

**ISTA 116: WEB QUIZ 6 (6 PTS)**

- (1) Suppose  $E_1$  and  $E_2$  are disjoint events, with  $P(E_1) = 0.5$  and  $P(E_2) = 0.2$ . What is  $P_{E_1}(E_2)$ ?
- (a): 0.00
  - (b): 0.10
  - (c): 0.20
  - (c): 0.40
  - (d): 0.50
  - (e): 0.70
  - (f): There is not enough information.
- (2) For two events  $E_1$  and  $E_2$  (not necessarily disjoint this time), which of the following characterizes the relationship between  $P_{E_1}(E_2)$  and  $P_{E_2}(E_1)$ ?
- (a): They are always equal.
  - (b): They are equal if  $E_1$  and  $E_2$  are independent.
  - (c): They are equal if  $P(E_1) = P(E_2)$ , but  $P_{E_1}(E_2)$  is greater than  $P_{E_2}(E_1)$  if  $P(E_1) > P(E_2)$ .
  - (d): They are equal if  $P(E_1) = P(E_2)$ , but  $P_{E_1}(E_2)$  is greater than  $P_{E_2}(E_1)$  if  $P(E_2) > P(E_1)$ .
  - (e): They are equal if  $P(E_1) = P(E_2)$ , but otherwise it depends on the context.
  - (f): We can't say anything about the relationship without knowing the context.

Questions 3-6 refer to the following scenario:

A store manager reads that about 1 in 10 employees steal small amounts of cash during work. When the books don't balance one month, she decides to investigate with a lie detector (this may well be illegal, but let's roll with it for the sake of the example). The lie detector is supposedly 80% accurate in both directions (i.e., 80% of true statements pass without setting it off, and 80% of false statements do set it off). Supposing the above probabilities are correct, what is:

- (3) the (joint) probability that a given employee *both* stole *and* sets off the machine?
- (a): 0.080
  - (b): 0.100
  - (c): 0.125
  - (d): 0.700
  - (e): 0.800
- (4) the (joint) probability that a given employee did not steal but sets off the machine anyway?
- (a): 0.100
  - (b): 0.180
  - (c): 0.200
  - (d): 0.720
  - (e): 0.800
- (5) the *marginal* probability that an employee sets off the lie detector?
- (a): 0.200
  - (b): 0.260
  - (c): 0.500
  - (d): 0.720
  - (e): 0.800

(6) the *conditional* probability that an employee stole, *given* that s/he has set off the lie detector?

(a): 0.100

(b): 0.308

(c): 0.385

(d): 0.800

(e): 0.900