Template For ICPC



Author: HKing

Email: 1470042308@qq.com

目录

1	Graph 1				
	1.1 Dinic		1		
	1.2 KM		2		
	1.3 MixedEulerCircuit		4		
2	Tree		5		
	${\tt 2.1 \ DivideAndConquerTree} \ . \ . \ . \ . \ . \ . \ . \ . \ . \ $		5		
	2.2 LinkTree		7		
	2.3 SegmentTree		10		
	2.4 SplayTree		14		
	2.5 Treap		17		
3	Geometry		19		
	3.1 BasicStructandAlgorithm	•	19		
	3.2 PolygonArea		20		
	3.3 HalfPlaneIntersection		20		
4	Math		20		
	4.1 ChinaRemainderTheory				
	4.2 Decompose				
	4.3 EulerPhi	•	22		
	4.4 ExtendGCD		23		
	4.5 IntegerInverse		23		
	4.6 LineMod		23		
	4.7 LogMod		23		
	4.8 Lucas		24		
	4.9 MillerRabin		25		
	4.10 MulMod		25		
	4.11 PollardRho		25		
	4.12 PowMod		26		
	4.13 PowerMod		26		
	4.14 PrimitiveRoot				
	4.15 SquareMod	•	21		
5	Others		28		
•	5.1 ExactCover				
	5.2 MatrixFastPower				
	5.3 Polynomial				
	5.5 Folyhomial	•	31		
6	字符串		33		
	6.1 test		33		
		•			
7	数学		35		
	7.1 高斯消元		35		
	7.2 快速幂		35		
	7.3 欧几里德				
	7.4 扩展欧几里德算法				

	7.5	试除法分解质因数	6
	7.6	试除法判定质数	6
	7.7	试除法求所有约数	7
	7.8	约数个数和约数之和	7
	7.9	组合数	7
		7.9.1 递推法求组合数	7
		7.9.2 通过预处理逆元的方式求组合数	7
		7.9.3 Lucas 定理求组合数	8
		7.9.4 分解质因数法求组合数	8
	7.10	欧拉函数	0
		7.10.1求欧拉函数	0
		7.10.2筛法求欧拉函数	0
	7.11	筛法	1
		7.11.1朴素筛法	1
		7.11.2线性筛法	1
8	数据		_
		Trie 树	_
	8.2	并查集.cpp	2
9	图论	4	2
9	•	test	_
	J.1		0
10	动态	规划 4	5
	10.1	test	5
11	计算		
	11.1	test	7
12	其他	4	a
12		test	-
	14 · 1	. 0000	J

1 Graph

1.1 Dinic

```
1
    const int inf = 0x3f3f3f3f;
 2
    const int N = 205;
    const int M = 1205;
 4
    struct Edge{
 5
       int v,f,nxt;
 6
    };
 7
    struct Dicnic{
 8
       int src,sink;
 9
       int g[N],en;
       Edge e[M*2];
10
11
       int level[N];
       void _addEdge(int u,int v,int f){
12
13
           e[en].v=v;
14
           e[en].f=f;
15
           e[en].nxt=g[u];
16
           g[u]=en++;
17
18
       void addEdge(int u,int v,int f){
19
           addEdge(u,v,f);
20
           _addEdge(v,u,0);
21
       }
22
       void init(){
23
           en=0;
24
           memset(g,-1,sizeof(g));
25
       }
26
       int q[N],front,rear;
27
       bool bfs(){
28
           memset(level,0,sizeof(level));
29
           level[src]=1;
30
           front=0; rear=1;
31
           q[0]=src;
           while(front<rear){</pre>
32
              int u=q[front++];
33
34
              if(u==sink)return 1;
35
              for(int i=g[u];i!=-1;i=e[i].nxt){
36
                  int v=e[i].v,f=e[i].f;
37
                  if(!level[v]&&f){
38
                     level[v]=level[u]+1;
39
                     q[rear++]=v;
40
                  }
41
              }
42
           }
43
           return 0;
44
       int dfs(int u,int delta){
45
           if(u==sink || delta==0)return delta;
46
47
           int ret=0;
48
           for(int i=g[u];i!=-1;i=e[i].nxt){
```

```
49
              int v=e[i].v, f=e[i].f;
50
              if(level[v]==level[u]+1&&f){
51
                  int minf=min(delta-ret,f);
52
                  f=dfs(v,minf);
53
                  e[i].f-=f;
                  e[i^1].f+=f;
54
55
                  delta-=f;
56
                  ret+=f;
57
                  if(ret==delta)return ret;
58
              }
59
           }
60
           return ret;
61
       }
       int maxflow(int _src,int _sink){
62
63
           src=_src;
64
           sink=_sink;
65
           int ret=0;
66
           while(bfs())ret+=dfs(src,inf);
67
           return ret;
68
       }
69
    }dicnic_solver;
```

1.2 KM

```
1
    // eg: soj 1013
 2
    const int N = 105;
    const int inf = 1000000000;
 4
    struct KM{
 5
       int w[N][N],x[N],y[N];
 6
       int px[N],py[N],sy[N],sk[N],pr[N];
 7
       int lx,ly,n;
 8
       void adjust(int v){
 9
           sy[v]=py[v];
10
           if(px[sy[v]]!=-2)adjust(px[sy[v]]);
11
       }
12
       int solve(int _n,int _w[][N]){
13
           n=_n;
14
           memcpy(w,_w,sizeof(w));
15
           return km();
16
       }
       bool find(int v){
17
           for(int i=0;i<n;++i)if(py[i]==-1){</pre>
18
19
              if(sk[i]>x[v]+y[i]-w[v][i]){
20
                  sk[i]=x[v]+y[i]-w[v][i];
21
                  pr[i]=v;
22
23
              if(x[v]+y[i]==w[v][i]){
24
                  py[i]=v;
25
                  if(sy[i]==-1){
26
                     adjust(i);
27
                     return 1;
```

```
28
                   }
29
                   if(px[sy[i]]!=-1)continue;
30
                   px[sy[i]]=i;
31
                   if(find(sy[i]))return 1;
32
               }
           }
33
34
           return 0;
35
        }
36
        int km(){
           int i,j,m;
37
38
           for(i=0;i<n;++i){</pre>
39
               sy[i]=-1;
40
               y[i]=0;
41
           }
42
           for(i=0;i<n;++i){</pre>
43
               x[i]=0;
44
               for(j=0;j<n;++j){</pre>
45
                   x[i]=max(x[i],w[i][j]);
               }
46
47
           }
48
           bool f;
           for(i=0;i<n;++i){</pre>
49
50
               for(j=0;j<n;++j){</pre>
51
                   px[j]=py[j]=-1;
52
                   sk[j]=inf;
53
               }
54
               px[i]=-2;
55
               if(find(i))continue;
               f=0;
56
57
               while(!f){
58
                   m=inf;
                   for(j=0;j<n;++j)if(py[j]==-1)m=min(m,sk[j]);</pre>
59
60
                   for(j=0;j<n;++j){</pre>
61
                       if(px[j]!=-1)x[j]-=m;
                       if(py[j]!=-1)y[j]+=m;else sk[j]-=m;
62
63
                   }
64
                   for(j=0;j<n;++j)if(py[j]==-1&&!sk[j]){</pre>
                       py[j]=pr[j];
65
                       if(sy[j]==-1){
66
67
                          adjust(j);
68
                          f=1;
69
                          break;
70
                       }
71
                       px[sy[j]]=j;
72
                       if(find(sy[j])){
73
                          f=1;
74
                          break;
75
                       }
76
                   }
77
               }
78
           }
79
           int ans=0;
80
           for(i=0;i<n;++i)ans+=w[sy[i]][i];</pre>
```

```
81    return ans;
82    }
83    }km_solver;
```

1.3 MixedEulerCircuit

```
// eg: soj 1066
    const int N = 205;
 3
    int degree[N],n;
    void init(){
 5
       dicnic_solver.init();
       int m,a,b,c;
 6
 7
       scanf("%d%d",&n,&m);
 8
       memset(degree,0,sizeof(degree));
 9
       while(m--){
10
           // c=0,a<->b; c=1,a->b
11
           scanf("%d%d%d",&a,&b,&c);
12
           a--; b--;
13
           degree[a]--;
14
           degree[b]++;
15
           if(!c)dicnic_solver.addEdge(a,b,1);
16
       }
17
18
    bool work(){
19
       int ans=0;
20
       for(int i=0;i<n;++i)if(degree[i]&1)return 0;</pre>
21
       for(int i=0;i<n;++i){</pre>
22
           if(degree[i]<0){</pre>
23
              dicnic_solver.addEdge(n,i,-degree[i]/2);
24
              ans-=degree[i]/2;
25
           }else if(degree[i]>0){
26
              dicnic_solver.addEdge(i,n+1,degree[i]/2);
27
           }
28
       return dicnic_solver.maxflow(n,n+1)>=ans;
29
30
    }
    void solve(){
31
32
       puts(work()?"possible":"impossible");
33
   }
    int main(){
34
35
       int t;
36
       scanf("%d",&t);
       while(t--){
37
38
           init();
39
           solve();
40
41
       return 0;
42
   }
```

2 Tree

2.1 DivideAndConquerTree

```
//hdu 4812 D Tree
1
   #include <iostream>
   #include <cstdio>
   #include <cstring>
 5
   #include <vector>
 6
    #pragma comment(linker, "/STACK:102400000, 102400000")
 7
    using namespace std;
8
   const int maxn = 1e5 + 10;
    const int md = 1e6 + 3;
   int N,K;
10
    vector<int > edge[maxn];
11
    void add_edge(int from,int to) {
12
13
     edge[from].push_back(to);
   }
14
15
    void init() {
    for(int i = 1;i <= N;i ++) edge[i].clear();</pre>
16
17
18
    int vi[maxn];
19
   int vis[maxn];
20 | int root;
21 int mi;
22 | int son[maxn];
23 | int hash[md + 10];
24 int vers[md + 10];
25 | int verc;
26 | pair<int , int > ans;
   int fastpow(int x,int y) {
27
     int ret = 1 ,mul = x;
28
29
     while(y) {
       if(y & 1 ) ret = 1LL * mul * ret % md;
30
31
       mul = 1LL * mul* mul % md;
32
       y >>= 1;
33
     }
34
     return ret;
35
36
    int comm[md + 10];
37
    void inv1() {
38
     for(int i = 0;i < md;i ++) {</pre>
       comm[i] = fastpow(i, md - 2);
39
40
     }
41
42
    int inv(int t) {
43
     return comm[t];
44
45
    void getroot(int t,int sz) {
46
     vis[t] = true;
47
     son[t] = 1;
48
    int mx = 0;
```

```
49
      for(int i = 0;i < edge[t].size();i ++) {</pre>
50
        int nxt = edge[t][i];
51
        if(!vis[nxt]) {
52
          getroot(nxt,sz);
53
          son[t] += son[nxt];
54
          mx = max(mx,son[nxt]);
55
        }
56
      }
57
      mx = max(mx,sz - son[t]);
58
      if(mx <= mi) {
59
        root = t;
60
        mi = mx;
61
62
      vis[t] = false;
63
64
     void dfs(int t,int mul,int ri) {
65
      vis[t] = true;
66
      //query
      mul = 1LL * mul * vi[t] % md;
67
68
      if(1LL * mul * ri % md == K) {
69
        pair<int ,int > tmp = pair<int ,int > (min(root,t),max(root,t));
70
        if(tmp < ans) ans = tmp;</pre>
71
      }
72
      int q = 1LL* inv(1LL * mul * ri % md) * K % md;
73
      if(vers[q] == verc && hash[q]!= 0 ) {
74
        pair<int ,int > tmp = pair<int ,int > (min(t,hash[q]),max(t,hash[q]));
75
        if(tmp < ans) ans = tmp;</pre>
76
      }
77
      son[t] = 1;
78
      for(int i = 0;i < edge[t].size();i ++) {</pre>
79
        int nxt = edge[t][i];
80
        if(!vis[nxt]) {
81
          dfs(nxt,mul,ri);
82
          son[t] += son[nxt];
83
        }
84
      }
85
      //set
86
      if(vers[mul] != verc ) {
87
        vers[mul] = verc;
88
        hash[mul] = t;
89
90
      hash[mul] = min(hash[mul],t);
91
      vis[t] = false;
92
93
     void work(int t,int sz) {
94
      mi = sz;
95
      getroot(t,sz);
96
      // dfs
97
      int rt = root;
98
      vis[rt] =true;
99
      verc ++;
100
      for(int i = 0;i < edge[root].size();i ++) {</pre>
101
        int nxt = edge[rt][i];
```

```
102
        if(!vis[nxt]) {
103
          dfs(nxt,1,vi[rt] % md);
104
        }
105
       }
106
       for(int i = 0;i < edge[rt].size();i ++) {</pre>
107
        int nxt = edge[rt][i];
108
        if(!vis[nxt]) {
109
          work(nxt,son[rt]);
110
        }
111
       }
112
     }
113
     int main() {
114
       inv1();
115
       verc = 0;
       while(scanf("%d%d",&N,&K) != EOF) {
116
117
        init();
118
        for(int i = 1;i <= N;i ++) {</pre>
119
          scanf("%d",&vi[i]);
120
        }
        for(int i = 0; i < N - 1; i ++) {
121
122
          int u,v;
123
          scanf("%d%d",&u,&v);
124
          add_edge(u,v);
125
          add_edge(v,u);
126
127
        memset(vis,0,sizeof(vis));
128
        ans = pair<int ,int > (N+1,N+1);
129
        work(1,N);
130
        if(ans.first == N+1 && ans.second == N + 1) {
131
          puts("No solution");
132
        } else {
          printf("%d %d\n",ans.first,ans.second);
133
134
        }
135
       }
136
     }
```

2.2 LinkTree

```
//HDU 3966
   //operation1 path c1 to c2 plus k
 3
   //operation2 path c1 to c2 minus k
   #include <iostream>
   #include <cstdio>
 5
 6
   #include <algorithm>
 7
   #include <vector>
 8
   #include <cstring>
   #pragma comment(linker, "/STACK:1024000000,1024000000")
 9
10 using namespace std;
   #define lc (o<<1)
   |#define rc (o<<1|1)
12
13 | int N,M,P;
```

```
const int maxn = 100010;
    vector<int > edge[maxn];
    int ai[maxn];
16
17
    void add_edge(int from,int to) {
18
     edge[from].push_back(to);
19
20
    void init() {
21
    for(int i = 1;i <= N;i ++) edge[i].clear();</pre>
22
23
   int son[maxn]; // size of children
   int fa[maxn];
25 | int wn[maxn]; //index in segment
26 | int wcnt;
27
   int vis[maxn];
28
   int dep[maxn]; // depth
29
   int top[maxn]; // link fa
30
   //Tree link
31
    void dfs1(int t,int d) {
32
     vis[t] = true;
33
     dep[t] = d;
34
      son[t] = 1;
35
     for(int i = 0;i < edge[t].size();i ++) {</pre>
36
       int nxt = edge[t][i];
37
       if(!vis[nxt]) {
38
         fa[nxt] = t;
39
         dfs1(nxt,d + 1);
40
         son[t] += nxt;
41
       }
42
      }
43
      vis[t] = false;
44
45
    void dfs2(int t) {
46
     vis[t] = true;
47
      wn[t] = wcnt ++;
48
      bool first = true;
49
      int index = -1;
50
      for(int i = 0;i < edge[t].size();i ++) {</pre>
51
       int nxt = edge[t][i];
52
       if(!vis[nxt]) {
53
         if(first) {
54
           first =false;
55
           index = nxt;
56
         }
57
         if(son[nxt] > son[index]) {
58
           index= nxt;
59
         }
60
       }
61
      }
62
      if(!first ) {
63
       top[index] = top[t];
64
       dfs2(index);
65
       for(int i = 0;i < edge[t].size();i ++) {</pre>
66
         int nxt = edge[t][i];
```

```
67
          if(!vis[nxt] && nxt != index) {
68
            top[nxt] = nxt;
69
            dfs2(nxt);
70
          }
71
        }
72
73
       vis[t] = false;
74
75
     //segment tree
76
     int addv[maxn << 2];</pre>
77
     void add(int o,int l,int r,int y1,int y2,int v) {
       if(y1 <= 1 && r <= y2) {
78
79
        addv[o] += v;
80
       } else {
        int m = (1 + r) >> 1;
81
82
        if(y1 <= m) add(lc,1,m,y1,y2,v);</pre>
83
        if(m < y2) add(rc,m+1,r,y1,y2,v);</pre>
84
       }
85
86
     void query(int o,int l,int r,int x,int & ans) {
87
       if(1 == r \&\& r == x) {
        ans += addv[o];
88
89
       } else {
90
        int m = (1 + r) >> 1;
91
        ans += addv[o];
92
        if(x <= m ) {
93
          query(lc,1,m,x,ans);
94
        } else {
95
          query(rc,m+1,r,x,ans);
96
        }
97
       }
98
99
     void init seg() {
100
       memset(addv,0,sizeof(addv));
101
     }
102
     char buff[5];
103
     int main() {
104
       while(~scanf("%d%d%d",&N,&M,&P) ) {
105
         init();
106
        for(int i = 1;i <= N;i ++) {</pre>
107
          scanf("%d",&ai[i]);
108
109
        for(int i = 0;i < M;i ++) {</pre>
110
          int u,v;
111
          scanf("%d%d",&u,&v);
112
          add_edge(u,v);
113
          add_edge(v,u);
114
         }
115
        dfs1(1,1);
116
        wcnt = 0;
117
        top[1] = 1;
118
        dfs2(1);
119
        init_seg();
```

```
120
        while(P --) {
121
          scanf("%s",buff);
122
          if(buff[0] == 'I' || buff[0] == 'D') {
123
            int c1,c2,k;
124
            scanf("%d%d%d",&c1,&c2,&k);
125
            if(buff[0] == 'D') k = - k;
126
            /// query path
127
            while(top[c1] != top[c2]) {
128
              int f1 = top[c1];
129
              int f2 = top[c2];
130
             if(dep[f1] < dep[f2]) {</pre>
131
               swap(f1,f2);
132
               swap(c1,c2);
133
             }
134
              add(1,0,N - 1,wn[f1],wn[c1],k);
135
              c1 = fa[f1];
136
            }
137
            if(dep[c1] < dep[c2]) {</pre>
138
              swap(c1,c2);
139
            }
140
            add(1,0,N-1,wn[c2],wn[c1],k);
141
          } else if(buff[0] == 'Q') {
142
            int d;
143
            scanf("%d",&d);
144
            int ans = 0;
145
            query(1,0,N-1,wn[d],ans);
146
            ans += ai[d];
147
            printf("%d\n",ans);
148
          }
149
        }
150
       }
151
     }
```

2.3 SegmentTree

```
//HDU 4578
   //segment plus mul power sum
 3
   #include <cstdio>
   #include <algorithm>
 5
   using namespace std;
 6
    #define lc (o<<1)
 7
    #define rc (o<<1|1)
8
    const int maxn = 100010;
9
    const int md = 10007;
   int sumv1[maxn<<2], sumv2[maxn<<2], sumv3[maxn<<2];</pre>
10
11
    int addv[maxn<<2], setv[maxn<<2], timv[maxn<<2];</pre>
12
    void pushdown(int o) {
13
     if (setv[o] >= 0) {
14
       setv[lc] = setv[rc] = setv[o];
15
       addv[lc] = addv[rc] = 0;
       timv[lc] = timv[rc] = 1;
16
```

```
17
       setv[o] = -1;
18
     }
     if (timv[o] != 1) {
19
20
       addv[lc] *= timv[o];
21
       addv[lc] %= md;
22
       addv[rc] *= timv[o];
23
       addv[rc] %= md;
24
       timv[lc] *= timv[o];
       timv[lc] %= md;
25
26
       timv[rc] *= timv[o];
27
       timv[rc] %= md;
28
       timv[o] = 1;
29
30
     if (addv[o] > 0) {
31
       addv[lc] += addv[o];
32
       addv[lc] %= md;
33
       addv[rc] += addv[o];
34
       addv[rc] %= md;
35
       addv[o] = 0;
36
     }
37
    void maintain(int o,int l,int r) {
38
39
     if (1 == r) {
40
       if (setv[o] != -1) {
41
         sumv1[o] = setv[o];
42
         setv[o] = -1;
43
44
       if (timv[o] != 1) {
45
         sumv1[o] *= timv[o];
46
         timv[o] = 1;
47
         sumv1[o] %= md;
48
49
       if (addv[o] > 0) {
50
         sumv1[o] += addv[o];
51
         sumv1[o] %= md;
52
         addv[o] = 0;
53
54
       sumv2[o] = sumv1[o] * sumv1[o] % md;
55
       sumv3[o] = sumv1[o] * sumv2[o] % md;
56
     } else {
57
       sumv1[o] = (sumv1[lc] + sumv1[rc]) % md;
58
       sumv2[o] = (sumv2[lc] + sumv2[rc]) % md;
59
       sumv3[o] = (sumv3[lc] + sumv3[rc]) % md;
       if (setv[o] != -1) {
60
61
         sumv1[o] = setv[o] * (r - 1 +1) % md;
62
         sumv2[o] = setv[o] * setv[o] % md * (r - 1 + 1) % md;
         sumv3[o] = setv[o] * setv[o] % md * setv[o] % md * (r - 1 + 1) % md;
63
64
       }
65
       if (timv[o] != 1) {
66
         sumv1[o] *= timv[o];
         sumv1[o] %= md;
67
68
         sumv2[o] *= timv[o] * timv[o] % md;
69
         sumv2[o] \%= md;
```

```
70
                         sumv3[o] *= timv[o] * timv[o] % md * timv[o] % md;
  71
                         sumv3[o] %= md;
  72
                     }
  73
                     if (addv[o] > 0) {
  74
                         int tmp1 = sumv1[0];
  75
                         sumv1[o] += addv[o] * (r - 1 + 1) % md;
  76
                         sumv1[o] %= md;
  77
                         int tmp2 = sumv2[o];
  78
                         int tmp3 = sumv3[o];
                         sumv2[o] = (tmp2 + 2*tmp1\%md * addv[o]\%md + addv[o] * addv[o] \%md* (r - 1) + addv[o] * addv[o]
  79
                                   +1)%md) % md;
  80
                         sumv3[o] = tmp3 + 3 * tmp2%md * addv[o] % md + 3 * tmp1 % md * addv[o]%md *
                                   addv[o] \% md + addv[o] * addv[o] \% md * addv[o] \% md * (r - 1 + 1) %md;
  81
                         sumv3[o] %= md;
  82
                     }
  83
                 }
  84
  85
             void setq(int o,int l,int r,int y1,int y2,int v) {
  86
                if (y1 <= 1 && r <= y2) {
  87
                     setv[o] = v;
  88
                     addv[o] = 0;
  89
                    timv[o] = 1;
  90
                 } else {
                     pushdown(o);
  91
  92
                     int m = (1 + r) >> 1;
  93
                    if (y1 <= m) setq(lc,l,m,y1,y2,v);</pre>
  94
                     else maintain(lc,l,m);
  95
                     if (m < y2) setq(rc,m+1,r,y1,y2,v);</pre>
  96
                    else maintain(rc,m+1,r);
  97
                 }
  98
                 maintain(o,1,r);
  99
             void addq(int o,int l,int r,int y1,int y2,int v) {
100
101
                if (y1 <= 1 && r <= y2) {
102
                     addv[o] += v;
103
                     addv[o] %= md;
104
                 } else {
105
                     pushdown(o);
106
                     int m = (1 + r) >> 1;
                    if (y1 \leftarrow m) addq(lc,1,m,y1,y2,v);
107
                     else maintain(lc,l,m);
108
109
                    if (m < y2) addq(rc,m+1,r,y1,y2,v);</pre>
                     else maintain(rc,m+1,r);
110
111
                 }
112
                maintain(o,l,r);
113
             void timq(int o,int l,int r,int y1,int y2,int v) {
114
115
                 if (y1 <= 1 && r <= y2) {
                    timv[o] *= v;
116
117
                     timv[o] %= md;
118
                     addv[o] *= v;
119
                    addv[o] %= md;
120
                 } else {
```

```
121
        pushdown(o);
122
        int m = (1 + r) >> 1;
123
        if (y1 <= m) timq(lc,1,m,y1,y2,v);</pre>
124
        else maintain(lc,l,m);
125
        if (m < y2) timq(rc,m+1,r,y1,y2,v);</pre>
126
        else maintain(rc,m+1,r);
127
      }
      maintain(o,1,r);
128
129
130
     int ans1, ans2, ans3;
131
     void query(int o,int l,int r,int y1,int y2,int add,int ti) {
132
      if (setv[o] > 0) {
133
        add = ti * addv[o] % md + add;
134
        ti = ti * timv[o] % md;
135
        int len = min(r,y2) - max(y1,1) + 1;
136
        int tmp1 = setv[o] * len % md * ti % md;
137
        int tmp2 = setv[o] * setv[o] % md * len % md * ti%md * ti %md;
138
        int tmp3 = setv[o] * setv[o] % md * setv[o] % md * len % md * ti % md* ti % md*
            ti % md;
139
        int _sum1 = tmp1 + add * len % md;
140
        _sum1 %= md;
141
        int _sum2 = (tmp2 + 2* tmp1 * add % md + add * add % md * len % md) % md;
142
        int _sum3 = (tmp3 + 3 * tmp2 * add % md + 3 * tmp1 * add % md * add % md + len
             * add % md * add % md *add % md) % md;
143
        ans1 = (ans1 + \_sum1) \% md;
144
        ans2 = (ans2 + \_sum2) \% md;
145
        ans3 = (ans3 + \_sum3) % md;
146
        return ;
147
      }
148
      if (y1 <= 1 && r <= y2) {
149
        int tmp1 = sumv1[o] * ti % md;
150
        int tmp2 = sumv2[o] * ti % md * ti % md;
151
        int tmp3 = sumv3[o] * ti % md * ti % md * ti % md;
152
        int _sum = tmp1 + add * (r - 1 + 1) % md;
        int _sum2 = tmp2 + 2* tmp1 * add % md + add * add % md * (r - 1 + 1) % md;
153
154
        int _sum3 = tmp3 + 3 * tmp2 % md * add % md + 3 * tmp1 % md * add % md * add %
            md + add * add % md * add % md * (r-1+1) % md;
        sum %= md;
155
156
        _sum2 %= md;
157
        sum3 %= md;
158
        ans1 = (ans1 + \_sum) \% md;
159
        ans2 = (ans2 + \_sum2) \% md;
        ans3 = (ans3 + sum3) \% md;
160
161
162
      } else {
163
        int m = (1 + r) >> 1;
        if (y1 <= m) query(lc,l,m,y1,y2,(ti * addv[o] % md + add) % md,ti * timv[o] %</pre>
164
            md);
165
        if (m < y2) query(rc,m+1,r,y1,y2,(ti * addv[o] % md + add) % md,ti * timv[o] %</pre>
166
      }
167
     }
     void init(int o,int l,int r) {
```

```
169
       setv[o] = -1;
170
       timv[o] = 1;
       addv[o] = 0;
171
172
       sumv1[o] = sumv2[o] = sumv3[o] = 0;
173
       if (1 == r) {
174
       } else {
175
        int m = (1 + r) >> 1;
176
        init(lc,1,m);
177
        init(rc,m+1,r);
178
       }
179
     }
180
     int main() {
181
      int N,M;
182
       while (scanf("%d%d",&N,&M)==2 && N && M) {
183
        init(1,1,N);
184
        while (M --) {
185
          int cmd,x,y,c;
          scanf("%d%d%d%d",&cmd,&x,&y,&c);
186
          if(cmd == 1) {
187
188
            c %= md;
189
            addq(1,1,N,x,y,c);
190
          } else if(cmd == 2) {
191
            c %= md;
            timq(1,1,N,x,y,c);
192
193
          } else if(cmd == 3) {
194
            c %= md;
195
            setq(1,1,N,x,y,c);
196
          } else if(cmd == 4) {
197
            ans1 = ans2 = ans3 = 0;
198
            query(1,1,N,x,y,0,1);
199
            if(c == 1) {
200
              printf("%d\n",ans1);
201
            } else if(c == 2){
202
              printf("%d\n",ans2);
203
            } else if(c == 3) {
204
              printf("%d\n",ans3);
205
            }
206
207
        }
208
      }
209
     }
```

2.4 SplayTree

```
#include <cstdio>
#include <iostream>
using namespace std;

Node* ch[2];
int v, s, flip;
void maintain() {
```

```
8
        s = 1 + ch[0] -> s + ch[1] -> s;
 9
10
      void pushdown() {
11
        if (flip) {
12
          flip = 0;
13
          swap(ch[0], ch[1]);
          ch[0]->flip ^= 1;
14
15
          ch[1]->flip ^= 1;
        }
16
17
      }
18
      int cmp(int k) const {
19
        int d = k - ch[0] \rightarrow s;
        if (d == 1) return -1;
20
21
        return d <= 0 ? 0 : 1;
22
      }
23
    };
24
    Node* null = new Node();
25
    void rotate(Node* &o, int d) {
      Node* k = o \rightarrow ch[d^1];
26
27
      o\rightarrow ch[d^1] = k\rightarrow ch[d];
28
      k\rightarrow ch[d] = o;
29
      o->maintain();
30
      k->maintain();
31
      o = k;
32
33
    void splay(Node* &o, int k) {
34
      o->pushdown();
35
      int d = o \rightarrow cmp(k);
      if (d == 1) k -= o \rightarrow ch[0] \rightarrow s + 1;
36
37
      if (d != -1) {
38
        Node* p = o \rightarrow ch[d];
39
        p->pushdown();
40
        int d2 = p \rightarrow cmp(k);
41
        int k2 = (d2 == 0) ? k : k - p \rightarrow ch[0] \rightarrow s - 1;
42
        if (d2 != -1) {
43
          splay(p->ch[d2], k2);
44
          if (d == d2) {
45
            rotate(o, d^1);
46
          } else {
47
            rotate(o->ch[d], d);
48
          }
49
50
        rotate(o, d^1);
51
52
53
    Node* merge(Node* left, Node* right) { // make sure left != null
      splay(left, left->s);
54
55
      left->ch[1] = right;
56
      left->maintain();
57
      return left;
58
59
    void split(Node* o, int k, Node* &left, Node* &right) { // make sure 1 <= k <= o->s
      splay(o, k);
```

```
left = o;
61
62
       right = o \rightarrow ch[1];
       o\rightarrow ch[1] = null;
63
64
       left->maintain();
65
66
     const int maxn = 300000 + 10;
     struct SS {
67
68
       int n;
69
       Node seq[maxn];
70
       Node* root;
71
       Node* build(int sz) {
72
        if (!sz) return null;
73
        Node * L = build(sz/2);
        Node* o = &seq[++n];
74
75
        o \rightarrow v = n-1;
76
        o\rightarrow flip = 0;
77
        o\rightarrow ch[0] = L;
78
        o\rightarrow ch[1] = build(sz - sz/2 - 1);
79
        o->maintain();
80
        return o;
81
       }
82
       void init(int sz) {
83
        n = 0;
84
        null->s = null->flip = 0;
85
        root = build(sz);
86
       }
87
       void print(Node *o) {
88
        if (o != null) {
89
          o->pushdown();
          print(o->ch[0]);
90
91
          if (o->v) {
            if (o->v != 1) putchar(' ');
92
            printf("%d", o->v);
93
94
          }
95
          print(o->ch[1]);
96
        }
97
       }
98
     } ss;
99
     int n, m, a, b, c;
100
     char op[10];
101
     int main() {
102
       while (scanf("%d%d",&n,&m) == 2 && n != -1 && m != -1) {
103
         ss.init(n+1);
104
        Node *t1, *t2, *t3;
105
        while(m--){
          scanf("%s",op);
106
107
          if(op[0]=='C'){ // split [a,b], put it after c
108
            scanf("%d%d%d",&a,&b,&c);
109
            split(ss.root, b+1, t1, t2);
110
            split(t1, a, t1, t3);
111
            ss.root = merge(t1, t2);
112
            split(ss.root, c+1, t1, t2);
113
            ss.root = merge(merge(t1, t3), t2);
```

```
114
          } else { // flip [a,b]
115
            scanf("%d%d",&a,&b);
            split(ss.root, b+1, t1, t3);
116
117
           split(t1, a, t1, t2);
118
           t2->flip ^= 1;
119
            ss.root = merge(merge(t1, t2), t3);
120
          }
121
        }
122
        ss.print(ss.root);
123
        puts("\n");
124
      }
125
    }
```

2.5 Treap

```
1
    struct Node {
 2
      Node *ch[2]; // 0-left 1-right
 3
      int r, v, s; // rank, val, #node
 4
      Node(int v): v(v) {
 5
        ch[0] = ch[1] = NULL;
 6
        r = rand();
 7
        s = 1;
 8
      }
 9
      int cmp(int x) const {
10
        if (x == v) return -1;
11
        return x < v ? 0 : 1;</pre>
12
13
      void maintain() { // maintain #node
14
        s = 1;
15
        if (ch[0] != NULL) s += ch[0]->s;
        if (ch[1] != NULL) s += ch[1]->s;
16
17
      }
18
    };
19
    void rotate(Node* &o, int d) {
20
      Node* k = o \rightarrow ch[d^1];
21
      o\rightarrow ch[d^1] = k\rightarrow ch[d];
22
      k\rightarrow ch[d] = o;
23
      o->maintain();
      k->maintain();
24
      o = k;
25
26
    void insert(Node* &o, int x) {
27
28
      if (o == NULL) {
29
        o = new Node(x);
30
      } else {
31
        int d = o \rightarrow cmp(x);
        if (d !=-1) { // same ele won't be inserted
32
33
          insert(o->ch[d], x);
34
          if (o\rightarrow ch[d]\rightarrow r \rightarrow o\rightarrow r) rotate(o, d^1);
35
        }
      }
36
```

```
37
      o->maintain();
38
39
    void remove(Node* &o, int x) {
40
      if (o == NULL) return ; // ele to be removed not exist
41
      int d = o \rightarrow cmp(x);
42
      if (d == -1) {
43
        Node* ret = o;
44
        if (o->ch[0] != NULL && o->ch[1] != NULL) {
          int d2 = (o \rightarrow ch[0] \rightarrow r > o \rightarrow ch[1] \rightarrow r ? 1 : 0);
45
46
          rotate(o, d2);
47
          remove(o \rightarrow ch[d2], x);
48
        } else {
49
          if (o\rightarrow ch[0] == NULL) o = o\rightarrow ch[1];
50
          else o = o \rightarrow ch[0];
51
          delete ret;
52
        }
53
      } else {
54
        remove(o->ch[d], x);
55
56
      if (o) o->maintain();
57
    int find(Node* o, int x) {
58
59
      while (o != NULL) {
60
        int d = o \rightarrow cmp(x);
61
        if (d == -1) return 1;
62
        else o = o \rightarrow ch[d];
63
      }
64
      return 0;
65
66
    int kth_big(Node* o, int k) {
67
      if (o == NULL \mid k \le 0 \mid k > o \rightarrow s) return 0;
      int s = o \rightarrow ch[1] == NULL ? 0 : o \rightarrow ch[1] \rightarrow s;
68
      if (k == s+1) return o \rightarrow v;
69
70
      else if (k <= s) return kth_big(o->ch[1], k);
71
      else return kth_big(o->ch[0], k-s-1);
72
73
    int kth_small(Node* o, int k) {
      if (o == NULL | | k <= 0 | | k > o \rightarrow s) return 0;
74
75
      int s = o \rightarrow ch[0] == NULL ? 0 : o \rightarrow ch[0] \rightarrow s;
76
      if (k == s) return o->v;
77
      else if (k < s) return kth_small(o->ch[0], k);
78
      else return kth_small(o->ch[1], k-s-1);
79
    void merge(Node* &src, Node* &dest) {
80
      if (src == NULL) return ;
81
82
      merge(src->ch[0], dest);
83
      merge(src->ch[1], dest);
84
      insert(dest, src->v);
85
      delete src;
86
      src = NULL;
87
88
    void clear(Node* &o) {
     if (o == NULL) return ;
```

3 Geometry

3.1 BasicStructandAlgorithm

```
1
    struct Point {
 2
     double x, y;
 3
     Point(double x=0, double y=0):x(x),y(y){}
   };
 5
 6
   typedef Point Vector;
 7
 8
    Vector operator + (const Vector &A, const Vector &B) { return Vector(A.x+B.x,
        A.y+B.y); }
    Vector operator - (const Point &A, const Point &B) { return Vector(A.x-B.x,
        A.y-B.y); }
    Vector operator * (const Vector &A, double p) { return Vector(A.x*p, A.y*p); }
10
    double Dot(const Vector &A, const Vector &B) { return A.x*B.x + A.y*B.y; }
11
    double Cross(const Vector &A, const Vector &B) { return A.x*B.y - A.y*B.x; }
    double Length(const Vector &A) { return sqrt(Dot(A, A)); }
13
   | Vector Normal(const Vector &A) { double L = Length(A); return Vector(-A.y/L,
14
        A.x/L); }
15
   struct Line {
16
17
     Point P;
18
     Vector v;
19
     double ang;
20
     Line() {}
     Line(Point P, Vector v):P(P),v(v){ ang = atan2(v.y, v.x); }
21
     bool operator < (const Line &L) const {</pre>
22
       return ang < L.ang;</pre>
23
24
     }
25
   |};
26
27
    // if $p$ is on the left side of $L$
28
    bool OnLeft(const Line &L, const Point &p) {
29
     return Cross(L.v, p-L.P) > 0;
30
   }
31
32
   // intersection of line $a$ and $b$
   | Point GetLineIntersection(const Line &a, const Line &b) {
33
     Vector u = a.P-b.P;
34
35
     double t = Cross(b.v, u) / Cross(a.v, b.v);
36
     return a.P+a.v*t;
37
```

3.2 PolygonArea

```
double PolygonArea(vector<Point> p) {
  int n = p.size();
  double area = 0;
  for(int i = 1; i < n-1; i++)
    area += Cross(p[i]-p[0], p[i+1]-p[0]);
  return area/2;
}</pre>
```

3.3 HalfPlaneIntersection

```
1
   const double eps = 1e-6;
   // intersection of areas (leftside of lines)
    vector<Point> HalfplaneIntersection(vector<Line> L) {
 4
      int n = L.size();
 5
      sort(L.begin(), L.end());
 6
      int first, last;
 7
      vector<Point> p(n);
 8
      vector<Line> q(n);
 9
      vector<Point> ans;
10
      q[first=last=0] = L[0];
      for(int i = 1; i < n; i++) {</pre>
11
12
       while(first < last && !OnLeft(L[i], p[last-1])) last--;</pre>
13
       while(first < last && !OnLeft(L[i], p[first])) first++;</pre>
       q[++last] = L[i];
14
15
       if(fabs(Cross(q[last].v, q[last-1].v)) < eps) {</pre>
16
         last--;
17
         if(OnLeft(q[last], L[i].P)) q[last] = L[i];
18
       if(first < last) p[last-1] = GetLineIntersection(q[last-1], q[last]);</pre>
19
20
21
      while(first < last && !OnLeft(q[first], p[last-1])) last--;</pre>
      if(last - first <= 1) return ans;</pre>
22
23
      p[last] = GetLineIntersection(q[last], q[first]);
24
      for(int i = first; i <= last; i++) ans.push_back(p[i]);</pre>
25
      return ans;
26
```

4 Math

4.1 ChinaRemainderTheory

```
// china remainder theory, no matter whether gcd(m[i],m[j])=1
LL CRT(const vector<LL>&m, const vector<LL> &b){
  bool flag = false;
LL x, y, i, d, result, a1, m1, a2, m2, Size = m.size();
  m1 = m[0], a1 = b[0];
  for(int i = 1; i < Size; i++){</pre>
```

```
7
       m2 = m[i], a2 = b[i];
 8
       d = exgcd(m1, m2, x, y);
 9
       if ((a2 - a1) % d != 0) flag = true;
10
       result = (mul_mod(x, (a2 - a1) / d, m2) \% m2 + m2) \% m2;
11
       LL tmp = m1;
       m1 = m1 / d * m2;
12
13
       a1 = (a1 + mul_mod(tmp, result, m1)) % m1;
14
       a1 = (a1 \% m1 + m1) \% m1;
15
      }
16
     if (flag) return -1;
17
      else return a1;
18
```

4.2 Decompose

```
1
   // eg: poj 3471
    const int maxn = 10000000;
    const int maxp = 700000; // about maxn/log(maxn)
 4
    struct Factor{ // factor as p^num
 5
     int p, num;
 6
   };
7
    struct DeComposer {
     DeComposer() { gen_primes(); }
 8
9
     bool vis[maxn+5];
10
     int pn, prime[maxp];
11
     void sieve() {
12
       int m = (int)sqrt(maxn+0.5);
13
       memset(vis,0,sizeof(vis));
14
       for(int i=2;i<=m;++i)if(!vis[i])</pre>
15
         for(int j=i*i;j<=maxn;j+=i)vis[j]=1;</pre>
16
      }
17
     void gen_primes() {
18
       sieve();
19
       pn = 0;
20
       for (int i = 2; i <= maxn; ++ i) {</pre>
21
         if (!vis[i]) prime[pn++] = i;
22
       }
23
      }
24
      int fcn;
      Factor fc[64]; // x = p1^a1 * p2^a2 * ...
25
      int fn, factor[maxp]; // all y satisify y|x
26
27
      void decompose2(int x,int d){
28
       if(d==fcn){
29
         factor[fn++] = x;
30
       } else {
         for(int i = 0; i <= fc[d].num; ++ i) {</pre>
31
32
           decompose2(x, d+1);
33
           x *= fc[d].p;
34
         }
35
       }
     }
36
```

```
37
      void decompose1(int x) {
38
       fcn = 0;
       for(int i = 0; i < pn && prime[i] * prime[i] <= x; ++ i) if (x % prime[i] == 0)
39
           {
40
         fc[fcn].p = prime[i];
41
         fc[fcn].num = 0;
42
         while(x % prime[i] == 0) {
43
          fc[fcn].num ++;
44
          x /= prime[i];
45
         }
46
         fcn ++;
47
       }
       if (x > 1) {
48
49
         fc[fcn].p = x;
50
         fc[fcn].num = 1;
51
         fcn ++;
52
       }
53
      }
54
      void decompose(int x){
55
       decompose1(x);
56
       fn = 0;
57
       decompose2(1,0);
     }
58
59
    } dc_solver;
```

4.3 EulerPhi

```
1
   // #x that x<=n && gcd(x,n)==1
 2
    int euler_phi(int n) {
 3
     int m = (int)sqrt(n+0.5);
 4
     int ans = n;
 5
     for (int i = 2; i <= m; ++ i) if (n % i == 0) {
 6
       ans = ans / i * (i-1);
 7
       while (n%i == 0) n /= i;
 8
     }
9
     if (n > 1) ans = ans / n * (n-1);
10
      return ans;
11
    }
    int phi[maxn];
12
13
    void phi_table(int n) {
14
     for (int i = 2; i <= n; ++ i) phi[i] = 0;</pre>
15
     phi[1] = 1;
16
      for (int i = 2; i <= n; ++ i) {
17
       if (!phi[i]) {
         for (int j = i; j <= n; j += i) {</pre>
18
19
          if (!phi[j]) phi[j] = j;
20
          phi[j] = phi[j] / i * (i-1);
21
         }
22
23
       phi[i] += phi[i-1];
24
     }
```

25 }

4.4 ExtendGCD

```
1  // a * x + b * y = d, |x| + |y| get the minimum
2  LL exgcd(LL a, LL b, LL &d, LL &x, LL &y){
3   if (a) { x = 0; y = 1; return a; }
4   else { exgcd(b, a%b, d, y, x); y -= x*(a/b); }
5  }
```

4.5 IntegerInverse

```
LL inv1(LL a, LL n) { // a^-1 under n
LL d, x, y;
gcd(a,n,d,x,y);
return d == 1 ? (x+n)%n : -1;
}
LL inv2(LL a, LL p) { // in case that p is a prime
return pow_mod(a, p-2, p);
}
```

4.6 LineMod

```
1
   // ax = b \pmod{n}
   // let d = gcd(a,n), use exgcd to solve ax + ny = d
   // if b|d, then there are #ans=d, otherwise, no solution
 4
    vector<LL> line_mod(LL a, LL b, LL n) {
 5
     LL x, y;
 6
     exgcd(a,n,x,y);
 7
     vector<LL>ans;
 8
     ans.clear();
 9
     if(b%d==0){
       x%=n; x+=n; x%=n;
10
11
       ans.push_back(x*(b/d)%(n/d));
12
       for(LL i=1;i<d;++i){</pre>
13
         ans.push_back((ans[0]+i*n/d)%n);
14
       }
15
      }
16
      return ans;
17
    }
```

4.7 LogMod

```
1  // eg: hdu 2815
2  // d*a^(x-c) = b (mod n), make sure that (a,n) = 1 and (d,n) = 1
3  map<LL,LL>f;
4  LL log_mod(LL a, LL b, LL n, LL c, LL d) {
```

```
5
      LL m, v, e=1, i, x, y, dd;
      m = ceil( sqrt(n + 0.5) );
 7
     f.clear();
 8
     f[1] = m;
9
     for(i = 1; i < m; ++ i) {</pre>
10
       e = e*a%n;
       if (!f[e]) f[e] = i;
11
12
13
      e = (e*a)%n;
     for (i = 0; i < m; ++ i) {</pre>
14
15
       exgcd(d,n,dd,x,y);
16
       x = (x*b%n + n) % n;
17
       if (f[x]) {
18
         LL num = f[x];
19
         return c + i*m + (num==m ? 0 : num);
20
       }
21
       d = (d*e) \% n;
22
23
      return -1;
24
25
    // a^x = b (mod n), no restriction
26
    LL log_mod(LL a, LL b, LL n) {
27
     b%=n;
28
      LL c = 0, d = 1, t;
29
      while((t=__gcd(a,n))!=1){
30
       if(b%t) return −1;
31
       c++;
32
       n/=t;
33
       b/=t;
34
       d=d*a/t%n;
35
       if(d==b)return c;
36
37
      return log_mod(a,b,n,c,d);
38
```

4.8 Lucas

```
1 // C(n,m) % p, make sure p is prime, p <= 10<sup>5</sup>
   // n = n[k] * p^k + n[k-1] * p^k-1 + ... + n[0]
    // m = m[k] * p^k + m[k-1] * p^k-1 + ... + m[0]
   // then, C(n,m) = C(n[k],m[k])*C(n[k-1],m[k-1])*..*C(n[0],m[0]) (mod p)
   // C(n,m) = C(n\%p, m\%p) * C(n/p, m/p) (mod p)
 6
   // eg: hdu3037
7
   LL Lucas(LL n, LL m, LL p) {
8
     LL ret = 1;
9
     while(n && m) {
10
       LL np = n%p, mp = m%p;
11
       if(np < mp) return 0;</pre>
       ret = ret * factorial(np) % p * reverse(factorial(mp), p) % p *
           reverse(factorial(np-mp), p) % p;
13
       n /= p;
```

4.9 MillerRabin

```
// prime test
1
2
   bool Witness(LL n, LL a) {
     LL m = n-1, j = 0;
 3
     while(!(m&1)) m >>= 1, j ++;
 4
 5
     LL ans = pow_mod(a, m, n);
 6
     while (j --) {
 7
       LL tmp = mul mod(ans, ans, n);
 8
       if (tmp == 1 \&\& ans != 1 \&\& ans != n-1) return 1;
9
       ans = tmp;
10
      }
11
      return ans != 1;
    }
12
13
    bool Miller_Rabin(LL n) {
     if (n < 2) return 0;</pre>
14
15
     if (n == 2) return 1;
     if (!(n&1)) return 0;
16
17
     for (int i = 0; i < max_test; ++ i) {</pre>
      11 a = rand() \% (n-2) + 2;
18
19
       if (Witness(n,a)) return 0;
20
     }
21
     return 1;
22
```

4.10 MulMod

```
1
   // x*y % n
 2
   LL mul_mod(LL x, LL y, LL n) {
     LL T = floor(sqrt(n) + 0.5);
     LL t = T * T - n;
 4
 5
     LL a = x / T, b = x % T;
     LL c = y / T, d = y % T;
 6
     LL e = a * c / T, f = a * c % T;
 7
 8
     LL v = ((a*d + b*c) % n + e*t) % n;
     LL g = v / T, h = v % T;
9
10
     LL ret = (((f+g)*t % n + b*d) % n + h*T) % n;
     return (ret % n + n) % n;
11
12
```

4.11 PollardRho

```
1 // get a factor of n in log(n)
2 LL Pollard_Rho(LL n, LL c=1) {
```

```
3
      LL i=1, k=2, x=rand()\%(n-1)+1, y=x, d;
 4
      while(1) {
 5
       i++;
 6
       x = (mul_mod(x,x,n)+c)%n;
 7
       d=gcd(n,y-x);
 8
       if(d>1 && d<n) return d;</pre>
9
       if(y==x) return n;
10
       if(i==k){
         k<<=1;
11
12
         y=x;
13
       }
14
      }
15
    }
```

4.12 PowMod

```
// a^x % n
 1
   LL pow_mod(LL a, LL x, LL n) {
 3
     LL ret = 1, mul = a;
     while (x) {
 5
       if (x&1) ret = mul_mod(ret, mul, n);
 6
       mul = mul_mod(mul, mul, n);
 7
       x >>= 1;
 8
     }
 9
     return ret;
10
```

4.13 PowerMod

```
// x^n = a \pmod{p}, make sure that p is prime
   // let g be a primitive root of p, x = g^y, a = g^m
   // use log_mod to get m, g^(yn) = g^m (mod p)
   // thus yn = m (mod p-1), use exgcd to solve and get back
 5
   vector<int> power_mod(int a, int n, int p) {
     int g = primitive_root(p);
 6
 7
     LL m = log_mod(g, a, p);
 8
     vector<int>ret;
9
     if(a==0){
10
       ret.push_back(0);
       return ;
11
12
     }
13
     if(m==-1)return ret;
14
     LL A=n,B=p-1,C=m,x,y;
15
     LL d = exgcd(A,B,x,y);
16
     if(C%d!=0)return ret;
     x=x*(C/d)%B;
17
18
     LL delta=B/d;
19
     for(int i=0;i<d;++i){</pre>
20
       x=((x+delta)\%B+B)\%B;
21
       ret.push_back((int)pow_mod(g,x,p));
```

```
22  }
23  sort(ret.begin(),ret.end());
24  ret.erase(unique(ret.begin(),ret.end()), ret.end());
25  return ret;
26  }
```

4.14 PrimitiveRoot

```
1
   // eg: SGU 511
    struct PR {
 2
      // make sure that p is prime
 4
     // if p = 2, solve the prob. without PR
 5
     int divs[N+5];
 6
     int primitive_root(const int p) {
 7
       if (p == 2) return 1;
 8
       int cnt = 0, m = p-1;
 9
       for (int i = 2; i*i <= m; ++ i) if (m%i == 0) {
10
         divs[cnt++] = i;
11
         if (i*i < m) divs[cnt++] = m/i;</pre>
12
       int r = 2, j = 0;
13
14
       while (1) {
         for (j = 0; j < cnt; ++ j) {</pre>
15
16
           if (fastpow(r, divs[j], p) == 1) break;
17
         }
18
         if (j >= cnt) return r;
19
         r ++;
20
       }
21
       return -1;
22
     }
23
   |} pr_solver;
```

4.15 SquareMod

```
// x*x = a \pmod{n}, make sure that n is prime
   // be careful there is a single sol. when n = 2
   // otherwise, x and n-x are both okay
 4
   // eg: ural 1132
 5
   LL modsqr(LL a, LL n) {
 6
     LL b, k, i, x;
 7
     if (n == 2) return a % n;
 8
     if (pow_mod(a, (n-1)/2, n) == 1) {
 9
       if (n%4 == 3) {
10
         x = pow_mod(a, (n+1)/4, n);
11
       }else{
        for(b=1; pow_mod(b, (n-1)/2, n) == 1; b ++);
12
13
         i = (n-1)/2;
14
         k = 0;
15
         do {
16
          i/=2;
```

```
17
          k/=2;
18
           if((pow_mod(a,i,n) * pow_mod(b,k,n)+1) %n == 0) {
19
            k += (n-1)/2;
20
          }
21
         } while(i%2 == 0);
22
         x = (pow_mod(a,(i+1)/2,n) * pow_mod(b,k/2,n)) %n;
23
24
       if(x*2 > n) x = n-x;
25
       return x;
26
      }
27
      return -1;
28
```

5 Others

5.1 ExactCover

```
// la 2659
1
 2
   #include <cstdio>
   #include <vector>
 3
 4 using namespace std;
 5
    const int MROW = 16*16*16 + 5;
    const int MCOL = 16*16*4 + 5;
 6
 7
    const int NODE = 16*16*16*4 + 5;
8
    struct DLX {
9
     int n, sz;
10
     int S[MCOL];
     int row[NODE], col[NODE];
11
     int ansd, ans[MROW];
12
13
     int L[NODE], R[NODE], U[NODE], D[NODE];
14
     void init(int n) {
15
       this->n = n;
16
       for (int i = 0; i <= n; ++ i) {
         U[i] = D[i] = i;
17
         L[i] = i-1; R[i] = i+1;
18
19
         S[i] = 0;
20
21
       R[n] = 0; L[0] = n;
22
       sz = n+1;
23
24
     void addRow(int r, const vector<int> &columns) {
25
       int first = sz;
26
       for (int i = 0; i < columns.size(); ++ i) {</pre>
27
         int c = columns[i];
28
         L[sz] = sz-1; R[sz] = sz+1;
29
         D[sz] = c; U[sz] = U[c];
30
         D[U[c]] = sz; U[c] = sz;
31
         row[sz] = r; col[sz] = c;
32
         S[c] ++; sz ++;
33
34
       R[sz-1] = first; L[first] = sz-1;
```

```
35
      }
36
      #define FOR(i,A,s) for(int i=A[s];i!=s;i=A[i])
37
      void remove(int c) {
38
       L[R[c]] = L[c]; R[L[c]] = R[c];
39
       FOR(i,D,c)
         FOR(j,R,i) \{ U[D[j]] = U[j]; D[U[j]] = D[j]; -- S[col[j]]; \}
40
41
      }
42
      void restore(int c) {
43
       FOR(i,U,c)
44
         FOR(j,L,i) { ++S[col[j]]; U[D[j]]=j; D[U[j]]=j; }
45
       L[R[c]] = c; R[L[c]] = c;
46
      }
47
      bool dfs(int d) {
48
       if (R[0] == 0) {
49
         ansd = d;
50
         return 1;
51
       }
52
       int c = R[0];
53
       FOR(i,R,0) if(S[i]<S[c]) c=i;</pre>
54
       remove(c);
55
       FOR(i,D,c) {
56
         ans[d] = row[i];
57
         FOR(j,R,i) remove(col[j]);
58
         if(dfs(d+1)) return 1;
59
         FOR(j,L,i) restore(col[j]);
60
       }
61
       restore(c);
62
       return 0;
63
      }
64
      bool solve(vector<int>&v) {
65
       v.clear();
66
       if (!dfs(0)) return 0;
       for (int i = 0; i < ansd; ++ i) v.push_back(ans[i]);</pre>
67
68
       return 1;
     }
69
70
    } dlx;
71
    char data[18][18];
72
    bool input() {
73
     for (int i = 0; i < 16; ++ i) {
74
       if (scanf("%s",data[i]) == EOF) return 0;
75
     }
76
      return 1;
77
    enum { SLOT=0, ROW, COL, BLOK };
78
79
    int encode(int i, int j, int k) {
80
     return i*256 + j*16 + k + 1;
81
82
    int block(int i, int j) {
83
      return 4*(i/4) + (j/4);
84
85
    void decode(int x, int &a, int &b, int &c) {
86
     x --;
     c = x \% 16; x /= 16;
```

```
88
      b = x \% 16; x /= 16;
89
      a = x;
90
91
     vector<int>columns;
92
     void solve() {
93
      dlx.init(16*16*4);
94
      for (int i = 0; i < 16; ++ i) {
95
        for (int j = 0; j < 16; ++ j) {
          for (int k = 0; k < 16; ++ k) {
96
97
           if (data[i][j] == '-' || data[i][j] == k+'A') {
98
             columns.clear();
99
             columns.push_back(encode(SLOT, i, j));
             columns.push_back(encode(ROW, i, k));
100
101
             columns.push_back(encode(COL, j, k));
102
             columns.push_back(encode(BLOK, block(i,j), k));
103
             dlx.addRow(encode(i,j,k), columns);
104
           }
105
          }
106
        }
107
      }
108
      columns.clear();
109
      dlx.solve(columns);
110
      for (int i = 0; i < columns.size(); ++ i) {</pre>
111
        int r, c, v;
112
        decode(columns[i], r, c, v);
113
        data[r][c] = char('A' + v);
114
115
      for (int i = 0; i < 16; ++ i) {
        printf("%s\n", data[i]);
116
117
118
119
    int main() {
120
      int kcase = 0;
121
      while (input()) {
        if (kcase) puts("");
122
123
        kcase ++;
124
        solve();
125
      }
126
    }
```

5.2 MatrixFastPower

```
1
   struct Matrix {
2
    int n, a[N][N];
3
    Matrix operator * (const Matrix &b) const {
4
      Matrix ret; ret.clear();
5
      ret.n = n;
6
      for (int i = 0; i < n; ++ i) {</pre>
7
        for (int k = 0; k < n; ++ k) if (a[i][k]) {
8
         for (int j = 0; j < n; ++ j) {
9
           ret.a[i][j] += a[i][k] * b.a[k][j];
```

```
10
            ret.a[i][j] %= mod;
11
          }
12
         }
13
14
       return ret;
15
      }
      void clear() {
16
17
       memset(a,0,sizeof(a));
18
     }
19
    };
20
    Matrix matrix_one(int n) {
21
     Matrix ret; ret.clear();
22
      ret.n = n;
23
      for (int i = 0; i < n; ++ i) {
24
       ret.a[i][i] = 1;
25
      }
26
      return ret;
27
   |Matrix matrix_pow(Matrix x, int n) {
28
29
     Matrix ret = matrix_one(x.n), mul = x;
30
     while (n) {
31
       if (n&1) ret = ret * mul;
32
       mul = mul * mul;
33
       n >>= 1;
34
     }
35
      return ret;
36
```

5.3 Polynomial

```
1
   // eg: UVALive 4305
    const int MAXN = 500;
    const double EPS = 1e-10;
   inline int sgn(const double &a) { return a > EPS ? 1 : (a < -EPS ? -1 : 0); }
 5
    struct Polynomial {
 6
     double data[MAXN];
 7
     int n;
 8
     Polynomial() {}
 9
     Polynomial(int _n) : n(_n) {
10
       memset(data, 0, sizeof(data));
11
12
     Polynomial(double *_data, int _n) {
13
       memset(data, 0, sizeof(data));
14
       n = _n;
       for (int i = n; i \ge 0; i--) data[i] = _data[i];
15
16
     Polynomial operator + (const Polynomial &a) {
17
18
       Polynomial c(max(n, a.n));
19
       for (int i = c.n; i \ge 0; i--) c.data[i] = data[i] + a.data[i];
20
       while (sgn(c.data[c.n]) == 0 && c.n) c.n--;
21
       return c;
```

```
22
     }
23
     Polynomial operator — (const Polynomial &a) {
24
       Polynomial c(max(n, a.n));
25
       for (int i = c.n; i \ge 0; i--) c.data[i] = data[i] - a.data[i];
26
       while (sgn(c.data[c.n]) == 0 && c.n) c.n--;
27
       return c;
28
29
     Polynomial operator * (const Polynomial &a) {
30
       Polynomial c(n + a.n);
31
       for (int i = n; i >= 0; i--) for (int j = a.n; j >= 0; j--) c.data[i + j] +=
           data[i] * a.data[j];
32
       return c;
33
     }
34
     Polynomial operator / (const Polynomial &a) {
35
       if (n < a.n) return *this;</pre>
36
       else {
37
         Polynomial c(n - a.n);
38
         for (int i = c.n; i \ge 0; i--) c.data[i] = data[i + a.n];
39
         for (int i = c.n; i >= 0; i--) {
40
          c.data[i] /= a.data[a.n];
41
          for (int j = i - 1; a.n - i + j >= 0 && j >= 0; j--) c.data[j] -=
               c.data[i] * a.data[a.n - i + j];
42
         }
43
         return c;
44
       }
45
     Polynomial operator % (const Polynomial &a) {
46
47
       Polynomial c = *this - *this / a * a;
48
       while (sgn(c.data[c.n]) == 0 && c.n) c.n--;
49
       return c;
50
     }
51
     bool iszero() {
52
       return n == 0 && sgn(data[0]) == 0;
53
54
     bool isconst() {
55
       return n > 0;
56
57
     Polynomial derivative() {
58
       Polynomial a(n - 1);
59
       for (int i = n - 1; i \ge 0; i - -) a.data[i] = data[i + 1] * (double)(i + 1);
60
       return a;
61
     Polynomial integral() {
62
63
       Polynomial a(n + 1);
       for (int i = n + 1; i >= 1; i --) a.data[i] = data[i - 1] / (double)i;
64
65
       return a;
66
     }
67
     void show() {
68
       for (int i = n; i >= 0; i--) {
69
         printf("%.6f", data[i], i);
70
         if (i != 0) printf(" x");
71
         if (i != 1 && i != 0) printf(" ^ %d", i);
72
         if (i != 0) printf(" + ");
```

```
73    else printf("\n");
74    }
75    }
76    };
77    Polynomial gcd(Polynomial a , Polynomial b) {
78     if (b.iszero()) return a;
79     else return gcd(b, a % b);
80    }
```

6 字符串

6.1 test

```
1
   > File Name: test.cpp
 2
    > Author: HKing
 3
    > Mail: 1470042308@qq.com
 5
    > Created Time: 2021年05月25日 星期二 15时20分17秒
 6
   ************************************
7
8
   #include <algorithm>
9
   #include <cmath>
10
   #include <cstring>
11
   #include <iostream>
   #include <map>
12
13
   #include <queue>
   #include <set>
   #include <stack>
15
   #include <string>
16
   #include <vector>
17
18
   #define IOS ios::sync_with_stdio(0), cin.tie(0), cout.tie(0)
   #define endl '\n'
19
20
   #define out(n) cout << n << ' '</pre>
   #define outl(n) cout << n << endl</pre>
21
22
   #define sd(n) scanf("%d", &n)
   #define sdd(n, m) scanf("%d%d", &n, &m)
24
   #define sddd(n, m, k) scanf("%d%d%d", &n, &m, &k)
   #define pd(n) printf("%d\n", (n))
25
26
   #define pdd(n, m) printf("%d %d\n", n, m)
27
   #define pddd(n, m, k) printf("%d %d %d\n", n, m, k)
   #define sld(n) scanf("%11d", &n)
28
29
   #define sldd(n, m) scanf("%lld%lld", &n, &m)
   #define slddd(n, m, k) scanf("%lld%lld", &n, &m, &k)
   #define pld(n) printf("%lld\n", n)
31
32
   #define pldd(n, m) printf("%lld %lld\n", n, m)
   #define plddd(n, m, k) printf("%lld %lld %lld\n", n, m, k)
   #define sf(n) scanf("%lf", &n)
34
   #define sff(n, m) scanf("%lf%lf", &n, &m)
35
36 | #define sfff(n, m, k) scanf("%lf%lf%lf", &n, &m, &k)
37 | #define ss(str) scanf("%s", str)
38 | #define ps(str) printf("%s", str)
```

```
#define x first
    #define y second
    #define pi acos(-1)
41
42
    #define de(c, n) \
43
     for (int i = 0; i < n; ++i) \</pre>
44
       cout << c; \
45
      cout << endl
46
    #define debug(a) cout << #a << '=' << a << endl</pre>
    #define INF_INT 0x3f3f3f3f;
47
48
    #define INF_LONG 4557430888798830399
    #define mem(ar, num) memset(ar, num, sizeof(ar))
   #define me(ar) memset(ar, 0, sizeof(ar))
   #define all(v) v.begin(), v.end()
51
52
   #define max(a, b, c) max(a, max(b, c))
53
    #define lowbit(x) (x & (-x))
54
    #define gcd(a, b) __gcd(a, b)
   #define lcm(a, b) a / gcd(a, b) * b
55
56
    #define qpow(a, k, p) \
57
     ({ \
58
       LL s = 1; \
59
       while (k > 0) \{ \
         if (k & 1) \
60
61
           s = s * a % p; \setminus
62
         a = a * a % p; \setminus
63
         k >>= 1; \
64
       } \
65
       s; \
66
     })
67
    #define inv(a, p) \
68
     ({ \
69
       LL q = p - 2; \setminus
70
       qpow(a, q, p); \
71
     })
72
    #define W(t) \
73
     cin >> t; \
74
     while (t--)
75
    using namespace std;
76
    typedef long long LL;
77
    typedef unsigned long long ULL;
78
   typedef pair<int, int> PII;
   typedef pair<int, PII> PIII;
79
80
    typedef pair<LL, LL> PLL;
81
   typedef pair<LL, PLL> PLLL;
82
83
    int main() {
84
     IOS;
85
86
      return 0;
87
```

7 数学

7.1 高斯消元

```
1
    // a[N][N]是增广矩阵
 2
   int gauss() {
 3
     int c, r;
 4
     for (c = 0, r = 0; c < n; c++) {
 5
       int t = r;
 6
       for (int i = r; i < n; i++) // 找到绝对值最大的行
 7
        if (fabs(a[i][c]) > fabs(a[t][c]))
 8
          t = i;
 9
       if (fabs(a[t][c]) < eps)</pre>
10
        continue;
11
12
13
       for (int i = c; i <= n; i++)
14
        swap(a[t][i], a[r][i]); // 将绝对值最大的行换到最顶端
15
       for (int i = n; i >= c; i--)
16
        a[r][i] /= a[r][c]; // 将当前行的首位变成1
       for (int i = r + 1; i < n; i++) // 用当前行将下面所有的列消成0
17
18
        if (fabs(a[i][c]) > eps)
19
          for (int j = n; j >= c; j--)
20
            a[i][j] -= a[r][j] * a[i][c];
21
22
       r++;
23
     }
24
25
     if(r < n) {
       for (int i = r; i < n; i++)</pre>
26
27
        if (fabs(a[i][n]) > eps)
          return 2; // 无解
28
       return 1; // 有无穷多组解
29
30
     }
31
32
     for (int i = n - 1; i >= 0; i--)
      for (int j = i + 1; j < n; j++)</pre>
33
34
        a[i][n] -= a[i][j] * a[j][n];
35
     return 0; // 有唯一解
36
37
   }
```

7.2 快速幂

```
8     t = t * t % p;
9     k >>= 1;
10     }
11     return res;
12 }
```

7.3 欧几里德

```
1 { return b ? gcd(b, a % b) : a; }
2 }
```

7.4 扩展欧几里德算法

```
// 求x, y, 使得ax + by = gcd(a, b)
   int exgcd(int a, int b, int &x, int &y) {
 3
     if (!b) {
 4
      x = 1;
 5
       y = 0;
 6
      return a;
7
     int d = exgcd(b, a % b, y, x);
8
9
     y -= (a / b) * x;
     return d;
10
11 | }
```

7.5 试除法分解质因数

```
1
    void divide(int x) {
 2
     for (int i = 2; i <= x / i; i++)
      if (x % i == 0) {
 3
        int s = 0;
 4
        while (x \% i == 0)
 5
 6
          x /= i, s++;
7
        cout << i << ' ' << s << endl;
8
       }
9
     if(x > 1)
       cout << x << ' ' << 1 << endl;
10
11
     cout << endl;</pre>
12 }
```

7.6 试除法判定质数

```
bool is_prime(int x) {
   if (x < 2)
     return false;
   for (int i = 2; i <= x / i; i++)
     if (x % i == 0)</pre>
```

```
6    return false;
7    return true;
8 }
```

7.7 试除法求所有约数

```
vector<int> get_divisors(int x) {
1
     vector<int> res;
     for (int i = 1; i <= x / i; i++)</pre>
 3
       if (x % i == 0) {
 4
 5
         res.push_back(i);
 6
        if (i != x / i)
 7
           res.push_back(x / i);
 8
 9
      sort(res.begin(), res.end());
10
      return res;
11
```

7.8 约数个数和约数之和

```
1 //如果 N = p1^c1 * p2^c2 * ... *pk^ck
2 //约数个数: (c1 + 1) * (c2 + 1) * ... * (ck + 1)
3 //约数之和: (p1^0 + p1^1 + ... + p1^c1) * ... * (pk^0 + pk^1 + ... + pk^ck)
```

7.9 组合数

7.9.1 递推法求组合数

7.9.2 通过预处理逆元的方式求组合数

```
1 //首先预处理出所有阶乘取模的余数fact[N],以及所有阶乘取模的逆元infact[N]
   //如果取模的数是质数,可以用费马小定理求逆元
3
  | int qmi(int a, int k, int p) // 快速幂模板
4
5
    int res = 1;
    while (k) {
6
7
     if (k & 1)
       res = (LL)res * a % p;
 9
      a = (LL)a * a % p;
      k >>= 1;
10
```

```
11
    }
12
     return res;
13
   }
14
15
   // 预处理阶乘的余数和阶乘逆元的余数
16 | fact[0] = infact[0] = 1;
   for (int i = 1; i < N; i++) {
17
18
    fact[i] = (LL)fact[i - 1] * i % mod;
     infact[i] = (LL)infact[i - 1] * qmi(i, mod - 2, mod) % mod;
19
20 | }
```

7.9.3 Lucas 定理求组合数

```
//若p是质数,则对于任意整数 1 <= m <= n,有:
   // C(n, m) = C(n \% p, m \% p) * C(n / p, m / p) (mod p)
3
   |int qmi(int a, int k, int p) // 快速幂模板
 5
   {
 6
     int res = 1 % p;
7
     while (k) {
8
      if (k & 1)
9
        res = (LL)res * a % p;
10
      a = (LL)a * a % p;
11
      k >>= 1;
12
     }
13
     return res;
14
15
   | int C(int a, int b, int p) // 通过定理求组合数C(a, b)
16
17
   {
18
     if (a < b)
19
      return 0;
20
21
     LL x = 1, y = 1; // x是分子, y是分母
     for (int i = a, j = 1; j <= b; i--, j++) {
22
23
      x = (LL)x * i % p;
24
      y = (LL)y * j % p;
25
     }
26
27
     return x * (LL)qmi(y, p - 2, p) % p;
28
   }
29
30
   int lucas(LL a, LL b, int p) {
     if (a < p && b < p)
31
32
      return C(a, b, p);
33
     return (LL)C(a % p, b % p, p) * lucas(a / p, b / p, p) % p;
34
```

7.9.4 分解质因数法求组合数

```
1 //当我们需要求出组合数的真实值,而非对某个数的余数时,分解质因数的方式比较好用:
  // 1. 筛法求出范围内的所有质数
  /// 2. 通过 C(a, b) = a! / b! / (a - b)! 这个公式求出每个质因子的次数。 n!
   // 中p的次数是 n / p + n / p^2 + n / p^3 + ...
   // 3. 用高精度乘法将所有质因子相乘
6
7
   int primes[N], cnt; // 存储所有质数
   int sum[N]; // 存储每个质数的次数
   bool st[N]; // 存储每个数是否已被筛掉
9
10
11
   void get_primes(int n) // 线性筛法求素数
12
13
    for (int i = 2; i <= n; i++) {
14
      if (!st[i])
15
        primes[cnt++] = i;
16
      for (int j = 0; primes[j] <= n / i; j++) {</pre>
17
        st[primes[j] * i] = true;
18
       if (i % primes[j] == 0)
19
         break;
20
      }
21
22
   }
23
24
   int get(int n, int p) // 求n! 中的次数
25
    int res = 0;
26
27
     while (n) {
28
      res += n / p;
29
      n /= p;
30
31
     return res;
32
   }
33
34
   vector<int> mul(vector<int> a, int b) // 高精度乘低精度模板
35
36
     vector<int> c;
37
     int t = 0;
38
     for (int i = 0; i < a.size(); i++) {</pre>
39
      t += a[i] * b;
40
      c.push_back(t % 10);
41
      t /= 10;
42
     }
43
44
     while (t) {
45
      c.push_back(t % 10);
46
      t /= 10;
47
     }
48
49
     return c;
50
51
52
   get_primes(a); // 预处理范围内的所有质数
53
```

```
54
   | for (int i = 0; i < cnt; i++) // 求每个质因数的次数
55
56
     int p = primes[i];
57
     sum[i] = get(a, p) - get(b, p) - get(a - b, p);
58
59
   vector<int> res;
60
61
   res.push_back(1);
62
63
   | for (int i = 0; i < cnt; i++) // 用高精度乘法将所有质因子相乘
64
    for (int j = 0; j < sum[i]; j++)</pre>
65
      res = mul(res, primes[i]);
```

7.10 欧拉函数

7.10.1 求欧拉函数

```
1
   int phi(int x) {
     int res = x;
 2
 3
     for (int i = 2; i <= x / i; i++)
 4
       if (x % i == 0) {
 5
         res = res / i * (i - 1);
         while (x \% i == 0)
 6
 7
          x /= i;
 8
       }
9
     if (x > 1)
       res = res / x * (x - 1);
10
11
12
     return res;
13
   }
```

7.10.2 筛法求欧拉函数

```
1
   |int primes[N], cnt; // primes[]存储所有素数
   |int euler[N]; // 存储每个数的欧拉函数
   bool st[N]; // st[x]存储x是否被筛掉
 3
4
   void get_eulers(int n) {
 6
     euler[1] = 1;
7
     for (int i = 2; i <= n; i++) {
8
      if (!st[i]) {
9
        primes[cnt++] = i;
10
        euler[i] = i - 1;
11
12
       for (int j = 0; primes[j] <= n / i; j++) {</pre>
13
        int t = primes[j] * i;
14
        st[t] = true;
15
        if (i % primes[j] == 0) {
          euler[t] = euler[i] * primes[j];
16
17
          break;
```

7.11 筛法

7.11.1 朴素筛法

```
1 int primes[N], cnt; // primes[]存储所有素数
   bool st[N]; // st[x]存储x是否被筛掉
   void get_primes(int n) {
4
5
     for (int i = 2; i <= n; i++) {</pre>
 6
      if (st[i])
 7
        continue;
 8
       primes[cnt++] = i;
 9
       for (int j = i + i; j <= n; j += i)
10
        st[j] = true;
11
     }
12
   }
```

7.11.2 线性筛法

```
int primes[N], cnt; // primes[]存储所有素数
2
   bool st[N]; // st[x]存储x是否被筛掉
 4
    void get_primes(int n) {
5
     for (int i = 2; i <= n; i++) {</pre>
 6
       if (!st[i])
 7
         primes[cnt++] = i;
 8
       for (int j = 0; primes[j] <= n / i; j++) {</pre>
9
         st[primes[j] * i] = true;
10
         if (i % primes[j] == 0)
11
          break;
12
       }
13
     }
14
```

8 数据结构

8.1 Trie 树

```
      1
      int son[N][26], cnt[N], idx;

      2
      // 0号点既是根节点,又是空节点

      3
      // son[][]存储树中每个节点的子节点

      4
      // cnt[]存储以每个节点结尾的单词数量
```

```
5
   // 插入一个字符串
 7
   void insert(char *str) {
8
     int p = 0;
9
     for (int i = 0; str[i]; i++) {
10
       int u = str[i] - 'a';
      if (!son[p][u])
11
12
        son[p][u] = ++idx;
13
       p = son[p][u];
14
     }
15
     cnt[p]++;
16
17
   // 查询字符串出现的次数
18
19
   int query(char *str) {
20
     int p = 0;
21
     for (int i = 0; str[i]; i++) {
22
       int u = str[i] - 'a';
23
       if (!son[p][u])
24
        return 0;
25
       p = son[p][u];
26
     }
27
     return cnt[p];
28
```

8.2 并查集.cpp

```
(1) 朴素并查集:
1
 2
3
      int p[N]; //存储每个点的祖宗节点
4
5
   // 返回X的祖宗节点
  int find(int x) {
7
    if (p[x] != x)
8
      p[x] = find(p[x]);
9
    return p[x];
10
11
   // 初始化,假定节点编号是1~n
12
   for (int i = 1; i <= n; i++)
13
    p[i] = i;
14
15
   // 合并a和b所在的两个集合:
16
   p[find(a)] = find(b);
17
18
19
   (2) 维护size的并查集:
20
21
      int p[N],
      size[N];
  // p[]存储每个点的祖宗节点,
23
24 // size[]只有祖宗节点的有意义,表示祖宗节点所在集合中的点的数量
```

```
25
26
   // 返回X的祖宗节点
27
   int find(int x) {
28
     if (p[x] != x)
29
      p[x] = find(p[x]);
30
     return p[x];
31
   }
32
   // 初始化,假定节点编号是1~n
33
34
   for (int i = 1; i <= n; i++) {
35
    p[i] = i;
36
     size[i] = 1;
37
38
39
   // 合并a和b所在的两个集合:
40
   size[find(b)] += size[find(a)];
41
   p[find(a)] = find(b);
42
43
   (3) 维护到祖宗节点距离的并查集:
44
45
      int p[N],
46
      d[N];
47
   // p[]存储每个点的祖宗节点, d[x]存储x到p[x]的距离
48
49
   // 返回X的祖宗节点
50
   int find(int x) {
51
     if (p[x] != x) {
52
      int u = find(p[x]);
53
      d[x] += d[p[x]];
54
      p[x] = u;
55
56
     return p[x];
57
58
59
   // 初始化,假定节点编号是1~n
60
   for (int i = 1; i <= n; i++) {
61
     p[i] = i;
     d[i] = 0;
62
63
64
65
   // 合并a和b所在的两个集合:
66
   p[find(a)] = find(b);
   |d[find(a)] = distance; // 根据具体问题, 初始化find(a)的偏移量
```

9 图论

9.1 test

```
4
   > Mail: 1470042308@qq.com
    > Created Time: 2021年05月25日 星期二 15时21分42秒
   8
   #include <algorithm>
9
   #include <cmath>
   #include <cstring>
10
   #include <iostream>
   #include <map>
12
   #include <queue>
13
   #include <set>
15
   #include <stack>
   #include <string>
16
17
   #include <vector>
18
   #define IOS ios::sync_with_stdio(0), cin.tie(0), cout.tie(0)
19
   #define endl '\n'
20 | #define out(n) cout << n << ' '
   #define outl(n) cout << n << endl</pre>
   #define sd(n) scanf("%d", &n)
22
23
   #define sdd(n, m) scanf("%d%d", &n, &m)
24
   #define sddd(n, m, k) scanf("%d%d%d", &n, &m, &k)
25
   #define pd(n) printf("%d\n", (n))
   #define pdd(n, m) printf("%d %d\n", n, m)
   #define pddd(n, m, k) printf("%d %d %d\n", n, m, k)
   #define sld(n) scanf("%lld", &n)
28
29
   #define sldd(n, m) scanf("%lld%lld", &n, &m)
   #define slddd(n, m, k) scanf("%11d%11d%11d", &n, &m, &k)
30
31
   #define pld(n) printf("%lld\n", n)
32 | #define pldd(n, m) printf("%lld %lld\n", n, m)
   #define plddd(n, m, k) printf("%lld %lld %lld\n", n, m, k)
   #define sf(n) scanf("%lf", &n)
   #define sff(n, m) scanf("%lf%lf", &n, &m)
35
   #define sfff(n, m, k) scanf("%lf%lf", &n, &m, &k)
36
37
   #define ss(str) scanf("%s", str)
   #define ps(str) printf("%s", str)
38
39
   #define x first
   #define y second
   #define pi acos(-1)
41
42
   #define de(c, n) \
43
     for (int i = 0; i < n; ++i) \
44
      cout << c; \
45
     cout << endl
   #define debug(a) cout << #a << '=' << a << endl</pre>
   #define INF INT 0x3f3f3f3f3f;
47
48
   #define INF_LONG 4557430888798830399
   #define mem(ar, num) memset(ar, num, sizeof(ar))
   #define me(ar) memset(ar, 0, sizeof(ar))
51
   #define all(v) v.begin(), v.end()
52
   #define max(a, b, c) max(a, max(b, c))
53
   #define lowbit(x) (x & (-x))
54 | #define gcd(a, b) __gcd(a, b)
55 | #define lcm(a, b) a / gcd(a, b) * b
56 | #define qpow(a, k, p) \
```

```
57
      ({ \
58
       LL s = 1; \
59
       60
         if (k & 1) \
61
           s = s * a % p; \setminus
62
         a = a * a % p; \setminus
63
         k >>= 1; \setminus
64
       } \
65
       s; \
66
     })
67
    #define inv(a, p) \
68
     ({ \
69
       LL q = p - 2; \setminus
70
       qpow(a, q, p); \
71
72
    #define W(t) \
73
     cin >> t; \
74
     while (t--)
75
    using namespace std;
    typedef long long LL;
76
77
    typedef unsigned long long ULL;
    typedef pair<int, int> PII;
78
79
   typedef pair<int, PII> PIII;
    typedef pair<LL, LL> PLL;
    typedef pair<LL, PLL> PLLL;
81
82
83
    int main() {
84
     IOS;
85
86
      return 0;
87
```

10 动态规划

10.1 test

```
1
  2
  > File Name: test.cpp
  > Author: HKing
3
4
  > Mail: 1470042308@qq.com
  > Created Time: 2021年05月25日 星期二 15时23分33秒
  6
7
  #include <algorithm>
8
  #include <cmath>
9
  #include <cstring>
11
  #include <iostream>
12
  #include <map>
13 | #include <queue>
14 #include <set>
15 | #include <stack>
```

```
16
    #include <string>
17
    #include <vector>
    #define IOS ios::sync_with_stdio(0), cin.tie(0), cout.tie(0)
18
19
    #define endl '\n'
    #define out(n) cout << n << ' '</pre>
21
   |#define outl(n) cout << n << endl
    #define sd(n) scanf("%d", &n)
22
   #define sdd(n, m) scanf("%d%d", &n, &m)
24
    #define sddd(n, m, k) scanf("%d%d%d", &n, &m, &k)
    #define pd(n) printf("%d\n", (n))
25
    #define pdd(n, m) printf("%d %d\n", n, m)
27
    #define pddd(n, m, k) printf("%d %d %d\n", n, m, k)
   #define sld(n) scanf("%lld", &n)
28
29
    #define sldd(n, m) scanf("%lld%lld", &n, &m)
30
    #define slddd(n, m, k) scanf("%lld%lld", &n, &m, &k)
31
    #define pld(n) printf("%lld\n", n)
   #define pldd(n, m) printf("%lld %lld\n", n, m)
    #define plddd(n, m, k) printf("%lld %lld %lld\n", n, m, k)
    #define sf(n) scanf("%lf", &n)
34
35
   #define sff(n, m) scanf("%lf%lf", &n, &m)
    #define sfff(n, m, k) scanf("%lf%lf%lf", &n, &m, &k)
36
37
    #define ss(str) scanf("%s", str)
38
   #define ps(str) printf("%s", str)
39
    #define x first
40
    #define y second
41
    #define pi acos(-1)
42
    #define de(c, n) \
43
     for (int i = 0; i < n; ++i) \
44
       cout << c; \
45
     cout << endl
46
    #define debug(a) cout << #a << '=' << a << endl</pre>
47
    #define INF_INT 0x3f3f3f3f;
48
    #define INF LONG 4557430888798830399
49
    #define mem(ar, num) memset(ar, num, sizeof(ar))
   #define me(ar) memset(ar, 0, sizeof(ar))
50
51
    #define all(v) v.begin(), v.end()
   #define max(a, b, c) max(a, max(b, c))
53
    #define lowbit(x) (x & (-x))
54
    #define gcd(a, b) __gcd(a, b)
    #define lcm(a, b) a / gcd(a, b) * b
56
    #define qpow(a, k, p) \
57
     ({ \
       LL s = 1; \
58
59
       while (k > 0) { \
60
         if (k & 1) \
61
          s = s * a % p; \setminus
62
         a = a * a % p; \setminus
63
         k >>= 1; \
64
       } \
65
       s; \
66
     })
67
    #define inv(a, p) \
68
     ({ \
```

```
LL q = p - 2; \
69
70
       qpow(a, q, p); \
71
     })
72
    #define W(t) \
73
     cin >> t; \
74
     while (t--)
75
    using namespace std;
   typedef long long LL;
77
    typedef unsigned long long ULL;
78
    typedef pair<int, int> PII;
   typedef pair<int, PII> PIII;
   typedef pair<LL, LL> PLL;
80
   typedef pair<LL, PLL> PLLL;
81
82
83
    int main() {
84
     IOS;
85
86
     return 0;
87
    }
```

11 计算几何

11.1 test

```
1
  2
   > File Name: test.cpp
 3
    > Author: HKing
   > Mail: 1470042308@qq.com
 4
    > Created Time: 2021年05月25日 星期二 15时23分57秒
   **********************************
7
  #include <algorithm>
8
   #include <cmath>
  #include <cstring>
10
  #include <iostream>
11
   #include <map>
13
  #include <queue>
14 #include <set>
   #include <stack>
15
  #include <string>
17
  #include <vector>
18
   #define IOS ios::sync_with_stdio(0), cin.tie(0), cout.tie(0)
19
  |#define endl '\n'
  #define out(n) cout << n << ' '</pre>
20
21
  #define outl(n) cout << n << endl</pre>
  #define sd(n) scanf("%d", &n)
   #define sdd(n, m) scanf("%d%d", &n, &m)
23
24
   #define sddd(n, m, k) scanf("%d%d%d", &n, &m, &k)
25 | #define pd(n) printf("%d\n", (n))
26 | #define pdd(n, m) printf("%d %d\n", n, m)
27 | #define pddd(n, m, k) printf("%d %d %d\n", n, m, k)
```

```
#define sld(n) scanf("%11d", &n)
28
    #define sldd(n, m) scanf("%lld%lld", &n, &m)
    #define slddd(n, m, k) scanf("%lld%lld", &n, &m, &k)
30
31
    #define pld(n) printf("%lld\n", n)
    #define pldd(n, m) printf("%lld %lld\n", n, m)
    #define plddd(n, m, k) printf("%lld %lld %lld\n", n, m, k)
33
    #define sf(n) scanf("%lf", &n)
34
   #define sff(n, m) scanf("%lf%lf", &n, &m)
    #define sfff(n, m, k) scanf("%lf%lf", &n, &m, &k)
36
37
    #define ss(str) scanf("%s", str)
    #define ps(str) printf("%s", str)
39
    #define x first
40
    #define y second
41
    #define pi acos(-1)
42
    #define de(c, n) \
43
     for (int i = 0; i < n; ++i) \
44
       cout << c; \
     cout << endl
45
    #define debug(a) cout << #a << '=' << a << endl</pre>
46
47
    #define INF INT 0x3f3f3f3f3f;
48
    #define INF_LONG 4557430888798830399
49
    #define mem(ar, num) memset(ar, num, sizeof(ar))
50
    #define me(ar) memset(ar, 0, sizeof(ar))
    #define all(v) v.begin(), v.end()
52
    #define max(a, b, c) max(a, max(b, c))
53
    #define lowbit(x) (x & (-x))
54
    #define gcd(a, b) __gcd(a, b)
55
    #define lcm(a, b) a / gcd(a, b) * b
    #define qpow(a, k, p) \
56
57
     ({ \
58
       LL s = 1; \
59
       while (k > 0) \{ \
60
         if (k & 1) \
61
          s = s * a % p; \setminus
         a = a * a % p; \setminus
62
63
         k >>= 1; \
64
       } \
65
       s; \
66
     })
    #define inv(a, p) \
67
68
69
       LL q = p - 2; \
70
       qpow(a, q, p); \
71
72
    #define W(t) \
73
     cin >> t; \
74
     while (t--)
75
    using namespace std;
76
    typedef long long LL;
77
    typedef unsigned long long ULL;
78
   typedef pair<int, int> PII;
   typedef pair<int, PII> PIII;
80 | typedef pair<LL, LL> PLL;
```

```
81     typedef pair<LL, PLL> PLLL;
82
83     int main() {
84         IOS;
85         return 0;
87     }
```

12 其他

```
12.1 test
```

```
前提: 安装好 xelatex
git clone https://github.com/HKing147/ACM-Template.git

cd ACM-template/.fonts/
cp ./* /usr/share/fonts/
mkfontscale
mkfontdir
fc-cache

cd ..
```

使用

make

```
1
  2
   > File Name: test.cpp
3
   > Author: HKing
   > Mail: 1470042308@gg.com
5
   > Created Time: 2021年05月25日 星期二 15时24分28秒
   6
8
  #include <algorithm>
9
  #include <cmath>
10
   #include <cstring>
11
  #include <iostream>
12 | #include <map>
   #include <queue>
13
14
  #include <set>
15
  #include <stack>
   #include <string>
16
17
  #include <vector>
  #define IOS ios::sync_with_stdio(0), cin.tie(0), cout.tie(0)
18
   #define endl '\n'
19
  #define out(n) cout << n << ' '</pre>
21 | #define outl(n) cout << n << endl
22 | #define sd(n) scanf("%d", &n)
23 | #define sdd(n, m) scanf("%d%d", &n, &m)
24 | #define sddd(n, m, k) scanf("%d%d%d", &n, &m, &k)
```

```
#define pd(n) printf("%d\n", (n))
    #define pdd(n, m) printf("%d %d\n", n, m)
27
    #define pddd(n, m, k) printf("%d %d %d\n", n, m, k)
28
    #define sld(n) scanf("%lld", &n)
29
    #define sldd(n, m) scanf("%lld%lld", &n, &m)
   #define slddd(n, m, k) scanf("%lld%lld", &n, &m, &k)
30
    #define pld(n) printf("%lld\n", n)
31
   #define pldd(n, m) printf("%lld %lld\n", n, m)
33
    #define plddd(n, m, k) printf("%lld %lld %lld\n", n, m, k)
34
    #define sf(n) scanf("%lf", &n)
    #define sff(n, m) scanf("%lf%lf", &n, &m)
    #define sfff(n, m, k) scanf("%lf%lf%lf", &n, &m, &k)
    #define ss(str) scanf("%s", str)
37
38
    #define ps(str) printf("%s", str)
39
    #define x first
40
    #define y second
41
    #define pi acos(-1)
42
    #define de(c, n) \
43
     for (int i = 0; i < n; ++i) \</pre>
44
       cout << c; \
45
     cout << endl
46
    #define debug(a) cout << #a << '=' << a << endl</pre>
47
    #define INF_INT 0x3f3f3f3f;
48
    #define INF LONG 4557430888798830399
    #define mem(ar, num) memset(ar, num, sizeof(ar))
49
50
    #define me(ar) memset(ar, 0, sizeof(ar))
    #define all(v) v.begin(), v.end()
51
52
    #define max(a, b, c) max(a, max(b, c))
53
   #define lowbit(x) (x & (-x))
54
    #define gcd(a, b) __gcd(a, b)
    #define lcm(a, b) a / gcd(a, b) * b
56
   #define qpow(a, k, p) \
57
     ({ \
58
       LL s = 1; \
59
       while (k > 0) \{ \
60
         if (k & 1) \
          s = s * a % p; \
61
         a = a * a % p; \setminus
62
63
         k >>= 1; \
64
       } \
65
       s; \
66
     })
67
    #define inv(a, p) \
68
69
       LL q = p - 2; \
70
       qpow(a, q, p); \
71
     })
72
    #define W(t) \
73
     cin >> t; \
74
     while (t--)
75
    using namespace std;
76 typedef long long LL;
77 | typedef unsigned long long ULL;
```

```
78 | typedef pair<int, int> PII;
   typedef pair<int, PII> PIII;
   typedef pair<LL, LL> PLL;
80
   typedef pair<LL, PLL> PLLL;
81
82
   int main() {
83
84
     IOS;
85
86
     return 0;
87
   }
```