

japan_95

March 19, 2020

```
[1]: %load_ext autoreload
      %autoreload 2
      %matplotlib inline
```

```
[2]: import pandas as pd
      import numpy as np
```

```
[3]: import sys

      sys.path.append("/disk/home/amy/rankability_toolbox")
```

```
[4]: import pyrankability
```

0.1 Analysis of the 1995 Japan with trimming

```
[5]: DATAFILE="/disk/home/amy/data/jpn2005_liot_w_trim/jpn1995_liot.csv"
```

```
[6]: SECTORSFILE="/disk/home/amy/data/jpn2005_liot_sector_name.csv"
```

```
[7]: sectors = pd.read_csv(SECTORSFILE,header=None)
      sectors = sectors[0]
      sectors
```

```
[7]: 0          Crop cultivation
      1          Livestock
      2    Agricultural services
      3          Forestry
      4          Fisheries
      ...
      97          Accommodations
      98    Cleaning, barber shops, beauty shops and publi...
      99          Other personal services
      100         Office supplies
      101    Activities not elsewhere classified
      Name: 0, Length: 102, dtype: object
```

```
[8]: D = pd.read_table(DATAFILE,sep=',',header=None)
```

```
[9]: D
```

```
[9]:
```

	0	1	2	3	4	5	6	\
0	0.023481	0.104087	0.000000	0.000000	0.000000	0.0	0.000000	
1	0.012583	0.107123	0.000000	0.000000	0.000000	0.0	0.000000	
2	0.069588	0.046472	0.000000	0.000000	0.000000	0.0	0.000000	
3	0.000000	0.000000	0.000000	0.234211	0.000000	0.0	0.000000	
4	0.000000	0.000000	0.000000	0.000000	0.049383	0.0	0.000000	
..	
97	0.000000	0.000000	0.000000	0.000000	0.000000	0.0	0.000000	
98	0.000000	0.000000	0.000000	0.000000	0.000000	0.0	0.000000	
99	0.000000	0.000000	0.000000	0.000000	0.000000	0.0	0.000000	
100	0.000000	0.000000	0.000000	0.000000	0.000000	0.0	0.000000	
101	0.020168	0.010237	0.039641	0.017655	0.019263	0.0	0.017799	

	7	8	9	...	92	93	94	95	96	\
0	0.000000	0.137335	0.054858	...	0.0	0.0	0.0	0.0	0.017944	
1	0.000000	0.092838	0.000000	...	0.0	0.0	0.0	0.0	0.000000	
2	0.000000	0.000000	0.000000	...	0.0	0.0	0.0	0.0	0.000000	
3	0.000000	0.000000	0.000000	...	0.0	0.0	0.0	0.0	0.000000	
4	0.000000	0.052294	0.000000	...	0.0	0.0	0.0	0.0	0.000000	
..	
97	0.000000	0.000000	0.000000	...	0.0	0.0	0.0	0.0	0.000000	
98	0.000000	0.000000	0.000000	...	0.0	0.0	0.0	0.0	0.000000	
99	0.000000	0.000000	0.000000	...	0.0	0.0	0.0	0.0	0.000000	
100	0.000000	0.000000	0.000000	...	0.0	0.0	0.0	0.0	0.000000	
101	0.018245	0.016881	0.013235	...	0.0	0.0	0.0	0.0	0.000000	

	97	98	99	100	101
0	0.013755	0.000000	0.0	0.0	0.0
1	0.000000	0.000000	0.0	0.0	0.0
2	0.000000	0.000000	0.0	0.0	0.0
3	0.000000	0.000000	0.0	0.0	0.0
4	0.000000	0.000000	0.0	0.0	0.0
..
97	0.000000	0.000000	0.0	0.0	0.0
98	0.000000	0.028682	0.0	0.0	0.0
99	0.000000	0.000000	0.0	0.0	0.0
100	0.000000	0.000000	0.0	0.0	0.0
101	0.000000	0.000000	0.0	0.0	0.0

[102 rows x 102 columns]

```
[10]: D.columns=sectors
```

```
[11]: D.index=sectors
```

```
[12]: D.isnull().sum()
```

```
[12]: 0
      Crop cultivation          0
      Livestock                0
      Agricultural services    0
      Forestry                 0
      Fisheries                0
      ..
      Accommodations          0
      Cleaning, barber shops, beauty shops and public baths 0
      Other personal services  0
      Office supplies          0
      Activities not elsewhere classified 0
      Length: 102, dtype: int64
```

```
[13]: D.dtypes
```

```
[13]: 0
      Crop cultivation          float64
      Livestock                float64
      Agricultural services    float64
      Forestry                 float64
      Fisheries                float64
      ..
      Accommodations          float64
      Cleaning, barber shops, beauty shops and public baths float64
      Other personal services  float64
      Office supplies          float64
      Activities not elsewhere classified float64
      Length: 102, dtype: object
```

0.2 Run the lp solver

```
[14]: k,details = pyrankability.lop.lp(D.values)
```

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```
[98]: k
```

```
[98]: 46.85598382000097
```

0.3 Run the bilp solver and report up to 50 unique solutions

```
[ ]: k_bilp,details_bilp = pyrankability.lop.bilp(D.  
    ↪values,max_solutions=1,num_random_restarts=50)
```

```
[99]: k_bilp
```

```
[99]: 46.855983820000006
```

```
[100]: len(details_bilp['P'])
```

```
[100]: 51
```

0.4 What is saved in the details

In case we want, I have stored the first P found, all the P found, the first x found, the objective values each time, and the x matrices each time

```
[101]: details_bilp.keys()
```

```
[101]: dict_keys(['Pfirst', 'P', 'x', 'objs', 'xs'])
```

0.5 Important to check

It is important to check and make sure all solutions are optimal. Running this check helped me sort out a bug or two.

```
[102]: objs=[]  
    for perm in details_bilp['P']:  
        objs.append(pyrankability.lop.objective_count_perm(D.values,perm))
```

```
[104]: pd.Series(objs)
```

```
[104]: 0      46.855984  
      1      46.855984  
      2      46.855984  
      3      46.855984  
      4      46.855984  
      5      46.855984  
      6      46.855984  
      7      46.855984  
      8      46.855984  
      9      46.855984  
     10      46.855984  
     11      46.855984
```

12	46.855984
13	46.855984
14	46.855984
15	46.855984
16	46.855984
17	46.855984
18	46.855984
19	46.855984
20	46.855984
21	46.855984
22	46.855984
23	46.855984
24	46.855984
25	46.855984
26	46.855984
27	46.855984
28	46.855984
29	46.855984
30	46.855984
31	46.855984
32	46.855984
33	46.855984
34	46.855984
35	46.855984
36	46.855984
37	46.855984
38	46.855984
39	46.855984
40	46.855984
41	46.855984
42	46.855984
43	46.855984
44	46.855984
45	46.855984
46	46.855984
47	46.855984
48	46.855984
49	46.855984
50	46.855984

dtype: float64

0.6 Now let's put the unique solutions in a Pandas dataframe

```
[105]: P_unique = list(set(details_bilp['P']))
P_df = pd.DataFrame(P_unique)
P_df
```

```
[105]:
```

	0	1	2	3	4	5	6	7	8	9	...	92	93	94	95	\
0	94	72	73	71	93	88	92	7	27	67	...	9	86	96	66	
1	94	72	73	71	93	88	92	7	27	67	...	52	56	61	49	
2	94	72	73	71	93	88	92	7	27	67	...	97	47	100	52	
3	94	72	73	71	93	92	88	7	27	67	...	53	52	47	100	
4	94	72	73	71	93	88	92	7	27	67	...	78	68	89	56	
5	94	72	73	71	93	92	88	7	27	67	...	74	99	53	47	
6	94	72	73	71	93	92	88	7	27	67	...	69	53	45	79	
7	94	72	73	71	93	88	92	7	27	67	...	9	31	96	47	
8	94	72	73	71	93	88	92	7	27	67	...	86	100	66	49	
9	94	72	73	71	93	88	92	7	27	67	...	69	70	86	96	
10	94	72	73	71	93	88	92	7	27	67	...	65	98	89	47	
11	94	72	73	71	93	92	88	7	27	67	...	79	52	56	45	
12	94	72	73	71	93	92	88	7	27	67	...	78	75	57	49	
13	94	72	73	71	93	92	88	7	27	67	...	75	70	86	57	
14	94	72	73	71	93	92	88	7	27	67	...	78	75	70	97	
15	94	72	73	71	93	92	88	7	27	67	...	86	9	53	31	
16	94	72	73	71	93	92	88	7	27	67	...	98	89	100	52	
17	94	72	73	71	93	88	92	7	27	67	...	57	61	31	87	
18	94	72	73	71	93	92	88	7	27	67	...	75	70	99	9	
19	94	72	73	71	93	92	88	7	27	67	...	96	65	56	75	
20	94	72	73	71	93	88	92	7	27	67	...	89	87	78	49	
21	94	72	73	71	93	88	92	7	27	67	...	11	70	86	79	
22	94	72	73	71	93	88	92	7	27	67	...	89	49	9	97	
23	94	72	73	71	93	88	92	7	27	67	...	69	9	97	96	
24	94	72	73	71	93	88	92	7	27	67	...	86	52	99	56	
25	94	72	73	71	93	92	88	7	27	67	...	53	78	74	98	
26	94	72	73	71	93	88	92	7	27	67	...	51	78	11	74	
27	94	72	73	71	93	88	92	7	27	67	...	53	69	96	98	
28	94	72	73	71	93	92	88	7	27	67	...	99	11	56	61	
29	94	72	73	71	93	92	88	7	27	67	...	13	90	69	98	
30	94	72	73	71	93	92	88	7	27	67	...	13	90	69	98	
31	94	72	73	71	93	88	92	7	27	67	...	96	53	86	100	
32	94	72	73	71	93	88	92	7	27	67	...	61	56	98	89	
33	94	72	73	71	93	92	88	7	27	67	...	70	86	97	51	
34	94	72	73	71	93	92	88	7	27	67	...	84	69	98	89	
35	94	72	73	71	93	92	88	7	27	67	...	89	49	96	66	
36	94	72	73	71	93	88	92	7	27	67	...	51	11	86	63	
37	94	72	73	71	93	92	88	7	27	67	...	47	100	68	78	
38	94	72	73	71	93	92	88	7	27	67	...	60	89	75	78	
39	94	72	73	71	93	92	88	7	27	67	...	49	57	52	98	

40	94	72	73	71	93	92	88	7	27	67	...	66	96	56	98
41	94	72	73	71	93	92	88	7	27	67	...	99	9	96	11
42	94	72	73	71	93	88	92	7	27	67	...	86	47	57	100
43	94	72	73	71	93	88	92	7	27	67	...	86	66	87	52
44	94	72	73	71	93	92	88	7	27	67	...	66	61	86	100
45	94	72	73	71	93	92	88	7	27	67	...	66	56	87	65
46	94	72	73	71	93	92	88	7	27	67	...	47	97	96	100
47	94	72	73	71	93	88	92	7	27	67	...	60	75	70	86
48	94	72	73	71	93	92	88	7	27	67	...	66	74	87	61
49	94	72	73	71	93	88	92	7	27	67	...	86	65	63	47
50	94	72	73	71	93	88	92	7	27	67	...	52	66	65	51

	96	97	98	99	100	101
0	61	97	89	31	51	68
1	51	97	45	66	99	31
2	79	56	96	51	11	89
3	56	51	49	45	31	11
4	96	75	70	86	97	49
5	100	66	68	56	78	97
6	96	74	98	89	100	97
7	97	74	11	100	49	45
8	56	65	11	57	53	96
9	98	89	31	100	97	74
10	86	100	52	56	97	96
11	57	75	70	97	86	99
12	9	96	70	97	86	53
13	89	31	56	47	97	100
14	86	96	51	56	99	66
15	96	97	52	56	100	65
16	56	86	11	45	61	53
17	68	75	70	100	97	86
18	97	96	86	63	87	65
19	70	86	63	68	99	97
20	96	57	61	100	66	74
21	9	97	74	96	100	89
22	96	45	66	52	56	31
23	98	89	53	63	78	66
24	78	66	79	87	68	11
25	31	66	9	89	96	97
26	47	100	68	79	53	49
27	11	86	74	97	51	89
28	51	78	97	45	87	74
29	9	96	57	89	86	97
30	53	89	56	9	96	97
31	51	56	79	61	97	57
32	97	96	53	45	65	51
33	99	68	65	66	52	56

34	96	53	100	66	97	56
35	74	57	47	100	51	78
36	96	89	49	56	61	79
37	11	96	57	66	79	45
38	9	96	61	70	86	97
39	89	63	11	96	56	45
40	31	89	100	79	61	68
41	60	78	75	70	97	86
42	97	61	68	52	56	89
43	56	99	89	61	65	31
44	11	31	96	87	99	78
45	45	47	100	53	63	68
46	66	53	98	89	56	45
47	78	97	87	52	56	63
48	89	68	52	65	56	53
49	100	96	89	31	11	68
50	31	99	45	49	89	56

[51 rows x 102 columns]

```
[117]: P_series=P_df.T.stack()
```

```
[124]: pos_df = P_series.index.to_frame()
pos_df.columns=["Position","Solution Index"]
pos_df["Item"] = P_series
pos_df.set_index("Solution Index",inplace=True)
pos_df
```

```
[124]:
```

	Position	Item
Solution Index		
0	0	94
1	0	94
2	0	94
3	0	94
4	0	94
...
46	101	45
47	101	63
48	101	53
49	101	68
50	101	56

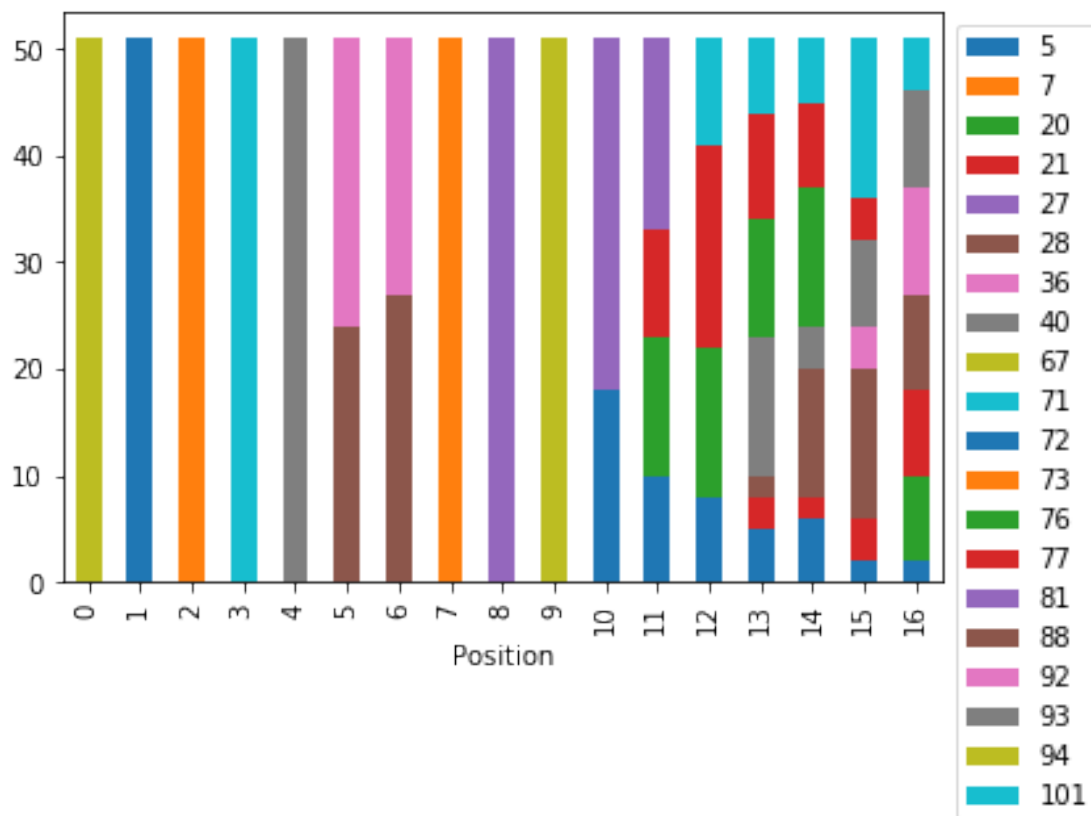
[5202 rows x 2 columns]

0.7 Visualizing some of the top items

In the graph below the x axis is the rank or position in the solutions. I'm keeping it simple and showing the top 16. What I would point out is that things like items 77 and 21 (unfortunately they are both red, so I need more colors). I think that constitutes a lot of movement. If I've got everything aligned correct 77 and 21 were associated with Water transport and Petrochemical basic products. Item 5 is another interesting case that goes from position 10 to position 16. Item 5 is Metallic ores. So the big question is so what? Is this the breakthrough reason for our approach? Would anyone be interested in these alternative solutions?

```
[164]: graph_df = pos_df.groupby("Position")["Item"].value_counts().to_frame()
graph_df.columns = ["Count"]
graph_df = graph_df.head(50).reset_index().set_index("Position").
↳pivot(columns="Item").fillna(0)
graph_df.columns = [v[1] for v in graph_df.columns]
graph_df.plot.bar(stacked=True).legend(bbox_to_anchor=(1, 1))
```

```
[164]: <matplotlib.legend.Legend at 0x7f4d97120d68>
```



```
[168]: D.index[77],D.index[101],D.index[21],D.index[5]
```

```
[168]: ('Water transport',
        'Activities not elsewhere classified',
        'Petrochemical basic products',
        'Metallic ores')
```

0.8 Save the results for later

```
[106]: #!/mkdir /disk/home/amy/results/
```

```
[107]: import joblib
joblib.dump(details_bilp, "/disk/home/amy/results/japan_95_details_bilp.joblib.
↪z")
```

```
[107]: ['/disk/home/amy/results/japan_95_details_bilp.joblib.z']
```

0.9 Below is analysis of the lp results

```
[111]: Xstar = pyrankability.lop.
↪threshold_x(details['x'], lower_cut=1e-3, upper_cut=1-1e-3)

record_ixs = []
r = np.sum(Xstar, axis=1)
ixs = np.argsort(r)
record_ixs.append(ixs)
Xstar_rowsum = Xstar[np.ix_(ixs, ixs)]

r = np.sum(details_bilp['x'], axis=1)
ixs = np.argsort(r)
record_ixs.append(ixs)
Xstar_bilp = Xstar[np.ix_(ixs, ixs)]

labels = ["A. BILP by rowsum", "B. Ordered by rowsum"]
Xstars = [Xstar_bilp, Xstar_rowsum]
```

```
[112]: import altair as alt
alt.data_transformers.disable_max_rows()

all_df = pd.DataFrame(columns=["i", "j", "x", "Label", "oi", "oj"])
for ix, Xstar in enumerate(Xstars):
    x = pd.DataFrame(Xstar)
    df = x.stack().reset_index()
    df.columns = ["i", "j", "x"]
    df["oi"] = df["i"].copy()
    df["oj"] = df["j"].copy()
```

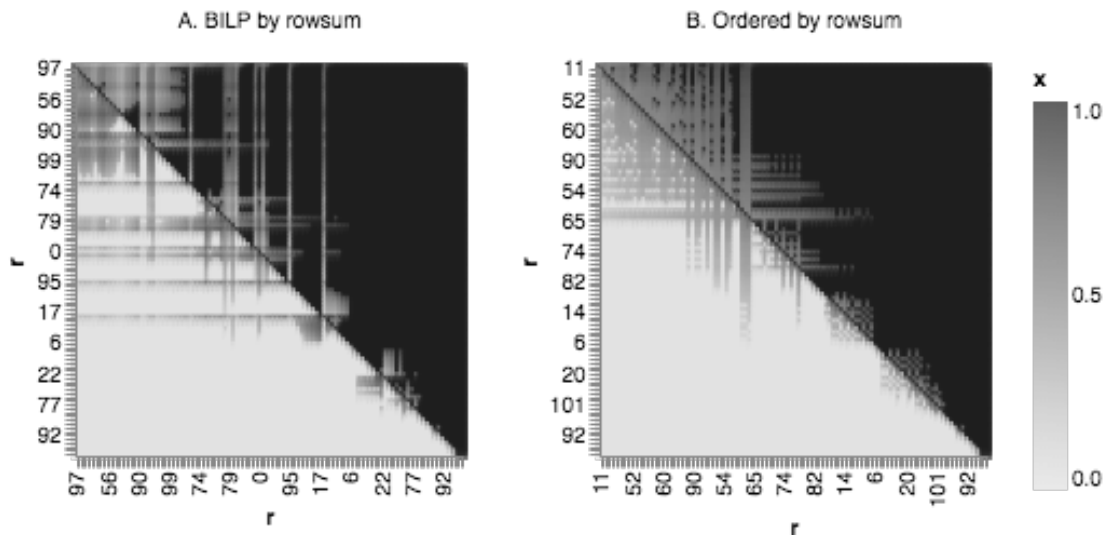
```

df["i"] = record_ixs[ix][df["i"]]
df["j"] = record_ixs[ix][df["j"]]
df["Label"] = labels[ix]
all_df = all_df.append(df)

#all_df = all_df.loc[(all_df.x != 0) & (all_df.x != 1)]
alt.Chart(all_df).mark_square().encode(
    x=alt.X(
        'i:N',
        axis=alt.Axis(labelOverlap="parity"),
        title="r",
        sort=alt.EncodingSortField(field="oi",order="ascending") # The order to
→sort in
    ),
    y=alt.Y(
        'j:N',
        axis=alt.Axis(labelOverlap="parity"),
        title="r",
        sort=alt.EncodingSortField(field="oj",order="ascending") # The order to
→sort in
    ),
    color=alt.Color("x",scale=alt.Scale(scheme='greys'))
).properties(
    width=180,
    height=180
).facet(
    column=alt.Column("Label:N", title=None)
).resolve_scale(x='independent',y='independent')

```

[112]:



```
[114]: pd.Series(D.columns[record_ixs[0]])
```

```
[114]: 0                      Accommodations
1      Medical service, health, social security and n...
2                      Eating and drinking places
3                      Public administration
4      Cleaning, barber shops, beauty shops and publi...
...
97                      Repair of motor vehicles and machine
98                      Commerce
99      Real estate agencies and rental services
100                     Finance and insurance
101                     Other business services
Name: 0, Length: 102, dtype: object
```

0.10 Still in development

This is still in development for this size.

```
[26]: # P,info = pyrankability.lop.find_P_from_x(D.values,k,details)
```

```
Going to loop for 2.0
Going to loop for 4194304.0
Going to loop for 524288.0
Going to loop for 2.4049076047604052e+111
```

```
KeyboardInterrupt                                Traceback (most recent call
last)

<ipython-input-26-9668fe832127> in <module>
----> 1 P,info = pyrankability.lop.find_P_from_x(D.
values,k,details,lower_cut=0.4,upper_cut=1-0.4)

~/rankability_toolbox/pyrankability/lop.py in find_P_from_x(D, k,
details, lower_cut, upper_cut)
203         Xsub = np.round(new_details['x'])
204         Xsub[np.ix_(group,group)] = Xstar[np.ix_(group,group)]
--> 205         obj_sub, permutations_sub =
objective_count(Dordered,Dordered[np.ix_(group,group)],Xsub,k,group)
206         perm_iters.append((group[0],permutations_sub))
207         permutations = generate_perms(perm_iters)
```

```

~/rankability_toolbox/pyrankability/lop.py in objective_count(Dordered,
↳D, Xstar, min_value, group)
    267         return min_value, Xsub_min_value, frac_ixs_min_value
    268
--> 269     results = Parallel(n_jobs=cpu_count)(delayed(compute)(init_seq)
↳for init_seq in init_seqs)
    270     # combine
    271     #min_value = np.Inf

/data/env/lib/python3.6/site-packages/joblib/parallel.py in
↳__call__(self, iterable)
    1014
    1015         with self._backend.retrieval_context():
-> 1016             self.retrieve()
    1017             # Make sure that we get a last message telling us we are
↳done
    1018             elapsed_time = time.time() - self._start_time

/data/env/lib/python3.6/site-packages/joblib/parallel.py in
↳retrieve(self)
    906         try:
    907             if getattr(self._backend, 'supports_timeout', False):
--> 908                 self._output.extend(job.get(timeout=self.
↳timeout))
    909             else:
    910                 self._output.extend(job.get())

/data/env/lib/python3.6/site-packages/joblib/_parallel_backends.py in
↳wrap_future_result(future, timeout)
    552         AsyncResults.get from multiprocessing."""
    553         try:
--> 554             return future.result(timeout=timeout)
    555         except LokyTimeoutError:
    556             raise TimeoutError()

/usr/lib/python3.6/concurrent/futures/_base.py in result(self, timeout)
    425         return self.__get_result()
    426
--> 427         self._condition.wait(timeout)
    428
    429         if self._state in [CANCELLED, CANCELLED_AND_NOTIFIED]:

```

```

        /usr/lib/python3.6/threading.py in wait(self, timeout)
    293         try:      # restore state no matter what (e.g.,
KeyboardInterrupt)
    294             if timeout is None:
--> 295                 waiter.acquire()
    296                 gotit = True
    297             else:

KeyboardInterrupt:

```