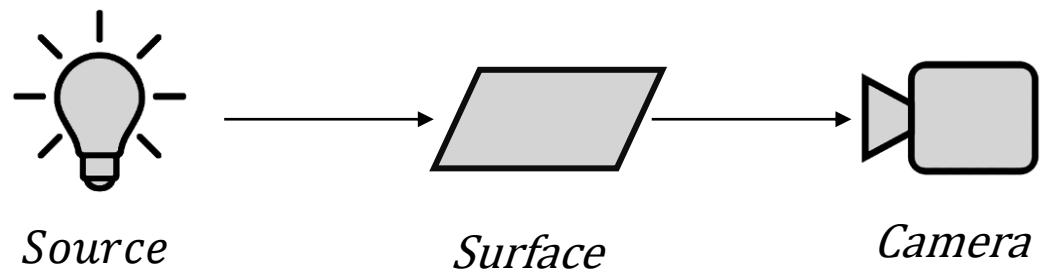
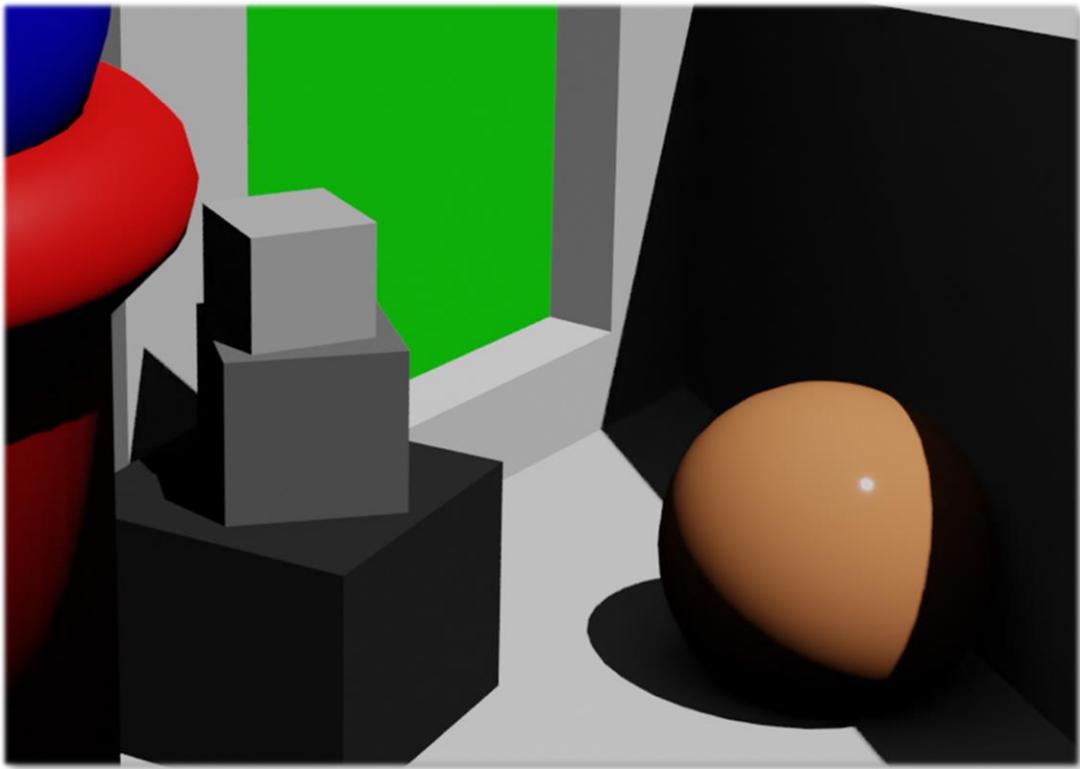


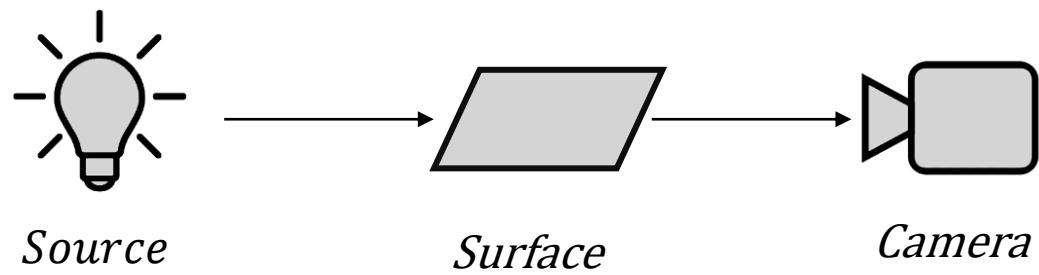
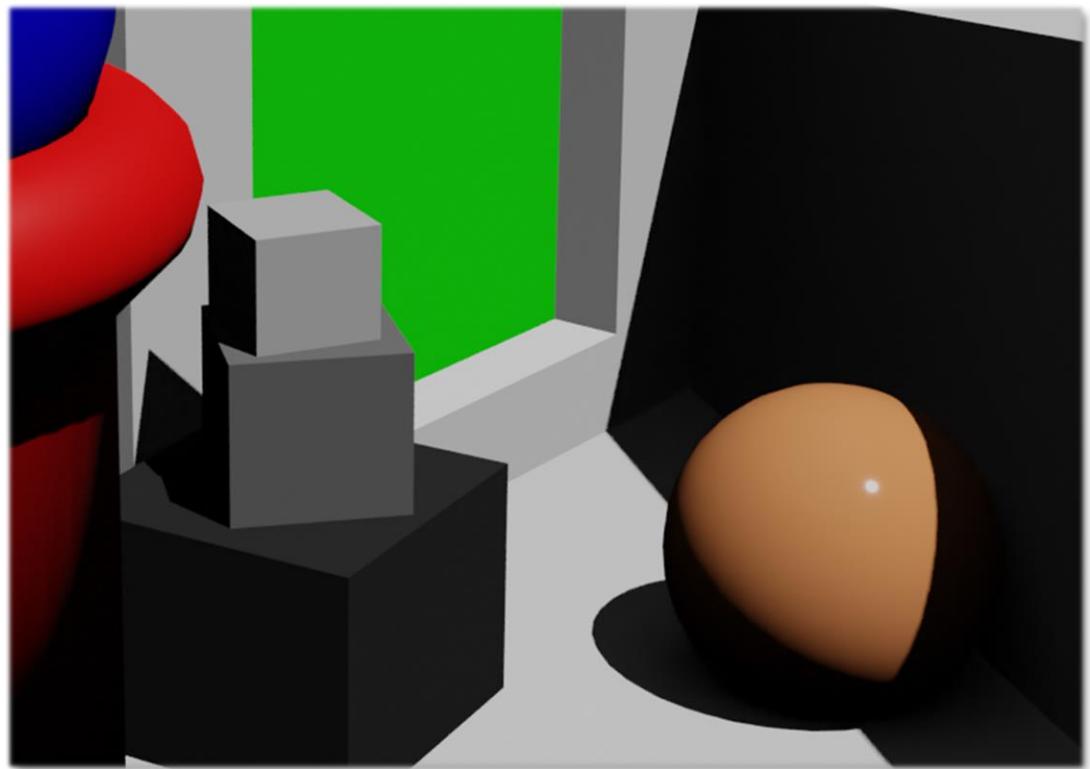
# Hardware Acceleration of Progressive Refinement Radiosity using Nvidia RTX

Benjamin Kahl  
10.11.2022

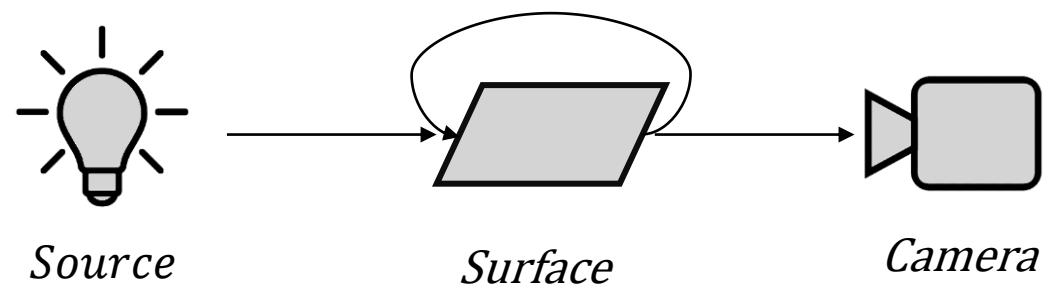
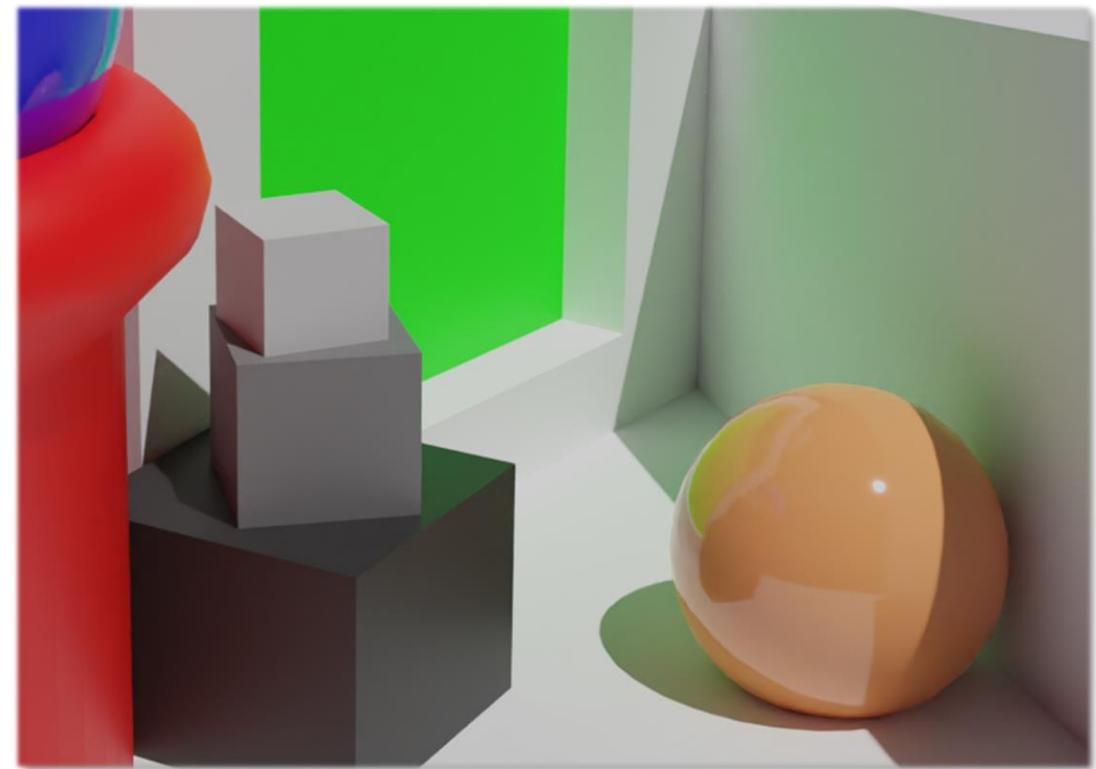
## Local Illumination

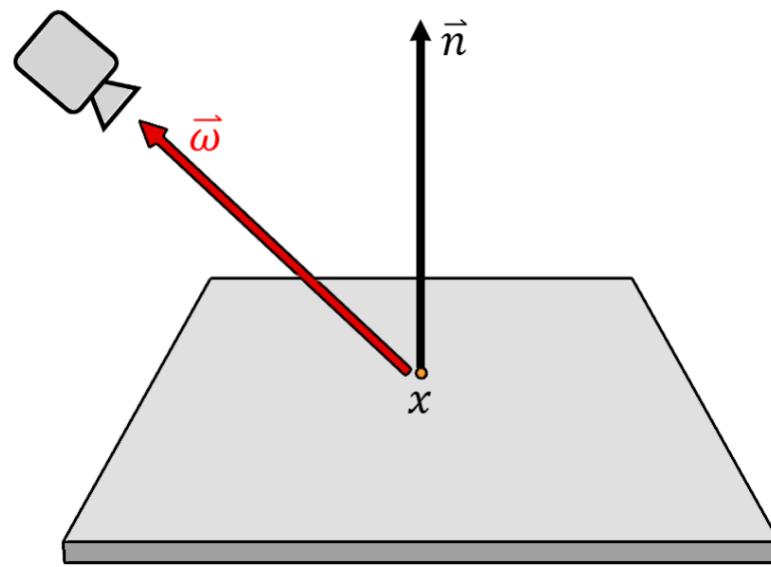


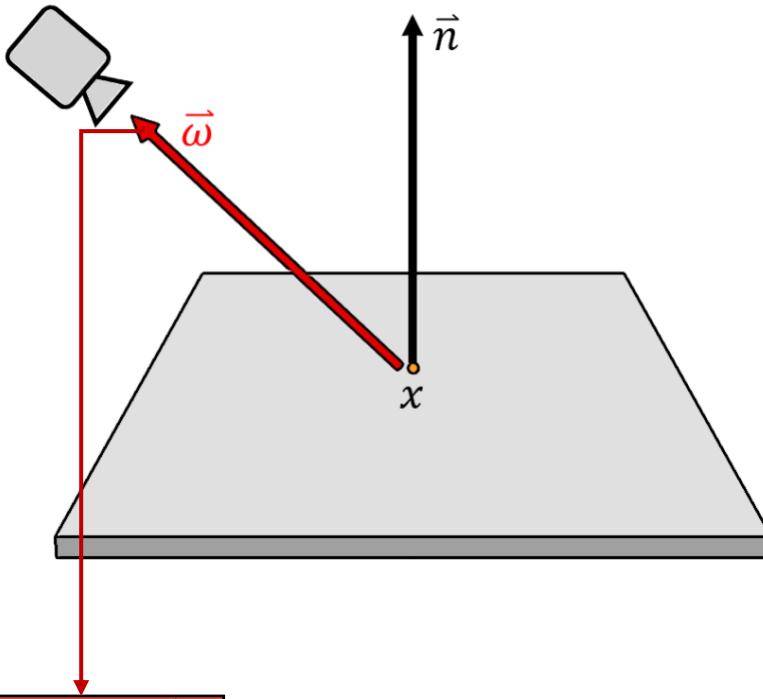
**Local Illumination**



**Global Illumination**



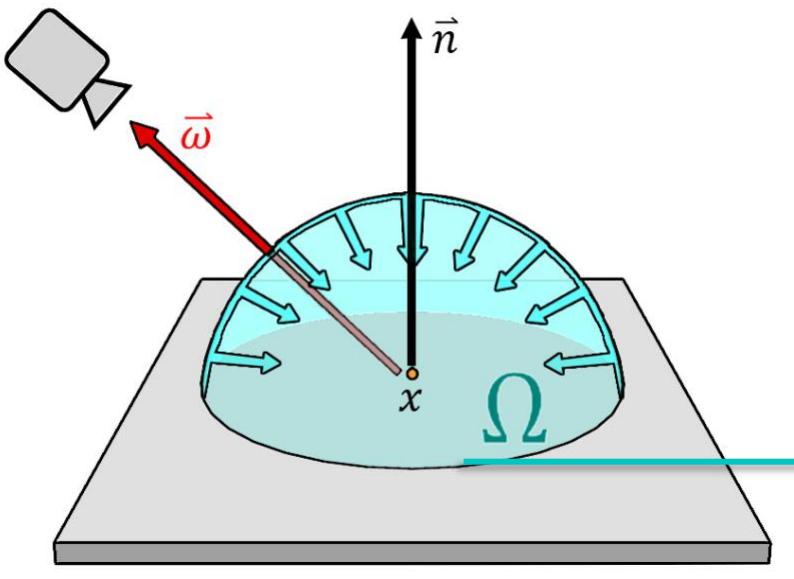




**Rendering Equation:**

(Kajiya et al. 1986)

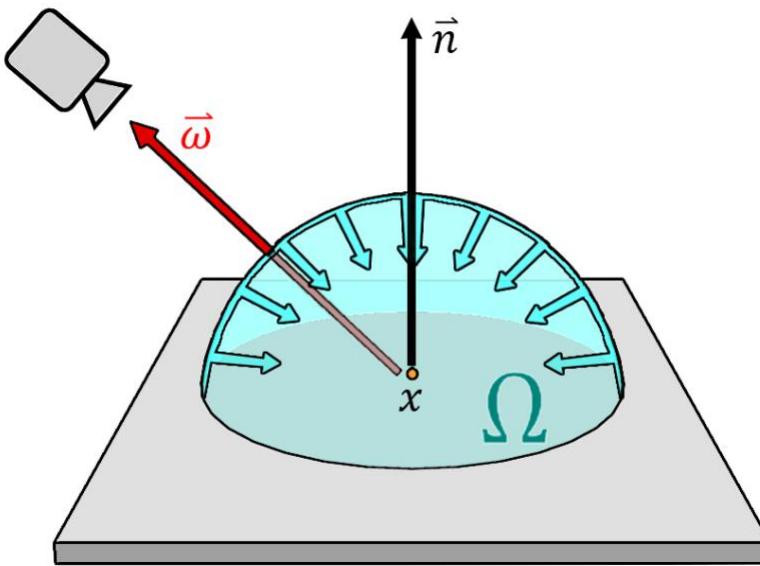
$$L(x, \vec{\omega}) = L_e(x, \vec{\omega}) + L_r(x, \vec{\omega})$$



### Rendering Equation:

(Kajiya et al. 1986)

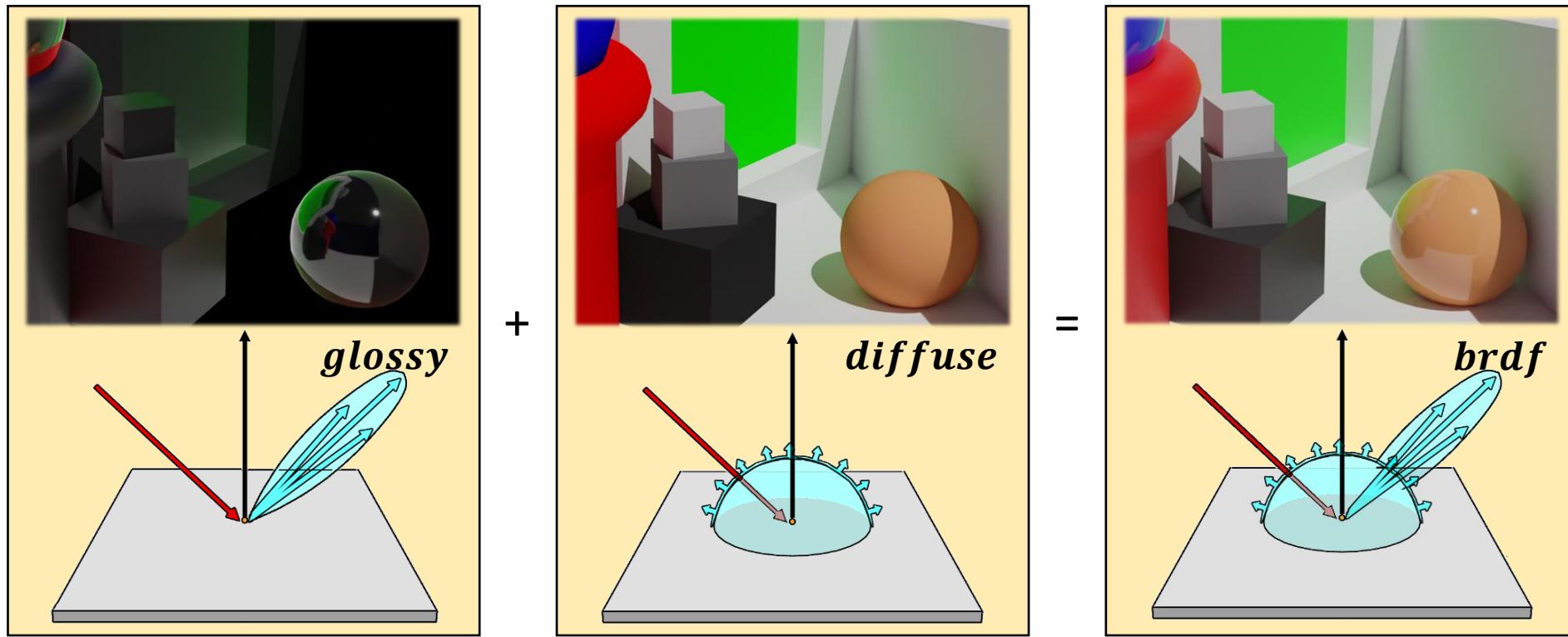
$$L(x, \vec{\omega}) = L_e(x, \vec{\omega}) + \int_{\Omega} L_i(x, \vec{\omega}') \dots$$



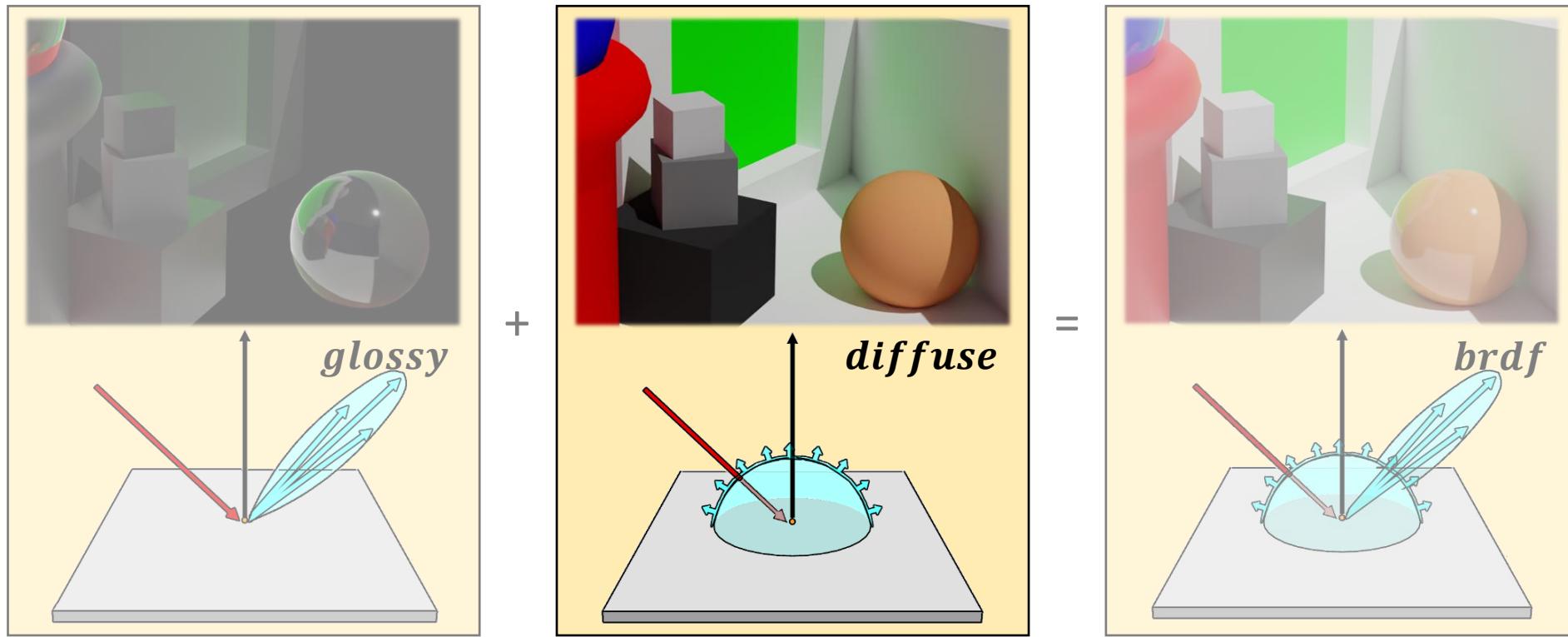
**Rendering Equation:**

(Kajiya et al. 1986)

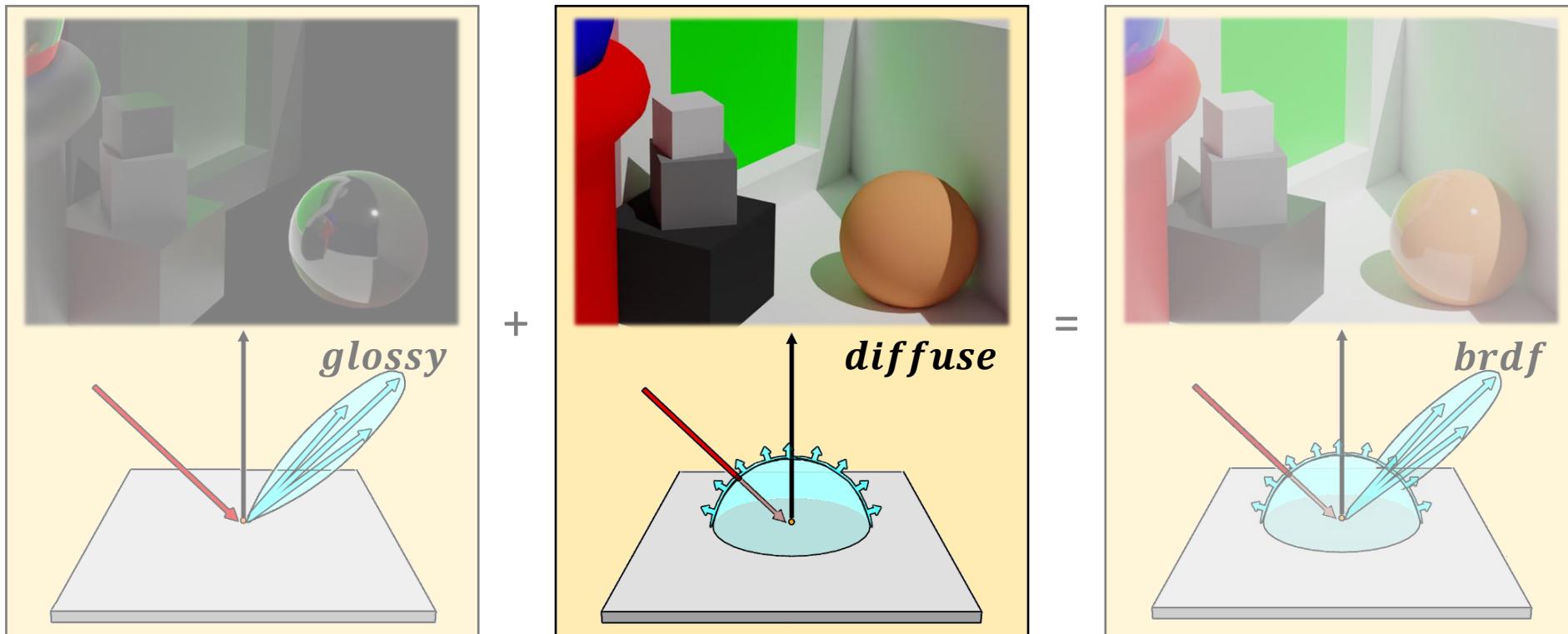
$$L(x, \vec{\omega}) = L_e(x, \vec{\omega}) + \int_{\Omega} L_i(x, \vec{\omega}') f_r(\vec{\omega}' \rightarrow \vec{\omega}) \cos \theta' d\omega'$$



$$L(x, \vec{\omega}) = L_{e(x, \vec{\omega})} + \int_{\Omega} L_i(x, \vec{\omega}') f_r(\vec{\omega}' \rightarrow \vec{\omega}) \cos \theta' d\omega'$$



$$L(x, \vec{\omega}) = L_{e(x, \vec{\omega})} + \int_{\Omega} L_i(x, \vec{\omega}') f_r(\vec{\omega}' \rightarrow \vec{\omega}) \cos \theta' d\omega'$$

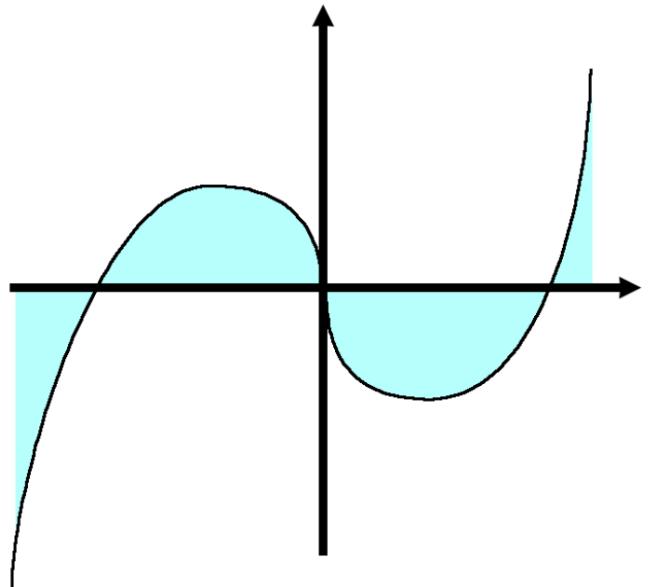


$$L(x, \vec{\omega}) = L_{e(x, \vec{\omega})} + \frac{\rho}{\pi} \int_{\Omega} L_i(x, \vec{\omega}') \cos \theta' d\omega'$$

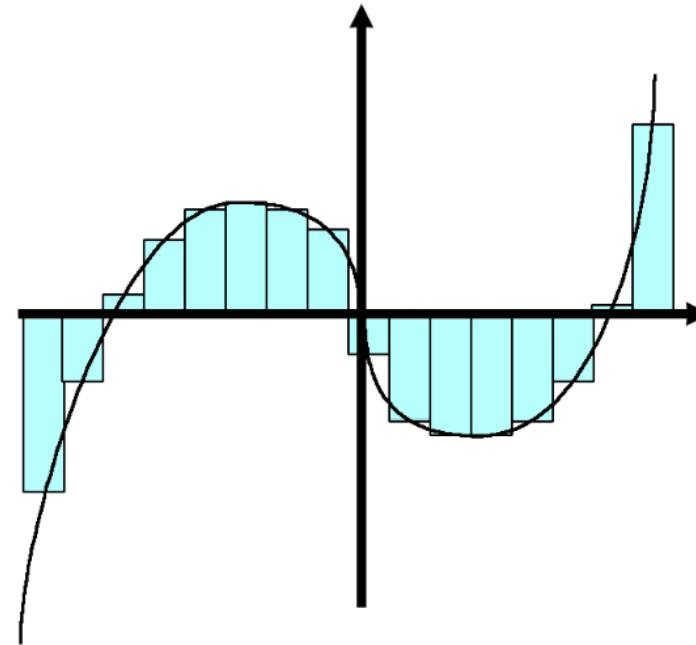
$$L(x,\overrightarrow{\omega})=L_{e(x,\overrightarrow{\omega})}+\boxed{\frac{\rho}{\pi}}\int\limits_{\Omega}\boxed{L_i\big(x,\overrightarrow{\omega'}\big)}\cos\theta'\,d\omega'$$

$$L(x,\vec{\omega}) = L_{e(x,\vec{\omega})} + \boxed{\frac{\rho}{\pi}} \int\limits_S L_o\left(x',\overrightarrow{\omega'}\right) V(x,x') \boxed{\frac{\cos\theta \cos\theta'}{|x-x'|^2}} d\omega'$$

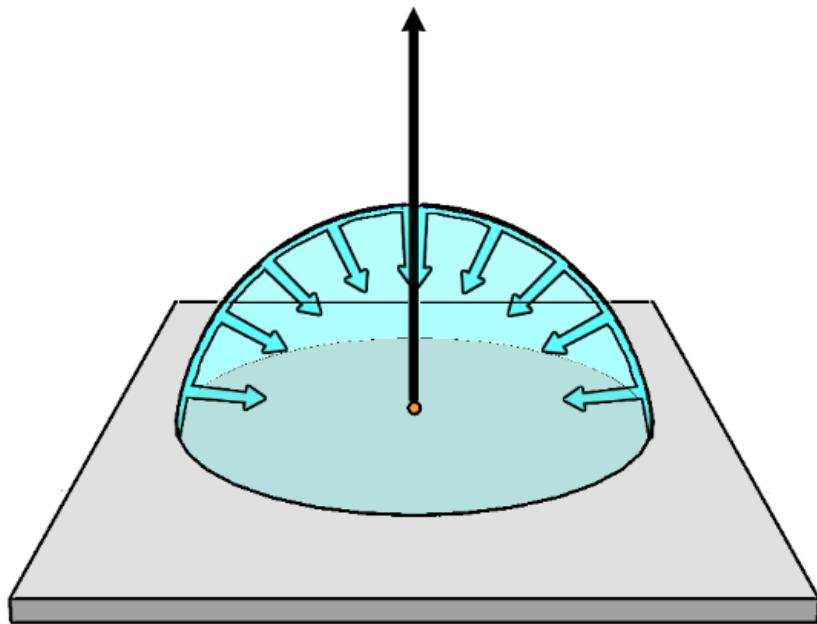
$$L(x,\vec{\omega}) = L_{e(x,\vec{\omega})} + \boxed{\frac{\rho}{\pi}} \int\limits_\Omega L_i\left(x,\overrightarrow{\omega'}\right) \cos\theta' d\omega'$$



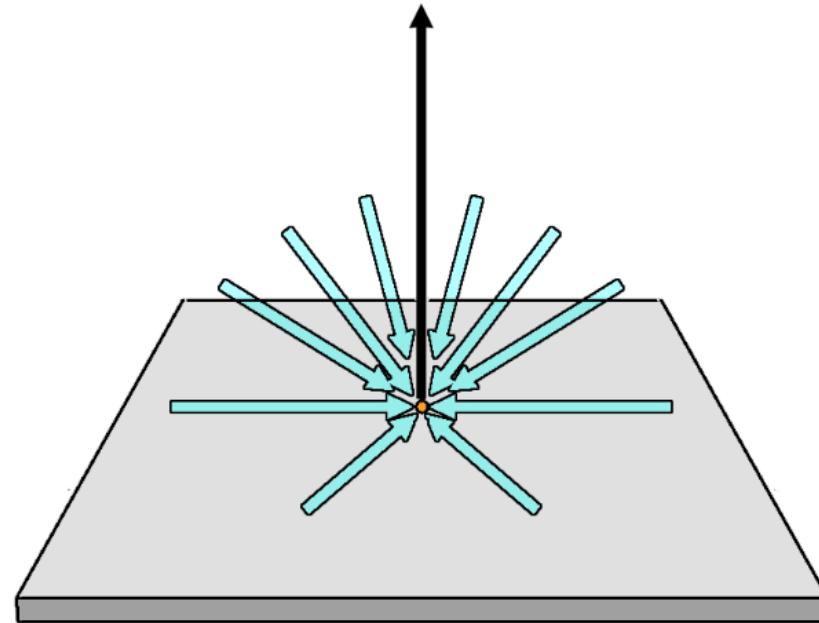
$$\int f(x) \, dx$$



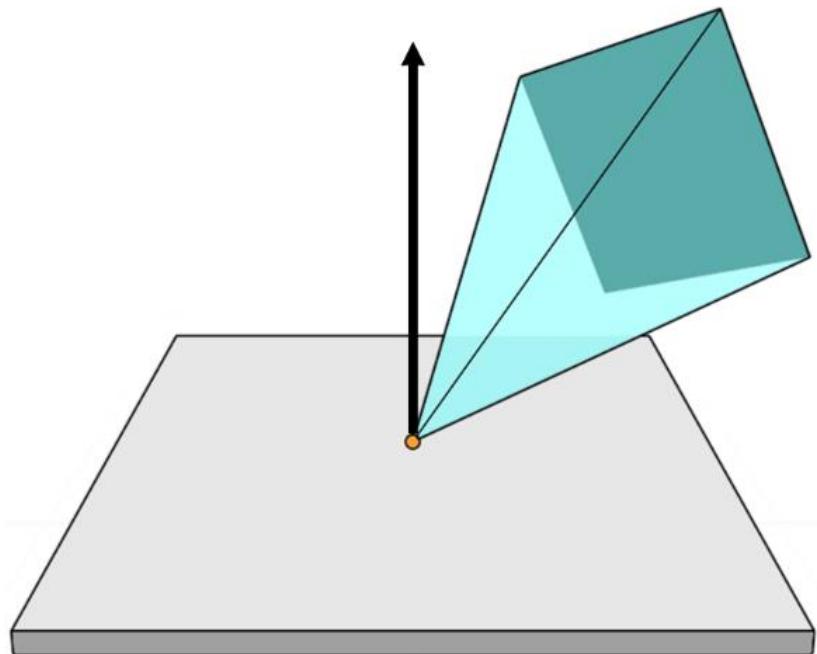
$$\sum f(x_i) \Delta x$$



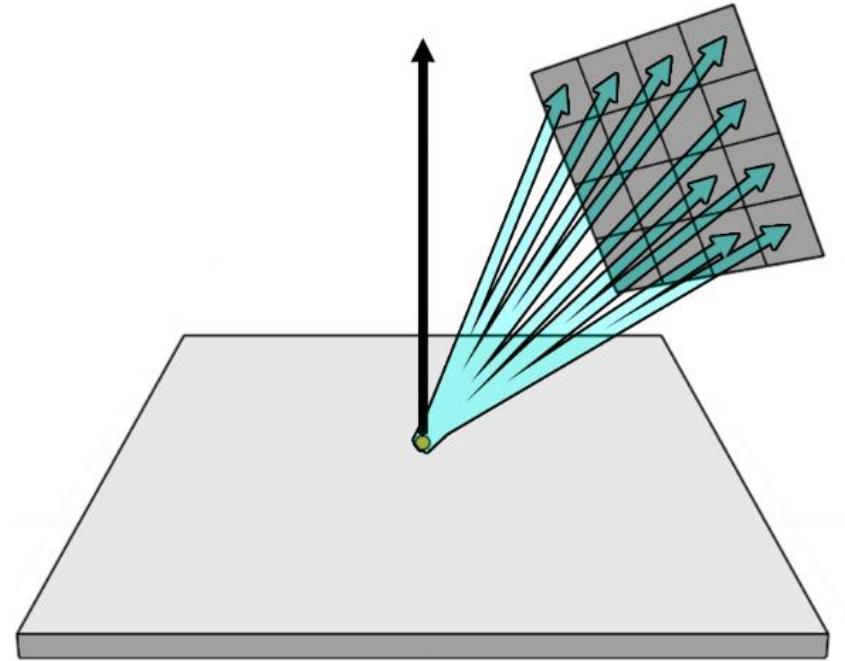
$$L_{e(x,\vec{\omega})} + \frac{\rho}{\pi} \int_{\Omega} L_i(x, \vec{\omega}') \cos \theta' d\omega'$$



$$L_{e(x,\vec{\omega})} + \frac{1}{|\Omega|} \frac{\rho}{\pi} \sum L_i(x, \vec{\omega}') \cos \theta'$$



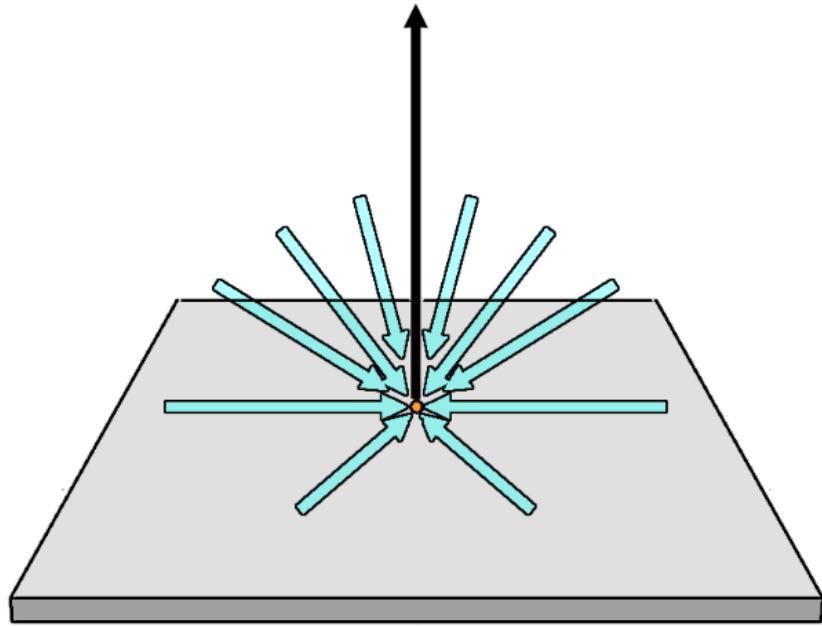
$$L_{e(x,\vec{\omega})} + \frac{\rho}{\pi} \int_S L_o(x', \vec{\omega}') V(x, x') \frac{\cos \theta \cos \theta'}{|x - x'|^2} d\omega'$$



$$L_{e(x,\vec{\omega})} + \frac{1}{|S|} \frac{\rho}{\pi} \sum L_o(x', \vec{\omega}') V(x, x') \frac{\cos \theta \cos \theta'}{|x - x'|^2}$$

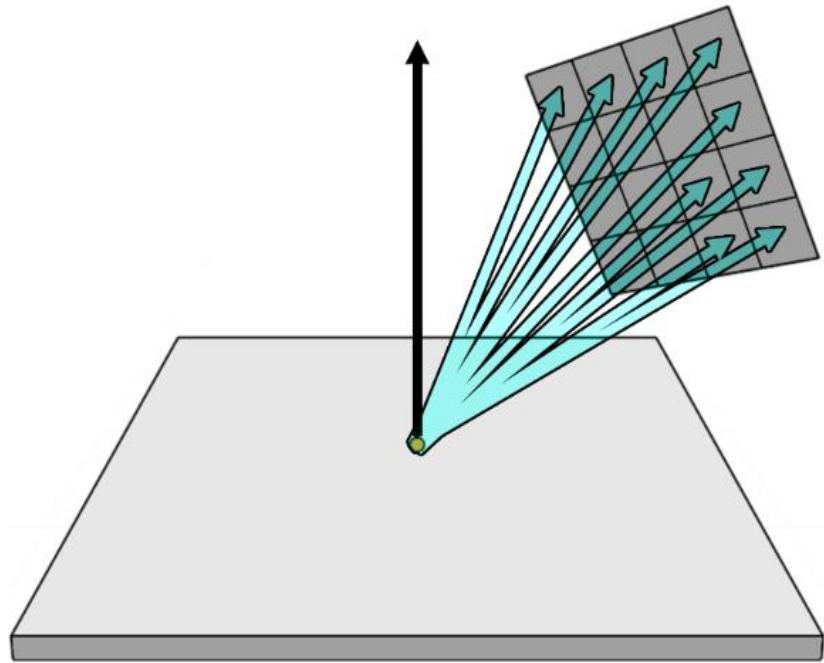
**Raytracing**

$$L_{e(x,\vec{\omega})} + \frac{1}{|\Omega|} \frac{\rho}{\pi} \sum L_i(x, \vec{\omega}') \cos \theta'$$



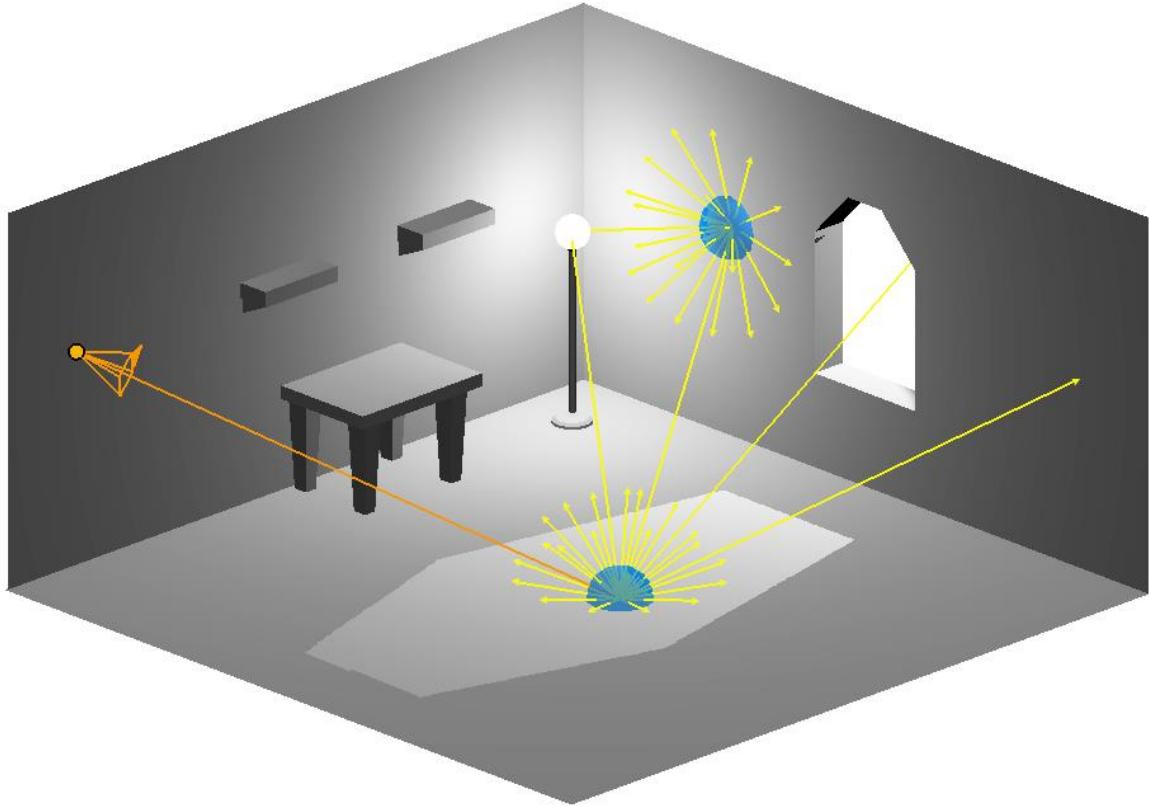
**Radiosity**

$$L_{e(x,\vec{\omega})} + \frac{1}{|S|} \frac{\rho}{\pi} \sum L_o(x', \vec{\omega}') V(x, x') \frac{\cos \theta \cos \theta'}{|x - x'|^2}$$



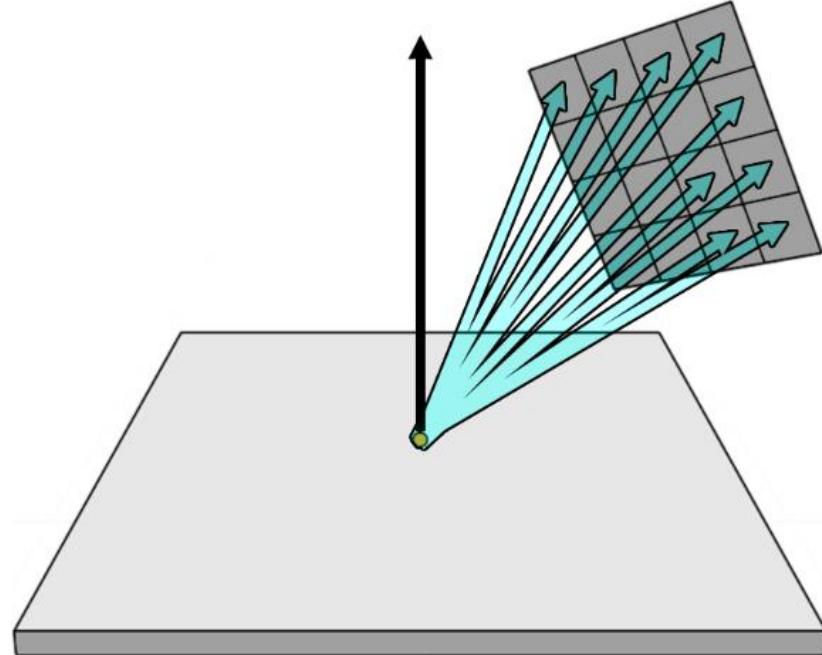
**Raytracing**

$$L_{e(x,\bar{\omega})} + \frac{1}{|\Omega|} \frac{\rho}{\pi} \sum L_i(x, \bar{\omega}') \cos \theta'$$



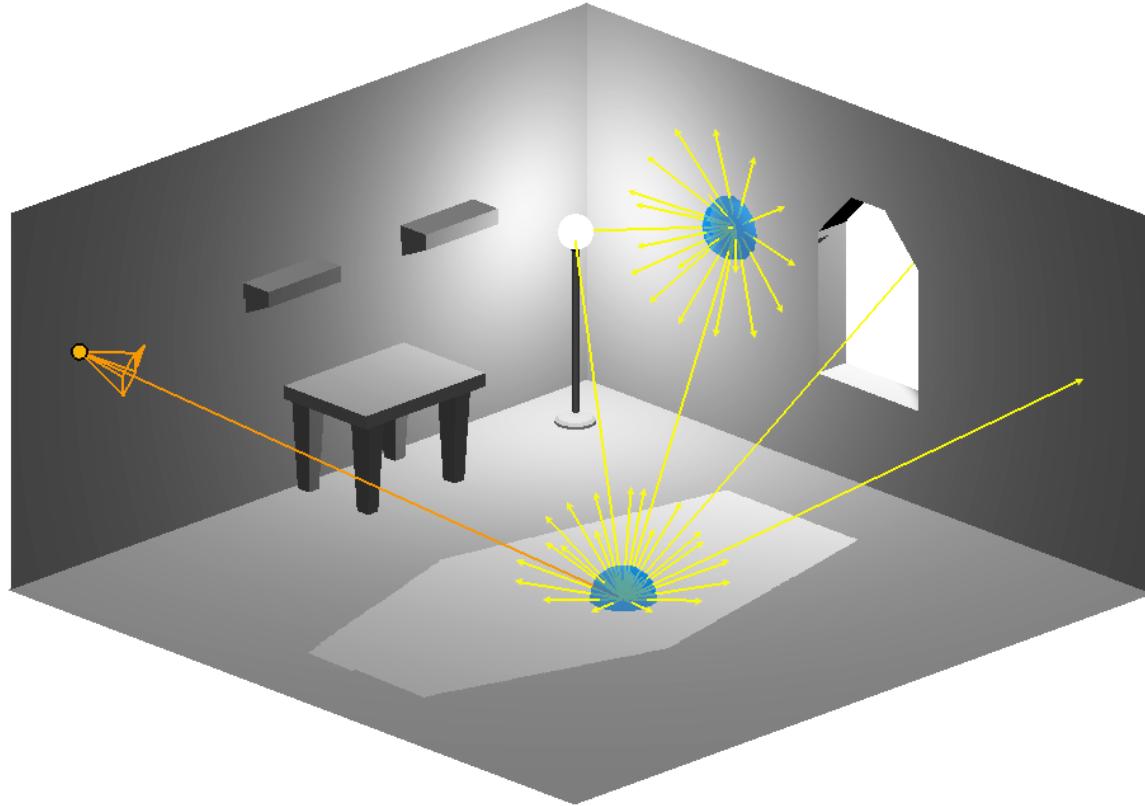
**Radiosity**

$$L_{e(x,\bar{\omega})} + \frac{1}{|S|} \frac{\rho}{\pi} \sum L_o(x', \bar{\omega}') V(x, x') \frac{\cos \theta \cos \theta'}{|x - x'|^2}$$



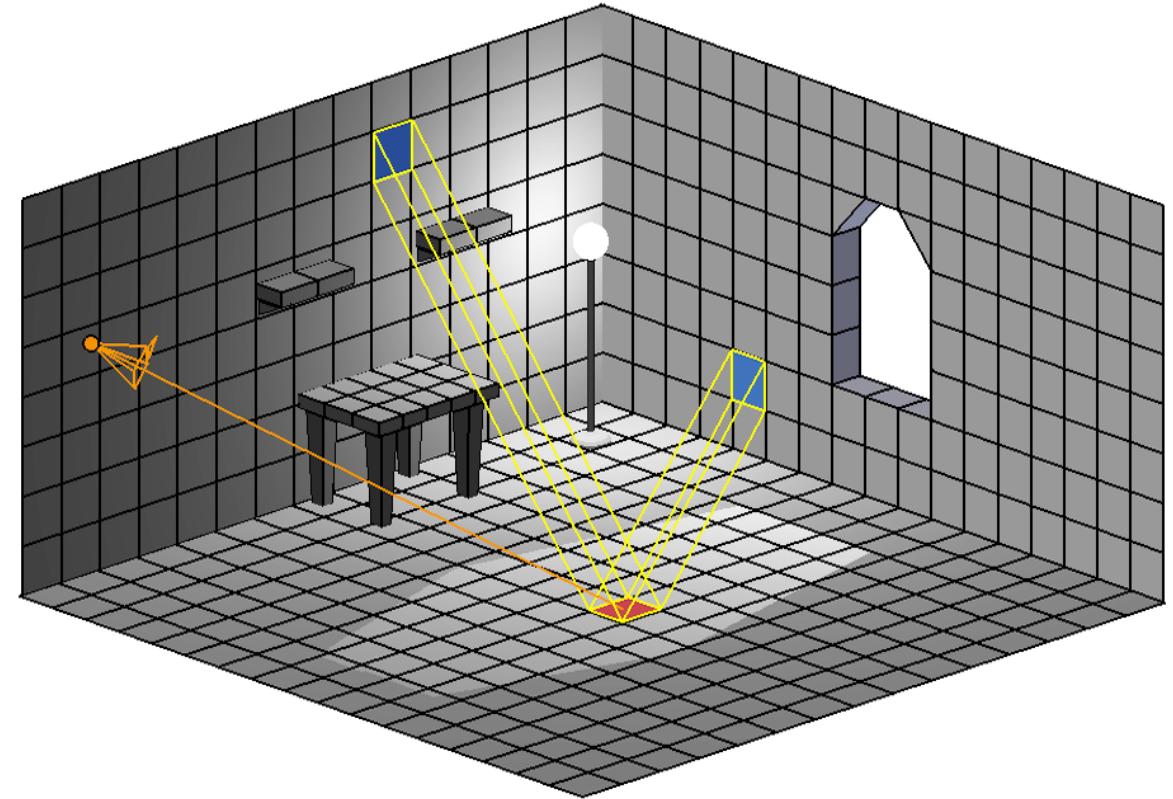
**Raytracing**

$$L_{e(x,\bar{\omega})} + \frac{1}{|\Omega|} \frac{\rho}{\pi} \sum L_i(x, \bar{\omega}') \cos \theta'$$



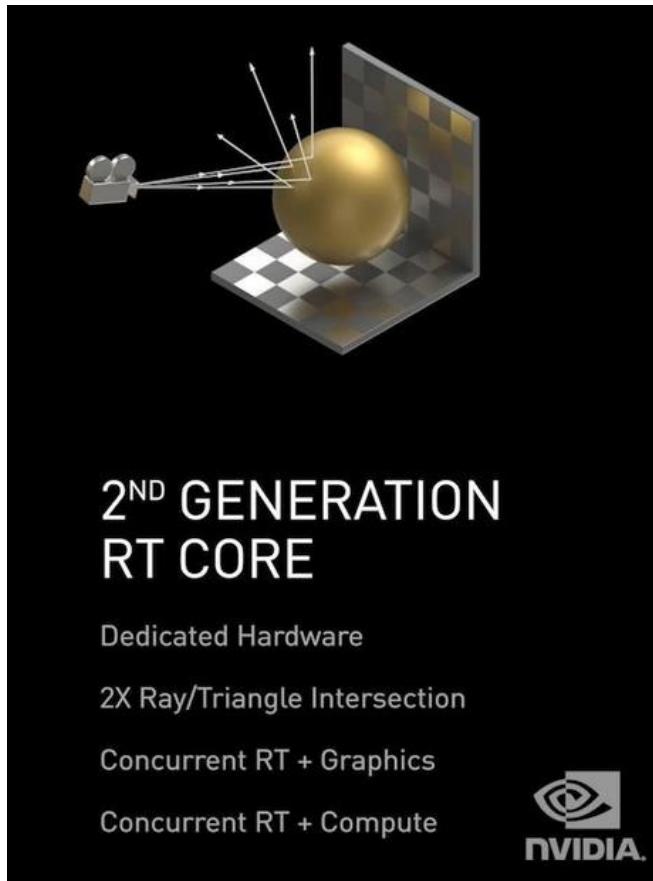
**Radiosity**

$$L_{e(x,\bar{\omega})} + \frac{1}{|S|} \frac{\rho}{\pi} \sum L_o(x', \bar{\omega}') V(x, x') \frac{\cos \theta \cos \theta'}{|x - x'|^2}$$



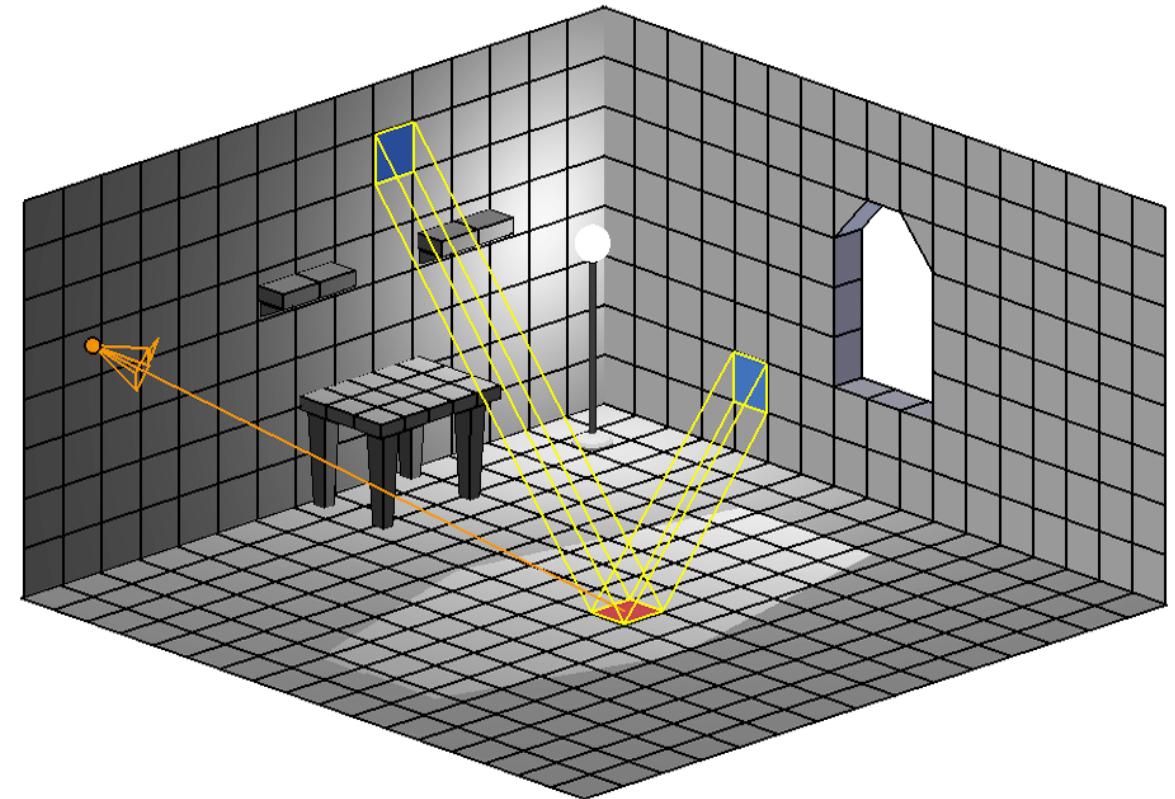
## Raytracing

$$L_{e(x,\vec{\omega})} + \frac{1}{|\Omega|} \frac{\rho}{\pi} \sum L_i(x, \vec{\omega}') \cos \theta'$$



## Radiosity

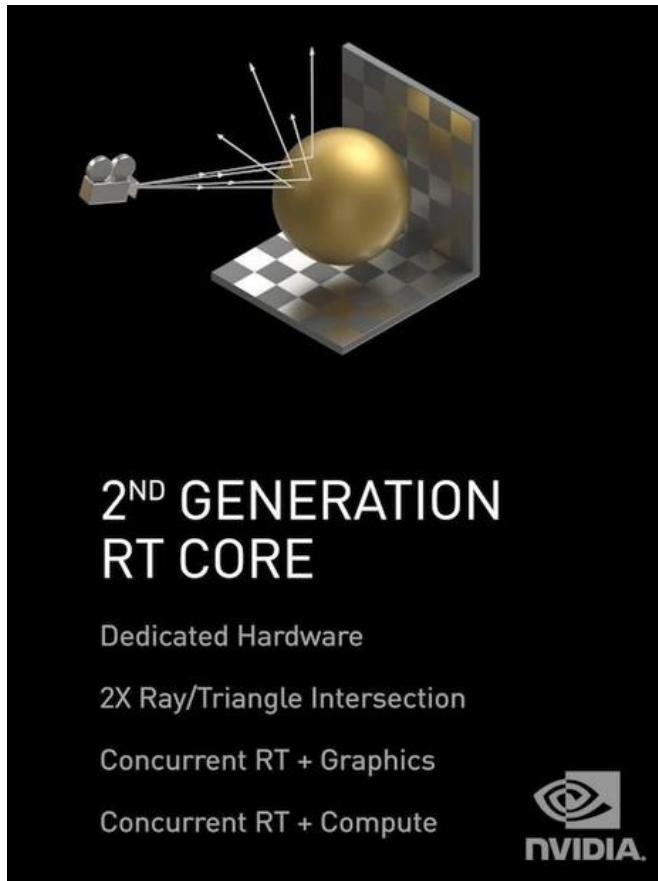
$$L_{e(x,\vec{\omega})} + \frac{1}{|S|} \frac{\rho}{\pi} \sum L_o(x', \vec{\omega}') V(x, x') \frac{\cos \theta \cos \theta'}{|x - x'|^2}$$



From: GeForce RTX 30 Series Launch Event

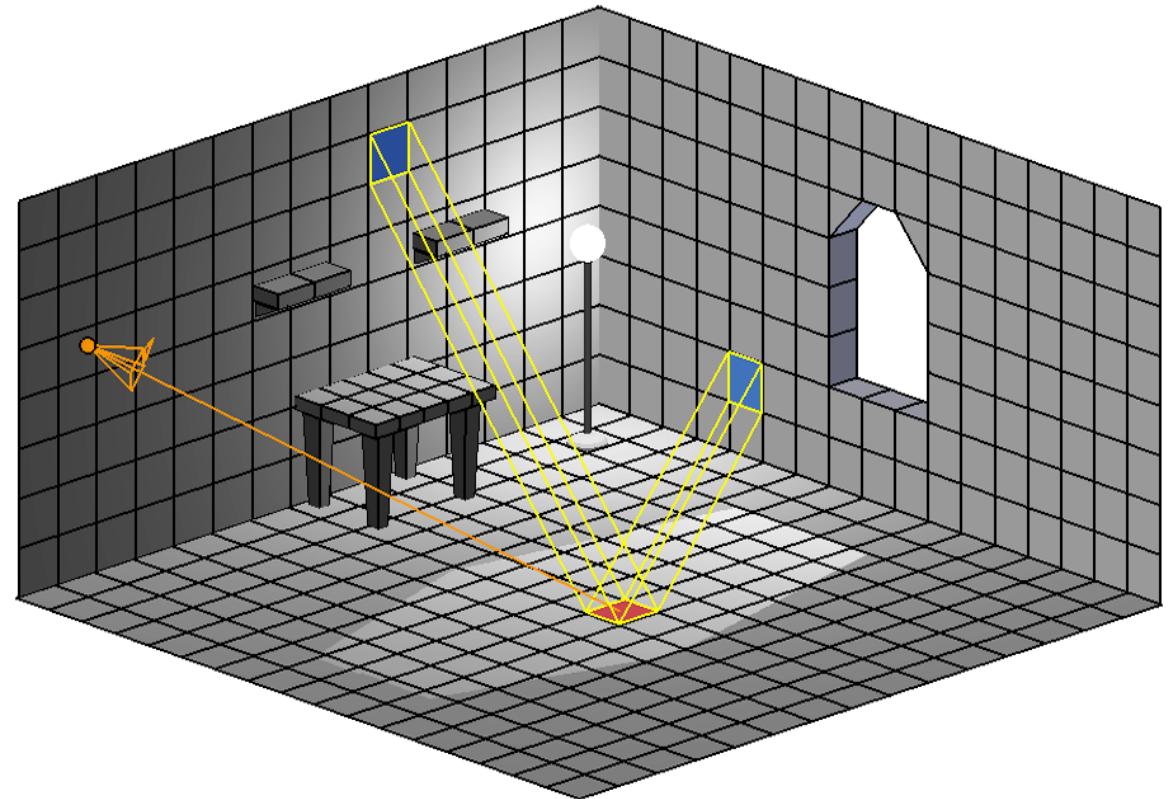
## Raytracing

$$L_{e(x,\vec{\omega})} + \frac{1}{|\Omega|} \frac{\rho}{\pi} \sum L_i(x, \vec{\omega}') \cos \theta'$$



## Radiosity

$$L_{e(x,\vec{\omega})} + \frac{1}{|S|} \frac{\rho}{\pi} \sum L_o(x', \vec{\omega}') \boxed{V(x, x')} \frac{\cos \theta \cos \theta'}{|x - x'|^2}$$



From: GeForce RTX 30 Series Launch Event

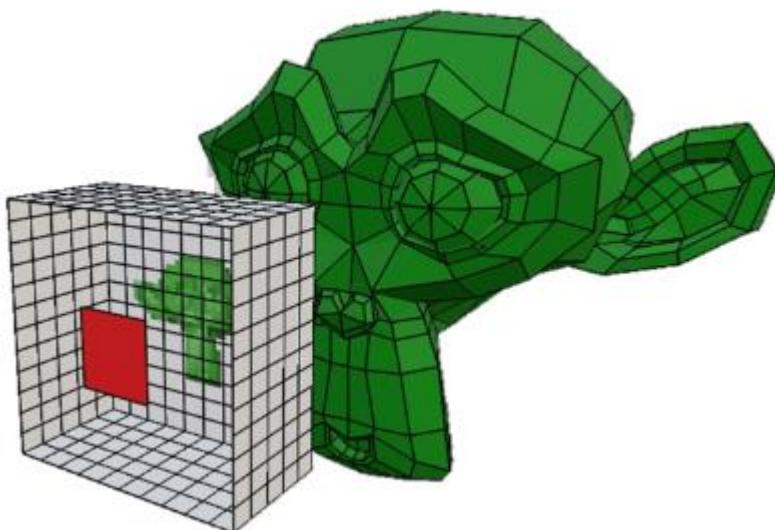
## Raytracing

$$L_{e(x,\vec{\omega})} + \frac{1}{|\Omega|} \frac{\rho}{\pi} \sum L_i(x, \vec{\omega}') \cos \theta'$$

## Radiosity

$$L_{e(x,\vec{\omega})} + \frac{1}{|S|} \frac{\rho}{\pi} \sum L_o(x', \vec{\omega}') V(x, x') \frac{\cos \theta \cos \theta'}{|x - x'|^2}$$

Z-Buffering



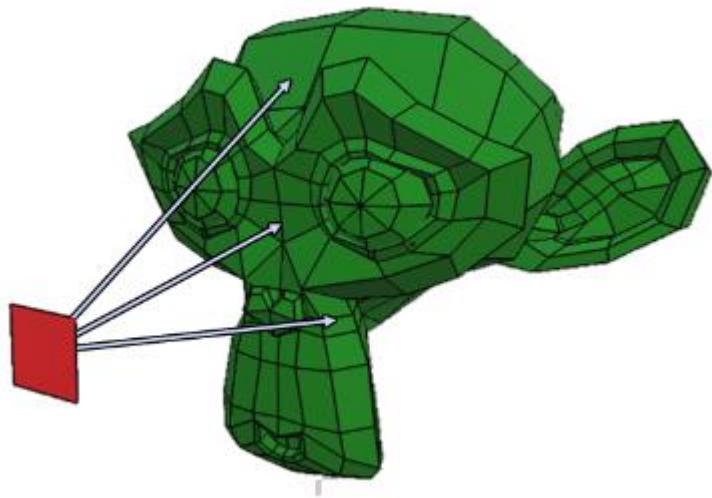
## Raytracing

$$L_{e(x,\vec{\omega})} + \frac{1}{|\Omega|} \frac{\rho}{\pi} \sum L_i(x, \vec{\omega}') \cos \theta'$$

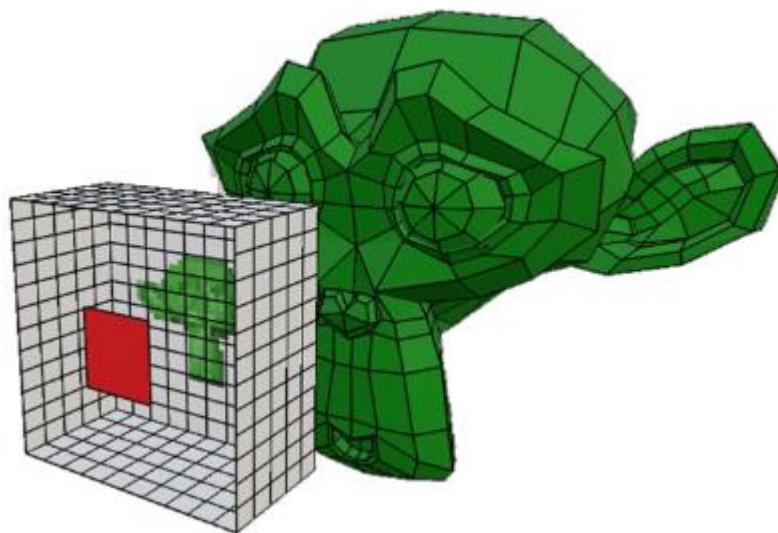
## Radiosity

$$L_{e(x,\vec{\omega})} + \frac{1}{|S|} \frac{\rho}{\pi} \sum L_o(x', \vec{\omega}') V(x, x') \frac{\cos \theta \cos \theta'}{|x - x'|^2}$$

RTX

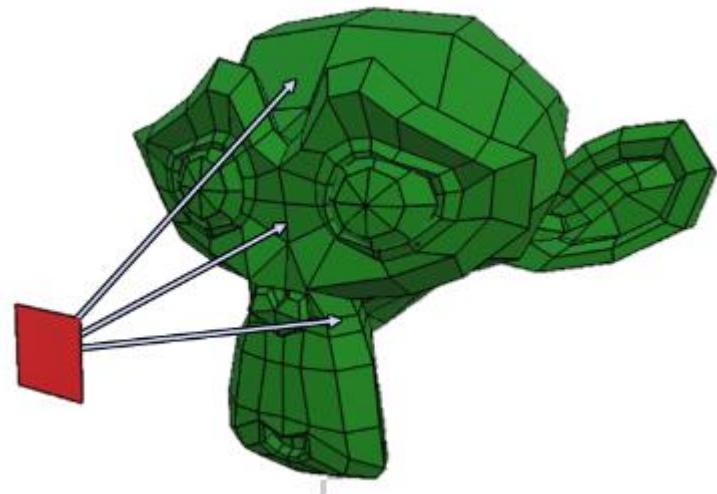


Z-Buffering



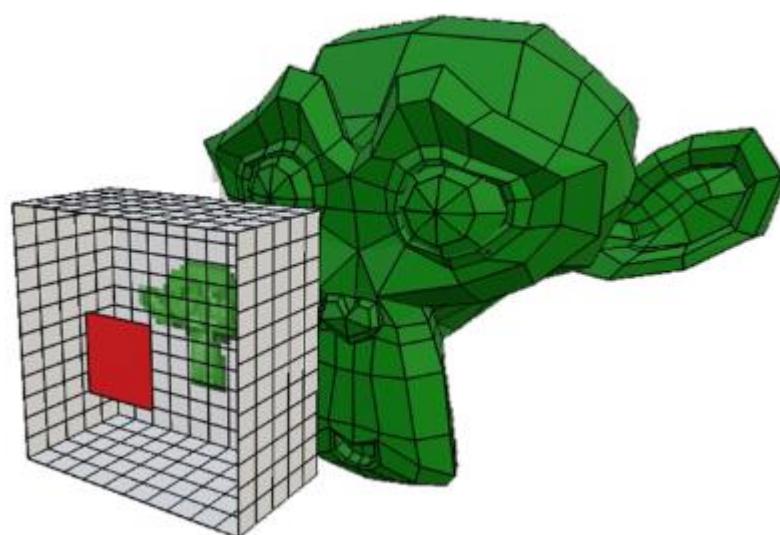
## Raytracing

$$L_{e(x,\vec{\omega})} + \frac{1}{|\Omega|} \frac{\rho}{\pi} \sum L_i(x, \vec{\omega}') \cos \theta'$$

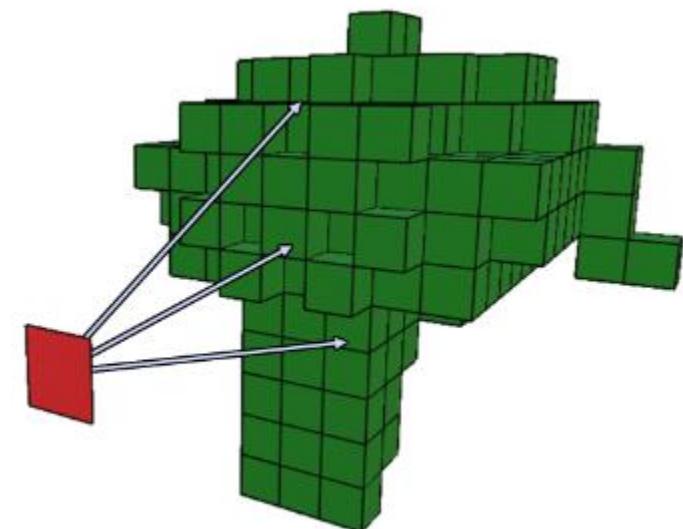


## Radiosity

$$L_{e(x,\vec{\omega})} + \frac{1}{|S|} \frac{\rho}{\pi} \sum L_o(x', \vec{\omega}') V(x, x') \frac{\cos \theta \cos \theta'}{|x - x'|^2}$$



Voxel-Raymarching



RTX

Z-Buffering

## **RTX Radiosity?**

Goals:

- Determine if RTX can be used to accelerate Radiosity.

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Goals:

- Determine if RTX can be used to accelerate Radiosity.
- Demonstrate this through a competitively fast implementation.

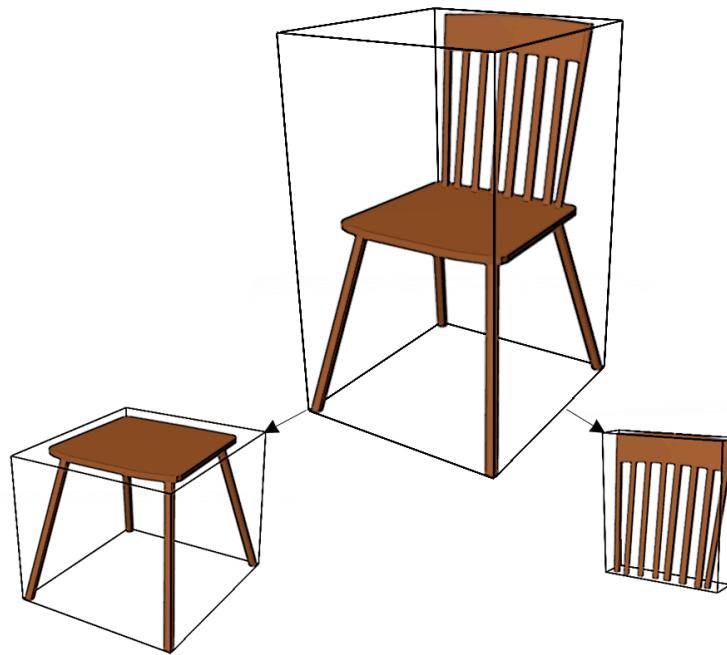
## **RTX Radiosity?**

### **Goals:**

- Determine if RTX can be used to accelerate Radiosity.
- Demonstrate this through a competitively fast implementation.
- Find the best practices for RTX radiosity.

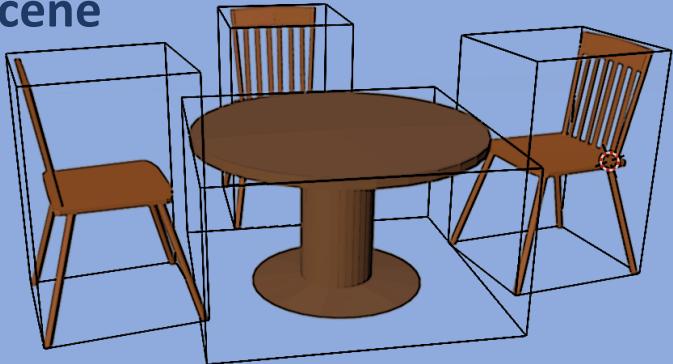
## Bounding Volume Hierarchies



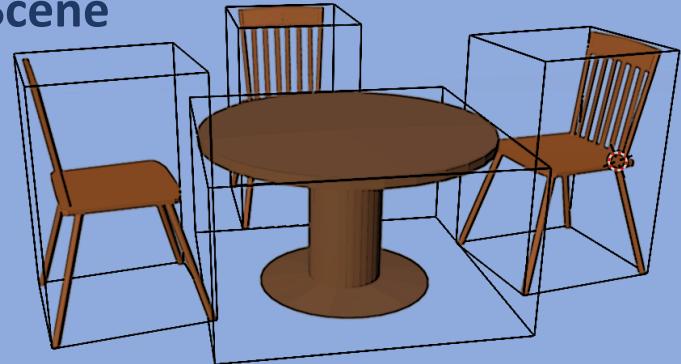




## Scene



**Scene**



**TLAS**

**Chair 1**

$$M_1 = [...]$$

**Chair 2**

$$M_2 = [...]$$

**Chair 3**

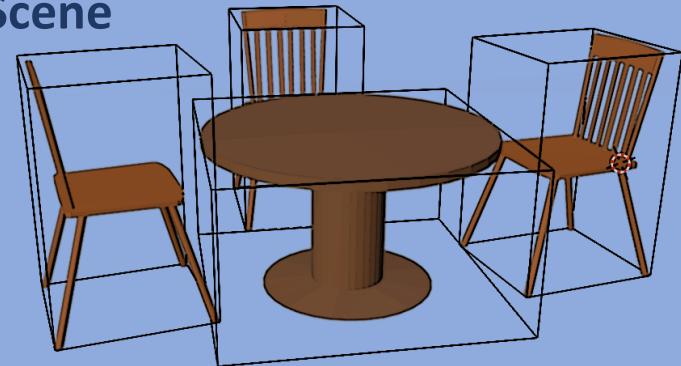
$$M_3 = [...]$$

**Table 1**

$$M_4 = [...]$$



**Scene**



**TLAS**

**Chair 1**

$$M_1 = [...]$$

**Chair 2**

$$M_2 = [...]$$

**Chair 3**

$$M_3 = [...]$$

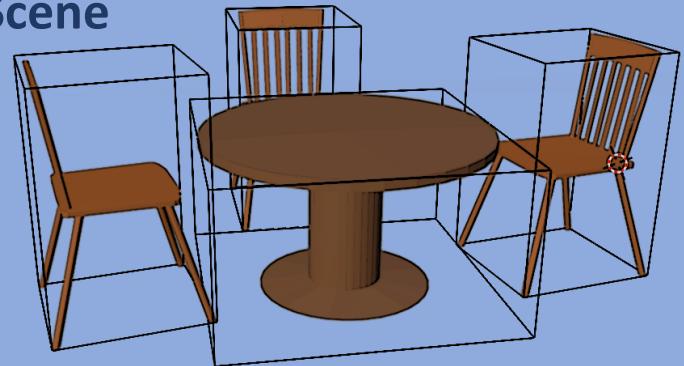
**Table 1**

$$M_4 = [...]$$

**BLAS 1**



**Scene**



**TLAS**

**Chair 1**

$$M_1 = [...]$$

**Chair 2**

$$M_2 = [...]$$

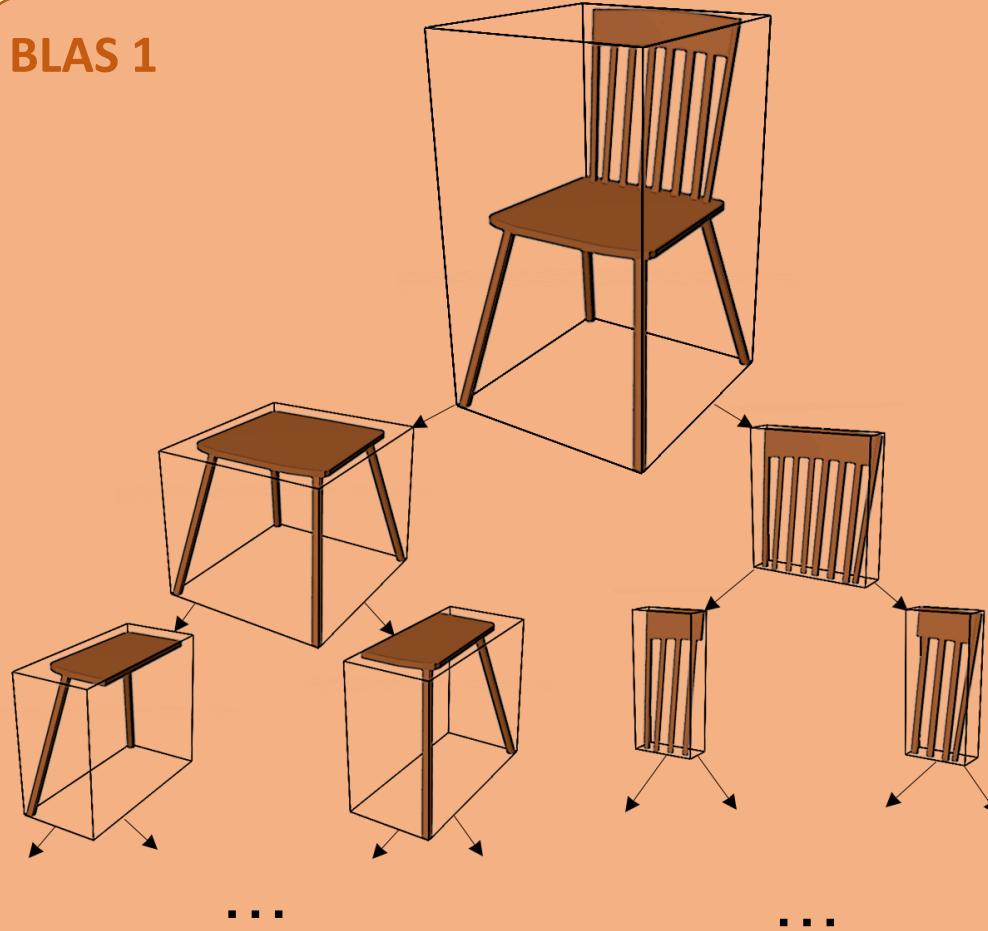
**Chair 3**

$$M_3 = [...]$$

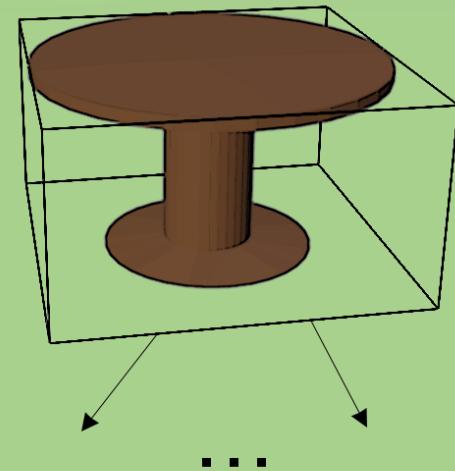
**Table 1**

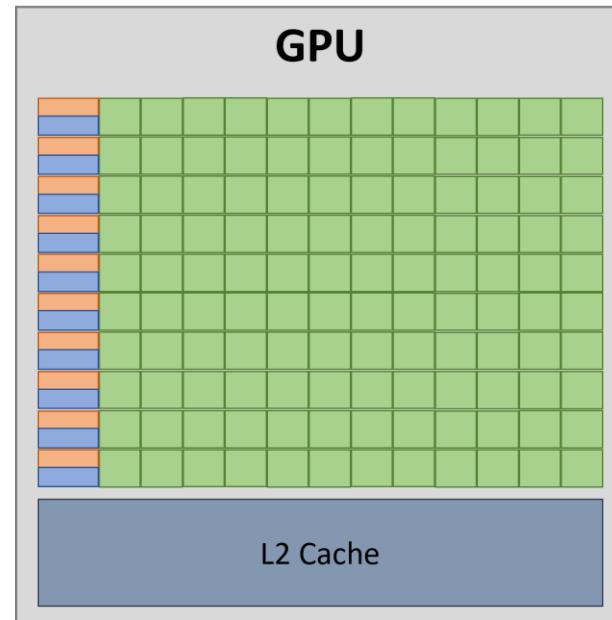
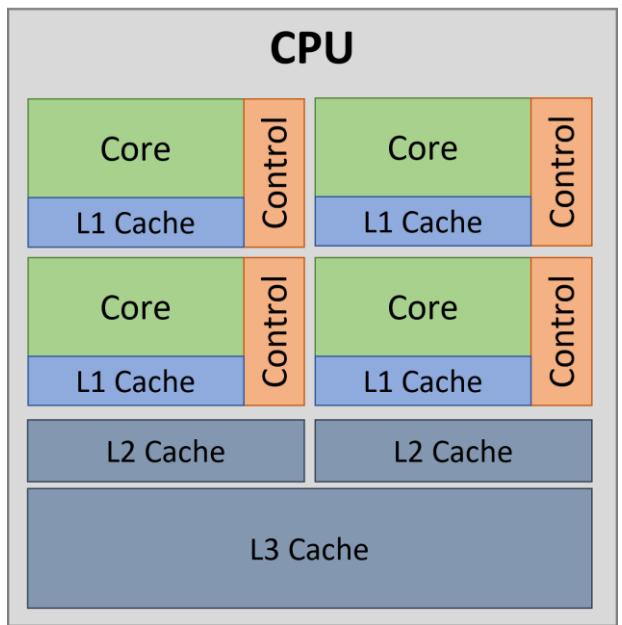
$$M_4 = [...]$$

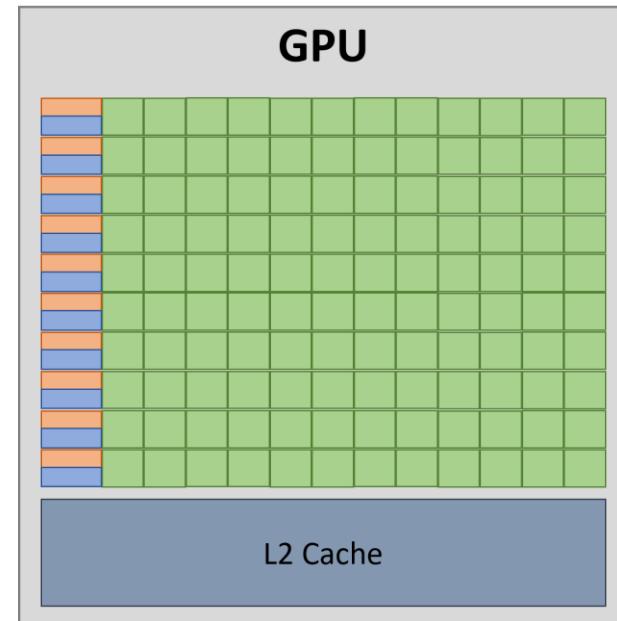
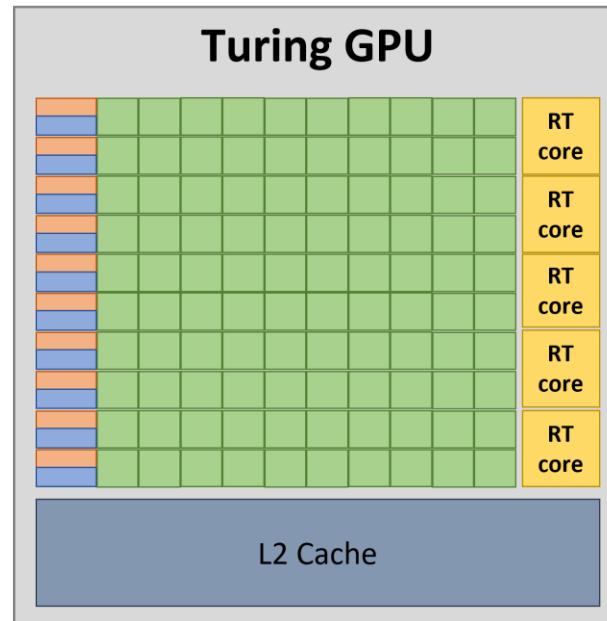
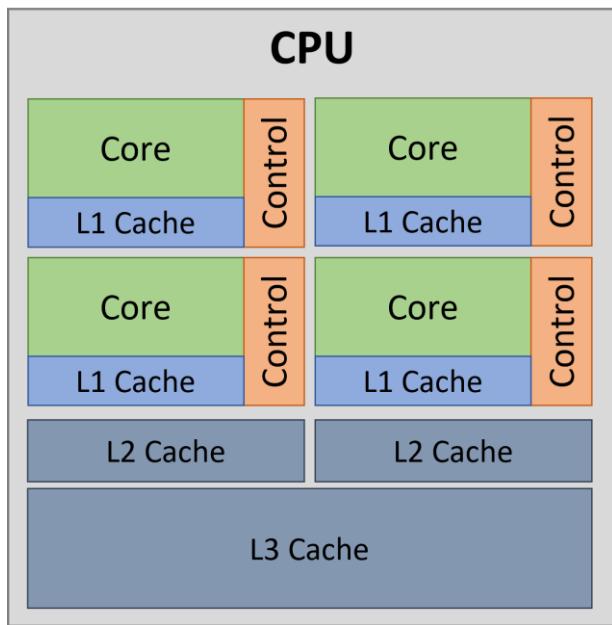
**BLAS 1**



**BLAS 2**



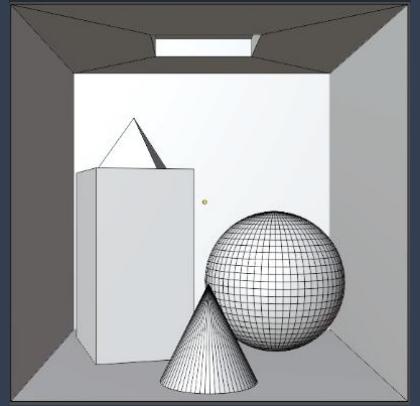




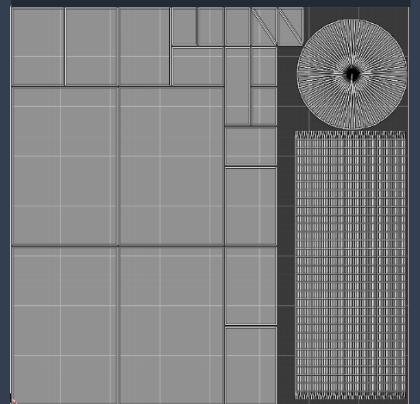
**RTRad**

## Input

### Geometry



### UV Coordinates



### Materials

Material1 (color,  $L_e$ ) ...

Material2 (color,  $L_e$ ) ...

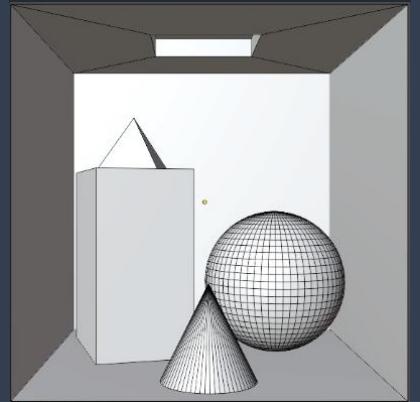
...



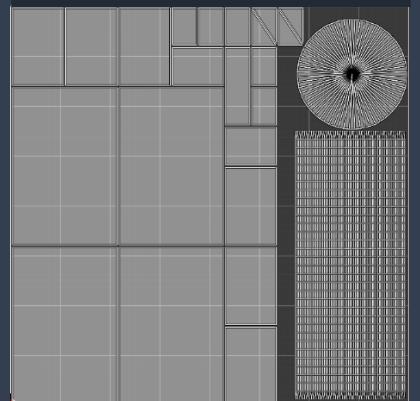
RTRad

## Input

### Geometry



### UV Coordinates



### Materials

Material1 (color,  $L_e$ ) ...

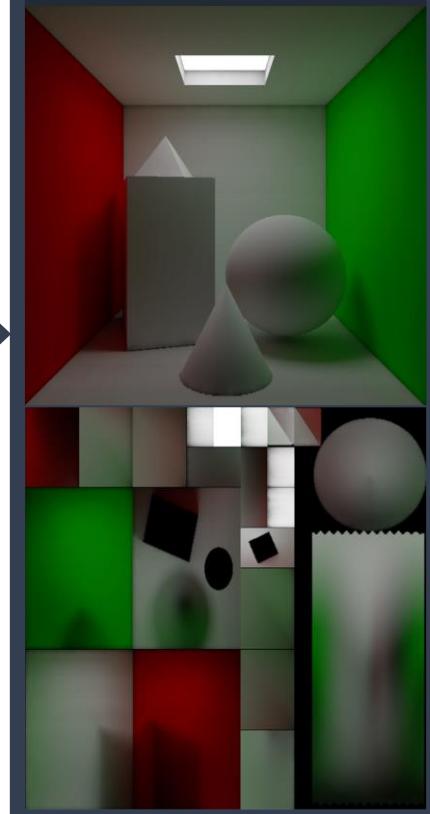
Material2 (color,  $L_e$ ) ...

...

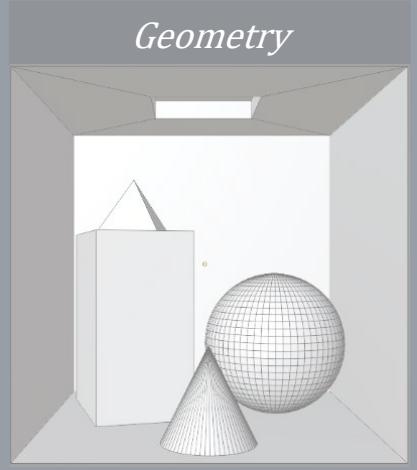
RTRad

## Output

### Lightmap



## Input



## RTRad

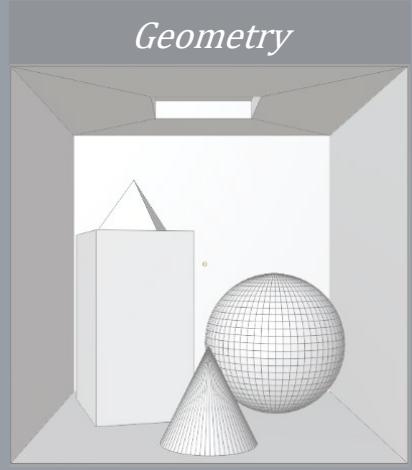
$\text{For } i \in S$

RTLPass

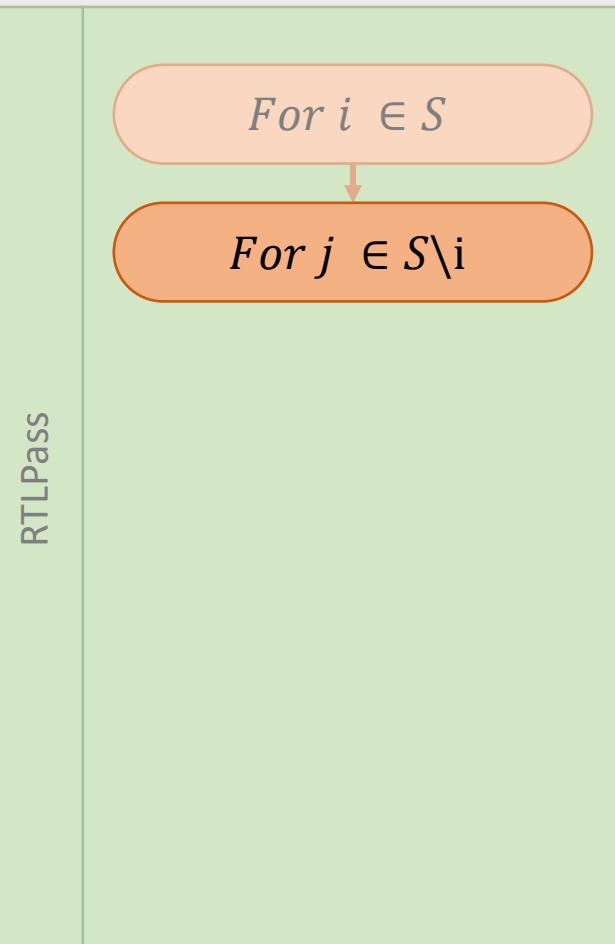
## Output

Lightmap

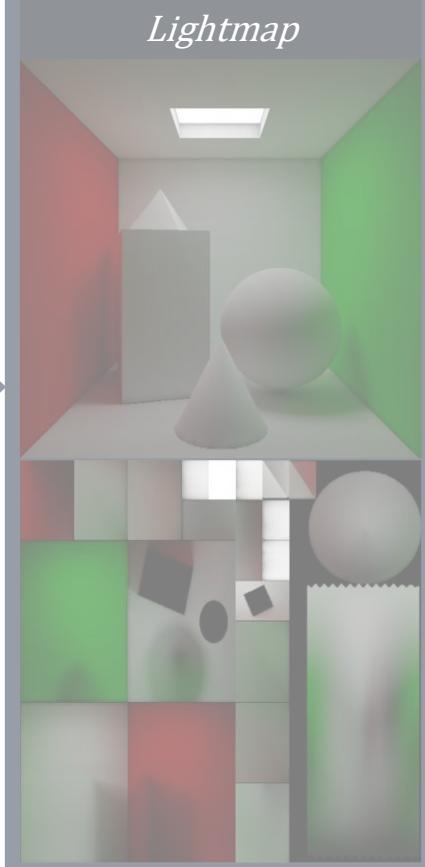
## Input



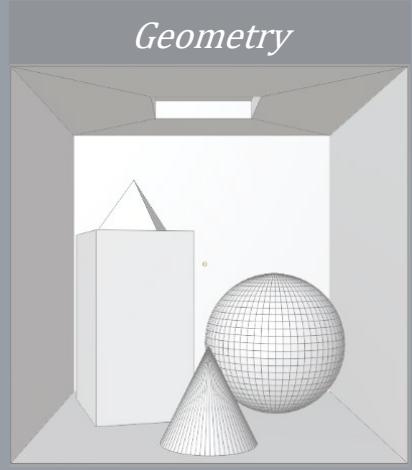
## RTRad



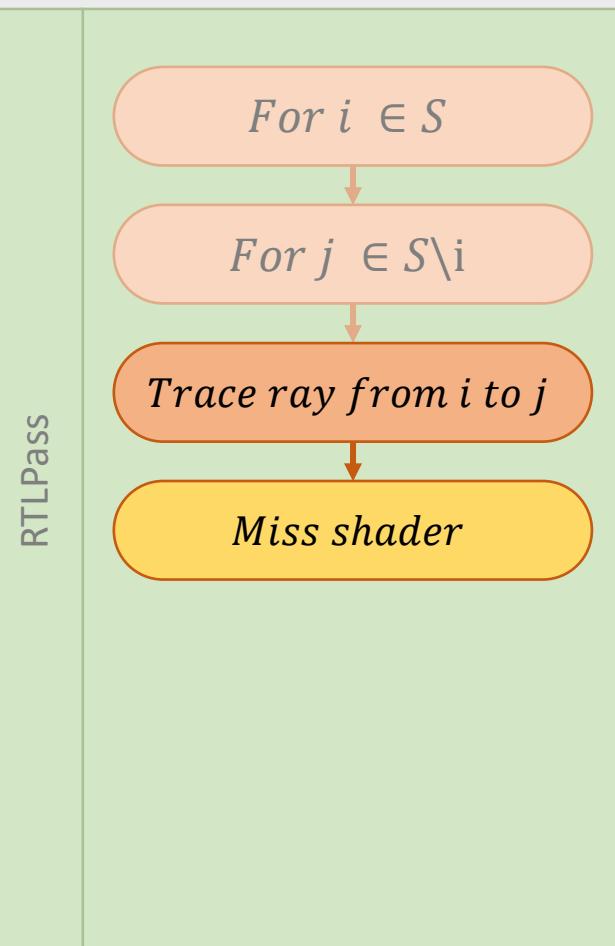
## Output



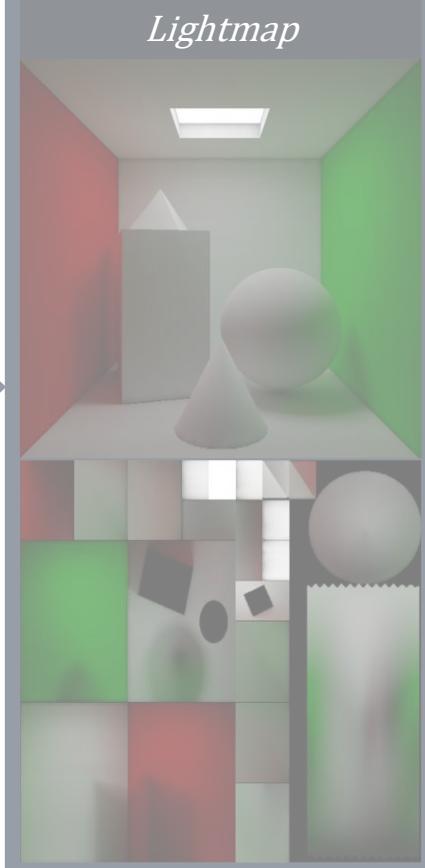
## Input



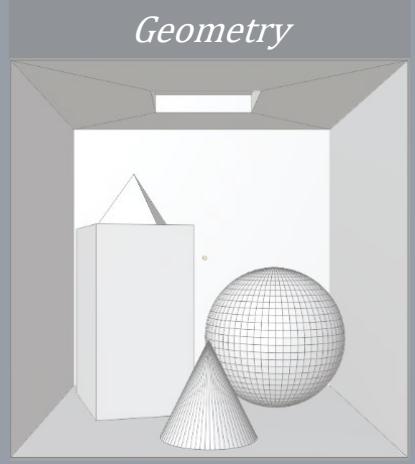
## RTRad



## Output



## Input



## Materials

Material1 (color,  $L_e$ ) ...

Material2 (color,  $L_e$ ) ...

...

## RTRad

### RTLPass

For  $i \in S$

For  $j \in S \setminus i$

Trace ray from  $i$  to  $j$

Miss shader

$$F_{ij} = A_j \frac{\cos \theta_i \cos \theta_j}{\|x_i - x_j\|^2}$$

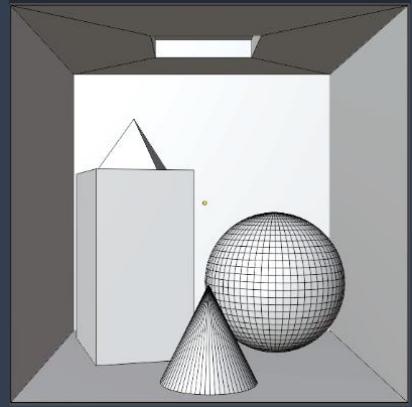
$$L_{out}(i) += F_{ij} \frac{\rho}{\pi} * \text{color}(i) * L_{in}(j)$$

## Output

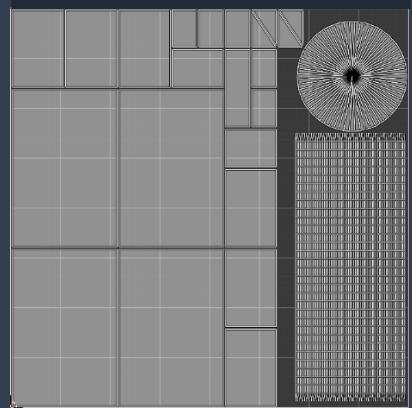
### Lightmap

## Input

### Geometry



### UV Coordinates



### Materials

Material1 (color,  $L_e$ ) ...

Material2 (color,  $L_e$ ) ...

...

## RTRad

### RTLPass

For  $i \in S$

For  $j \in S \setminus i$

Trace ray from  $i$  to  $j$

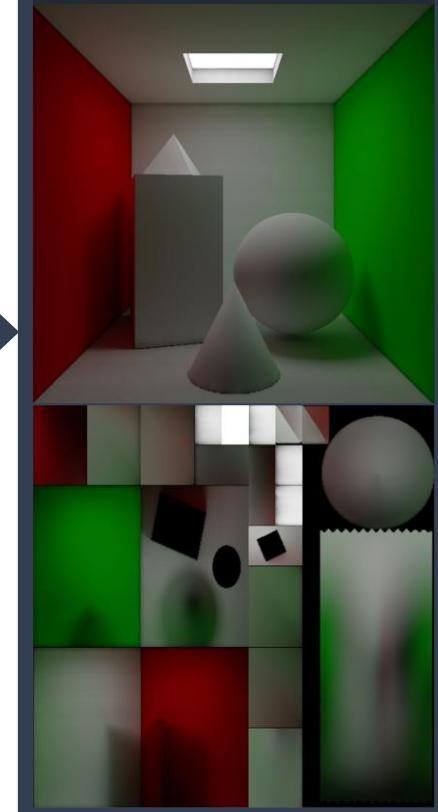
Miss shader

$$F_{ij} = A_j \frac{\cos \theta_i \cos \theta_j}{\|x_i - x_j\|^2}$$

$$L_{out}(i) += F_{ij} \frac{\rho}{\pi} * \text{color}(i) * L_{in}(j)$$

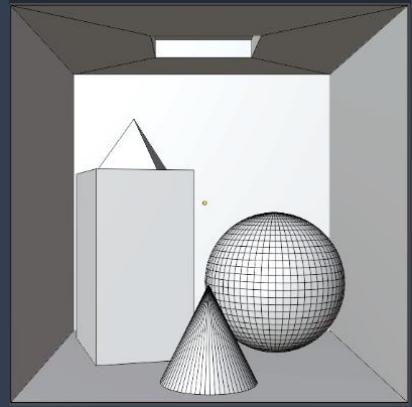
## Output

### Lightmap

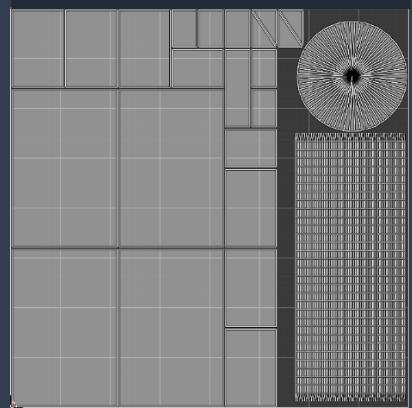


## Input

### Geometry



### UV Coordinates



### Materials

Material1 (color,  $L_e$ ) ...

Material2 (color,  $L_e$ ) ...

...

## RTRad

### RTLPass

For  $i \in S$

For  $j \in S \setminus i$

Trace ray from  $i$  to  $j$

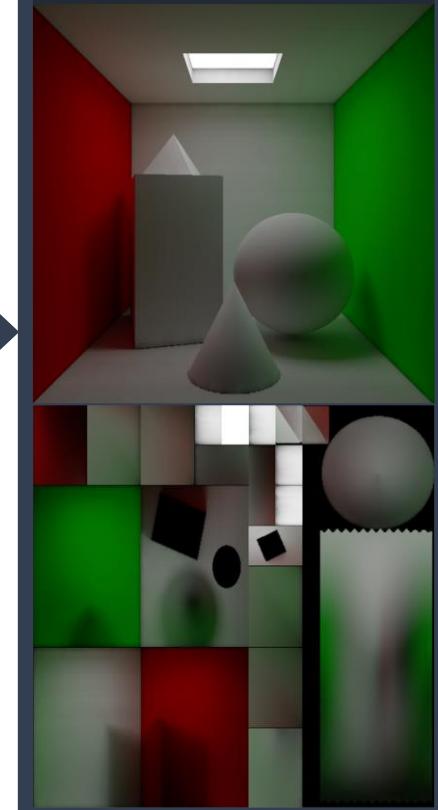
Miss shader

$$F_{ij} = A_i \frac{\cos \theta_i \cos \theta_j}{\|x_i - x_j\|^2}$$

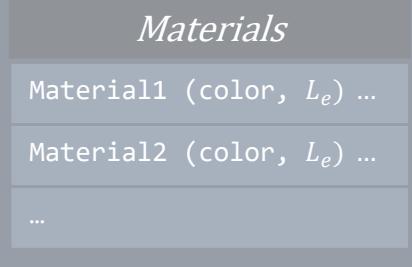
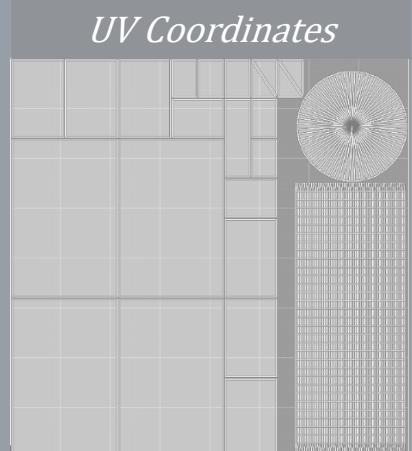
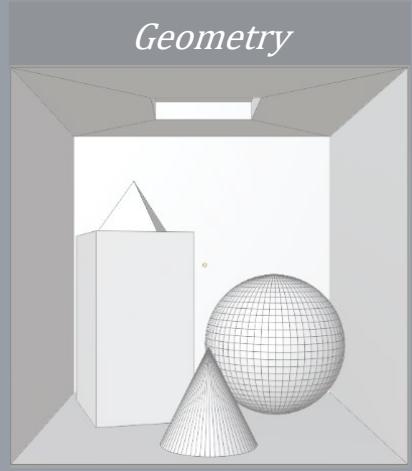
$$\underline{L}_{out}(i) += \frac{\rho}{F_{ij}} * \underline{color}(i) * \underline{L}_{in}(j)$$

## Output

### Lightmap



## Input



## RTRad

### RTLPass

For  $i \in S$

For  $j \in S \setminus i$

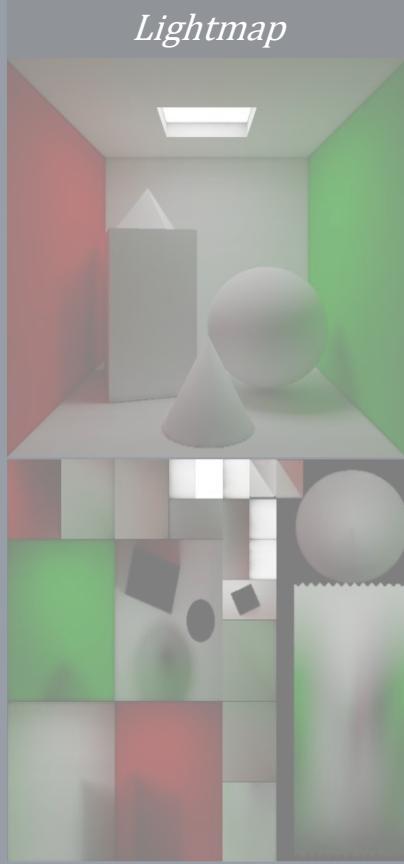
Trace ray from  $i$  to  $j$

Miss shader

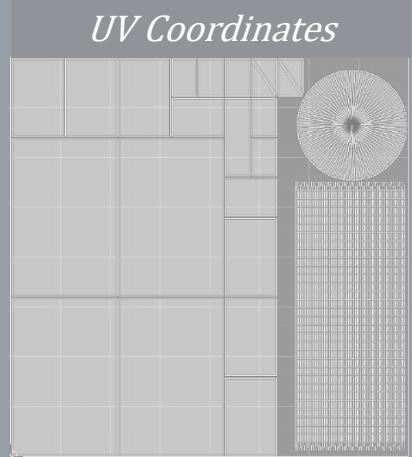
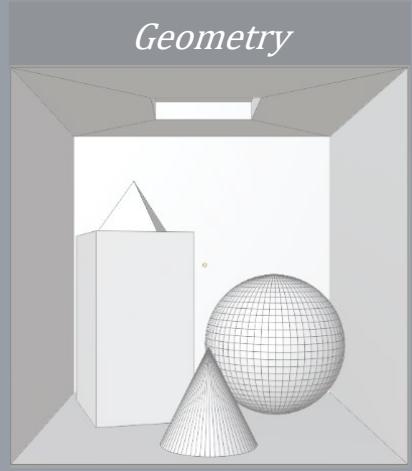
$$F_{ij} = A_j \frac{\cos \theta_i \cos \theta_j}{\|x_i - x_j\|^2}$$

$$\underline{L}_{out}(i) += F_{ij} \frac{\rho}{\pi} * color(i) * \underline{L}_{in}(j)$$

## Output



## Input

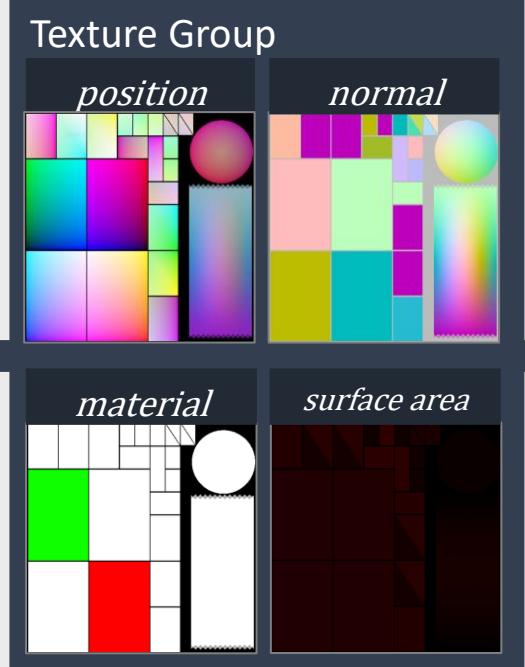


Materials

Material1 (color,  $L_e$ ) ...

Material2 (color,  $L_e$ ) ...

...



CITPass

## RTRad

### RTLPass

For  $i \in S$

For  $j \in S \setminus i$

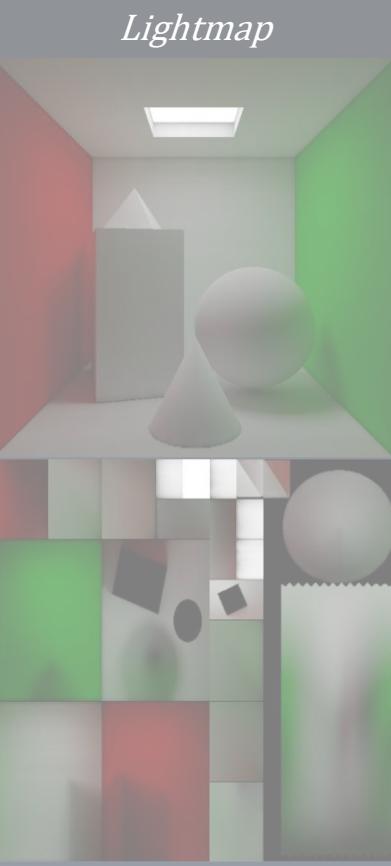
Trace ray from  $i$  to  $j$

Miss shader

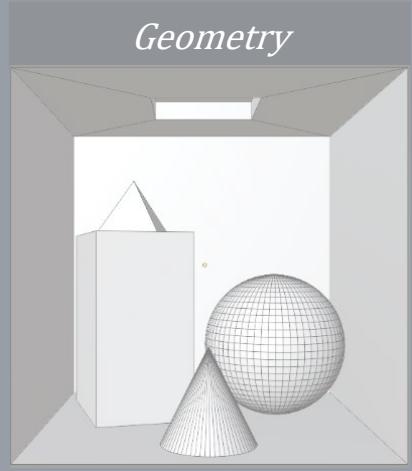
$$F_{ij} = A_j \frac{\cos \theta_i \cos \theta_j}{\|x_i - x_j\|^2}$$

$$L_{out}(i) += F_{ij} \frac{\rho}{\pi} * color(i) * L_{in}(j)$$

## Output



## Input



Geometry

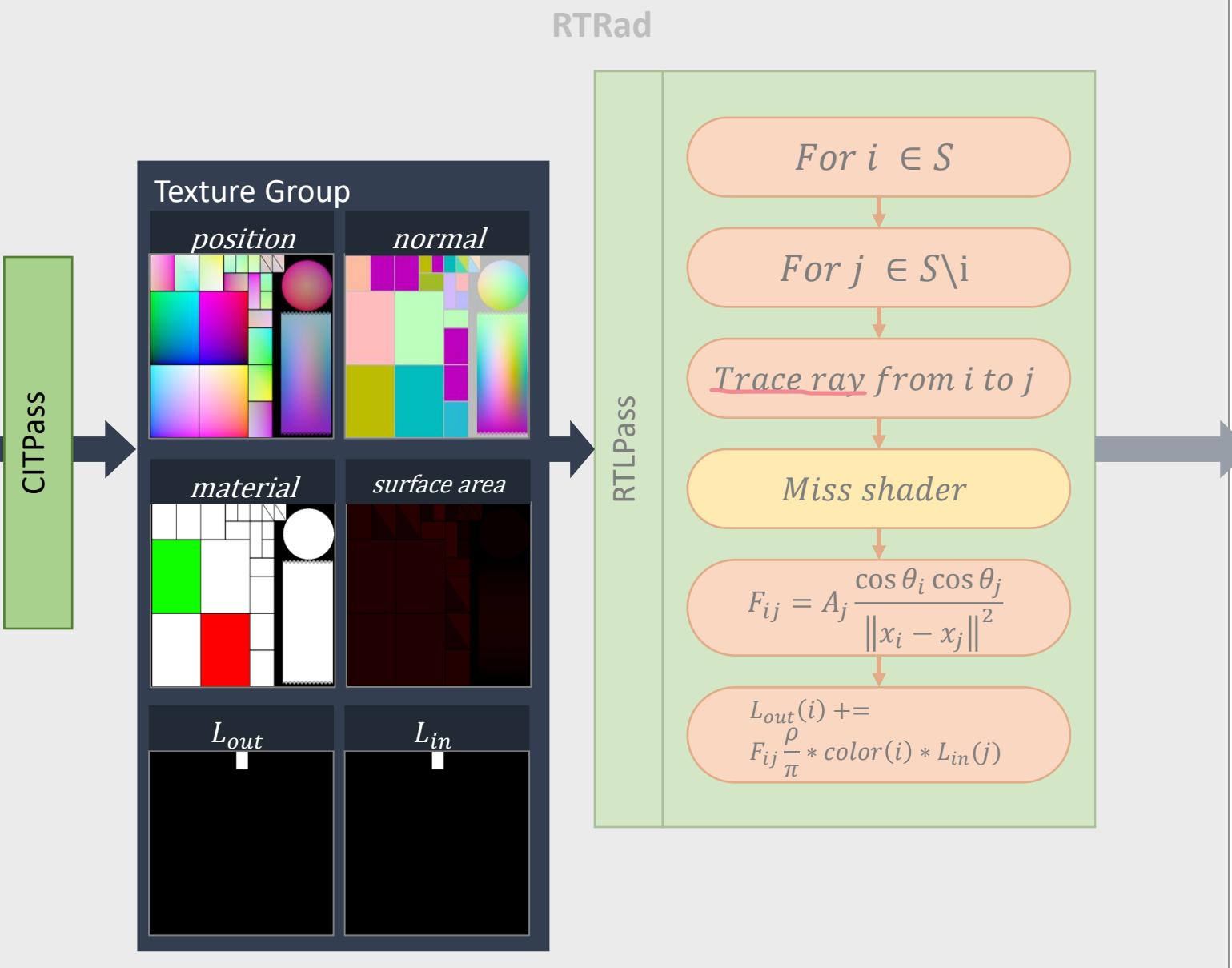
UV Coordinates

Materials

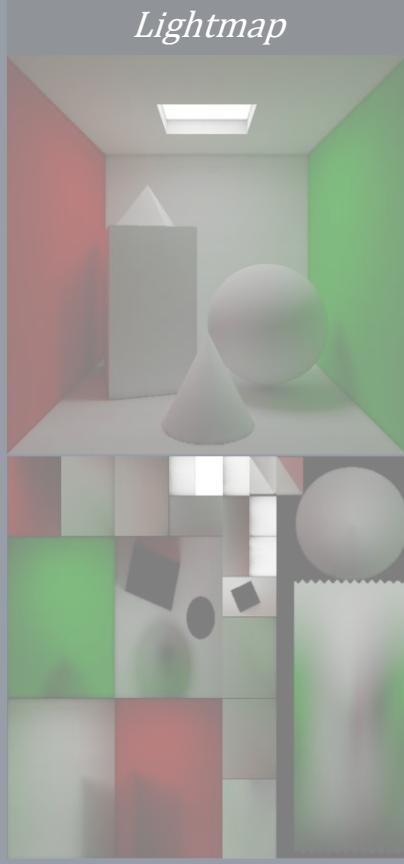
Material1 (color,  $L_e$ ) ...

Material2 (color,  $L_e$ ) ...

...

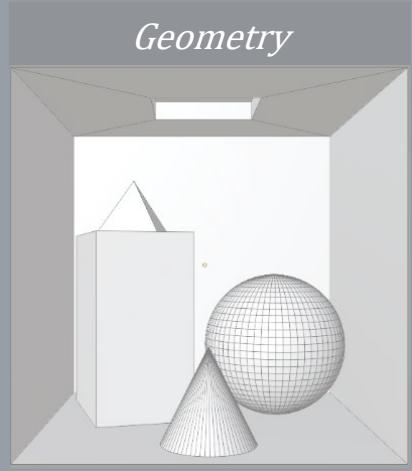


## Output



Lightmap

## Input



Geometry

UV Coordinates

Materials

Material1 (color,  $L_e$ ) ...

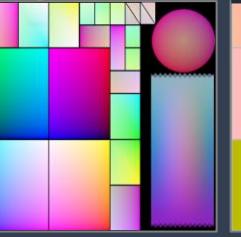
Material2 (color,  $L_e$ ) ...

...

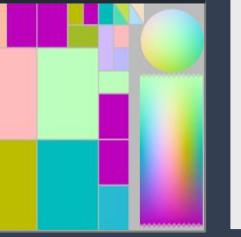
## RTRad

### Texture Group

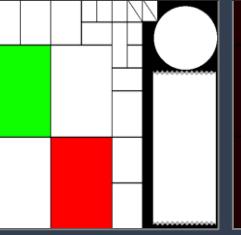
*position*



*normal*



*material*



*surface area*



$L_{out}$



$L_{in}$



CITPass

RTLPass

For  $i \in S$

For  $j \in S \setminus i$

Trace ray from  $i$  to  $j$

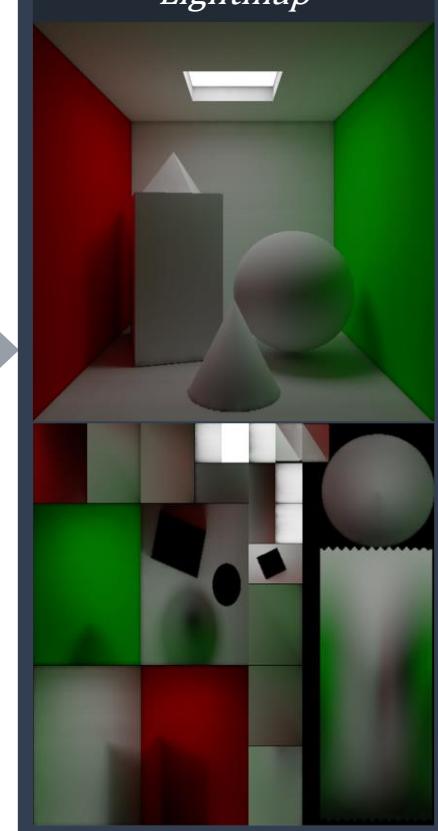
Miss shader

$$F_{ij} = A_j \frac{\cos \theta_i \cos \theta_j}{\|x_i - x_j\|^2}$$

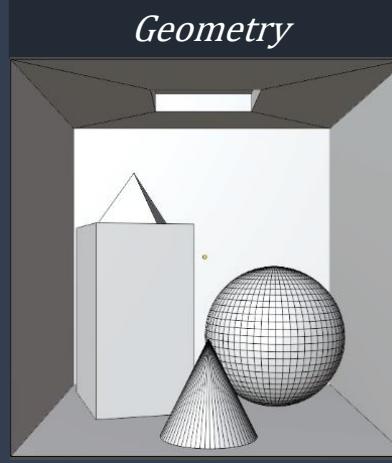
$$L_{out}(i) += F_{ij} \frac{\rho}{\pi} * color(i) * L_{in}(j)$$

## Output

Lightmap



## Input



## Materials

Material1 (color,  $L_e$ ) ...

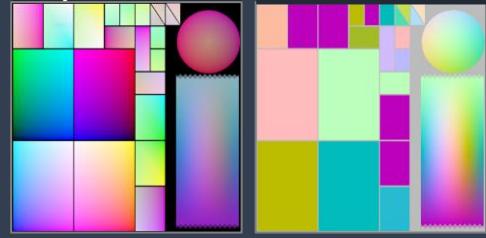
Material2 (color,  $L_e$ ) ...

...

## RTRad

### Texture Group

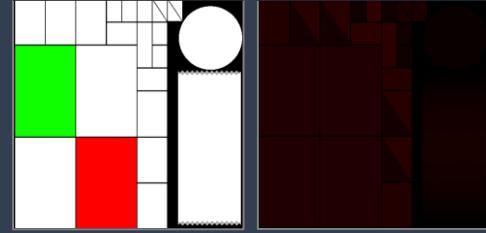
position



normal



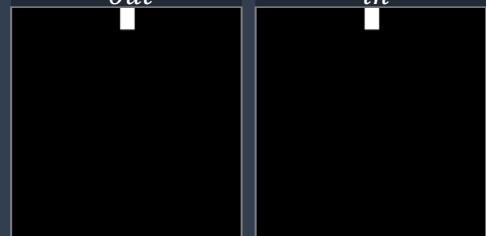
material



surface area



$L_{out}$



$L_{in}$

### RTLPass

For  $i \in S$

For  $j \in S \setminus i$

Trace ray from  $i$  to  $j$

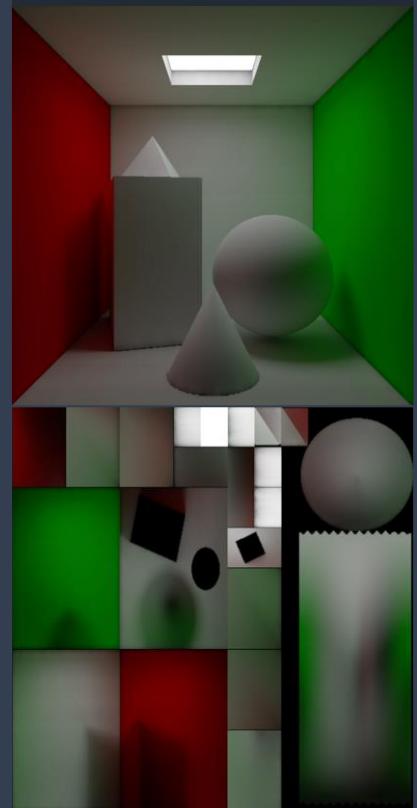
Miss shader

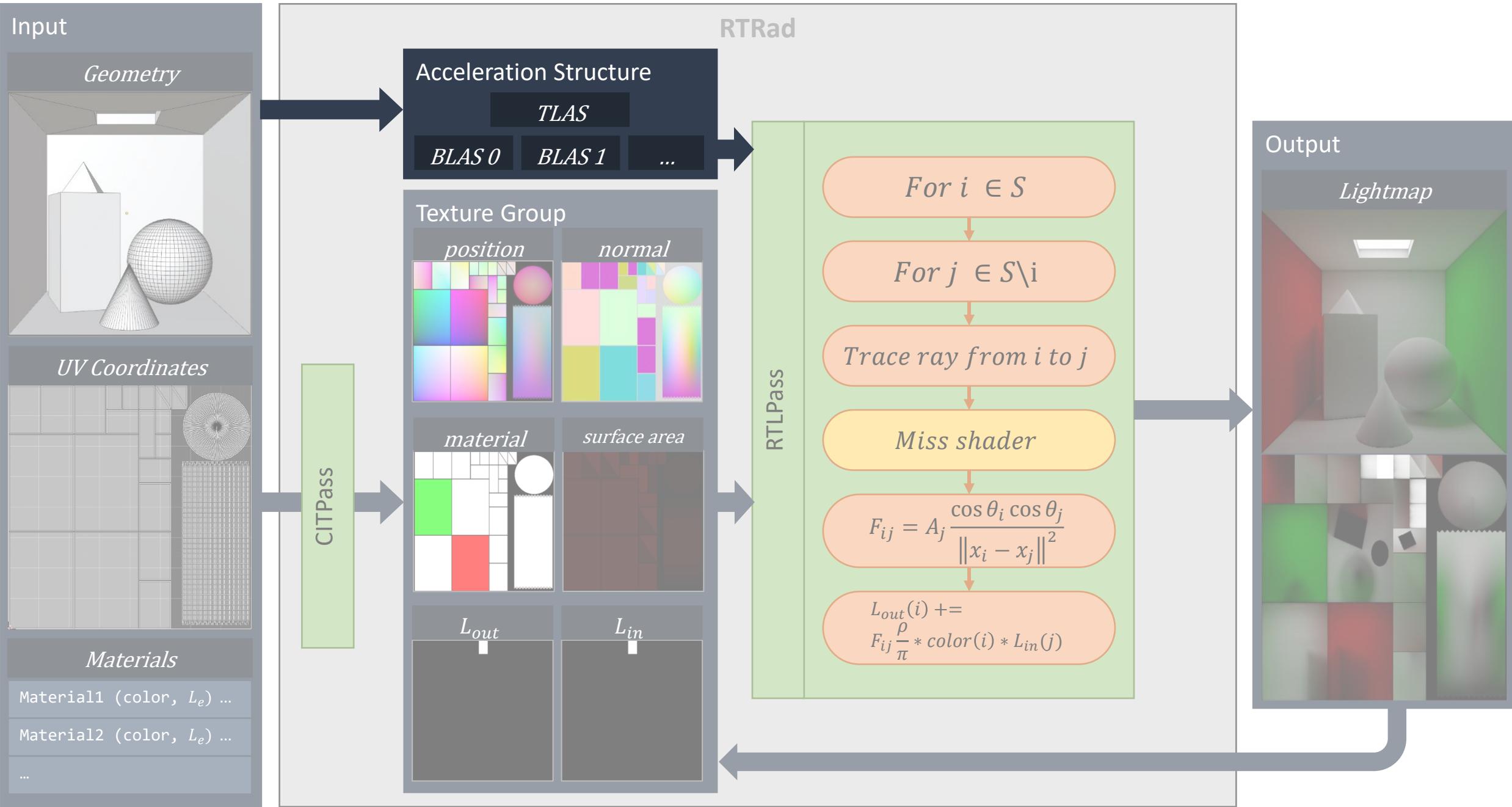
$$F_{ij} = A_j \frac{\cos \theta_i \cos \theta_j}{\|x_i - x_j\|^2}$$

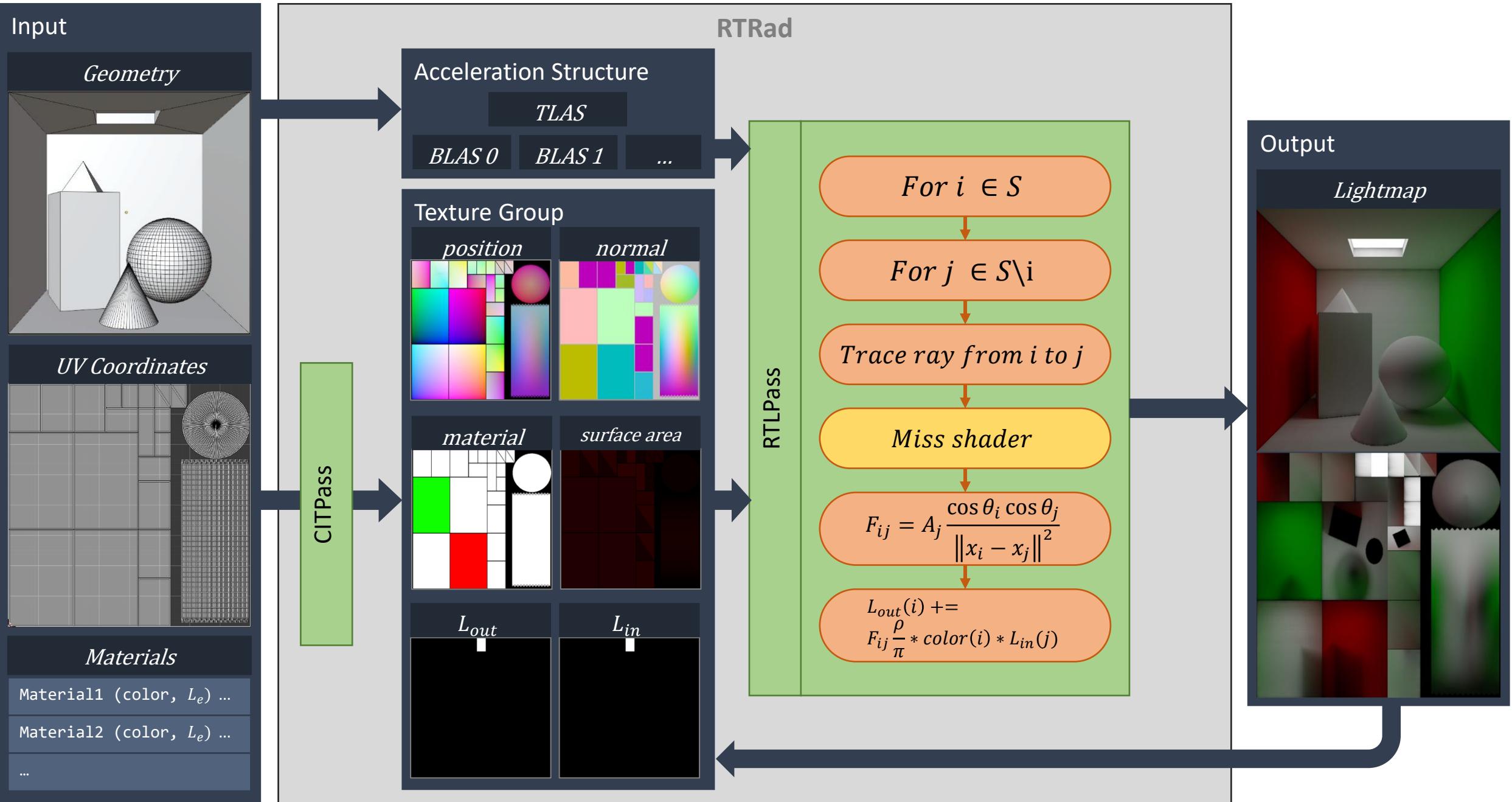
$$L_{out}(i) += F_{ij} \frac{\rho}{\pi} * color(i) * L_{in}(j)$$

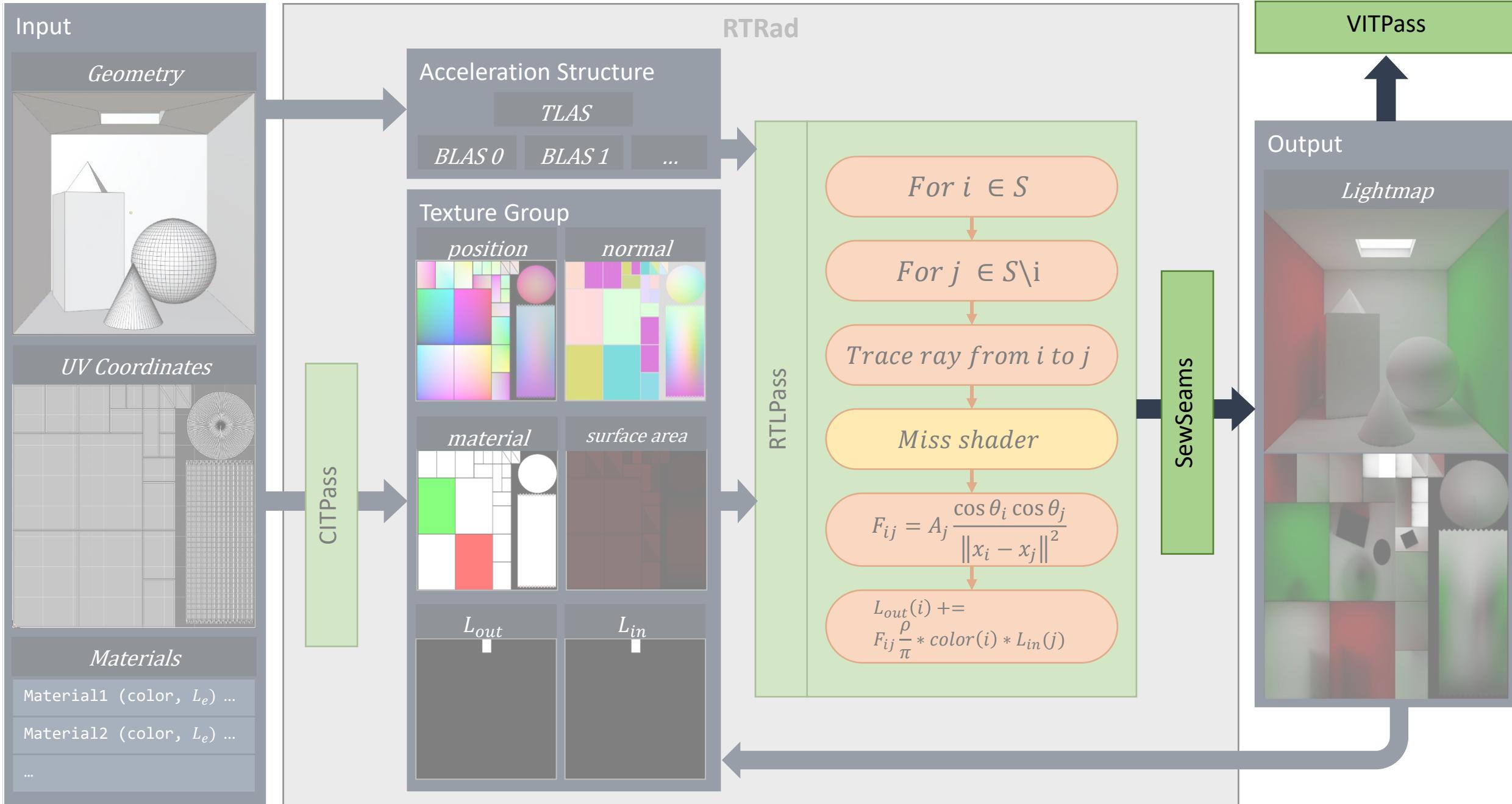
## Output

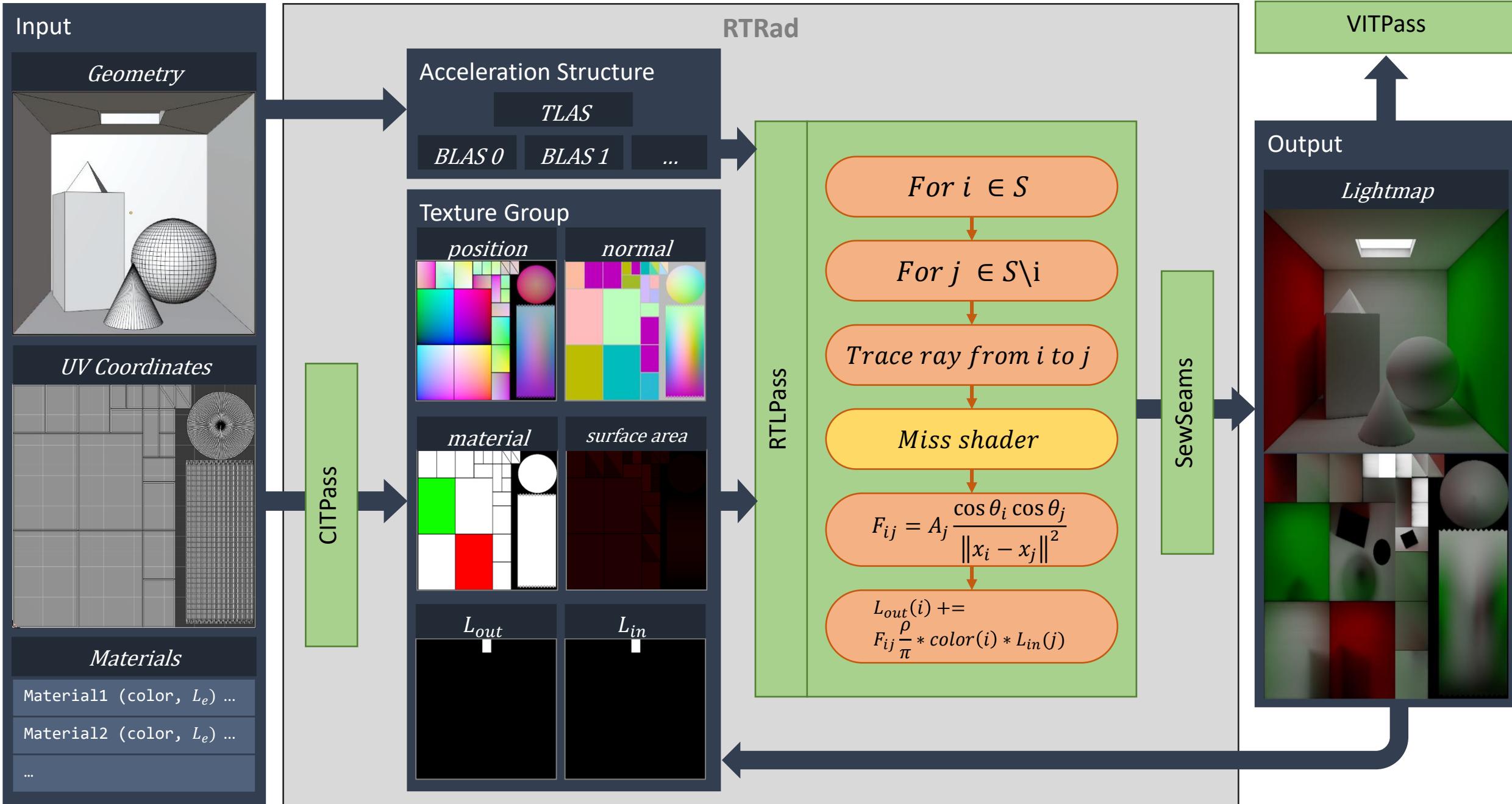
### Lightmap

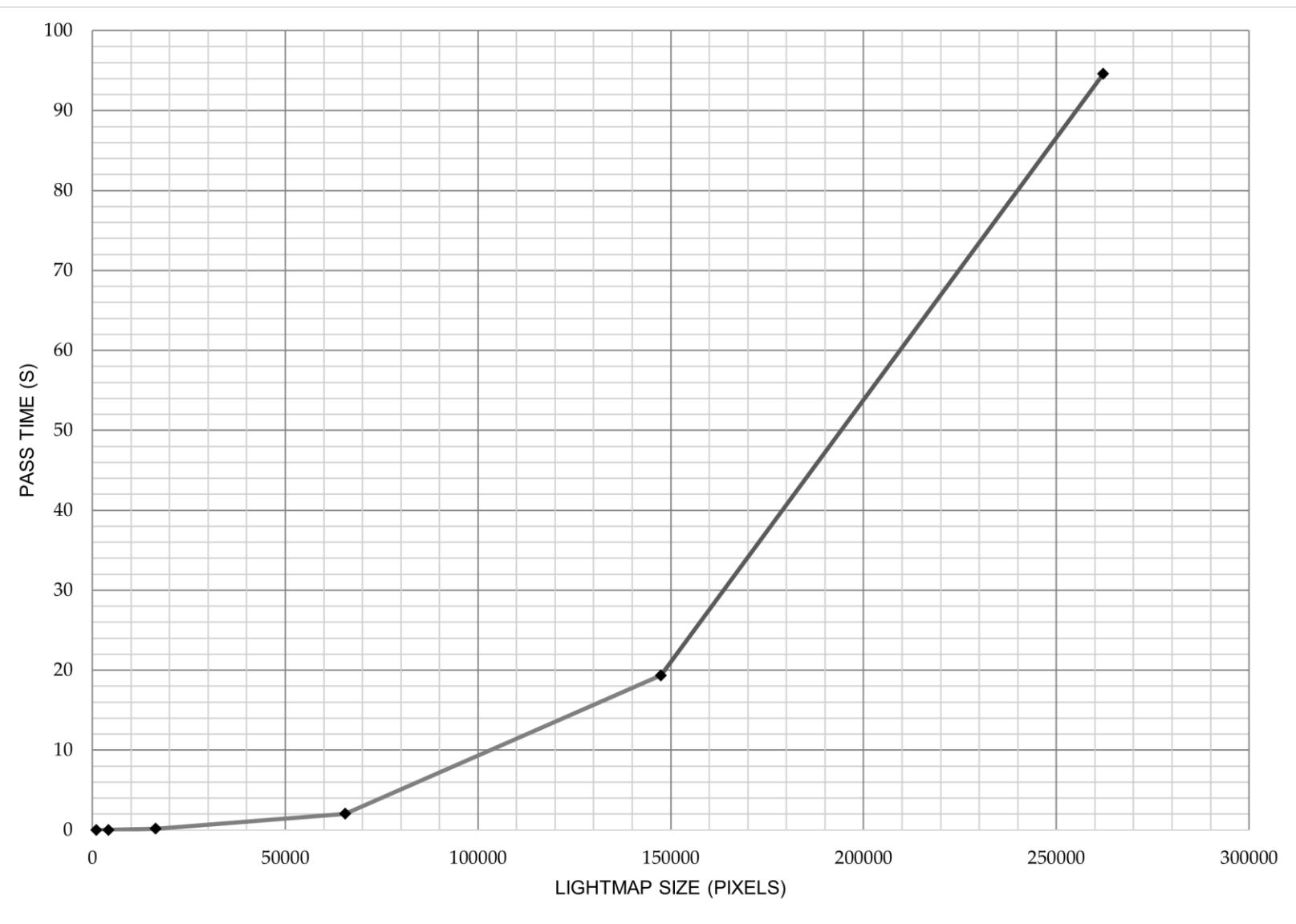








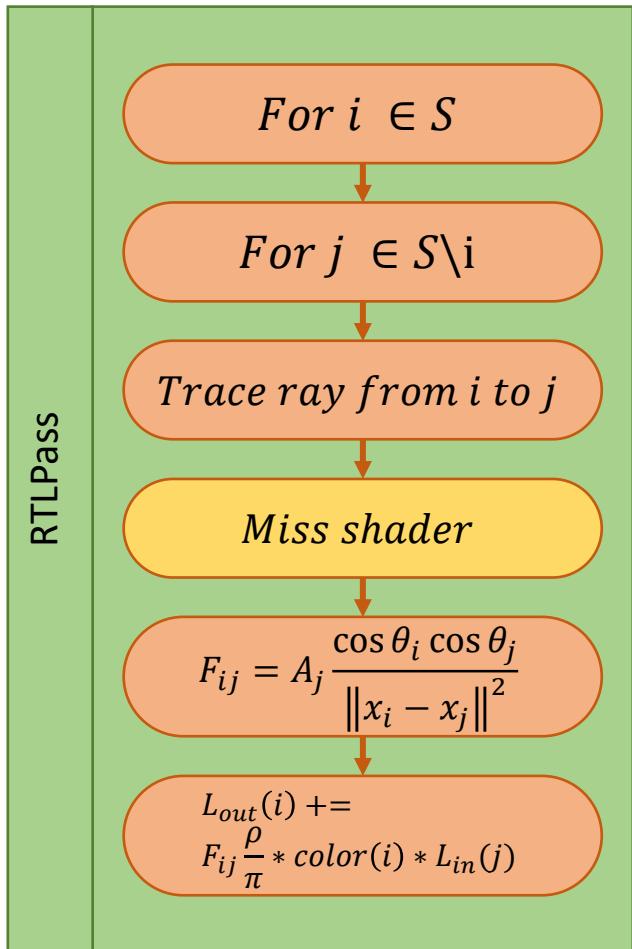




**Reciprocity Rule:**

$$V(i,j) = V(j,i)$$

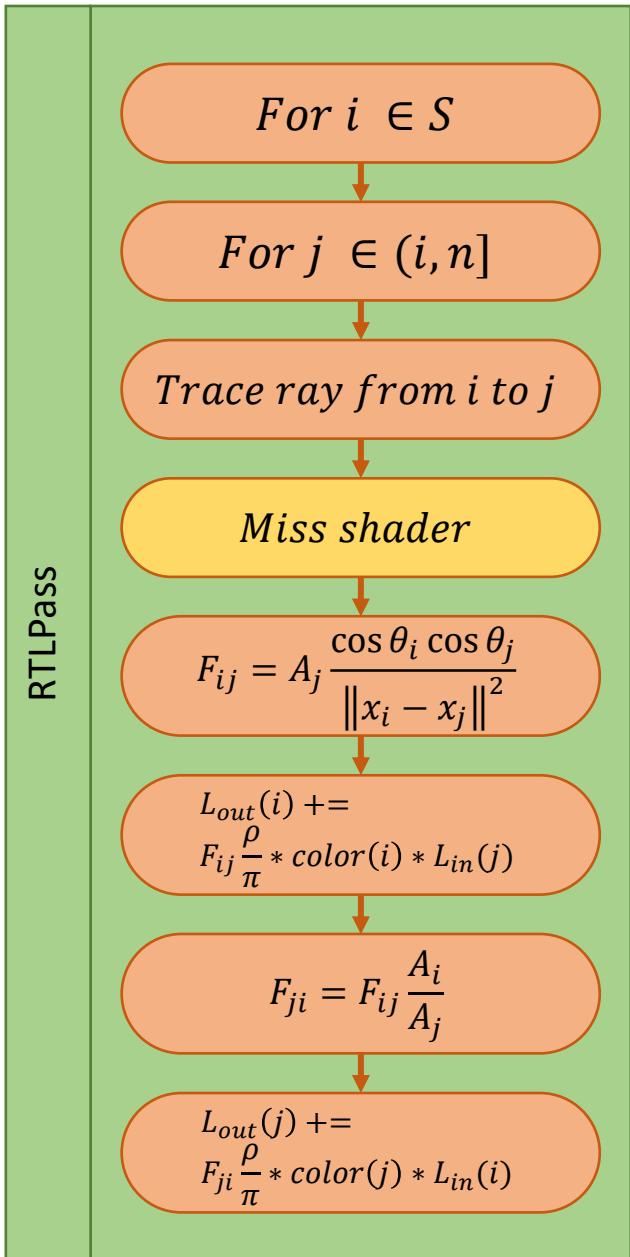
$$F_{ij} = F_{ji} \frac{A_j}{A_i}$$



**Reciprocity Rule:**

$$V(i,j) = V(j,i)$$

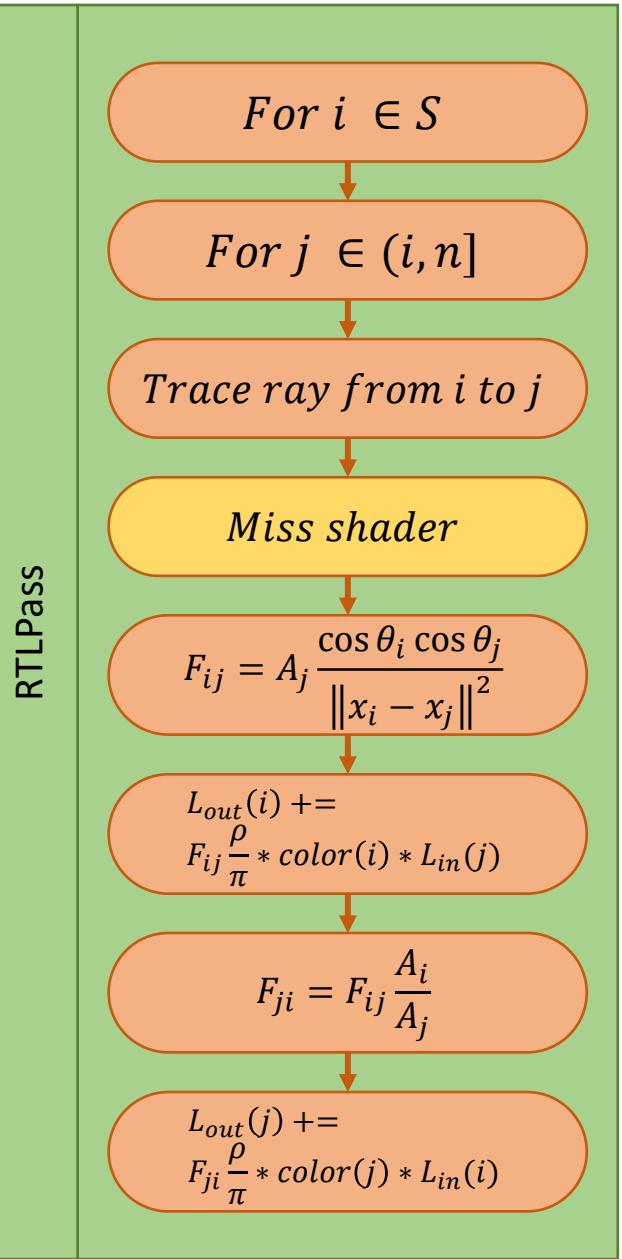
$$F_{ij} = F_{ji} \frac{A_j}{A_i}$$



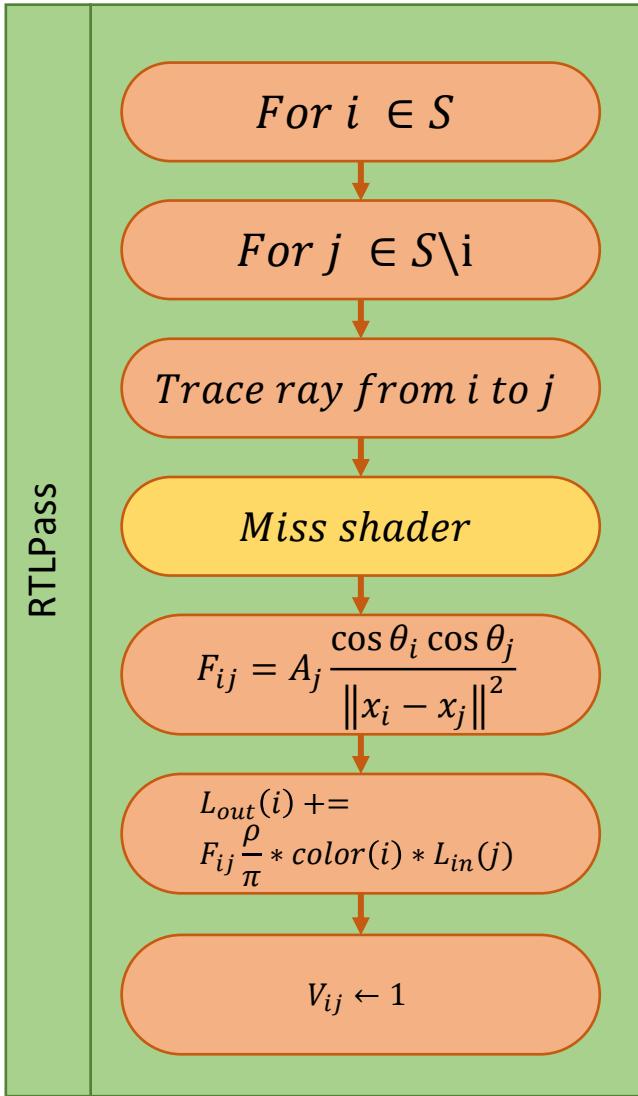
**Reciprocity Rule:**

$$V(i, j) = V(j, i)$$

$$F_{ij} = F_{ji} \frac{A_j}{A_i}$$

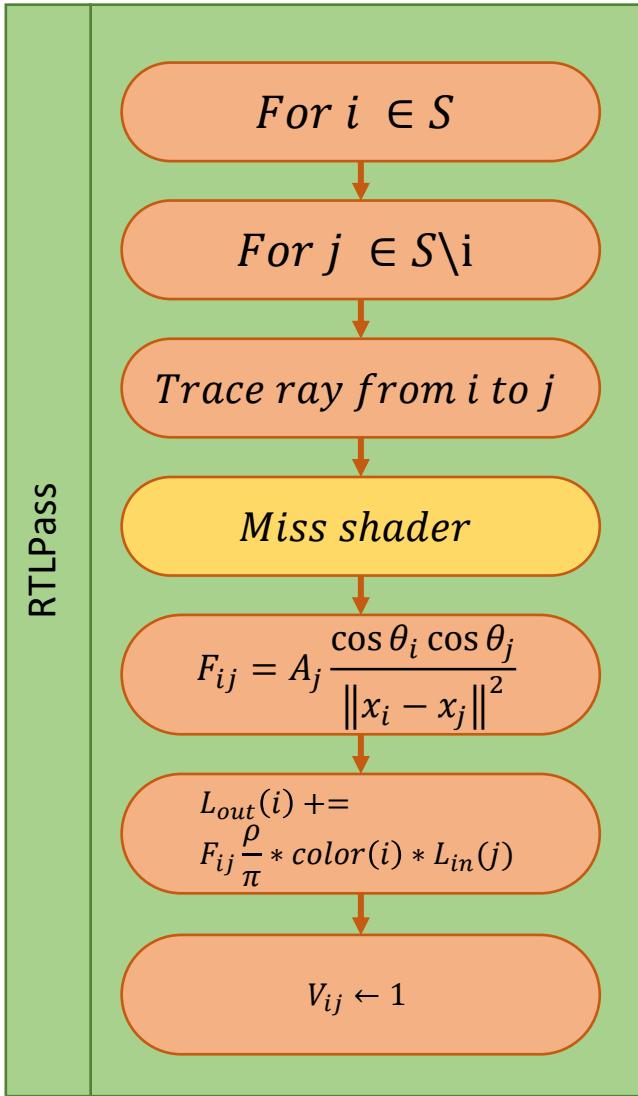


## Visibility Caching:

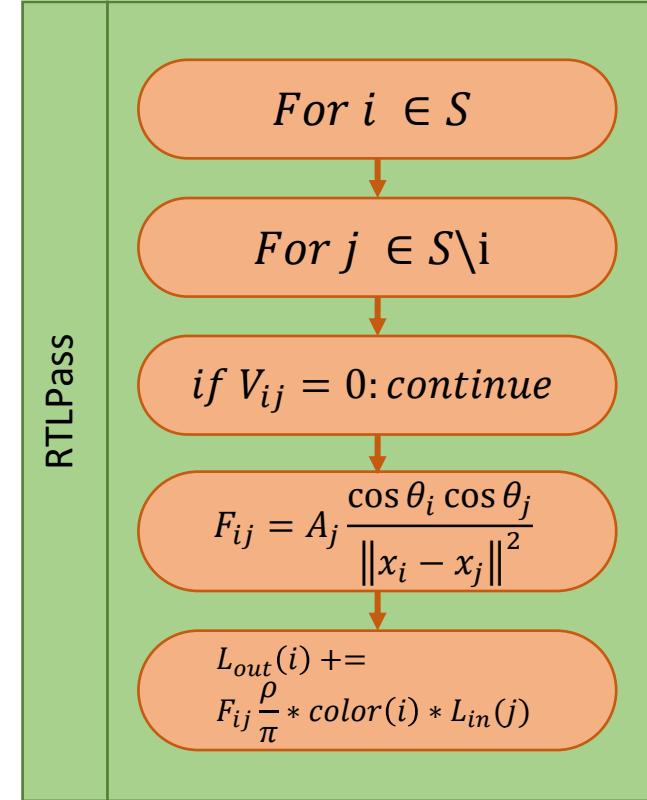


First Iteration

## Visibility Caching:

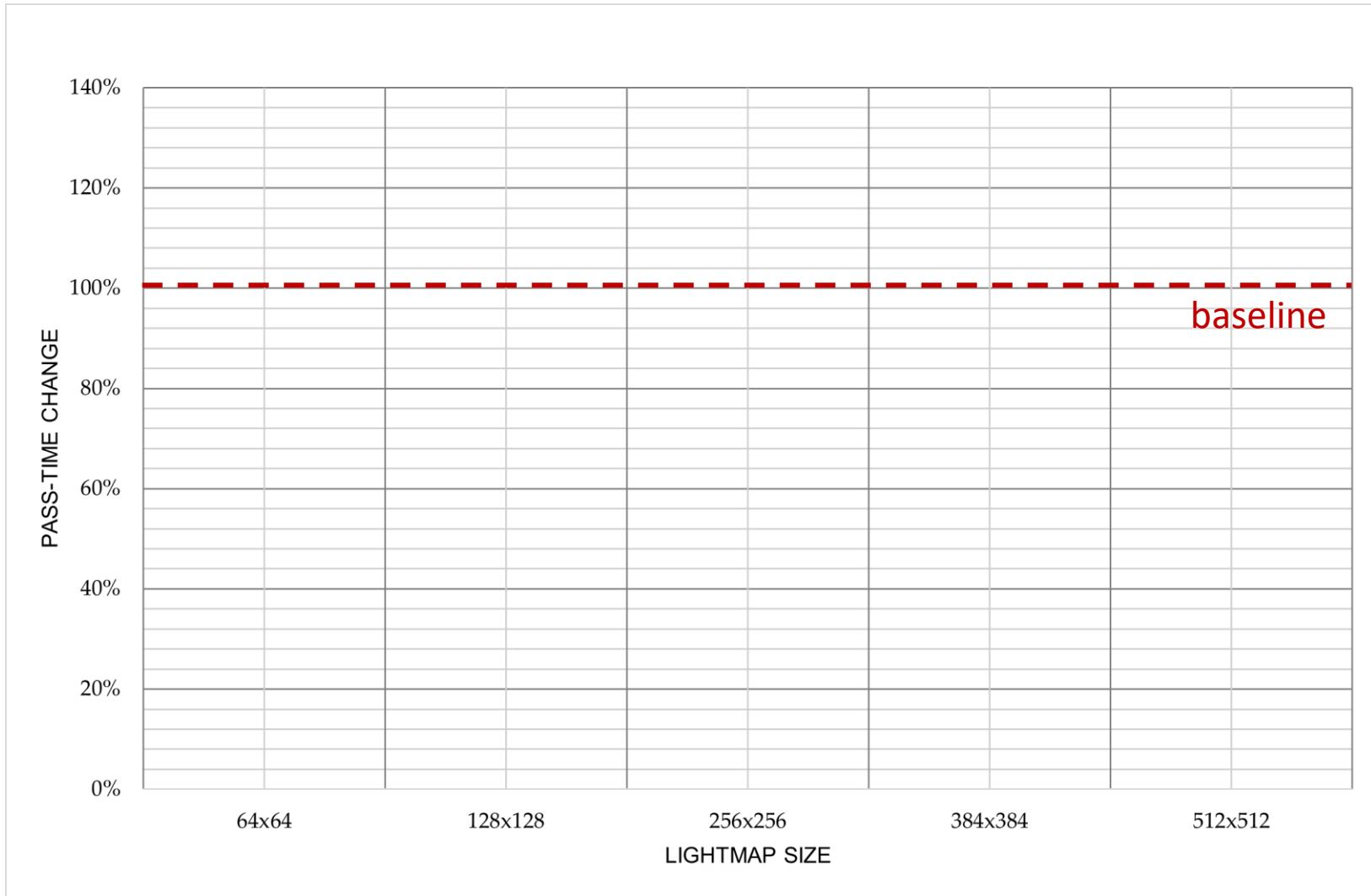


First Iteration

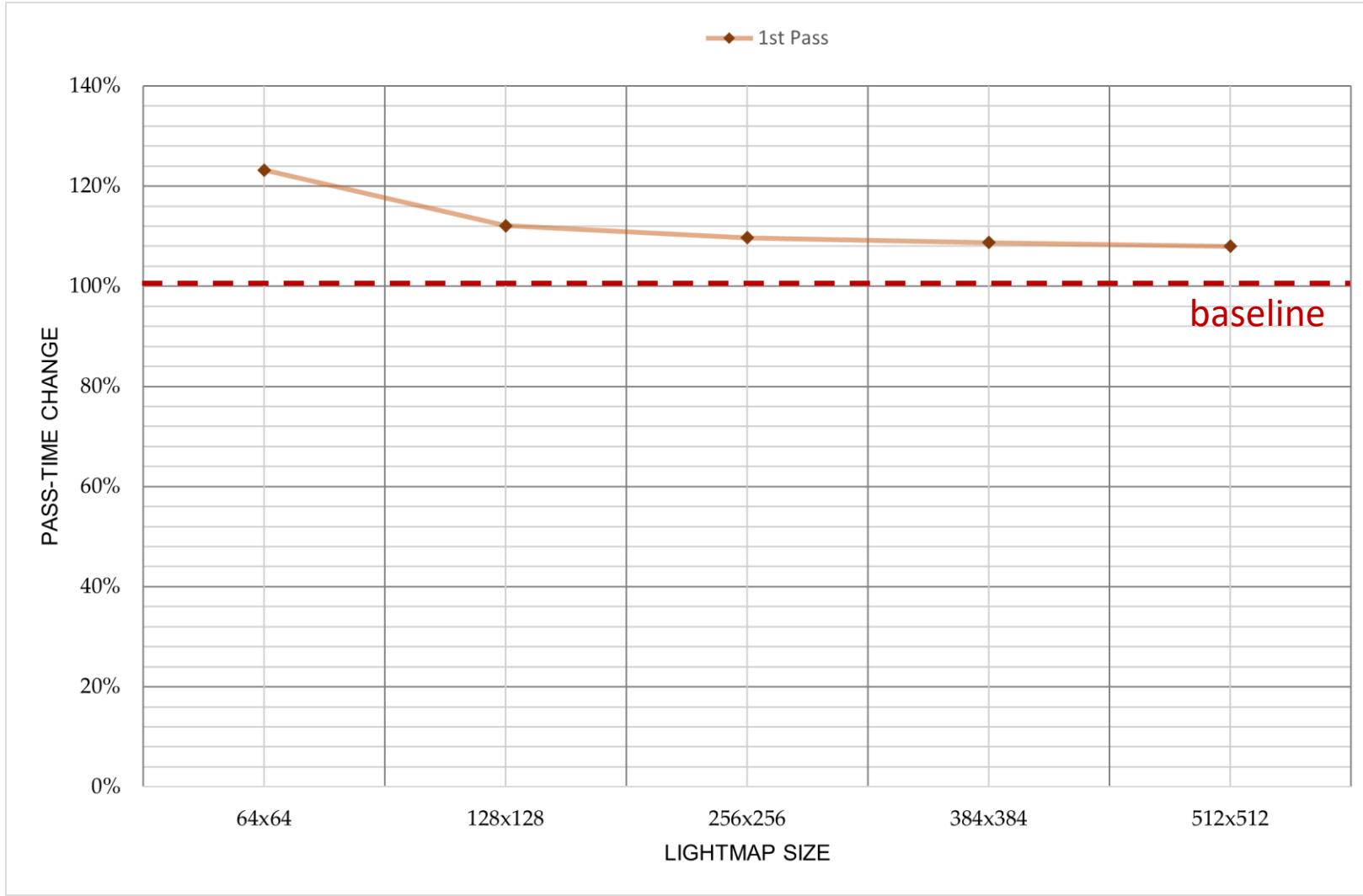


Subsequent Iterations

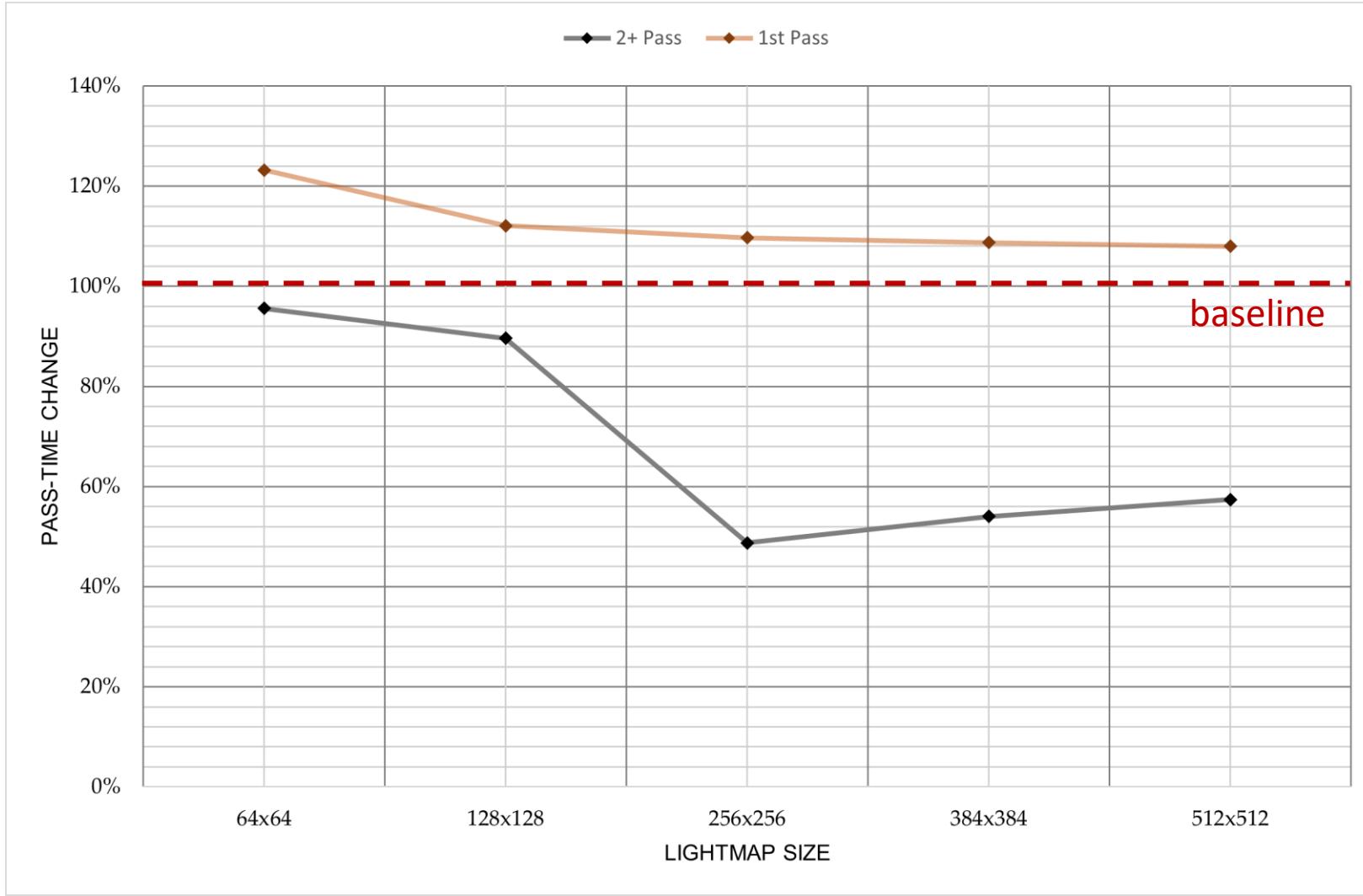
## Visibility Caching:



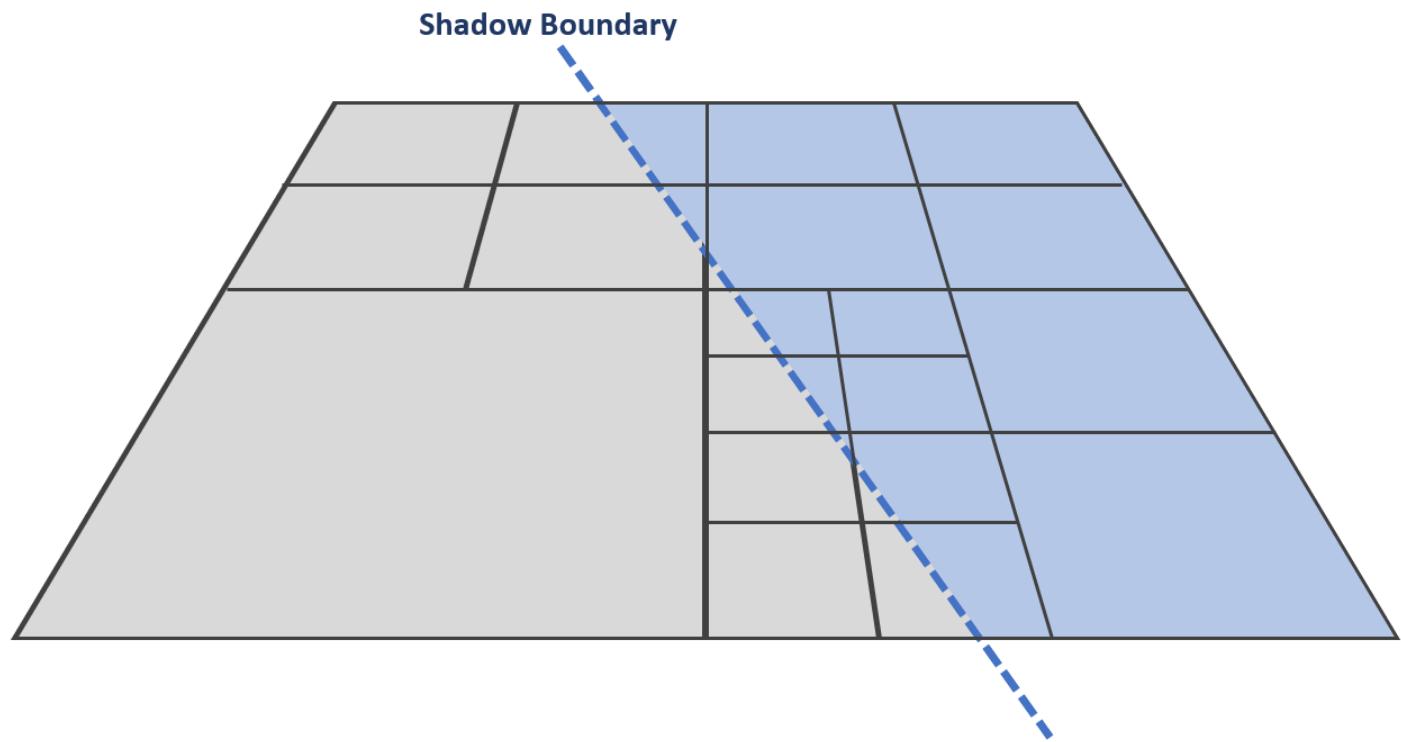
## Visibility Caching:



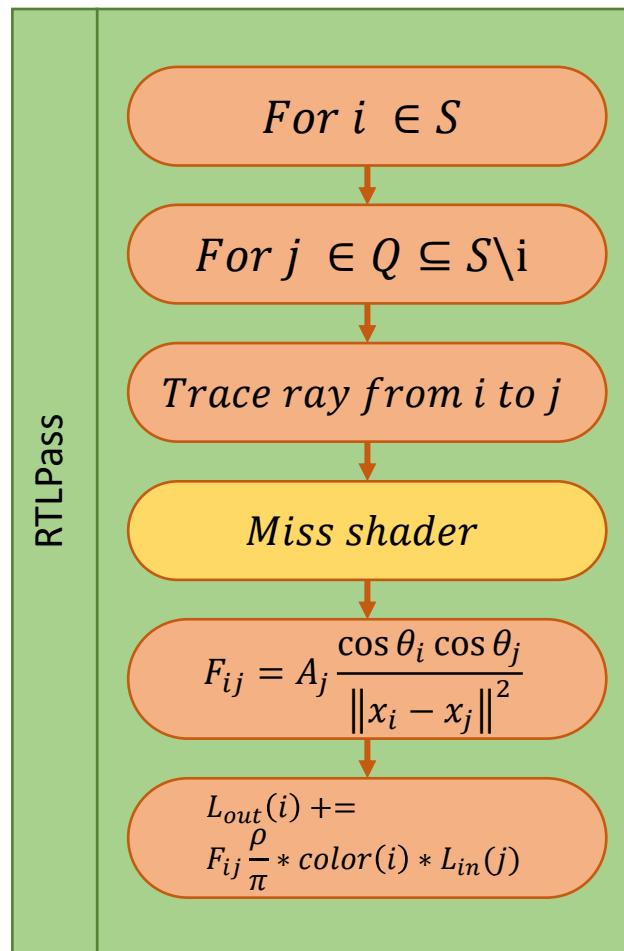
## Visibility Caching:



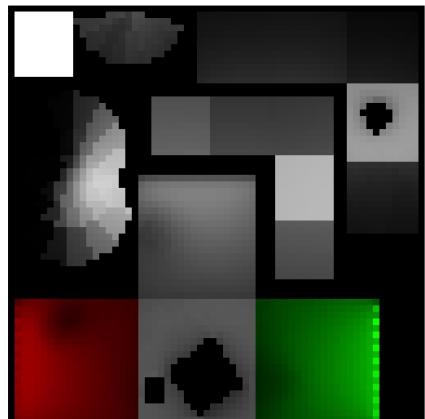
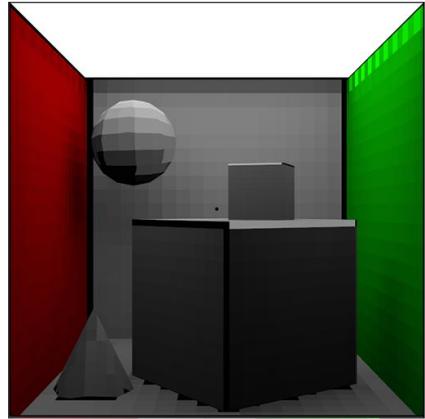
# Refinement



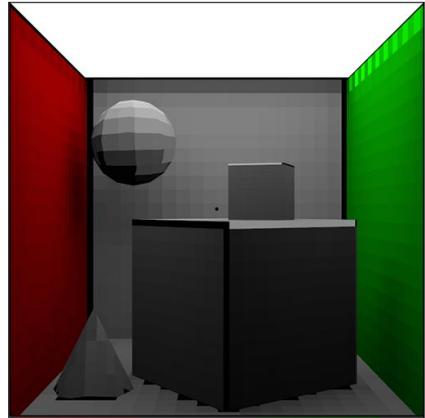
## Refinement



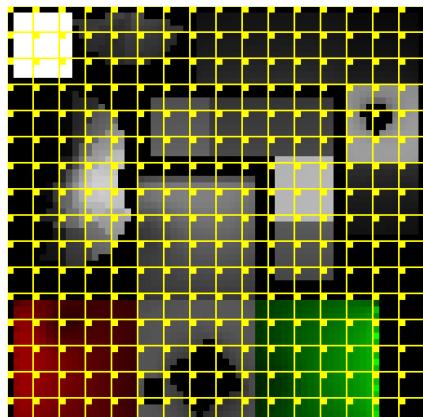
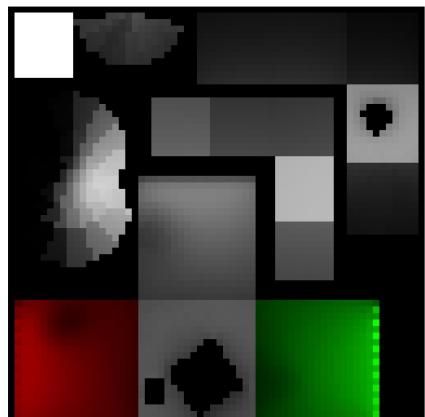
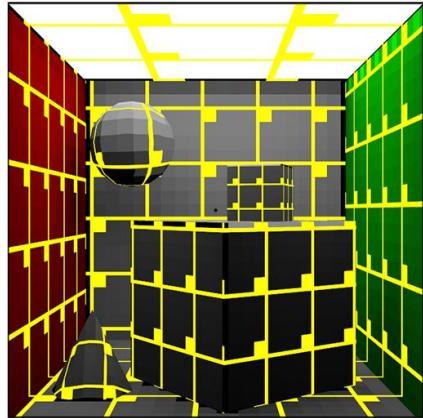
*Scene*



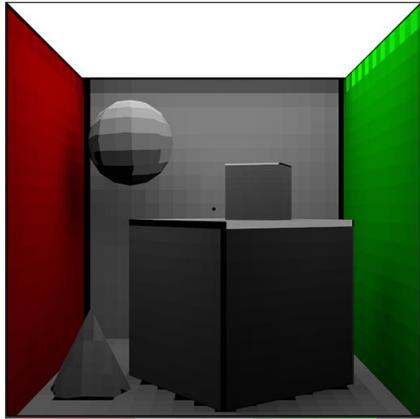
*Scene*



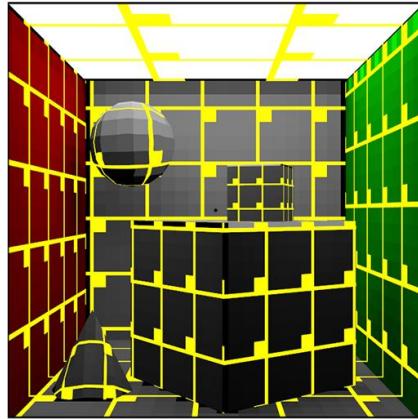
*Static Undersampling*



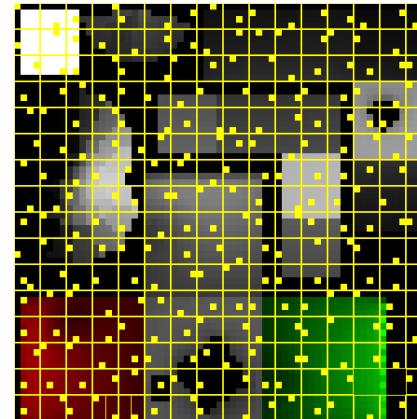
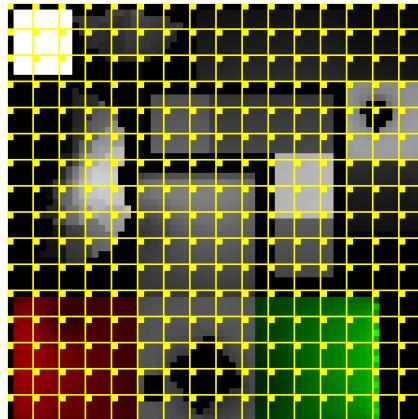
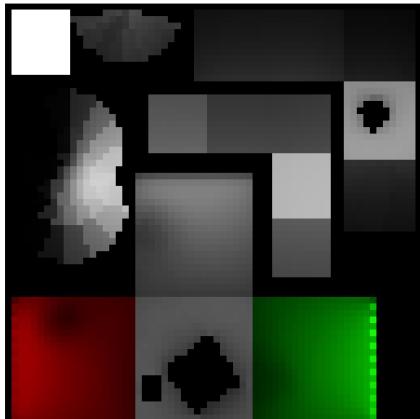
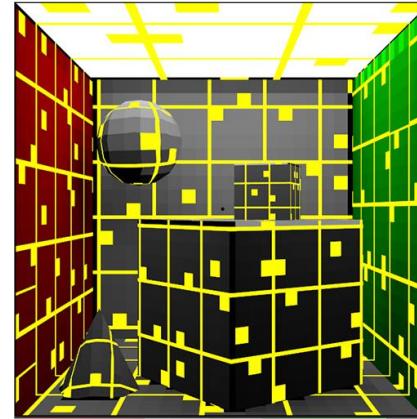
*Scene*



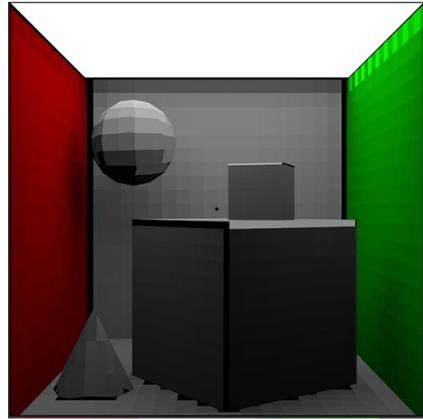
*Static Undersampling*



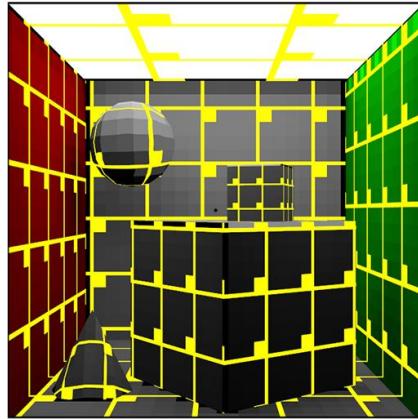
*Monte Carlo  
Undersampling*



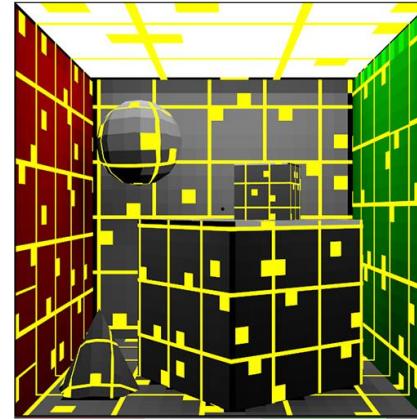
*Scene*



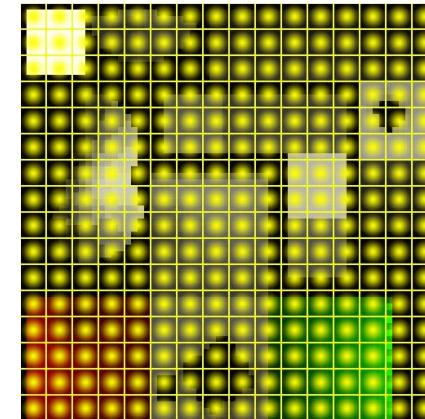
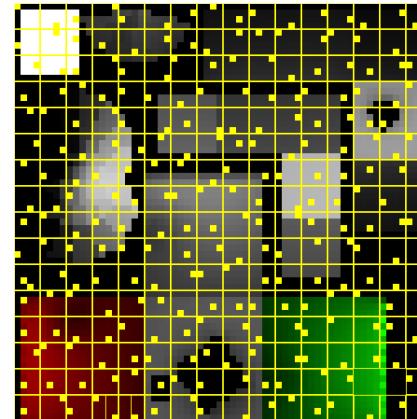
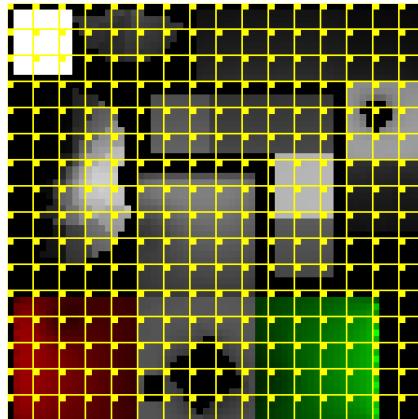
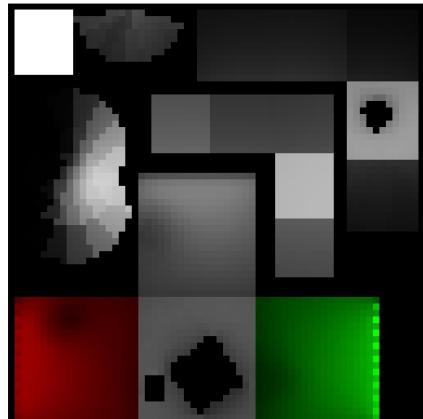
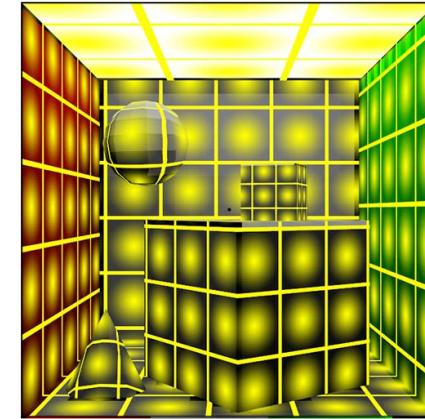
*Static Undersampling*

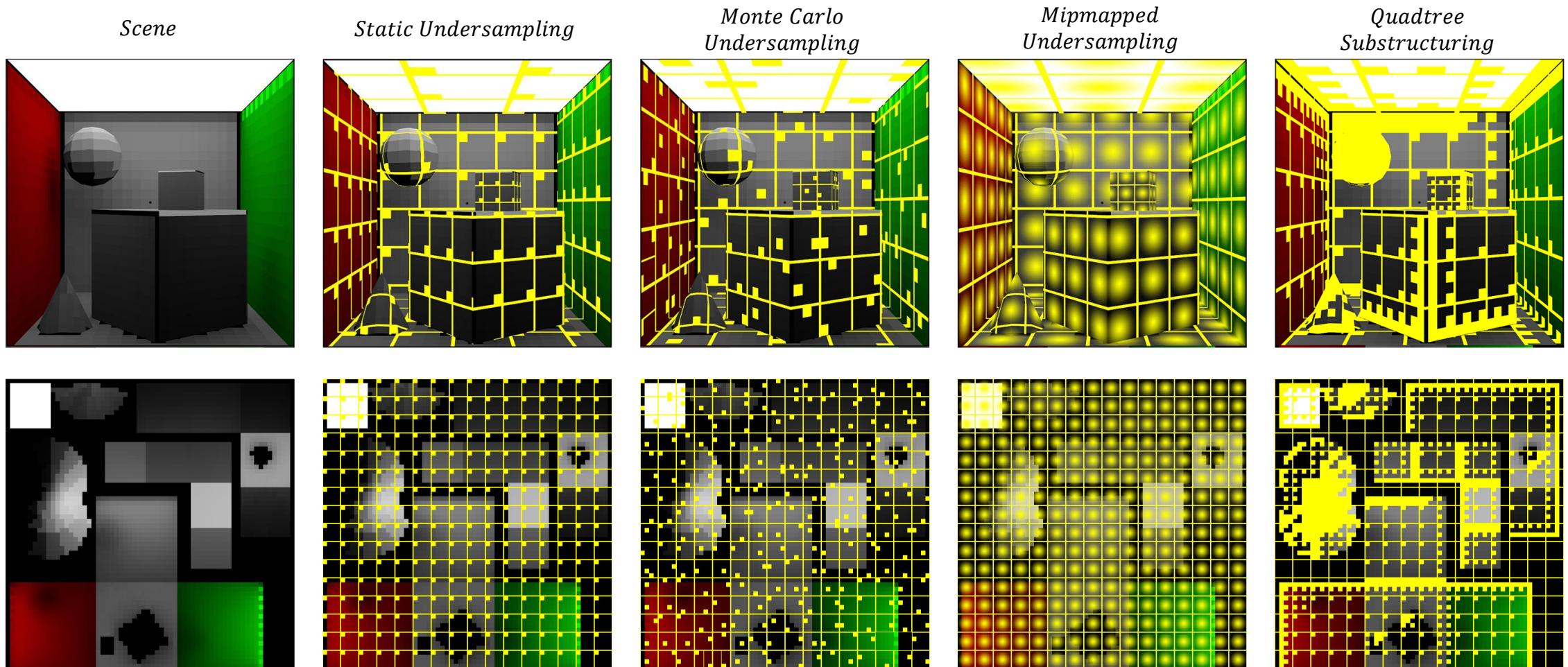


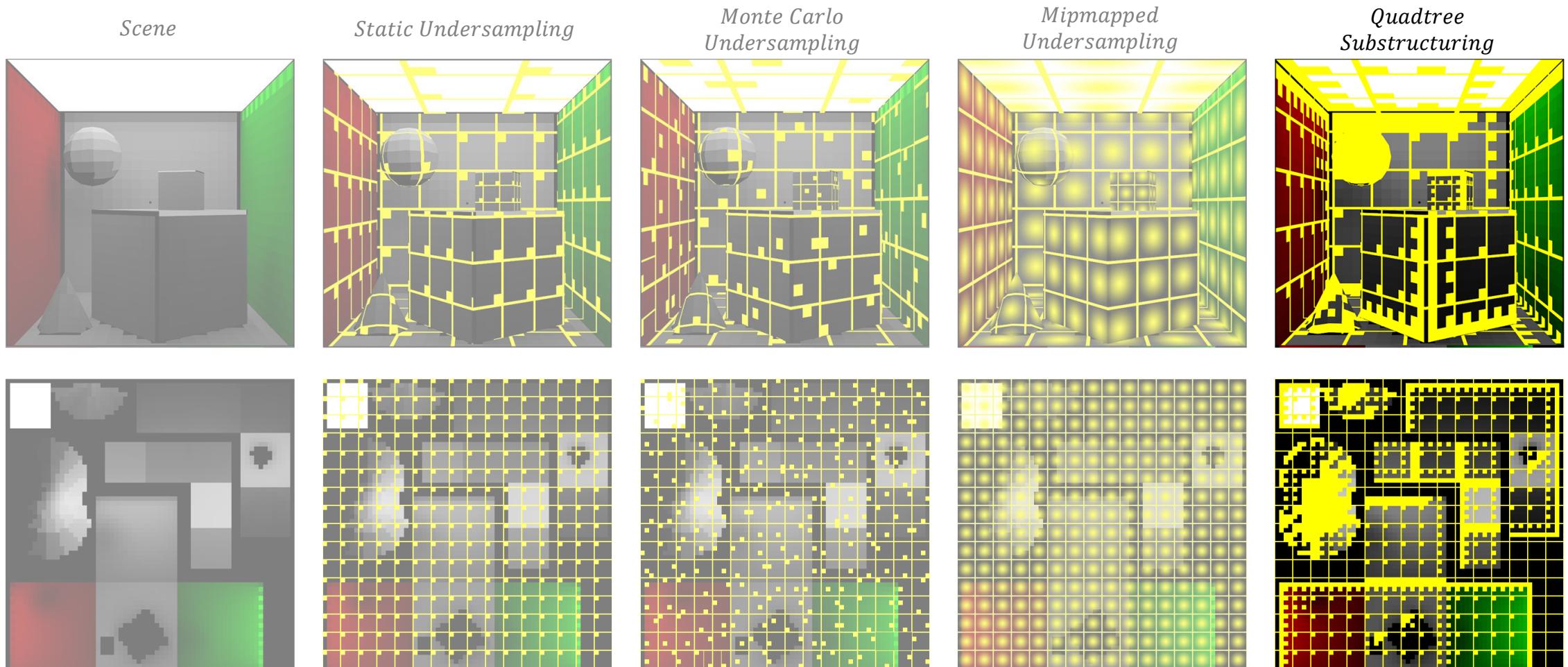
*Monte Carlo  
Undersampling*

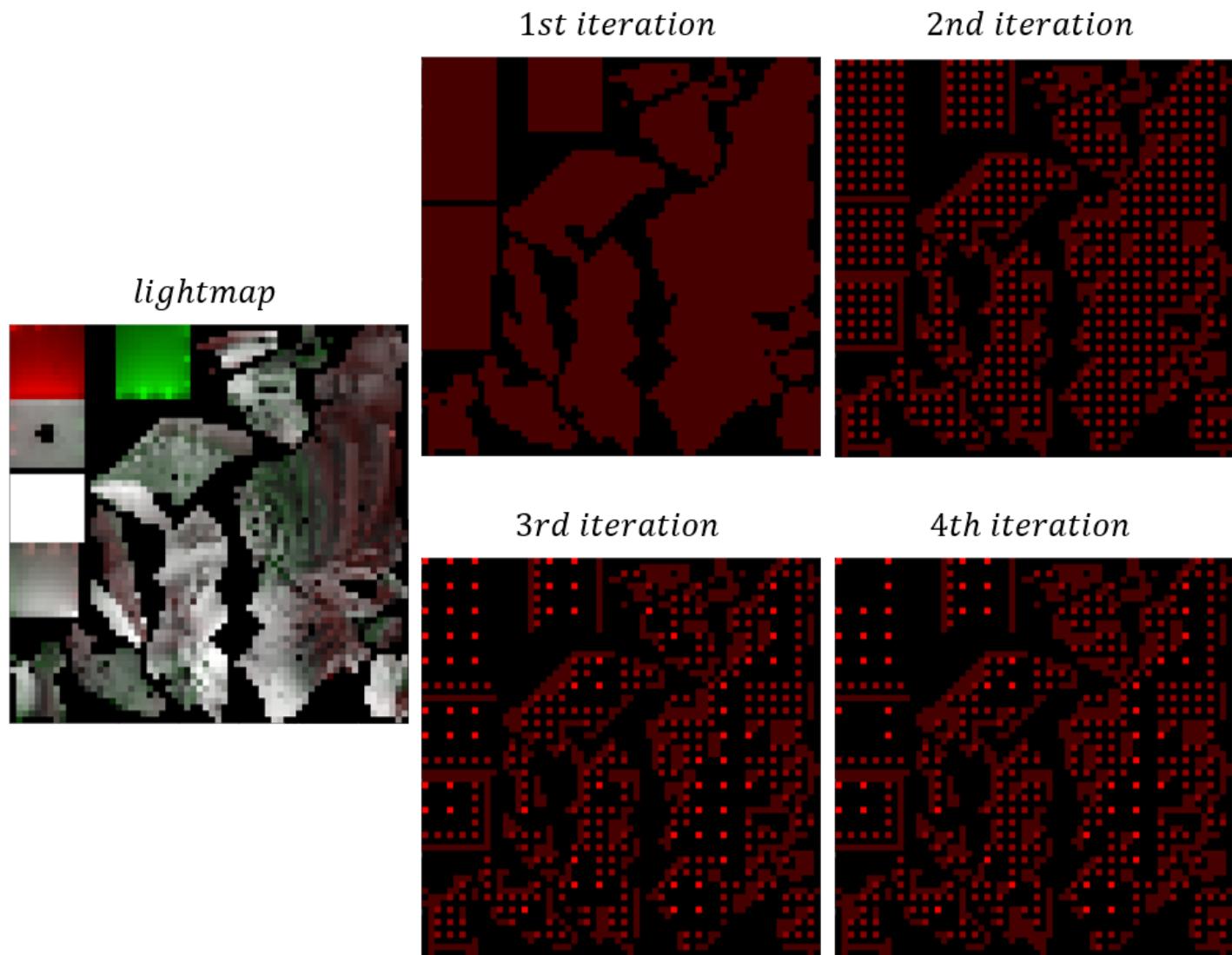


*Mipmapped  
Undersampling*

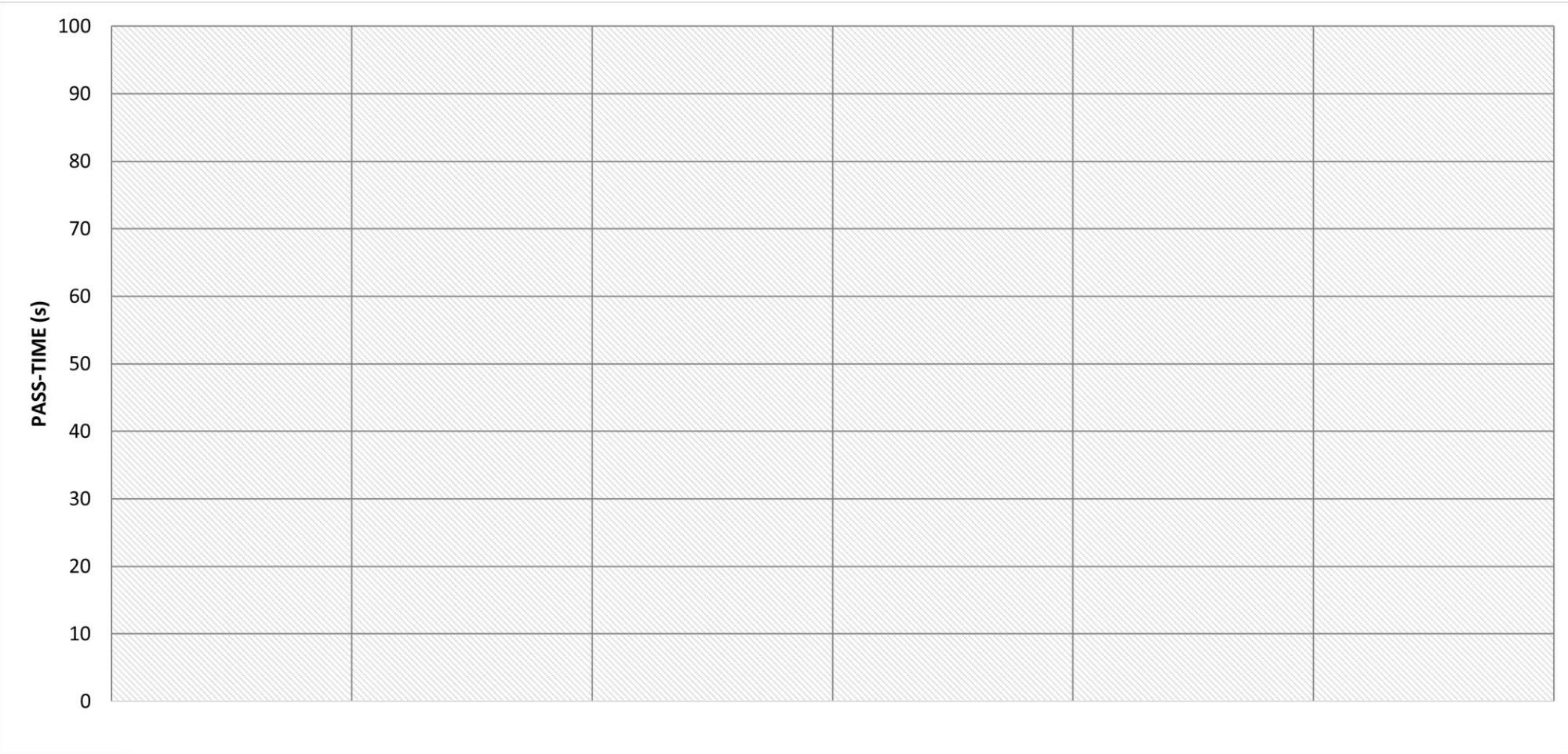




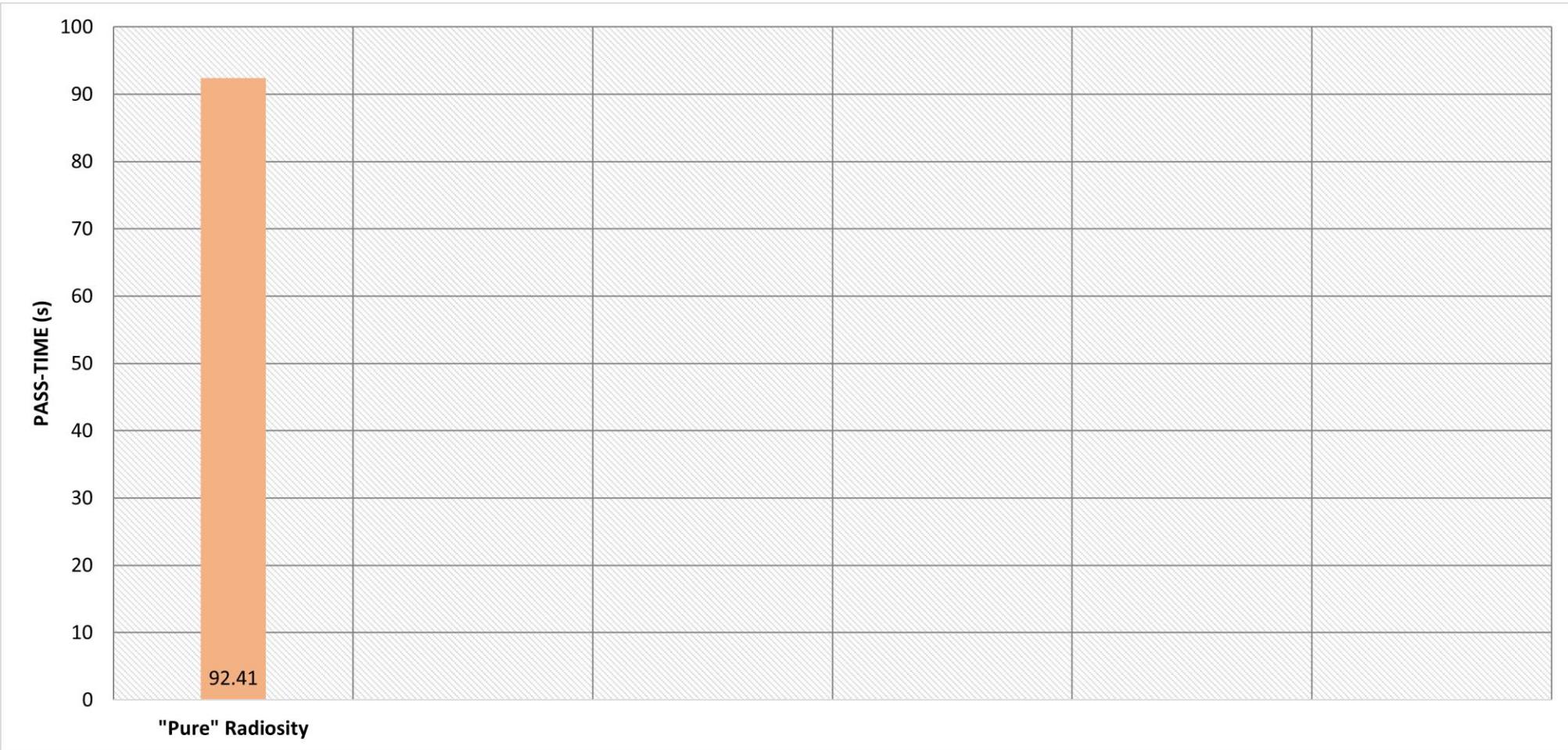




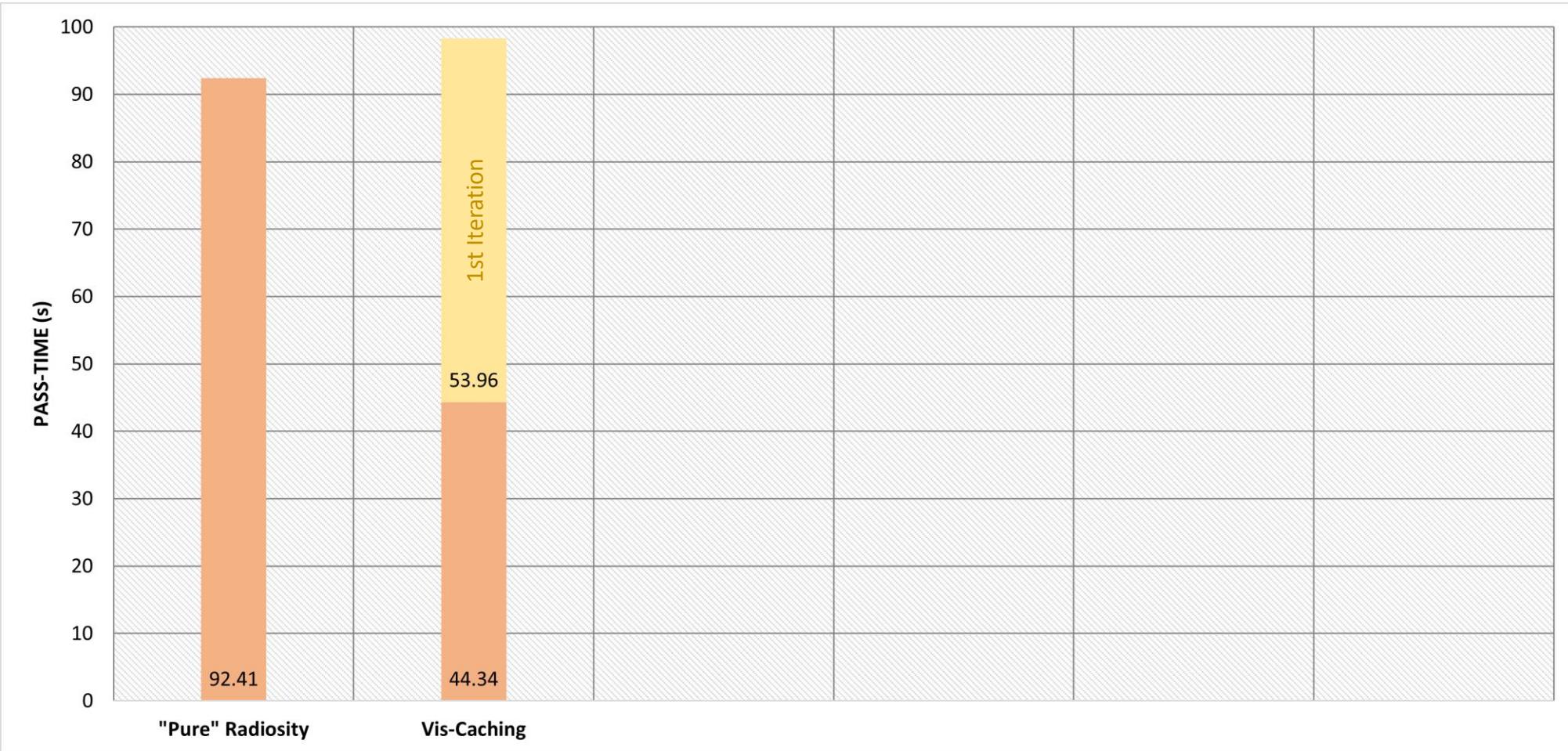
Lightmap size: 512x512



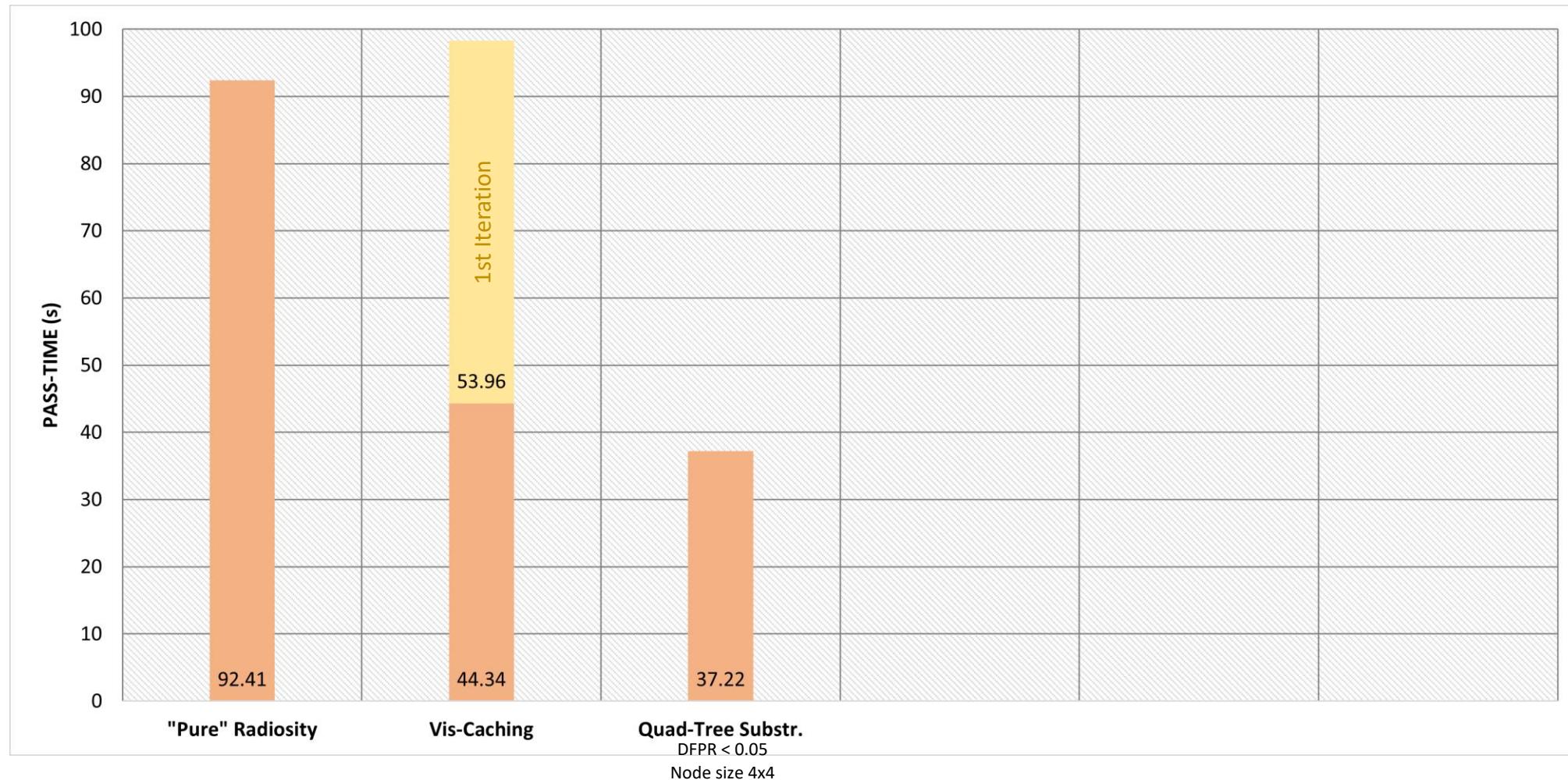
Lightmap size: 512x512



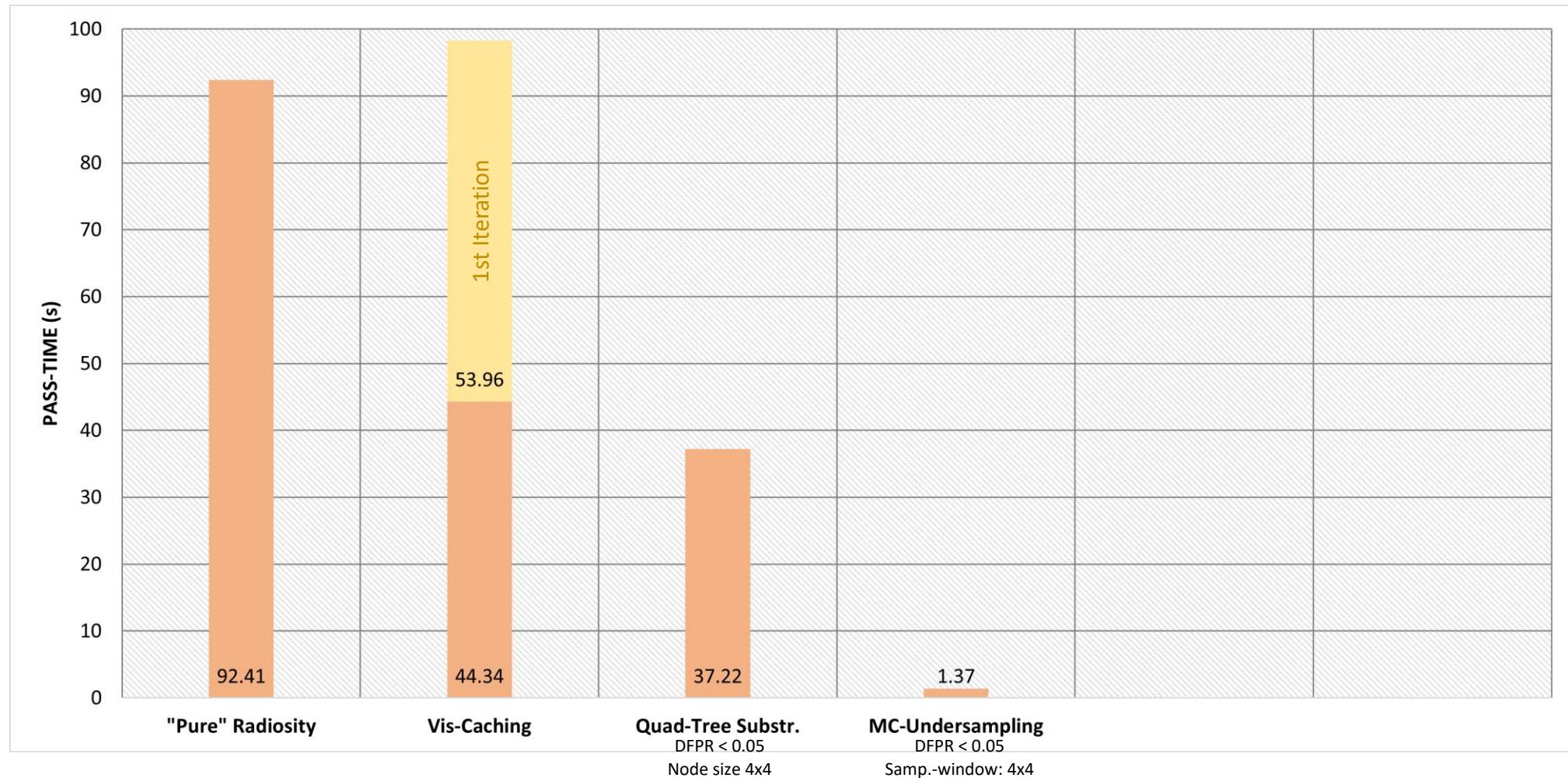
Lightmap size: 512x512



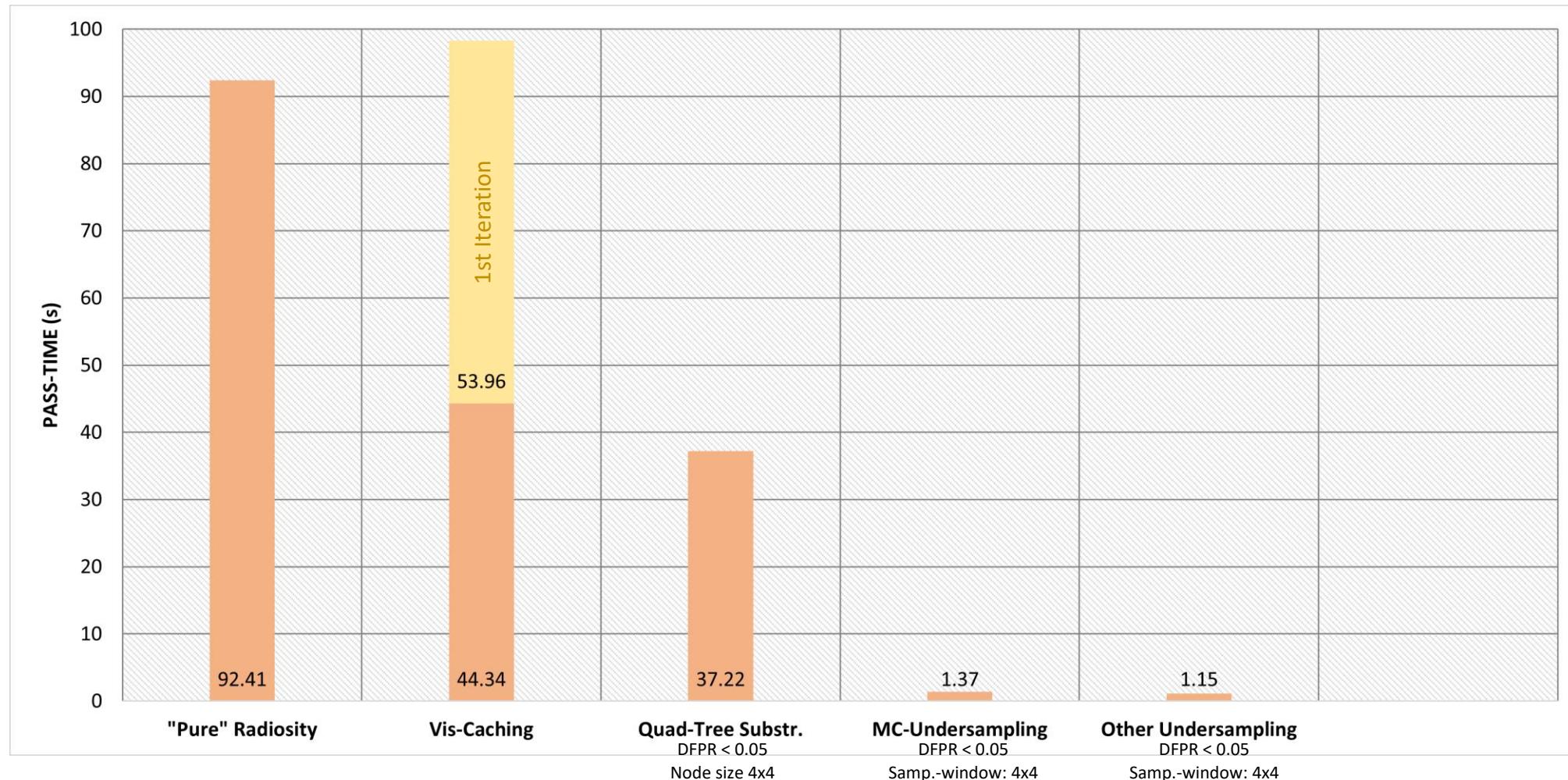
Lightmap size: 512x512



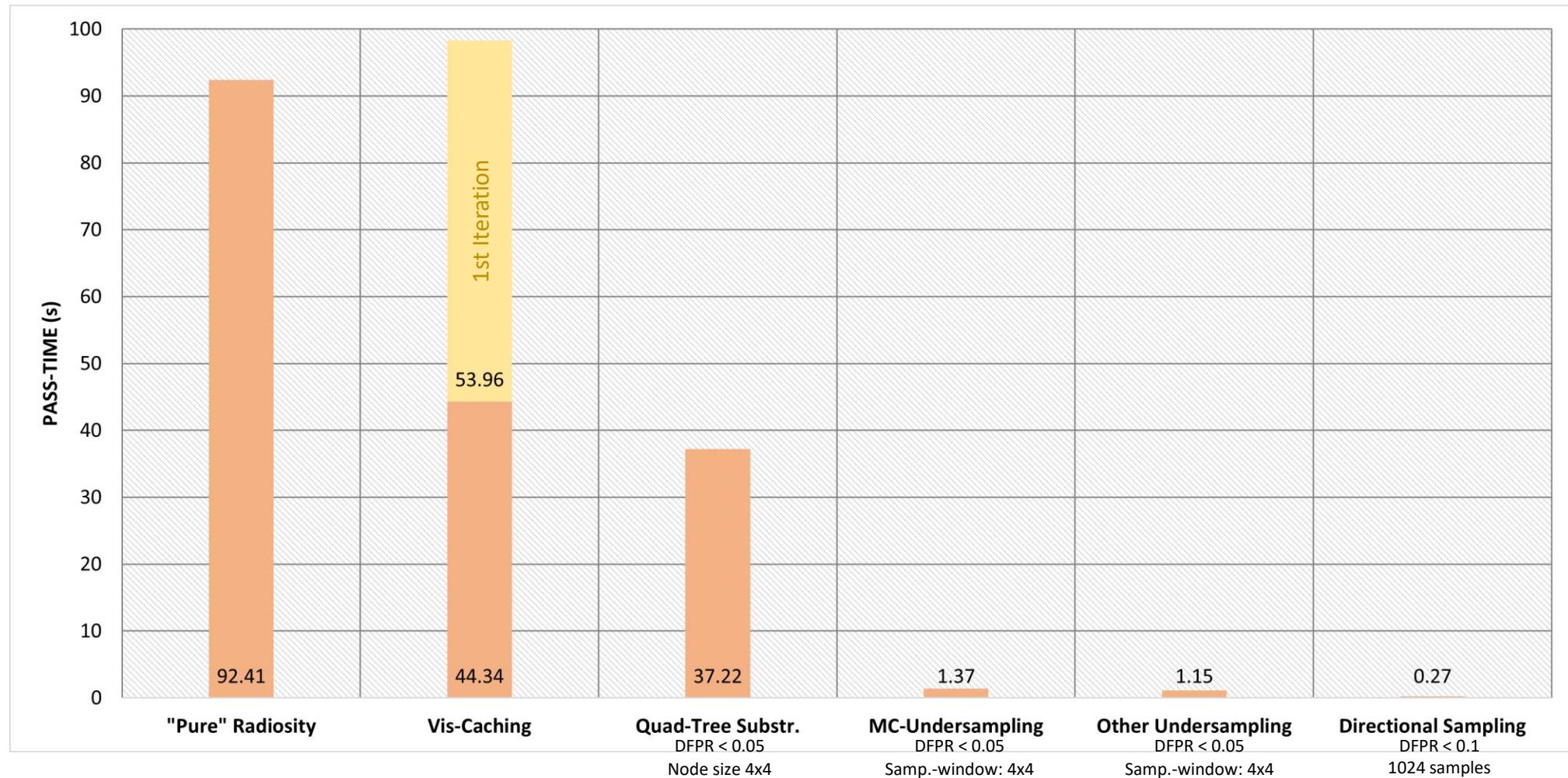
Lightmap size: 512x512



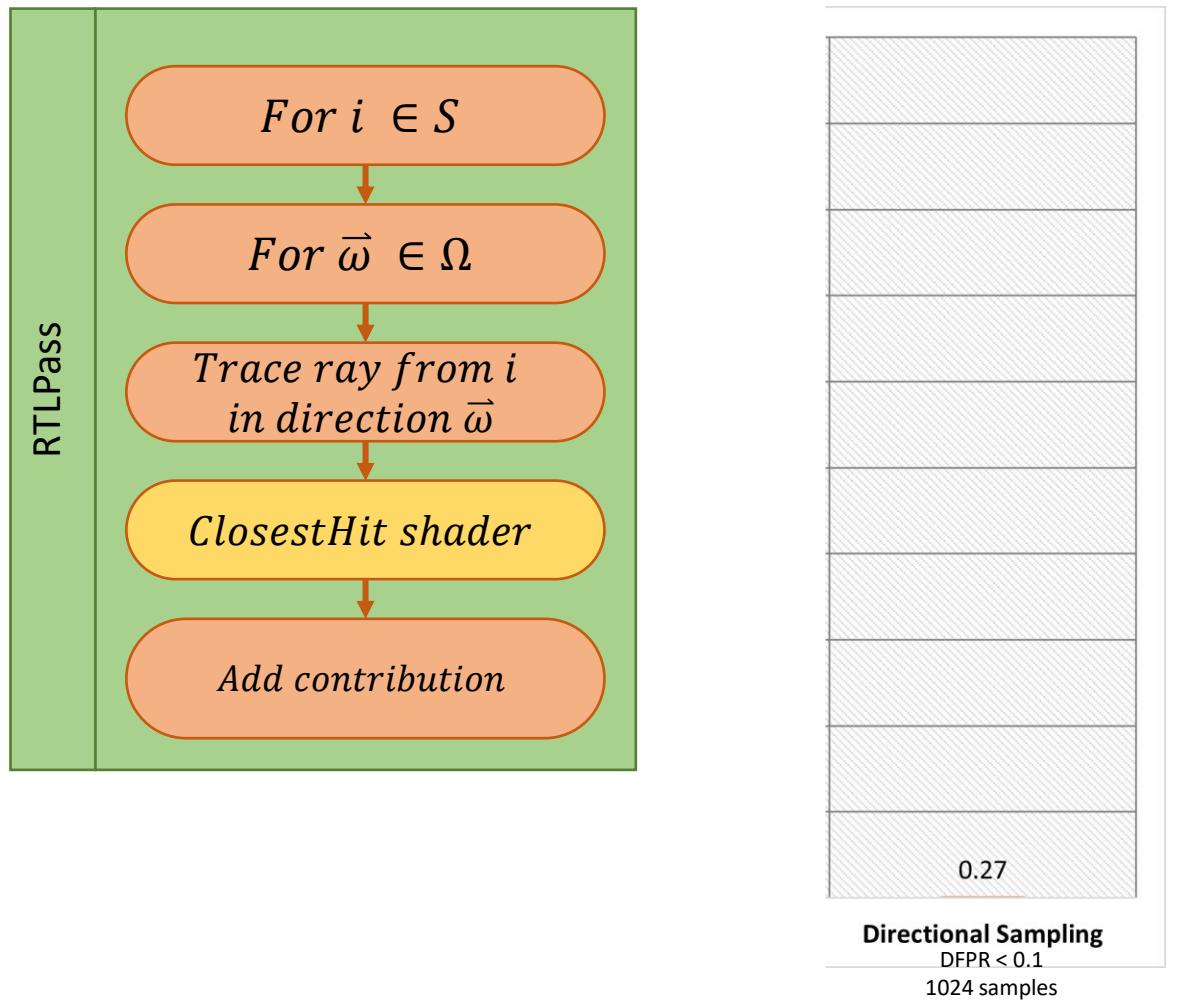
Lightmap size: 512x512



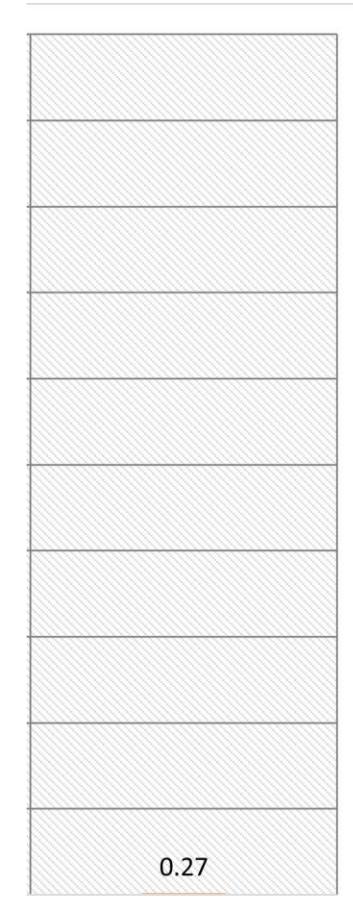
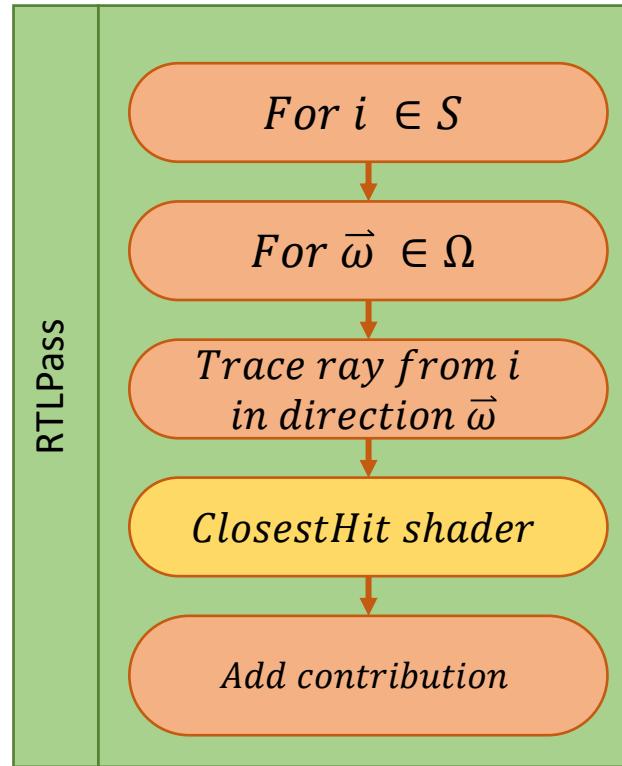
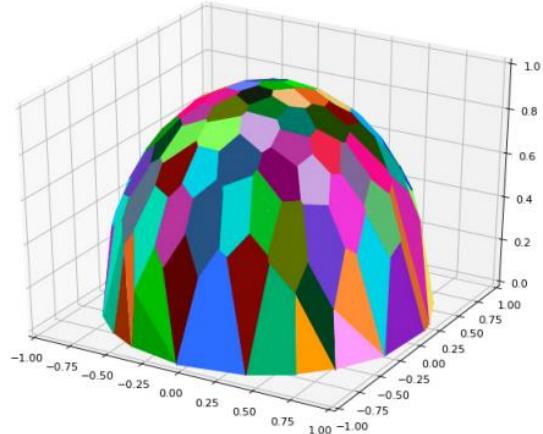
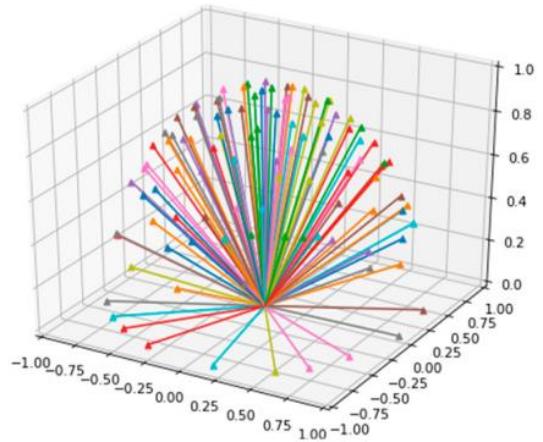
Lightmap size: 512x512



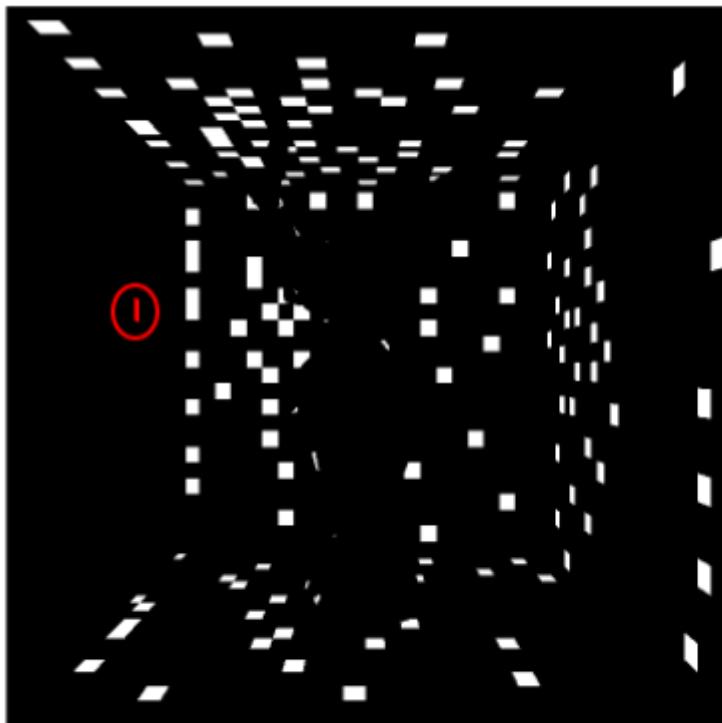
# Directional Sampling



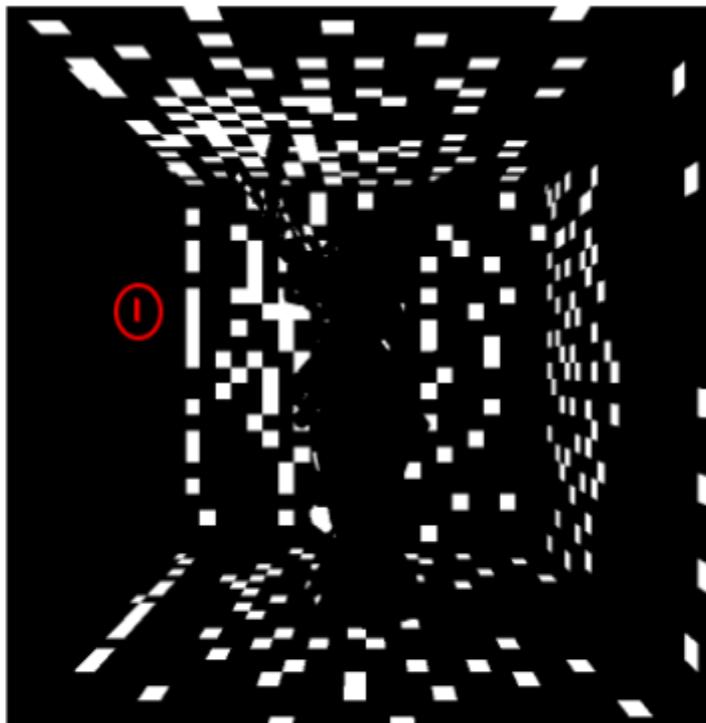
# Directional Sampling



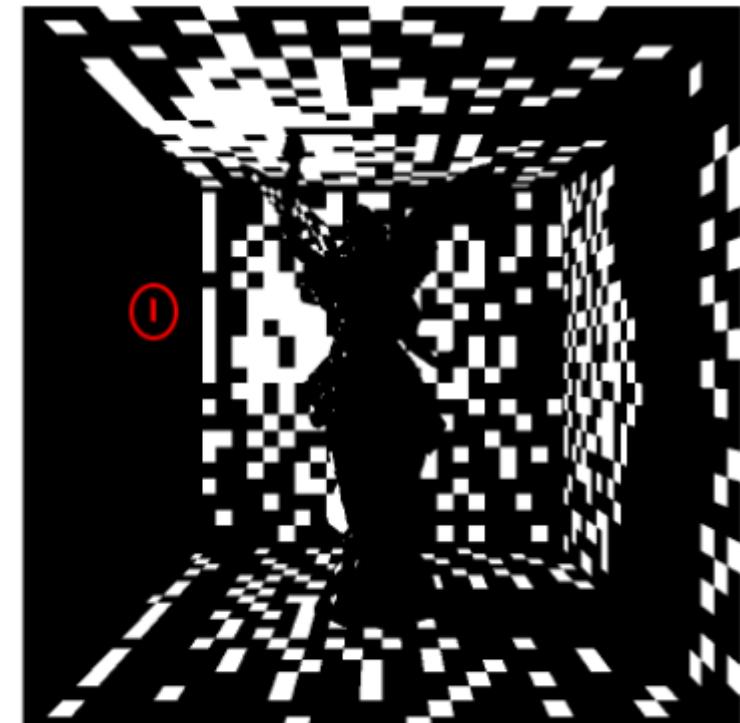
## Directional Sampling



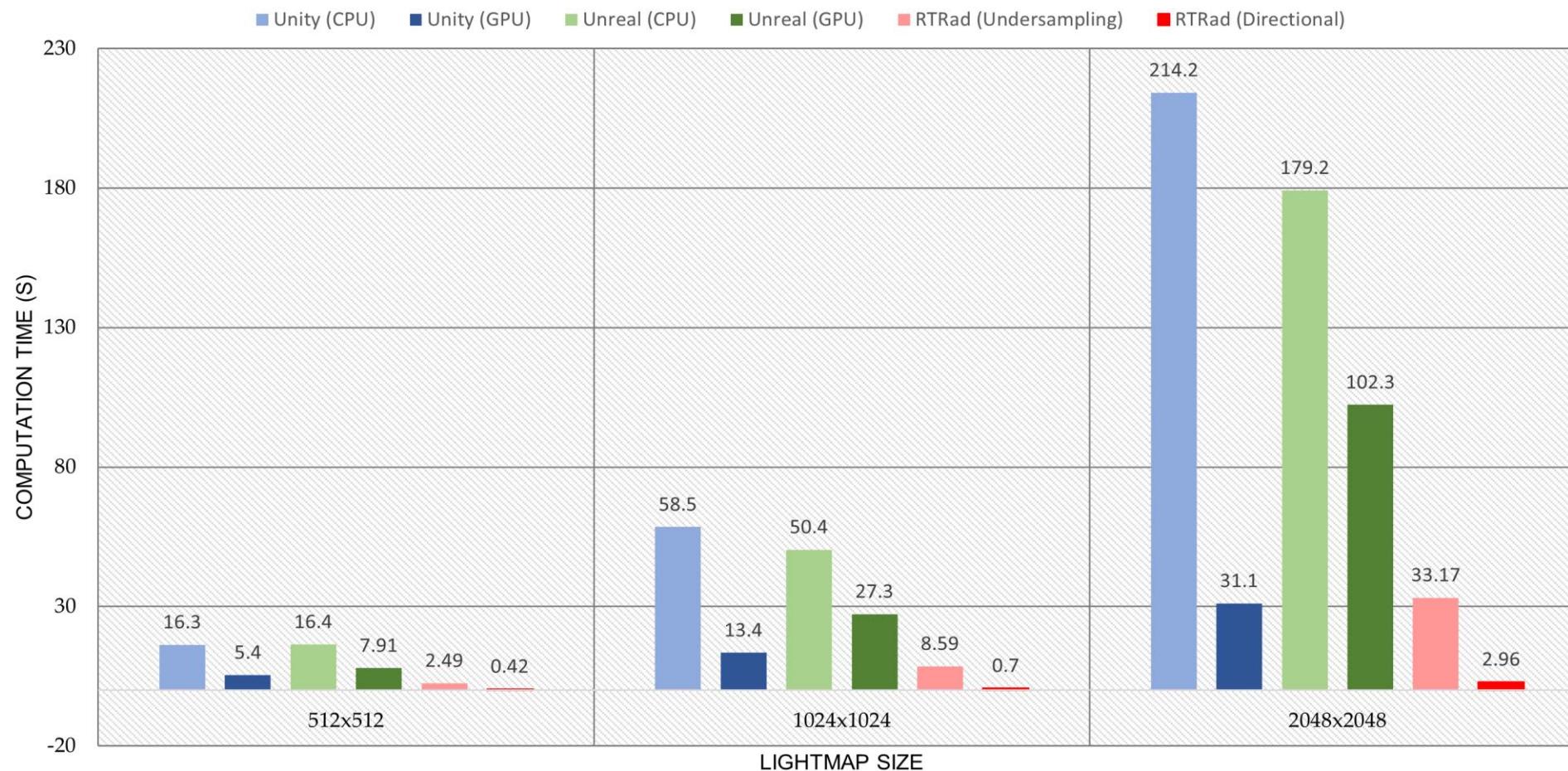
256 samples

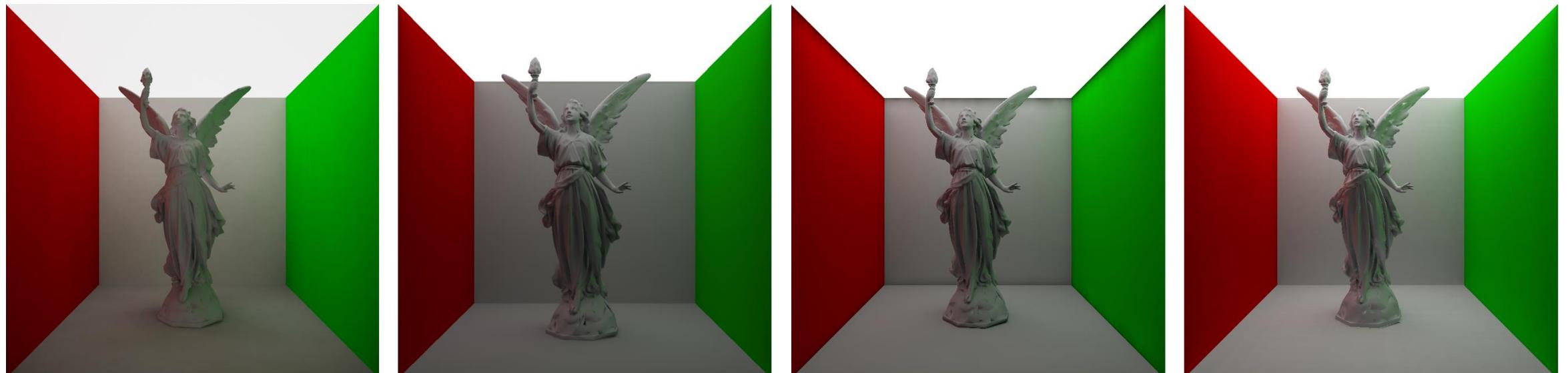


512 samples



1024 samples





Unreal Engine 5.0.3

Unity 2020.3.21

RTRad (Undersampling)

RTRad (Directional)

## **Conclusions**

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- RTX can speed up radiosity on the GPU, as well as visibility calculations at large.
- RTX can not negate radiosity's quadratic complexity.
- Specifically for RTRad:
  - Voxel-raymarching and visibility-caching are of limited usability.
  - A ratio of  $\frac{1}{128}$  between sampling window and lightmap provides balanced results in undersampling.
  - Monte-Carlo undersampling tends to produce the least artifacts.
  - 'Alpha-embedding' quadtrees in a lightmap is convenient, but not as fast.
  - Directional sampling can be tremendously fast, but does not provide the same quality and only works with larger light-sources.

## **The Future for *RTRad***

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- Direct light calculated separately.
- Rely mostly on directional sampling with directions generated from a hemicube.
- Hybrid inclusion of manually sampled patches deemed as 'important' through a quad-tree or similar.

