Introduction to R

Regression in R

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Variables of the mtcars dataset

Help for the mtcars dataset:

?mtcars

- mpg Miles/(US) gallon
- cyl Number of cylinders
- disp Displacement (cu.in.)
- hp Gross horsepower
- drat Rear axle ratio
- wt Weight (1000 lbs)
- qsec 1/4 mile time
- vs Engine (0 = V-shaped, 1 = straight)
- am Transmission (0 = automatic, 1 = manual)
- gear Number of forward gears
- carb Number of carburetors

Dataset mtcars

	mpg	cyl	disp	hp	drat	wt	qsec	vs	am	gear	carb
Mazda RX4	21.0	6	160.0	110	3.90	2.620	16.46	0	1	4	4
Mazda RX4 Wag	21.0	6	160.0	110	3.90	2.875	17.02	0	1	4	4
Datsun 710	22.8	4	108.0	93	3.85	2.320	18.61	1	1	4	1
Hornet 4 Drive	21.4	6	258.0	110	3.08	3.215	19.44	1	0	3	1
Hornet Sportabout	18.7	8	360.0	175	3.15	3.440	17.02	0	0	3	2
Valiant	18.1	6	225.0	105	2.76	3.460	20.22	1	0	3	1
Duster 360	14.3	8	360.0	245	3.21	3.570	15.84	0	0	3	4
Merc 240D	24.4	4	146.7	62	3.69	3.190	20.00	1	0	4	2
Merc 230	22.8	4	140.8	95	3.92	3.150	22.90	1	0	4	2
Merc 280	19.2	6	167.6	123	3.92	3.440	18.30	1	0	4	4
Merc 280C	17.8	6	167.6	123	3.92	3.440	18.90	1	0	4	4
Merc 450SE	16.4	8	275.8	180	3.07	4.070	17.40	0	0	3	3

Distributions of two variables of mtcars

```
par(mfrow=c(1,2))
plot(density(mtcars$wt)); plot(density(mtcars$mpg))
```

A simple regression model

Dependent variable - miles per gallon (mpg)

Independent variable - weight (wt)

```
m1 <- lm(mpg ~ wt,data=mtcars)
m1

##

## Call:
## lm(formula = mpg ~ wt, data = mtcars)
##

## Coefficients:
## (Intercept) wt
## 37.285 -5.344</pre>
```

Get the model summary

```
summary(m1)
```

```
##
## Call:
## lm(formula = mpg ~ wt, data = mtcars)
##
## Residuals:
## Min 10 Median 30
                                   Max
## -4.5432 -2.3647 -0.1252 1.4096 6.8727
##
## Coefficients:
##
             Estimate Std. Error t value Pr(>|t|)
## (Intercept) 37.2851 1.8776 19.858 < 2e-16 ***
## wt
      -5.3445 0.5591 -9.559 1.29e-10 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.046 on 30 degrees of freedom
## Multiple R-squared: 0.7528, Adjusted R-squared: 0.7446
## F-statistic: 91.38 on 1 and 30 DF, p-value: 1.294e-10
```

The model formula

Model without intercept

```
m2 <- lm(mpg ~ - 1 + wt,data=mtcars)
summary(m2)$coefficients

## Estimate Std. Error t value Pr(>|t|)
## wt 5.291624 0.5931801 8.920771 4.55314e-10
```

Adding further variables

```
m3 <- lm(mpg ~ wt + cyl,data=mtcars)
summary(m3)$coefficients
```

```
## (Intercept) 39.686261 1.7149840 23.140893 3.043182e-20
## wt -3.190972 0.7569065 -4.215808 2.220200e-04
## cyl -1.507795 0.4146883 -3.635972 1.064282e-03
```

Estimation based on a subsample

```
lm(mpg~wt+disp, data=mtcars, subset=(wt>3))

##
## Call:
## lm(formula = mpg ~ wt + disp, data = mtcars, subset = (wt > 3))
##
## Coefficients:
## (Intercept) wt disp
## 28.40497 -1.46360 -0.02016
```

• where only cars heavier than 3000 lb are considered.

The command as.formula

Creating a formula object

```
?as.formula

fo <- mpg ~ wt + cyl

class(fo)

## [1] "formula"

# The formula object can be used in the regression:
m3 <- lm(fo,data=mtcars)</pre>
```

Further possibilities to specify the formula

Take all available predictors

```
m3_a<-lm(mpg~.,data=mtcars)
```

Interaction effect

```
# effect of cyl and interaction effect:
m3a<-lm(mpg~wt*cyl,data=mtcars)

# only interaction effect:
m3b<-lm(mpg~wt:cyl,data=mtcars)</pre>
```

Take the logarithm

```
m3d<-lm(mpg~log(wt),data=mtcars)
```

Further transformations

Further transformations:

Tranformations of variables are directly included with the I() function:

```
fo2 <- I(log(mpg))~wt+I(wt^2)+disp
lm(fo2, data=mtcars)

##
## Call:
## lm(formula = fo2, data = mtcars)
##
## Coefficients:
## (Intercept) wt I(wt^2) disp
## 4.0000825 -0.3499056 0.0275548 -0.0009865</pre>
```

The command setdiff

• We can use the command to create a dataset with only the features, without the dependent variable

```
names(mtcars)

## [1] "mpg" "cyl" "disp" "hp" "drat" "wt" "qsec" "vs"

## [9] "am" "gear" "carb"

features <- setdiff(names(mtcars), "mpg")
 features

## [1] "cyl" "disp" "hp" "drat" "wt" "qsec" "vs" "am"

## [9] "gear" "carb"

featdat <- mtcars[,features]</pre>
```

The command model.matrix

 With model.matrix the qualitative variables are automatically dummy encoded

```
?model.matrix
model.matrix(m3d)
```

```
##
                        (Intercept) log(wt)
## Mazda RX4
                                  1 0.9631743
## Mazda RX4 Wag
                                  1 1.0560527
## Datsun 710
                                  1 0.8415672
## Hornet 4 Drive
                                  1 1.1678274
## Hornet Sportabout
                                  1 1.2354715
## Valiant
                                  1 1.2412686
## Duster 360
                                  1 1.2725656
## Merc 240D
                                  1 1.1600209
## Merc 230
                                  1 1.1474025
## Merc 280
                                  1 1.2354715
## Merc 280C
                                  1 1.2354715
## Merc 450SE
                                  1 1.4036430
## Merc 450SL
                                  1 1.3164082
## Merc 450SLC
                                  1 1.3297240
```

Model matrix (II)

- We can also create a model matrix directly from the formula and data arguments
- See Matrix::sparse.model.matrix for increased efficiency on large dimension data.

```
ff <- mpg ~ log(wt):cyl
m <- model.frame(ff, mtcars)</pre>
```

```
(mat <- model.matrix(ff, m))</pre>
```

```
##
                        (Intercept) log(wt):cyl
## Mazda RX4
                                       5,779046
## Mazda RX4 Wag
                                    6.336316
## Datsun 710
                                      3.366269
## Hornet 4 Drive
                                      7.006964
## Hornet Sportabout
                                       9.883772
## Valiant
                                  1
                                       7.447612
## Duster 360
                                      10.180525
## Merc 240D
                                  1
                                      4.640084
## Merc 230
                                  1
                                       4.589610
## Merc 280
                                  1
                                       7.412829
## Merc 280C
                                       7.412829
```

A model with interaction effect

```
# disp - Displacement (cu.in.)
m3d<-lm(mpg~wt*disp,data=mtcars)
m3dsum <- summary(m3d)
m3dsum$coefficients</pre>
```

```
## (Intercept) 44.08199770 3.123062627 14.114990 2.955567e-14
## wt -6.49567966 1.313382622 -4.945763 3.216705e-05
## disp -0.05635816 0.013238696 -4.257078 2.101721e-04
## wt:disp 0.01170542 0.003255102 3.596022 1.226988e-03
```

Residual plot - model assumptions violated?

• We have model assumptions violated if points deviate with a pattern from the line

```
plot(m3,1)
```

Residual plot

plot(m3,2)

Another example for object orientation

- m3 is now a special regression object
- Various functions can be applied to this object

```
predict(m3) # Prediction
resid(m3) # Residuals
```

```
##
           Mazda RX4
                         Mazda RX4 Wag
                                              Datsun 710
##
            22,27914
                                                26,25203
                              21.46545
     Hornet 4 Drive Hornet Sportabout
##
                                                 Valiant
##
            20.38052
                              16.64696
                                                19.59873
##
           Mazda RX4
                         Mazda RX4 Wag
                                              Datsun 710
##
          -1.2791447
                            -0.4654468
                                              -3.4520262
                                                 Valiant
##
     Hornet 4 Drive Hornet Sportabout
##
           1.0194838
                             2.0530424
                                              -1.4987281
```

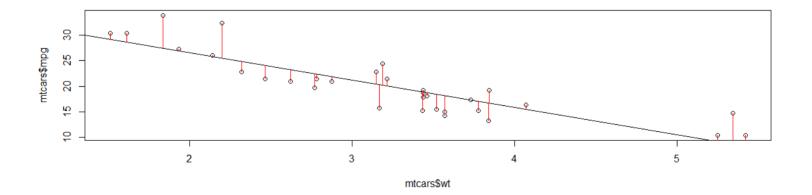
Make model prediction

```
pre <- predict(m1)</pre>
head(mtcars$mpg)
## [1] 21.0 21.0 22.8 21.4 18.7 18.1
head(pre)
           Mazda RX4
                          Mazda RX4 Wag
##
                                                Datsun 710
##
            23.28261
                               21.91977
                                                  24.88595
##
      Hornet 4 Drive Hornet Sportabout
                                                  Valiant
##
            20.10265
                               18.90014
                                                  18.79325
```

Regression diagnostic with base-R

Visualizing residuals

```
plot(mtcars$wt,mtcars$mpg)
abline(m1)
segments(mtcars$wt, mtcars$mpg, mtcars$wt, pre, col="red")
```



The bias-variance tradeoff (I)

The bias–variance tradeoff is the property of a set of predictive models whereby models with a lower bias in parameter estimation have a higher variance of the parameter estimates across samples, and vice versa.

The bias error

... is an error from erroneous assumptions in the learning algorithm. High bias can cause an algorithm to miss the relevant relations between features and target outputs (underfitting).

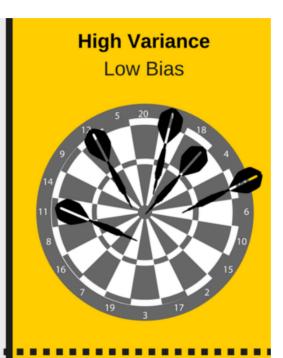
The variance

... is an error from sensitivity to small fluctuations in the training set. High variance can cause an algorithm to model the random noise in the training data, rather than the intended outputs (overfitting).

The bias-variance tradeoff (II)

High Bias Low Variance

High bias, low variance algorithms train models that are consistent, but inaccurate *on average*.



High variance, low bias algorithms train models that are accurate *on average*, but inconsistent.

The mean squared error (mse)

- The MSE measures the average of the squares of the errors
- The lower the better

```
(mse5 <- mean((mtcars$mpg - pre)^2)) # model 5

## [1] 8.697561

(mse3 <- mean((mtcars$mpg - predict(m3))^2))

## [1] 5.974124</pre>
```

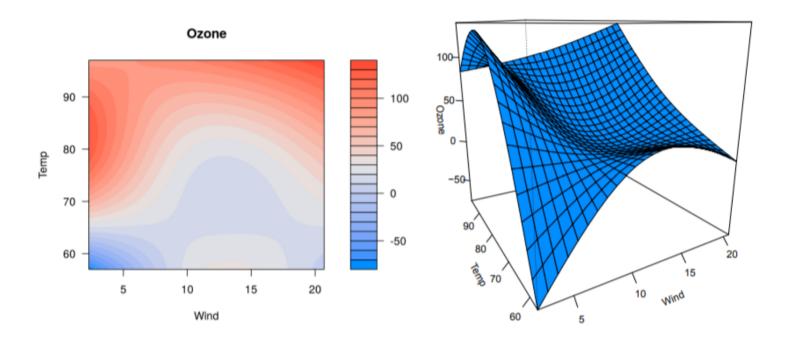
Package Metrics to compute mse

```
library(Metrics)
mse(mtcars$mpg,predict(m3))
```

```
## [1] 5.974124
```

The visreg-package

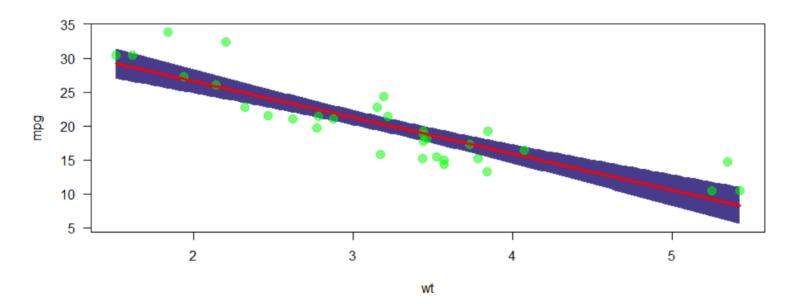
library(visreg)



The visreg-package

- The default-argument for type is conditional.
- Scatterplot of mpg and wt plus regression line and confidence bands

```
visreg(m1, "wt", type = "conditional")
```



Regression with factors

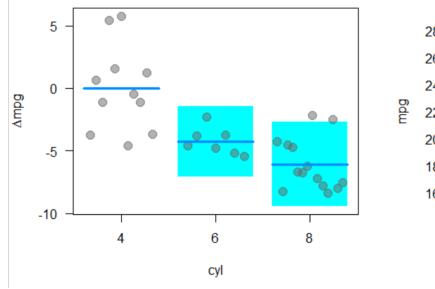
• The effects of factors can also be visualized with visreg:

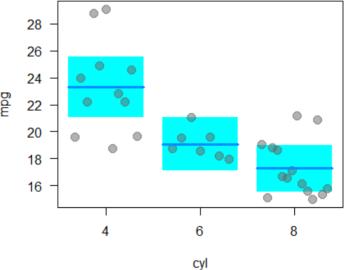
```
mtcars$cyl <- as.factor(mtcars$cyl)
m4 <- lm(mpg ~ cyl + wt, data = mtcars)
# summary(m4)</pre>
```

```
## (Intercept) 33.990794 1.8877934 18.005569 6.257246e-17
## cyl6 -4.255582 1.3860728 -3.070244 4.717834e-03
## cyl8 -6.070860 1.6522878 -3.674214 9.991893e-04
## wt -3.205613 0.7538957 -4.252065 2.130435e-04
```

Effects of factors

```
par(mfrow=c(1,2))
visreg(m4, "cyl", type = "contrast")
visreg(m4, "cyl", type = "conditional")
```





The package visreg - Interactions

```
m5 <- lm(mpg ~ cyl*wt, data = mtcars)
# summary(m5)</pre>
```

```
## (Intercept) 39.571196 3.193940 12.3894599 2.058359e-12
## cyl6 -11.162351 9.355346 -1.1931522 2.435843e-01
## cyl8 -15.703167 4.839464 -3.2448150 3.223216e-03
## wt -5.647025 1.359498 -4.1537586 3.127578e-04
## cyl6:wt 2.866919 3.117330 0.9196716 3.661987e-01
## cyl8:wt 3.454587 1.627261 2.1229458 4.344037e-02
```

Control of the graphic output with layout.

```
visreg(m5, "wt", by = "cyl",layout=c(3,1))
```

The package visreg - Interactions overlay

```
m6 <- lm(mpg ~ hp + wt * cyl, data = mtcars)
visreg(m6, "wt", by="cyl", overlay=TRUE, partial=FALSE)</pre>
```

The package visreg-visreg2d

```
visreg2d(m6, "wt", "hp", plot.type = "image")
```

Exercise: regression Ames housing data

- 1) Install the package AmesHousing and create a **processed version** of the Ames housing data with (at least) the variables Sale_Price, Gr_Liv_Area and TotRms_AbvGrd
- 2) Create a regression model with Sale_Price as dependent and Gr_Liv_Area and TotRms_AbvGrd as independent variables. Then create seperated models for the two independent variables. Compare the results. What do you think?

The Ames Iowa Housing Data

```
ames_data <- AmesHousing::make_ames()</pre>
```

Some Variables

- Gr_Liv_Area: Above grade (ground) living area square feet
- TotRms_AbvGrd: Total rooms above grade (does not include bathrooms
- MS_SubClass: Identifies the type of dwelling involved in the sale.
- MS_Zoning: Identifies the general zoning classification of the sale.
- Lot_Frontage: Linear feet of street connected to property
- Lot_Area: Lot size in square feet
- Street: Type of road access to property
- Alley: Type of alley access to property
- Lot_Shape: General shape of property
- Land_Contour: Flatness of the propert

Multicollinearity

- As p increases we are more likely to capture multiple features that have some multicollinearity.
- When multicollinearity exists, we often see high variability in our coefficient terms.
- E.g. we have a correlation of 0.801 between Gr_Liv_Area and TotRms_AbvGrd
- Both variables are strongly correlated to the response variable (Sale_Price).

```
ames_data <- AmesHousing::make_ames()
cor(ames_data[,c("Sale_Price","Gr_Liv_Area","TotRms_AbvGrd")])</pre>
```

```
## Sale_Price Gr_Liv_Area TotRms_AbvGrd

## Sale_Price 1.0000000 0.7067799 0.4954744

## Gr_Liv_Area 0.7067799 1.0000000 0.8077721

## TotRms AbvGrd 0.4954744 0.8077721 1.0000000
```

Multicollinearity

```
lm(Sale_Price ~ Gr_Liv_Area + TotRms_AbvGrd, data = ames_data)

##
## Call:
## lm(formula = Sale_Price ~ Gr_Liv_Area + TotRms_AbvGrd, data = ames_data)
##
## Coefficients:
## (Intercept) Gr_Liv_Area TotRms_AbvGrd
## 42767.6 139.4 -11025.9
```

• When we fit a model with both these variables we get a positive coefficient for Gr_Liv_Area but a negative coefficient for TotRms_AbvGrd, suggesting one has a positive impact to Sale_Price and the other a negative impact.

Seperated models

- If we refit the model with each variable independently, they both show a positive impact.
- The Gr_Liv_Area effect is now smaller and the TotRms_AbvGrd is positive with a much larger magnitude.

```
lm(Sale_Price ~ Gr_Liv_Area, data = ames_data)$coefficients

## (Intercept) Gr_Liv_Area
## 13289.634 111.694

lm(Sale_Price ~ TotRms_AbvGrd, data = ames_data)$coefficients

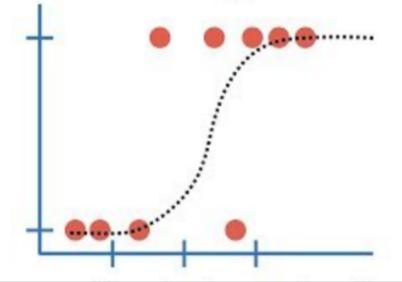
## (Intercept) TotRms_AbvGrd
## 18665.40 25163.83
```

- This is a common result when collinearity exists.
- Coefficients for correlated features become over-inflated and can fluctuate significantly.

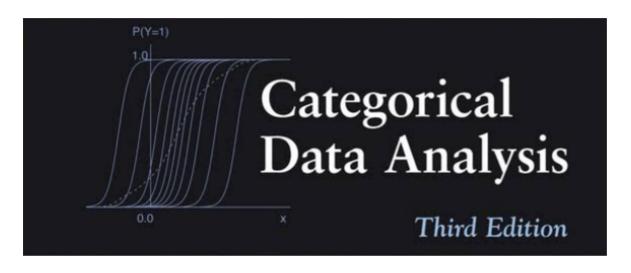
Consequences

- One consequence of these large fluctuations in the coefficient terms is **overfitting**, which means we have high variance in the bias-variance tradeoff space.
- We can use tools such as **variance inflaction factors** (Myers, 1994) to identify and remove those strongly correlated variables, but it is not always clear which variable(s) to remove.
- Nor do we always wish to remove variables as this may be removing signal in our data.

Logistic Regression...



Agresti - Categorical Data Analysis (2002)



- Very intuitively written book
- Very detailed accompanying script by Laura A. Thompson
- The paper deals with categorical data analysis in general.

Faraway books on regression with R

Extending the Linear Model with R

- Logistic regression intuitively explained
- Examples with R-code
 - Faraway Extending the linear model with R
 - Faraway Practical Regression and Anova using R

Import the GESIS Panel dataset again

The argument convert.factors:

• logical. If TRUE, factors from Stata value labels are created.

A function to recode the missing values

```
transform_missings <- function(var){
  misvals <- c(-11,-22,-33,-44,-55,-66,-77,-88,-99,-111)
  var[var %in% misvals] <- NA
  return(var)
}</pre>
```

Variables for glm's

• a11d056z: age group

```
table(datf$a11d056z)
##
## -99
                        5
                            6
                                           10
                                                   12
                                               11
                                                       13
##
           87 101
                   91 83 100 163 159 133
                                               56 105
       31
                                           64
                                                       44
age <- transform_missings(datf$a11d056z)</pre>
table(age)
## age
## 1
                        6
                                       10
                                           11
                                               12
                                                   13
## 31 87 101
                  83 100 163 159 133
                                           56 105 44
               91
                                       64
```

GP variable a11d094a: Children under 16 years

Does your household include children under 16?

- 1 Yes
- 2 No

```
children <- as.factor(transform_missings(datf$a11d094a))
table(children)</pre>
```

```
## children
## 1 2
## 325 681
```

Conditional Density Plot (GESIS Panel)

```
cdplot(children ~ age, data = dat)
```

Binary independent variables with glm

- The logistic regression belongs to the class of generalized linear models (GLM)
- The function for estimating a model of this class in is called glm()
- glm()

Specifying a glm

- formula object
- the class (binomial, gaussian, gamma)
- including link function (logit, probit, cauchit, log, cloglog)

must be specified

Logistic regression with R

Interpreting the coefficients

Consider the logistic model of children in household as a function of age.

```
sum_glm1$coefficients
```

```
## Estimate Std. Error z value Pr(>|z|)
## (Intercept) -0.7194058 0.16384386 -4.390801 1.129338e-05
## age 0.2225862 0.02376266 9.367056 7.458415e-21
```

- The estimates and standard errors are given in terms of log odds, not in terms of probability.
- The p-values mean the same thing they always have.

The inverse logit

```
sum_glm1$coefficients
```

```
## Estimate Std. Error z value Pr(>|z|)
## (Intercept) -0.7194058 0.16384386 -4.390801 1.129338e-05
## age 0.2225862 0.02376266 9.367056 7.458415e-21
```

• The coefficients can't be interpreted as simply as 'the children in household at age group 0'. We have to use the inverse logit in order to find that.

Log-odds of -0.7194058 is the same as probability 0.3275238.

```
library(faraway)
ilogit(sum_glm1$coefficients[1,1])
```

```
## [1] 0.3275238
```

About the intercept in a logistic model

- It is possible to get an intercept of less than 0.
- This means that the log-odds are negative, NOT the probability.
- E.g. a log-odds of 0 translates to a probability of 0.5.

Log-odds and the probability

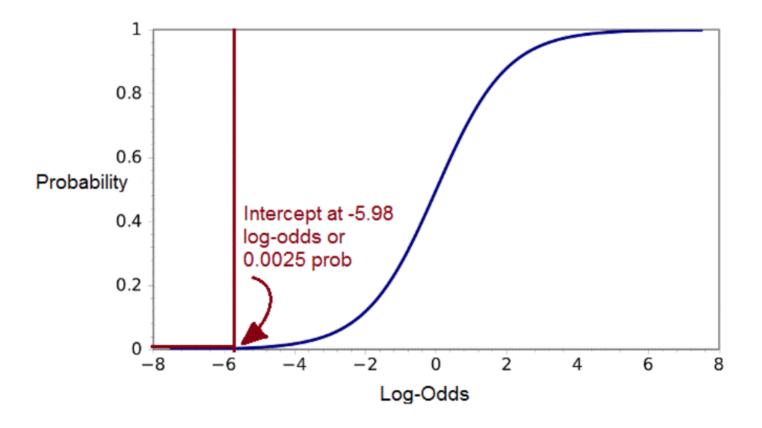
• Log-odds always increases as probability increases.

Therefore...

- A positive slope coefficient means that the response increases with the associated explanatory variable.
- In this case, the probability of children in the household increases with age.

Plotting the result

but it increases by the sigmoid curve, not at a constant rate.



Logistic regression model formula

Logistic models have regression formulas. This model's formula is:

```
Log-Odds(Children) = -0.7194058 + 0.2225862(Age) + error
```

We can plug age values into this formula to get predicted log-odds at different ages.

Log-odds for age group 5

```
-0.7194058 + 0.2225862*(5) = 0.3935251
```

Children probability in age group 5

```
ilogit(0.3935251)
```

```
## [1] 0.597131
```

Interpreting the results

• The difference between the null deviance and the residual deviance shows how our model is doing against the null model (a model with only the intercept). The wider this gap, the better.

```
anova(glm_1, test="Chisq")
```

```
## Analysis of Deviance Table
##
## Model: binomial, link: logit
##
## Response: children
##
## Terms added sequentially (first to last)
##
##
       Df Deviance Resid. Df Resid. Dev Pr(>Chi)
##
## NULL
                        1000
                                  1259
## age 1 98.956
                    999 1160 < 2.2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Mc Fadden's \mathbb{R}^2

```
library(pscl)
pR2(glm_1)
```

```
## llh llhNull G2 McFadden

## -580.02210772 -632.93066002 105.81710461 0.08359297

## r2ML r2CU

## 0.10031573 0.13978426
```

The log-likelihood from the fitted model

The log-likelihood from the intercept-only restricted model

Minus two times the difference in the log-likelihoods

McFadden McFadden's pseudo r-squared

Maximum likelihood pseudo r-squared

Cragg and Uhler's pseudo r-squared

Distance between residential area and large city

How far is it from where you live to the center of the nearest large city?

- 1 In the center of a big city
- 6 60 km and more

```
region <- transform_missings(datf$bczd001a)
table(region)</pre>
```

```
## region
## 1 2 3 4 5 6
## 87 191 279 157 126 165
```

Satisfaction life in place of residence

How satisfied are you - all in all - with your life in [place of residence] at the moment?

- 1 Very satisfied
- 5 Very dissatisfied

```
satisfactionplace <- datf$a11c019a
table(satisfactionplace)</pre>
```

```
## satisfactionplace
## 1 2 3 4 5
## 553 534 99 30 6
```

Another model

```
pseudor2 <- pR2(glm_2)
pseudor2["McFadden"]</pre>
```

```
## McFadden
## 0.258121
```

Exercise: logistic regression with Smarket data

- load the Smarket data from the ISLR package
- create a pairs plot of the data
- check if there are missing values in the data
- have a look at the correltations between variables
- create a corrplot
- run a logistic model and look at the deviance

Another variable in the Gesis Panel data

• Number of tattoos:

```
Tatoos <- transform_missings(datf$bdao067a)
Tatoos[Tatoos==97]<-0

table(Tatoos)

## Tatoos
## 0 1 2 3 4 5 6
## 871 56 28 13 7 4 8</pre>
```

Generalized regression with R - more functions

• Logistic model with Probit link:

```
probitmod <- glm(children ~ age,
    family=binomial(link=probit))</pre>
```

• Regression with count data:

```
modp <- glm(Tatoos ~ age,family=poisson)</pre>
```

Proportional odds logistic regression in library MASS:

```
library("MASS")
mod_plr<-polr(a11c020a ~ a11d096b ,data=dat)</pre>
```

Exercise: logistic regression

We will use a data on containing health-related measurements on women and whether they can be (or will be at a future point?) classified as diabetic. The data was collected by the US National Institute of Diabetes and is contained in the MASS package.

Load dataset and create test and train dataset

Load the MASS package and combine Pima.tr and Pima.tr2 to a data.frame called train and save Pima.te as test. Change the coding of our variable of interest to (type) to 0 (non-diabetic) and 1 (diabetic). Check for and take note of any missing values.

Plotting using pairs() and jitter

Take a look at the data. Plot a scatterplot matrix between all the explanatory variables using pairs(), and color code the dots according to diabetic classification. Furthermore, try to plot type as a function of age. Use jitter to make your graph more informative. Bonus: Can you add a logistic fit based on age on top of your plot?

Exercise: logistic regression II

Coefficients and p-values

Using the glm() and the train data fit a logistic model of type on age and bmi. Print out the coefficients and their p-value.

Prediction

What does the model fitted in exercise 3 predict in terms of probability for someone age 35 with bmi of 32, what about bmi of 22?

Odds ratios

According to our model what are the odds that a woman in our sample is diabetic given age 55 and a bmi 37? Remember that odds in this context have a very precise definition which is different from probability.

Exercise: Confusion matrix

Build the confusion matrix, a table of actual diabetic classification against model prediction. Use a cutoff value of 0.5, meaning that women who the model estimates to have at least 0.5 chance of being diabetic are predicted to be diabetic. What is the prediction accuracy?

Links - regression

- Regression **r-bloggers**
- The complete book of **Faraway** very intuitive
- Good introduction on Quick-R
- Multiple regression
- 15 Types of Regression you should know
- ggeffects Create Tidy Data Frames of Marginal Effects for 'ggplot' from Model Outputs
- Machine learning iteration

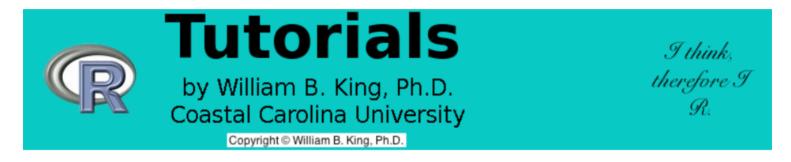
Nice table output with stargazer

```
library(stargazer)
stargazer(m3, type="html")
```

Example HTML output:

Links - logistic regression

• Introduction to logistic regression



Code for the book of Faraway

```
library(faraway)
data(orings)
plot(damage/6 ~ temp, orings, xlim=c(25,85), ylim = c(0,1), xlab="Temperature", ylab="Prob of damage")
lmod <- lm(damage/6 ~ temp, orings)
abline(lmod)
logitmod <- glm(cbind(damage,6-damage) ~ temp, family=binomial, orings)
summary(logitmod)
plot(damage/6 ~ temp, orings, xlim=c(25,85), ylim = c(0,1), xlab="Temperature", ylab="Prob of damage")
```

- Categorical data: How to perform a Logistic Regression in R
- Logistic Regression in R Tutorial

Links and resources

Shiny Apps - Diagnostics for linear regression

- Simple Linear Regression
- Multicollinearity in multiple regression
- Diagnostics for simple linear regression

Further resources

- Elegant regression results
- Regression analysis essentials