Theorem The algorithm produces a topological sort of the input DAG. [Just need to show if $(u, v) \in E$], then v.f < u.f]

When (u, v) is explored, u is gray.

v is not gray. If it were, then (u, v) would be back edge and contract with the lemma.