

Data models (1 / 2)

- A **model** is an abstract representation
 - We care about data, so we have **data models**
- Do you know your data?
 - Is there something missing?
 - Are there redundancies?
 - How do various components of your data fit together?

Data models (2/2)

- To design a database, we first need a schema
 - Remember logical/physical independence ?
- Use a data model to design the schema
 - We will study two data models: ER and relational

ER MODEL

Entity-Relationship model (2/2)

- Entity sets ←
 - Actors, movies, studios
- Attributes ←
 - Atomic values
 - Name, age, height ← Actors
- Relationships ←
 - Between two entity sets
 - Actors actsIn Movies
↑ ↑

Go back and revise from the text book. Almost all material is from there.

ER diagram



Entity set

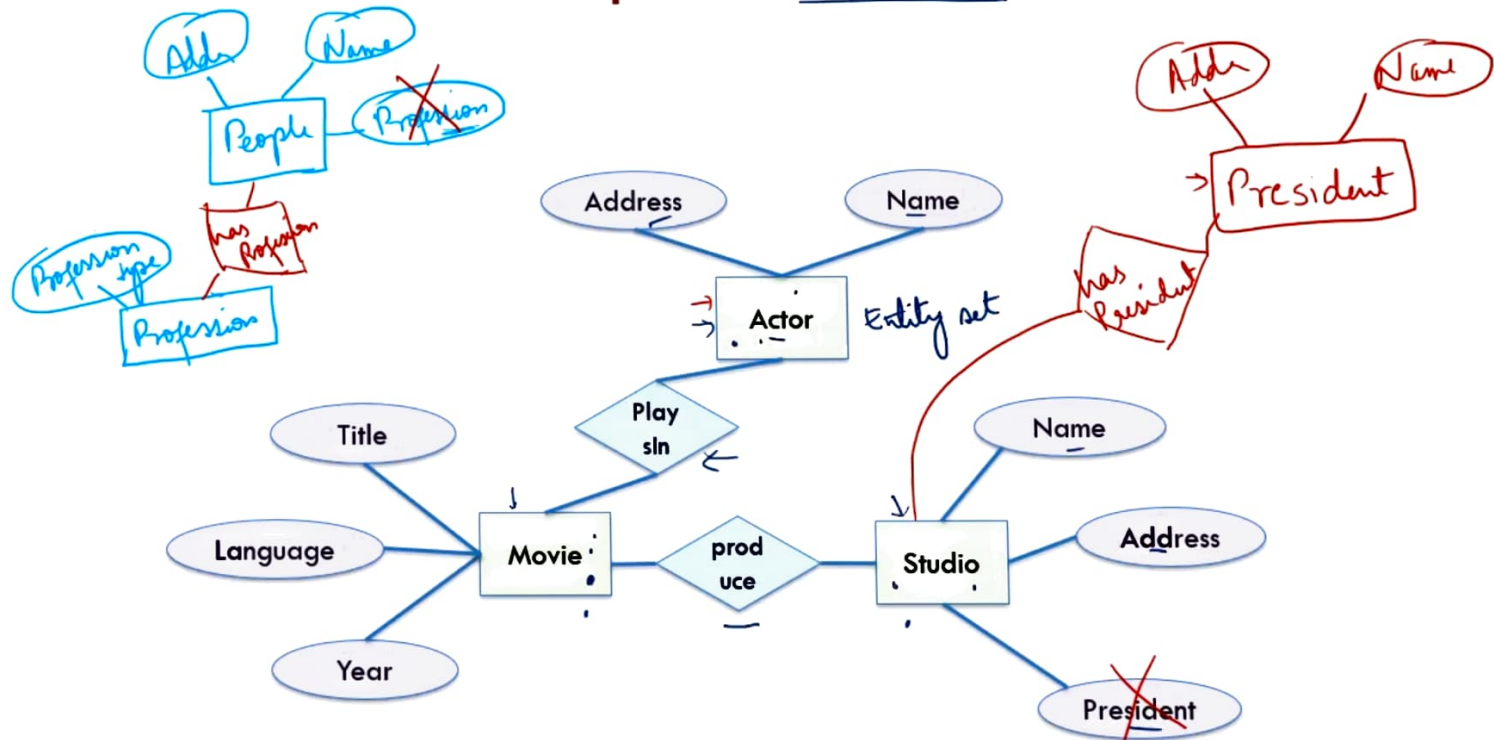


Attribute



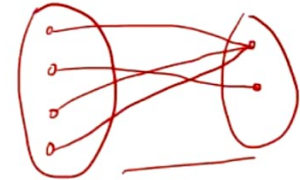
Relationship

Example – Movie DB



Types of relationships (1 / 2)

Movie produced by *at most* one studio, but a studio produces many movies



An actor plays at most one role, a role is played by at most one actor



Double roles

A movie has many actors, an actor plays in many movies



Types of relationships (2/2)

- **one-one**
 - an entity of one entity set is related to *at most* one entity of another entity set *and vice-versa*
- **many-one**
 - many entities of one entity set are related to *at most* one entity of another entity set
- **many-many**

Remember the maths

$$\begin{array}{l} \text{Entity} \\ \text{sets} \end{array} - A = \{a_1, a_2, a_3\}$$

$$- B = \{b_1, b_2\}$$

$$A \times B = \{(a_1, b_1), (a_1, b_2), (a_2, b_1), (a_2, b_2), (a_3, b_1), (a_3, b_2)\}$$

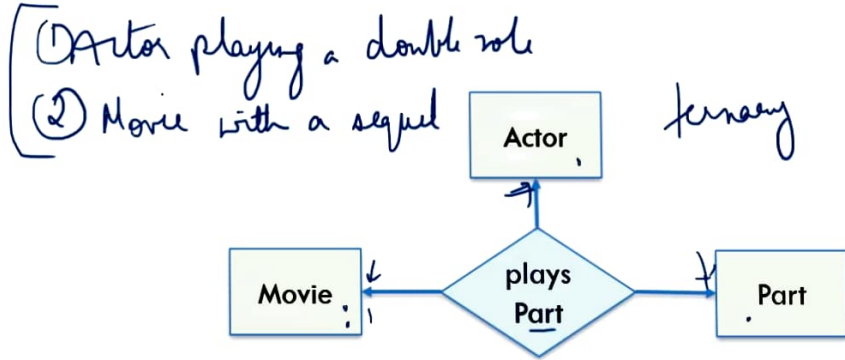
$$\begin{array}{l} \nearrow \\ \text{relation} \end{array} R \subseteq A \times B$$

one-one
many-one
man

ER model: Relationships

Multi-way relationships

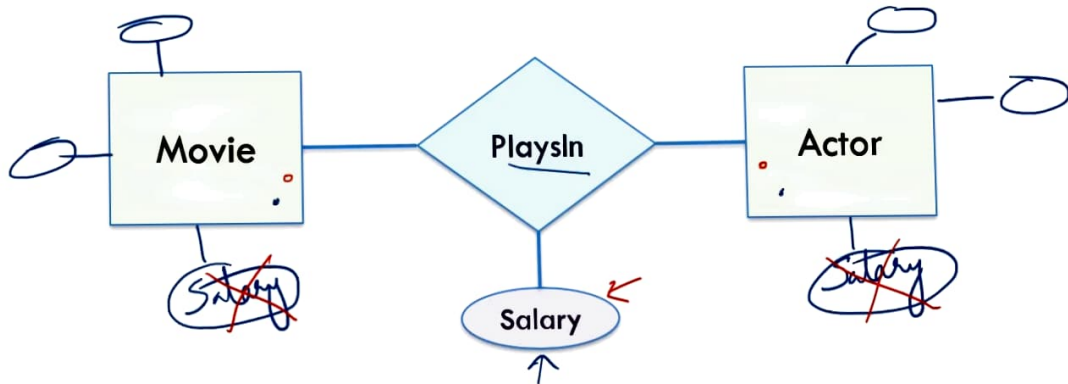
- Non-binary relationships



↓	↓	↓
Priyanka Chopra	Baywatch	Victoria Leeds
Anthony Hopkins	Thor: Ragnarok	Odin

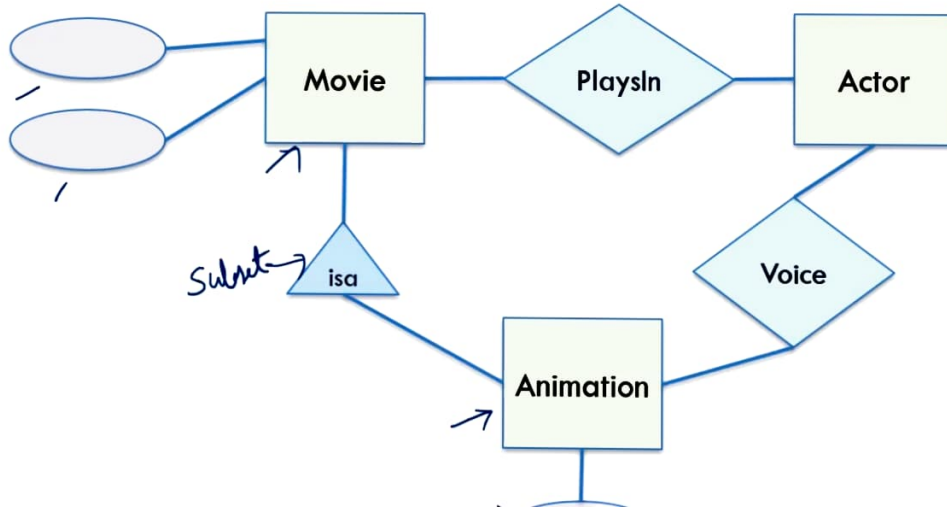
Attributes on relationships

- An attribute depends on a combination of entities, not a single entity
 - Relationships are how entities are combined!

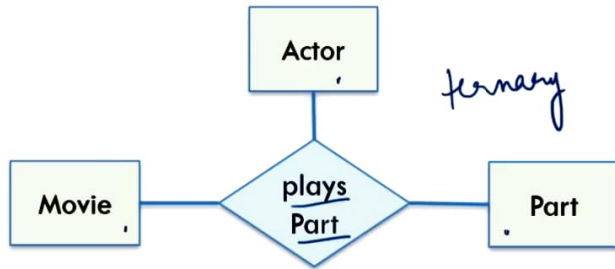


Modeling subsets

- ER model allows for hierarchies
 - Sound familiar?



N-ary to binary

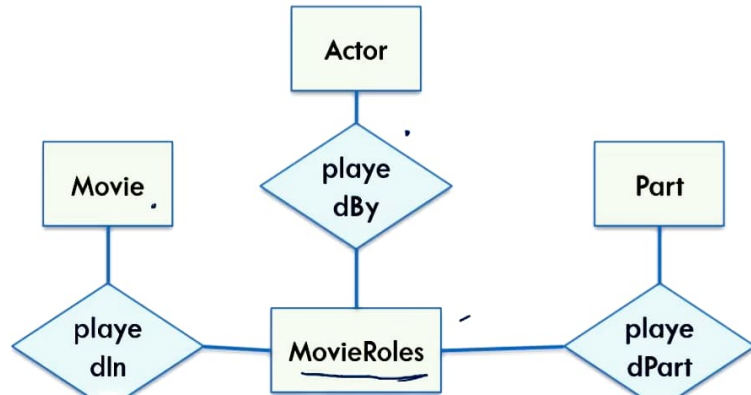


ternary

MRI
MRI
MRI

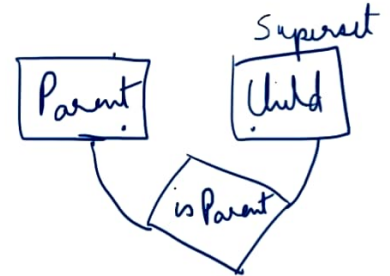
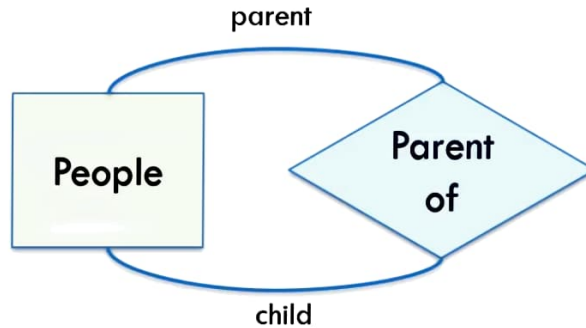
X - Movie
Y - Actor
Z - Part

MRI	X	Y	Z
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“Parallel” relationships

- A relationship from an entity set to itself
 - Each edge indicates a *role*



ER model

CONSTRAINTS

Modeling constraints

- Constraints model restrictions on the data
 - Data may be erroneous
 - Mistakes may be made during the data entry process 650^{0, 100}
↑
- Modeling the correct constraints are part of the design process

Common constraints (1 / 2)

- Keys

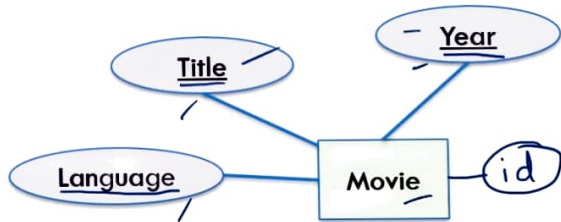
- How is an entity uniquely identified?
- (Name, Year of birth) identifies an actor uniquely

- Single-value constraints

- Unique values in a given context
- Place of birth has to be unique
- Null values

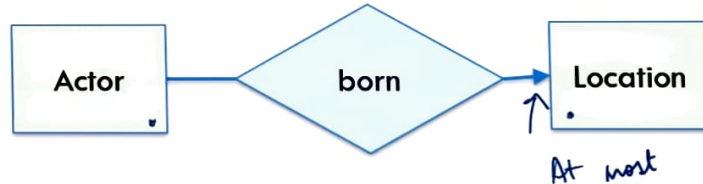
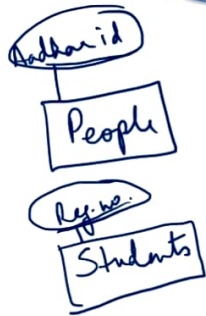
Profession

Key constraints and single value constraints



- Every entity set should have a key
- There could be more than one key ←

Keys



Common constraints (2/2)

- Referential integrity



- Remove the null, insist on the value

- If an actor acts in a movie, then that movie has to exist in the database

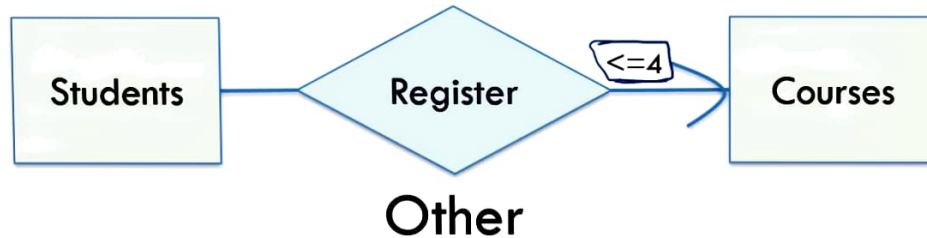
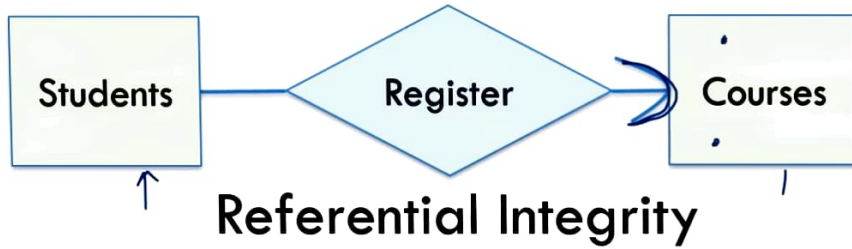
- Domain constraints ←

- Restricting the value set of attributes ←

- Age in range from 0 to 100 (or is it 0 to 25?)

- General constraints ←

Representing constraints (2/2)



The Relational Model

Only one structure – relation

- A relation is both a mathematical concept and just a table of values
- The relational model models “everything” as relations

Example

Schema of the relation:

Actor-Movies (Name varchar(20), Movie varchar(50), Character varchar(20))

*Name of
relation/table*

Actor-Movies

instance of the relation

Name	Movie	Character
Priyanka Chopra	Baywatch	Victoria Leeds
Tom Cruise	MI-I	Ethan Hunt
Anthony Hopkins	Thor: Ragnarok	Odin

←

← *tuple*

More about relations

- A relation is a set of tuples, not a bag
- Permuting the order of attributes does not matter

$$R \subseteq A \times B$$

↑ set ↑ sets

↓

↓

↓

Name	Movie	Character
Priyanka Chopra	Baywatch	Victoria Leeds
Tom Cruise	MI-I	Ethan Hunt
Anthony Hopkins	Thor: Ragnarok	Odin

→

↓

↓

↓

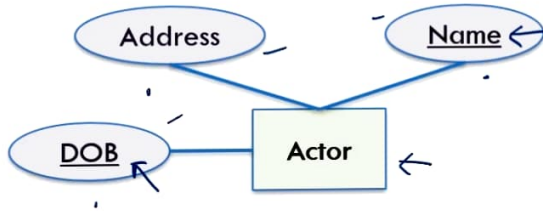
Character	Movie	Name
Victoria Leeds	Baywatch	Priyanka Chopra
Ethan Hunt	MI-I	Tom Cruise
Odin	Thor: Ragnarok	Anthony Hopkins

=

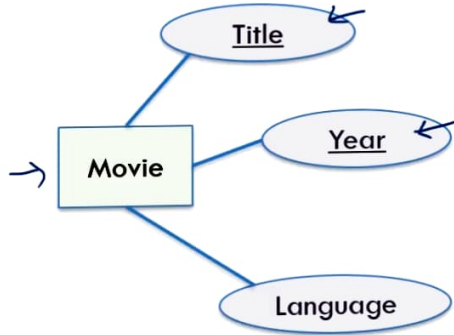
ER to relational

- ER diagrams are easy to comprehend and closer to how we think
- Relational model is powerful because it is simple – only one kind of object
 - Any operation on the relation, results in yet another relation
- So, let's convert our ER diagrams to relational!

Entity sets/attributes

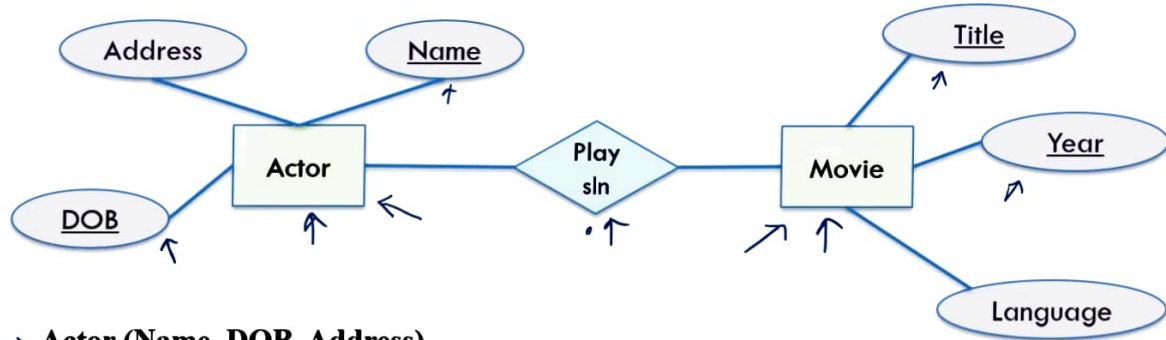


Actor (Name, DOB, Address)



Movie (Title, Year, Language)

Relationships to relations



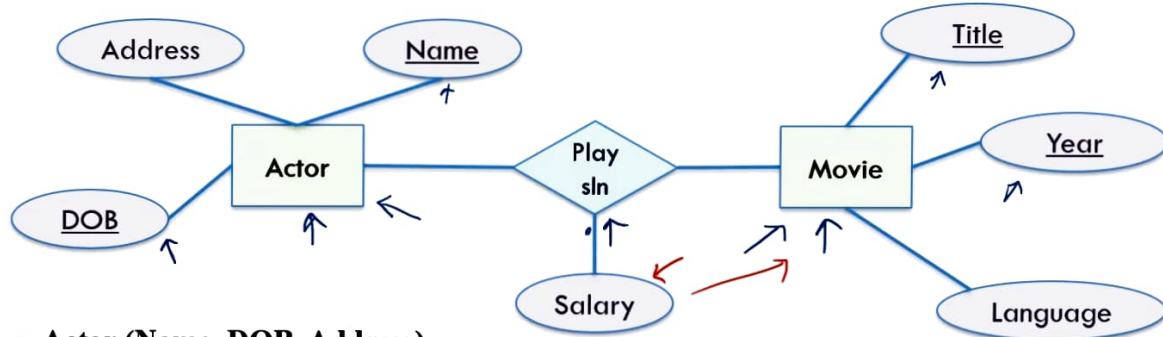
→ Actor (Name, DOB, Address)

→ Movie (Title, Year, Language)

→ PlaysIn (Name, DOB, Title, Year)

↑ Actor ↑ Movie

Relationships to relations



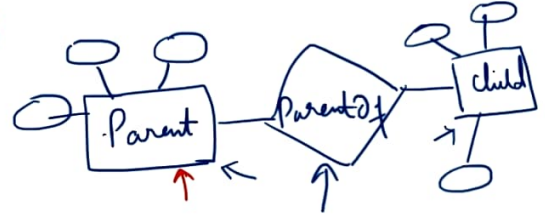
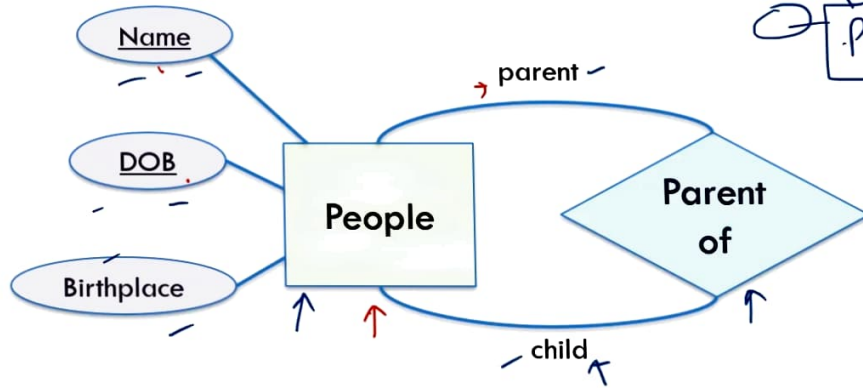
→ Actor (Name, DOB, Address)

→ Movie (Title, Year, Language)

→ PlaysIn (Name, DOB, Title, Year), Salary)

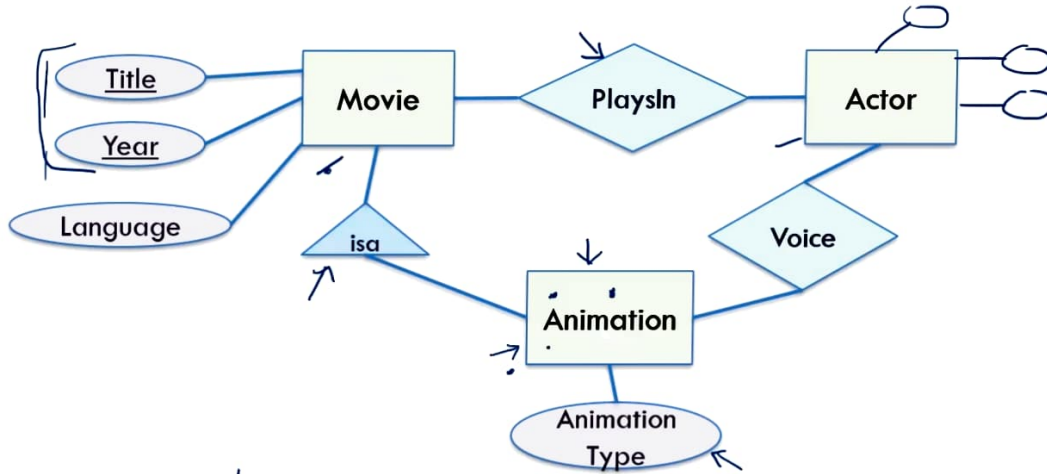
PlaysIn (Name, DOB, Title, Year, Salary)

Roles to relations



→ People (Name, DOB, Birthplace)
parentOf (parentName, parentDOB, ^{child}childName, childDOB)

Hierarchies to relations



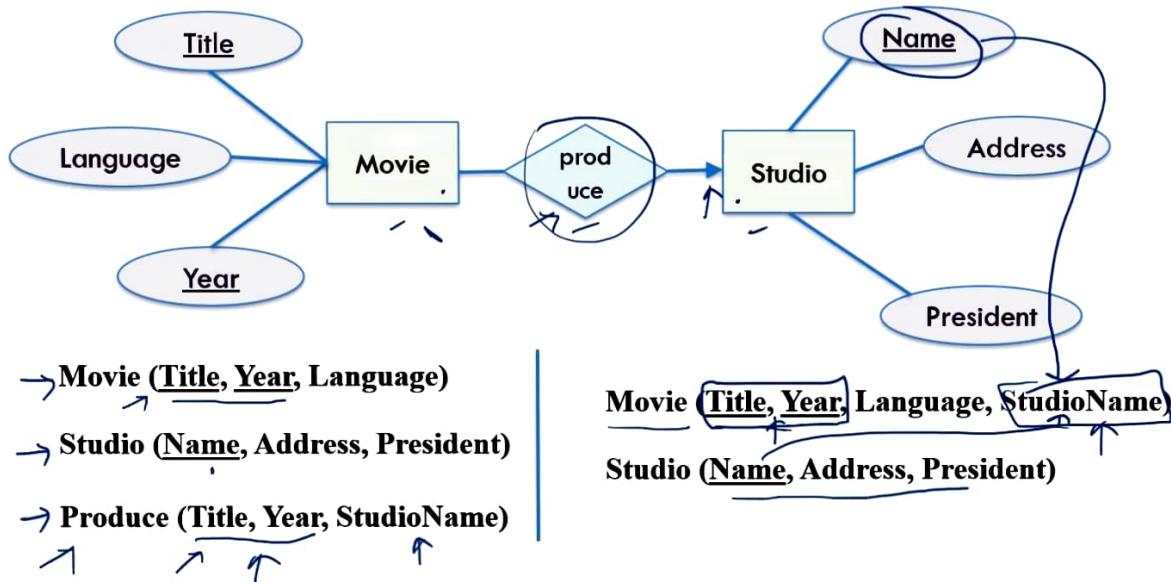
→ **Movie** (Title, Year, Language)

→ **Actor** (Name, DOB, City)

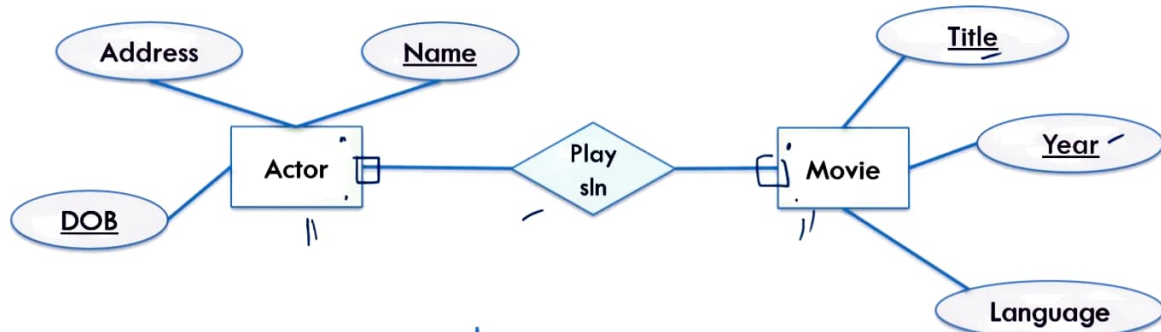
Animation (Title, Year, AnimationType)

AllMovies (Title, Year, Language, AnimationType)

Combining relations (1 / 2)



Combining relations (2/2)



→ Actor (Name, DOB, Address)

→ Movie (Title, Year, Language)

→ PlaysIn (Name, DOB, Title, Year)

Actor (Name, DOB, Address, MovieTitle, Year)

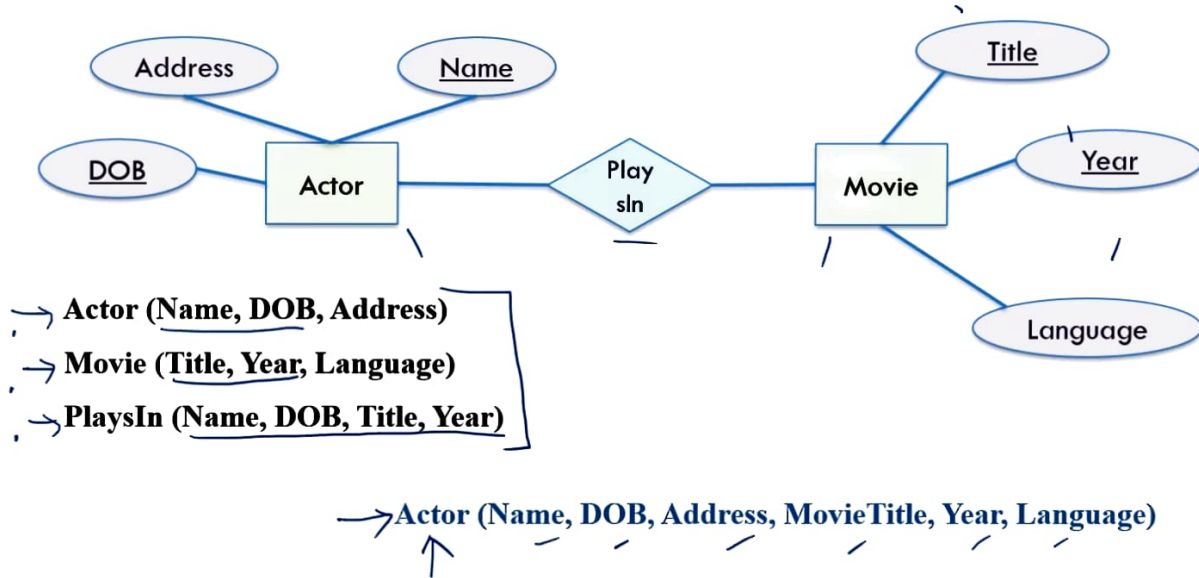
Movie (Title, Year, Language)

→ Actor (Name, DOB, Address)

→ Movie (Title, Year, Language, ActorName, DOB)

NORMALIZATION

Designing good schemas



"Universal Table"

Anomalies

Actor Movie

Name	DOB	Address	MTitle	Year	Language
Priyanka Chopra	1992	Mumbai	Don	2006	Hindi
Priyanka Chopra	1992	Mumbai	Don II	2011	Hindi
Anthony Hopkins	1937	LA	Thor: Ragnarok	2017	English
Tom Cruise	1962	LA	Valkyrie	2008	English
Bill Nighy	1949	LA	Valkyrie	2008	English

• Redundancy ←

• Update Anomalies

- Priyanka Chopra's changed to Priyankaa Chopra

• Deletion Anomalies

- Delete the movie "Valkyrie" from the DB

→ **Normalization** is the process of systematically eliminating these anomalies

Functional Dependencies (1 / 2)

- A functional dependency is another kind of constraint
- If two tuples in a relation agree on the values of one set of attributes then they must also agree on the values of another set of attributes.

$\rightarrow R(A_1, A_2, A_3, B_1, B_2, B_3)$

$\rightarrow A_1 A_2 A_3 \xrightarrow{\text{functionally determine}} B_1$

$\rightarrow A_1 A_2 A_3 \rightarrow B_2$

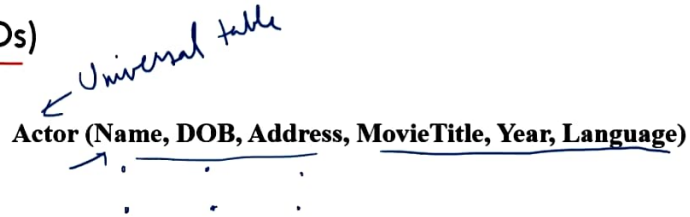
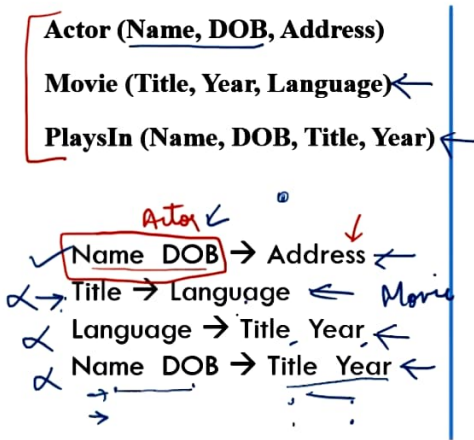
$A_1 A_2 A_3 \rightarrow B_3$

Shorthand $\rightarrow \underline{A_1 A_2 A_3} \rightarrow \underline{B_1 B_2 B_3}$

	A_1	A_2	A_3	B_1	B_2	B_3
+1 \rightarrow	1	2	3	0	1	0
	1	0	1	1	0	1
+3 \rightarrow	1	2	3	0	1	0
	1	0	1	1	0	1

Functional Dependencies (2/2)

- Example (figure out the right FDs)



Trivial and non-trivial FDs

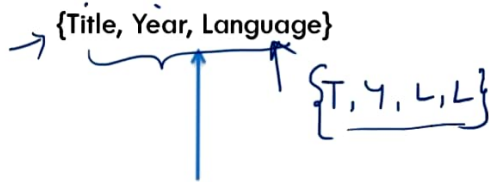
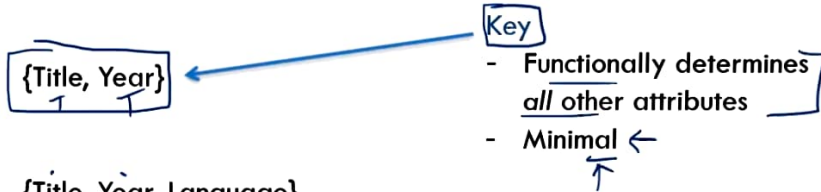
Actor (Name, DOB, Address)**Movie (Title, Year, Language)****PlaysIn (Name, DOB, Title, Year)**

Name DOB → Address ← Non-keyed FD
 Name DOB → Name ← keyed FD
 Name DOB → Name Address ← Non-keyed FD
 ↑
 Address

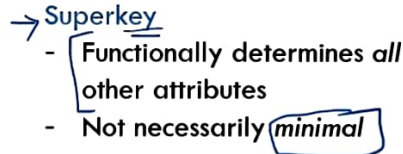
Keys and superkeys

→ Movie (Title, Year, Language, Length)

$T, Y \rightarrow L, L$



$T, Y, L \rightarrow L$
 $T, Y, L \rightarrow T$
 $T, Y, L \rightarrow Y$



Terminology

- Key ✓
 - Superkey ✓
 - Candidate key ✓
 - Primary key ✓
 - Prime attribute
- Keys*
Only one candidate key

Inferring FDs

- Given a set of FDs, which other FDs follow from it?
- **Example:**

– Given: $\left\{ \begin{array}{l} \{\text{Name}, \text{DOB}\} \rightarrow \text{Address} \\ \text{Address} \rightarrow \text{City} \end{array} \right.$

– Inferred: $\{\text{Name}, \text{DOB}\} \rightarrow \text{City}$



Inferred through *transitivity* of FDs

- Reflexivity \leftarrow
If B is a subset of A, then A \rightarrow B Trivial FD

Trivial FD

- Augmentation \leftarrow
If $A \rightarrow B$, then $\underline{AC} \rightarrow \underline{BC}$

If $A \rightarrow B$, then $\underline{AC} \rightarrow \underline{BC}$

- Transitivity \leftarrow
If $A \rightarrow B$ and $B \rightarrow C$, then $A \rightarrow C$

If $A \rightarrow B$ and $B \rightarrow C$, then $A \rightarrow C$

Closure of FDs

- Given: S , the set of FDs
- Output: S^+ , the closure of S , containing all FDs derivable from S

- Example: $\{A, B, C, D, E\}$

$$\begin{array}{l} \rightarrow AB \rightarrow C \\ \rightarrow C \rightarrow ED \end{array}$$

Basis



Is this set S^+

$$\begin{array}{l} AB \rightarrow ED \\ AB \rightarrow E \\ ABC \rightarrow ED \\ C \rightarrow E \\ C \rightarrow D \end{array}$$

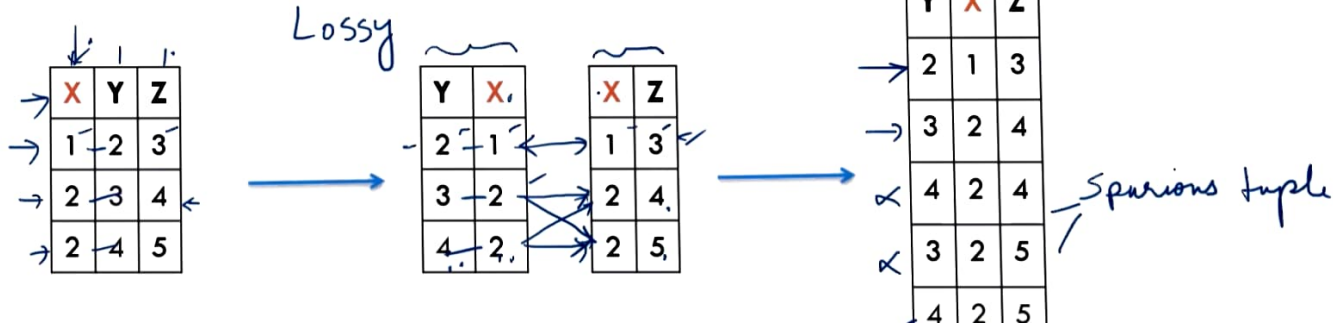
① Are they correctly derived?

② What is missing from this set

NORMAL FORMS

Relation decomposition

- Breaking up a relation into two or more
- Tuples are projected accordingly
- Lossy and lossless decomposition
 - Can the original table be recovered from the decomposed tables?



First normal form

- 1NF (First normal form)
 - A relation is in 1NF iff every tuple contains an atomic value for each attribute
 - Follows directly from definition of relation
 - Relation contains a key ←

Second normal form (1/2)

→ No non-prime attribute in the table is functionally dependent on a proper subset of any candidate key

Universal relation

Name DOB MTitle Year → Address Language

<u>Name</u>	<u>DOB</u>	<u>Address</u>	<u>MTitle</u>	<u>Year</u>	<u>Language</u>
Priyanka Chopra	1992	Mumbai	Don	2006	Hindi
Priyanka Chopra	1992	Mumbai	Don II	2011	Hindi
Tom Cruise	1962	LA	MI-IV	2011	English
Anthony Hopkins	1937	LA	Thor: Ragnarok	2017	English
Bill Nighy	1949	LA	Valkyrie	2008	English

N, D → A

<u>Name</u>	<u>DOB</u>	<u>Address</u>
Priyanka Chopra	1992	Mumbai
Anthony Hopkins	1937	LA
Bill Nighy	1949	LA
Tom Cruise	1962	LA

T, Y → L

<u>MTitle</u>	<u>Year</u>	<u>Language</u>
Don	2006	Hindi
Don II	2011	Hindi
MI-IV	2011	English
Valkyrie	2008	English

What are we missing here?

Second normal form (2/2)

Name	DOB	Address	MTitle	Year	Language
Priyanka Chopra	1992	Mumbai	Don	2006	Hindi
Priyanka Chopra	1992	Mumbai	Don II	2011	Hindi
Anthony Hopkins	1937	LA	MI-IV	2011	English
Anthony Hopkins	1937	LA	Valkyrie	2017	English
Bill Nighy	1949	LA	Valkyrie	2008	English

No non-prime attribute in the table is functionally dependent on a proper subset of any candidate key

Lossless

↓

ID	Name	DOB	Address
1	Priyanka Chopra	1992	Mumbai
2	Anthony Hopkins	1937	LA
3	Bill Nighy	1949	LA

→

AID	MID
1	1
1	2
2	3
3	4
4	5

↓

ID	MTitle	Year	Language
1	Don	2006	Hindi
2	Don II	2011	Hindi
3	MI-IV	2011	English
4	Valkyrie	2008	English
5	Thor: Ragnarok	2017	English

Third normal form

- 3NF (third normal form)
 - For a non-trivial FD $X \rightarrow Y$,
 X is a superkey or Y is prime

→

<u>Name</u>	<u>DOB</u>	Address	Country
Priyanka Chopra	1992	Mumbai	India
Anthony Hopkins	1937	LA	USA
Bill Nighy	1949	LA	USA

<u>Name</u>	<u>DOB</u>	<u>AID</u>	<u>ID</u>	<u>Address</u>	Country
Priyanka Chopra	1992	1	1	Mumbai	India
Anthony Hopkins	1937	2	2	LA	USA

$\text{Address} \rightarrow \text{Country}$
 Name, DOB \rightarrow Address
 Name, DOB \rightarrow Country

↓
 Addr → Country
 ↑

Violation of 3NF
 $X \rightarrow Y$
 $X \rightarrow A_1 A_2 A_3 \rightarrow Y$
 $X \rightarrow A_1 \rightarrow Y$

Boyce-Codd normal form

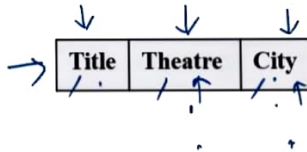
BCNF

For a non-trivial FD $X \rightarrow Y$,

X is a superkey [or Y is prime]

Addresses the following additional scenarios:

- Multiple candidate keys with intersecting elements
- All attributes are part of some key



Keys: Title, City

Theatre, Title

FDs:

$\text{Theatre} \rightarrow \text{City}$

$\text{Title, City} \rightarrow \text{Theatre}$

$\text{Theatre, Title} \rightarrow \text{City}$

Violating
BCNF

Lossless decomposition

- Algorithm:

- If $X \rightarrow Y$ is a BCNF violation, then form two relations:

- with attributes from $X \cup Y$

- with attributes from $X \cup (all-X-Y)$

$X \rightarrow Y$
 $X \mid A_1 \ A_2 \ Y$

X	Y
.	.

X	A ₁	A ₂
.	.	.

X	Y	Z
.	.	.

$X \ Y \quad X \ Z$