;
  Factor fc[64]; // x = p1^a1 * p2^a2 * ...
  int fn, factor[maxp]; // all y satisify y|x
  void decompose2(int x,int d){
    if(d==fcn){
      factor[fn++] = x;
    } else {
      for(int i = 0; i <= fc[d].num; ++ i) {
        decompose2(x, d+1);
        x *= fc[d].p;
      }
    }
  }
  void decompose1(int x) {
    fcn = 0;
    for(int i = 0; i < pn && prime[i] * prime[i] <= x; ++ i) if (x % prime[i]
        == 0) {
      fc[fcn].p = prime[i];
      fc[fcn].num = 0;
      while(x % prime[i] == 0) {
        fc[fcn].num ++;
        x /= prime[i];
      }
      fcn ++;
    }
    if (x > 1) {
      fc[fcn].p = x;
      fc[fcn].num = 1;
      fcn ++;
    }
  }
  void decompose(int x){
    decompose1(x);
    fn = 0;
    decompose2(1,0);
  }
} dc_solver;
```

4.3 Euler Phi

```
// #x that x<=n && gcd(x,n)==1
int euler_phi(int n) {
  int m = (int)sqrt(n+0.5);
  int ans = n;
  for (int i = 2; i <= m; ++ i) if (n % i == 0) {
    ans = ans / i * (i-1);
    while (n%i == 0) n /= i;
  }
  if (n > 1) ans = ans / n * (n-1);
  return ans;
}
int phi[maxn];
void phi_table(int n) {
  for (int i = 2; i <= n; ++ i) phi[i] = 0;
  phi[1] = 1;
  for (int i = 2; i <= n; ++ i) {
    if (!phi[i]) {
      for (int j = i; j <= n; j += i) {
        if (!phi[j]) phi[j] = j;
        phi[j] = phi[j] / i * (i-1);
      }
    }
    phi[i] += phi[i-1];
  }
}
```

4.4 Extend GCD

```
// a * x + b * y = d, |x| + |y| get the minimum
LL exgcd(LL a, LL b, LL &d, LL &x, LL &y){
 if (a) { x = 0; y = 1; return a; }
 else { exgcd(b, a%b, d, y, x); y -= x*(a/b); }
}
```

4.5 Integer Inverse

```
LL inv1(LL a, LL n) { // a^-1 under n
 LL d, x, y;
 gcd(a,n,d,x,y);
 return d == 1 ? (x+n)%n : -1;
}
LL inv2(LL a, LL p) { // in case that p is a prime
 return pow_mod(a, p-2, p);
}
```

4.6 Line Mod

```
// ax = b (mod n)
// let d = gcd(a,n), use exgcd to solve ax + ny = d
// if b|d, then there are #ans=d, otherwise, no solution
vector<LL> line_mod(LL a, LL b, LL n) {
 LL x, y;
 exgcd(a,n,x,y);
 vector<LL>ans;
 ans.clear();
 if(b%d==0){
  x%=n; x+=n; x%=n;
  ans.push_back(x*(b/d)%(n/d));
  for(LL i=1;i<d;++i){
   ans.push_back((ans[0]+i*n/d)%n);
  }
 }
 return ans;
}
```

4.7 Log Mod

```
// eg: hdu 2815
// d*a^(x-c) = b (mod n), make sure that (a,n) = 1 and (d,n) = 1
map<LL,LL>f;
LL log_mod(LL a, LL b, LL n, LL c, LL d) {
  LL m, v, e=1, i, x, y, dd;
  m = ceil( sqrt(n + 0.5) );
  f.clear();
  f[1] = m;
  for(i = 1; i < m; ++ i) {
    e = e*a%n;
    if (!f[e]) f[e] = i;
  }
  e = (e*a)%n;
  for (i = 0; i < m; ++ i) {
    exgcd(d,n,dd,x,y);
    x = (x*b%n + n) % n;
    if (f[x]) {
      LL num = f[x];
      return c + i*m + (num==m ? 0 : num);
    }
    d = (d*e) % n;
  }
  return -1;
}
// a^x = b (mod n), no restriction
LL log_mod(LL a, LL b, LL n) {
  b%=n;
  LL c = 0, d = 1, t;
  while((t=__gcd(a,n))!=1){
    if(b%t) return -1;
    c++;
    n/=t;
    b/=t;
    d=d*a/t%n;
    if(d==b)return c;
  }
  return log_mod(a,b,n,c,d);
}
```

4.8 Lucas

```
// C(n,m) % p, make sure p is prime, p <= 10^5
// n = n[k] * p^k + n[k-1] * p^(k-1) + .. + n[0]
// m = m[k] * p^k + m[k-1] * p^(k-1) + .. + m[0]
// then, C(n,m) = C(n[k],m[k])*C(n[k-1],m[k-1])*..*C(n[0],m[0]) (mod p)
// C(n,m) = C(n%p, m%p) * C(n/p, m/p) (mod p)
// eg: hdu3037
LL Lucas(LL n, LL m, LL p) {
  LL ret = 1;
  while(n && m) {
    LL np = n%p, mp = m%p;
    if(np < mp) return 0;
    ret = ret * factorial(np) % p * reverse(factorial(mp), p) % p *
        reverse(factorial(np-mp), p) % p;
    n /= p;
    m /= p;
  }
  return ret;
}
```

4.9 Miller Rabin

```
// prime test
bool Witness(LL n, LL a) {
  LL m = n-1, j = 0;
  while(!(m&1)) m >>= 1, j ++;
  LL ans = pow_mod(a, m, n);
  while (j --) {
    LL tmp = mul_mod(ans, ans, n);
    if (tmp == 1 && ans != 1 && ans != n-1) return 1;
    ans = tmp;
  }
  return ans != 1;
}
bool Miller_Rabin(LL n) {
  if (n < 2) return 0;
  if (n == 2) return 1;
  if (!(n&1)) return 0;
  for (int i = 0; i < max_test; ++ i) {
    ll a = rand() % (n-2) + 2;
    if (Witness(n,a)) return 0;
  }
  return 1;
}
```

4.10 Mul Mod

```
// x*y % n
LL mul_mod(LL x, LL y, LL n) {
  LL T = floor(sqrt(n) + 0.5);
  LL t = T * T - n;
  LL a = x / T, b = x % T;
  LL c = y / T, d = y % T;
  LL e = a * c / T, f = a * c % T;
  LL v = ((a*d + b*c) % n + e*t) % n;
  LL g = v / T, h = v % T;
  LL ret = (((f+g)*t % n + b*d) % n + h*T) % n;
  return (ret % n + n) % n;
}
```

4.11 Pollard Rho

```cpp
// get a factor of n in log(n)
LL Pollard_Rho(LL n, LL c=1) {
  LL i=1, k=2, x=rand()%(n-1)+1, y=x, d;
  while(1) {
    i++;
    x = (mul_mod(x,x,n)+c)%n;
    d=__gcd(n,y-x);
    if(d>1 && d<n) return d;
    if(y==x) return n;
    if(i==k){
      k<<=1;
      y=x;
    }
  }
}
```

4.12 Pow Mod

```cpp
// a^x % n
LL pow_mod(LL a, LL x, LL n) {
  LL ret = 1, mul = a;
  while (x) {
    if (x&1) ret = mul_mod(ret, mul, n);
    mul = mul_mod(mul, mul, n);
    x >>= 1;
  }
  return ret;
}
```

4.13 Power Mod

```cpp
// x^n = a (mod p), make sure that p is prime
// let g be a primitive root of p, x = g^y, a = g^m
// use log_mod to get m, g^(yn) = g^m (mod p)
// thus yn = m (mod p-1), use exgcd to solve and get back
vector<int> power_mod(int a, int n, int p) {
  int g = primitive_root(p);
  LL m = log_mod(g, a, p);
  vector<int>ret;
  if(a==0){
    ret.push_back(0);
    return ;
  }
  if(m==-1)return ret;
  LL A=n,B=p-1,C=m,x,y;
  LL d = exgcd(A,B,x,y);
  if(C%d!=0)return ret;
  x=x*(C/d)%B;
  LL delta=B/d;
  for(int i=0;i<d;++i){
    x=((x+delta)%B+B)%B;
    ret.push_back((int)pow_mod(g,x,p));
  }
  sort(ret.begin(),ret.end());
  ret.erase(unique(ret.begin(),ret.end()), ret.end());
  return ret;
}
```

4.14 Primitive Root

```
// eg: SGU 511
struct PR {
  // make sure that p is prime
  // if p = 2, solve the prob. without PR
  int divs[N+5];
  int primitive_root(const int p) {
    if (p == 2) return 1;
    int cnt = 0, m = p-1;
    for (int i = 2; i*i <= m; ++ i) if (m%i == 0) {
      divs[cnt++] = i;
      if (i*i < m) divs[cnt++] = m/i;
    }
    int r = 2, j = 0;
    while (1) {
      for (j = 0; j < cnt; ++ j) {
        if (fastpow(r, divs[j], p) == 1) break;
      }
      if (j >= cnt) return r;
      r ++;
    }
    return -1;
  }
} pr_solver;
```

4.15 Square Mod

```
// x*x = a (mod n), make sure that n is prime
// be careful there is a single sol. when n = 2
// otherwise, x and n-x are both okay
// eg: ural 1132
LL modsqr(LL a, LL n) {
  LL b, k, i, x;
  if (n == 2) return a % n;
  if (pow_mod(a, (n-1)/2, n) == 1) {
    if (n%4 == 3) {
      x = pow_mod(a, (n+1)/4, n);
    }else{
      for(b=1; pow_mod(b, (n-1)/2, n) == 1; b ++);
      i = (n-1)/2;
      k = 0;
      do {
        i/=2;
        k/=2;
        if((pow_mod(a,i,n) * pow_mod(b,k,n)+1) %n == 0) {
          k += (n-1)/2;
        }
      } while(i%2 == 0);
      x = (pow_mod(a,(i+1)/2,n) * pow_mod(b,k/2,n)) %n;
    }
    if(x*2 > n) x = n-x;
    return x;
  }
  return -1;
}
```

5 Others

5.1 Exact Cover

```
// la 2659
#include <cstdio>
#include <vector>
using namespace std;
const int MROW = 16*16*16 + 5;
const int MCOL = 16*16*4 + 5;
const int NODE = 16*16*16*4 + 5;
struct DLX {
  int n, sz;
  int S[MCOL];
  int row[NODE], col[NODE];
  int ansd, ans[MROW];
  int L[NODE], R[NODE], U[NODE], D[NODE];
  void init(int n) {
    this->n = n;
    for (int i = 0; i <= n; ++ i) {
      U[i] = D[i] = i;
      L[i] = i-1; R[i] = i+1;
      S[i] = 0;
    }
    R[n] = 0; L[0] = n;
    sz = n+1;
  }
  void addRow(int r, const vector<int> &columns) {
    int first = sz;
    for (int i = 0; i < columns.size(); ++ i) {
      int c = columns[i];
      L[sz] = sz-1; R[sz] = sz+1;
      D[sz] = c; U[sz] = U[c];
      D[U[c]] = sz; U[c] = sz;
    row[sz] = r; col[sz] = c;
    S[c] ++; sz ++;
   }
   R[sz-1] = first; L[first] = sz-1;
  }
  #define FOR(i,A,s) for(int i=A[s];i!=s;i=A[i])
  void remove(int c) {
   L[R[c]] = L[c]; R[L[c]] = R[c];
   FOR(i,D,c)
    FOR(j,R,i) { U[D[j]] = U[j]; D[U[j]] = D[j]; -- S[col[j]]; }
  }
  void restore(int c) {
   FOR(i,U,c)
    FOR(j,L,i) { ++S[col[j]]; U[D[j]]=j; D[U[j]]=j; }
   L[R[c]] = c; R[L[c]] = c;
  }
  bool dfs(int d) {
   if (R[0] == 0) {
    ansd = d;
    return 1;
   }
   int c = R[0];
   FOR(i,R,0) if(S[i]<S[c]) c=i;
   remove(c);
   FOR(i,D,c) {
    ans[d] = row[i];
    FOR(j,R,i) remove(col[j]);
    if(dfs(d+1)) return 1;
    FOR(j,L,i) restore(col[j]);
   }
   restore(c);
   return 0;
  }
  bool solve(vector<int>&v) {
   v.clear();
   if (!dfs(0)) return 0;
   for (int i = 0; i < ansd; ++ i) v.push_back(ans[i]);
   return 1;
  }
} dlx;
char data[18][18];
bool input() {
  for (int i = 0; i < 16; ++ i) {
   if (scanf("%s",data[i]) == EOF) return 0;
  }
  return 1;
}
enum { SLOT=0, ROW, COL, BLOK };
int encode(int i, int j, int k) {
  return i*256 + j*16 + k + 1;
}
int block(int i, int j) {
  return 4*(i/4) + (j/4);
```

```
}
void decode(int x, int &a, int &b, int &c) {
  x --;
  c = x % 16; x /= 16;
  b = x % 16; x /= 16;
  a = x;
}
vector<int>columns;
void solve() {
  dlx.init(16*16*4);
  for (int i = 0; i < 16; ++ i) {
    for (int j = 0; j < 16; ++ j) {
      for (int k = 0; k < 16; ++ k) {
        if (data[i][j] == '-' || data[i][j] == k+'A') {
          columns.clear();
          columns.push_back(encode(SLOT, i, j));
          columns.push_back(encode(ROW, i, k));
          columns.push_back(encode(COL, j, k));
          columns.push_back(encode(BLOK, block(i,j), k));
          dlx.addRow(encode(i,j,k), columns);
        }
      }
    }
  }
  columns.clear();
  dlx.solve(columns);
  for (int i = 0; i < columns.size(); ++ i) {
    int r, c, v;
    decode(columns[i], r, c, v);
    data[r][c] = char('A' + v);
  }
  for (int i = 0; i < 16; ++ i) {
    printf("%s\n", data[i]);
  }
}
int main() {
  int kcase = 0;
  while (input()) {
    if (kcase) puts("");
    kcase ++;
    solve();
  }
}
```

5.2 Matrix Fast Power

```
struct Matrix {
  int n, a[N][N];
  Matrix operator * (const Matrix &b) const {
    Matrix ret; ret.clear();
    ret.n = n;
  for (int i = 0; i < n; ++ i) {
    for (int k = 0; k < n; ++ k) if (a[i][k]) {
      for (int j = 0; j < n; ++ j) {
        ret.a[i][j] += a[i][k] * b.a[k][j];
        ret.a[i][j] %= mod;
      }
    }
  }
  return ret;
 }
 void clear() {
  memset(a,0,sizeof(a));
 }
};
Matrix matrix_one(int n) {
 Matrix ret; ret.clear();
 ret.n = n;
 for (int i = 0; i < n; ++ i) {
  ret.a[i][i] = 1;
 }
 return ret;
}
Matrix matrix_pow(Matrix x, int n) {
 Matrix ret = matrix_one(x.n), mul = x;
 while (n) {
  if (n&1) ret = ret * mul;
  mul = mul * mul;
  n >>= 1;
 }
 return ret;
}
```

5.3 Polynomial

```
// eg: UVALive 4305
const int MAXN = 500;
const double EPS = 1e-10;
inline int sgn(const double &a) { return a > EPS ? 1 : (a < -EPS ? -1 : 0); }
struct Polynomial {
 double data[MAXN];
 int n;
 Polynomial() {}
 Polynomial(int _n) : n(_n) {
  memset(data, 0, sizeof(data));
 }
 Polynomial(double *_data, int _n) {
  memset(data, 0, sizeof(data));
  n = _n;
  for (int i = n; i >= 0; i--) data[i] = _data[i];
 }
 Polynomial operator + (const Polynomial &a) {
    Polynomial c(max(n, a.n));
    for (int i = c.n; i >= 0; i--) c.data[i] = data[i] + a.data[i];
    while (sgn(c.data[c.n]) == 0 && c.n) c.n--;
    return c;
  }
  Polynomial operator - (const Polynomial &a) {
    Polynomial c(max(n, a.n));
    for (int i = c.n; i >= 0; i--) c.data[i] = data[i] - a.data[i];
    while (sgn(c.data[c.n]) == 0 && c.n) c.n--;
    return c;
  }
  Polynomial operator * (const Polynomial &a) {
    Polynomial c(n + a.n);
    for (int i = n; i >= 0; i--) for (int j = a.n; j >= 0; j--) c.data[i + j] += data[i] * a.data[j];
    return c;
  }
  Polynomial operator / (const Polynomial &a) {
    if (n < a.n) return *this;
    else {
      Polynomial c(n - a.n);
      for (int i = c.n; i >= 0; i--) c.data[i] = data[i + a.n];
      for (int i = c.n; i >= 0; i--) {
        c.data[i] /= a.data[a.n];
        for (int j = i - 1; a.n - i + j >= 0 && j >= 0; j--) c.data[j] -= c.data[i] * a.data[a.n - i + j];
      }
      return c;
    }
  }
  Polynomial operator % (const Polynomial &a) {
    Polynomial c = *this - *this / a * a;
    while (sgn(c.data[c.n]) == 0 && c.n) c.n--;
    return c;
  }
  bool iszero() {
    return n == 0 && sgn(data[0]) == 0;
  }
  bool isconst() {
    return n > 0;
  }
  Polynomial derivative() {
    Polynomial a(n - 1);
    for (int i = n - 1; i >= 0; i--) a.data[i] = data[i + 1] * (double)(i + 1);
    return a;
  }
  Polynomial integral() {
    Polynomial a(n + 1);
    for (int i = n + 1; i >= 1; i--) a.data[i] = data[i - 1] / (double)i;
    return a;
  }
  void show() {
    for (int i = n; i >= 0; i--) {
      printf("%.6f", data[i], i);
      if (i != 0) printf(" x");
      if (i != 1 && i != 0) printf(" ^ %d", i);
      if (i != 0) printf(" + ");
      else printf("\n");
    }
  }
};
Polynomial gcd(Polynomial a , Polynomial b) {
  if (b.iszero()) return a;
  else return gcd(b, a % b);
}
```

6 测试

6.1 测试

```
/*************************************************************************
 > File Name: test.cpp
 > Author: HKing
 > Mail: 1470042308@qq.com
 > Created Time: 2021年05月23日 星期日 20时13分14秒
 ************************************************************************/

#include <algorithm>
#include <cmath>
#include <cstring>
#include <iostream>
#include <map>
#include <queue>
#include <set>
#include <stack>
#include <string>
#include <vector>
#define IOS ios::sync_with_stdio(0), cin.tie(0), cout.tie(0)
#define endl '\n'
#define out(n) cout << n << ' '
#define outl(n) cout << n << endl
#define sd(n) scanf("%d", &n)
#define sdd(n, m) scanf("%d%d", &n, &m)
#define sddd(n, m, k) scanf("%d%d%d", &n, &m, &k)
#define pd(n) printf("%d\n", (n))
#define pdd(n, m) printf("%d %d\n", n, m)
#define pddd(n, m, k) printf("%d %d %d\n", n, m, k)
#define sld(n) scanf("%lld", &n)
#define sldd(n, m) scanf("%lld%lld", &n, &m)
#define slddd(n, m, k) scanf("%lld%lld%lld", &n, &m, &k)
#define pld(n) printf("%lld\n", n)
#define pldd(n, m) printf("%lld %lld\n", n, m)
#define plddd(n, m, k) printf("%lld %lld %lld\n", n, m, k)
```

```cpp
#define sf(n) scanf("%lf", &n)
#define sff(n, m) scanf("%lf%lf", &n, &m)
#define sfff(n, m, k) scanf("%lf%lf%lf", &n, &m, &k)
#define ss(str) scanf("%s", str)
#define ps(str) printf("%s", str)
#define x first
#define y second
#define pi acos(-1)
#define de(c, n) \
  for (int i = 0; i < n; ++i) \
    cout << c; \
  cout << endl
#define debug(a) cout << #a << '=' << a << endl
#define INF_INT 0x3f3f3f3f;
#define INF_LONG 4557430888798830399
#define mem(ar, num) memset(ar, num, sizeof(ar))
#define me(ar) memset(ar, 0, sizeof(ar))
#define all(v) v.begin(), v.end()
#define max(a, b, c) max(a, max(b, c))
#define lowbit(x) (x & (-x))
#define gcd(a, b) __gcd(a, b)
#define lcm(a, b) a / gcd(a, b) * b
#define qpow(a, k, p) \
  ({ \
    LL s = 1; \
    while (k > 0) { \
      if (k & 1) \
        s = s * a % p; \
      a = a * a % p; \
      k >>= 1; \
    } \
    s; \
  })
#define inv(a, p) \
  ({ \
    LL q = p - 2; \
    qpow(a, q, p); \
  })
#define W(t) \
  cin >> t; \
  while (t--)
using namespace std;
typedef long long LL;
typedef unsigned long long ULL;
typedef pair<int, int> PII;
typedef pair<int, PII> PIII;
typedef pair<LL, LL> PLL;
typedef pair<LL, PLL> PLLL;

int main() {
  IOS;

  return 0;
}
```