

R Notebook

```
printTibble <- ARL %>% ungroup() %>%
  mutate(t2 = paste(format(t2ARLmean, digits = 7), "±", format(as.numeric(format(t2ARLmean - t2ARLlwr,
    mewma = paste(format(meARLmean, digits = 7), "±", format(as.numeric(format(meARLmean - meARLlwr,
    mcusum = paste(format(mcARLmean, digits = 7), "±", format(as.numeric(format(mcARLmean - mcARLlwr,
  select(rho, copula, shift, t2, mewma, mcusum)
  print(printTibble, n = 144)
```

```
## # A tibble: 144 x 6
##   rho  copula  shift  t2          mewma          mcusum
##   <fct> <fct>   <fct>   <chr>          <chr>          <chr>
## 1 0.6   Normal  0/0     "300.347222 ± 12~ "298.764857 ± 18.~ "299.387147 ± 20~
## 2 0.6   Normal  0/0.5   "104.699835 ± 3~  " 2.433377 ± 0.~  " 1.040252 ± 0~
## 3 0.6   Normal  0/1     " 26.173685 ± 0~  " 1.011943 ± 0.~  " 1.007327 ± 0~
## 4 0.6   Normal  0/2     " 3.465635 ± 0~  " 1.001021 ± 0.~  " 1.002577 ± 0~
## 5 0.6   Normal  0/3     " 1.327446 ± 0~  " 1.000212 ± 0.~  " 1.001388 ± 0~
## 6 0.6   Normal  0.5/0.5 "129.983944 ± 5~  " 3.483435 ± 0.~  " 1.091599 ± 0~
## 7 0.6   Normal  1/1     " 36.292447 ± 0~  " 1.042887 ± 0.~  " 1.009546 ± 0~
## 8 0.6   Normal  2/2     " 5.211555 ± 0~  " 1.001474 ± 0.~  " 1.003035 ± 0~
## 9 0.6   Normal  3/3     " 1.715517 ± 0~  " 1.000403 ± 0.~  " 1.001701 ± 0~
## 10 0.2   Normal  0/0     "299.878114 ± 12~ "300.154081 ± 18.~ "299.496828 ± 21~
## 11 0.2   Normal  0/0.5   "144.159205 ± 5~  " 4.465539 ± 0.~  " 1.234239 ± 0~
## 12 0.2   Normal  0/1     " 45.263568 ± 0~  " 1.091219 ± 0.~  " 1.010741 ± 0~
## 13 0.2   Normal  0/2     " 6.870526 ± 0~  " 1.001936 ± 0.~  " 1.003621 ± 0~
## 14 0.2   Normal  0/3     " 2.109827 ± 0~  " 1.000530 ± 0.~  " 1.001928 ± 0~
## 15 0.2   Normal  0.5/0.5 "107.917053 ± 3~  " 2.346271 ± 0.~  " 1.037775 ± 0~
## 16 0.2   Normal  1/1     " 25.913006 ± 0~  " 1.010756 ± 0.~  " 1.007047 ± 0~
## 17 0.2   Normal  2/2     " 3.403819 ± 0~  " 1.000963 ± 0.~  " 1.002547 ± 0~
## 18 0.2   Normal  3/3     " 1.313192 ± 0~  " 1.000190 ± 0.~  " 1.001342 ± 0~
## 19 -0.2  Normal  0/0     "300.034199 ± 12~ "299.995930 ± 18.~ "299.161275 ± 20~
## 20 -0.2  Normal  0/0.5   "144.995632 ± 5~  " 4.389707 ± 0.~  " 1.236306 ± 0~
## 21 -0.2  Normal  0/1     " 44.438596 ± 0~  " 1.088678 ± 0.~  " 1.010991 ± 0~
## 22 -0.2  Normal  0/2     " 6.760048 ± 0~  " 1.001873 ± 0.~  " 1.003565 ± 0~
## 23 -0.2  Normal  0/3     " 2.091456 ± 0~  " 1.000573 ± 0.~  " 1.001969 ± 0~
## 24 -0.2  Normal  0.5/0.5 " 74.543223 ± 1~  " 1.469322 ± 0.~  " 1.018949 ± 0~
## 25 -0.2  Normal  1/1     " 14.354783 ± 0~  " 1.003609 ± 0.~  " 1.005225 ± 0~
## 26 -0.2  Normal  2/2     " 1.917406 ± 0~  " 1.000439 ± 0.~  " 1.001812 ± 0~
## 27 -0.2  Normal  3/3     " 1.056362 ± 0~  " 1.000044 ± 0.~  " 1.001015 ± 0~
## 28 -0.6  Normal  0/0     "299.840992 ± 12~ "298.962793 ± 18.~ "300.664447 ± 21~
## 29 -0.6  Normal  0/0.5   "111.450619 ± 4~  " 2.398246 ± 0.~  " 1.036735 ± 0~
## 30 -0.6  Normal  0/1     " 27.046563 ± 0~  " 1.011800 ± 0.~  " 1.007342 ± 0~
## 31 -0.6  Normal  0/2     " 3.528507 ± 0~  " 1.001003 ± 0.~  " 1.002522 ± 0~
## 32 -0.6  Normal  0/3     " 1.335426 ± 0~  " 1.000179 ± 0.~  " 1.001326 ± 0~
## 33 -0.6  Normal  0.5/0.5 " 34.721704 ± 0~  " 1.032854 ± 0.~  " 1.008857 ± 0~
## 34 -0.6  Normal  1/1     " 4.797069 ± 0~  " 1.001381 ± 0.~  " 1.002971 ± 0~
## 35 -0.6  Normal  2/2     " 1.084991 ± 0~  " 1.000063 ± 0.~  " 1.001051 ± 0~
## 36 -0.6  Normal  3/3     " 1.000121 ± 0~  " 1.000000 ± 0.~  " 1.000406 ± 0~
## 37 0.6   Frank   0/0     "300.257984 ± 12~ "299.127095 ± 18.~ "300.430916 ± 20~
```

##	38	0.6	Frank	0/0.5	"149.381237 ± 6~	" 2.763912 ± 0.~	" 1.047704 ± 0~
##	39	0.6	Frank	0/1	" 46.534412 ± 0~	" 1.018431 ± 0.~	" 1.007971 ± 0~
##	40	0.6	Frank	0/2	" 6.143819 ± 0~	" 1.001182 ± 0.~	" 1.002771 ± 0~
##	41	0.6	Frank	0/3	" 1.635886 ± 0~	" 1.000243 ± 0.~	" 1.001508 ± 0~
##	42	0.6	Frank	0.5/0.5	"182.162019 ± 7~	" 3.377918 ± 0.~	" 1.084148 ± 0~
##	43	0.6	Frank	1/1	" 60.487465 ± 1~	" 1.038617 ± 0.~	" 1.009383 ± 0~
##	44	0.6	Frank	2/2	" 6.942180 ± 0~	" 1.001456 ± 0.~	" 1.003062 ± 0~
##	45	0.6	Frank	3/3	" 2.037463 ± 0~	" 1.000390 ± 0.~	" 1.001710 ± 0~
##	46	0.2	Frank	0/0	"299.577814 ± 12~	"299.000417 ± 18.~	"299.859085 ± 20~
##	47	0.2	Frank	0/0.5	"146.879970 ± 5~	" 4.568323 ± 0.~	" 1.249158 ± 0~
##	48	0.2	Frank	0/1	" 47.994859 ± 0~	" 1.095327 ± 0.~	" 1.011161 ± 0~
##	49	0.2	Frank	0/2	" 7.181810 ± 0~	" 1.001899 ± 0.~	" 1.003529 ± 0~
##	50	0.2	Frank	0/3	" 2.164226 ± 0~	" 1.000598 ± 0.~	" 1.001980 ± 0~
##	51	0.2	Frank	0.5/0.5	"109.679665 ± 3~	" 2.325382 ± 0.~	" 1.034697 ± 0~
##	52	0.2	Frank	1/1	" 26.155850 ± 0~	" 1.010913 ± 0.~	" 1.007489 ± 0~
##	53	0.2	Frank	2/2	" 3.342183 ± 0~	" 1.001005 ± 0.~	" 1.002528 ± 0~
##	54	0.2	Frank	3/3	" 1.314629 ± 0~	" 1.000190 ± 0.~	" 1.001324 ± 0~
##	55	-0.2	Frank	0/0	"300.287734 ± 12~	"299.629299 ± 18.~	"297.644616 ± 20~
##	56	-0.2	Frank	0/0.5	"145.572795 ± 5~	" 4.367710 ± 0.~	" 1.217868 ± 0~
##	57	-0.2	Frank	0/1	" 47.146895 ± 0~	" 1.088765 ± 0.~	" 1.010686 ± 0~
##	58	-0.2	Frank	0/2	" 7.165227 ± 0~	" 1.001877 ± 0.~	" 1.003514 ± 0~
##	59	-0.2	Frank	0/3	" 2.159665 ± 0~	" 1.000514 ± 0.~	" 1.001917 ± 0~
##	60	-0.2	Frank	0.5/0.5	" 75.486533 ± 1~	" 1.506763 ± 0.~	" 1.019522 ± 0~
##	61	-0.2	Frank	1/1	" 15.771653 ± 0~	" 1.003625 ± 0.~	" 1.005156 ± 0~
##	62	-0.2	Frank	2/2	" 2.012572 ± 0~	" 1.000459 ± 0.~	" 1.001829 ± 0~
##	63	-0.2	Frank	3/3	" 1.064987 ± 0~	" 1.000056 ± 0.~	" 1.001014 ± 0~
##	64	-0.6	Frank	0/0	"299.146501 ± 12~	"299.171026 ± 18.~	"301.048605 ± 20~
##	65	-0.6	Frank	0/0.5	"147.680580 ± 6~	" 2.773082 ± 0.~	" 1.051122 ± 0~
##	66	-0.6	Frank	0/1	" 45.959072 ± 0~	" 1.019217 ± 0.~	" 1.007984 ± 0~
##	67	-0.6	Frank	0/2	" 6.086804 ± 0~	" 1.001199 ± 0.~	" 1.002806 ± 0~
##	68	-0.6	Frank	0/3	" 1.630720 ± 0~	" 1.000265 ± 0.~	" 1.001491 ± 0~
##	69	-0.6	Frank	0.5/0.5	" 57.803567 ± 1~	" 1.057652 ± 0.~	" 1.009960 ± 0~
##	70	-0.6	Frank	1/1	" 9.248483 ± 0~	" 1.001681 ± 0.~	" 1.003377 ± 0~
##	71	-0.6	Frank	2/2	" 1.193509 ± 0~	" 1.000072 ± 0.~	" 1.001138 ± 0~
##	72	-0.6	Frank	3/3	" 1.002716 ± 0~	" 1.000000 ± 0.~	" 1.000639 ± 0~
##	73	0.6	Clayton	0/0	"300.399242 ± 12~	"300.204832 ± 17.~	"300.421821 ± 20~
##	74	0.6	Clayton	0/0.5	"132.919898 ± 5~	" 2.595306 ± 0.~	" 1.040509 ± 0~
##	75	0.6	Clayton	0/1	" 40.980556 ± 0~	" 1.011084 ± 0.~	" 1.007560 ± 0~
##	76	0.6	Clayton	0/2	" 5.808143 ± 0~	" 1.001068 ± 0.~	" 1.002614 ± 0~
##	77	0.6	Clayton	0/3	" 1.573744 ± 0~	" 1.000198 ± 0.~	" 1.001428 ± 0~
##	78	0.6	Clayton	0.5/0.5	"164.076613 ± 6~	" 3.482281 ± 0.~	" 1.086189 ± 0~
##	79	0.6	Clayton	1/1	" 59.352965 ± 1~	" 1.050300 ± 0.~	" 1.009454 ± 0~
##	80	0.6	Clayton	2/2	" 7.380326 ± 0~	" 1.001572 ± 0.~	" 1.003195 ± 0~
##	81	0.6	Clayton	3/3	" 2.031727 ± 0~	" 1.000441 ± 0.~	" 1.001750 ± 0~
##	82	0.2	Clayton	0/0	"299.604870 ± 13~	"298.827176 ± 18.~	"298.870717 ± 20~
##	83	0.2	Clayton	0/0.5	"167.782164 ± 7~	" 4.426291 ± 0.~	" 1.221352 ± 0~
##	84	0.2	Clayton	0/1	" 53.261486 ± 1~	" 1.085998 ± 0.~	" 1.011133 ± 0~
##	85	0.2	Clayton	0/2	" 7.599629 ± 0~	" 1.001813 ± 0.~	" 1.003519 ± 0~
##	86	0.2	Clayton	0/3	" 2.209908 ± 0~	" 1.000545 ± 0.~	" 1.001907 ± 0~
##	87	0.2	Clayton	0.5/0.5	"137.759662 ± 5~	" 2.341766 ± 0.~	" 1.036150 ± 0~
##	88	0.2	Clayton	1/1	" 31.881115 ± 0~	" 1.012275 ± 0.~	" 1.007241 ± 0~
##	89	0.2	Clayton	2/2	" 3.558212 ± 0~	" 1.001019 ± 0.~	" 1.002576 ± 0~
##	90	0.2	Clayton	3/3	" 1.336681 ± 0~	" 1.000183 ± 0.~	" 1.001338 ± 0~
##	91	-0.2	Clayton	0/0	"298.751227 ± 12~	"300.166550 ± 18.~	"299.329737 ± 20~

##	92	-0.2	Clayton	0/0.5	"119.348538 ± 4~	" 4.527603 ± 0.~	" 1.247461 ± 0~
##	93	-0.2	Clayton	0/1	" 39.471415 ± 0~	" 1.093726 ± 0.~	" 1.011422 ± 0~
##	94	-0.2	Clayton	0/2	" 6.702284 ± 0~	" 1.001846 ± 0.~	" 1.003632 ± 0~
##	95	-0.2	Clayton	0/3	" 2.147602 ± 0~	" 1.000564 ± 0.~	" 1.001993 ± 0~
##	96	-0.2	Clayton	0.5/0.5	" 59.572833 ± 1~	" 1.505400 ± 0.~	" 1.019494 ± 0~
##	97	-0.2	Clayton	1/1	" 13.506629 ± 0~	" 1.003575 ± 0.~	" 1.005279 ± 0~
##	98	-0.2	Clayton	2/2	" 2.016787 ± 0~	" 1.000497 ± 0.~	" 1.001878 ± 0~
##	99	-0.2	Clayton	3/3	" 1.041943 ± 0~	" 1.000023 ± 0.~	" 1.001015 ± 0~
##	100	-0.6	Clayton	0/0	"299.305628 ± 12~	"299.947501 ± 18.~	"299.362882 ± 20~
##	101	-0.6	Clayton	0/0.5	" 99.759281 ± 3~	" 2.813770 ± 0.~	" 1.045808 ± 0~
##	102	-0.6	Clayton	0/1	" 37.892424 ± 0~	" 1.011537 ± 0.~	" 1.008062 ± 0~
##	103	-0.6	Clayton	0/2	" 7.376746 ± 0~	" 1.001165 ± 0.~	" 1.002812 ± 0~
##	104	-0.6	Clayton	0/3	" 2.152268 ± 0~	" 1.000266 ± 0.~	" 1.001543 ± 0~
##	105	-0.6	Clayton	0.5/0.5	" 42.489778 ± 0~	" 1.032370 ± 0.~	" 1.009888 ± 0~
##	106	-0.6	Clayton	1/1	" 9.949000 ± 0~	" 1.001476 ± 0.~	" 1.003192 ± 0~
##	107	-0.6	Clayton	2/2	" 1.298807 ± 0~	" 1.000000 ± 0.~	" 1.001107 ± 0~
##	108	-0.6	Clayton	3/3	" 1.000000 ± 0~	" 1.000000 ± 0.~	" 1.000675 ± 0~
##	109	0.6	Gumbel	0/0	"299.640476 ± 12~	"300.919213 ± 18.~	"298.675208 ± 20~
##	110	0.6	Gumbel	0/0.5	"139.048731 ± 5~	" 2.413139 ± 0.~	" 1.037604 ± 0~
##	111	0.6	Gumbel	0/1	" 39.322662 ± 0~	" 1.013220 ± 0.~	" 1.007459 ± 0~
##	112	0.6	Gumbel	0/2	" 4.400302 ± 0~	" 1.001052 ± 0.~	" 1.002615 ± 0~
##	113	0.6	Gumbel	0/3	" 1.429164 ± 0~	" 1.000153 ± 0.~	" 1.001348 ± 0~
##	114	0.6	Gumbel	0.5/0.5	"180.727144 ± 7~	" 3.660749 ± 0.~	" 1.104748 ± 0~
##	115	0.6	Gumbel	1/1	" 57.025477 ± 1~	" 1.043623 ± 0.~	" 1.009203 ± 0~
##	116	0.6	Gumbel	2/2	" 7.445416 ± 0~	" 1.001537 ± 0.~	" 1.003206 ± 0~
##	117	0.6	Gumbel	3/3	" 2.029755 ± 0~	" 1.000418 ± 0.~	" 1.001770 ± 0~
##	118	0.2	Gumbel	0/0	"299.908874 ± 12~	"299.403224 ± 17.~	"299.579319 ± 20~
##	119	0.2	Gumbel	0/0.5	"143.310599 ± 5~	" 4.412530 ± 0.~	" 1.217104 ± 0~
##	120	0.2	Gumbel	0/1	" 49.171943 ± 0~	" 1.090098 ± 0.~	" 1.011050 ± 0~
##	121	0.2	Gumbel	0/2	" 7.621021 ± 0~	" 1.001928 ± 0.~	" 1.003617 ± 0~
##	122	0.2	Gumbel	0/3	" 2.241693 ± 0~	" 1.000564 ± 0.~	" 1.001962 ± 0~
##	123	0.2	Gumbel	0.5/0.5	"108.570028 ± 3~	" 2.427671 ± 0.~	" 1.038699 ± 0~
##	124	0.2	Gumbel	1/1	" 29.561511 ± 0~	" 1.010952 ± 0.~	" 1.007396 ± 0~
##	125	0.2	Gumbel	2/2	" 3.903135 ± 0~	" 1.000974 ± 0.~	" 1.002529 ± 0~
##	126	0.2	Gumbel	3/3	" 1.363149 ± 0~	" 1.000203 ± 0.~	" 1.001365 ± 0~
##	127	-0.2	Gumbel	0/0	"298.673846 ± 12~	"298.761634 ± 18.~	"300.729111 ± 20~
##	128	-0.2	Gumbel	0/0.5	"140.584189 ± 5~	" 4.686835 ± 0.~	" 1.276347 ± 0~
##	129	-0.2	Gumbel	0/1	" 46.335986 ± 0~	" 1.107954 ± 0.~	" 1.011162 ± 0~
##	130	-0.2	Gumbel	0/2	" 7.158074 ± 0~	" 1.001925 ± 0.~	" 1.003591 ± 0~
##	131	-0.2	Gumbel	0/3	" 2.203777 ± 0~	" 1.000582 ± 0.~	" 1.001999 ± 0~
##	132	-0.2	Gumbel	0.5/0.5	" 89.096503 ± 2~	" 1.877834 ± 0.~	" 1.025286 ± 0~
##	133	-0.2	Gumbel	1/1	" 19.675986 ± 0~	" 1.005594 ± 0.~	" 1.006191 ± 0~
##	134	-0.2	Gumbel	2/2	" 2.583338 ± 0~	" 1.000749 ± 0.~	" 1.002229 ± 0~
##	135	-0.2	Gumbel	3/3	" 1.157949 ± 0~	" 1.000112 ± 0.~	" 1.001186 ± 0~
##	136	-0.6	Gumbel	0/0	"298.644877 ± 12~	"300.386102 ± 18.~	"299.146799 ± 20~
##	137	-0.6	Gumbel	0/0.5	"147.983769 ± 5~	" 4.721787 ± 0.~	" 1.294738 ± 0~
##	138	-0.6	Gumbel	0/1	" 46.824570 ± 0~	" 1.108033 ± 0.~	" 1.011409 ± 0~
##	139	-0.6	Gumbel	0/2	" 7.224251 ± 0~	" 1.001968 ± 0.~	" 1.003694 ± 0~
##	140	-0.6	Gumbel	0/3	" 2.216310 ± 0~	" 1.000601 ± 0.~	" 1.002008 ± 0~
##	141	-0.6	Gumbel	0.5/0.5	" 91.235535 ± 2~	" 1.891946 ± 0.~	" 1.026349 ± 0~
##	142	-0.6	Gumbel	1/1	" 20.162489 ± 0~	" 1.005854 ± 0.~	" 1.006383 ± 0~
##	143	-0.6	Gumbel	2/2	" 2.599165 ± 0~	" 1.000748 ± 0.~	" 1.002223 ± 0~
##	144	-0.6	Gumbel	3/3	" 1.160601 ± 0~	" 1.000093 ± 0.~	" 1.001173 ± 0~

```

#print(printTibble %>% arrange(rho))

for(i in rhoList) {
  tmpTibble <- ARL %>%
    filter(rho == i)
  t2plot <- tmpTibble %>%
    ggplot(aes(x = copula, y = t2ARLmean, fill = shift)) +
    geom_bar(position = "dodge", stat = "identity") +
    geom_errorbar(aes(ymin = t2ARLlwr, ymax = t2ARLupr), width = .2, position = position_dodge(.9)) +
    ggtitle(paste("Hotelling T-squared, Correlation", i))
  meplot <- tmpTibble %>%
    ggplot(aes(x = copula, y = meARLmean, fill = shift)) +
    geom_bar(position = "dodge", stat = "identity") +
    geom_errorbar(aes(ymin = meARLlwr, ymax = meARLupr), width = .2, position = position_dodge(.9)) +
    ggtitle(paste("MEWMA, Correlation", i))
  mcplot <- tmpTibble %>%
    ggplot(aes(x = copula, y = mcARLmean, fill = shift)) +
    geom_bar(position = "dodge", stat = "identity") +
    geom_errorbar(aes(ymin = mcARLlwr, ymax = mcARLupr), width = .2, position = position_dodge(.9)) +
    ggtitle(paste("MCUSUM, Correlation", i))
  print(t2plot)
  print(meplot)
  print(mcplot)
}

```













