Dataset3-Boston_output_5

November 3, 2021

1 Dataset 1 - Regression

1.1 Experiment Details

The aim of the experiment is to verify if the: 1. ABC_GAN model corrects model misspecification 2. ABC_GAN model performs better and converges faster than a simple C-GAN model

In the experiment we predict the distribution that represents the real data and simulate realistic fake data points using statistical mode, C-GAN and ABC-GAN model with 3 priors. We analyze and compare their performance using metrics like mean squared error, mean absolute error , manhattan distance and euclidean distance between y_{real} and y_{pred}

The models are as follows:

1. The statistical model assumes the distribution $Y = \beta X + \mu$ where $\mu \sim N(0, 1)$
2. The Conditional GAN consists of
    1. Generator with 2 hidden layers with 100 nodes each and ReLu activation.
    2. Discriminator with 2 hidden layers with 25 and 50 nodes and ReLu activation. We use Adam's optimser and BCE Logit Loss to train the model. The input to the Generator of the GAN is (x,e) where x are the features and $e \sim N(0, 1)$. The discriminator output is linear.
3. The ABC GAN Model consists of
    1. ABC generator is defined as follows:
        1. $Y = 1 + \beta_1 x_1 + \beta_2 x_2 + \beta_2 x_3 + ... + \beta_n x_n + N(0, \sigma)$ where $\sigma = 0.1$
        2. $\beta_i \sim N(0, \sigma^*)$ when $\mu = 0$ else $\beta_i \sim N(\beta_i^*, \sigma^*)$ where $\beta_i^* s$ are coefficients obtained from statistical model
        3. σ^* takes the values 0.01,0.1 and 1

    2. C-GAN network is as defined above. However the input to the Generator of the GAN is (x, y_{abc}) where y_{abc} is the output of the ABC Generator.

1.2 Import Libraries

[1]:
```
import warnings
import sys
sys.path.insert(0, '../src')
warnings.filterwarnings('ignore')
```

[2]:
```
import train_test
import ABC_train_test
import bostonDataset
import network
import statsModel
import performanceMetrics
import dataset
import sanityChecks
import torch
import matplotlib.pyplot as plt
import seaborn as sns
from scipy.stats import norm
from torch.utils.data import Dataset,DataLoader
from torch import nn
```

1.3 Parameters

General Parameters

1. Number of Samples
2. Number of features

ABC-Generator parameters are as mentioned below: 1. mean : 1 ($\beta \sim N(\beta^*, \sigma)$ where β^* are coefficients of statistical model) or 1 ($\beta \sim N(0, \sigma)$ 2. std : $\sigma = 1, 0.1, 0.01$ (standard deviation)

[3]:
```
n_features = 13
n_samples= 506

#ABC Generator Parameters
mean = 1
variance = 0.001
```

[4]:
```
# Parameters
mean = 0
variance = 0.01
```

1.4 Dataset

Generate a random regression problem

$Y = 1 + \beta_1 x_1 + \beta_2 x_2 + \beta_2 x_3 + ... + \beta_n x_n + N(0, \sigma)$ where $\sigma = 0.1$

[5]:
```
X,Y = bostonDataset.boston_data()
```

```
        X1    X2    X3   X4     X5     X6    X7      X8   X9     X10   X11  \
0  0.00632  18.0  2.31  0.0  0.538  6.575  65.2  4.0900  1.0  296.0  15.3
1  0.02731   0.0  7.07  0.0  0.469  6.421  78.9  4.9671  2.0  242.0  17.8
2  0.02729   0.0  7.07  0.0  0.469  7.185  61.1  4.9671  2.0  242.0  17.8
3  0.03237   0.0  2.18  0.0  0.458  6.998  45.8  6.0622  3.0  222.0  18.7
4  0.06905   0.0  2.18  0.0  0.458  7.147  54.2  6.0622  3.0  222.0  18.7
```

```
      X12   X13     Y
0  396.90  4.98  24.0
1  396.90  9.14  21.6
2  392.83  4.03  34.7
3  394.63  2.94  33.4
4  396.90  5.33  36.2
```

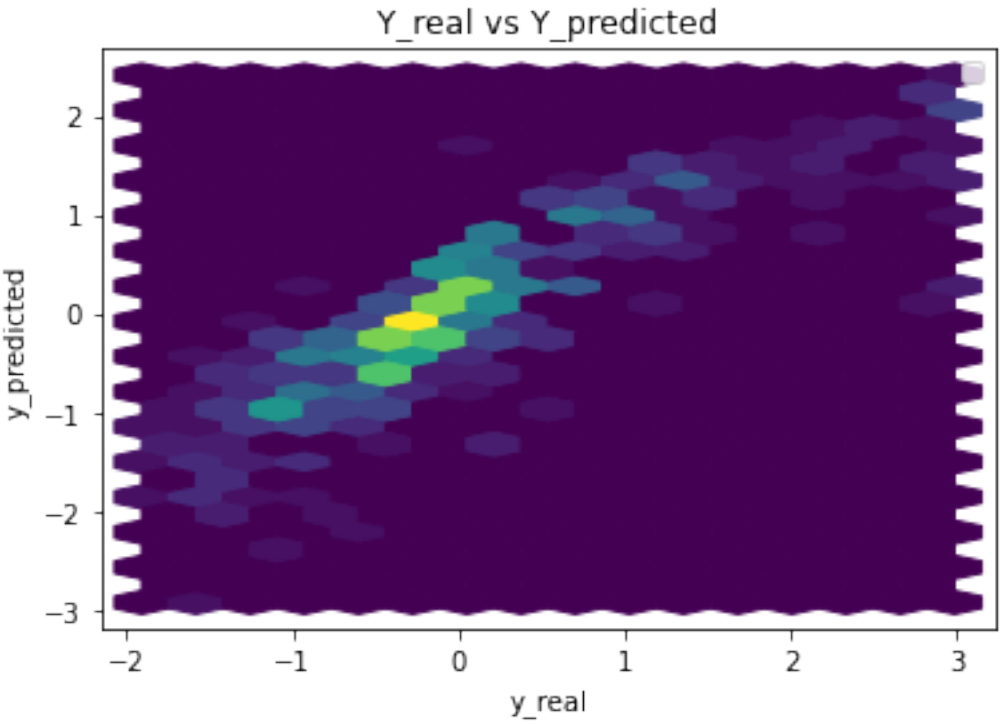
1.5 Stats Model

[6]:
```
[coeff,y_pred] = statsModel.statsModel(X,Y)
```

```
No handles with labels found to put in legend.
```

```
                            OLS Regression Results
==============================================================================
Dep. Variable:                      Y   R-squared:                       0.741
Model:                            OLS   Adj. R-squared:                  0.734
Method:                 Least Squares   F-statistic:                     108.1
Date:                Wed, 03 Nov 2021   Prob (F-statistic):          6.72e-135
Time:                        20:42:48   Log-Likelihood:                -376.55
No. Observations:                 506   AIC:                             781.1
Df Residuals:                     492   BIC:                             840.3
Df Model:                          13
Covariance Type:            nonrobust
==============================================================================
                 coef    std err          t      P>|t|      [0.025      0.975]
------------------------------------------------------------------------------
const      -1.635e-15      0.023  -7.12e-14      1.000      -0.045       0.045
x1            -0.1010      0.031     -3.287      0.001      -0.161      -0.041
x2             0.1177      0.035      3.382      0.001       0.049       0.186
x3             0.0153      0.046      0.334      0.738      -0.075       0.105
x4             0.0742      0.024      3.118      0.002       0.027       0.121
x5            -0.2238      0.048     -4.651      0.000      -0.318      -0.129
x6             0.2911      0.032      9.116      0.000       0.228       0.354
x7             0.0021      0.040      0.052      0.958      -0.077       0.082
x8            -0.3378      0.046     -7.398      0.000      -0.428      -0.248
x9             0.2897      0.063      4.613      0.000       0.166       0.413
x10           -0.2260      0.069     -3.280      0.001      -0.361      -0.091
x11           -0.2243      0.031     -7.283      0.000      -0.285      -0.164
x12            0.0924      0.027      3.467      0.001       0.040       0.145
x13           -0.4074      0.039    -10.347      0.000      -0.485      -0.330
==============================================================================
Omnibus:                      178.041   Durbin-Watson:                   1.078
Prob(Omnibus):                  0.000   Jarque-Bera (JB):              783.126
Skew:                           1.521   Prob(JB):                    8.84e-171
Kurtosis:                       8.281   Cond. No.                         9.82
==============================================================================
```

```
Notes:
[1] Standard Errors assume that the covariance matrix of the errors is correctly
specified.
Parameters:  const   -1.634977e-15
x1       -1.010171e-01
x2        1.177152e-01
x3        1.533520e-02
x4        7.419883e-02
x5       -2.238480e-01
x6        2.910565e-01
x7        2.118638e-03
x8       -3.378363e-01
x9        2.897491e-01
x10      -2.260317e-01
x11      -2.242712e-01
x12       9.243223e-02
x13      -4.074469e-01
dtype: float64
```




```
Performance Metrics
Mean Squared Error: 0.2593573358905904
Mean Absolute Error: 0.3559924576478399
Manhattan distance: 180.1321835698068
Euclidean distance: 11.45577635783096
```

1.6 Common Training Parameters (GAN & ABC_GAN)

[7]:
```
n_epochs = 1000
error = 0.1
batch_size = n_samples
```

1.7 GAN Model

[8]:
```
real_dataset = dataset.CustomDataset(X,Y)
device = torch.device('cuda' if torch.cuda.is_available() else 'cpu')
```

Training GAN for n_epochs number of epochs

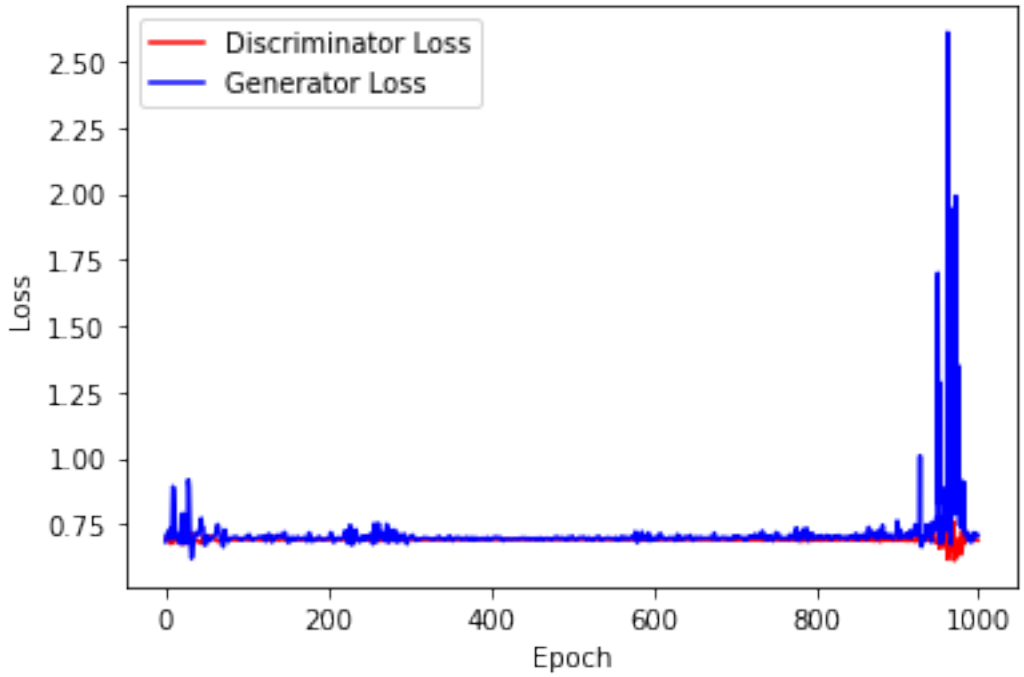
[9]:
```
generator = network.Generator(n_features+2)
discriminator = network.Discriminator(n_features+2)

criterion = torch.nn.BCEWithLogitsLoss()
gen_opt = torch.optim.Adam(generator.parameters(), lr=0.01, betas=(0.5, 0.999))
disc_opt = torch.optim.Adam(discriminator.parameters(), lr=0.01, betas=(0.5, 0.
↪999))
```

[10]:
```
print(generator)
print(discriminator)
```

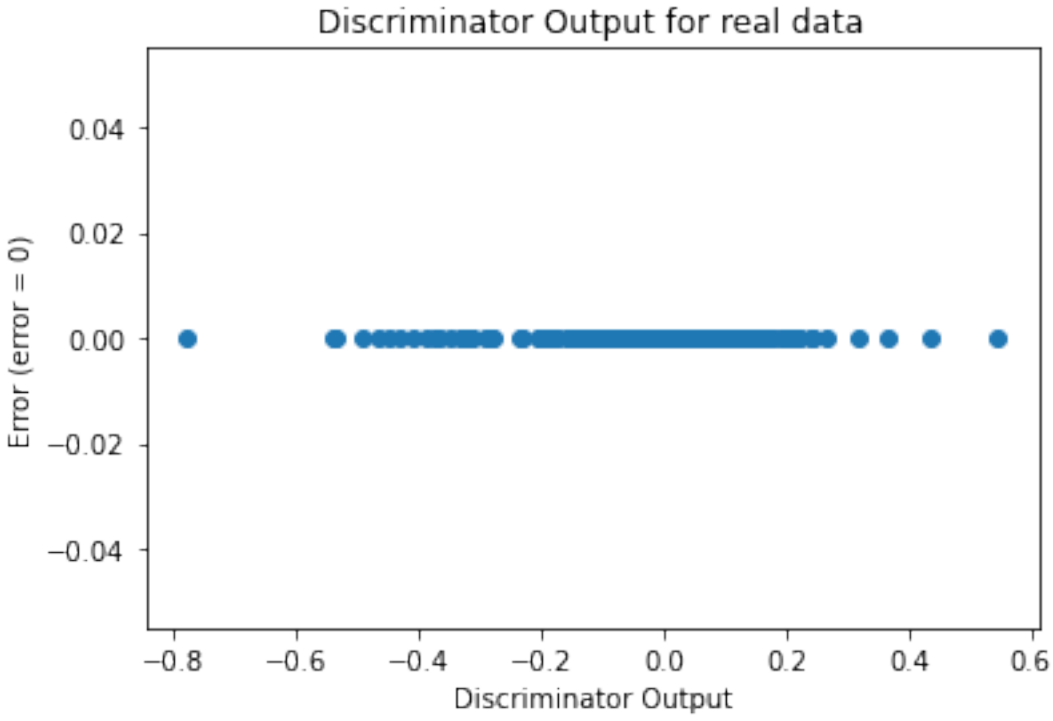
```
Generator(
  (hidden1): Linear(in_features=15, out_features=100, bias=True)
  (hidden2): Linear(in_features=100, out_features=100, bias=True)
  (output): Linear(in_features=100, out_features=1, bias=True)
  (relu): ReLU()
)
Discriminator(
  (hidden1): Linear(in_features=15, out_features=25, bias=True)
  (hidden2): Linear(in_features=25, out_features=50, bias=True)
  (output): Linear(in_features=50, out_features=1, bias=True)
  (relu): ReLU()
)
```

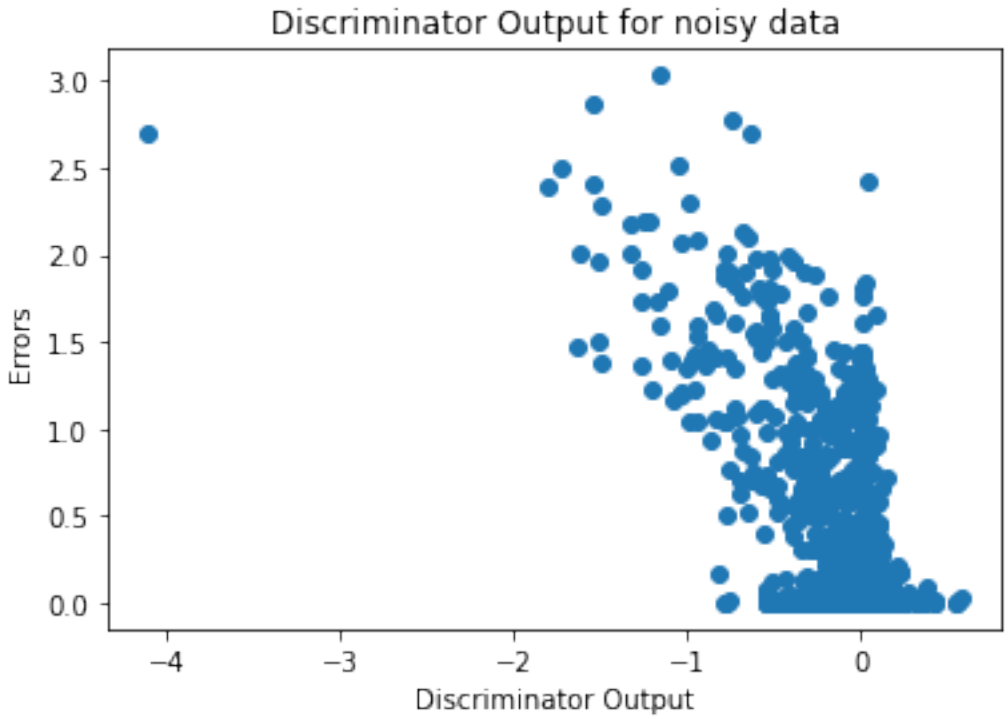
[11]:
```
train_test.
↪training_GAN(discriminator,generator,disc_opt,gen_opt,real_dataset,batch_size,␣
↪n_epochs,criterion,device)
```



[12]:
```
GAN1_metrics = train_test.test_generator(generator,real_dataset,device)
```

[13]:
```
sanityChecks.discProbVsError(real_dataset,discriminator,device)
```



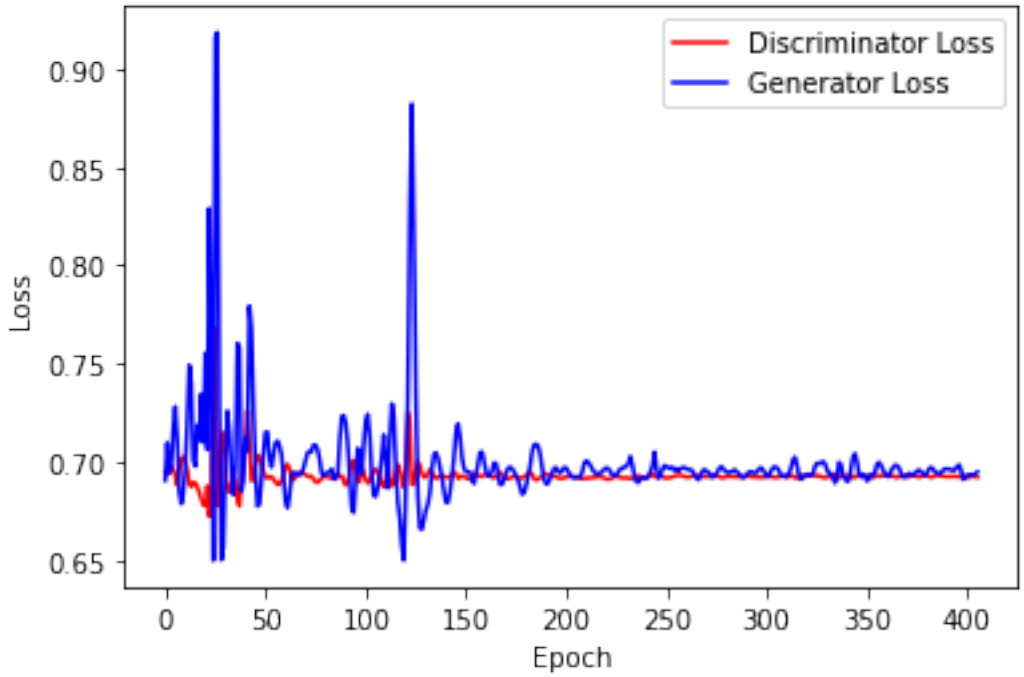


Training GAN until mse of y_pred is $>$ 0.1 or n_epochs $<$ 30000

[14]:
```
generator2 = network.Generator(n_features+2)
discriminator2 = network.Discriminator(n_features+2)
criterion = torch.nn.BCEWithLogitsLoss()
gen_opt = torch.optim.Adam(generator2.parameters(), lr=0.01, betas=(0.5, 0.999))
disc_opt = torch.optim.Adam(discriminator2.parameters(), lr=0.01, betas=(0.5, 0.
↪999))
```

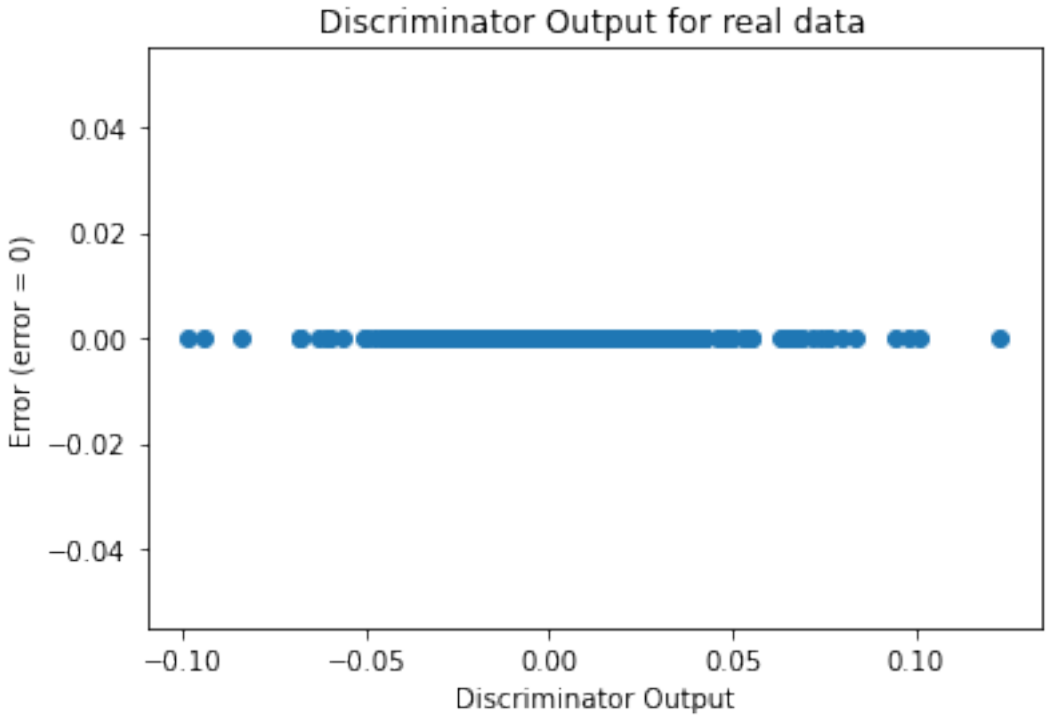
[15]:
```
train_test.
↪training_GAN_2(discriminator2,generator2,disc_opt,gen_opt,real_dataset,batch_size,error,cri
```

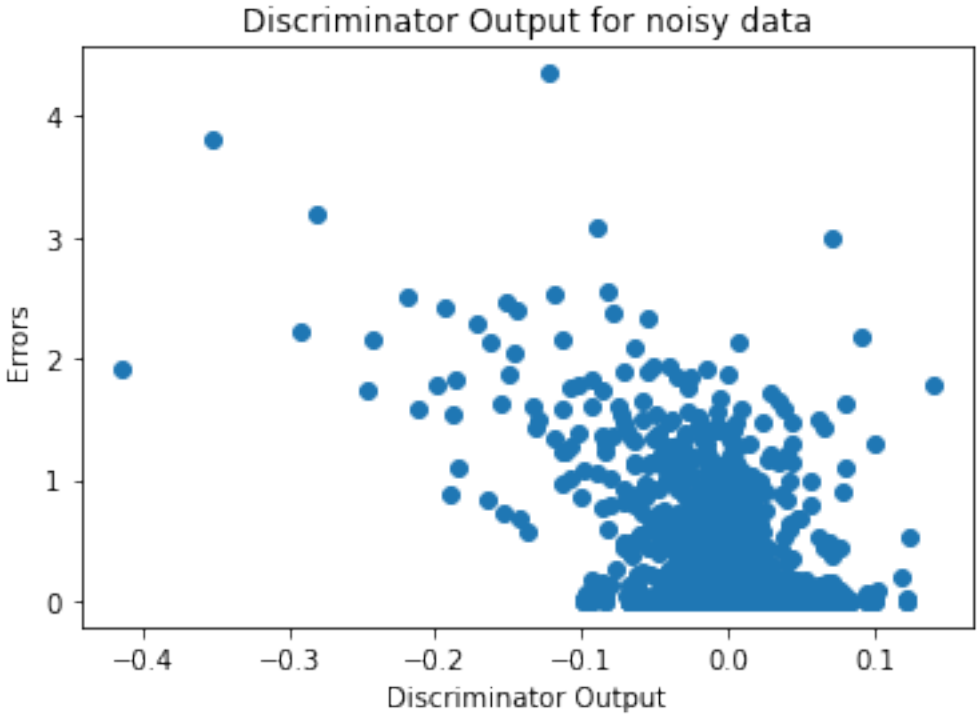
```
Number of epochs needed 406
```



[16]:
```
GAN2_metrics=train_test.test_generator_2(generator2,real_dataset,device)
```

[17]:
```
sanityChecks.discProbVsError(real_dataset,discriminator2,device)
```





2 ABC GAN Model

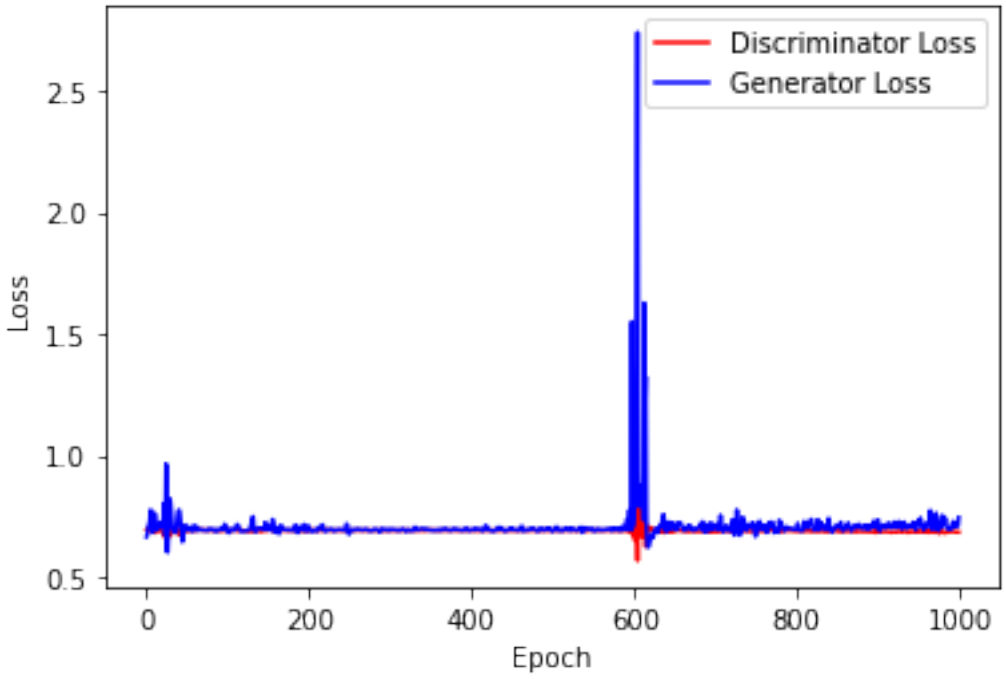
2.0.1 Training the network

Training ABC-GAN for n_epochs number of epochs

[18]:
```
gen = network.Generator(n_features+2)
disc = network.Discriminator(n_features+2)

criterion = torch.nn.BCEWithLogitsLoss()
gen_opt = torch.optim.Adam(gen.parameters(), lr=0.01, betas=(0.5, 0.999))
disc_opt = torch.optim.Adam(disc.parameters(), lr=0.01, betas=(0.5, 0.999))
```

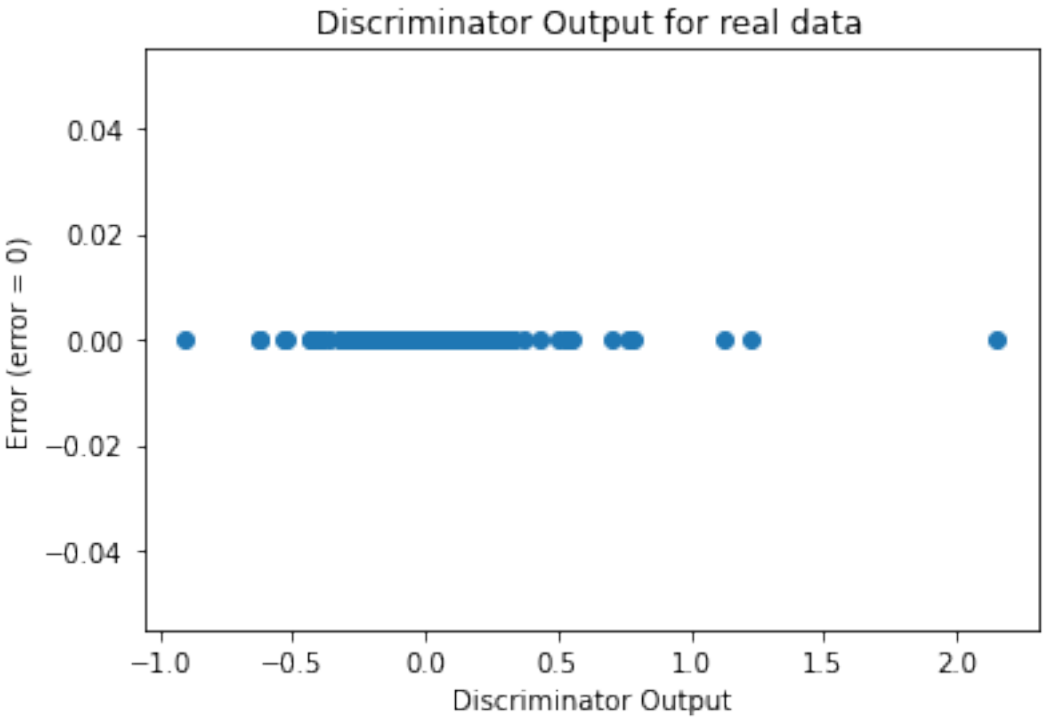
[19]:
```
ABC_train_test.training_GAN(disc, gen,disc_opt,gen_opt,real_dataset,␣
↪batch_size, n_epochs,criterion,coeff,mean,variance,device)
```

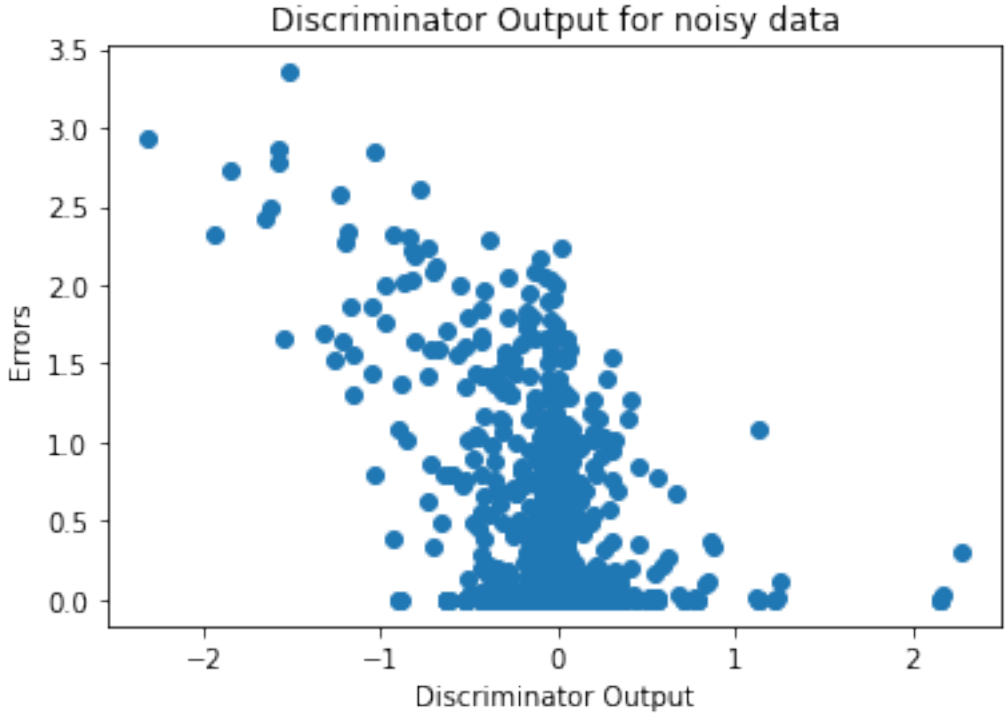


[20]:
```
ABC_GAN1_metrics=ABC_train_test.
↪test_generator(gen,real_dataset,coeff,mean,variance,device)
```

Sanity Checks

[21]:
```
sanityChecks.discProbVsError(real_dataset,disc,device)
```


Discriminator Output for real data
Error (error = 0)
0.04
0.02
0.00
−0.02
−0.04
−1.0
−0.5
0.0
0.5
1.0
1.5
2.0
Discriminator Output


Discriminator Output for noisy data
Errors
3.5
3.0
2.5
2.0
1.5
1.0
0.5
0.0
−2
−1
0
1
2
Discriminator Output

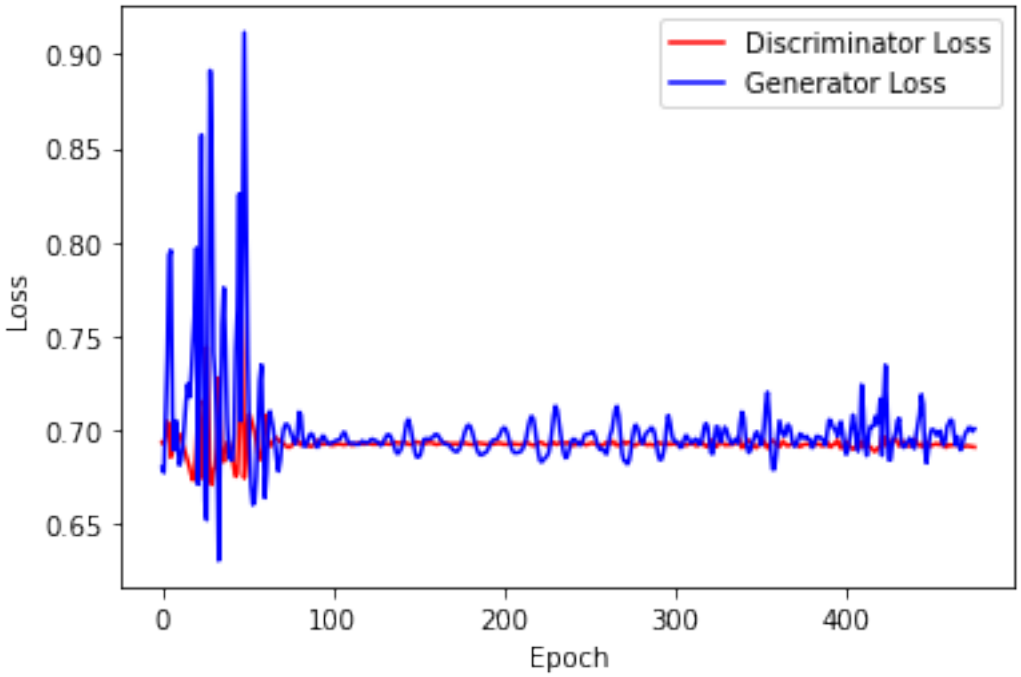
Training GAN until mse of y_pred is > 0.1 or n_epochs < 30000

[22]:
```
gen2 = network.Generator(n_features+2)
disc2 = network.Discriminator(n_features+2)

criterion = torch.nn.BCEWithLogitsLoss()
gen_opt = torch.optim.Adam(gen2.parameters(), lr=0.01, betas=(0.5, 0.999))
disc_opt = torch.optim.Adam(disc2.parameters(), lr=0.01, betas=(0.5, 0.999))
```

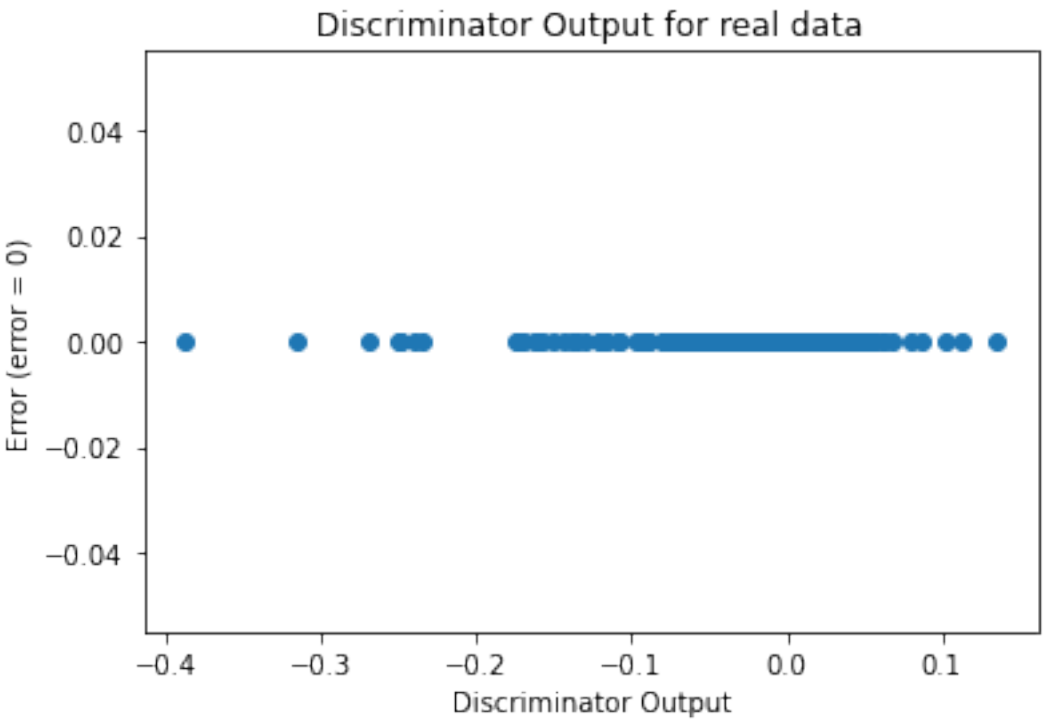
[23]:
```
ABC_train_test.
↪training_GAN_2(disc2,gen2,disc_opt,gen_opt,real_dataset,batch_size,␣
↪error,criterion,coeff,mean,variance,device)
```

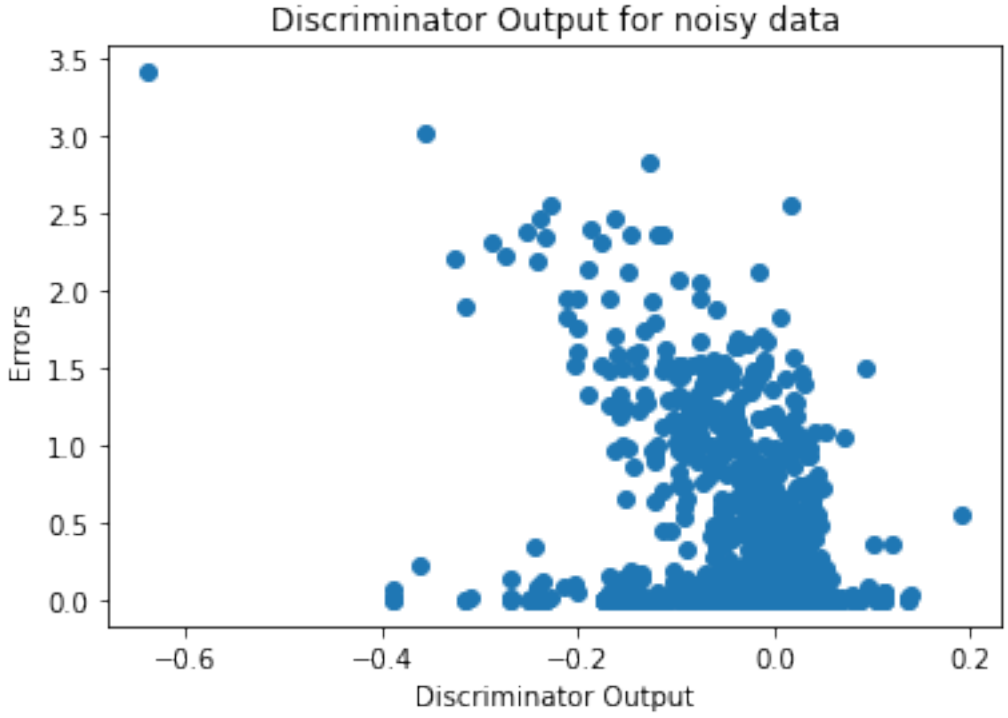
```
Number of epochs 476
```



[24]:
```
ABC_GAN2_metrics=ABC_train_test.
↪test_generator_2(gen2,real_dataset,coeff,mean,variance,device)
```

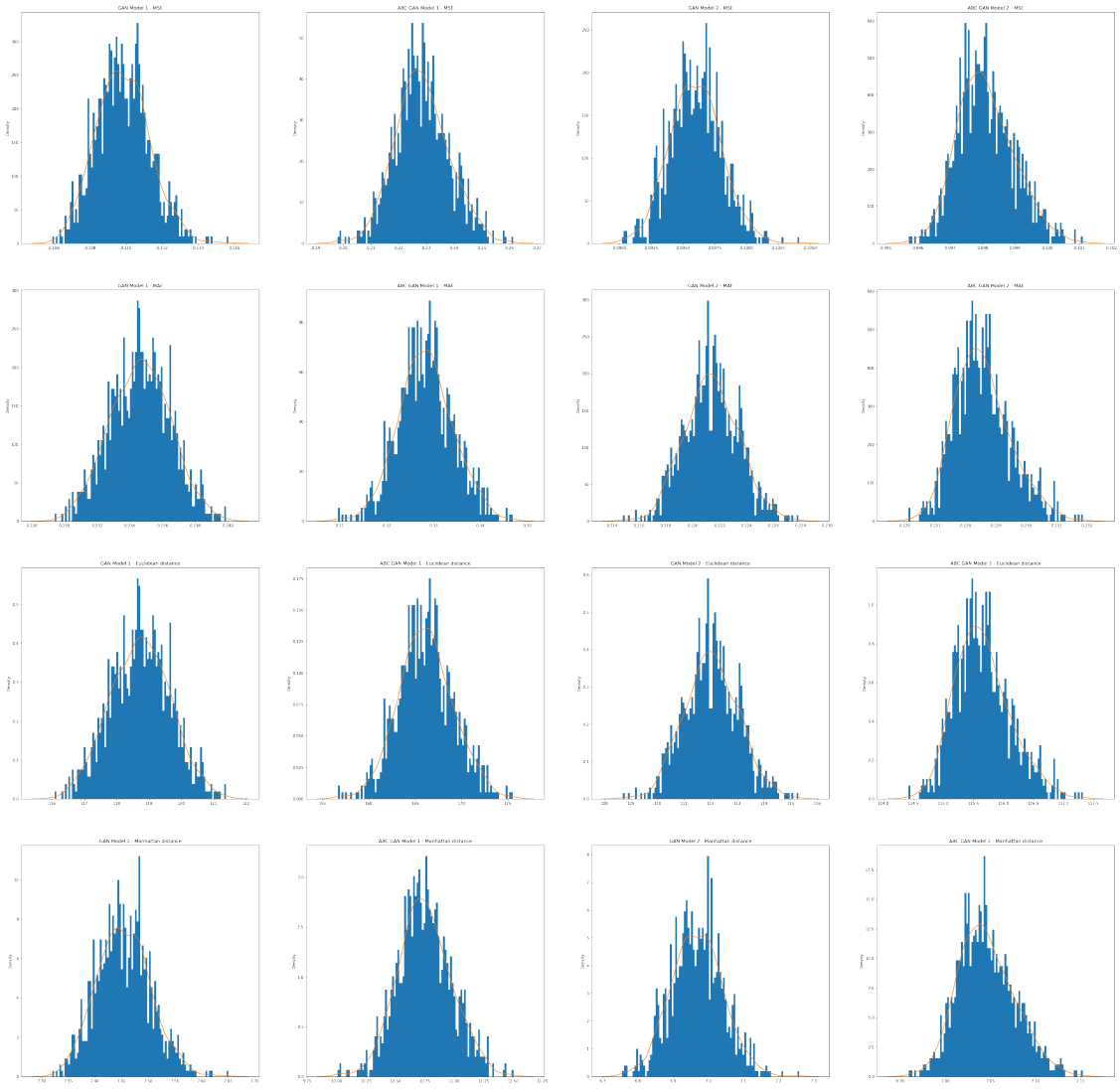
[25]:
```
sanityChecks.discProbVsError(real_dataset,disc2,device)
```


Discriminator Output for real data
Error (error = 0)
0.04
0.02
0.00
−0.02
−0.04
−0.4
−0.3
−0.2
−0.1
0.0
0.1
Discriminator Output


Discriminator Output for noisy data
Errors
3.5
3.0
2.5
2.0
1.5
1.0
0.5
0.0
−0.6
−0.4
−0.2
0.0
0.2
Discriminator Output

3 Model Analysis

[26]:
```
performanceMetrics.
↪modelAnalysis(GAN1_metrics,ABC_GAN1_metrics,GAN2_metrics,ABC_GAN2_metrics)
```



[ ]: