

# Routing Algorithms

- IP v6
- Routing algorithms
  - Link state
  - Distance Vector

# IPv6

- ❖ **Initial motivation:** 32-bit address space soon to be completely allocated.
- ❖ **Additional motivation:**
  - header format helps speed processing/forwarding
  - header changes to facilitate QoS

## **IPv6 datagram format:**

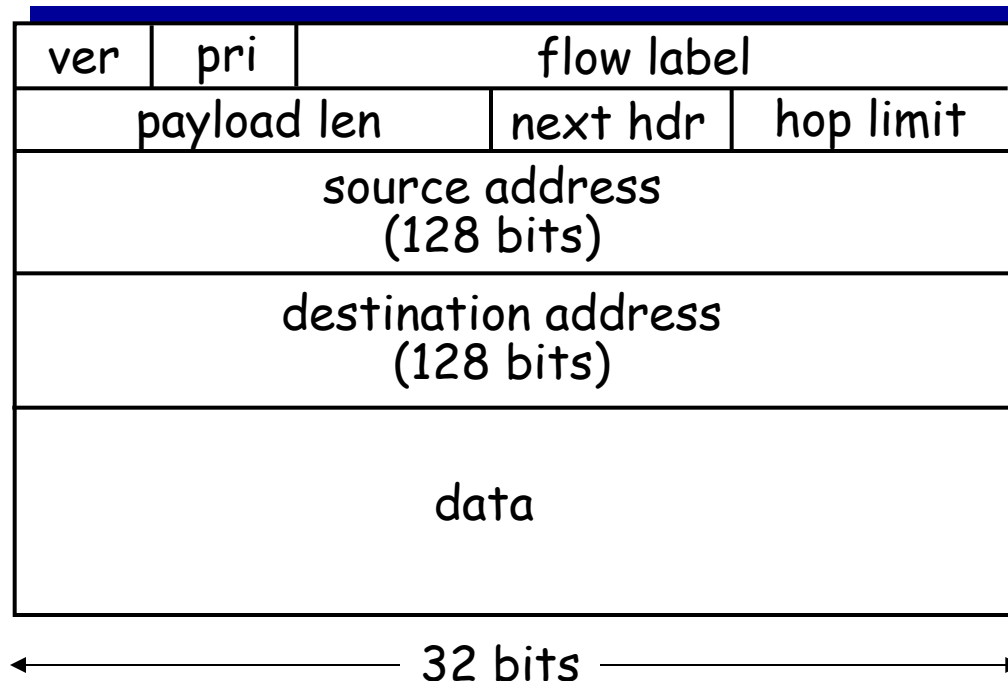
- fixed-length 40 byte header
- no fragmentation allowed

# IPv6 Header (Cont)

*Priority:* identify priority among datagrams in flow

*Flow Label:* identify datagrams in same "flow."  
(concept of "flow" not well defined).

*Next header:* identify upper layer protocol for data



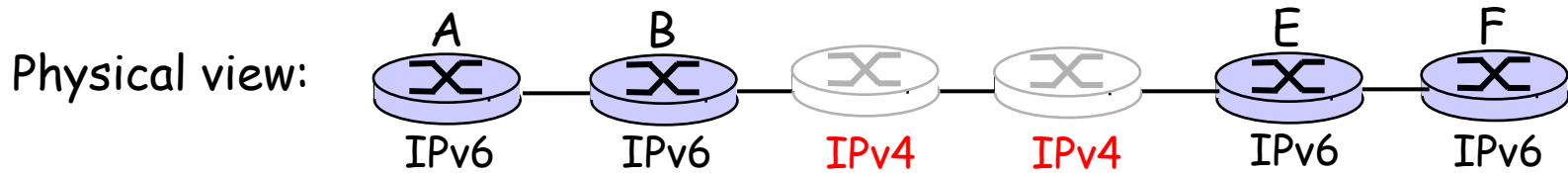
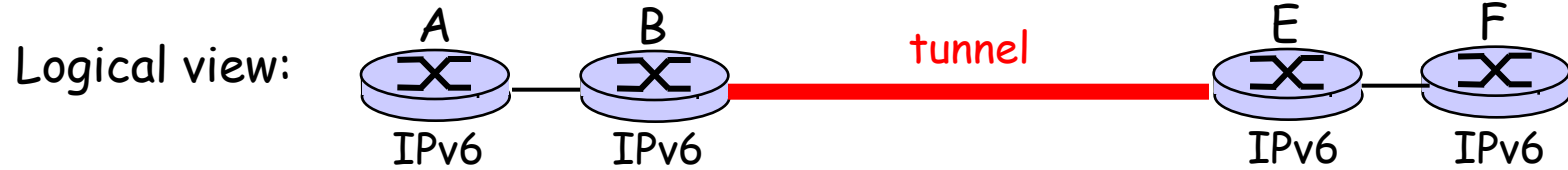
# Other Changes from IPv4

- ❖ *Checksum*: removed entirely to reduce processing time at each hop
- ❖ *Options*: allowed, but outside of header, indicated by "Next Header" field
- ❖ *ICMPv6*: new version of ICMP
  - additional message types, e.g. "Packet Too Big"
  - multicast group management functions

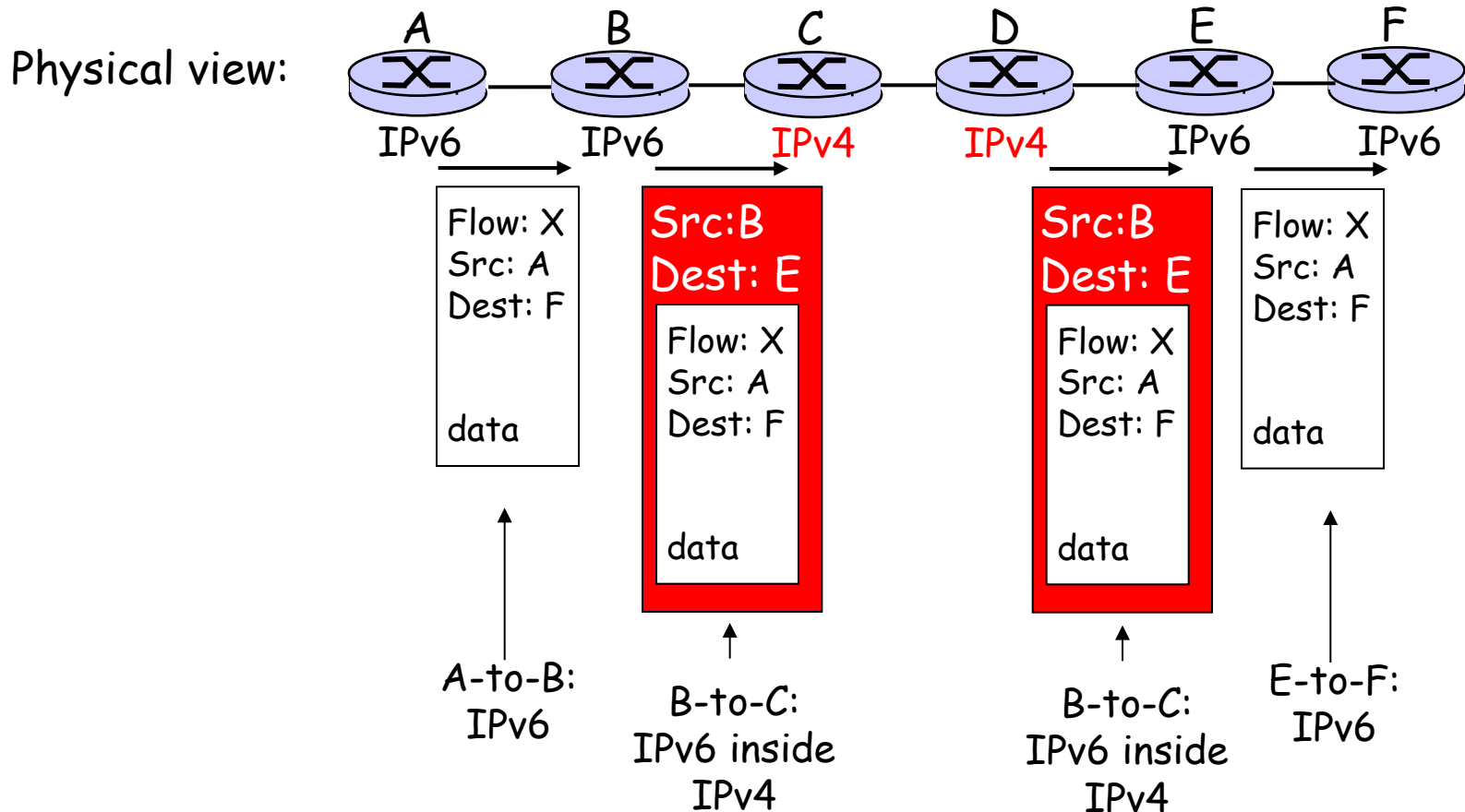
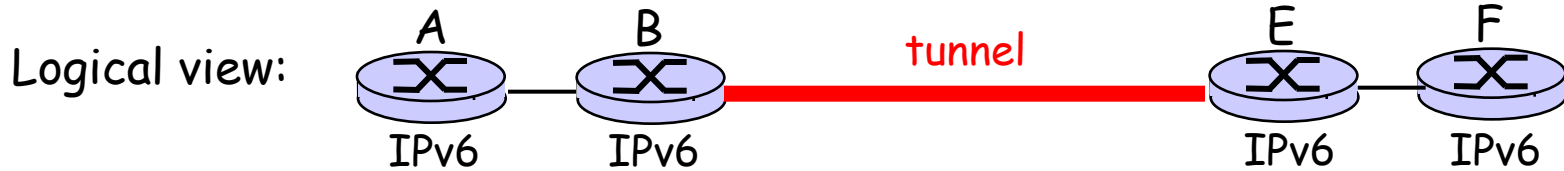
# Transition From IPv4 To IPv6

- ❖ Not all routers can be upgraded simultaneous
  - no “flag days”
  - How will the network operate with mixed IPv4 and IPv6 routers?
- ❖ *Tunneling*: IPv6 carried as payload in IPv4 datagram among IPv4 routers

# Tunneling



# Tunneling



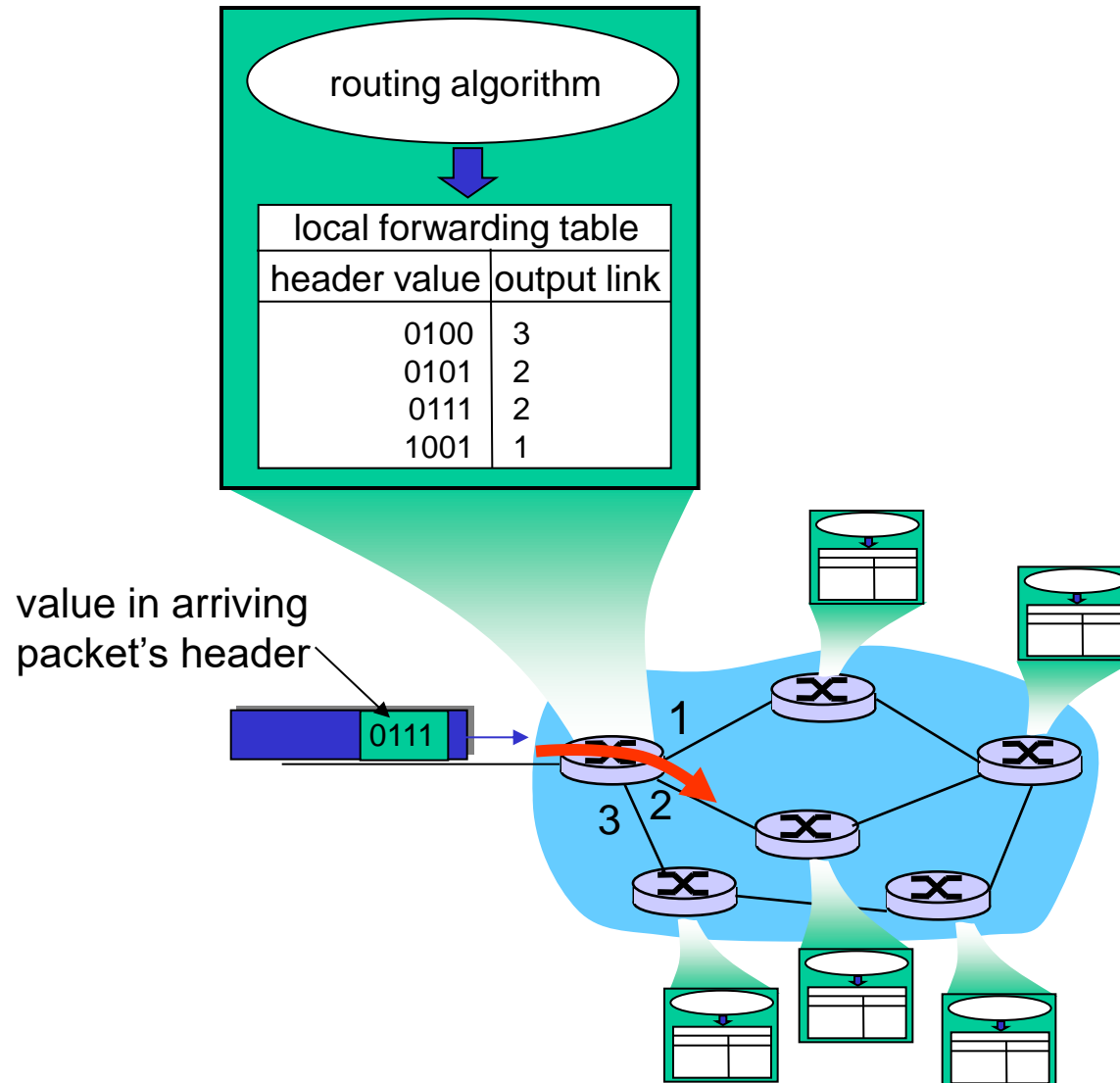
# Network Layer

## Routing algorithms

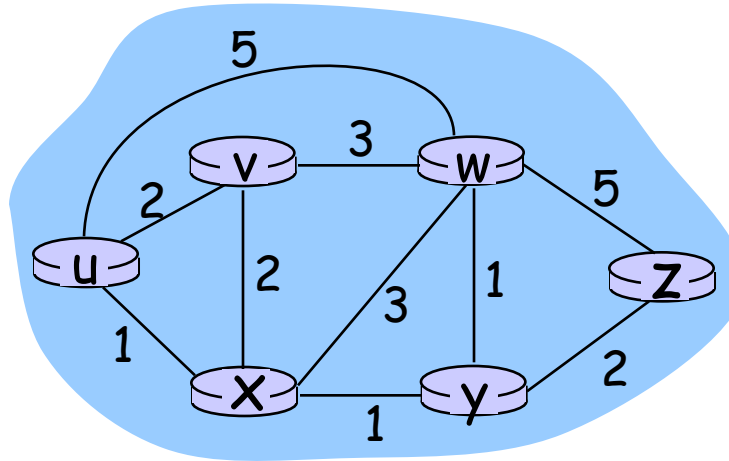
- Link state
- Distance Vector



# Interplay between routing, forwarding



# Graph abstraction



Graph:  $G = (N, E)$

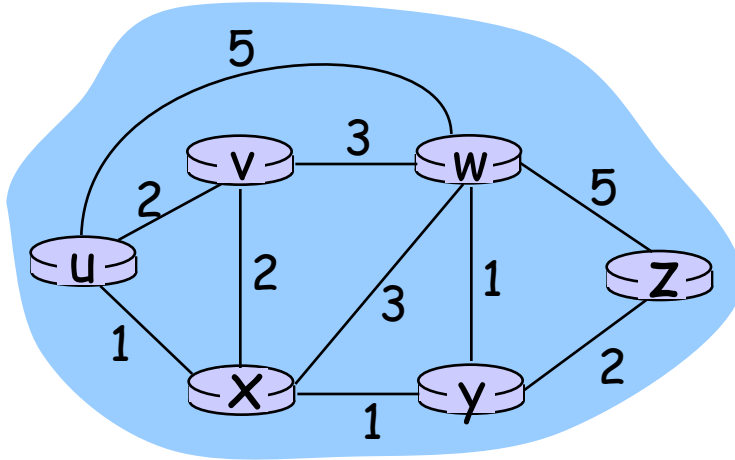
$N$  = set of routers =  $\{ u, v, w, x, y, z \}$

$E$  = set of links =  $\{ (u,v), (u,x), (v,x), (v,w), (x,w), (x,y), (w,y), (w,z), (y,z) \}$

Remark: Graph abstraction is useful in other network contexts

Example: P2P, where  $N$  is set of peers and  $E$  is set of TCP connections

# Graph abstraction: costs



- $c(x,x')$  = cost of link  $(x,x')$ 
  - e.g.,  $c(w,z) = 5$
- cost could always be 1, or inversely related to bandwidth, or inversely related to congestion

Cost of path  $(x_1, x_2, x_3, \dots, x_p) = c(x_1, x_2) + c(x_2, x_3) + \dots + c(x_{p-1}, x_p)$

Question: What's the least-cost path between u and z ?

Routing algorithm: algorithm that finds least-cost path

# Routing Algorithm classification

## Global or decentralized information?

### Global:

- ❖ all routers have complete topology, link cost info
- ❖ "link state" algorithms

### Decentralized:

- ❖ router knows physically-connected neighbors, link costs to neighbors
- ❖ iterative process of computation, exchange of info with neighbors
- ❖ "distance vector" algorithms

## Static or dynamic?

### Static:

- ❖ routes change slowly over time

### Dynamic:

- ❖ routes change more quickly
  - periodic update
  - in response to link cost changes

# Network Layer

## Routing algorithms

- Link state
- Distance Vector

# A Link-State Routing Algorithm

## Dijkstra's algorithm

- ❖ net topology, link costs known to all nodes
  - accomplished via "link state broadcast"
  - all nodes have same info
- ❖ computes least cost paths from one node ('source') to all other nodes
  - gives *forwarding table* for that node
- ❖ iterative: after k iterations, know least cost path to k dest.'s

## Notation:

- ❖  $c(x,y)$ : link cost from node x to y;  $= \infty$  if not direct neighbors
- ❖  $D(v)$ : current value of cost of path from source to dest. v
- ❖  $p(v)$ : predecessor node along path from source to v
- ❖  $N'$ : set of nodes whose least cost path definitively known

# Dijkstra's Algorithm

1 **Initialization:**

2  $N' = \{u\}$

3 for all nodes  $v$

4 if  $v$  adjacent to  $u$

5 then  $D(v) = c(u,v)$

6 else  $D(v) = \infty$

7

8 **Loop**

9 find  $w$  not in  $N'$  such that  $D(w)$  is a minimum

10 add  $w$  to  $N'$

11 update  $D(v)$  for all  $v$  adjacent to  $w$  and not in  $N'$  :

12  $D(v) = \min( D(v), D(w) + c(w,v) )$

13 /\* new cost to  $v$  is either old cost to  $v$  or known

14 shortest path cost to  $w$  plus cost from  $w$  to  $v$  \*/

15 **until all nodes in  $N'$**

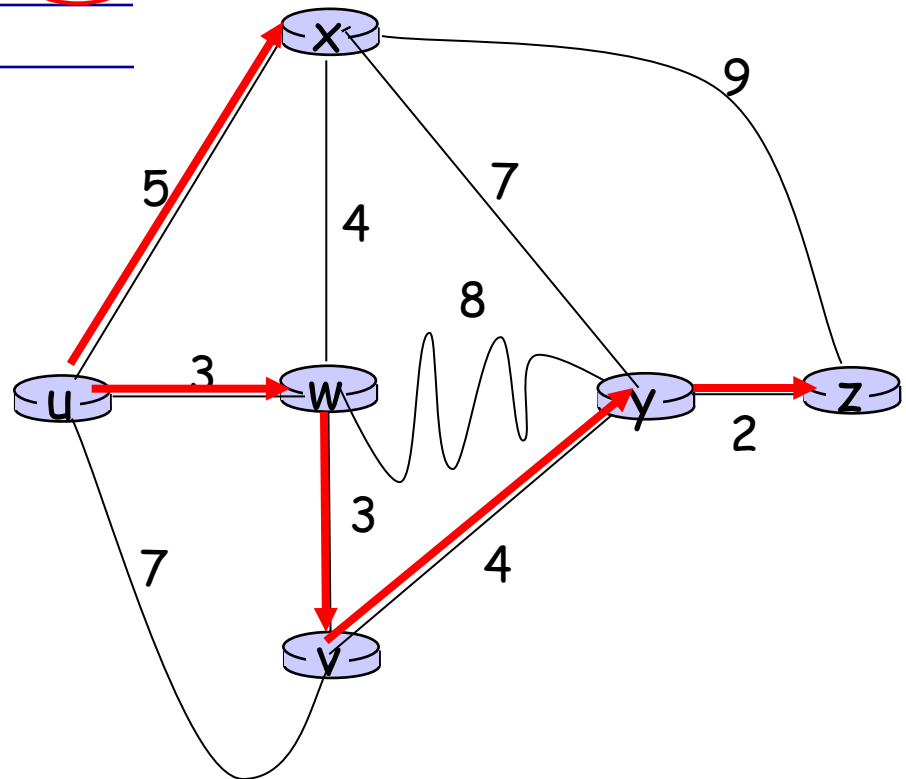


# Dijkstra's algorithm: example

Step	N'	D(v) p(v)	D(w) p(w)	D(x) p(x)	D(y) p(y)	D(z) p(z)
0	u	7,u	3,u	5,u	$\infty$	$\infty$
1	uw	6,w		5,u	11,w	$\infty$
2	uwx	6,w			11,w	14,x
3	uwxv				10,v	14,x
4	uwxvy					12,y
5	uwxvyz					

## Notes:

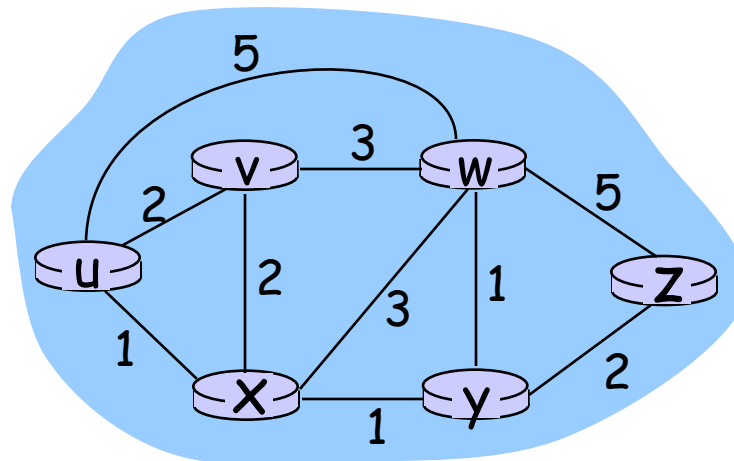
- ❖ construct shortest path tree by tracing predecessor nodes
- ❖ ties can exist (can be broken arbitrarily)

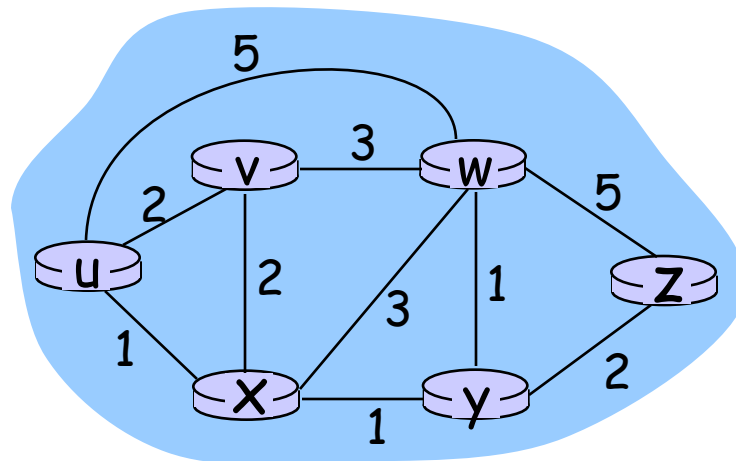




# Dijkstra's algorithm: another example

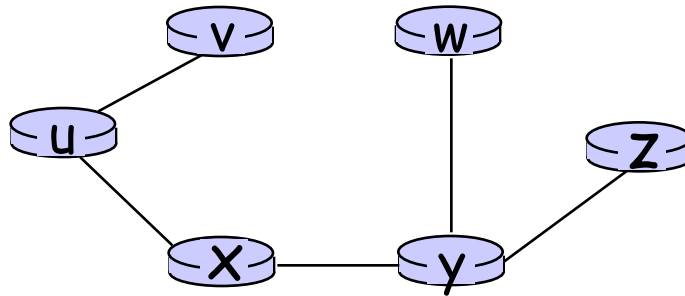
Step	N'	D(v),p(v)	D(w),p(w)	D(x),p(x)	D(y),p(y)	D(z),p(z)
0	u	2,u	5,u	1,u	$\infty$	$\infty$
1	ux	2,u	4,x		2,x	$\infty$
2	uxy	2,u	3,y			4,y
3	uxyv		3,y			4,y
4	uxyvw					4,y
5	uxyvwz					





# Dijkstra's algorithm: example (2)

Resulting shortest-path tree from u:



Resulting forwarding table in u:

destination	link
v	(u,v)
x	(u,x)
y	(u,x)
w	(u,x)
z	(u,x)

# Network Layer

## Routing algorithms

- Link state
- Distance Vector

# Distance Vector Algorithm

## Bellman-Ford Equation (dynamic programming)

Define

$d_x(y) :=$  cost of least-cost path from  $x$  to  $y$

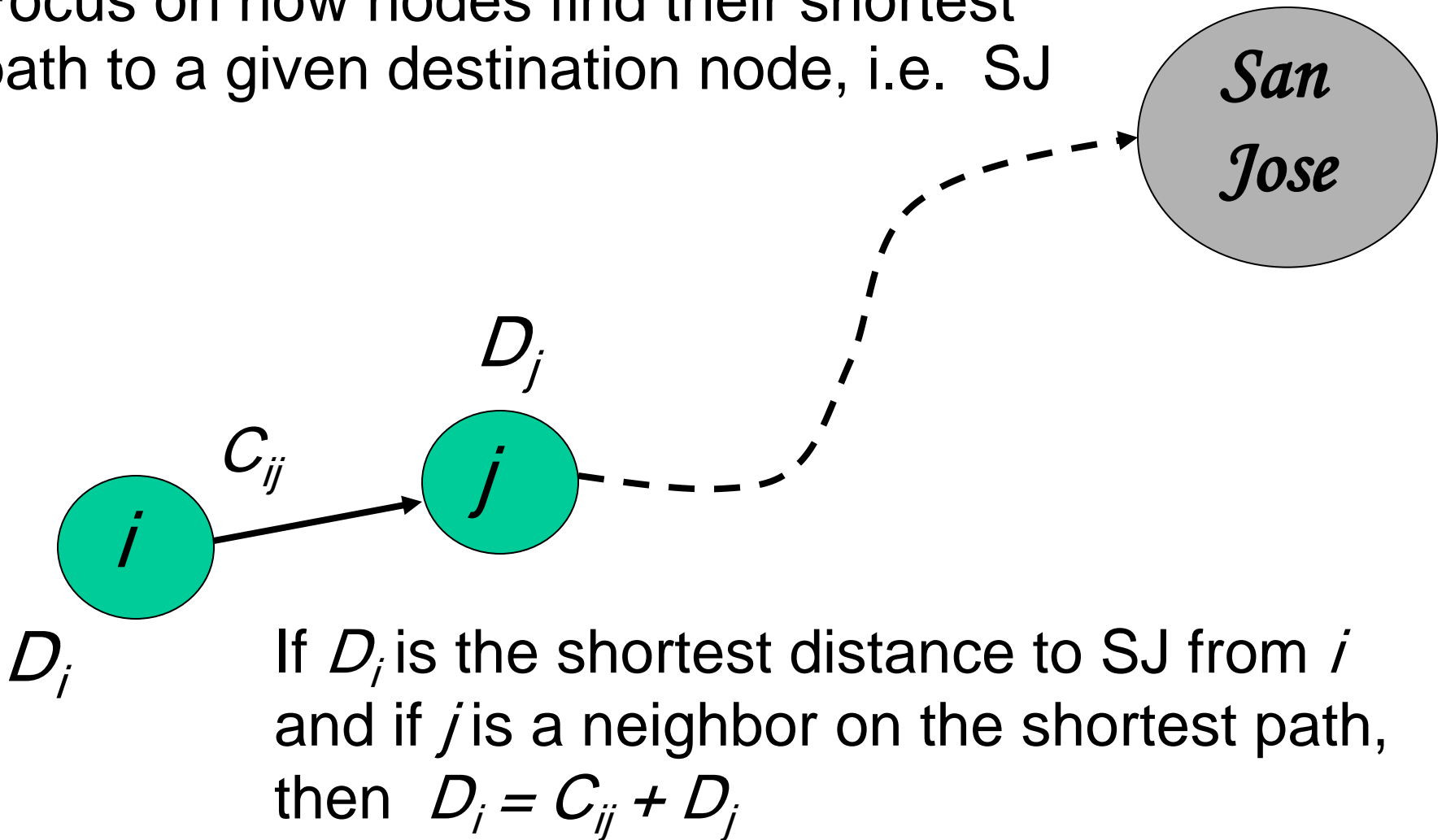
Then

$$d_x(y) = \min_v \{c(x,v) + d_v(y)\}$$

where min is taken over all neighbors  $v$  of  $x$

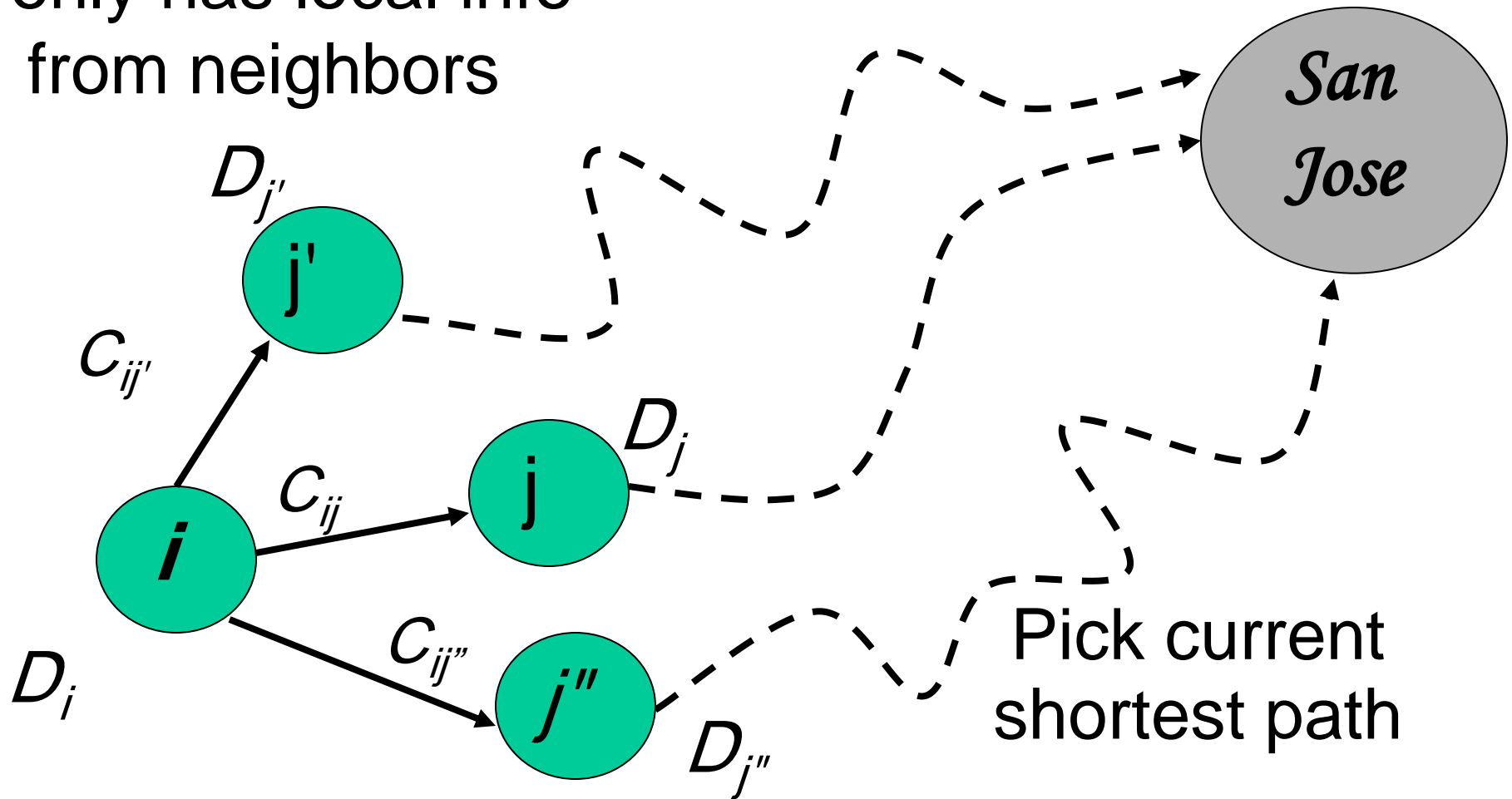
# Shortest Path to SJ

Focus on how nodes find their shortest path to a given destination node, i.e. SJ

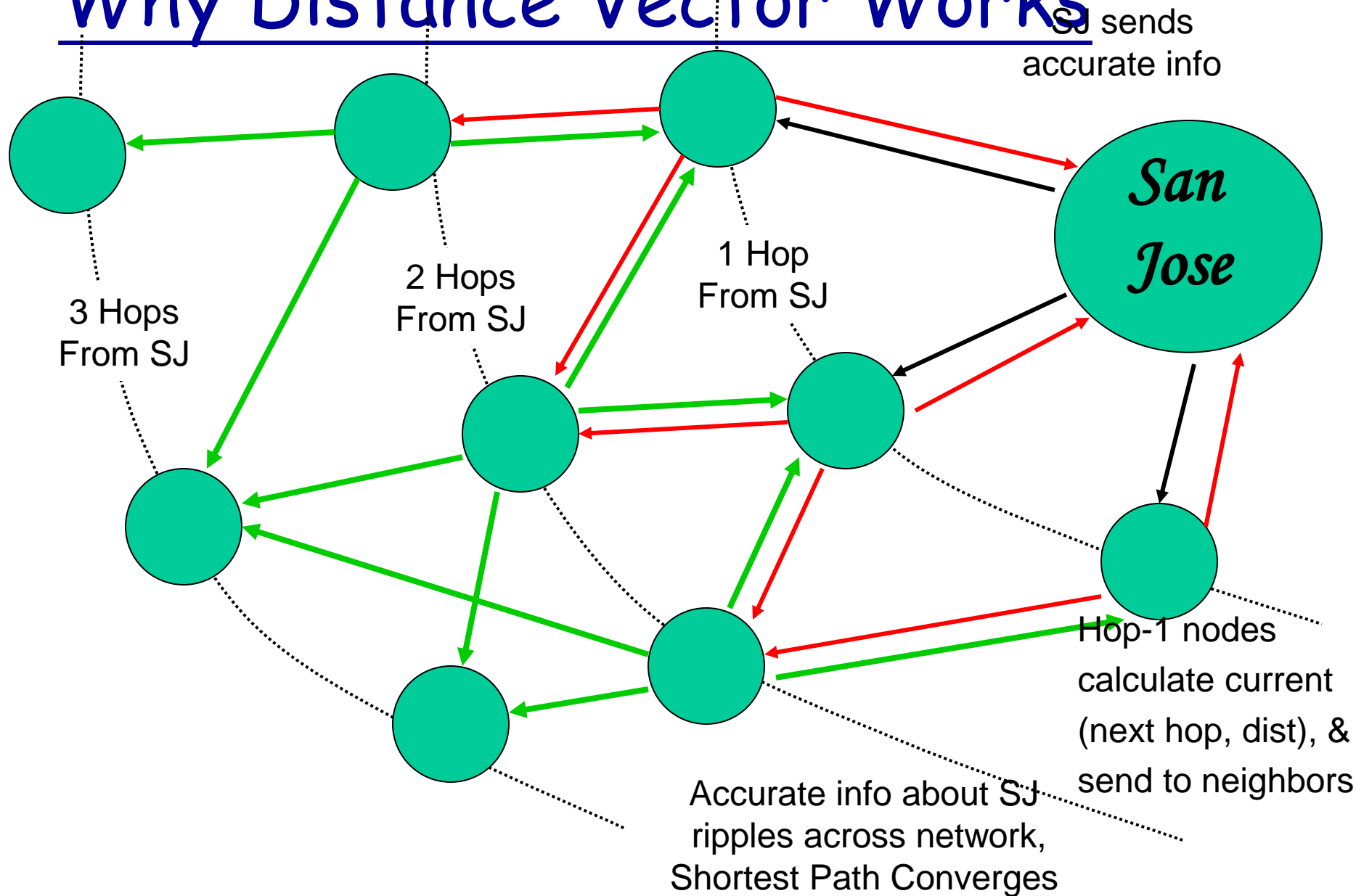


## But we don't know the shortest paths

$i$  only has local info  
from neighbors

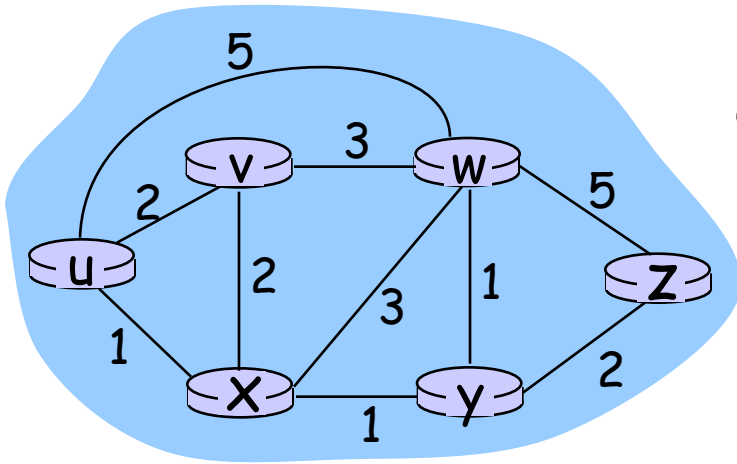


# Why Distance Vector Works





# Bellman-Ford example



Clearly,  $d_v(z) = 5$ ,  $d_x(z) = 3$ ,  $d_w(z) = 3$

B-F equation says:

$$\begin{aligned} d_u(z) &= \min \{ c(u,v) + d_v(z), \\ &\quad c(u,x) + d_x(z), \\ &\quad c(u,w) + d_w(z) \} \\ &= \min \{ 2 + 5, \\ &\quad 1 + 3, \\ &\quad 5 + 3 \} = 4 \end{aligned}$$

Node that achieves minimum is next  
hop in shortest path → forwarding table

# Distance Vector Algorithm

- ❖  $D_x(y)$  = estimate of least cost from  $x$  to  $y$ 
  - $x$  maintains distance vector  $D_x = [D_x(y): y \in N]$
- ❖ node  $x$ :
  - knows cost to each neighbor  $v$ :  $c(x,v)$
  - maintains its neighbors' distance vectors.  
For each neighbor  $v$ ,  $x$  maintains  
 $D_v = [D_v(y): y \in N]$

# Distance vector algorithm (4)

## Basic idea:

- ❖ from time-to-time, each node sends its own distance vector estimate to neighbors
- ❖ when  $x$  receives new DV estimate from neighbor, it updates its own DV using B-F equation:

$$D_x(y) \leftarrow \min_v \{c(x,v) + D_v(y)\} \quad \text{for each node } y \in N$$

- ❖ under minor, natural conditions, the estimate  $D_x(y)$  converge to the actual least cost  $d_x(y)$

# Distance Vector Algorithm (5)

## Iterative, asynchronous:

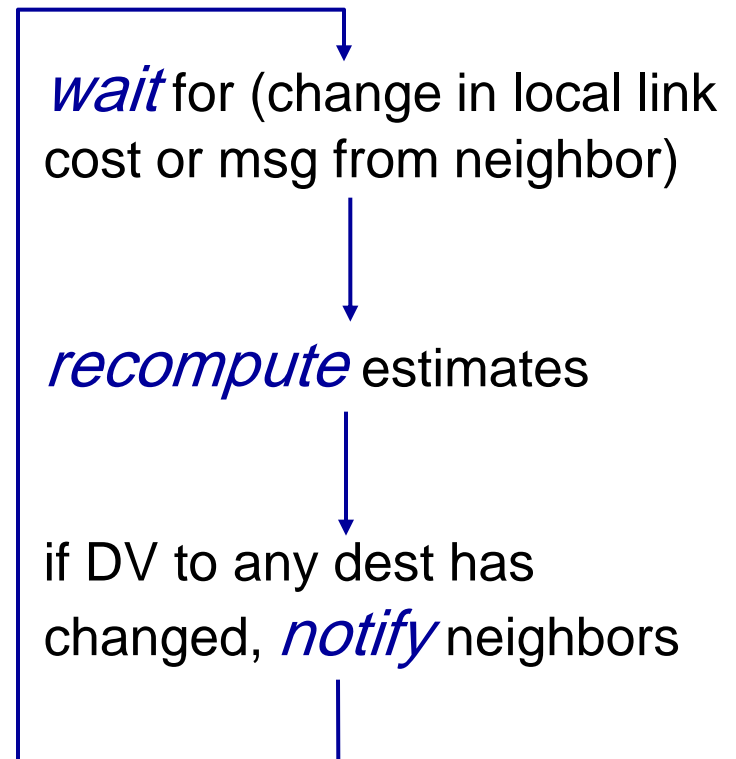
each local iteration caused by:

- ❖ local link cost change
- ❖ DV update message from neighbor

## Distributed:

- ❖ each node notifies neighbors *only* when its DV changes
  - neighbors then notify their neighbors if necessary

## Each node:



# Distance Vector Algorithm

- $c(x,v)$  = cost for direct link from  $x$  to  $v$ 
  - Node  $x$  maintains costs of direct links  $c(x,v)$
- $D_x(y)$  = estimate of least cost from  $x$  to  $y$ 
  - Node  $x$  maintains distance vector  $\mathbf{D}_x = [D_x(y): y \in N]$
- Node  $x$  maintains its neighbors' distance vectors
  - For each neighbor  $v$ ,  $x$  maintains  $\mathbf{D}_v = [D_v(y): y \in N]$
- Each node  $v$  periodically sends  $\mathbf{D}_v$  to its neighbors
  - And neighbors update their own distance vectors
  - $D_x(y) \leftarrow \min_v \{c(x,v) + D_v(y)\}$  for each node  $y \in N$
- Over time, the distance vector  $\mathbf{D}_x$  converges

1 **Initialization:**

2     for all destinations  $y$  in  $N$ :

3          $D_x(y) = c(x,y)$      /\* if  $y$  is not a neighbor then  $c(x,y) = \infty$  \*/

4     for each neighbor  $w$

5          $D_w(y) = ?$  for all destinations  $y$  in  $N$

6     for each neighbor  $w$

7         send distance vector  $D_x = [D_x(y): y \text{ in } N]$  to  $w$

8

9 **loop**

10     **wait** (until I see a link cost change to some neighbor  $w$  or

11         until I receive a distance vector from some neighbor  $w$ )

12

13     for each  $y$  in  $N$ :

14          $D_x(y) = \min_v \{c(x,v) + D_v(y)\}$

15

16     **if**  $D_x(y)$  changed for any destination  $y$

17         send distance vector  $D_x = [D_x(y): y \text{ in } N]$  to all neighbors

18

19 **forever**

$$D_x(y) = \min\{c(x,y) + D_y(y), c(x,z) + D_z(y)\} \\ = \min\{2+0, 7+1\} = 2$$

$$D_x(z) = \min\{c(x,y) + D_y(z), c(x,z) + D_z(z)\} \\ = \min\{2+1, 7+0\} = 3$$

### node x table

		cost to		
		x	y	z
from	x	0	2	7
	y	∞	∞	∞
	z	∞	∞	∞

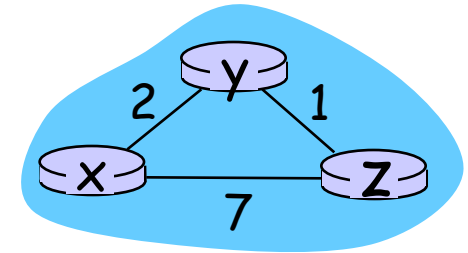
### node y table

		cost to		
		x	y	z
from	x	∞	∞	∞
	y	2	0	1
	z	∞	∞	∞

### node z table

		cost to		
		x	y	z
from	x	∞	∞	∞
	y	∞	∞	∞
	z	7	1	0

		cost to		
		x	y	z
from	x	0	2	3
	y	2	0	1
	z	7	1	0



time

$$D_x(y) = \min\{c(x,y) + D_y(y), c(x,z) + D_z(y)\} \\ = \min\{2+0, 7+1\} = 2$$

$$D_x(z) = \min\{c(x,y) + D_y(z), c(x,z) + D_z(z)\} \\ = \min\{2+1, 7+0\} = 3$$

### node x table

		cost to		
from		x	y	z
	x	0	2	7
	y	∞	∞	∞
	z	∞	∞	∞

### node y table

		cost to		
from		x	y	z
	x	∞	∞	∞
	y	2	0	1
	z	∞	∞	∞

### node z table

		cost to		
from		x	y	z
	x	∞	∞	∞
	y	∞	∞	∞
	z	7	1	0

		cost to		
from		x	y	z
	x	0	2	3
	y	2	0	1
	z	7	1	0

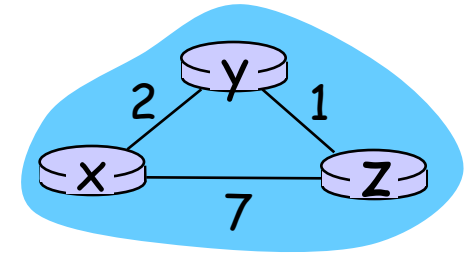
		cost to		
from		x	y	z
	x	0	2	7
	y	2	0	1
	z	7	1	0

		cost to		
from		x	y	z
	x	0	2	7
	y	2	0	1
	z	3	1	0

		cost to		
from		x	y	z
	x	0	2	3
	y	2	0	1
	z	3	1	0

		cost to		
from		x	y	z
	x	0	2	3
	y	2	0	1
	z	3	1	0

		cost to		
from		x	y	z
	x	0	2	3
	y	2	0	1
	z	3	1	0



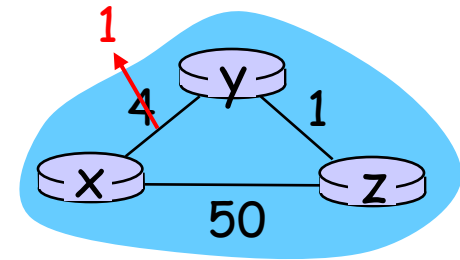
time →



# Distance Vector: link cost changes

## Link cost changes:

- ❖ node detects local link cost change
- ❖ updates routing info, recalculates distance vector
- ❖ if DV changes, notify neighbors



"good  
news  
travels  
fast"

$t_0$ : y detects link-cost change, updates its DV, informs its neighbors.

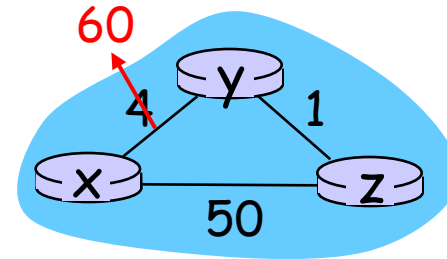
$t_1$ : z receives update from y, updates its table, computes new least cost to x, sends its neighbors its DV.

$t_2$ : y receives z's update, updates its distance table. y's least costs do *not* change, so y does *not* send a message to z.

# Distance Vector: link cost changes

## Link cost changes:

- ❖ good news travels fast
- ❖ bad news travels slow - "count to infinity" problem!
- ❖ 44 iterations before algorithm stabilizes.



## Poisoned reverse:

- ❖ If Z routes through Y to get to X :
  - Z tells Y its (Z's) distance to X is infinite (so Y won't route to X via Z)
- ❖ will this completely solve count to infinity problem?

# Routing Protocol

# Hierarchical routing

our routing study thus far - idealization

- ❖ all routers identical
- ❖ network “flat”

... *not* true in practice

*scale:* with 600 million destinations:

- ❖ can't store all dest's in routing tables!
- ❖ routing table exchange would swamp links!

*administrative autonomy*

- ❖ internet = network of networks
- ❖ each network admin may want to control routing in its own network

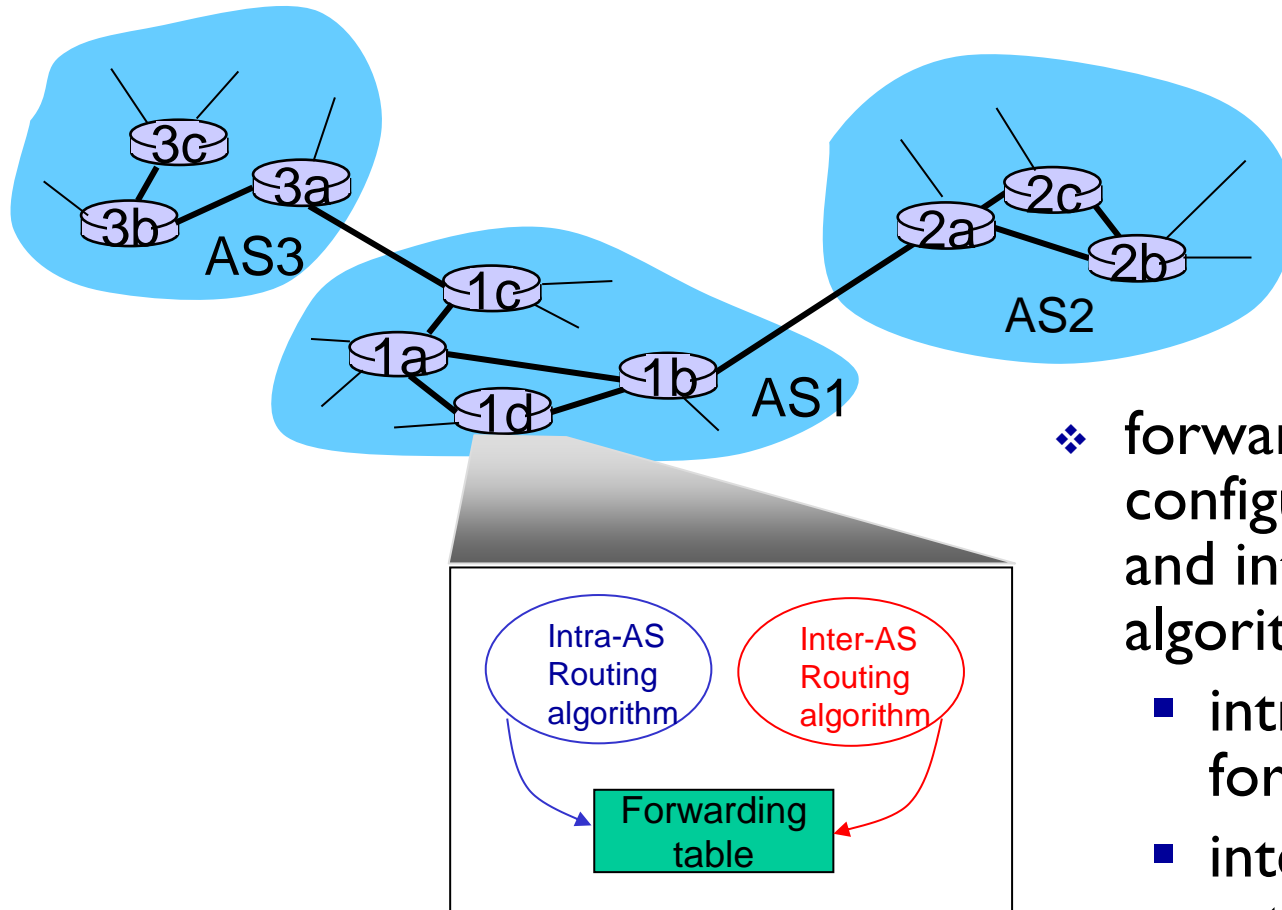
# Hierarchical routing

- ❖ aggregate routers into regions, “**autonomous systems**” (AS)
- ❖ routers in same AS run same routing protocol
  - “**intra-AS**” routing protocol
  - routers in different AS can run different intra-AS routing protocol

## *gateway router:*

- ❖ at “edge” of its own AS
- ❖ has link to router in another AS

# Interconnected ASes



- ❖ forwarding table configured by both intra- and inter-AS routing algorithm
  - intra-AS sets entries for internal dests
  - inter-AS & intra-AS sets entries for external dests

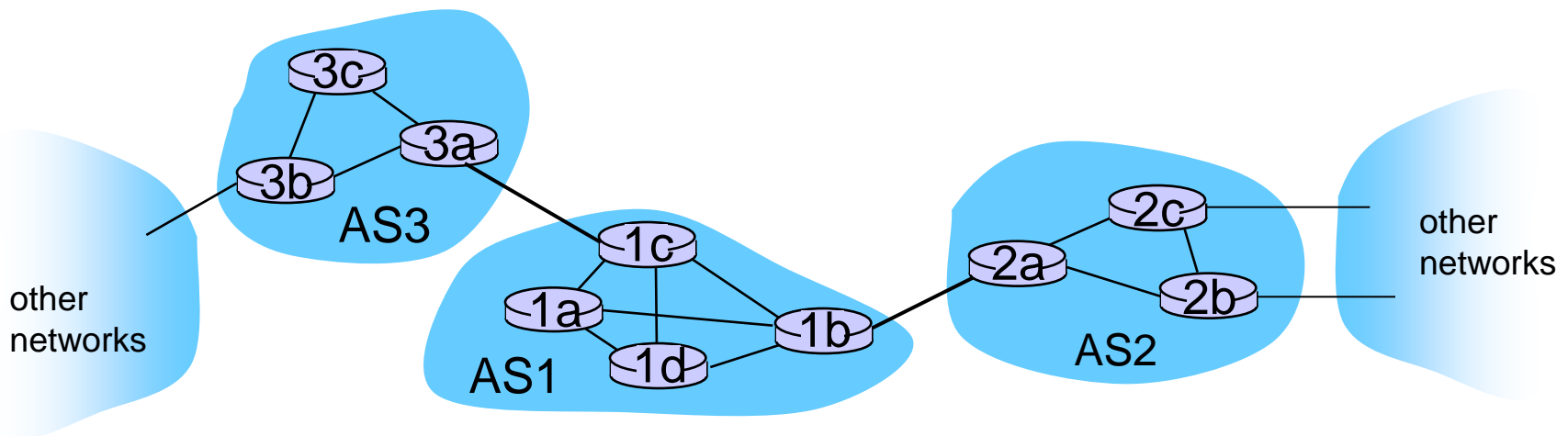
# Inter-AS tasks

- ❖ suppose router in AS1 receives datagram destined outside of AS1:
  - router should forward packet to gateway router, but which one?

*AS1 must:*

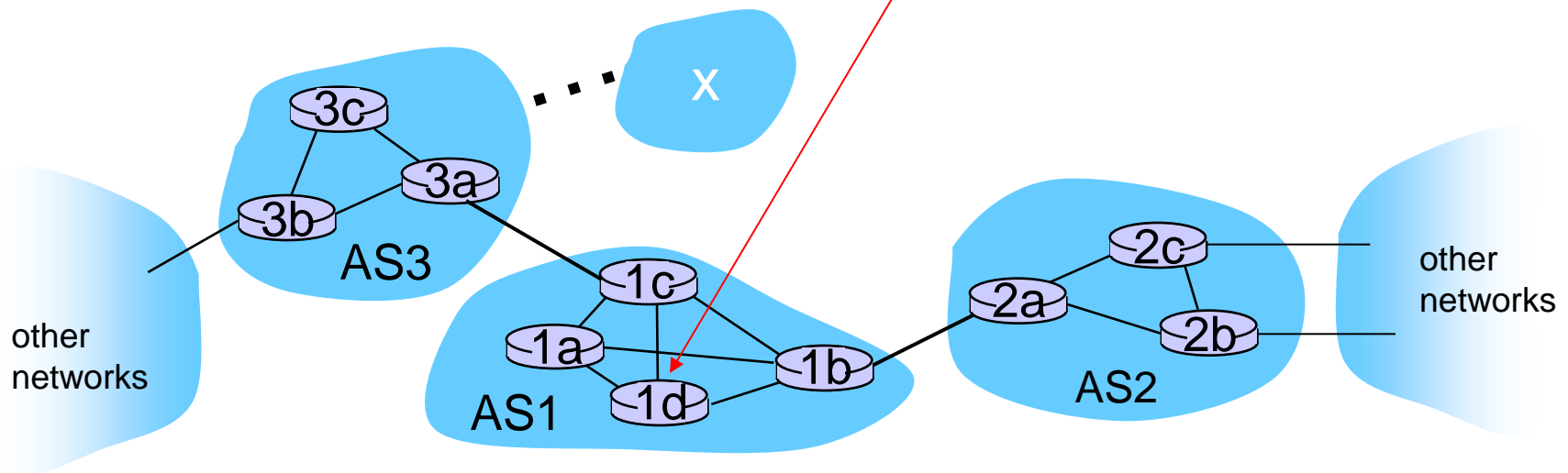
1. learn which destds are reachable through AS2, which through AS3
2. propagate this reachability info to all routers in AS1

*job of inter-AS routing!*



# Example: setting forwarding table in router 1d

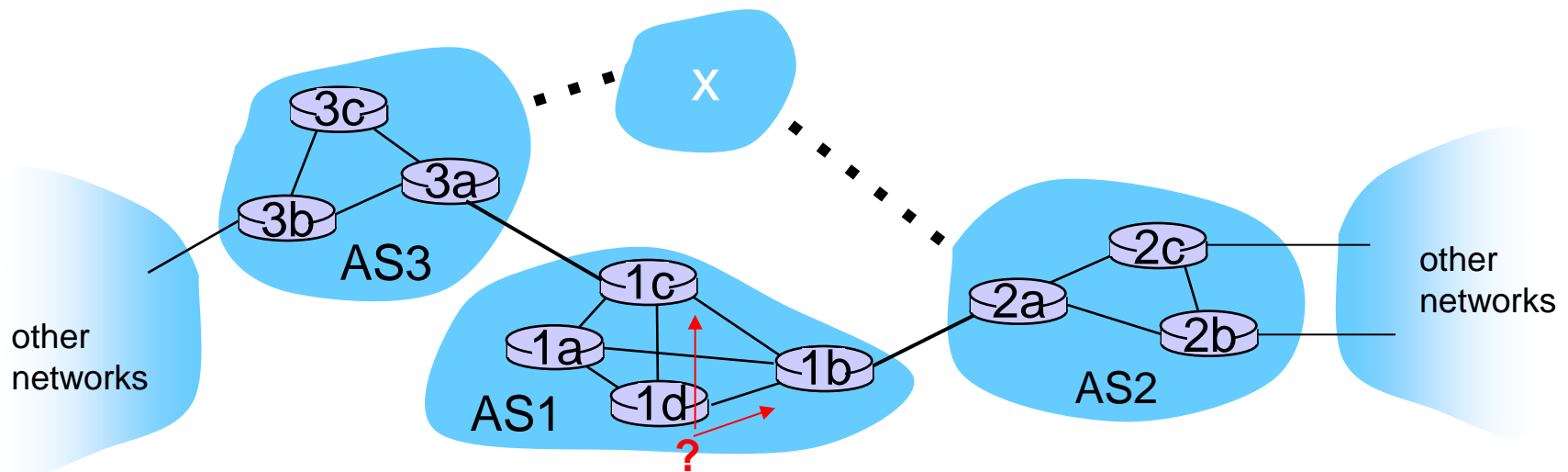
- ❖ suppose AS1 learns (via inter-AS protocol) that subnet **x** reachable via AS3 (gateway 1c), but not via AS2
  - inter-AS protocol propagates reachability info to all internal routers
- ❖ router 1d determines from intra-AS routing info that its interface **l** is on the least cost path to 1c
  - installs forwarding table entry **(x,l)**





# Example: choosing among multiple ASes

- ❖ now suppose AS1 learns from inter-AS protocol that subnet **x** is reachable from AS3 *and* from AS2.
- ❖ to configure forwarding table, router 1d must determine which gateway it should forward packets towards for dest **x**
  - this is also job of inter-AS routing protocol!

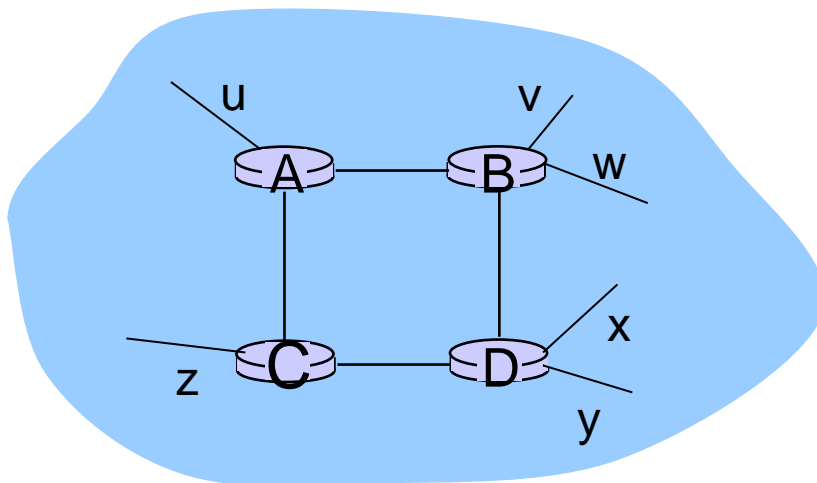


# Intra-AS Routing

- ❖ also known as *interior gateway protocols (IGP)*
- ❖ most common intra-AS routing protocols:
  - RIP: Routing Information Protocol
  - OSPF: Open Shortest Path First
  - IGRP: Interior Gateway Routing Protocol (Cisco proprietary)

# RIP ( Routing Information Protocol)

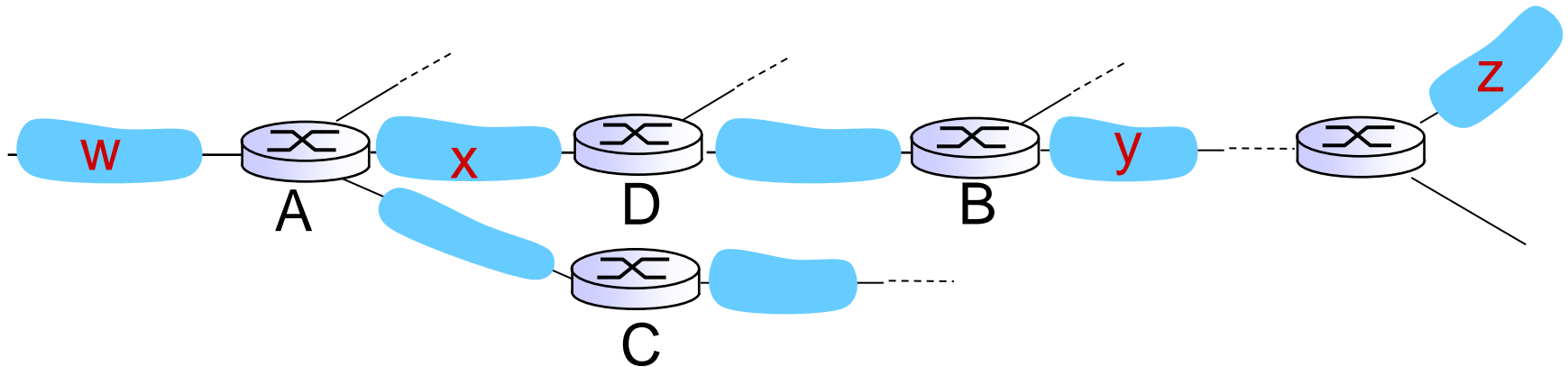
- ❖ included in BSD-UNIX distribution in 1982
- ❖ distance vector algorithm
  - distance metric: # hops (max = 15 hops), each link has cost 1
  - DVs exchanged with neighbors every 30 sec in response message (aka **advertisement**)
  - each advertisement: list of up to 25 destination **subnets** (in IP addressing sense)



from router A to destination **subnets**:

<u>subnet</u>	<u>hops</u>
u	1
v	2
w	2
x	3
y	3
z	2

# RIP: example



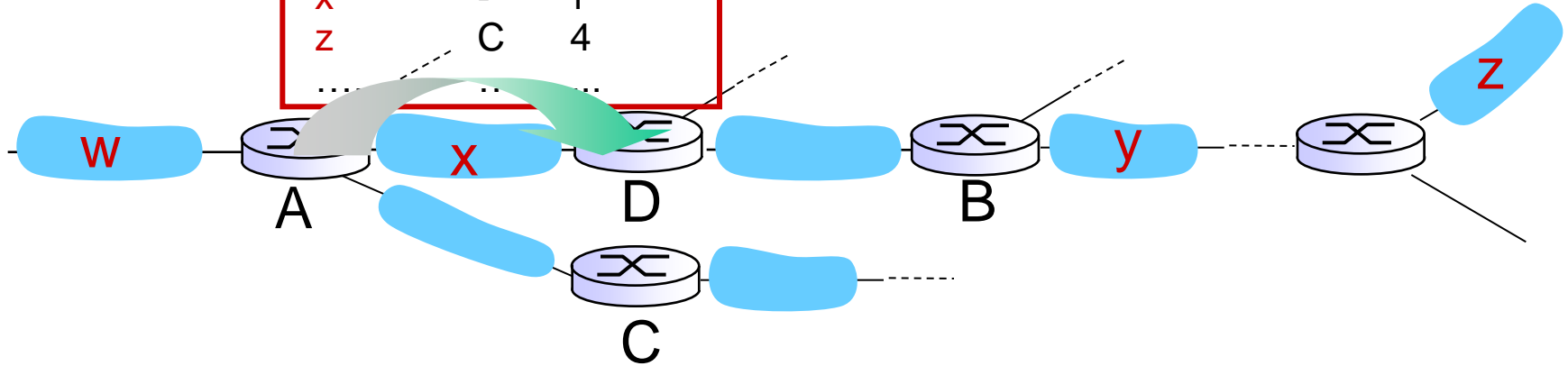
routing table in router D

destination subnet	next router	# hops to dest
w	A	2
y	B	2
z	B	7
x	--	1
....	....	....

# RIP: example

A-to-D advertisement

dest	next	hops
w	-	1
x	-	1
z	C	4
...	...	...



routing table in router D

destination subnet	next router	# hops to dest
w	A	2
y	B	2
z	<del>B</del> → A	<del>7</del> → 5
x	--	1
....	....	....

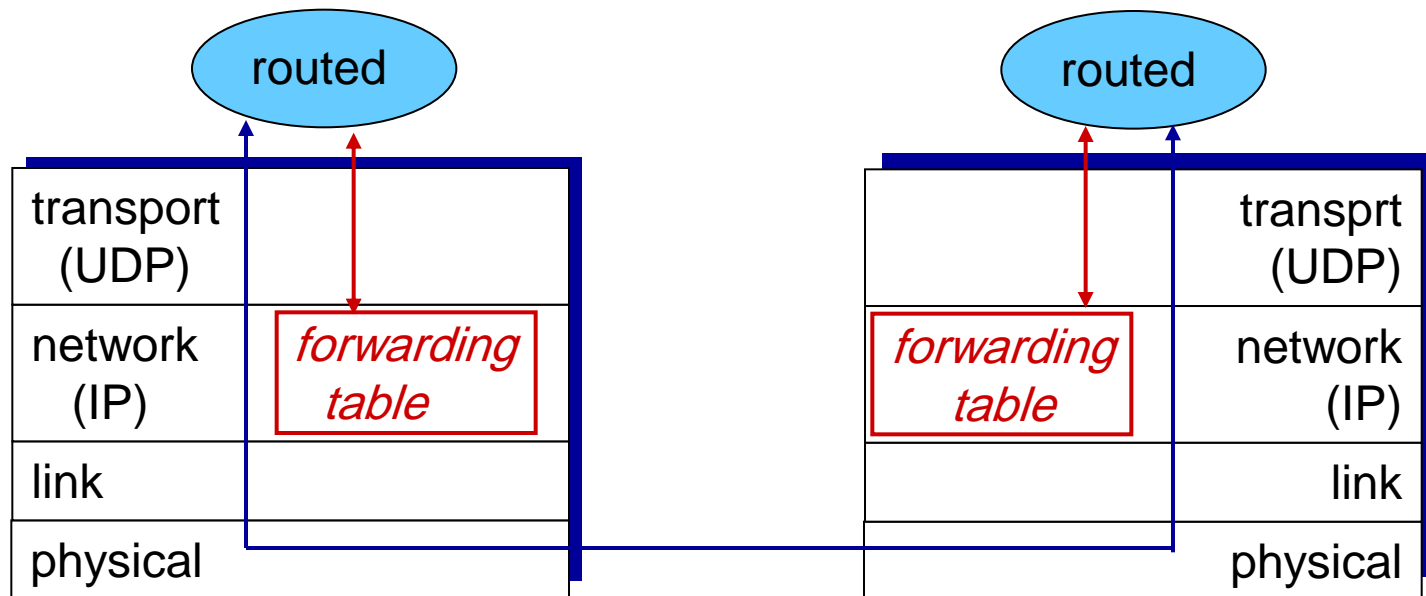
# RIP: link failure, recovery

if no advertisement heard after 180 sec -->  
neighbor/link declared dead

- routes via neighbor invalidated
- new advertisements sent to neighbors
- neighbors in turn send out new advertisements (if tables changed)
- link failure info quickly (?) propagates to entire net
- *poison reverse* used to prevent ping-pong loops (infinite distance = 16 hops)

# RIP table processing

- ❖ RIP routing tables managed by *application-level* process called route-d (daemon)
- ❖ advertisements sent in UDP packets, periodically repeated



# OSPF (Open Shortest Path First)

- ❖ “open”: publicly available
- ❖ uses link state algorithm
  - LS packet dissemination
  - topology map at each node
  - route computation using Dijkstra’s algorithm
- ❖ OSPF advertisement carries one entry per neighbor
- ❖ advertisements flooded to *entire* AS
  - carried in OSPF messages directly over IP (rather than TCP or UDP)
- ❖ *IS-IS routing* protocol: nearly identical to OSPF