# **C28x IQmath Library**

**A Virtual Floating Point Engine** 

V1.5a

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Module user's Guide C28x Foundation Software



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# **Acronyms**

C28x+FPU: Refers to devices with the C28x plus floating-point-unit.

IQmath: High Accuracy Mathematical Functions (32-bit implementation).

QMATH: Fixed Point Mathematical computation

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# **Chapter 1. Introduction**

## 1.1. Introduction

Texas Instruments TMS320C28x IQmath Library is collection of highly optimized and high precision mathematical functions for C/C++ programmers to seamlessly port a floating-point algorithm into fixed point code on TMS320C28x devices. These routines are typically used in computationally intensive real-time applications where optimal execution speed and high accuracy is critical. By using these routines you can achieve execution speeds considerable faster than equivalent code written in standard ANSI C language. In addition, by providing ready-to-use high precision functions, TI IQmath library can shorten significantly your DSP application development time.

# **Chapter 2. Installing the IQmath Library**

# 2.1. IQmath Package Contents

The TI IQmath library can be used in both C and C++ programs and it consists of 5 parts:

- The IQmath header files
   The header files include the definitions needed to interface with the IQmath library.
   C programs use IQmathLib.h
  - a) C++ programs use both IQmathLib.h and IQmathCPP.h
- 2) The IQmath object library. The library contains all of the IQmath functions and look-up tables. There are two builds of the library:
  - a) IQmath.lib: This build of the library can be linked with code built for fixed-point.
  - b) IQmath\_f32.lib: This build of the library can be linked with code built with the --float\_support=fpu32 switch. This can be useful for mixing IQmath with native floating-point code on devices with the C28x+FPU.
- 3) Example linker command files. The example linker command files allocate the sections used by the IQmath library. For some sections the location is device specific. For example, the tables used by the IQsin and IQcos functions are located within the boot ROM of the device.
- 4) IQmath GEL file. These gel functions are useful when using a version of Code Composer Studio that does not support IQ data types directly.
- 5) Example programs

# 2.2. How to Install the IQmath Library

The IQmath library is distributed in the form of a self-extracting ZIP file. By default, the install restores the IQmath library individual components in the directory structure shown below.

#### NOTE:

The directory structure of previous versions differed from what is shown below. For this release it has been reorganized to reduce duplication of files.

<base> install directory is C:\tidcs\c28x\lQmath\v15a

<base>\include The IQmath header files

C code uses IQmathLib.h

C++ code uses IQmathLib.h and IQmathCPP.h

<br/>the lQmath library files. These are used by both C and C++

Refer to Chapter 4.

<base>\gel
Legacy GEL file for debug

Refer to section 3.9.

<base>\examples\C
C example: Refer to ReadMe SampleC.txt

<base>\examples\Cpp\projects CCS projects for the C++ example
<base>\examples\Cpp\source Source code for the C++ example

# **Chapter 3. Using the IQmath Library**

# 3.1. IQmath Arguments and Data Types

Input/output of the IQmath functions are typically 32-bit fixed-point numbers and the Q format of the fixed-point number can vary from Q1 to Q30.

We have used typedefs to create aliases for IQ data types. This facilitates the user to define the variable of IQmath data type in the application program.

```
typedef
                                         /* Fixed point data type: GLOBAL_Q format */
                            _iq;
                            _iq30; /* Fixed point data type: Q30 format
typedef long
                           _iq29; /* Fixed point data type: Q29 format
typedef long
typedef long _iq28; /* Fixed point data type: Q28 format typedef long _iq27; /* Fixed point data type: Q27 format
                                                                                                            */
typedef long _iq26; /* Fixed point data type: Q26 format
                                                                                                            */
                           _iq25; /* Fixed point data type: Q25 format
typedef long
                                                                                                            */
typedef long _iq24; /* Fixed point data type: Q24 format
typedef long _iq23; /* Fixed point data type: Q23 format typedef long _iq22; /* Fixed point data type: Q22 format typedef long _iq21; /* Fixed point data type: Q21 format
typedef long _iq20; /* Fixed point data type: Q20 format
                           _iq19; /* Fixed point data type: Q19 format
typedef long
                           _iq18; /* Fixed point data type: Q18 format
typedef long
                                                                                                            */
typedef long
                           _iq17; /* Fixed point data type: Q17 format
                                                                                                            * /
typedef long
                           _iq16; /* Fixed point data type: Q16 format
                                                                                                            * /
typedef long _iq15; /* Fixed point data type: Q15 format
                                                                                                            */
typedef long _iq14; /* Fixed point data type: Q14 format
                                                                                                            * /
typedef long _iq13; /* Fixed point data type: Q13 format
                                                                                                            */
                           _iq12; /* Fixed point data type: Q12 format
typedef long
                                                                                                            */
                           _iq11; /* Fixed point data type: Q11 format
typedef long
                                                                                                            */
typedef long _iq11; /* Fixed point data type: Q11 format typedef long _iq10; /* Fixed point data type: Q10 format typedef long _iq9; /* Fixed point data type: Q9 format typedef long _iq8; /* Fixed point data type: Q8 format typedef long _iq7; /* Fixed point data type: Q7 format typedef long _iq6; /* Fixed point data type: Q6 format typedef long _iq5; /* Fixed point data type: Q6 format typedef long _iq4; /* Fixed point data type: Q4 format typedef long _iq3; /* Fixed point data type: Q4 format typedef long _iq2; /* Fixed point data type: Q3 format typedef long _iq2; /* Fixed point data type: Q2 format typedef long _iq1; /* Fixed point data type: Q1 format typedef long _iq1; /* Fixed point data type: Q1 format
                                                                                                            * /
                                                                                                           */
                                                                                                           */
                                                                                                           * /
                                                                                                          * /
                                                                                                            */
```

# 3.2. IQmath Data type: Range & Resolution

Following table summarizes the Range & Resolution of 32-bit fixed-point number for different Q format representation. Typically IQmath function supports Q1 to Q30 format, nevertheless some functions like IQNsin, IQNcos, IQNatan2, IQNatan2PU, IQatan do not support Q30 format, due to the fact that these functions input or output vary between  $-\pi$  to  $\pi$  radians.

Data Type		Range	Resolution/Precision
	Min Max		
_iq30	-2	1.999 999 999	0.000 000 001
_iq29	-4	3.999 999 998	0.000 000 002
_iq28	-8	7.999 999 996	0.000 000 004
_iq27	-16	15.999 999 993	0.000 000 007
_iq26	-32	31.999 999 985	0.000 000 015
_iq25	-64	63.999 999 970	0.000 000 030
_iq24	-128	127.999 999 940	0.000 000 060
_iq23	-256	255.999 999 981	0.000 000 119
_iq22	-512	511.999 999 762	0.000 000 238
_iq21	-1024	1023.999 999 523	0.000 000 477
_iq20	-2048	2047.999 999 046	0.000 000 954
_iq19	-4096	4095.999 998 093	0.000 001 907
_iq18	-8192	8191.999 996 185	0.000 003 815
_iq17	-16384	16383.999 992 371	0.000 007 629
_iq16	-32768	32767.999 984 741	0.000 015 259
_iq15	-65536	65535.999 969 482	0.000 030 518
_iq14	-131072	131071.999 938 965	0.000 061 035
_iq13	-262144	262143.999 877 930	0.000 122 070
_iq12	-524288	524287.999 755 859	0.000 244 141
_iq11	-1048576	1048575.999 511 719	0.000 488 281
_iq10	-2097152	2097151.999 023 437	0.000 976 563
_iq9	-4194304	4194303.998 046 875	0.001 953 125
_iq8	-8388608	8388607.996 093 750	0.003 906 250
_iq7	-16777216	16777215.992 187 500	0.007 812 500
_iq6	-33554432	33554431.984 375 000	0.015 625 000
_iq5	-67108864	67108863.968 750 000	0.031 250 000
_iq4	-134217728	134217727.937 500 000	0.062 500 000
_iq3	-268435456	268435455.875 000 000	0.125 000 000
_iq2	-536870912	536870911.750 000 000	0.250 000 000
_iq1	-1073741824	1 073741823.500 000 000	0.500 000 000

# 3.3. Calling an IQmath Function from C

In addition to installing the IQmath software, to include an IQmath function in your code you have to:

- Include the IQmathLib.h include file
- Link your code with the IQmath object code library. This will normally be the IQmath.lib library. If you have a C28x with floating-point device and wish to mix IQmath and native floating-point, then use the IQmath\_fpu32.lib. This file contains all of the IQmath functions in object format. The library is constructed such that ONLY the functions that are used are included as part of the project. This minimizes code size.
- The linker command file should be updated to properly access the IQmath lookup tables and place the IQmath code in the memory block you wish. These sections are described later in this chapter.
- Call the functions using the \_iq and \_iqN data types along with the C-code function definitions. For example, the following code contains a call to the *IQ25sin* routines in IQmath Library:

# 3.4. Calling an IQmath function from C++

In C++ the \_iq type becomes the iq class. This allows for function overloading of operators such as multiply and divide. To access the library from C++ follow these steps:

Include both the IQmathLib.h and the IQmathCPP.h header file as shown below:

```
extern "C" {
#include "IQmathLib.h"
}
#include "IQmathCPP.h"
```

- Link your code with the IQmath object code library. This will normally be the IQmath.lib library. If you have a C28x with floating-point device and wish to mix IQmath and native floating-point, then use the IQmath\_fpu32.lib. Notice the same library is used by both C and C++ code. This file contains all of the IQmath functions in object format. The library is constructed such that ONLY the functions that are used are included as part of the project. This minimizes code size.
- The linker command file should be updated to properly access the IQmath lookup tables and place the IQmath code in the memory block you wish. These sections are described later in this chapter.

 Call the functions using the iq and iqN classes along with the C++ code function definitions. In C++ the functions are called without the leading underscore and the math operations are overloaded For example:

The following example code contains a call to the *IQ25sin* routines in IQmath Library using C++ code:

# 3.5. IQmath Section and Lookup Tables

Some of the IQmath functions use look-up tables. Many of these tables are included in the boot ROM of 28x devices. Using the boot ROM copy will save you memory space and the time required to load the tables themselves. Note that the boot ROM on some devices is 1 wait state compared to SARAM that is usually 0 wait state. The look-up tables are usually not accessed often enough for this to cause an issue with performance. Therefore, in most cases you will want to use the boot ROM look-up tables.

The IQmath library uses the following lookup tables:

#### IQmathTables:

This section contains look-up tables for the most often used IQmath functions. This includes IQdiv, IQsin, IQcos, IQsqrt and IQatan2. The IQmathTables are available in the boot ROM of all 28x devices. Hence, this section should be identified as a "NOLOAD" type in the linker command file. This facilitates referencing look-up table symbols without actually loading the section into the target.

#### IQmathTablesRam:

This section contains initialized look-up tables used by the IQexp, IQasin and IQacos functions. If you do not call these functions, then there is no need to load this section. Some devices also include some of these tables in the boot ROM as shown in the following table.

Device	Assembly Section Name	<b>Boot ROM Location</b>
	(i.esect)	
281x	IQmathTables	0x3FF000
280x	IQmathTables	0x3FF000
2801x	IQmathTables	0x3FF000
2833x/2823x	IQmathTables	0x3FE000
2834x	IQmathTablesRam (IQNexpTable.obj only)	0x3FEB50
2802x	IQmathTables	0x3FE000
2803x	IQmathTablesRam (IQNexpTable.obj)	0x3FEB50
2003X	IQmathTablesRam (IQNasinTable.obj)	0x3FEBDC

If your device is not listed, refer to the boot ROM reference guide and the boot ROM source code for your device to get more information.

If a table is not included in the boot ROM of the device, then it must be loaded into the appropriate memory in the linker command file.

### NOTE: IQmathTablesRam

The section name IQmathTablesRam may be a bit misleading. This table contains initialized data tables for the IQexp, IQasin, and IQacos functions. During debug, these tables can be loaded directly into SARAM as shown in the linker file below.

During stand-alone operation, if these functions are used, then the table should be loaded into non-volatile memory (for example flash). If you want to access them in SARAM then copy them from flash to SARAM during initialization.

Assembly Section Name and obj file	Symbols / Initialized Tables Defined		
	IQdivTable QdivTableEnd IQdivRoundSatTable	IQsinTable IQsinTableEnd IQcosTable IQcosTableEnd	
IQmathTables (IQmathTables.obj)	IQsqrtTable IQsqrtTableEnd IQisqrtTable IQisqrtTableEnd IQsqrtRoundSatTable IQisqrtRoundSatTable	IQatan2Table IQatan2TableEnd IQatan2HalfPITable	
IQmathTablesRam (IQNexpTable.obj)	IQexpTable IQexpTableMinMax IQexpTableMinMaxEnd IQexpTableCoeff IQexpTableCoeffEnd		
IQmathTablesRam (IQNasinTable.obj)	IQasinTable		

The following is an example of a linker file for the 281x devices. In this case only the IQmathTables section is in the boot ROM. If used, the IQmathTablesRam section must be loaded into the device along with the application itself.

```
MEMORY
{
PAGE 0:
    PRAMHO (RW) : origin = 0x3f8000, length = 0x001000
PAGE 1:
    IQTABLES (R) : origin = 0x3fF000, length = 0x000b50
    DRAMHO (RW) : origin = 0x3f9000, length = 0x001000
}
SECTIONS
{
    IQmathTables : load = IQTABLES, type = NOLOAD, PAGE = 1
    IQmathTablesRam : load = DRAMHO, PAGE = 1
    IQmath : load = PRAMHO, PAGE = 0
}
```

The 2833x and 2823x boot ROM includes the IQNexpTable used by the IQNexp() and IQexp() functions. In this case the IQNexpTable can be placed into its own section and identified as type NOLOAD as shown in the next example. The remainder of the IQmathTablesRam section is allocated to SARAM.

```
IQmath Linker Command File Example:
                              2823x Device
MEMORY
PAGE 0:
  PRAMLO (RW) : origin = 0x008000, length = 0x001000
PAGE 1:
   IQTABLES (R) : origin = 0x3FE000, length = 0x000b50 IQTABLES2 (R) : origin = 0x3FEB50, length = 0x00008c
   DRAML1 (RW)
                    : origin = 0x009000, length = 0x001000
SECTIONS
   IQmathTables : load = IQTABLES, type = NOLOAD, PAGE = 1
   IQmathTables2 > IQTABLES2, type = NOLOAD, PAGE = 1
       IQmath.lib<IQNexpTable.obj> (IQmathTablesRam)
   IQmathTablesRam : load = DRAML1, PAGE = 1
             : load = PRAMLO, PAGE = 0
   IOmath
```

Some devices, such as the 2802x and 2803x, include both IQNexpTable used by the IQNexp() and IQexp() functions as well as the IQasinTable used by the IQasin() and IQNasin() functions. In this case the IQNexpTable and IQasinTable can be placed into their own section and identified as type NOLOAD as shown in the next example.

```
IQmath Linker Command File Example:
                            2803x Device
MEMORY
PAGE 0:
  PRAMLO (RW) : origin = 0x008000, length = 0x001000
PAGE 1:
  IQTABLES (R) : origin = 0x3FE000, length = 0x000b50
   IQTABLES2 (R) : origin = 0x3FEB50, length = 0x00008c
   IQTABLES3 (R) : origin = 0x3FEBDC, length = 0x0000AA
                  : origin = 0x009000, length = 0x001000
   DRAML1 (RW)
SECTIONS
   IQmathTables
                  : load = IQTABLES, type = NOLOAD, PAGE = 1
   IQmathTables2 > IQTABLES2, type = NOLOAD, PAGE = 1
       IQmath.lib<IQNexpTable.obj> (IQmathTablesRam)
   IQmathTables3 > IQTABLES3, type = NOLOAD, PAGE = 1
       IQmath.lib<IQNasinTable.obj> (IQmathTablesRam)
                   : load = PRAMLO, PAGE = 0
   IQmath
```

# NOTE: When including IQNexpTable.obj and/or IQNasinTable.obj in the linker file SECTIONS:

It should be noted that if the IQexp() function is not called in the application, then the allocation for IQNexpTable.obj will result in a linker warning. Likewise if IQasin() or IQacos() are not called, then IQNasinTable.obj will result in a linker warning. This is because the table will not be included if it is not used. This warning will not cause any ill effects to the normal operation of the application.

# 3.6. Accessing IQmath Functions in the Boot ROM

Some devices contain selected IQmath functions within the boot ROM itself. You can use these copies to save both flash and RAM space. If your device is not listed in the table below, then refer to the boot ROM guide for more information.

Device	IQmath Functions in Boot ROM	I Values of N
281x	none	N/A
280x	none	N/A
2801x	none	N/A
2833x, 2823x	none	N/A
2834x	none	N/A
2802x, 2803x	IQNatan2 IQNsqrt IQNdiv IQNsin IQNmag IQNcos IQNisqrt	15, 20, 24, 29

To easily use the boot ROM copies of the functions in place of the existing functions, an IQmath boot ROM symbol library has been provided with the boot ROM source code. This source code is available for download from the TI website with the boot ROM reference guide.

You will link the IQmath Boot ROM symbol library before the normal IQmath library. The boot ROM symbol library replaces only the subset of functions in the boot ROM. Therefore, the standard IQmath library should be linked after the boot ROM symbol library.

The following instructions apply to Code Composer Studio V3.3

1. Add the boot ROM symbol library (for example: 2802x\_IQmath\_BootROMSymbols.lib) and the standard IQmath.lib library to the project using

Project->Add Files to Project

Once the libraries are added to the project they will appear in the link order tab of the build options.

- 2. Open the build options dialog box under Project->Build Options
- 3. Under the Linker->Advanced tab, select the –priority linker switch.

This will force the linker to resolve symbols to the first library linked.

4. Under the Link Order tab, select the two libraries and add them to the link order.

Use the up/down arrows to arrange them in the proper order. The first library listed will be linked first.

5. Under the Linker->Libraries dialog add the path to the 2802x IQmath BootROMSymbols.lib and the IQmath library in the search path.

Do not include either libraries in the "Incl. Libraries" box. Doing so can cause problems when changing the link order since Code Composer uses both this field and the link order tab to determine which object files are linked first.

6. Save the project. (Project->Save).

To confirm that the boot ROM copies of the functions are being used, check the generated map file. Look for the symbols of the functions. For example, the address of the IQ24div, IQ24exp and IQ24sin symbols shown below are from the boot ROM area of the 2803x device. The remaining symbols are in RAM.

Address	Symbol	
0000821a	IQ24atan2PU	
003ff083	IQ24div	<- Boot ROM
000082a2	IQ24exp	
003fef35	IQ24mag	<- Boot ROM
000082df	IQ24mpyI32int	
003ff3c2	IQ24sin	<- Boot ROM

# 3.7. IQmath Naming Conventions

Each IQmath function comes in two types as shown below:

□ GLOBAL\_Q function, that takes input/output in GLOBAL\_Q format C-Code Examples:

# C++ Code Examples:

•	IQsin(A)	/* High Precision SIN	*/
•	IQcos(A)	/* High Precision COS	*/
•	IQrmpy(A,B)	/* IQ multiply with rounding	*/
•	A*B	/* IO multiply	*/

□ Q-format specific functions to cater to Q1 to Q30 data format.

# C-Code Examples:

•	_IQ29sin(A)	/* High Precision SIN: input/output are in Q29	*/
•	_IQ28sin(A)	/* High Precision SIN: input/output are in Q28	*/
•	_IQ27sin(A)	/* High Precision SIN: input/output are in Q27	*/
•	_IQ26sin(A)	/* High Precision SIN: input/output are in Q26	*/
•	_IQ25sin(A)	/* High Precision SIN: input/output are in Q25	*/
•	_IQ24sin(A)	/* High Precision SIN: input/output are in Q24	*/

## C++ Code Examples:

•	IQ29sin(A)	/* High Precision SIN: input/output are in Q29	*/
•	IQ28sin(A)	/* High Precision SIN: input/output are in Q28	*/
•	IQ27sin(A)	/* High Precision SIN: input/output are in Q27	*/
•	IQ26sin(A)	/* High Precision SIN: input/output are in Q26	*/
•	IQ25sin(A)	/* High Precision SIN: input/output are in Q25	*/
•	IQ24sin(A)	/* High Precision SIN: input/output are in Q24	*/

```
IQmath C Function Naming Convention

GLOBAL_Q Function
_IQXXX(), Where "XXX" is the Function Name

Q Specific Function
_IQNXXX(), Where "XXX" is the Function Name &

"N" is the Q format of input/output
```

# 3.8. Selecting the GLOBAL\_Q format

Numerical precision and dynamic range requirement will vary considerably from one application to other. IQmath Library facilitates the application programming in fixed-point arithmetic, without fixing the numerical precision up-front. This allows the system engineer to check the application performance with different numerical precision and finally fix the numerical resolution. As explained in section 3.2, higher the precision results in lower dynamic range. Hence, the system designer must trade-off between the range and resolution before choosing the GLOBAL\_Q format.

#### CASE I:

Default GLOBAL\_Q format is set to Q24. Edit "IQmathLib.h" header file to modify this value as required, user can choose from Q1 to Q29 as GLOBAL\_Q format. Modifying this value means that all the GLOBAL\_Q functions will use this Q format for input/output, unless this symbolic definition is overridden in the source code.

IQmathLib.h : Selecting GLOBAL_Q format				
#ifndef #define #endif	GLOBAL_Q GLOBAL_Q	24	/* Q1 to Q29	*/

# CASE II:

A complete system consists of various modules. Some modules may require different precision, then the rest of the system. In such situation, we need to over-ride the GLOBAL\_Q defined in the "IQmathLib.h" file and use the local Q format.

This can be easily done by defining the GLOBAL\_Q constant in the source file of the module before the include statement.

```
#define GLOBAL_Q 27  /* Set the Local Q value */
#include <IQmathLib.h>
```

# 3.9. Using the IQmath GEL file for Debugging

This information is useful when using an older version of Code Composer Studio that does not support IQ data types directly.

IQmath GEL file contains GEL functions that helps to view IQ variables in watch window and allows the setting of IQ variable values via dialogue boxes.

#### Step 1: Define "GlobalQ" variable

In one of the user source file, the following global variable must be defined:

long GlobalQ = GLOBAL\_Q;

This variable is used by the GEL functions to determine the current GLOBAL\_Q setting.

#### Step 2: Load GEL file

Load the "IQmath.gel" file into the user project. This will automatically load a set of GEL functions for displaying IQ variables in the watch window and create the following menus under the GEL toolbar

- > IQ C Support
- ➤ IQ C++ Support

### Step 3: Viewing IQmath variable

To view a variable in the watch window, simply type the following commands in the watch window. They will convert the specified "VarName" in IQ format to the equivalent floating-point value:

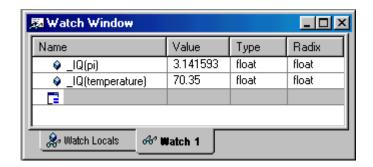
For C variables:

\_IQ(VarName) ; GLOBAL\_Q value IQN(VarName) ; N = 1 to 30

For C++ variables:

IQ(VarName) ; GLOBAL\_Q value

IQN(VarName); N = 1 to 30



## Step 4: Modifying IQmath variable

The watch window does not allow the modification of variables that are not of native type. To facilitate this, the following GEL operations can be found under the GEL toolbar:

### **IQ C Support**

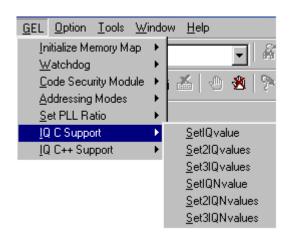
SetIQvalue ; GLOBAL Q format

Set2IQvalues

Set3IQvalues

SetIQNvalue ; IQN format

Set2IQNvaluesSet3IQNvalues



## IQ C++ Support

SetIQvalue ; GLOBAL Q format

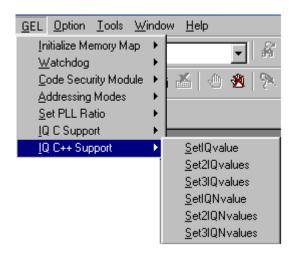
Set2lQvalues

Set3IQvalues

SetIQNvalue ; IQN format

Set2IQNvalues

Set3IQNvalues



Invoking one of the above GEL operations will bring up a dialogue box window, which the user can enter the variable name and the floating-point value to set. The function will convert the float value to the appropriate IQ value.

# 3.10. Converting an IQmath Application to Floating-Point

To convert an IQmath application to floating point, follow these steps:

- 1. In the IQmath header file, select FLOAT\_MATH. The header file will convert all IQmath function calls to their floating-point equivalent.
- 2. When writing a floating-point number into a device register, you need to convert the floating-point number to an integer. Likewise when reading a value from a register it will need to be converted to float. In both cases, this is done by multiplying the number by a conversion factor.

For example to convert a floating-point number to IQ15, multiply by 32768.0.

```
#if MATH_TYPE == IQ_MATH
    PwmReg = (int16)_IQtoIQ15(Var1);
#else // MATH_TYPE is FLOAT_MATH
    PwmReg = (int16)(32768.0L*Var1);
#endif
```

Likewise, to convert from an IQ15 value to a floating-point value, multiply by 1/32768.0 or 0.00030518.0.

Note: The integer range is restricted to 24-bits for a 32-bit floating-point value.

- 3. If your device has the on-chip floating-point processing unit (C28x+FPU), then you can take advantage of the on-chip floating point unit by doing the following:
  - Use C28x codegen tools version 5.0.2 or later.
  - Tell the compiler it can generate native C28x floating-point code. To do this, use the -v28 --float\_support=fpu32 compiler switches. In Code Composer Studio the float\_support switch is on the advanced tab of the compiler options.
  - Use the correct run-time support library for native 32-bit floating-point. For C code this is rts2800\_fpu32.lib. For C++ code with exception handling, use rts2800\_fpu32\_eh.lib.
  - Use the C28x FPU Fast RTS library (SPRC664) to get a performance boost from math functions such as sin, cos, div, sqrt, and atan. The Fast RTS library should be linked in before the normal run-time support library.

# 3.11. The IQmath C-Calling Convention

All of the IQmath functions strictly adhere to the C28x C-Calling conventions. To understand the C28x C-Calling convention, Please refer Chapter 7 (Run-time Environment) of TMC320C28x Optimizing C/C++ Compiler User's Guide (SPRU514).

# **Chapter 4. Libraries Available**

This chapter lists the builds available for the IQmath source.

### IQmath.lib

The IQmath.lib library has been built for use on standard C28x fixed-point devices. This library can be used with both C and C++ code.

## IQmath\_fpu32.lib

The IQmath\_fpu32.lib library is useful for users who want to use both IQmath functions as well as native C28x floating-point code within their project. This library can be used with both C and C++ code.

The IQmath fpu32.lib library has been built with the following compiler flags:

IQmath\_fpu32.lib still contains the same IQmath functions as IQmath.lib. It does not contain native floating-point functions. The float\_support option is available in the C28x compiler version 5.0.0 and later.

# **Chapter 5. Function Summary**

The routines included within the IQmath library are organized as follows

□ Format conversion utilities : atoIQ, IQtoF, IQtoIQN etc.

□ Arithmetic Functions : IQmpy, IQdiv etc.

□ Trigonometric Functions : IQsin, IQcos, IQatan2 etc.

□ Mathematical functions : IQsqrt, IQisqrt etc.□ Miscellaneous : IQabs, IQsat etc

# 5.1. Arguments and Conventions Used

The following convention has been followed when describing the arguments for each individual function:

QN	16-bit fixed point Q number, where N=1:15
IQN	32-bit fixed point Q number, where N=1:31
int	16-bit number
long	32-bit number
_iq	_iq is the C-code data type definition equating a long, a 32-bit value representing a GLOBAL_Q number. Usage of _iq instead of long is recommended to increase future portability across devices.  For C++ code the iq class is used instead.
_iqN	_iqN is the C-code data type definition equating a long, a 32-bit value representing a IQN number, where N=1:30  For C++ code, the iqN class is used instead.
iq	C++ iq class for handling the _iq data type.
iqN	C++ iqN class for handling the _iqN data type.
A, B	Input operand to IQmath function or Macro
F	Floating point input: Ex: -1.232, +22.433, 0.4343, -0.32
S	Floating point string: "+1.32", "0.232", "-2.343" etc
Р	Positive Saturation value
N	Negative Saturation value

# 5.2. IQmath Function Overview

# **Format conversion Utilities**

Functions	Description	IQ format
_iq _IQ(float F)	Converts float to IQ value	Q=GLOBAL_Q
_iqN _IQN(float F)		Q=1:30
float _IQtoF(_iq A)	IQ to Floating point	Q=GLOBAL_Q
float _IQNtoF( _iqN A)		Q=1:30
_iq _atoIQ( char *S)	Float ASCII string to IQ	Q=GLOBAL_Q
_iqN _atoIQN( char *S)		Q=1:30
int _IQtoa(char *S, const * format, long x)	IQ to ASCII string	Q=GLOBAL_Q
int _IQNtoa(char *S, const * format, long x)		Q=1:30
long _IQint( _iq A)	extract integer portion of IQ	Q=GLOBAL_Q
long _IQNint( _iqN A)		Q=1:30
_iq _lQfrac( _iq A)	extract fractional portion of IQ	Q=GLOBAL_Q
_iqN _IQNfrac( _iqN A)		Q=1:30
_iqN _IQtoIQN( _iq A)	Convert IQ number to IQN number (32-bit)	Q=GLOBAL_Q
_iq _IQNtoIQ( _iqN A)	Convert IQN (32-bit) number to IQ number	Q=GLOBAL_Q
int _IQtoQN( _iq A)	Convert IQ number to QN number (16-bit)	Q=GLOBAL_Q
_iq _QNtoIQ( int A)	Convert QN (16-bit) number to IQ number	Q=GLOBAL_Q

# **Arithmetic Operations**

Functions	Description	IQ format
_iq _IQmpy( _iq A, _iq B)	IQ Multiplication	Q=GLOBAL_Q
_iqN _IQNmpy( _iqN A, _iqN B)		Q=1:30
_iq _IQrmpy( _iq A, _iq B)	IQ Multiplication with rounding	Q=GLOBAL_Q
_iqN _IQNrmpy( _iqN A, _iqN B)		Q=1:30
_iq _IQrsmpy( _iq A, _iq B)	IQ multiplication with rounding & saturation	Q=GLOBAL_Q
_iqN _IQNrsmpy( _iqN A, _iqN B)		Q=1:30
_iq _IQmpyl32( _iq A, long B)	Multiply IQ with "long" integer	Q=GLOBAL_Q
_iqN _IQNmpyl32( _iqN A, long B)		Q=1:30
long _IQmpyl32int( _iq A, long B)	Multiply IQ with "long", return integer	Q=GLOBAL_Q
long _IQNmpyl32int( _iqN A, long B)	part	Q=1:30
long _IQmpyl32frac( _iq A, long B)	Multiply IQ with "long", return fraction	Q=GLOBAL_Q
long _IQNmpyl32frac( _iqN A, long B)	part	Q=1:30
_iq _IQmpyIQX( _iqN1 A, N1, _iqN2 B, N2 )	Multiply two 2-different IQ number	Q=GLOBAL_Q
_iqN _lQmpylQX( _iqN1 A, N1, _iqN2 B, N2 )		Q=1:30
_iq _IQdiv( _iq A, _iq B)	Fixed point division	Q=GLOBAL_Q
_iqN _lQNdiv( _iqN A, _iqN B)		Q=1:30

**Trigonometric Functions:** 

Functions	Description	IQ format
_iq _IQasin(_iq A)	High precision ASIN (output in radians)	Q=GLOBAL_Q
_iqN _IQNasin( _iqN A)		Q=1:29
_iq _lQsin(_iq A)	High precision SIN (input in radians)	Q=GLOBAL_Q
_iqN _IQNsin( _iqN A)		Q=1:29
_iq _IQsinPU( _iq A)	High precision SIN (input in per-unit)	Q=GLOBAL_Q
_iqN _IQNsinPU( _iqN A)		Q=1:30
_iq _IQacos(_iq A)	High precision ACOS (output in radians)	Q=GLOBAL_Q
_iqN _IQNacos( _iqN A)		Q=1:30
_iq _IQcos(_iq A)	High precision COS (Input in radians)	Q=GLOBAL_Q
_iqN _IQNcos( _iqN A)		Q=1:29
_iq _IQcosPU( _iq A)	High precision COS (input in per-unit)	Q=GLOBAL_Q
_iqN _IQNcosPU( _iqN A)		Q=1:30
_iq _IQatan2( _iq A, _iq B)	4-quadrant ATAN (output in radians)	Q=GLOBAL_Q
_iqN _IQNatan2( _iqN A, _iqN B)		Q=1:29
_iq _IQatan2PU( _iq A, _iq B)	4-quadrant ATAN (output in per-unit)	Q=GLOBAL_Q
_iqN _IQNatanPU( _iqN A, _iqN B)		Q=1:29
_iq _IQatan( _iq A, _iq B)	Arctangent	Q=GLOBAL_Q
_iqN _IQNatan( _iqN A, _iqN B)		Q=1:29

# **Mathematical Functions:**

Functions	Description	IQ format
_iq _IQexp(_iq A)	High precision e raised to the A power	Q=GLOBAL_Q
_iqN _IQNexp( _iqN A)		Q=1:29
_iq _IQsqrt(_iq A)	High precision square root	Q=GLOBAL_Q
_iqN _IQNsqrt( _iqN A)		Q=1:30
_iq _IQisqrt(_iq A)	High precision inverse square root	Q=GLOBAL_Q
_iqN _IQNisqrt( _iqN A)		Q=1:30
_iq _IQmag( _iq A, _iq B)	Magnitude Square: sqrt(A^2 + B^2)	Q=GLOBAL_Q
_iqN _IQNmag( _iqN A, _iqN B)		Q=1:30

# Miscellaneous

Functions	Description	Q format	
_iq _IQsat(_iq A, long P, long N)	Saturate the IQ number	Q=GLOBAL_Q	
_iq _lQabs( _iq A)	Absolute value of IQ number	Q=GLOBAL_Q	

# 5.3. C28x IQmath Library Benchmarks

Function Name	IQ Format	Execution Cycles	Accuracy (in bits)	Program Memory (words)	Input format	Output format	Remarks
	I I		Trigonometr	ic Functions			
IQNasin	1-29	154		82 words	IQN	IQN	Note A
IQNsin	1-29	46	30 bits	49 words	IQN	IQN	
IQNsinPU	1-30	40	30 bits	41 words	IQN	IQN	
IQNacos	1-29	170		93 words	IQN	IQN	Note A
IQNcos	1-29	44	30 bits	47 words	IQN	IQN	
IQNcosPU	1-30	38	29 bits	39 words	IQN	IQN	
IQNatan2	1-29	109	26 bits	123 words	IQN	IQN	
IQNatan2PU	1-29	117	27 bits	136 words	IQN	IQN	
IQatan	1-29	109	25 bits	123 words	IQN	IQN	
			Mathematic	al Functions	1		•
IQNexp	1-29	190		61 words	IQN	IQN	Note A
IQNsqrt	1-30	63	29 bits	66 words	IQN	IQN	
IQNisqrt	1-30	64	29 bits	69 words	IQN	IQN	
IQNmag	1-30	86	29 bits	96 words	IQN	IQN	
			Arithmetic	Functions	1		•
IQNmpy	1-30	~ 6	32 bits	NA	IQN*IQN	IQN	INTRINSIC
IQNrmpy	1-30	17	32 bits	13 words	IQN*IQN	IQN	
IQNrsmpy	1-30	21	32 bits	21 words	IQN*IQN	IQN	
IQNmpyl32	1-30	~ 4	32 bits	NA	IQN*long	IQN	C-MACRO
IQNmpyl32int	1-30	22	32 bits	16 words	IQN*long	long	
IQNmpyl32frac	1-30	24	32 bits	20 words	IQN*long	IQN	
IQNmpyIQX		~ 7	32 bits	NA	IQN*IQN	IQN	INTRINSIC
IQNdiv	1-30	63	28 bits	71 words	IQN/IQN	IQN	
		ı	Format Conve	ersion Utilitie	S		
IQN	1-30	NA	N/A	NA	Float	IQN	C-MACRO
IQNtoF	1-30	22	N/A	20 words	IQN	Float	
IQNtoa	1-30	N/A	N/A	210 words	IQN	string	
atoIQN	1-30	N/A	N/A	143 words	char *	IQN	
IQNint	1-30	14	32 bits	8 words	IQN	long	
IQNfrac	1-30	17	32 bits	12 words	IQN	IQN	
IQtoIQN	1-30	~4	N/A	N/A	GLOBAL_Q	IQN	C-MACRO
IQNtoIQ	1-30	~4	N/A	N/A	IQN	GLOBAL_Q	C-MACRO
IQtoQN	1-15	~4	N/A	N/A	GLOBAL_Q	QN	C-MACRO
QNtoIQ	1-15	~4	N/A	N/A	QN	GLOBAL_Q	C-MACRO
Miscellaneous							
IQsat	1-30	~7	N/A	N/A	IQN	IQN	INTRINSIC
IQNabs	1-30	~2	N/A	N/A	IQN	IQN	INTRINSIC

### Notes:

- A. IQNexp, IQNasin and IQNacos use look-up tables in the IQmathTablesRam section. Refer to Section 3.3.
- B. Execution cycles & Program memory usage mentioned in the Table assumes IQ24 format. Execution cycles may vary by few cycles for some other IQ format. Program memory may vary by few words for some other IQ format.
- C. Execution Cycles mentioned in the table includes the CALL and RETURN (LCR + LRETR) and it assumes that the IQmath table is loaded in internal memory.
- D. Accuracy should always be verified and tested within the end application.

# **Chapter 6. Function Descriptions**

# 6.1. Conversion Utilities

Usage

IQN Float to IQN data type

Description This C-macro converts a floating-point constant or variable to the equivalent IQ

value

Declaration Global IQ Macro (IQ format = GLOBAL\_Q)

```
C _iq _IQ(float F)
C++ iq IQ(float F)
```

Q format specific IQ Macro (IQ format = IQ1 to IQ29)

```
C _iqN _IQN(float F)
C++ iq IQN(float F)
```

**Input** Floating point variable or constant

Output Global IQ Macro (IQ format = GLOBAL\_Q)

Fixed point equivalent of floating-point input in GLOBAL Q format

This operation is typically used to convert a floating-point constant or variable to

Q format specific IQ Macro (IQ format = IQ1 to IQ29)

Fixed point equivalent of floating-point input in IQN format

the equivalent IQ value.

#### **Example 1:** Implement an equation in IQmath

```
// Floating-point equation
Y = M*1.26 + 2.345

// IQmath equation using the GLOBAL_Q value
Y =_IQmpy(M, _IQ(1.26)) + _IQ(2.345)

// IQmath equation specifying the Q value
Y =_IQ23mpy(M, _IQ23(1.26)) +_IQ23(2.345)
```

### **Example 2:** Convert a floating-point variable to an IQ data type.

# **Example 3:** Initialize global variables or tables

#### Description

This function converts an IQ number to equivalent floating-point value in IEEE 754 format.

#### Declaration

### Global IQ function (IQ format = GLOBAL\_Q)

```
C float _IQtoF(_iq A)
C++ float IQtoF(const iq &A)
```

### Q format specific IQ function (IQ format = IQ1 to IQ30)

```
C float _IQNtoF(_iqN A)
C++ float IQNtoF(const iqN &A)
```

### Input

# Global IQ function (IQ format = GLOBAL\_Q)

Fixed point IQ number in GLOBAL Q format.

#### Q format specific IQ function (IQ format = IQ1 to IQ30)

Fixed point IQ number in IQN format.

#### Output

Floating point equivalent of fixed-point input.

### **Usage**

This operation is typically used in cases where the user may wish to perform some operations in floating-point format or convert data back to floating-point for display purposes.

### Example:

Convert an array of IQ numbers to their equivalent floating-point values

atolQN String to IQN

# **Description** This function converts a string to an IQ number.

#### Declaration Global IQ function (IQ format = GLOBAL\_Q)

```
C float _atoIQ(char *S)
C++ float atoIQ(char *S)
```

## Q format specific IQ function (IQ format = IQ1 to IQ30)

```
C float _atoIQN(char *S)
C++ float atoIQN(char *S)
```

## Input

This function recognizes (in order) an optional sign, a string of digits optionally containing a radix character.

Valid Input strings:

```
"12.23456", "-12.23456", "0.2345", "0.0", "0", "127", "-89"
```

#### Output

The first unrecognized character ends the string and returns zero. If the input string converts to a number greater then the max/min values for the given Q value, then the returned value will be limited to the min/max values

### Global IQ function (IQ format = GLOBAL Q)

Fixed point equivalent of input string in GLOBAL\_Q format

# Q format specific IQ function (IQ format = IQ1 to IQ29)

Fixed point equivalent of input string in IQN format

# Usage

This is useful for programs that need to process user input or ASCII strings.

#### **Example:**

The following code prompts the user to enter the value X:

```
char buffer[N];
_iq X;

printf("Enter value X = ");
gets(buffer);
X = _atoIQ(buffer);  // IQ value (GLOBAL_Q)
```

IQN to String **IQNtoa** 

#### Description

This function converts an IQ number to a string.

#### Declaration

## Global IQ function (IQ format = GLOBAL Q)

```
int _IQtoa(char *string, const char *format, _iq x)
C++
      int IQtoa(char *string, const char *format,
                const iq &x)
```

#### Q format specific IQ function (IQ format = IQ1 to IQ30)

```
int _IQNtoa(char *string, const char *format, _iqN x)
C++
      int IQNtoa(char *string, const char *format,
                 const iqN &x)
```

#### Input

string: output string

format: conversion format. Must be of the form "%xx.yyf" with

xx and yy at most 2 characters in length. For Example: "%10.12f", "%2.4f", "%11.6f"

The maximum supported integer field width (xx) is 11 (including any negative sign). This captures the full integer range for I2Q30 to I31Q1

numbers.

x: Global IQ function: input value in IQ format

Q format specific function: input value in IQN format

#### Output

The output string is returned in the location pointed to by the "string" argument.

If you are using MATH\_TYPE set to IQ\_MATH, then the return integer value is an error code with the following possible values:

0 = no error

1 = width too small to hold integer characters

2 = illegal format specified

If you are using MATH TYPE set to FLOAT MATH, then sprintf() is called and the return integer value is the number of characters written.

### Usage

- Any leading zeros are not printed for the integer part. Hence, the format specifies the maximum width of the integer field. The field may be smaller.
- The output string is terminated with the null character.
- The integer width in "format" includes the negative sign for negative numbers, e.g. -12.3456 is "%3.5f"
- The decimal width in "format" includes the decimal point. For example: -12.3456 is "%3.5f"
- "string" must be large enough to hold the output (including the negative sign, and the terminating null character). The program does not check for overrun. Memory corruption will occur if "string" is too small.
- A non-zero return value indicates that the output string is invalid.

## Example:

```
char buffer[30];
   _iq     x1 = _IQ(1.125);
   _iq1     x2 = _IQ1(-6789546.3);
   _iq14     x3 = _IQ14(-432.6778);
   _iq30     x4 = _IQ30(1.127860L);
int error;

// Global_Q
   error = _IQtoa(buffer, "%10.10f", x1);

// IQ1
   error = _IQ1toa(buffer, "%8.2f", x2);

// IQ14
   error = _IQ14toa(buffer, "%6.6f", x3);

// IQ30
   error = _IQ30toa(buffer, "%11.12f", x4);
```

**Description** This function returns the integer portion of IQ number.

### Declaration Global IQ function (IQ format = GLOBAL Q)

```
C long _IQint(_iq A)
C++ long IQint(const iq &A)
```

#### Q format specific IQ function (IQ format = IQ1 to IQ30)

```
C long _IQNint(_iqN A)
C++ long IQNint(const iqN &A)
```

### Input Global IQ function (IQ format = GLOBAL\_Q)

Fixed point IQ number in GLOBAL\_Q format.

## Q format specific IQ function (IQ format = IQ1 to IQ30)

Fixed point IQ number in IQN format.

# Output Integer part of the IQ number

### Usage Example 1:

Extract the integer and fractional part of an IQ number.

```
_iq Y0 = 2.3456;
_iq Y1 = -2.3456
long Y0int, Y1int;
_iq Y0frac, Y1frac;

Y0int = _IQint(Y0);  // Y0int = 2
Y1int = _IQint(Y1);  // Y1int = -2
Y0frac = _IQfrac(Y0);  // Y0frac = 0.3456
Y1frac = _IQfrac(Y1);  // Y1frac = -0.3456
```

#### Example 2:

Build an IQ number from an integer and fractional part

```
_iq Y;
long Yint;
_iq Yfrac;
Y = _IQmpyI32(_IQ(1.0), Yint) + Yfrac;
```

**Description** This function returns the fractional portion of IQ number.

## Declaration Global IQ function (IQ format = GLOBAL Q)

```
C _iq _IQfrac(_iq A)
C++    iq IQfrac(const iq &A)
```

#### Q format specific IQ function (IQ format = N = 1 to 30)

```
C _iqN _IQNfrac(_iqN A)
C++ iqN IQNfrac(const iqN &A)
```

### Input Global IQ function (IQ format = GLOBAL\_Q)

Fixed point IQ number in GLOBAL\_Q format.

## Q format specific IQ function (IQ format = IQ1 to IQ30)

Fixed point IQ number in IQN format.

Output Fractional part of the IQ number

### Usage Example 1:

Extract the integer and fractional part of an IQ number

```
_iq Y0 = _IQ(2.3456);
_iq Y1 = _IQ(-2.3456);
long Y0int, Y1int;
_iq Y0frac, Y1frac;

Y0int = _IQint(Y0);  // Y0int = 2
Y1int = _IQint(Y1);  // Y1int = -2
Y0frac = _IQfrac(Y0);  // Y0frac = 0.3456
Y1frac = _IQfrac(Y1);  // Y1frac = -0.3456
```

### Example 2:

Build an IQ number from an integer and fractional part.

```
_iq Y;
long Yint;
_iq Yfrac;
Y = _IQmpyI32(_IQ(1.0), Yint) + Yfrac;
```

# **IQtoIQN**

Description This Macro converts an IQ number in GLOBAL\_Q format to the specified IQ

format.

**Declaration** C \_\_iqN \_\_IQtoIQN(\_\_iq A)

C++ iqN IQtoIQN(const iq &A)

**Input** IQ number in GLOBAL\_Q format

Output Equivalent value of input in IQN format

Usage This macro may be used in cases where a calculation may temporarily overflow the IQ value resolution and hence require a different IQ value to be used for the

intermediate operations.

# Example:

The Following example calculates the magnitude of complex number (X+jY) in Q26 format:

```
Z = sqrt(X^2 + Y^2)
```

The values Z, X, Y are given as  $GLOBAL_Q = 26$ , but the equation itself may generate an overflow.

To guard against this, the intermediate calculations will be performed using Q = 23 and the value converted back at the end as shown below:

**Description** This Macro converts an IQ number in IQN format to the GLOBAL\_Q format.

Declaration C \_\_iq \_\_IQNtoIQ(\_iqN A)

C++ iq IQNtoIQ(const iqN &A)

**Input** IQ number in IQN format

Output Equivalent value of input in GLOBAL\_Q format

Usage This macro may be used in cases where the result of the calculation performed in different IQ resolution to be converted to GLOBAL Q format.

# Example:

Following example calculates the magnitude of complex number (X+jY) in Q26 format:

```
Z = sqrt(X^2 + Y^2)
```

The values Z, X, Y are given as  $GLOBAL_Q = 26$ , but the equation itself may generate an overflow. To guard against this, the intermediate calculations will be performed using Q = 23 and the value converted back at the end as shown below:

# **IQtoQN**

**Description** This Macro converts a 32-bit number in GLOBAL\_Q format to 16-bit number in

QN format.

**Declaration** C int \_IQtoQN(\_iq A)

C++ int IQtoQN(const iq &A)

**Input** IQ number in GLOBAL\_Q format

Output Equivalent value of input in QN format (16-bit fixed point number)

**Usage** This macro may be used in cases where the input and output data is 16-bits, but the intermediate operations are operated using IQ data types.

#### Example:

Sum of product computation using the input sequence that is not in GLOBAL\_Q format:

```
Y = X0*C0 + X1*C1 + X2*C2 // X0, X1, X2 in Q15 format //C0,C1, C2 in GLOBAL_Q format
```

We can convert the Q15 values to IQ, perform the intermediate sums using IQ and then store the result back as Q15:

**Description** This Macro converts a 16-bit number in QN format to 32-bit number in

GLOBAL\_Q format.

**Input** 16-bit fixed point number in QN format

Output Equivalent value of input in GLOBAL\_Q format

**Usage** This macro may be used in cases where the input and output data is 16-bits, but the intermediate operations are operated using IQ data types.

# Example:

Sum of product computation using the input sequence that is not in GLOBAL\_Q format:

```
Y = X0*C0 + X1*C1 + X2*C2 // X0, X1, X2 in Q15 format // C0, C1, C2 in GLOBAL_Q format
```

We can convert the Q15 values to IQ, perform the intermediate sums using IQ and then store the result back as Q15:

# 6.2. Arithmetic Operations

# **IQNmpy**

IQ Multiplication (IQN\*IQN)

#### Description

This C compiler intrinsic multiplies two IQ number. It does not perform saturation and rounding. In most cases, the multiplication of two IQ variables will not exceed the range of the IQ variable. This operation takes the least amount of cycles and code size and should be used most often.

#### Declaration

# Global IQ intrinsic (IQ format = GLOBAL\_Q)

```
C _iq _IQmpy(_iq A, _iq B)
C++ iq operator * (const iq &A, const iq &B)
    iq &iq :: operator *= (const iq &A)
```

#### Q format specific IQ intrinsic (IQ format = IQ1 to IQ30)

```
C _iqN _IQNmpy(_iqN A, _iqN B)
C++ iqN operator * (const iqN &A, const iqN &B)
    iqN &iqN :: operator *= (const iqN &A)
```

#### Input

# Global IQ intrinsic (IQ format = GLOBAL Q)

Inputs A and B are IQ numbers in GLOBAL\_Q format

#### Q format specific IQ intrinsic (IQ format = IQ1 to IQ30)

Inputs A and B are IQ numbers in IQN format

#### Output

# Global IQ intrinsic (IQ format = GLOBAL Q)

Result of multiplication in GLOBAL Q format

## Q format specific IQ intrinsic (IQ format = IQ1 to IQ30)

Result of multiplication in IQN format.

#### Usage

#### Example 1;

Compute Y = M\*X + B in GLOBAL\_Q format with no rounding or saturation.

```
_iq Y, M, X, B;
Y = _IQmpy(M,X) + B;
```

#### Example 2:

Compute Y = M\*X + B in IQ10 format with no rounding or saturation, assuming M, X, B are represented in IQ10 format.

```
_iq10 Y, M, X, B;
Y = _IQ10mpy(M,X) + B;
```

# **IQNrmpy**

#### Description

This function multiplies two IQ number and rounds the result. In cases where absolute accuracy is necessary, this operation performs the IQ multiply and rounds the result before storing back as an IQ number. This gives an additional 1/2 LSBit of accuracy.

#### Declaration

#### Global IQ function (IQ format = GLOBAL Q)

#### Q format specific IQ function (IQ format = IQ1 to IQ30)

#### Input

# Global IQ function (IQ format = GLOBAL\_Q)

Input "A" & "B" are IQ number in GLOBAL\_Q format

#### Q format specific IQ function (IQ format = IQ1 to IQ30)

Input "A" & "B" are IQ number in IQN format

#### Output

#### Global IQ function (IQ format = GLOBAL Q)

Result of multiplication in GLOBAL\_Q format

# Q format specific IQ function (IQ format = IQ1 to IQ30)

Result of multiplication in IQN format.

#### **Usage**

#### Example 1:

Compute Y = M\*X + B in GLOBAL\_Q format with rounding but without saturation.

# Example 2:

Compute Y = M\*X + B in IQ10 format with rounding but without saturation.

```
_iq10 Y, M, X, B;
Y = _IQ10rmpy(M,X) + B;
```

This function multiplies two IQ number with rounding and saturation. In cases where the calculation may possibly exceed the range of the IQ variable, then this operation will round and then saturate the result to the maximum IQ value range before storing.

#### **Declaration**

#### Global IQ function (IQ format = GLOBAL Q)

```
C _iq _IQrsmpy(_iq A, _iq B)
C++ iq IQrsmpy(iq &A, iq &B)
```

#### Q format specific IQ function (IQ format = IQ1 to IQ30)

```
C _iqN _IQNrsmpy(_iqN A, _iqN B)
C++ iqN IQNrsmpy(const iqN &A, const iqN &B)
```

#### Input

# Global IQ function (IQ format = GLOBAL\_Q)

Input "A" & "B" are IQ number in GLOBAL Q format

## Q format specific IQ function (IQ format = IQ1 to IQ30)

Input "A" & "B" are IQ number in IQN format

#### Output

#### Global IQ function (IQ format = GLOBAL\_Q)

Result of multiplication in GLOBAL Q format

#### Q format specific IQ function (IQ format = IQ1 to IQ30)

Result of multiplication in IQN format.

#### Usage

Let us assume that we use IQ26 are GLOBAL\_Q format. This means that the range of the numbers is approximately [-32.0, 32.0] (Refer section 3.2). If two IQ variables are multiplied together, then the maximum range of the result is [-1024, 1024]. This operation would make sure that the result is saturated to +/- 32 in cases where the result exceeds this.

#### Example 1:

Compute  $Y = M^*X$  in the GLOBAL\_Q format with rounding and saturation. Assume GLOBAL\_Q=IQ26 in the IQmath header file.

```
_iq Y, M, X;

M=_IQ(10.9);  // M=10.9

X=_IQ(4.5);  // X=4.5

Y = _IQrmpy(M,X); // Y= ~32.0, output is Saturated to MAX
```

#### Example 2:

Compute  $Y = M^*X$  in IQ26 format with rounding and saturation.

# **Description** This macro multiplies an IQ number with a long integer.

#### Declaration Global IQ Macro (IQ format = GLOBAL Q)

```
C _iq _IQmpyI32(_iq A, long B)
C++ iq IQmpyI32(const iq &A, long B)
```

# Q format specific IQ Macro (IQ format = IQ1 to IQ30)

```
C _iqN _IQNmpyI32( _iqN A, long B)
C++ iqN IQNmpyI32(const iqN &A, long B)
```

#### Input Global IQ Macro (IQ format = GLOBAL Q)

Operand A is an IQ number in GLOBAL\_Q format and B is the long integer.

# Q format specific IQ Macro (IQ format = IQ1 to IQ30)

Operand A is an IQ number in IQN format and B is the long integer.

#### Output Global IQ Macro (IQ format = GLOBAL Q)

Result of multiplication in GLOBAL\_Q format

# Q format specific IQ Macro (IQ format = IQ1 to IQ30)

Result of multiplication in IQN format.

# Usage Example 1:

Compute Y = 5\*X in the GLOBAL\_Q format. Assume GLOBAL\_Q =IQ26 in the IQmath header file.

#### Example 2:

Compute Y = 5\*X in IQ26 format.

```
_iq26 Y, X;
long M;
M=5;  // M=5
X = _IQ26(5.1);  // X=5.1 in IQ29 format
Y = _IQ26mpyI32(X,M);  // Y=25.5 in IQ29 format
```

This function multiplies an IQ number with a long integer and returns the integer part of the result.

#### Declaration

#### Global IQ function (IQ format = GLOBAL Q)

```
C long _IQmpyI32int(_iq A, long B)
C++ long IQmpyI32int(const iq &A, long B)
```

#### Q format specific IQ function (IQ format = IQ1 to IQ30)

```
C long _IQNmpyI32int(_iqN A, long B)
C++ long IQNmpyI32int(const iqN &A, long B)
```

#### Input

#### Global IQ function (IQ format = GLOBAL\_Q)

Operand "A" is an IQ number in GLOBAL\_Q format and "B" is the long integer.

#### Q format specific IQ function (IQ format = IQ1 to IQ30)

Operand "A" is an IQ number in IQN format and "B" is the long integer.

#### Output

# Global IQ function (IQ format = GLOBAL\_Q)

Integer part of the result (32-bit)

# Q format specific IQ function (IQ format = IQ1 to IQ30)

Integer part of the result (32-bit)

#### Usage

#### Example 1

Convert an IQ value in the range [-1.0, +1.0] to a DAC value with the range [0 to 1023]:

```
_iq Output;
long temp;
short OutputDAC;

// value converted to +/- 512
    temp = _IQmpyI32int(Output, 512);
// value scaled to 0 to 1023
    temp += 512;
// saturate within range of DAC
    if( temp > 1023 )temp = 1023;
    if( temp < 0 ) temp = 0;
// output to DAC value
    OutputDAC = (int )temp;</pre>
```

Note: The integer operation performs the multiply and calculates the integer portion from the resulting 64-bit calculation. Hence it avoids any overflow conditions.

This function multiplies an IQ number with a long integer and returns the fractional part of the result.

#### Declaration

#### Global IQ function (IQ format = GLOBAL Q)

```
C _iq _IQmpyI32frac(_iq A, long B)
C++ iq IQmpyI32frac(const iq &y, long x)
```

# Q format specific IQ function (IQ format = IQ1 to IQ30)

```
C _iqN _IQNmpyI32frac( _iqN A, long B)
C++ iqN IQNmpyI32frac(const iqN &A, long B)
```

#### Input

#### Global IQ function (IQ format = GLOBAL\_Q)

Operand A is an IQ number in GLOBAL\_Q format and B is a long integer.

# Q format specific IQ function (IQ format = IQ1 to IQ30)

Operand A is an IQ number in IQN format and B is the long integer.

#### Output

# Global IQ function (IQ format = GLOBAL\_Q)

Fractional part of the result (32-bit)

# Q format specific IQ function (IQ format = IQ1 to IQ30)

Fractional part of the result (32-bit)

#### **Usage**

#### **Example:**

The following example extracts the fractional part of result after multiplication (Assuming GLOBAL Q=IQ26)

```
_iq X1= _IQ(2.5);
_iq X2= _IQ26(-1.1);
_iq Y1frac, Y2frac;
long M1=5, M2=9;

// Y1frac = 0.5 in GLOBAL_Q
    Y1frac = IQmpyI32frac(X1, M1);
// Y2frac = -0.9 in GLOBAL_Q
    Y2frac = IQ26mpyI32frac(X2, M2);
```

This C compiler intrinsic multiplies two IQ number that are represented in different IQ format

#### Declaration

#### Global IQ Intrinsic (IQ format = GLOBAL Q)

```
C _iq _IQmpyIQX(_iqN1 A, int N1, _iqN2 B, int N2)
C++ iq IQmpyIQX(iqN1 A, int N1, iqN2 B, int N2)
```

# Q format specific IQ Intrinsic (IQ format = IQ1 to IQ30)

```
C _iqN _IQNmpyIQX(_iqN1 A, int N1, _iqN2 B, int N2)
C++ iqN IQNmpyIQX(iqN1 A, int N1, iqN2 B, int N2)
```

#### Input

Operand "A" is an IQ number in "IQN1" format and operand "B" is in "IQN2" format.

#### Output

#### Global IQ Intrinsic (IQ format = GLOBAL Q)

Result of the multiplication in GLOBAL\_Q format

#### Q format specific IQ Intrinsic (IQ format = IQ1 to IQ30)

Result of the multiplication in IQN format

#### **Usage**

This operation is useful when we wish to multiply values of different IQ.

#### Example:

Calculate the following equation: Y = X0\*C0 + X1\*C1 + X2\*C2

#### Where

```
X0, X1, X2 values are in IQ30 format (Range -2 to +2) C0, C1, C2 values are in IQ28 format (Range -8 to +8)
```

The maximum range of Y will be -48 to +48. Therefore, we will store the result in an IQ format that is less then IQ25.

#### Case 1: GLOBAL Q=IQ25

#### Case 2: IQ Specific computation

**IQNdiv** Fixed-point division

#### Description

This module divides two IQN number and provide 32-bit quotient (IQN format) using Newton-Raphson technique

#### Declaration

#### Global IQ function (IQ format = GLOBAL Q)

```
_iq _IQdiv(_iq A, _iq B)
C++
       iq operator / (const iq &A, const iq &B)
       iq &iq :: operator /= (const iq &A)
```

#### Q format specific IQ function (IQ format = IQ1 to IQ30)

```
_iqN _IQNdiv(_iqN A, iq B)
C++
       iqN operator / (const iqN &A, const iqN &B)
       iqN &iqN :: operator /= (const iqN &A)
```

#### Input

# Global IQ function (IQ format = GLOBAL\_Q)

Input "A" & "B" are fixed-point number represented in GLOBAL Q format.

# Q format specific IQ function (IQ format = IQ1 to IQ30)

Input 'A' & 'B' are fixed-point number in IQN format (N=1:30)

#### Output

#### Global IQ function (IQ format = GLOBAL Q)

Output in GLOBAL Q format.

# Q format specific IQ function (IQ format = IQ1 to IQ30)

Output in IQN format (N=1:30)

# Accuracy

= 
$$20\log_2(2^{31}) - 20\log_2(7)$$
 = 28 bits

# Usage

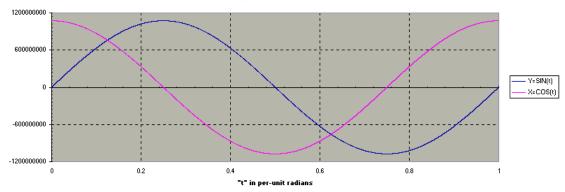
#### **Example:**

The following example obtains  $\frac{1}{15} = 0.666$  assuming that GLOBAL Q is set to Q28 format in the IQmath header file.

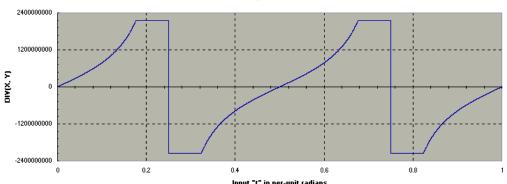
```
#include "IQmathLib.h"
_iq in1 out1;
_iq28 in2 out2;
void main(void )
   in1 = _{IQ}(1.5);
   out1 = _{IQdiv(_{IQ}(1.0), in1)};
   in2 = IQ28(1.5);
   out2 = IQ28div(IQ28(1.0), in2);
}
```

# Fixed Point division vs. C Float division

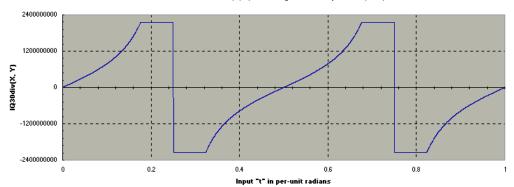




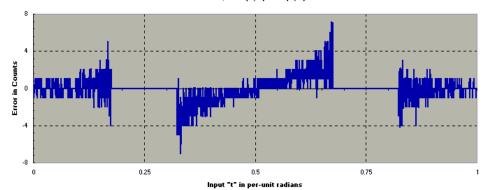
#### DIV(X, Y)-Floating Point Computation (Q30)



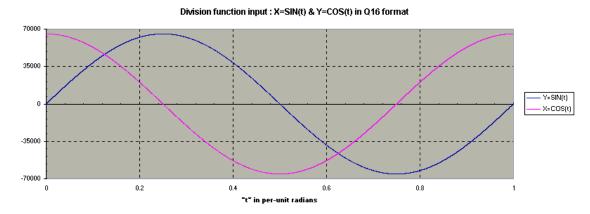
#### IQ30div(X, Y) - Floating Point Computation(Q30)

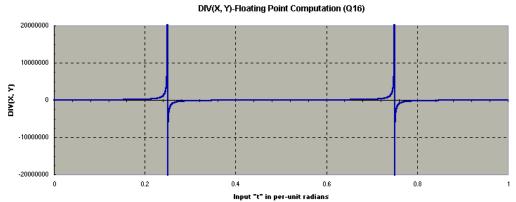


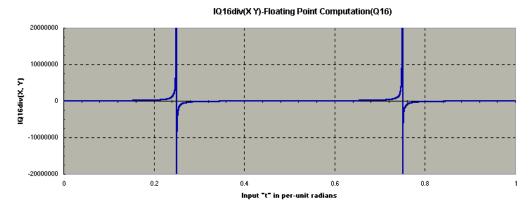
# Error=IQ30div(X, Y) - DIV(X, Y)

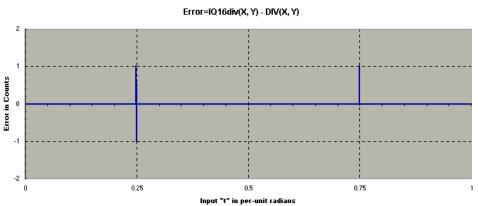


# Fixed Point division vs. C Float division









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# 6.3. Trigonometric Functions

**IQNasin** 

Fixed point ASIN (radians)

#### Description

This module computes the inverse sine of the input and returns the result in radians.

#### Declaration

#### Global IQ function (IQ format = GLOBAL Q)

```
C _iq _IQasin(_iq A)
C++ iq IQasin(const iq &A)
```

# Q format specific IQ function (IQ format = IQ1 to IQ29)

```
C _iqN _IQNasin(_iqN A)
C++ iqN IQNasin(const iqN &A)
```

#### Input

#### Global IQ function (IQ format = GLOBAL Q)

Input argument is in radians and represented as fixed-point number in GLOBAL Q format.

#### Q format specific IQ function (IQ format = IQ1 to IQ29)

Input argument is in radians and represented as fixed-point number in IQN format (N=1:29).

# Output

### Global IQ function (IQ format = GLOBAL\_Q)

This function returns the inverse sine of the input argument as fixed-point number in GLOBAL\_Q format.

#### Q format specific IQ function (IQ format = IQ1 to IQ29)

This function returns the inverse sine of the input argument as fixed-point number in IQN format (N=1:29)

# **Example**

The following example obtains the result of the equation  $asin(0.70710678) = (.25 \times pi)$ . It assumes that GLOBAL\_Q is set to Q29 format in the IQmath header file.

```
#include "IQmathLib.h"
#define PI 3.14156
_iq in1, out1;
_iq29 in2, out2;

void main(void)
{
// in1 = in2 = 0.70710678L x 2^29 = 0x16A09E60
// out1 = out2 = asin(0.70710678) = 0x1921FB4A

in1 =_IQ(0.70710678L);
out1 =_IQasin(in1);

in2 =_IQ29(0.70710678L)
out2 =_IQ29asin(in2);
}
```

This module computes the sine value of the input (in radians) using table look-up and Taylor series expansion between the look-up table entries.

#### **Declaration**

#### Global IQ function (IQ format = GLOBAL Q)

```
C _iq _IQsin(_iq A)
C++ iq IQsin(const iq &A)
```

#### Q format specific IQ function (IQ format = IQ1 to IQ29)

#### Input

# Global IQ function (IQ format = GLOBAL Q)

Input argument is in radians and represented as fixed-point number in GLOBAL\_Q format.

#### Q format specific IQ function (IQ format = IQ1 to IQ29)

Input argument is in radians and represented as fixed-point number in IQN format (N=1:29).

# Output

#### Global IQ function (IQ format = GLOBAL Q)

This function returns the sine of the input argument as fixed-point number in GLOBAL Q format.

# Q format specific IQ function (IQ format = IQ1 to IQ29)

This function returns the sine of the input argument as fixed-point number in IQN format (N=1:29)

# Accuracy

= 
$$20\log_2(\pi \times 2^{29}) - 20\log_2(1) = 30$$
 bits

#### Example

The following example obtains sin (0.25 x pi) = 0.707 assuming that GLOBAL\_Q is set to Q29 format in the IQmath header file.

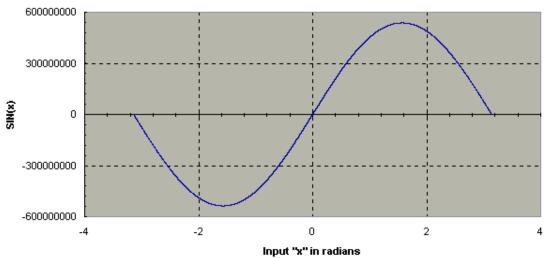
```
#include "IQmathLib.h"
#define PI 3.14156
_iq in1, out1;
_iq28 in2, out2;

void main(void ) {
    // in1 = 0.25 x pi x 2^29 = 0x1921FB54
    // out1 = sin(0.25 x pi)x 2^29 = 0x16A09E66
    // in2 = 0x25 x pi x 2^29 = 0x1921FB54
    // out2 = sin(0.25 x pi)x 2^29 = 0x16A09E66

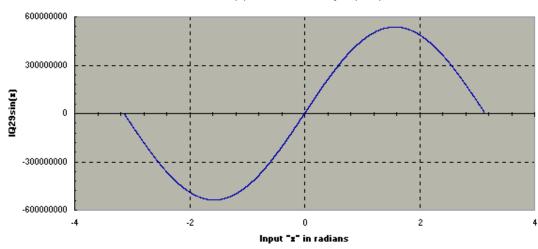
    in1=_IQ(0.25*PI);
    out1=_IQsin(in1)
    in2=_IQ29(0.25*PI)
    out2=_IQ29sin(in2);
}
```

# **IQNsin Function vs. C Float SIN:** Input varies from $-\pi$ to $\pi$

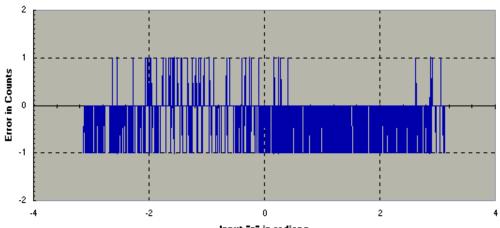




# IQ29sin(x)- Fixed Point Output (Q29)



# Error=IQ29sin(x) - SIN(x)



© Input "s" in radians 52

This module computes the sine value of the input (in per-unit radians) using table look-up and Taylor series expansion between the look-up table entries.

#### **Declaration**

#### Global IQ function (IQ format = GLOBAL\_Q)

```
C _iq _IQsinPU(_iq A)
C++ iq IQsinPU(const iq &A)
```

#### Q format specific IQ function (IQ format = IQ1 to IQ30)

#### Input

#### Global IQ function (IQ format = GLOBAL Q)

Input argument is in per-unit radians and represented as fixed-point number in GLOBAL Q format.

# Q format specific IQ function (IQ format = IQ1 to IQ30)

Input argument is in per-unit radians and represented as fixed-point number in IQN format (N=1:30).

#### Output

### Global IQ function (IQ format = GLOBAL\_Q)

This function returns the sine of the input argument as fixed-point number in GLOBAL\_Q format.

# Q format specific IQ function (IQ format = IQ1 to IQ30)

This function returns the sine of the input argument as fixed-point number in IQN format (N=1:30)

# Accuracy

= 
$$20\log_2(1\times2^{30}) - 20\log_2(1) = 30$$
 bits

#### Usage

#### Example:

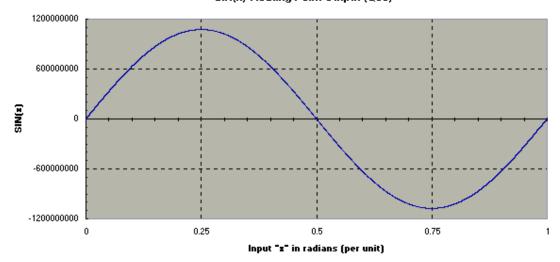
The following example obtains the  $\sin(0.25 \times \pi) = 0.707$  assuming that GLOBAL Q is set to Q30 format in the IQmath header file.

```
#include "IQmathLib.h"
#define PI 3.14156
_iq in1, out1;
_iq30 in2, out2;

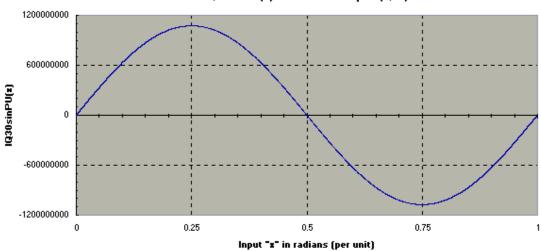
void main(void) {
// in1 = (0.25 x PI)/(2PI) x 2^30 = 0x08000000
// out1 = sin(0.25 x PI)x 2^30 = 0x2D413CCC
// in2 = (0.25 x PI)/(2PI) x 2^30 = 0x08000000
// out2 = sin(0.25 x PI)x 2^30 = 0x2D413CCC

in1 =_IQ(0.25L*PI);
   out1 =_IQsinPU(in1)
   in2 =_IQ30(0.25*PI/PI);
   out2 =_IQ30sinPU(in2);
}
```

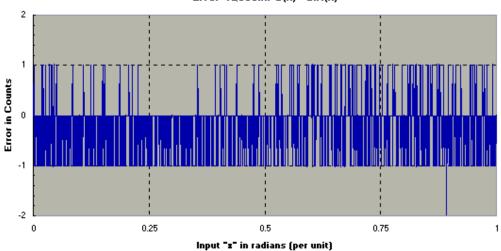
**IQNsinPU Function vs. C Float SIN:** Input varies from 0 to  $2\pi$  in per unit representation SIN(x)-Floating Point Output (Q30)



# IQ30sinPU(x)- Fixed Point Ouput (Q30)



# Error=IQ30sinPU(x) - SIN(x)



This module computes the inverse cosine of the input and returns the result in radians.

#### Declaration

## Global IQ function (IQ format = GLOBAL\_Q)

```
C _iq _IQacos(_iq A)
C++ iq IQacos( const iq & A)
```

#### Q format specific IQ function (IQ format = N = 1 to 29)

```
C _iqN _IQNacos(_iqN A)
C++ iq N IQNacos(const iqN &A)
```

#### Input

#### Global IQ function (IQ format = GLOBAL\_Q)

Input argument is in radians and represented as fixed-point number in GLOBAL Q format.

#### Q format specific IQ function (IQ format = IQ1 to IQ29)

Input argument is in radians and represented as fixed-point number in IQN format (N=1:29).

#### Output

# Global IQ function (IQ format = GLOBAL\_Q)

This function returns the inverse cosine of the input argument as fixed-point number in GLOBAL\_Q format.

#### Q format specific IQ function (IQ format = IQ1 to IQ29)

This function returns the inverse cosine of the input argument as fixed-point number in IQN format (N=1:29)

#### Example

The following example obtains the result of  $a\sin(0.70710678) = (0.25 \times \pi)$  assuming that GLOBAL Q is set to Q29 format in the IQmath header file.

```
#include "IQmathLib.h"
   _iq in1, out1;
   _iq29 in2, out2;

void main(void)
{
// in1 = 0x70710678 x 2^29 = 0x16A09E60
// out1 = acos(0.70710678L) x 2^29 = 0x1921FB5E
// in2 = 0x70710678 x 2^29 = 0x16A09E60
// out2 = acos(0.70710678L) x 2^29 = 0x1921FB5E

   in1 =_IQ(0.70710678L);
   out1 =_IQacos(in1);
   in2 =_IQ29(0.70710678L)
   out2 =_IQ29acos(in2);
}
```

# **IQNcos**

# Description

This module computes the cosine value of the input (in radians) using table lookup and Taylor series expansion between the look up table entries.

#### **Declaration**

#### Global IQ function (IQ format = GLOBAL\_Q)

```
C _iq _IQcos(_iq A)
C++ iq IQcos(const iq &A)
```

#### Q format specific IQ function (IQ format = IQ1 to IQ29)

#### Input

#### Global IQ function (IQ format = GLOBAL Q)

Input argument is in radians and represented as fixed-point number in GLOBAL Q format.

# Q format specific IQ function (IQ format = IQ1 to IQ29)

Input argument is in radians and represented as fixed-point number in IQN format (N=1:29).

### Output

### Global IQ function (IQ format = GLOBAL\_Q)

This function returns the cosine of the input argument as fixed-point number in GLOBAL\_Q format.

# Q format specific IQ function (IQ format = IQ1 to IQ29)

This function returns the cosine of the input argument as fixed-point number in IQN format (N=1:29)

# Accuracy

= 
$$20\log_2(\pi \times 2^{29}) - 20\log_2(2)$$
 = 30 bits

# Example

The following example obtains the  $\cos(0.25 \times \pi)$ =0.707 assuming that GLOBAL Q is set to Q29 format in the IQmath header file.

```
#include "IQmathLib.h"
#define PI 3.14156

_iq in1, out1;
_iq29 in2 out2;

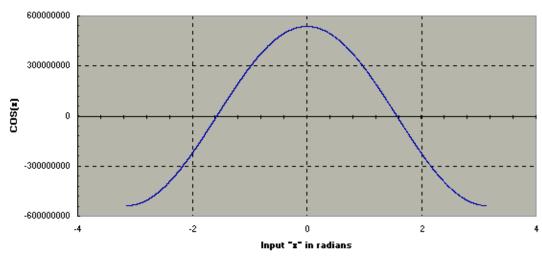
void main(void ) {
    // in = 0.25 x PI x 2^29 = 0x1921FB54
    // out1 = cos(.25 x PI) x 2^29 = 0x16A09E66
    // in = 0.25 x PI x 2^29 = 0x1921FB54
    // out1 = cos(.25 x PI) x 2^29 = 0x16A09E66

    in1 =_IQ(0.25 * PI) x 2^29 = 0x16A09E66

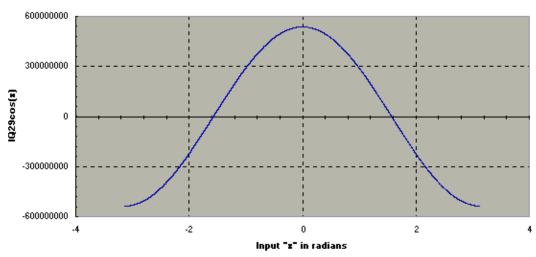
    in1 =_IQ(0.25 * PI);
    out1 =_IQcos(in1);
    in2 =_IQ29(0.25 * PI);
    out2 =_IQ29cos(in2);
}
```

# Fixed Point COS Function vs. C Float COS: Input varies from $-\pi$ to $\pi$

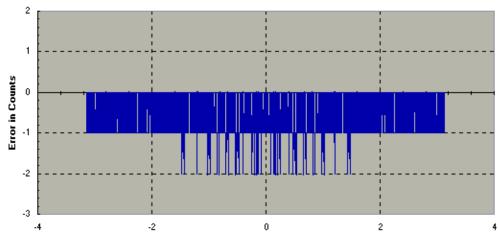
# COS(x)-Floating Point Output (Q29)



# IQ29cos-Fixed Point Output (Q29)







©T Input "z" in radians 57

This module computes the cosine value of the input (in per-unit radians) using table look-up and Taylor series expansion between the look up table entries.

#### **Declaration**

#### Global IQ function (IQ format = GLOBAL Q)

```
C _iq _IQcosPU(_iq A)
C++ iq IQcosPU(const iq &A)
```

#### Q format specific IQ function (IQ format = IQ1 to IQ30)

```
C _iqN _IQNcosPU(_iqN A)
C++ iqN IQNcosPU(const iqN &A)
```

#### Input

# Global IQ function (IQ format = GLOBAL Q)

Input argument is in per-unit radians and represented as fixed-point number in GLOBAL Q format.

# Q format specific IQ function (IQ format = IQ1 to IQ30)

Input argument is in per-unit radians and represented as fixed-point number in IQN format (N=1:30).

#### Output

# Global IQ function (IQ format = GLOBAL\_Q)

This function returns the sine of the input argument as fixed-point number in GLOBAL\_Q format.

#### Q format specific IQ function (IQ format = IQ1 to IQ30)

This function returns the sine of the input argument as fixed-point number in IQN format (N=1:30)

# Accuracy

$$=20\log_2(1\times2^{30})-20\log_2(2)$$
 = 29 bits

#### **Usage**

**Example:** The following sample code obtains the  $\cos(0.25 \times \pi) = 0.707$  assuming that GLOBAL\_Q is set to Q30 format in the IQmath header file.

```
#include "IQmathLib.h"
#define PI 3.14156

_iq in1, out1;
_iq30 in2, out2

void main(void ){
// in1 = in2 = (0.25 x PI)/(2PI) x 2^30 = 0x08000000
// out1 = out2 = cos(0.25 x PI) x 2^30 = 0x2D413CCC

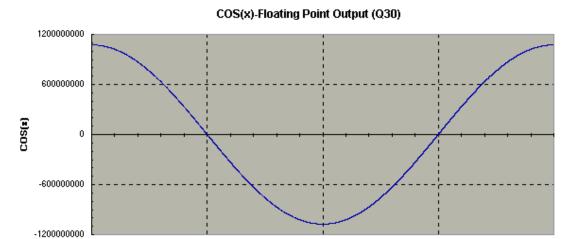
in1 =_IQ(0.25*PI/PI);
out1 =_IQcosPU(in1)

in2 =_IQ30(0.25*PI/PI);
out2 =_IQ30cosPU(in2);
}
```

0.75

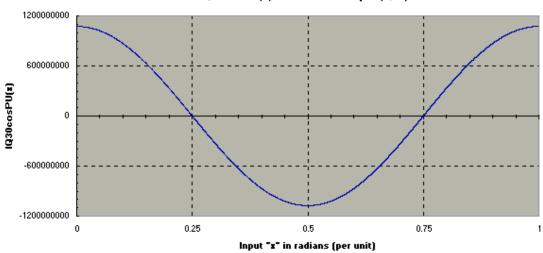
Fixed Point COS Function vs. C Float COS: Input varies from 0 to  $2\pi$  in per unit

0.25

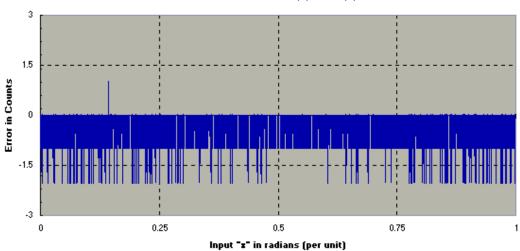


# IQ30cosPU(x)- Fixed Point Output (Q30)

Input "x" in radians (per unit)



# Error=IQ30cosPU(x) - COS(x)



This module computes 4-quadrant arctangent. Output of this module is in radians that varies from  $-\pi$  to  $\pi$ 

#### **Declaration**

# Global IQ function (IQ format = GLOBAL\_Q)

```
C _iq _IQatan2(_iq A, _iq B)
C++ iq IQatan2(const iq &A, const iq &B)
```

# Q format specific IQ function (IQ format = IQ1 to IQ29)

```
C _iqN _IQNatan2(_iqN A, _iqN B)
C++ iqN IQNatan2(const iqN &A, const iqN &B)
```

#### Input

#### Global IQ function (IQ format = GLOBAL Q)

Inputs A and B are fixed-point numbers represented in GLOBAL Q format.

#### Q format specific IQ function (IQ format = IQ1 to IQ29)

Inputs A and B are fixed-point numbers in IQN format (N=1:29)

#### Output

# Global IQ function (IQ format = GLOBAL\_Q)

This function returns the inverse tangent of the input argument as fixed-point number in GLOBAL\_Q format. The output contains the angle in radians between  $[-\pi,+\pi]$ 

# Q format specific IQ function (IQ format = IQ1 to IQ29)

This function returns the inverse tangent of the input argument as fixed-point number in IQN format (N=1:29). The output contains the angle in radians between  $[-\pi,+\pi]$ 

# Accuracy

= 
$$20\log_2(\pi \times 2^{29}) - 20\log_2(32) = 26$$
 bits

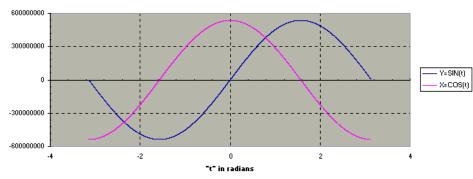
# **Usage**

The following example obtains  $\tan^{-1}(\sin(\frac{\pi}{5}),\cos(\frac{\pi}{5})) = \frac{\pi}{5}$ , assuming that the GLOBAL Q is set to Q29 format in the IQmath header file.

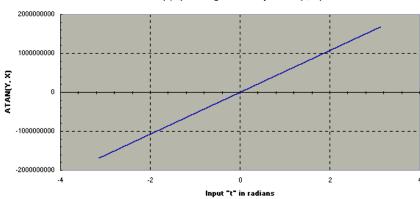
```
#include "IQmathLib.h"
#define
          PI 3.14156L
_iq xin1, yin1, out1;
_iq29 xin2, yin2, out2;
void main(void ) {
// xin1 = xin2 = cos(PI/5) x 2^29 = 0x19E37FA8
// yin1 = yin2 = sin(PI/5) \times 2^29 = 0x12CF17EF
 // out1 = out2 = PI/5 x 2^29 = 0x141B21C3
    xin1 = _{IQcos(_{IQ}(PI/5.0L))};
    yin1 = _{IQsin(_{IQ}(PI/5.0L))};
    out1 = _IQatan2(yin1, xin1);
    xin2 = _{IQ29cos(_{IQ29(PI/5.0L))};}
    vin2 = IO29sin(IO29(PI/5.0L));
    out2 = _{IQ29atan2(yin1,xin1)};
}
```

# **Fixed Point ARCTAN Function vs. C Float ARCTAN**

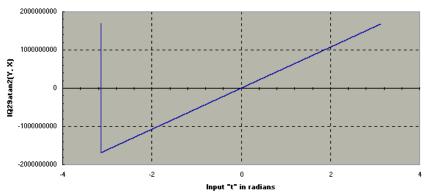




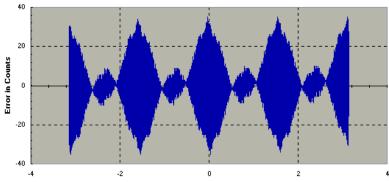
#### ATAN(Y, X)-Floating Point Computation (Q29)



#### IQ29atan2(Y, X)-Floating Point Computation(Q29)



# Error=IQ29atan2(Y, X) - ATAN(Y, X)



©Texas Insti Input "t" in radians 61

This module computes 4-quadrant arctangent. Output of this module is in per unit radians that varies from 0 (0 radians) to 1 ( $2\pi$  radians).

#### **Declaration**

#### Global IQ function (IQ format = GLOBAL Q)

```
C _iq _IQatan2PU(_iq A, _iq B)
C++ iq IQatan2PU(const iq &A, const iq &B)
```

#### Q format specific IQ function (IQ format = IQ1 to IQ29)

```
C _iqN _IQNatan2PU(_iqN A, _iqN B)
C++ iqN IQNatan2PU(const iqN &A, const iqN &B)
```

#### Input

# Global IQ function (IQ format = GLOBAL\_Q)

Inputs A and B are fixed-point number represented in GLOBAL Q format.

#### Q format specific IQ function (IQ format = IQ1 to IQ29)

Input A and B are fixed-point number in IQN format (N=1:29)

#### Output

#### Global IQ function (IQ format = GLOBAL Q)

This function returns the inverse tangent of the input argument as fixed-point number in GLOBAL\_Q format. The output contains the angle in per unit radians that varies from 0 (0 radians) to 1 ( $2\pi$  radians).

#### Q format specific IQ function (IQ format = IQ1 to IQ29)

This function returns the inverse tangent of the input argument as fixed-point number in IQN format (N=1:29). The output contains the angle in per unit radians that varies from 0 (0 radians) to 1 ( $2\pi$  radians).

# Accuracy

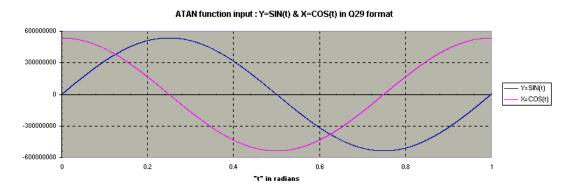
= 
$$20\log_2(1\times2^{29}) - 20\log_2(6) = 27$$
 bits

# Usage

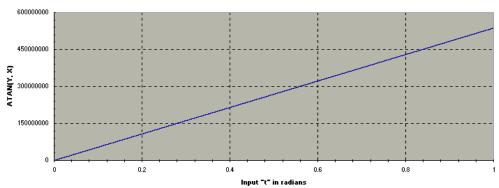
The following sample code obtains  $\tan^{-1}(\sin(\frac{\pi}{5}),\cos(\frac{\pi}{5})) = \frac{\pi}{5}$ , assuming that GLOBAL\_Q is set to Q29 format in the IQmath header file.

```
#include "IQmathLib.h"
         PI 3.14156L
#define
_iq xin1, yin1, out1;
_iq29 xin2, yin2, out2;
void main(void ) {
// xin1 = xin2 = cos(PI/5) x 2^29 = 0x19E37FA8
// yin1 = yin2 = sin(PI/5) \times 2^29 = 0x12CF17EF
 // \text{ out1} = \text{out2} = (PI/5)/(2PI) \times 2^29 = 0x03333104
    xin1 = _{IQcos(_{IQ}(PI/5.0L))};
    vin1 = IQsin(IQ(PI/5.0L));
    out1 = IQatan2PU(yin1,xin1);
    xin2 = _{IQ29cos(_{IQ29(PI/5.0L))};}
    vin2 = IO29sin(IO29(PI/5.0L));
    out2 = _{IQ29atan2PU(yin1,xin1)};
}
```

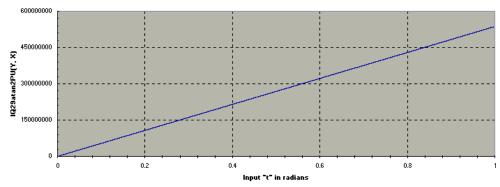
# **Fixed Point ARCTAN Function vs. C Float ARCTAN**



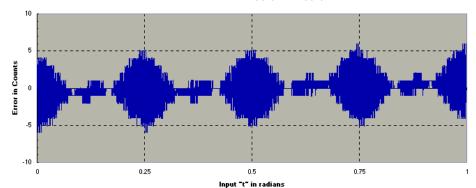




#### IQ29atan2PU(Y, X)-Floating Point Computation(Q29)



#### Error=IQ29atan2PU(Y, X) - ATAN(Y, X)



#### **IQNatan**

#### Description

This module computes arctangent. Output of this module is in radians that vary from  $-\frac{\pi}{2}$  to  $\frac{\pi}{2}$ .

#### **Declaration**

# Global IQ Macro (IQ format = GLOBAL\_Q)

# Q format specific IQ Macro (IQ format = IQ1 to IQ29)

#### Input

#### Global IQ function (IQ format = GLOBAL Q)

Input argument is a fixed-point number in GLOBAL\_Q format.

### Q format specific IQ function (IQ format = IQ1 to IQ29)

Input argument is a fixed-point number in IQN format (N=1:30)

#### Output

#### Global IQ function (IQ format = GLOBAL\_Q)

This function returns the inverse tangent of the input argument as fixed-point number in GLOBAL\_Q format. The output contains the angle in radians between  $\begin{bmatrix} -\pi/2, +\pi/2 \end{bmatrix}$ 

# Q format specific IQ function (IQ format = IQ1 to IQ29)

This function returns the inverse tangent of the input argument as fixed-point number in IQN format (N=1:29). The output contains the angle in radians between  $\left[-\frac{\pi}{2}, +\frac{\pi}{2}\right]$ 

# Accuracy

= 
$$20 \log_2 \left( \frac{\pi}{2} \times 2^{29} \right) - 20 \log_2 (2) = 25$$
 bits

#### **Usage**

The following example obtains  $\tan^{-1}(1) = \frac{\pi}{4}$ , assuming that GLOBAL\_Q is set to Q29 format in the IQmath header file.

```
#include "IQmathLib.h"
_iq in1, out1;
_iq29 in2, out2;

void main(void)
{
  in1 = _IQ(1.0L);
  out1 =_IQatan(in1);
  in2 =_IQ29(1.0L);
  out2 =_IQ29atan(in2)
}
```

#### 6.4. Mathematical Utilities

IQNexp Fixed point Exponential

**Description** This module computes the exponential of a value A.

# Declaration Global IQ function (IQ format = GLOBAL\_Q)

C \_iq \_IQexp(\_iq A)
C++ iq IQexp(const iq &A)

#### Q format specific IQ function (IQ format = IQ1 to IQ30)

C \_iqN \_IQNexp(\_iqN A)
C++ iqN IQNexp(const iqN &A)

# Input Global IQ function (IQ format = GLOBAL Q)

Input argument is a fixed-point number in GLOBAL\_Q format.

#### Q format specific IQ function (IQ format = IQ1 to IQ30)

Input argument is a fixed-point number in IQN format (N=1:30).

### Output Global IQ function (IQ format = GLOBAL\_Q)

Exponential value of the input in GLOBAL Q format.

#### Q format specific IQ function (IQ format = IQ1 to IQ30)

Exponential value of the input in IQN format (N=1:30).

#### Example

Calculate e(1.8) = 6.0496474, assuming that GLOBAL\_Q is set to Q24 format in the IQmath header file.

```
#include "IQmathLib.h"
_iq in1, out1;
_iq30 in2, out2;

void main(void )
{
// in1 = in2 = 1.8 x 2^24 = 0x01CCCCCC
// out1 = out2 = exp(1.8) x 2^24 = 0x060CB5AA

in1 = _IQ(1.8);
out1 = _IQexp(x);

in2 = _IQ24(1.8);
out2 = _IQ24exp(x);
}
```

This module computes the square root of the input using table lookup and Newton-Raphson approximation.

#### **Declaration**

# Global IQ function (IQ format = GLOBAL\_Q)

# Q format specific IQ function (IQ format = IQ1 to IQ30)

#### Input

#### Global IQ function (IQ format = GLOBAL Q)

Input argument is a fixed-point number in GLOBAL\_Q format.

# Q format specific IQ function (IQ format = IQ1 to IQ30)

Input argument is a fixed-point number in IQN format (N=1:30)

#### Output

#### Global IQ function (IQ format = GLOBAL Q)

Square root of input in GLOBAL\_Q format.

# Q format specific IQ function (IQ format = IQ1 to IQ30)

Square root of input in IQN format (N=1:30)

# Accuracy

$$= 20\log_2(2^{31}) - 20\log_2(6) = 29 \text{ bits}$$

# Usage

Calculate  $\sqrt{1.8}$  = 1.34164, assuming that GLOBAL\_Q is set to Q30 format in IQmath header file.

```
#include "IQmathLib.h"
_iq in1, out1;
_iq30 in2, out2;

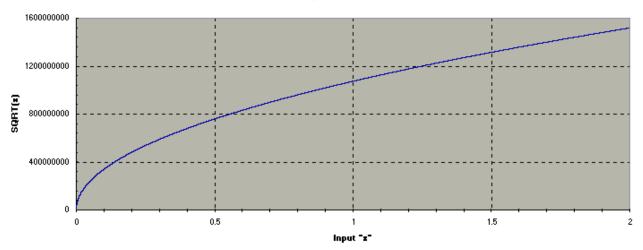
void main(void)
{
// in1 = in2 = 1.8 x 2^30 = 0x73333333
// out1 = out2 = sqrt(1.8) x 2^30 = 0x55DD7151

in1 = _IQ(1.8);
out1 = _IQsqrt(x);

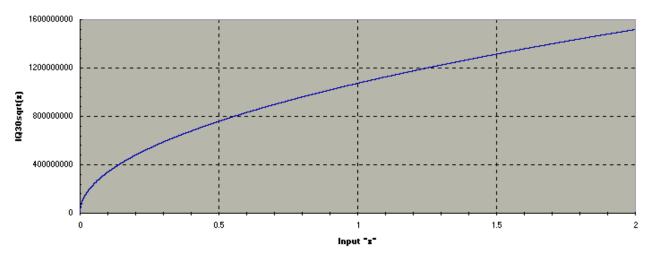
in2 = _IQ30(1.8);
out2 = _IQ30sqrt(x);
}
```

# **Fixed Point SQRT Function vs. C Float SQRT**

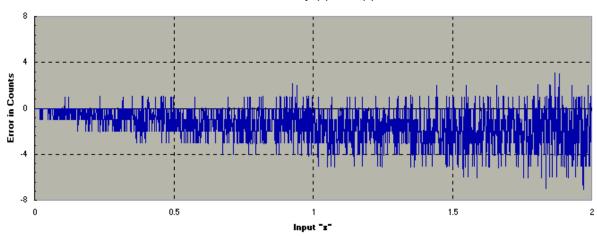
# SQRT(x)-Floating Point Computation (Q30)



# IQ30sqrt(x)-Floating Point Computation (Q30)



# Error=IQ30sqrt(x)-SQRT(x)



# **IQNisgrt**

# Description

This module computes the inverse square root of the input using table lookup and Newton-Raphson approximation.

#### **Declaration**

#### Global IQ function (IQ format = GLOBAL Q)

#### Q format specific IQ function (IQ format = IQ1 to IQ30)

#### Input

# Global IQ function (IQ format = GLOBAL\_Q)

Input argument is a fixed-point number in GLOBAL Q format.

# Q format specific IQ function (IQ format = IQ1 to IQ30)

Input argument is a fixed-point number in IQN format (N=1:30)

#### Output

#### Global IQ function (IQ format = GLOBAL\_Q)

Inverse square-root of the input expressed in GLOBAL Q format.

# Q format specific IQ function (IQ format = IQ1 to IQ30)

Inverse square root of input expressed in IQN format (N=1:30)

# Accuracy

= 
$$20\log_2(2^{31}) - 20\log_2(5) = 29$$
 bits

# **Usage**

Calculate  $\frac{1}{\sqrt{1.8}}$  =0.74535 assuming that GLOBAL\_Q is set to Q30 format in the IQmath header file.

```
#include "IQmathLib.h"
_iq in1, out1;
_iq30 in2, out2;

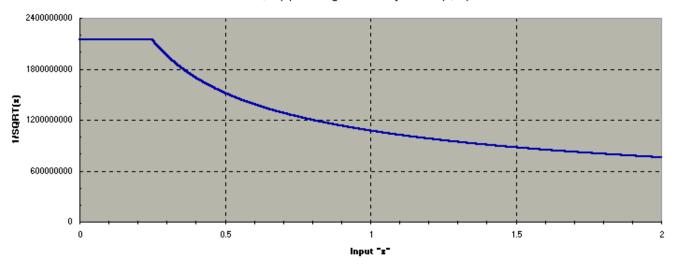
void main(void)
{

// in1 = in2 = 1.8 x 2^30 = 0x73333333
// out1 = out2 = 1/sqrt(1.8) x 2^30 = 0x2FB3E99E
    in1 =_IQ(1.8);
    out1 =_IQisqrt(in1);

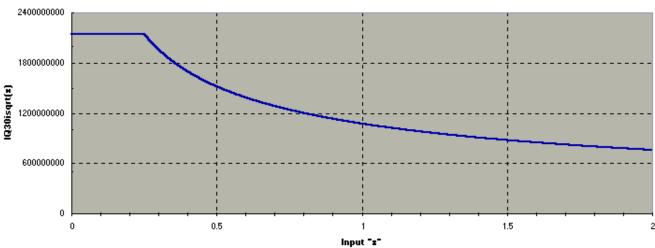
    in2 =_IQ30(1.8);
    out2 =_IQ30isqrt(in2);
}
```

# Fixed Point inverse SQRT Function vs. C Float inverse SQRT

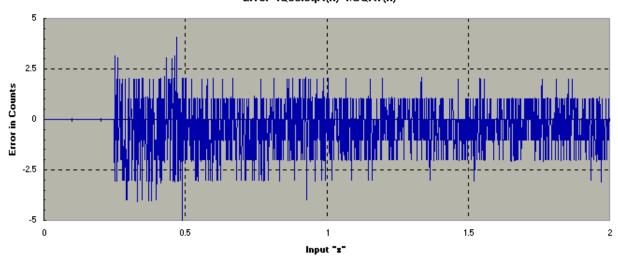
#### 1/SQRT(x)-Floating Point Computation (Q30)



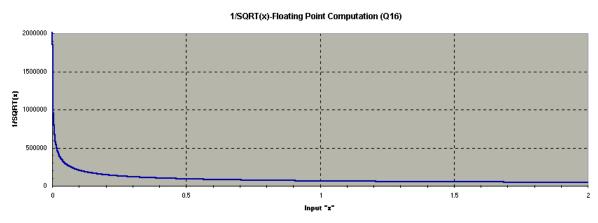
# IQ30isqrt(x)-Fixed Point Computation (Q30)

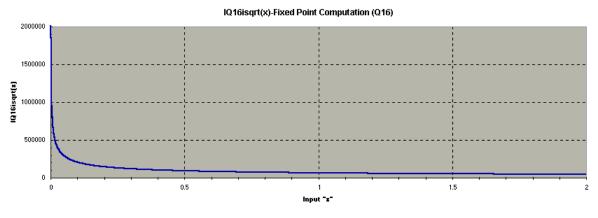


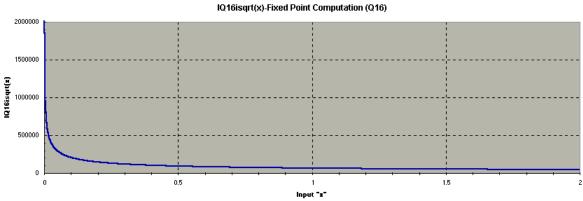
# Error=IQ30isqrt(x)-1/SQRT(x)

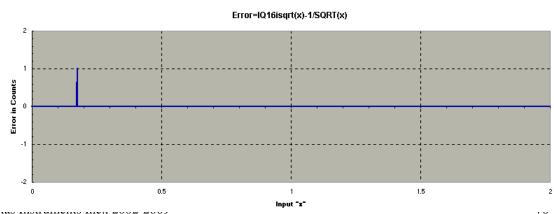


# Fixed Point inverse SQRT Function vs. C Float inverse SQRT









This function calculates the magnitude of two orthogonal vectors as follows: Mag =  $sqrt(A^2 + B^2)$ . This operation achieves better accuracy and avoids overflow problems that may be encountered by using the "\_IQsqrt" function.

#### **Declaration**

#### Global IQ function (IQ format = GLOBAL\_Q)

```
C _iq _IQmag(_iq A, _iq B)
C++ iq IQmag(const iq &A, const iq &B)
```

# Q format specific IQ function (IQ format = IQ1 to IQ30)

```
C _iqN _IQNmag(_iqN A, _iqN B)
C++ iqN IQNmag(const iqN &A, const iqN &B)
```

#### Input

#### Global IQ function (IQ format = GLOBAL Q)

Inputs A and B are IQ numbers represented in GLOBAL Q format.

# Q format specific IQ function (IQ format = IQ1 to IQ30)

Inputs A and B are IQ numbers represented in IQN format

#### Output

# Global IQ function (IQ format = GLOBAL\_Q)

Magnitude of the input vector in GLOBAL Q format

#### Q format specific IQ function (IQ format = IQ1 to IQ30)

Magnitude of the input vector in IQN format

#### Accuracy

29-bits (Same as SQRT function)

## Usage

## Example:

The following sample code obtains the magnitude of the complex number (Assuming GLOBAL\_Q=IQ28).

```
#include "IQmathLib.h"
// Complex number = real1 + j*imag1
// Complex number = real2 + j*imag2

_iq real1, imag1, mag1;
_iq28 real2, imag2, mag2;

void main(void)
{

// mag1 = 5.6568 in IQ28 format
    real1 = _IQ(4.0);
    imag1 = _IQ(4.0);
    mag1 = _IQmag(real1, imag1);

// mag2 =~8.0, saturated to MAX value (IQ28)!!!
    real2 = _IQ28(7.0);
    imag2 = _IQ28(7.0);
    imag2 = _IQ28mag(real2, imag2);
}
```

#### 6.5. Miscellaneous Utilities

**IQNabs** 

Absolute value of IQ number

**Description** This intrinsic calculates the absolute value of an IQ number.

Declaration Global IQ function (IQ format = GLOBAL Q)

```
C _iq _IQabs(_iq A)
C++ iq IQabs(const iq &A)
```

Q format specific IQ function (IQ format = IQ1 to IQ30)

```
C _iqN _IQNabs(_iqN A)
C++ iqN IQNabs(const iqN &A)
```

Input Global IQ function (IQ format = GLOBAL\_Q)

IQ number in GLOBAL\_Q format

Q format specific IQ function (IQ format = IQ1 to IQ30)

IQ number in IQN format

Output Global IQ function (IQ format = GLOBAL\_Q)

Absolute value of input in GLOBAL Q format

Q format specific IQ function (IQ format = IQ1 to IQ30)

Absolute value of input in IQN format

Usage Example:

Calculate the absolute sum of three IQ numbers assuming GLOBAL\_Q=IQ28 in the IQmath header file.

```
#include "IQmathLib.h"

void main(void)
{
    _iq xin1, xin2, xin3, xsum;
    _iq20 yin1, yin2, yin3, ysum;

    xsum = _IQabs(X0) + _IQabs(X1) + _IQabs(X2);
    xsum = _IQ28abs(X0) + _IQ28abs(X1) + _IQ28abs(X2);
}
```

This intrinsic saturates an IQ value to the given Positive and Negative limits. This operation is useful in areas where there is potential for overflow in a calculation.

Declaration

ig IQsat( ig A, long P, long N)

Input

Global IQ function (IQ format = GLOBAL Q)

IQ number in GLOBAL\_Q format

Output Format Global IQ function (IQ format = GLOBAL Q)

Saturated output in GLOBAL Q format

Usage

Example:

Calculate the linear equation "Y = M\*X + B", with saturation.

All variables are GLOBAL\_Q = 26. However, there is a possibility that the variable ranges may cause overflow, so we must perform the calculation and saturate the result.

To do this, we perform the intermediate operations using IQ = 20 and then saturate before converting the result back to the appropriate GLOBAL Q value:

# **Chapter 7. Revision History**

Version	Date	Comment
V1.5a	June 1, 2009	Rebuilt the IQmath.lib with large model enabled for the function IQNtoa. No other functions were changed.
		Updated documentation to include 2802x and 2803x devices.
		Added examples for Piccolo 28027 and 28035.
V1.5	July 8, 2008	Added IQNtoa.
		Header IQmathLib.h and IQmathCPP.h files were updated to fix typos and missing information. Refer to the header files themselves for more information.
		Added a version of the library built with the compiler switchfloat_support=fpu32. This enables mixing the IQmath with the native floating support capabilities of C28x+FPU.
		Added information describing how to convert between IQmath and float math.
		Added the IQexp, IQasin, IQacos, and IQNtoa function information to this document.
		Added C++ information to this document. Previously this information was only in a readme.txt file.
		Added information regarding locations of tables stored in the boot ROM of different devices.
		Noted the IQmath .gel file is most useful when using a legacy debugger that does not support IQmath.
		Added examples for 2808, 28335 and 28235. Updated the example flow to better match the header file and peripheral examples also provided by TI.
		General documentation cleanup and improvements.
		Install is now under a version specific directory. Changed the directory structure to reduce the number of duplicated files.
V1.4f	March 10, 2005	Fixed bug in IQexp.
V1.4e	June 17, 2004	Added IQexp, IQasin, IQacos.
V1.4d	March 30, 2003	Previous Web Release