Overall electrochemical reaction inside a fuel cell system

$$H_2(fuel) + O_2(oxidant) = W + Q + H_2O(product)$$
 E1

General electrical work

$$W = EI\Delta t = E2$$

The electrical work done in the fuel cell system

$$W = -nFE_{cell}$$
 E3

The Gibbs free energy is the maximum amount of work done on the system.

$$W_{el} = \Delta G$$
 E4

$$\Delta G = -nFE_{cell}$$
 E5

The maximum cell potential or the reversible cell potential becomes

$$E_{rev} = \frac{\Delta G}{-nF}$$
 E6

If all the potential chemical energy for a reaction went into electrical work and there was no heat transfer, there would be no entropy change; dG = dH. In this case, we can show that:

$$E_{rev} = \frac{\Delta H}{-nF}$$
 E7

For a generic reaction or process

$$aA + bB \rightarrow cC + dD$$
 E8

$$\Delta G_f = \Delta G_f^0 + RTIn[\frac{aC^c aD^d}{aA^a aB^a}]$$
 E9

To convert to voltage

$$RTIn\left(\frac{aC^{c}aD^{d}}{aA^{a}aB^{a}}\right)$$

$$E(T,P) = E^{o} - \frac{nF}{nF}$$
E10