

Validate Power: d2.2

February 25, 2022

Design: Cluster RCT, with 2 levels, and randomization done at level 2 (school level).

Models: random treatment effects.

Default parameters:

- $M = 3$
- $J = 60$
- rho: $\rho = 0.5$
- MDES = 0.125, 0.125, 0.125
- R2: $R_1^2 = 0.1, 0.1, 0.1, R_2^2 = 0.1, 0.1, 0.1$
- ICC: $ICC_2 = 0.1, 0.1, 0.1$

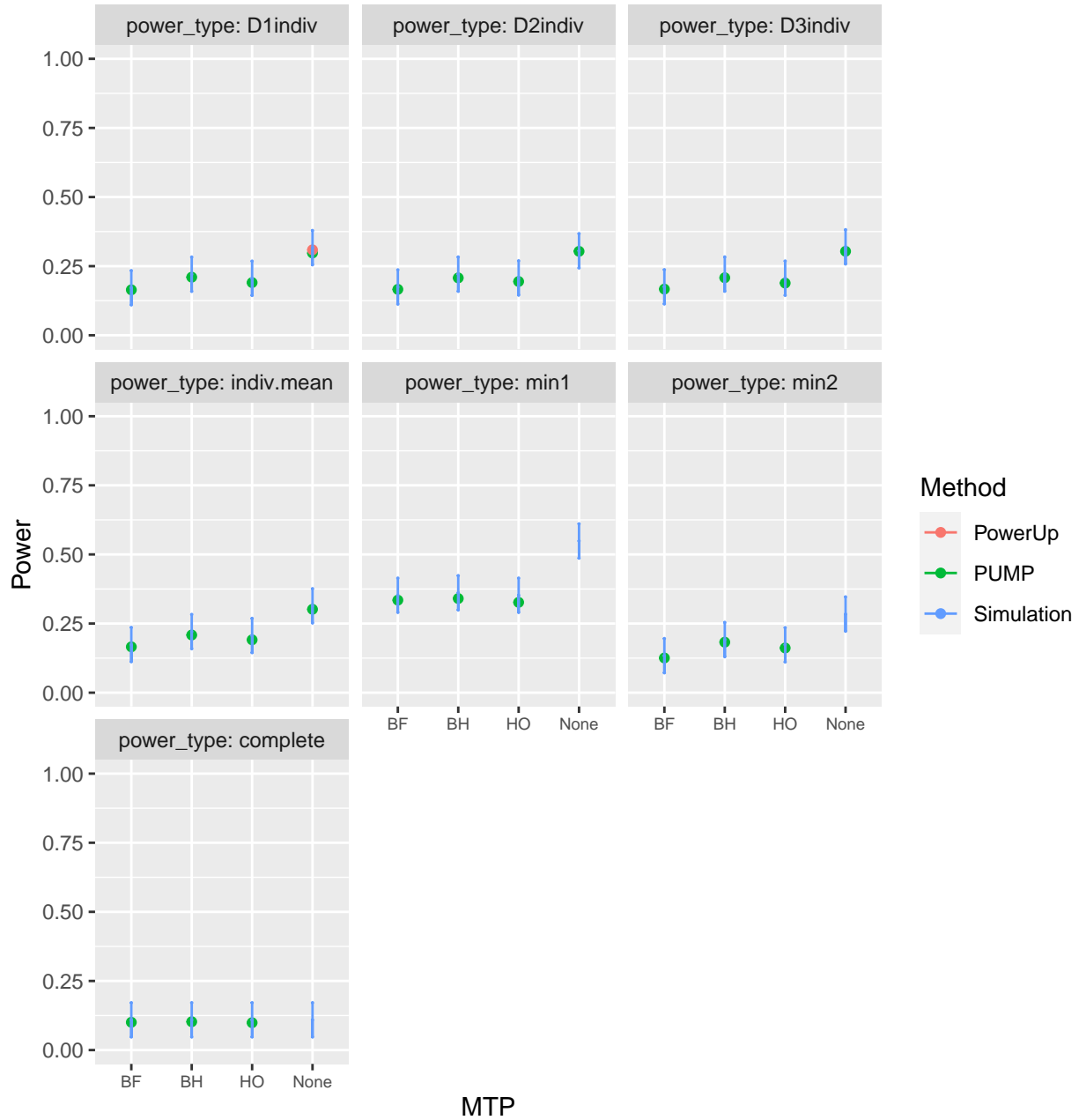
Assumptions

- Two-level design: $ICC_3 = 0, \omega_3 = 0, K = 1$
- Constant treatment effects: $\omega_2 = 0$

Power Validation

Base case

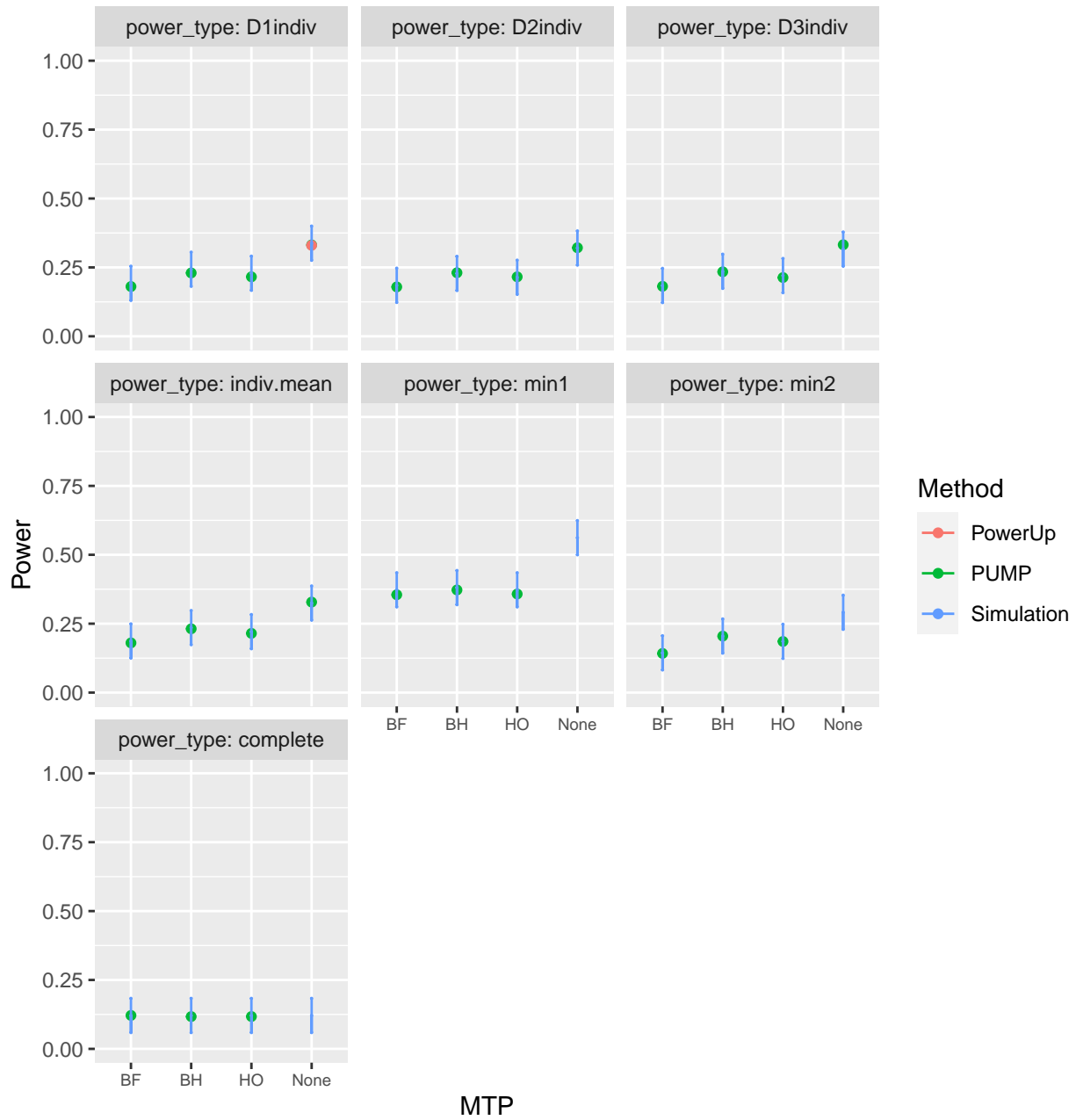
d_m: d2.2_m2rc



Varying school size

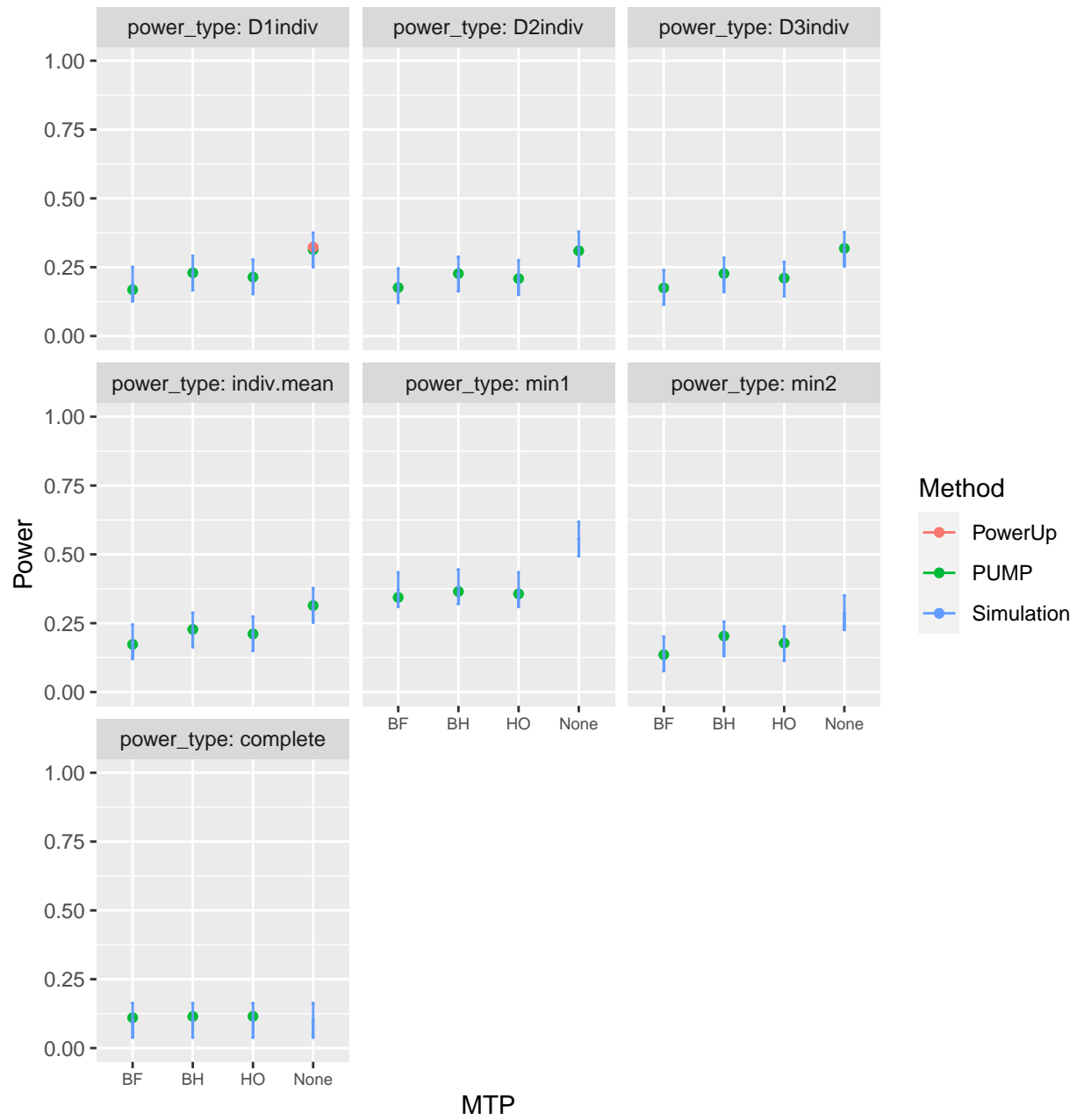
$\bar{n} = 100$

d_m: d2.2_m2rc



$\bar{n} = 75$

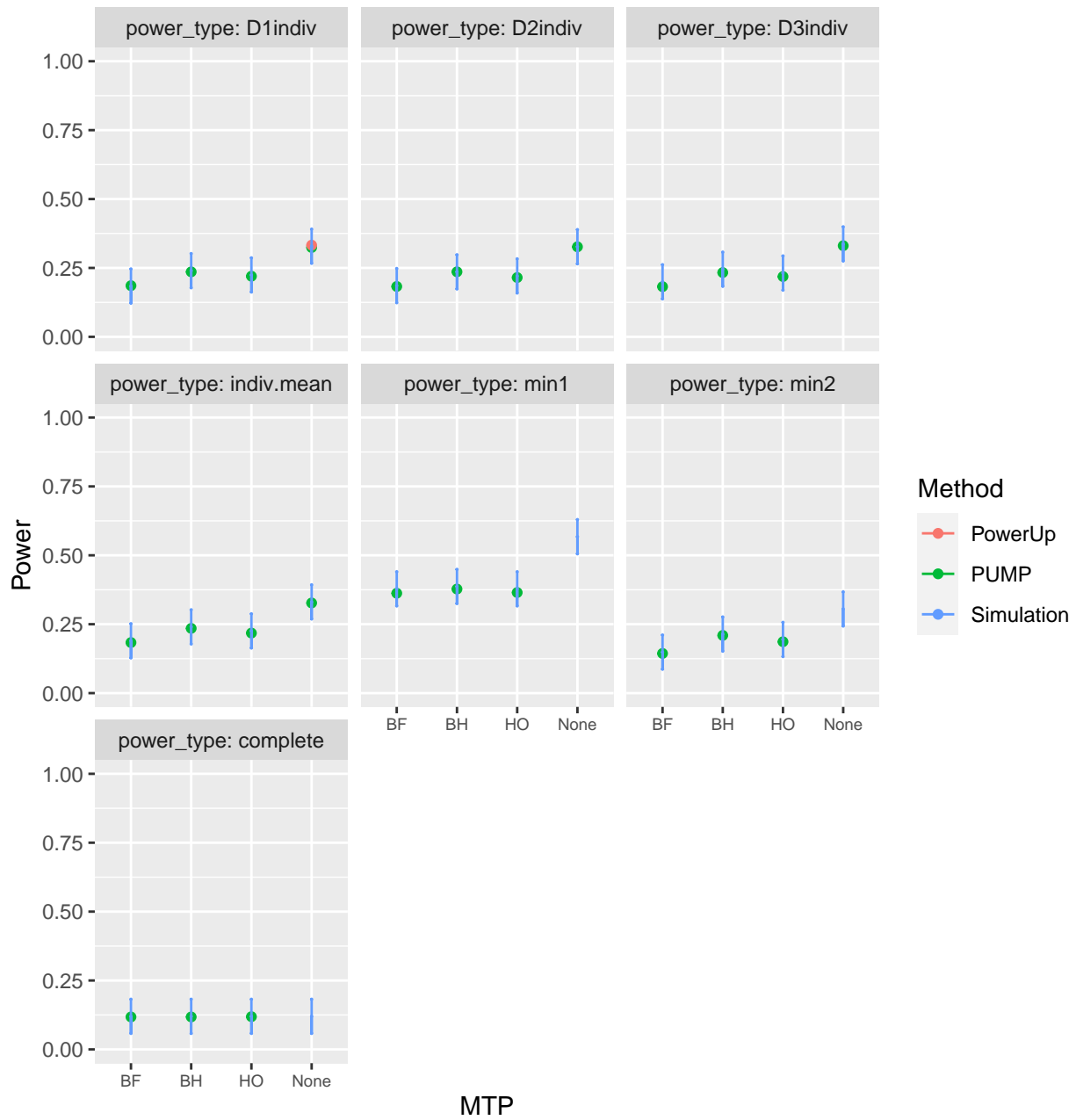
d_m: d2.2_m2rc



Varying R2

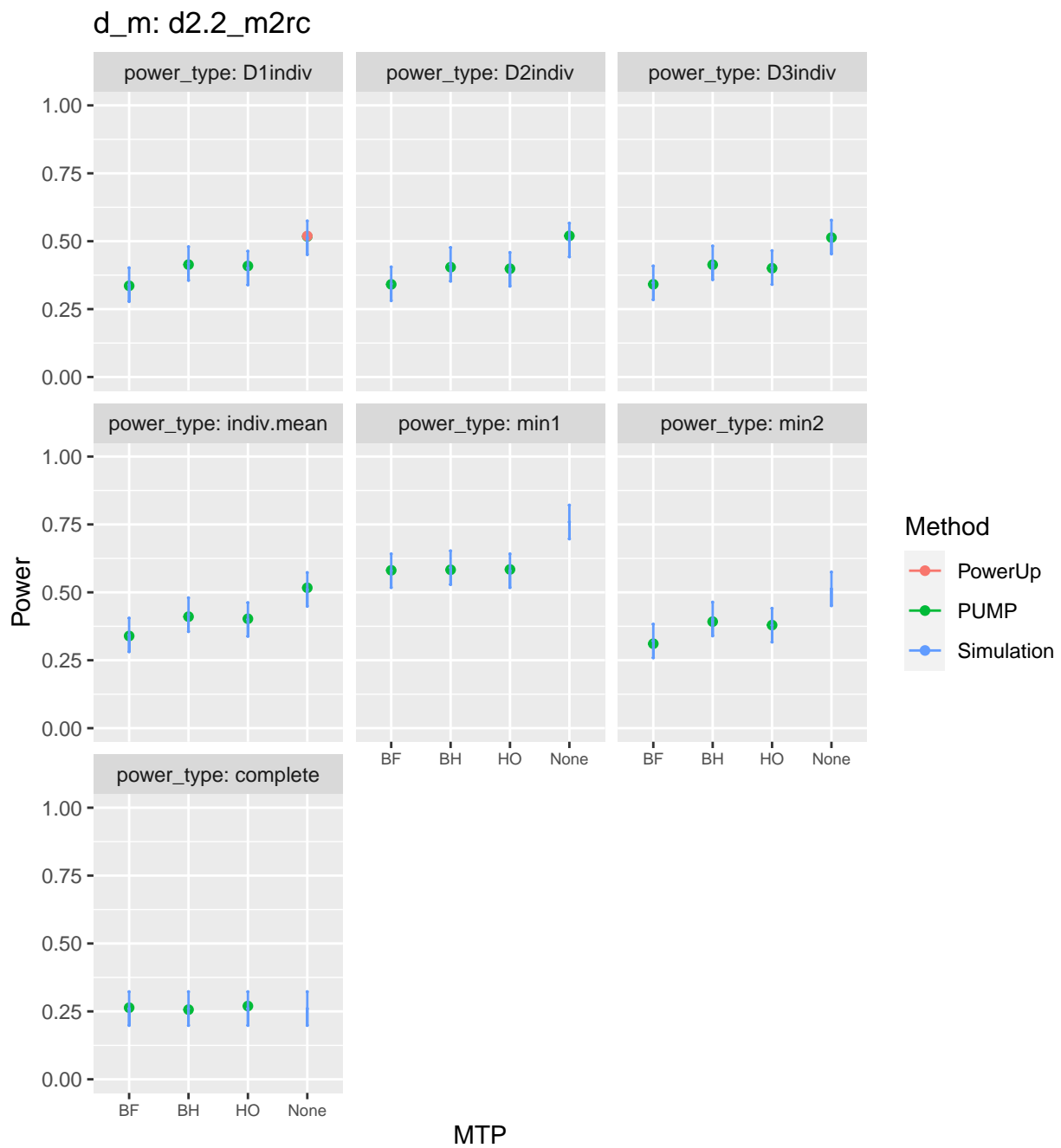
$R_1^2 = 0.6, 0.6, 0.6$

d_m: d2.2_m2rc



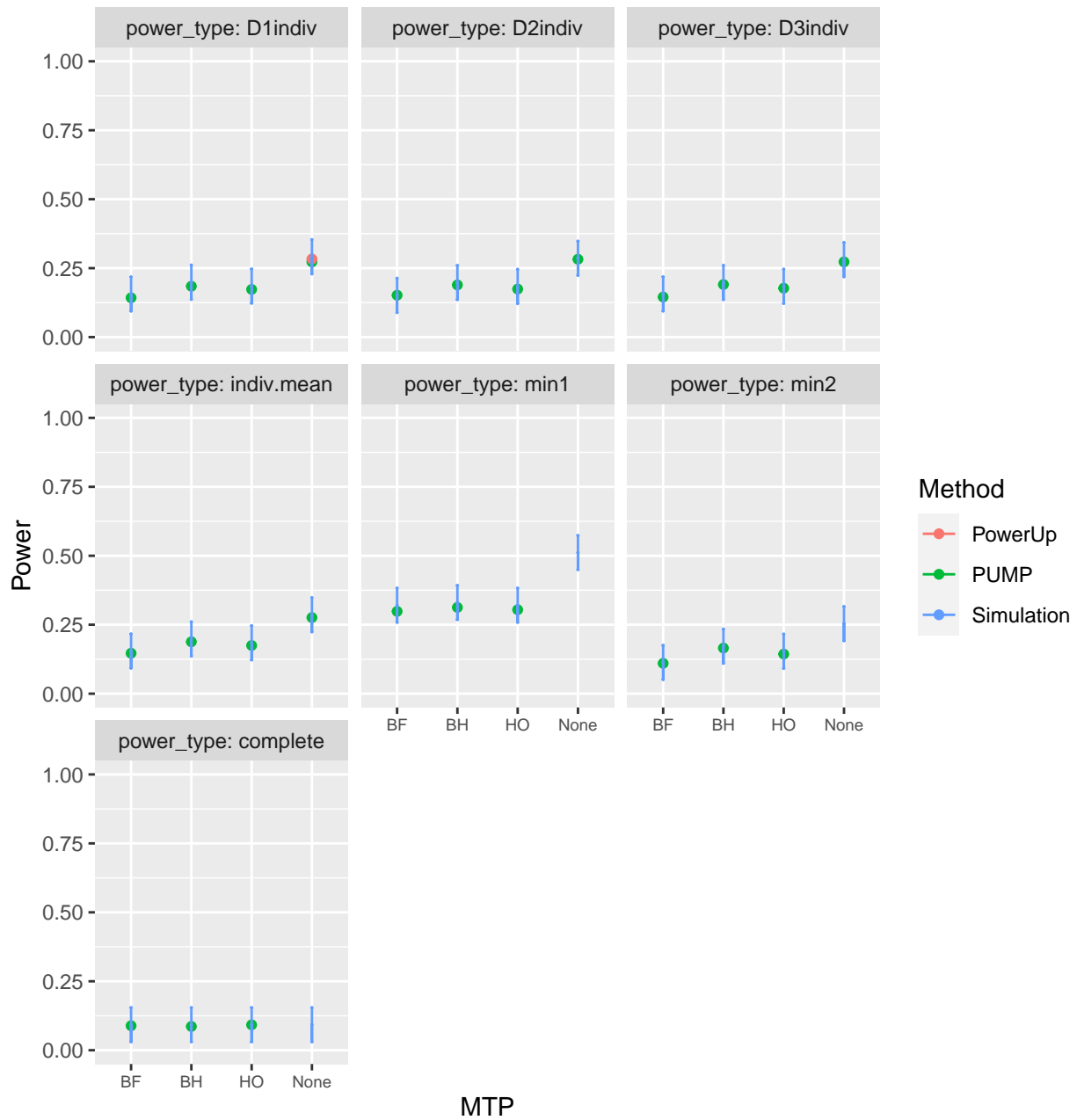
MTP

$$R_2^2 = 0.6, 0.6, 0.6$$



$$R_1^2 = 0, 0, 0 \quad R_2^2 = 0, 0, 0$$

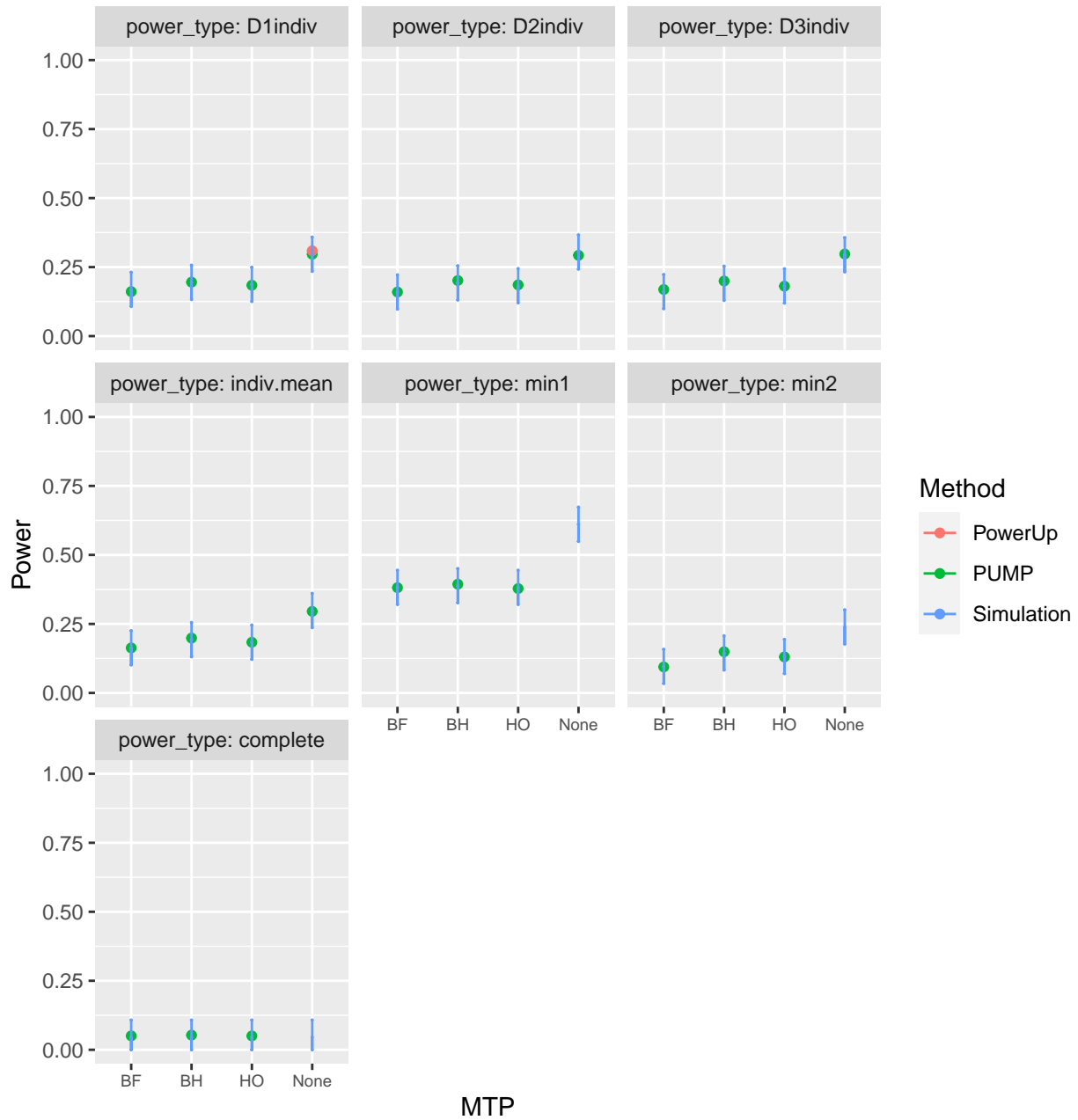
d_m: d2.2_m2rc



Varying rho

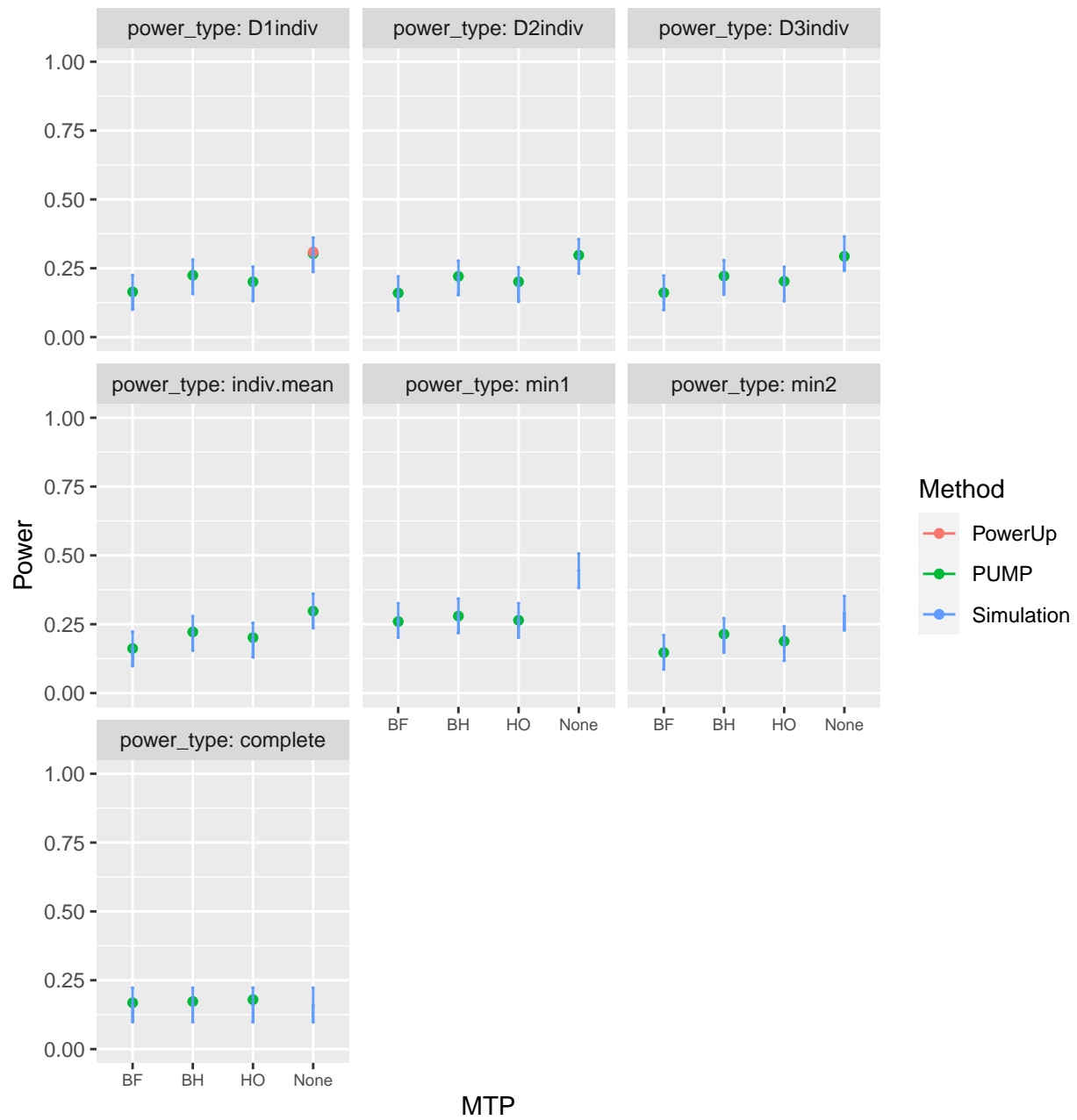
$\rho = 0.2$

d_m: d2.2_m2rc



$\rho = 0.8$

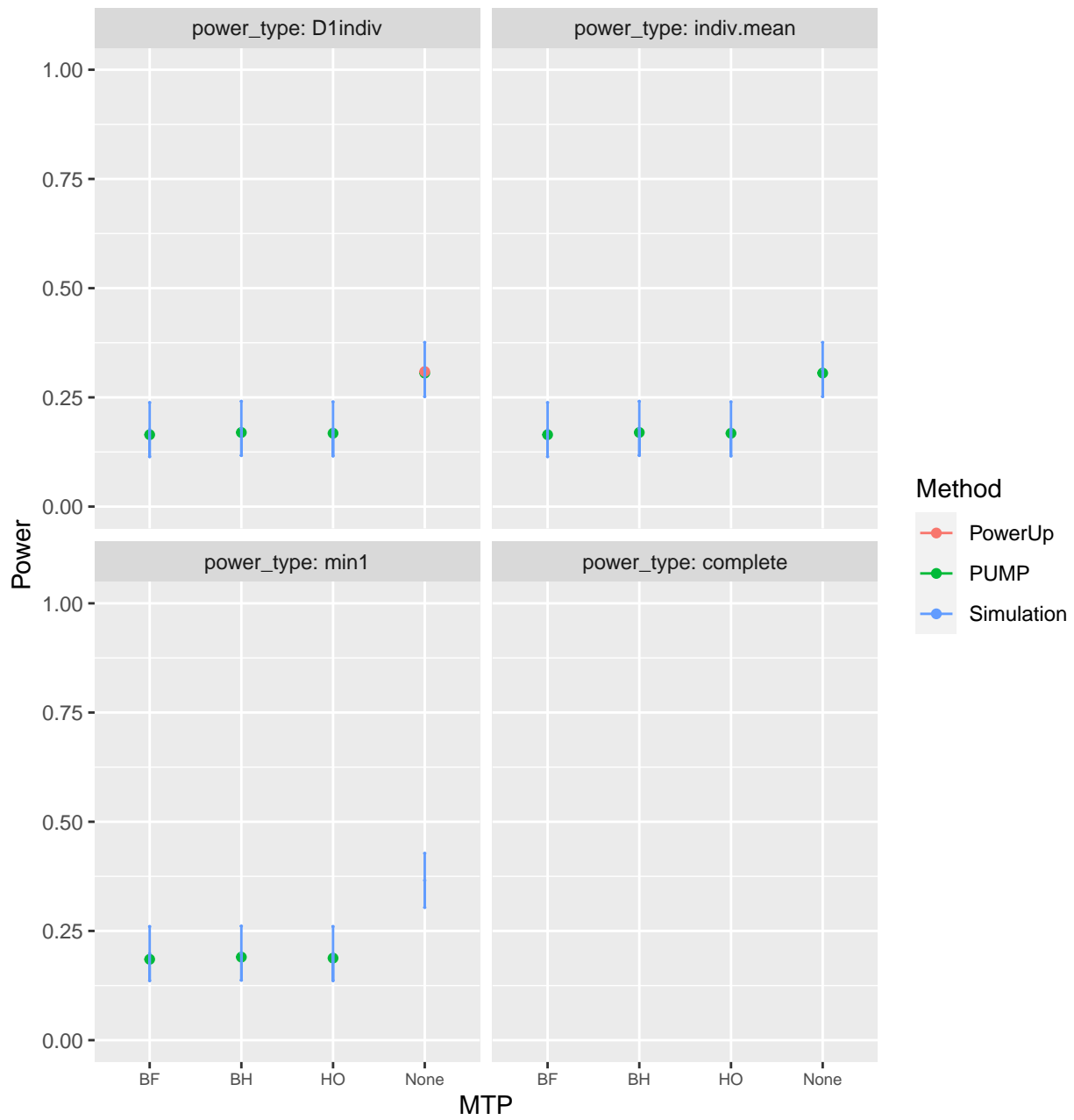
d_m: d2.2_m2rc



Varying true positives

MDES = 0.125, 0, 0

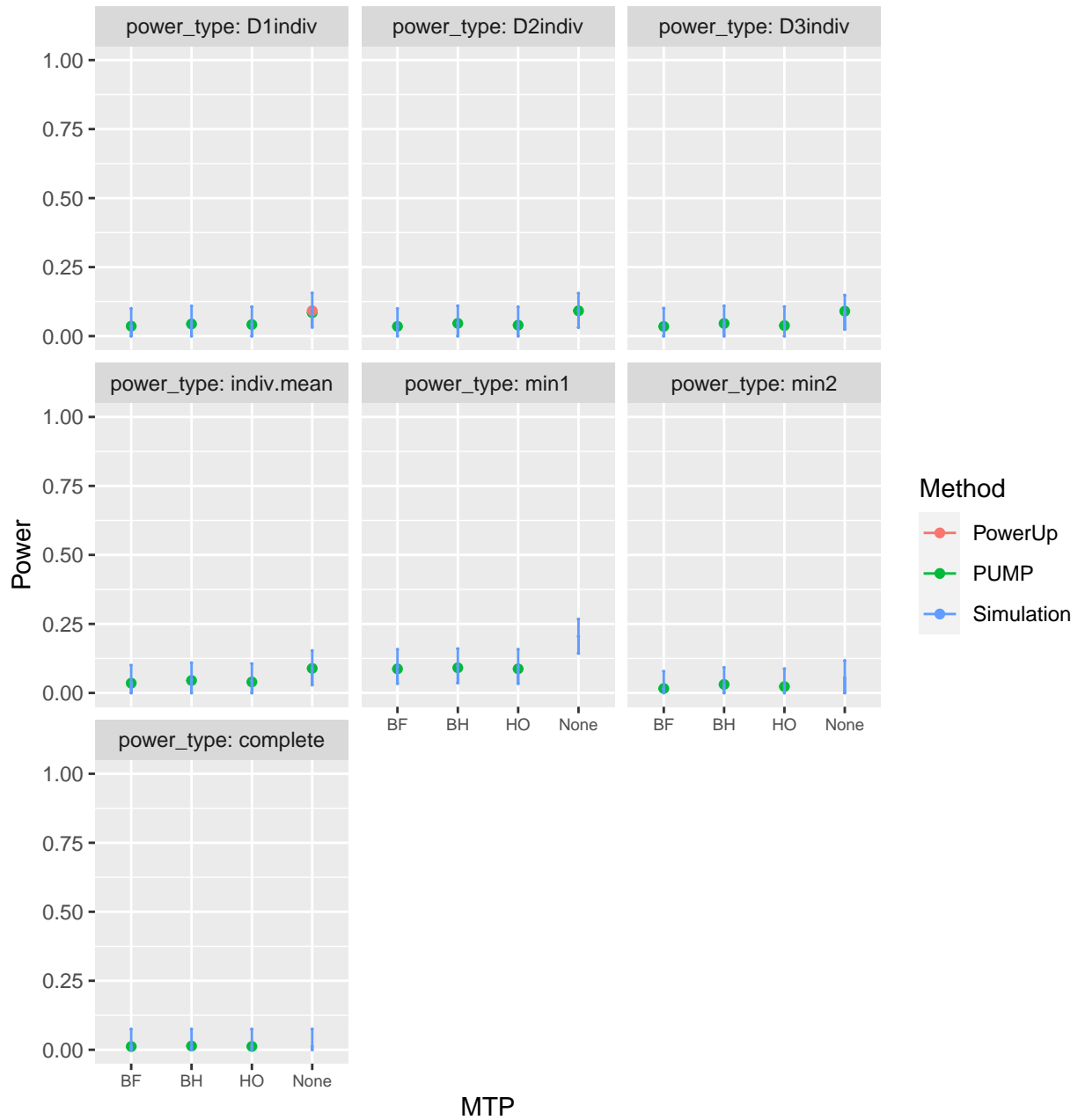
d_m: d2.2_m2rc



Varying ICC

$ICC_2 = 0.7, 0.7, 0.7$

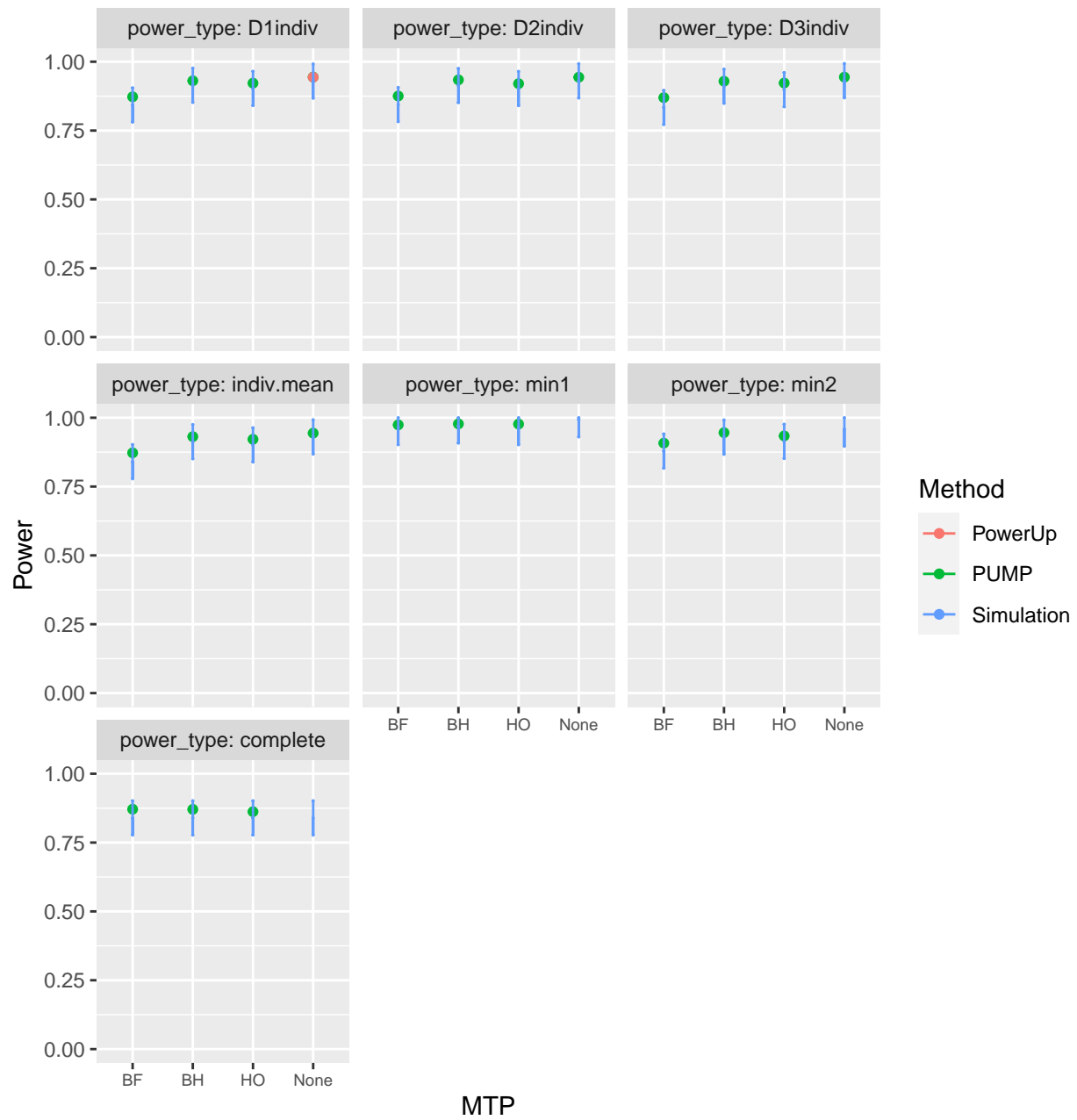
d_m: d2.2_m2rc



MTP

$ICC_2 = 0, 0, 0$

d_m: d2.2_m2rc



MDES validation

Target value: 0.125

```
##
##
## +-----+-----+-----+-----+-----+-----+-----+-----+-----+
## | MTP | Adjusted MDES | D1indiv Power | Target MDES | d_m | S | M | MDES |
## +=====+=====+=====+=====+=====+=====+=====+=====+
## | BF | 0.125 | 0.164 | 0.125 | d2.2_m2rc | 5000 | 3 | 0.125 |
## +-----+-----+-----+-----+-----+-----+-----+-----+
## | BH | 0.125 | 0.209 | 0.125 | d2.2_m2rc | 5000 | 3 | 0.125 |
## +-----+-----+-----+-----+-----+-----+-----+-----+
## | HO | 0.121 | 0.183 | 0.125 | d2.2_m2rc | 5000 | 3 | 0.125 |
## +-----+-----+-----+-----+-----+-----+-----+-----+
##
## Table: d2.2_m2rc (continued below)
##
##
##
## +-----+-----+-----+-----+-----+-----+-----+-----+-----+
## | numZero | J | K | nbar | rho | omega.2 | omega.3 | R2.1 | R2.2 | R2.3 | ICC.2 | ICC.3 |
## +=====+=====+=====+=====+=====+=====+=====+=====+=====+
## | 0 | 60 | 1 | 50 | 0.5 | NA | NA | 0.1 | 0.1 | NA | 0.1 | NA |
## +-----+-----+-----+-----+-----+-----+-----+-----+-----+
## | 0 | 60 | 1 | 50 | 0.5 | NA | NA | 0.1 | 0.1 | NA | 0.1 | NA |
## +-----+-----+-----+-----+-----+-----+-----+-----+-----+
## | 0 | 60 | 1 | 50 | 0.5 | NA | NA | 0.1 | 0.1 | NA | 0.1 | NA |
## +-----+-----+-----+-----+-----+-----+-----+-----+-----+
```

Sample size validation

Target value: 60

```
##
##
## +-----+-----+-----+-----+-----+-----+-----+-----+-----+
## | MTP | Sample.type | Sample.size | D1indiv.power | d_m | S | M | MDES | numZero |
## +=====+=====+=====+=====+=====+=====+=====+=====+=====+
## | BF | J | 60 | 0.164 | d2.2_m2rc | 5000 | 3 | 0.125 | 0 |
## +-----+-----+-----+-----+-----+-----+-----+-----+-----+
## | BH | J | 60 | 0.206 | d2.2_m2rc | 5000 | 3 | 0.125 | 0 |
## +-----+-----+-----+-----+-----+-----+-----+-----+-----+
## | HO | J | 62 | 0.199 | d2.2_m2rc | 5000 | 3 | 0.125 | 0 |
## +-----+-----+-----+-----+-----+-----+-----+-----+-----+
```

```
##
## Table: d2.2_m2rc (continued below)
##
```

```
##
## +-----+-----+-----+-----+-----+-----+-----+-----+-----+
## | J | K | nbar | rho | omega.2 | omega.3 | R2.1 | R2.2 | R2.3 | ICC.2 | ICC.3 |
## +=====+=====+=====+=====+=====+=====+=====+=====+=====+
## | NA | 1 | 50 | 0.5 | NA | NA | 0.1 | 0.1 | NA | 0.1 | NA |
## +-----+-----+-----+-----+-----+-----+-----+-----+-----+
## | NA | 1 | 50 | 0.5 | NA | NA | 0.1 | 0.1 | NA | 0.1 | NA |
## +-----+-----+-----+-----+-----+-----+-----+-----+-----+
## | NA | 1 | 50 | 0.5 | NA | NA | 0.1 | 0.1 | NA | 0.1 | NA |
## +-----+-----+-----+-----+-----+-----+-----+-----+-----+
```

Target value: 50

```
##
##
## +-----+-----+-----+-----+-----+-----+-----+-----+-----+
## | MTP | Sample.type | Sample.size | D1indiv.power | d_m | S | M | MDES | numZero |
## +=====+=====+=====+=====+=====+=====+=====+=====+=====+
## | BF | nbar | 48.18 | 0.164 | d2.2_m2rc | 5000 | 3 | 0.125 | 0 |
## +-----+-----+-----+-----+-----+-----+-----+-----+-----+
## | BH | nbar | 60 | 0.215 | d2.2_m2rc | 5000 | 3 | 0.125 | 0 |
## +-----+-----+-----+-----+-----+-----+-----+-----+-----+
## | HO | nbar | 55 | 0.199 | d2.2_m2rc | 5000 | 3 | 0.125 | 0 |
## +-----+-----+-----+-----+-----+-----+-----+-----+-----+
```

```
##
## Table: d2.2_m2rc (continued below)
##
```

```
##
## +-----+-----+-----+-----+-----+-----+-----+-----+-----+
## | J | K | rho | omega.2 | omega.3 | R2.1 | R2.2 | R2.3 | ICC.2 | ICC.3 |
## +=====+=====+=====+=====+=====+=====+=====+=====+=====+
## | 60 | 1 | 0.5 | NA | NA | 0.1 | 0.1 | NA | 0.1 | NA |
## +-----+-----+-----+-----+-----+-----+-----+-----+-----+
## | 60 | 1 | 0.5 | NA | NA | 0.1 | 0.1 | NA | 0.1 | NA |
## +-----+-----+-----+-----+-----+-----+-----+-----+-----+
```

```
## | 60 | 1 | 0.5 | NA | NA | 0.1 | 0.1 | NA | 0.1 | NA |
## +---+---+---+---+---+---+---+---+---+---+---+---+
```

Note: particularly flat power curves results in discrepancy for `nbar`.

