

Count digits in a factorial - Using

Kamenetsky's formula

$$d(n!) = \log_{10}((n/e)^n * \sqrt{2 * \pi * n})$$

$$d(n!) = \log_{10}((n/e)^n) + \log_{10}(\sqrt{2 * \pi * n})$$

$$d(n!) = \log_{10}((n/e)^n) + (1/2) * \log_{10}(2 * \pi * n)$$

$$d(n!) = \log_{10}((n/e)^n) + (\log_{10}(2 * \pi * n))/2$$

It approximates the number of digits in a factorial by :

$$f(x) = \log_{10}((n/e)^n * \text{sqrt}(2 * \pi * n))$$

Thus, we can pretty easily use the property of logarithms to,

$$f(x) = n * \log_{10}(n/e) + \log_{10}(2 * \pi * n)/2$$