IFOA eXplainable AI Workstream - SHAP

1. Intro to case study

1.1 Motivation

The aim of this document is to supply the reader of [All Clear](https://www.theactuary.com/issues/2022/03/march-2022) in The Actuary Magazine, with a practical, comprehensive example of applying SHAP to explain models' predictions.

1.2 Intro to dataset

The dataset can be downloaded from: freMTPL2freq

Originally it was accessible through CASdatasets R package. Excerpt from the original documentation:

Description

In the two datasets freMTPL2freq, freMTPL2sev, risk features are collected for 677,991 motor third-part liability policies (observed mostly on one year). In addition, we have claim numbers by policy as well as the corresponding claim amounts. freMTPL2freq contains the risk features and the claim number while freMTPL2sev contains the claim amount and the corresponding policy ID.

Format

IDpol The policy ID (used to link with the claims dataset).

ClaimNb Number of claims during the exposure period.

Exposure The period of exposure for a policy, in years.

VehPower The power of the car (ordered values).

VehAge The vehicle age, in years.

DrivAge The driver age, in years (in France, people can drive a car at 18).

BonusMalus Bonus/malus, between 50 and 350: <100 means bonus, >100 means malus in France.

VehBrand The car brand (unknown categories).

VehGas The car gas, Diesel or regular.

Area The density value of the city community where the car driver lives in: from "A" for rural area to "F" for urban centre.

Density The density of inhabitants (number of inhabitants per square-kilometer) of the city where the car driver lives in.

Region The policy region in France (based on the 1970-2015 classification)

```
if(FALSE){
  data_input = read.csv2("data/freMTPL2freq.csv",sep = ",") %>%
    as_tibble() %>%
    mutate(VehPower = factor(VehPower, order = TRUE,levels = 4:15),
        across(c(Area,Region,VehBrand,VehGas),factor)) %>%
    rowwise() %>%
    mutate(ClaimNb = as.integer(min(ClaimNb,4)),
        VehAge = as.integer(min(VehAge,20)),
        DrivAge = as.integer(min(DrivAge,90)),
        Exposure = as.numeric(min(Exposure,1)),
        Density = log(Density)) %>%
    ungroup()
}
```

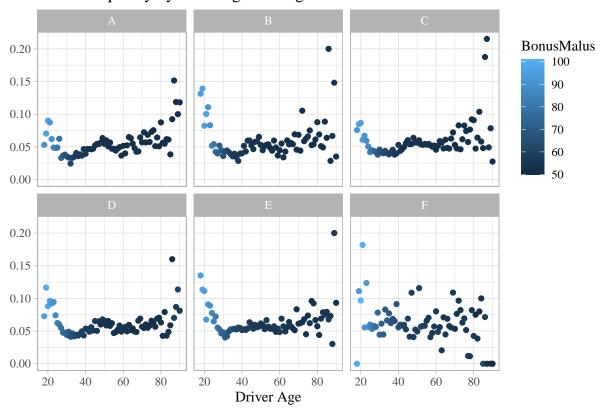
1.3 Preprocessing and Basic summary statistics

ClaimNb	Area	VehPower	VehAge	DrivAge	BonusMalus	VehBrand	VehGas	Density	Region
1	D	5	0	55	50	B12	Regular	7.104144	R82
1	D	5	0	55	50	B12	Regular	7.104144	R82
1	В	6	2	52	50	B12	Diesel	3.988984	R22
1	В	7	0	46	50	B12	Diesel	4.330733	R72
1	В	7	0	46	50	B12	Diesel	4.330733	R72
1	E	6	2	38	50	B12	Regular	8.007367	R31

1.4 EDA

`summarise()` has grouped output by 'DrivAge'. You can override using the `.groups` argument.

Claim frequency by driver age and region



2. Models - fitting, output comparison

In this section we build three models - a Neural Network, Gradient Boosted Trees (XGBoost), and a Poisson GLM.

We examine the models' outputs using a hold out test dataset (15% of available observations) and applying a model_evaluation function for additional statistics. The function lets us view: the obtained loss (MSE, MAE, Poisson Deviance); prediction statistics grouped by the actual claim number and raw predictions and more. Further details on model evaluation function along with the source code can be found in section 4.1

Note: Poisson deviance loss is not symmetrical around the actual value we compare the prediction against (in contrast to e.g. MSE and MAE). It puts more emphasis on differentiating between zero and non-zero claim instances than say observations with 1 and 2 claims (see 4.4 for additional information).

2.1 NN

```
# notrun
if(FALSE){
# don't enter next epoch if there are no significant performance gains
early_stop = callback_early_stopping(monitor = "val_loss", patience = 3)
# Neural network structure
Neural_Net = keras_model_sequential(input_shape = c(ncol(train))) %%
  layer dense(units = 64, activation = 'relu') %>%
  layer_dense(units = 64, activation = 'relu') %>%
  layer_dense(units = 32, activation = 'relu') %>%
  layer_dense(units = 1, activation = 'relu')
# Fitting the model
Neural_Net %>%
  compile(
   loss = "poisson",
   optimizer = optimizer_rmsprop()
 ) %>%
  fit(
    callbacks = list(early_stop),
   train %>% as.matrix(),
    (data[sample_TTS,"ClaimNb"]/data_input$Exposure[sample_TTS]) %>% as.matrix(),
   batch size = 2^13,
   epochs = 10,
   validation_split = 0.1,
   shuffle = TRUE ,
    sample_weight = data_input$Exposure[sample_TTS] %>% as.matrix()
  )
eval_list$Neural_Net = model_evalulation(Neural_Net,
                                     cbind(test,data[-sample_TTS,"ClaimNb"]),
                                     type = "NN",
                                     ClaimNBadj = FALSE)
}
summary(Neural Net)
```

	Model: "sequential_13"			
##				
	Layer (type)	Output	<u> -</u>	Param #
	dense_56 (Dense)	(None,	64)	3712
## ##	dense_55 (Dense)	(None,	64)	4160
## ##	dense_54 (Dense)	(None,	32)	2080
	dense_53 (Dense)	(None,	1)	33
##	Total params: 9,985			
	Trainable params: 9,985			
	Non-trainable params: 0			
##				

2.2 XGB

To be done

```
# notrun
if(FALSE){
 XGB_validation = 1:10000
 dtrain = xgb.DMatrix(data = train[-XGB_validation,] %>% as.matrix(),
                       label = data[sample_TTS,]$ClaimNb[-XGB_validation])
  dvalid = xgb.DMatrix(data = train[XGB_validation,] %>% as.matrix(),
                       label = data[sample_TTS,]$ClaimNb[XGB_validation])
  watchlist <- list(train=dtrain, test=dvalid)</pre>
 m5 xgb <-
   xgboost(
      # data = data[sample_TTS,] %>% select(-ClaimNb) %>% ,
      # label = data[sample_TTS,]$ClaimNb ,
      # data = train[-XGB_validation,] %>% as.matrix() ,
      # label = data[sample_TTS,]$ClaimNb[-XGB_validation],
      data = dtrain,
     nrounds = 200,
      weight = (data[sample_TTS, "ClaimNb"]+1) %>% as.matrix(),
     objective = "reg:squarederror",
     early_stopping_rounds = 3,
     max_depth = 8,
     eta = .3,
     verbose = 2,
      watchlist = watchlist
   )
# eval_list$xgb5 = model_evalulation(model = m5_xgb,
#
                                      data = data.frame(test,
#
                                                        ClaimNb = data[-sample_TTS, "ClaimNb"]),
#
                                      type = "XGB")
```

2.3 GLM

```
if(TRUE){
  GLM = glm(formula = ClaimNb/Exposure ~ Area + VehPower + VehAge + DrivAge + BonusMalus + VehBrand + V
            family = poisson(link = log),
            weights = Exposure,
            data = data_input[sample_TTS,] %>% select(-IDpol)) %>% suppressWarnings()
}
GLM
##
##
   Call:
          glm(formula = ClaimNb/Exposure ~ Area + VehPower + VehAge + DrivAge +
       BonusMalus + VehBrand + VehGas + Density + Region, family = poisson(link = log),
##
       data = data_input[sample_TTS, ] %>% select(-IDpol), weights = Exposure)
##
##
   Coefficients:
##
##
     (Intercept)
                           AreaB
                                           AreaC
                                                           AreaD
                                                                           AreaE
                                       0.0005032
##
      -4.0114467
                       0.0161407
                                                       0.0339460
                                                                       0.0184801
##
           AreaF
                      VehPower.L
                                      VehPower.Q
                                                      VehPower.C
                                                                      VehPower<sup>4</sup>
##
      -0.0737318
                      -0.0502667
                                      -0.1834956
                                                      -0.0409452
                                                                      -0.0923431
##
      VehPower<sup>5</sup>
                      VehPower^6
                                      VehPower^7
                                                      VehPower^8
                                                                      VehPower^9
##
       0.0140356
                      -0.2462388
                                      -0.1482789
                                                       0.0890247
                                                                       0.0124442
##
     VehPower^10
                     VehPower^11
                                                                      BonusMalus
                                          VehAge
                                                         DrivAge
##
      -0.0867967
                       0.1070066
                                      -0.0404711
                                                       0.0063530
                                                                       0.0225429
##
     VehBrandB10
                     VehBrandB11
                                     VehBrandB12
                                                     VehBrandB13
                                                                     VehBrandB14
                                                       0.0193933
##
       0.0173827
                       0.1143393
                                       0.1727967
                                                                      -0.0694485
##
      VehBrandB2
                      VehBrandB3
                                      VehBrandB4
                                                      VehBrandB5
                                                                      VehBrandB6
##
      -0.0132280
                      -0.0146900
                                      -0.0223253
                                                       0.0444672
                                                                      -0.0211478
   VehGasRegular
                                       RegionR21
                                                       RegionR22
##
                         Density
                                                                       RegionR23
##
       0.0668401
                       0.0378664
                                       0.1720110
                                                       0.0322257
                                                                      -0.0821447
##
       RegionR24
                       RegionR25
                                       RegionR26
                                                       RegionR31
                                                                       RegionR41
##
       0.0738775
                       0.0304650
                                      -0.0142948
                                                      -0.1117022
                                                                      -0.2737856
##
       RegionR42
                       RegionR43
                                       RegionR52
                                                       RegionR53
                                                                       RegionR54
##
      -0.0228858
                      -0.0797646
                                      -0.0230057
                                                       0.0716439
                                                                      -0.0464823
##
       RegionR72
                       RegionR73
                                       RegionR74
                                                       RegionR82
                                                                       RegionR83
##
      -0.0833502
                      -0.0988507
                                       0.1921085
                                                       0.0682227
                                                                      -0.2679160
##
       RegionR91
                       RegionR93
                                       RegionR94
##
      -0.0254702
                                       0.1421034
                       0.0077099
##
## Degrees of Freedom: 576310 Total (i.e. Null); 576258 Residual
## Null Deviance:
                         190400
```

AIC: Inf

Residual Deviance: 184100

2.4 Model comparison

Here we examine the model_evalulation outputs, starting with basic loss functions and then turning to more in-depth view and predictions statistics.

2.4.1 Loss Metrics Neural Network

absolute_error	$mean_squared_error$	${\bf Exposure Weighted Poisson Deviance Loss}$
0.136935	0.0613371	34750.78

XGB GLM

$ab solute_error$	$mean_squared_error$	${\bf Exposure Weighted Poisson Deviance Loss}$
0.1493149	0.0619182	36053.18

2.4.2 Broader summary statistics As an alternative to comparing the loss metrics, we can assess the models performance using summary statistics grouped by the actual claim number. It can be noted that the average predictions for the Network are higher than for the GLM for policies with ClaimNb>0 and lower for ClamNb=0 which would suggest a better fit. Furthermore, the

Neural Network

Actual	count	${\rm mean_pred}$	$\operatorname{sd_pred}$	\min	max	Q1	Q2	Q3
0	96495	0.095	0.078	0.000	1.016	0.050	0.074	0.111
1	4924	0.138	0.131	0.000	0.978	0.061	0.090	0.163
2	271	0.159	0.145	0.006	0.734	0.067	0.104	0.197
3	9	0.242	0.236	0.062	0.775	0.098	0.139	0.226
4	3	0.122	0.036	0.083	0.154	0.107	0.130	0.142

XGB GLM

Actual	count	mean_pred	sd_pred	min	max	Q1	Q2	Q3
0	96495	0.107	0.058	0.023	3.381	0.073	0.094	0.123
1	4924	0.122	0.075	0.034	1.504	0.079	0.103	0.139
2	271	0.149	0.133	0.042	1.182	0.088	0.116	0.158
3	9	0.215	0.172	0.055	0.600	0.112	0.155	0.244
4	3	0.113	0.074	0.058	0.197	0.071	0.084	0.141

3. XAI

Note that the current implementation of SHAP is insensitive to One-Hot Encoding, meaning that explanation of an instance might contain a non-zero contribution for both VehGas=Diesel AND VehGas!=Regular at the same time. This is caused by the lack of interface in the SHAP function to indicate the range of OHE variables.

Currently to apply SHAP in R, one has to access a Python environment (through reticulate package) that has SHAP package installed. Here, DALEX package is used as a wrapper for SHAP. Alternatively a work in progress version of a pure R implementation is available - shapr package v0.2.0.

For the full code producing graphs below go to: scripts/Prep_SHAP_Graphs.R, where you will find a wrapper for the original plotting function, to allow for selecting only the most significant variables. It will prove helpful in case the models use a large number of variables and/or including OHE.

3.1 Model - level SHAP

The code below is an example of how to call DALEX and SHAP in R. Here we estimate the SHAP values on a subset of 1000 observations. SHAP for the XGB and GLM are produced analogously.

```
if(FALSE){
  explainer = list()
  residuals = list()
  SHAP = list()
  row_subset = sample(1:nrow(test),1000)
  explainer$Neural_Net = explain(
   model = Neural_Net,
   data = test[row_subset,],
   y = (data[-sample_TTS, "ClaimNb"] %>% as.matrix())[row_subset],
   predict_function = predict_wrapper,
    label = "Neural Net"
  )
  SHAP$Neural_Net_1 = shap(explainer$Neural_Net,
                           new_observation = test[678,],
                           method = "KernelSHAP"
  )
  SHAP$Neural_Net_1_plot = CustomSHAPplot(dalex_output = SHAP$Neural_Net_1)
}
```

3.2 Individual SHAP

Neural Network Individual SHAP value plots for observations: * with 1 claim and low error for NN; * an instance with 0 claims and very high error * An instance with 2 claims

For this observation ClaimNb = 1, we can see (as in most cases) that the BonusMalus variable along with vehicle age and brand/gas type have the most impact on the final prediction.

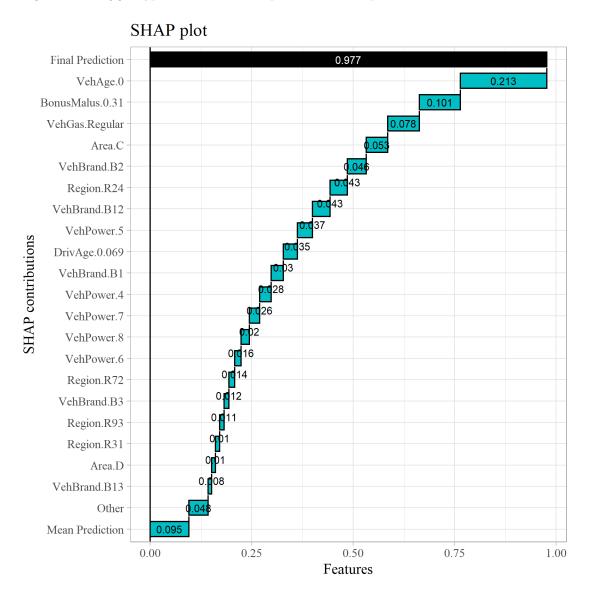


Figure 1: Individual SHAP

This instance, in reality has ClaimNb of 0 and Networks prediction for it, has the highest error from all observations with actual ClaimNb=0. Interestingly, if it wasn't for the BonusMalus value in case of this instance, the model could have output a much lower prediction. This could be confirmed using an ICE (Individual Conditional Expectation) plot for this observation.

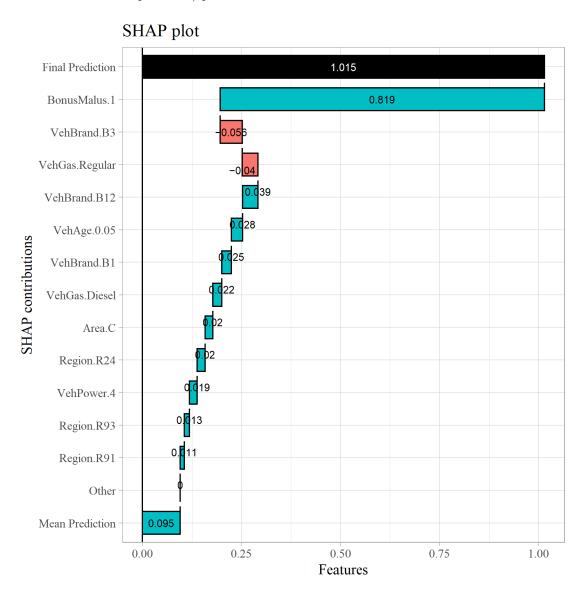


Figure 2: Individual SHAP

In case of this observation, the actual number of claims=2, and here again BonusMalus plays a siginficant role in the final prediction.

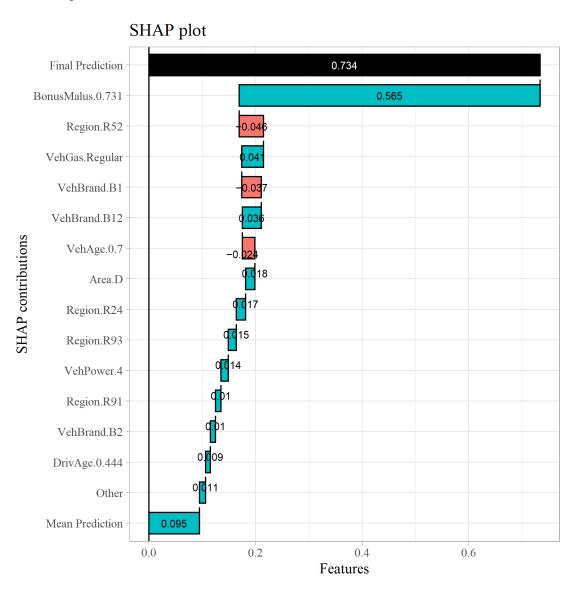


Figure 3: Individual SHAP

 \mathbf{XGB} Individual SHAP value plots for observations: * with 1 claim and low error for NN; * an instance with 0 claims and very high error * An instance with 2 claims

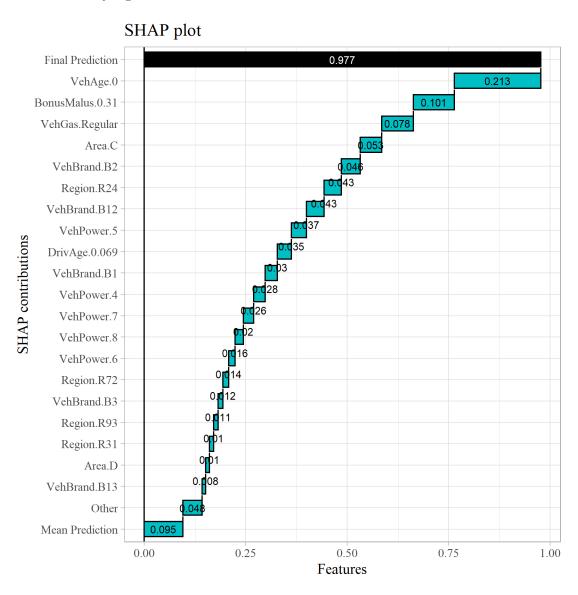


Figure 4: Individual SHAP

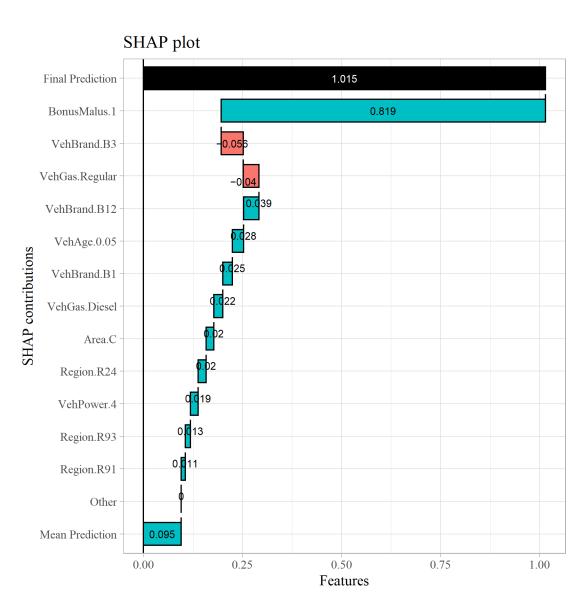


Figure 5: Individual SHAP

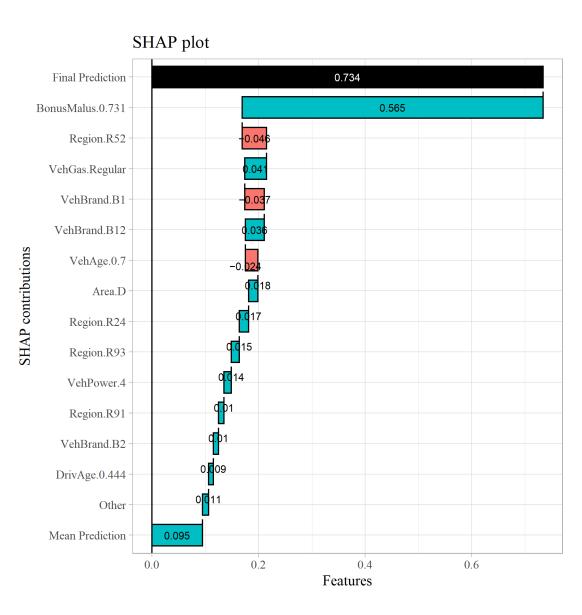


Figure 6: Individual SHAP

GLM For the GLM the contributions are going to be proportional directly to the obtained regression parameters, so SHAP plots here are not going to reveal anything that has not been implemented in the model by design.

To Do.

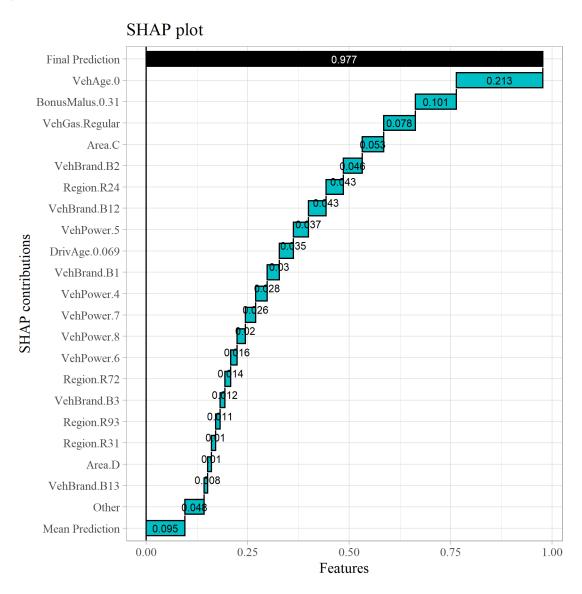


Figure 7: Individual SHAP

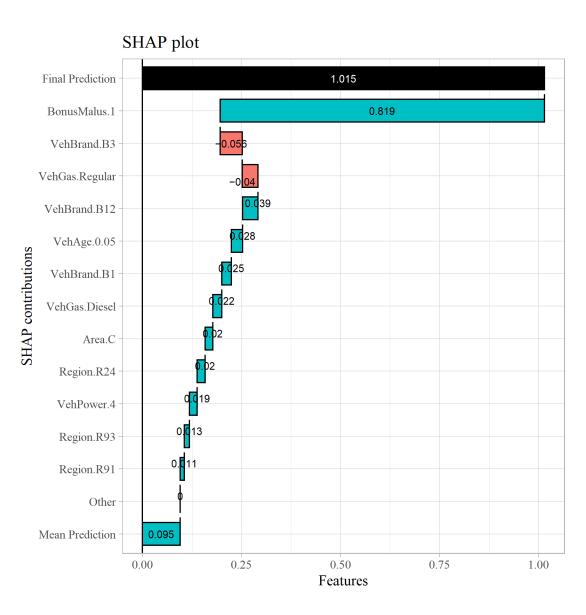


Figure 8: Individual SHAP

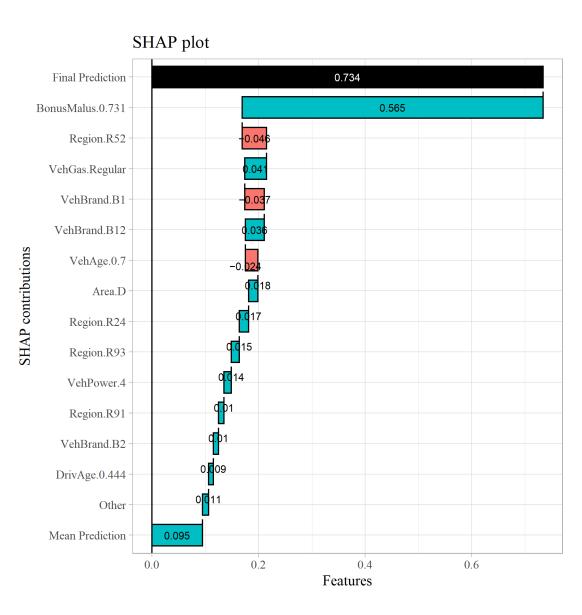


Figure 9: Individual SHAP

4. Additional Information

4.1 model_evalulation utility function

Utility function for analysing model performance.

```
Input:
```

model: KERAS Neural Network, XGBoost, GLM

type: specify the type of model can be done automatically data: named dataframe to assess models' performance on

ClaimNBadj: When passing a NN with poisson loss, an adjustment has to be made to the Claim Number

Output:

list(Evaluation = Evaluation, Predictions = Predictions, AvE = AvE, Sorted_by_MSE = Sorted_by_MSE))

```
if (FALSE){
  # utility function for analysing model performance
  model_evalulation = function(model,
                               data = test,
                               type = "NN",
                               ClaimNBadj = FALSE){
   if (type=="NN"){
      if( ClaimNBadj==TRUE){
        # rescaled Predictions
       Predictions = data.frame(Predicted = (model %% predict(data %% select(-ClaimNb) %% as.matrix
                                 Actual = data$ClaimNb)
      }else{
       Predictions = data.frame(Predicted = (model %>% predict(data %>% select(-ClaimNb) %>% as.matrix
                                 Actual = data$ClaimNb)
     }
   }else if(type=="GLM"){
     Predictions = data.frame(Predicted = predict(model,newdata = data %>% select(-ClaimNb,-Exposure,-
                               Actual = data$ClaimNb)
   }else if(type == "XGB"){
     Predictions = data.frame(Predicted = predict(model, newdata = data %>% select(-ClaimNb) %>% as.mat
                               Actual = data$ClaimNb)
   }
   Evaluation = data.frame(
      absolute_error = mean(abs(as.matrix(Predictions$Predicted - data$ClaimNb))),
     mean_squared_error = mean(as.matrix((Predictions$Predicted - data$ClaimNb)^2)),
     ExposureWeightedPoissonDevianceLoss = ExposureWeightedPoissonDevianceLoss(Predictions$Predicted,d
   )
```

```
AvE = Predictions %>% mutate(Actual = as.factor(Actual)) %>%
    group_by(Actual) %>%
    summarise(count = n(),
              mean_pred = mean(Predicted),
              sd_pred = sd(Predicted),
              min = min(Predicted),
              \max = \max(Predicted),
              Q1 = quantile(Predicted, probs = 0.25),
              Q2 = quantile(Predicted, probs = 0.5),
              Q3 = quantile(Predicted, probs = 0.75),
              IQR = (Q3-Q1)/Q2,
              Negative_Pred = sum(Predicted<0))</pre>
 Sorted_by_MSE = data %>% mutate(Predictions = Predictions$Predicted,
                                  SquaredError = (Predictions - ClaimNb)^2) %>% arrange(-SquaredError
 return(list(Evaluation = Evaluation,
              Predictions = Predictions,
              AvE = AvE,
              Sorted_by_MSE = Sorted_by_MSE))
}
# for DALEX and SHAP explainer objects
predict wrapper=function(model,new data){
 return(model %>% predict(new_data %>% as.matrix()))
predict_wrapper_GLM=function(model,new_data){
 return(predict(model, newdata = new_data, type="response"))
```

4.2

Data wrangling was not the main intention of this exercise, thus the dataset in Prep_RMD/XAI_data.rda has been already processed. The script below takes the raw freMTPL data as in the source and transforms it to our needs.

```
if (FALSE){

data_input=read.csv2("data/freMTPL2freq.csv",sep = ",") %>%
    as_tibble() %>%
    mutate(VehPower = factor(VehPower, order = TRUE,levels = 4:15),
        across(c(Area,Region,VehBrand,VehGas),factor)) %>%
    rowwise() %>%
    mutate(ClaimNb = as.integer(min(ClaimNb,4)),
        VehAge = as.integer(min(VehAge,20)),
        DrivAge = as.integer(min(DrivAge,90)),
        Exposure = as.numeric(min(Exposure,1)),
```

```
Density = log(Density)) %>%
  ungroup()
# remove ID's
data = data_input %>% select(-c(IDpol,Exposure))
# train/test split
sample_TTS = sample(x = 1:nrow(data), size = round(0.85 * nrow(data)), replace = FALSE)
train = data[sample_TTS,] %>% as.data.frame()
test = data[-sample_TTS,] %>% as.data.frame()
# Normalization of numeric variables
data_prep = function(data){
 Normalized = apply(data %>% select(-ClaimNb) %>% select_if(Negate(is.factor)),
                     FUN = function(x){return((x-min(x))/(max(x)-min(x)))}) %>%
    as_tibble()
 data = data %>% select_if(is.factor) %>% cbind(Normalized)
 data$VehPower = factor(data$VehPower, order = FALSE)
  # OHE of factor variables
 OHE = dummyVars("~.", data = data %>% select_if(is.factor)) %>%
   predict(newdata = data %>% select_if(is.factor)) %>%
   as_tibble()
 data = data %>% select_if(Negate(is.factor)) %>% cbind(OHE) %>% as_tibble()
 return(data)
# data prep separately for train and test
train = data_prep(train)
test = data_prep(test)
```

4.3

text

```
dalex_output$vname[dalex_output$vname=="VehAge"]=paste("VehAge",round(dalex_output$VehAge[1],3),sep
  dalex_output$vname[dalex_output$vname=="DrivAge"]=paste("DrivAge",round(dalex_output$DrivAge[1],3),
 dalex_output$vname[dalex_output$vname=="BonusMalus"]=paste("BonusMalus",round(dalex_output$BonusMal
 dalex_output = dalex_output %>% as_tibble()
 avg_pred = dalex_output$yhatmean
 total_pred = dalex_output$yhat
 other_pred = sum(dalex_output$attribution[abs(dalex_output$attribution)<=epsilon])</pre>
 plot_data = rbind(data.frame(values = c(avg_pred[1],other_pred),
                               labels = c("Mean Prediction","Other")),
                    dalex output %>%
                      as_tibble() %>%
                      filter(abs(attribution) > epsilon) %>%
                      mutate(attribution = attribution) %>%
                      transmute(values = attribution,
                                labels = vname) %>%
                      arrange(abs(values))) %>%
   mutate(values = round(values,3))
 plt = plot_data %>%
    waterfall(fill_by_sign = TRUE,
              calc_total = TRUE,
              total axis text = "Final Prediction")+
    coord_flip()+
    ggtitle("SHAP plot")+
   xlab("SHAP contributions")+
   ylab("Features")+
   theme_light()+
    theme(text=element_text(family="serif"),
          legend.justification = c("right", "top"))
 return(plt)
}
```

4.4 Poisson Deviance Loss

```
output[k] = 2*predicted[k]*exposure[k]

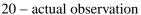
# actual non zero and predicted non-zero
m = (actual != 0 & predicted != 0 )
output[m] = 2*actual[m]*(predicted[m]*exposure[m]/actual[m] - 1 - log(predicted[m]*exposure[m]/actual

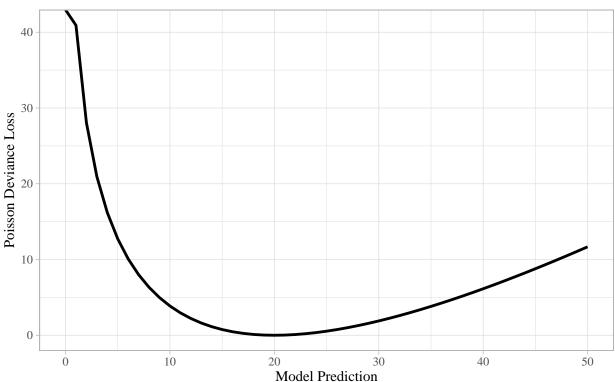
# actual non-zero and predicted zero
n = (actual != 0 & predicted == 0 )
output[n] = 2*actual[n]

output = sum(output)

return(output)
}
```

Poisson Deviance Loss function





4.5 Session information

Hardware, R and Python configuration

```
sessionInfo()
```

```
## R version 4.0.4 (2021-02-15)
## Platform: x86_64-w64-mingw32/x64 (64-bit)
## Running under: Windows 10 x64 (build 19044)
```

```
##
## Matrix products: default
##
## locale:
## [1] LC_COLLATE=English_United States.1252
## [2] LC CTYPE=English United States.1252
## [3] LC MONETARY=English United States.1252
## [4] LC NUMERIC=C
## [5] LC TIME=English United States.1252
## system code page: 1250
## attached base packages:
## [1] stats
                 graphics grDevices utils
                                                datasets methods
                                                                    base
##
## other attached packages:
   [1] xgboost_1.5.0.2
                         skimr_2.1.3
                                           keras_2.7.0
                                                            tensorflow_2.7.0
   [5] reticulate_1.18
                                           DALEX_2.2.0
                                                            caret_6.0-86
                         shapper_0.1.3
  [9] lattice 0.20-41
                         forcats 0.5.1
                                           stringr 1.4.0
                                                            dplyr 1.0.7
## [13] purrr_0.3.4
                         readr 1.4.0
                                           tidyr_1.1.4
                                                            tibble_3.1.6
## [17] ggplot2_3.3.5
                         tidyverse 1.3.1
##
## loaded via a namespace (and not attached):
## [1] nlme_3.1-152
                             fs_1.5.0
                                                   lubridate_1.7.10
   [4] httr 1.4.2
                             repr_1.1.3
                                                   tools 4.0.4
##
                                                   R6 2.5.0
## [7] backports 1.2.1
                             utf8 1.2.1
## [10] rpart_4.1-15
                             DBI_1.1.1
                                                   colorspace 2.0-0
## [13] nnet_7.3-15
                             withr_2.4.1
                                                   tidyselect_1.1.0
                                                   rvest_1.0.0
## [16] compiler_4.0.4
                             cli_3.1.0
## [19] xml2_1.3.2
                                                   scales_1.1.1
                             labeling_0.4.2
## [22] tfruns_1.5.0
                             rappdirs_0.3.3
                                                   digest_0.6.27
## [25] rmarkdown_2.7
                             base64enc_0.1-3
                                                   pkgconfig_2.0.3
## [28] htmltools_0.5.1.1
                             highr_0.8
                                                   dbplyr_2.1.1
## [31] rlang_0.4.10
                             readxl_1.3.1
                                                   rstudioapi_0.13
## [34] farver_2.1.0
                             generics_0.1.0
                                                   jsonlite_1.7.2
## [37] ModelMetrics_1.2.2.2 magrittr_2.0.1
                                                   Matrix 1.3-2
## [40] Rcpp_1.0.6
                             munsell_0.5.0
                                                   fansi_0.4.2
## [43] lifecycle 1.0.0
                             stringi 1.5.3
                                                   whisker 0.4
## [46] pROC_1.17.0.1
                             yaml_2.2.1
                                                   MASS_7.3-53
## [49] plyr_1.8.6
                             recipes_0.1.17
                                                   grid 4.0.4
## [52] crayon_1.4.1
                             haven_2.3.1
                                                   splines_4.0.4
                             zeallot_0.1.0
                                                   knitr 1.31
## [55] hms 1.0.0
## [58] pillar_1.6.4
                             reshape2 1.4.4
                                                   codetools 0.2-18
                             reprex_2.0.0
                                                   glue_1.4.2
## [61] stats4 4.0.4
                             data.table_1.14.0
## [64] evaluate_0.14
                                                   modelr_0.1.8
## [67] vctrs_0.3.8
                             foreach_1.5.1
                                                   cellranger_1.1.0
## [70] gtable_0.3.0
                             assertthat_0.2.1
                                                   xfun_0.22
## [73] gower_0.2.2
                             prodlim_2019.11.13
                                                   broom_0.7.10
## [76] class_7.3-18
                             survival_3.2-7
                                                   timeDate_3043.102
                                                   ellipsis_0.3.2
## [79] iterators_1.0.13
                             lava_1.6.9
## [82] ipred_0.9-12
```

Py: version: 3.8.5 (default, Sep 3 2020, 21:29:08) [MSC v.1916 64 bit (AMD64)] Architecture: 64bit numpy_version: 1.19.2