# Friedman3

July 27, 2022

```
[1]: import warnings
warnings.filterwarnings('ignore')

[2]: import scrapbook as sb
import pandas as pd
import numpy as np
import seaborn as sns
import numpy as np
from statistics import mean , median
import matplotlib.pyplot as plt
```

### 1 Baseline

```
books = sb.read_notebooks("./BaseLine_Model_Output")
baseLine_data = []
for nb in books.notebooks:
    nbList=[nb.scraps['Stats Model MAE'].data,nb.scraps['Catboost MAE'].data]
    baseLine_data.append(nbList)
df = pd.DataFrame(baseLine_data, columns = ["Stats Model","Catboost"])
baseline_data = np.array(baseLine_data)
stats = median(baseline_data[:,0])
catboost = median(baseline_data[:,1])
```

### 2 GAN Model

 ${\tt pandas.io.formats.style.Styler}$  at  ${\tt 0x7fd49812e640}$ 

MEDIAN:

MSE 0.363331
MAE 0.447715
Euclidean Distance 2.693012
Manhattan Distance 8.954302

dtype: float64 0.4477151076152455

# 3 ABC\_GAN Analysis

### 3.1 ABC Pre-generator - Catboost

```
[5]: book = sb.read notebooks("./ABC GAN Catboost")
     paramVal = [[1,1],[1,0.1],[1,0.01],[0.1,1],[0.1,0.1],[0.1,0.01],[0.01,1],[0.01,0.01]
      901,0.1],[0.01,0.01]]
     abc_mae = [[] for i in range(9)]
     abc_mae_skip = [[] for i in range(9)]
     abc_mae_mean = [[] for i in range(9)]
     abc_mae_skip_mean = [[] for i in range(9)]
     abc_weights = [[] for i in range(9)]
     prior_model = [[] for i in range(9)]
     abc_pre_generator = [[] for i in range(9)]
     for nb in book.notebooks:
         metrics1 = np.array(nb.scraps['ABC_GAN_1 Metrics'].data)
         metrics3 = np.array(nb.scraps['ABC_GAN_3 Metrics'].data)
         paramVar = float(nb.papermill_dataframe.iloc[0]['value'])
         paramBias = float(nb.papermill_dataframe.iloc[1]['value'])
         #Divide data according to parameters
         for i in range(9):
             if paramVar == paramVal[i][0] and paramBias == paramVal[i][1]:
                 for j in range(100):
                     abc_mae[i].append(metrics1[1,j])
                     abc_mae_skip[i].append(metrics3[1,j])
```

```
abc_weights[i].append(nb.scraps['Skip Connection Weight'].data)
                 prior_model[i].append(nb.scraps['Prior Model MSE'].data)
                 abc_pre_generator[i].append(nb.scraps['ABC Pre-generator MSE'].data)
                 abc_mae_skip_mean[i].append(mean(metrics3[1,:]))
                 abc_mae_mean[i].append(mean(metrics1[1,:]))
[6]: data = [[] for i in range(9)]
     for i in range(9):
        for j in range(len(abc_weights[i])):
             data[i].append([paramVal[i][0], paramVal[i][1],prior_model[i][j],
      -abc_pre_generator[i][j],abc_weights[i][j],abc_mae_mean[i][j],abc_mae_skip_mean[i][j]])
        df = pd.DataFrame(data[i], columns = ['Variance', 'Bias', 'Prior Model MAE',
                                            'ABC pre-generator MAE', 'Skip Node
      ⇒weight','ABC GAN MAE','ABC_GAN MAE (skip connection)'])
        display(df.round(5))
        print(df.median(axis=0))
        print("----")
       Variance Bias Prior Model MAE ABC pre-generator MAE Skip Node weight
    0
              1
                    1
                               0.55349
                                                      1.07389
                                                                        0.88728
              1
                                                                        0.12838
    1
                    1
                               0.49695
                                                      1.47991
    2
              1
                    1
                               0.46301
                                                      1.09640
                                                                        0.11156
    3
                               0.37491
                                                      1.20632
                                                                        0.14740
    4
              1
                               0.25901
                                                                        0.12584
                    1
                                                      1.39730
    5
              1
                    1
                               0.42910
                                                      1.32755
                                                                        0.59361
    6
              1
                               0.25064
                                                                        0.90036
                    1
                                                      1.21604
    7
              1
                    1
                               0.31530
                                                      1.47608
                                                                        0.12112
              1
    8
                    1
                               0.39262
                                                      1.35637
                                                                        0.32640
    9
              1
                                                                        0.21418
                               0.29455
                                                      1.13716
       ABC GAN MAE
                   ABC_GAN MAE (skip connection)
    0
           0.39999
                                          0.35076
    1
           0.49533
                                          0.51881
    2
           0.62987
                                          0.55632
    3
           0.31533
                                          0.33148
    4
           0.27767
                                          0.33092
    5
                                          0.40647
           0.42387
    6
           0.31985
                                          0.27739
    7
           0.35676
                                          0.37147
    8
           0.45790
                                          0.51406
    9
                                          0.33416
           0.37550
    Variance
                                     1.000000
                                     1.000000
    Bias
    Prior Model MAE
                                     0.383768
    ABC pre-generator MAE
                                     1.271793
    Skip Node weight
                                     0.180790
```

ABC GAN MAE 0.387748
ABC\_GAN MAE (skip connection) 0.361115

dtype: float64

-----

|   | Variance  | Bias                                       | Prior Model MAE   | ABC pre-generator MAE  | Skip Node weight | , |
|---|---|--|-------------------|--|------------------|---|
| 0   | 1   | 0.1  | 0.33982           | 0.99085  | 0.73196          |   |
| 1   | 1   | 0.1  | 0.36078           | 0.96710  | 0.42287          |   |
| 2   | 1   | 0.1  | 0.35341           | 1.20779  | 0.08241          |   |
| 3   | 1   | 0.1  | 0.29915           | 1.06911  | 0.08746          |   |
| 4   | 1   | 0.1  | 0.53808           | 1.13153  | 0.15200          |   |
| 5   | 1   | 0.1  | 0.52993           | 1.21257  | 0.52067          |   |
| 6   | 1   | 0.1  | 0.23190           | 0.91021  | 0.72811          |   |
| 7   | 1   | 0.1  | 0.46407           | 0.79147  | 0.06695          |   |
| 8   | 1   | 0.1  | 0.40931           | 0.97473  | 0.08642          |   |
| 9   | 1   | 0.1  | 0.25540           | 0.86825  | 0.07913          |   |
| 0<br>1<br>2<br>3<br>4<br>5<br>6<br>7<br>8 | ABC GAN M 0.353 0.398 0.369 0.306 0.586 0.505 0.232 0.421 0.379 0.250 | 85<br>959<br>900<br>882<br>816<br>82<br>81 | C_GAN MAE (skip o | 0.31337<br>0.37761<br>0.36547<br>0.30456<br>0.53587<br>0.48261<br>0.22546<br>0.47998<br>0.39480<br>0.26485 |                  |   |
| V۶  | Variance  |  |                   | .000000  |                  |   |
|   | Bias  |  |                   | .100000  |                  |   |
|   | Prior Model MAE   |  |                   | .357096  |                  |   |
| ΑE  | ABC pre-generator MAE   |  |                   | .982791  |                  |   |
|   | Skip Node weight  |  |                   | . 119727   |                  |   |
|   | ABC GAN MAE   |  |                   | . 374218   |                  |   |
| ABC_GAN MAE (skip connection)             |   |  |                   |  |                  |   |
| dtype: float64                            |   |  |                   |  |                  |   |
|   |   |  |                   |  |                  |   |
|   |   |  |                   |  |                  |   |

\

Variance Bias Prior Model MAE ABC pre-generator MAE Skip Node weight \ 0 1 0.01 0.19182 0.08454 0.94674 1 0.01 1 0.33837 1.08540 0.07246 1 0.01 2 0.06696 0.61920 1.28079 1 0.01 3 0.42694 1.13053 0.09642 4 1 0.01 0.35704 1.01274 0.76609 5 1 0.01 0.39605 1.17703 0.07694 6 1 0.01 0.23136 0.89273 0.36493 7 1 0.01 0.39765 0.07427 1.11745 8 1 0.01 0.60597 1.29207 0.06909

| 9   | 1 0.01   | 0.41245  | 1.05936   | 0.08070  |  |  |
|---|--|--|---|--|--|--|
| ABC<br>0<br>1<br>2<br>3<br>4<br>5<br>6<br>7<br>8<br>9 | C GAN MAE ABC_GA<br>0.18860<br>0.35540<br>0.60762<br>0.43520<br>0.35261<br>0.38179<br>0.29091<br>0.34863<br>0.59141<br>0.43538   | 0<br>0<br>0<br>0<br>0<br>0   | ction) .21433 .36636 .60012 .42548 .36901 .41878 .24130 .40664 .65434 .41649  |  |  |  |
| Bias<br>Prior<br>ABC pr<br>Skip I<br>ABC GA           | Variance       1.000000         Bias       0.010000         Prior Model MAE       0.396854         ABC pre-generator MAE       1.101427         Skip Node weight       0.078823         ABC GAN MAE       0.368590         ABC_GAN MAE (skip connection)       0.411566         dtype: float64 |  |   |  |  |  |
| Van<br>0<br>1<br>2<br>3<br>4<br>5<br>6<br>7<br>8      | 0.1 1 0.1 1 0.1 1 0.1 1 0.1 1 0.1 1 0.1 1 0.1 1 0.1 1 0.1 1 0.1 1 0.1 1 0.1 1 0.1 1  | 0.44355<br>0.33733<br>0.53141<br>0.52344<br>0.35908<br>0.24180<br>0.34376<br>0.69918<br>0.30807<br>0.45076 | pre-generator MAE<br>0.93825<br>0.97410<br>0.90917<br>0.95988<br>0.99645<br>0.60585<br>0.83138<br>1.08749<br>0.68183<br>0.88202 | Skip Node weight 0.19504 0.94731 0.18535 0.19841 0.36981 0.45198 0.27098 0.80777 0.19440 0.92793 |  |  |
| ABO<br>0<br>1<br>2<br>3<br>4<br>5<br>6<br>7<br>8      | C GAN MAE ABC_GA<br>0.52095<br>0.34799<br>0.39227<br>0.54389<br>0.44419<br>0.28643<br>0.29525<br>0.64926<br>0.46274<br>0.39831   | 0<br>0<br>0<br>0<br>0<br>0   | ction) .54467 .47004 .45380 .52574 .46829 .30646 .27337 .72885 .45162 .40029  |  |  |  |

Variance

```
Bias
                            1.000000
Prior Model MAE
                           0.401313
ABC pre-generator MAE
                           0.923711
Skip Node weight
                           0.320396
ABC GAN MAE
                           0.421251
ABC_GAN MAE (skip connection) 0.461044
dtype: float64
_____
  Variance Bias Prior Model MAE ABC pre-generator MAE Skip Node weight \
0
      0.1 0.1
                      0.48521
                                          0.49516
                                                        0.42236
      0.1 0.1
1
                      0.42198
                                          0.44762
                                                         0.17766
2
      0.1 0.1
                      0.37103
                                          0.40611
                                                         0.11748
3
      0.1 0.1
                      0.28395
                                          0.34739
                                                         0.46384
4
      0.1 0.1
                     0.31840
                                          0.31547
                                                         0.15693
5
      0.1 0.1
                                         0.25924
                     0.25629
                                                         0.11373
      0.1 0.1
6
                     0.31856
                                         0.32447
                                                         0.12191
7
      0.1 0.1
                     0.43340
                                        0.51264
                                                        0.07154
      0.1 0.1
8
                     0.18438
                                         0.18535
                                                         0.10086
9
      0.1 0.1
               0.44524
                                        0.46988
                                                         0.14702
  ABC GAN MAE ABC_GAN MAE (skip connection)
0
     0.47018
                                0.49758
1
     0.42187
                                0.43543
2
     0.39183
                                0.35301
3
     0.33538
                                0.30777
4
     0.35089
                                0.31495
5
     0.26756
                                0.26324
6
     0.30586
                                0.28880
7
                                0.46338
     0.43847
8
     0.19990
                                0.20868
9
     0.51996
                                0.50652
                           0.100000
Variance
Bias
                           0.100000
Prior Model MAE
                           0.344796
ABC pre-generator MAE
                           0.376749
Skip Node weight
                           0.134466
ABC GAN MAE
                           0.371360
ABC_GAN MAE (skip connection) 0.333982
dtype: float64
_____
  Variance Bias Prior Model MAE ABC pre-generator MAE Skip Node weight \
0
      0.1 0.01
                      0.48635
                                          0.46747
                                                         0.06486
                    0.72721
0.38121
      0.1 0.01
1
                                          0.73822
                                                         0.07148
2
      0.1 0.01
                                        0.36242
                                                         0.06480
      0.1 0.01
3
                     0.39256
```

0.1 0.01

0.40627

0.27401

0.06387

```
0.1 0.01
5
                          0.45537
                                                0.47982
                                                                 0.12060
6
       0.1 0.01
                          0.20045
                                                0.18354
                                                                 0.06223
7
       0.1 0.01
                          0.46530
                                                0.45927
                                                                 0.15143
8
       0.1 0.01
                          0.51858
                                                0.52908
                                                                 0.35577
9
       0.1 0.01
                          0.55905
                                                0.57888
                                                                 0.59082
  ABC GAN MAE ABC_GAN MAE (skip connection)
0
      0.49798
                                    0.48154
1
      0.68951
                                    0.72545
2
      0.40144
                                    0.38736
3
      0.40063
                                    0.38924
4
      0.28314
                                    0.25411
5
      0.44765
                                    0.44046
6
      0.20828
                                    0.20713
7
      0.47832
                                    0.46716
8
      0.53154
                                    0.50484
9
      0.56353
                                    0.55172
Variance
                               0.100000
Bias
                               0.010000
Prior Model MAE
                               0.460338
ABC pre-generator MAE
                              0.463369
Skip Node weight
                              0.068173
ABC GAN MAE
                               0.462983
ABC_GAN MAE (skip connection) 0.453812
dtype: float64
  Variance Bias Prior Model MAE ABC pre-generator MAE Skip Node weight \
0
      0.01
             1
                          0.49074
                                                0.98341
                                                                 0.14829
1
      0.01
              1
                          0.30582
                                                1.07661
                                                                 0.13859
2
      0.01
              1
                          0.40760
                                                1.12822
                                                                 0.98394
3
      0.01
             1
                          0.41272
                                                0.85661
                                                                 0.20137
4
      0.01
             1
                         0.33472
                                                0.97188
                                                                 0.88398
5
      0.01
              1
                        0.42780
                                                                 0.90054
                                                1.16855
6
      0.01
              1
                        0.36342
                                               1.14467
                                                                 0.79338
7
      0.01
              1
                          0.49722
                                                0.65774
                                                                 0.15495
8
      0.01
               1
                          0.38186
                                               1.06331
                                                                 0.14788
9
      0.01
                          0.28260
                                                0.77761
                                                                 0.77086
  ABC GAN MAE ABC_GAN MAE (skip connection)
0
      0.57054
                                    0.58423
1
      0.35546
                                    0.45770
2
      0.57490
                                    0.49541
3
      0.52824
                                    0.48841
4
      0.42478
                                    0.39342
5
      0.48665
                                    0.52362
6
      0.40927
                                    0.41868
7
      0.45248
                                    0.38027
```

```
8
      0.40990
                                   0.40441
9
                                   0.39131
      0.35585
Variance
                               0.010000
Bias
                               1.000000
Prior Model MAE
                               0.394727
ABC pre-generator MAE
                              1.023361
Skip Node weight
                               0.486114
ABC GAN MAE
                               0.438633
ABC_GAN MAE (skip connection) 0.438191
dtype: float64
______
  Variance Bias Prior Model MAE ABC pre-generator MAE Skip Node weight \
0
      0.01 0.1
                         0.38063
                                               0.37627
                                                                0.56189
      0.01 0.1
1
                         0.29615
                                               0.28527
                                                                0.15988
2
      0.01 0.1
                                                                0.23061
                         0.51166
                                               0.51358
3
      0.01 0.1
                         0.39900
                                               0.37510
                                                                0.20257
4
      0.01 0.1
                                               0.40724
                         0.39202
                                                                0.16257
5
    0.01 0.1
                         0.43905
                                              0.46808
                                                               0.75343
6
      0.01 0.1
                         0.41002
                                              0.40900
                                                               0.26527
7
      0.01 0.1
                         0.34874
                                              0.36578
                                                               0.00000
8
      0.01 0.1
                        0.41720
                                              0.44560
                                                               0.49396
9
      0.01 0.1
                       0.51847
                                              0.55573
                                                               0.29779
  ABC GAN MAE ABC_GAN MAE (skip connection)
0
      0.37685
                                   0.38667
1
      0.30385
                                   0.31401
2
      0.47840
                                   0.52289
3
      0.45131
                                   0.46101
4
      0.40694
                                   0.40043
5
      0.42816
                                   0.41135
6
      0.43447
                                   0.45689
7
      0.35072
                                   0.35708
8
      0.43446
                                   0.39402
      0.54807
                                   0.55994
Variance
                               0.010000
Bias
                               0.100000
Prior Model MAE
                               0.404513
ABC pre-generator MAE
                               0.408118
Skip Node weight
                               0.247944
                               0.431306
ABC GAN MAE
ABC_GAN MAE (skip connection)
                               0.405891
dtype: float64
  Variance Bias Prior Model MAE ABC pre-generator MAE Skip Node weight \
0
      0.01 0.01
                       0.33028
                                              0.33461
                                                               0.03296
```

0.04498

0.31899

1

0.01 0.01

```
2
           0.01 0.01
                                0.32634
                                                       0.32176
                                                                          0.09027
    3
           0.01 0.01
                                0.52266
                                                       0.51851
                                                                          0.05373
    4
           0.01 0.01
                                0.41068
                                                       0.41065
                                                                          0.00000
    5
           0.01 0.01
                                                       0.35787
                                                                          0.02500
                                0.36300
    6
           0.01 0.01
                                0.31797
                                                       0.31724
                                                                          0.00000
    7
           0.01 0.01
                                                       0.63322
                                0.63367
                                                                          0.11209
    8
           0.01 0.01
                                0.43524
                                                       0.43527
                                                                          0.06754
    9
           0.01 0.01
                                0.51606
                                                       0.51143
                                                                          0.06383
       ABC GAN MAE ABC_GAN MAE (skip connection)
    0
           0.30637
                                           0.32798
           0.33665
    1
                                           0.31979
    2
           0.34715
                                           0.33142
    3
           0.51330
                                           0.53628
    4
           0.43096
                                           0.41030
    5
           0.34682
                                           0.36348
    6
           0.31611
                                           0.31655
    7
           0.63902
                                           0.63554
    8
           0.45189
                                           0.43657
           0.54559
                                           0.54408
    Variance
                                      0.010000
    Bias
                                      0.010000
    Prior Model MAE
                                      0.386840
    ABC pre-generator MAE
                                      0.384259
    Skip Node weight
                                      0.049354
    ABC GAN MAE
                                      0.389054
    ABC_GAN MAE (skip connection)
                                      0.386888
    dtype: float64
[7]: # Display Catboost Summary Tables
     data = np.array(data)
     catboostData = []
     for i in range(9):
         catboostData.append([paramVal[i][0], __
      aparamVal[i][1], catboost, median(data[i][:,3]), median(data[i][:
      →,5]),median(data[i][:,6]),median(data[i][:,4])])
     df = pd.DataFrame(catboostData, columns = ['Variance', 'Bias', 'Catboost', 'Prior_
      →Model MAE', 'mGAN', 'skipGAN', 'Skip Node weight'])
     display(df.round(5))
                                                      mGAN skipGAN \
       Variance Bias Catboost Prior Model MAE
    0
           1.00 1.00
                        0.35587
                                          1.27179 0.38775 0.36111
    1
           1.00
                 0.10
                        0.35587
                                          0.98279 0.37422 0.37154
    2
           1.00
                 0.01
                        0.35587
                                          1.10143 0.36859 0.41157
           0.10 1.00
    3
                                          0.92371 0.42125 0.46104
                        0.35587
           0.10 0.10
                        0.35587
                                          0.37675 0.37136 0.33398
```

```
5
       0.10 0.01
                    0.35587
                                      0.46337 0.46298 0.45381
6
       0.01 1.00
                    0.35587
                                      1.02336 0.43863 0.43819
7
       0.01 0.10
                    0.35587
                                      0.40812 0.43131 0.40589
8
       0.01 0.01
                    0.35587
                                      0.38426 0.38905 0.38689
  Skip Node weight
            0.18079
0
            0.11973
1
2
            0.07882
3
            0.32040
4
            0.13447
5
            0.06817
6
            0.48611
7
            0.24794
8
            0.04935
```

# 3.2 ABC Pre-generator - Stats

```
[8]: book = sb.read notebooks("./ABC GAN Stats")
     paramVal = [[1,1],[0.1,1],[0.01,1],[1,0.1],[0.1,0.1],[0.01,0.1],[1,0.01],[0.1,0.1]
      \hookrightarrow 01],[0.01,0.01]]
     abc_mae = [[] for i in range(9)]
     abc mae skip = [[] for i in range(9)]
     abc_mae_mean = [[] for i in range(9)]
     abc mae skip mean = [[] for i in range(9)]
     abc_weights = [[] for i in range(9)]
     prior_model = [[] for i in range(9)]
     abc_pre_generator = [[] for i in range(9)]
     for nb in book.notebooks:
         metrics1 = np.array(nb.scraps['ABC GAN 1 Metrics'].data)
         metrics3 = np.array(nb.scraps['ABC_GAN_3 Metrics'].data)
         paramVar = float(nb.papermill_dataframe.iloc[0]['value'])
         paramBias = float(nb.papermill_dataframe.iloc[1]['value'])
         #Divide data according to parameters
         for i in range(9):
             if paramVar == paramVal[i][0] and paramBias == paramVal[i][1]:
                 for j in range(100):
                     abc mae[i].append(metrics1[1,j])
                     abc mae skip[i].append(metrics3[1,j])
                 abc_weights[i].append(nb.scraps['Skip Connection Weight'].data)
                 prior_model[i].append(nb.scraps['Prior Model MSE'].data)
                 abc_pre_generator[i].append(nb.scraps['ABC Pre-generator MSE'].data)
                 abc mae skip mean[i].append(mean(metrics3[1,:]))
                 abc_mae_mean[i].append(mean(metrics1[1,:]))
```

```
[9]: data = [[] for i in range(9)]
    for i in range(9):
        for j in range(len(abc_weights[i])):
            data[i].append([paramVal[i][0], paramVal[i][1],prior_model[i][j],
      abc_pre_generator[i][j],abc_weights[i][j],abc_mae_mean[i][j],abc_mae_skip_mean[i][j]])
        df = pd.DataFrame(data[i], columns = ['Variance', 'Bias', 'Prior Model MAE',
                                           'ABC pre-generator MAE', 'Skip Node
      ⇔weight','ABC GAN MAE','ABC_GAN MAE (skip connection)'])
        display(df.round(5))
        print(df.median(axis=0))
        print("----")
       Variance Bias Prior Model MAE ABC pre-generator MAE Skip Node weight
    0
                                                                       0.98985
                   1
                              0.45321
                                                     1.37373
    1
              1
                   1
                              0.46372
                                                     1.50672
                                                                       0.97564
    2
              1
                   1
                              0.58514
                                                     1.16563
                                                                       0.99841
    3
                   1
                              0.52032
                                                     1.42406
                                                                      1.00000
    4
              1
                  1
                              0.66686
                                                     1.11099
                                                                      0.99498
    5
              1
                  1
                              0.59179
                                                     1.56344
                                                                      0.99157
    6
              1
                  1
                              0.49935
                                                     1.69111
                                                                      1.00000
    7
              1
                  1
                              0.44243
                                                     1.40947
                                                                      0.98950
    8
              1
                   1
                              0.49656
                                                     1.25013
                                                                       1.00000
    9
                              0.55986
                                                                       0.99020
              1
                   1
                                                     1.11980
       ABC GAN MAE ABC_GAN MAE (skip connection)
    0
           0.46898
                                         0.40212
           0.40372
    1
                                         0.29641
    2
           0.44245
                                         0.42443
    3
          0.68059
                                         0.77544
    4
           0.51811
                                         0.51083
    5
           0.97788
                                         0.71474
    6
           0.46297
                                         0.32696
    7
                                         0.28979
           0.34726
    8
           0.61839
                                         0.49452
    9
           0.51472
                                         0.60578
    Variance
                                    1.000000
    Bias
                                    1.000000
    Prior Model MAE
                                    0.509832
    ABC pre-generator MAE
                                    1.391597
    Skip Node weight
                                    0.993273
    ABC GAN MAE
                                    0.491848
    ABC_GAN MAE (skip connection)
                                    0.459476
    dtype: float64
```

```
Variance Bias Prior Model MAE ABC pre-generator MAE Skip Node weight
0
       0.1
                          0.56628
                                                                   0.98871
               1
                                                 1.09693
       0.1
1
               1
                          0.64543
                                                 1.14204
                                                                   0.99631
2
       0.1
                          0.46983
                                                                   1.00000
               1
                                                 0.87978
3
       0.1
               1
                          0.43445
                                                 0.87695
                                                                   0.99956
4
       0.1
                          0.66464
                                                 1.07654
                                                                   0.99542
5
       0.1
                          0.47202
                                                 0.91590
                                                                   0.99953
       0.1
6
               1
                          0.43826
                                                 1.11128
                                                                   0.99706
7
       0.1
                          0.38618
               1
                                                 0.73310
                                                                   0.99848
       0.1
8
               1
                          0.58504
                                                 0.92217
                                                                   0.99854
9
       0.1
                          0.49714
               1
                                                 0.93450
                                                                   1.00000
  ABC GAN MAE ABC_GAN MAE (skip connection)
0
                                     0.46986
       0.53355
1
       0.64390
                                     0.86049
2
       0.47337
                                     0.36084
3
       0.43586
                                     0.36840
4
      0.36400
                                     0.42828
5
      0.39912
                                     0.46462
6
      0.33126
                                     0.36497
7
      0.42586
                                     0.34843
8
      0.53167
                                     0.69129
9
      0.48852
                                     0.44818
                                0.100000
Variance
Bias
                                1.000000
Prior Model MAE
                                0.484579
ABC pre-generator MAE
                                0.928335
Skip Node weight
                                0.998511
ABC GAN MAE
                                0.454615
ABC_GAN MAE (skip connection) 0.438231
dtype: float64
_____
  Variance Bias Prior Model MAE ABC pre-generator MAE Skip Node weight \
0
                                                                   0.99728
      0.01
               1
                          0.52735
                                                 0.88408
1
      0.01
               1
                          0.49734
                                                 0.82135
                                                                   0.99989
2
      0.01
                          0.71581
                                                 0.84162
                                                                   0.99677
3
      0.01
                          0.60416
                                                 1.24250
                                                                   0.99780
               1
4
      0.01
               1
                          0.35647
                                                 0.87529
                                                                   1.00000
5
      0.01
              1
                          0.53557
                                                 0.83153
                                                                   1.00000
6
      0.01
                          0.42949
                                                 0.75890
                                                                   0.99731
               1
7
      0.01
               1
                          0.66363
                                                 0.88791
                                                                   0.97753
8
       0.01
               1
                          0.48557
                                                 1.00044
                                                                   0.97891
9
       0.01
                          0.51627
                                                 0.94253
                                                                   1.00000
   ABC GAN MAE ABC_GAN MAE (skip connection)
0
       0.53225
                                     0.53593
```

1

```
2
      0.68773
                                    0.68961
3
                                    0.61441
      0.58669
4
      0.47759
                                    0.39850
5
      0.37981
                                    0.36269
6
      0.35582
                                    0.39652
7
      0.52959
                                    0.63537
8
      0.70407
                                    0.58905
9
      0.64813
                                    0.54281
Variance
                                0.010000
Bias
                                1.000000
Prior Model MAE
                               0.521810
ABC pre-generator MAE
                               0.879687
Skip Node weight
                               0.997553
ABC GAN MAE
                               0.530920
ABC_GAN MAE (skip connection) 0.545463
dtype: float64
_____
  Variance Bias Prior Model MAE ABC pre-generator MAE Skip Node weight \
0
         1 0.1
                          0.49666
                                                0.97503
                                                                  0.65040
            0.1
                                                                  0.49673
1
         1
                          0.34444
                                                1.15102
2
         1
            0.1
                          0.52253
                                                1.09027
                                                                  0.55306
3
            0.1
                          0.65495
                                                1.17778
                                                                  0.63340
4
         1
            0.1
                          0.55298
                                                0.99800
                                                                  0.79998
5
         1
            0.1
                          0.41945
                                                0.96008
                                                                  0.53853
6
         1
            0.1
                          0.45702
                                                1.13148
                                                                  0.71873
7
             0.1
         1
                          0.48078
                                                0.93613
                                                                  0.68116
8
         1
             0.1
                          0.49762
                                                1.10178
                                                                  0.80324
9
         1
             0.1
                          0.49122
                                                                  0.68719
                                                1.11605
  ABC GAN MAE ABC_GAN MAE (skip connection)
0
      0.65128
                                    0.55556
1
      0.68853
                                    0.40891
2
      0.42552
                                    0.32026
3
      0.70891
                                    0.71962
4
      0.39579
                                    0.40052
5
      0.53043
                                    0.44123
6
      0.39832
                                    0.48503
7
                                    0.44009
      0.48170
8
      0.43675
                                    0.37400
9
      0.56866
                                    0.40666
Variance
                                1.000000
Bias
                                0.100000
Prior Model MAE
                               0.493940
ABC pre-generator MAE
                               1.096027
Skip Node weight
                               0.665780
```

ABC GAN MAE

ABC\_GAN MAE (skip connection) 0.424501

dtype: float64

| _                    |                 |         |                    | ABC pre-generator MAE | -                | \ |
|----------------------|-----------------|---------|--------------------|-----------------------|------------------|---|
| 0                    | 0.1             | 0.1     | 0.56484            | 0.56716               | 0.28413          |   |
| 1                    | 0.1             | 0.1     | 0.47589            | 0.50338               | 0.47540          |   |
| 2                    | 0.1             | 0.1     | 0.61824            | 0.62408               |                  |   |
| 3                    | 0.1             | 0.1     | 0.50811            | 0.54184               | 0.40798          |   |
| 4                    | 0.1             | 0.1     | 0.62039            | 0.60978               | 0.22225          |   |
| 5                    | 0.1             | 0.1     | 0.47623            | 0.47478               | 0.67082          |   |
| 6                    | 0.1             | 0.1     | 0.65257            | 0.65590               | 0.57746          |   |
| 7                    | 0.1             | 0.1     | 0.56224            | 0.54549               | 0.70165          |   |
| 8                    | 0.1             | 0.1     | 0.42323            | 0.49448               | 0.50202          |   |
| 9                    | 0.1             | 0.1     | 0.55557            | 0.54320               | 0.19723          |   |
|                      | ABC GAN M       | IAE AE  | BC_GAN MAE (skip c | connection)           |                  |   |
| 0                    | 0.662           |         | ·                  | 0.38217               |                  |   |
| 1                    | 0.546           |         |                    | 0.48815               |                  |   |
| 2                    | 0.508           |         |                    | 0.42242               |                  |   |
| 3                    | 0.521           |         |                    | 0.60617               |                  |   |
| 4                    | 0.911           |         |                    | 0.55651               |                  |   |
| 5                    | 0.556           |         |                    | 0.50154               |                  |   |
| 6                    | 0.722           |         |                    | 0.55546               |                  |   |
| 7                    |                 |         |                    | 0.72986               |                  |   |
| 8                    |                 |         |                    | 0.44295               |                  |   |
| 9                    | 0.562           |         |                    | 0.47822               |                  |   |
| Va                   | riance          |         | 0                  | 100000                |                  |   |
| Bi                   |                 |         |                    | 100000                |                  |   |
|                      | as<br>ior Model | млг     |                    | 558905                |                  |   |
|                      |                 |         |                    | 544347                |                  |   |
|                      | C pre-gene      |         |                    |                       |                  |   |
| Skip Node weight     |                 |         |                    | 488711                |                  |   |
| ABC GAN MAE 0.559392 |                 |         |                    |                       |                  |   |
|                      |                 | _       | connection) 0.     | 494845                |                  |   |
| dt                   | ype: float<br>  | 564<br> |                    |                       |                  |   |
|                      | Variance        | Bias    | Prior Model MAE    | ABC pre-generator MAE | Skip Node weight | \ |
| 0                    | 0.01            | 0.1     | 0.51659            | 0.53017               | 0.27844          | \ |
| 1                    | 0.01            | 0.1     | 0.47934            | 0.47985               | 0.40315          |   |
| 2                    | 0.01            | 0.1     |                    |                       |                  |   |
|                      |                 |         | 0.46465            | 0.50323               | 0.27094          |   |
| 3                    | 0.01            | 0.1     | 0.51597            | 0.49841               | 0.24035          |   |
| 4                    | 0.01            | 0.1     | 0.60559            | 0.59758               | 0.23521          |   |
| 5                    | 0.01            | 0.1     | 0.57285            | 0.57108               | 0.20970          |   |
| 6                    | 0.01            | 0.1     | 0.56041            | 0.54468               | 0.18111          |   |
| 7                    | 0.01            | 0.1     | 0.51594            | 0.52984               | 0.39069          |   |
| 8                    | 0.01            | 0.1     | 0.30555            | 0.33567               | 0.69118          |   |
| 9                    | 0.01            | 0.1     | 0.56230            | 0.58217               | 0.38494          |   |

```
ABC GAN MAE ABC_GAN MAE (skip connection)
0
       0.52370
                                       0.32378
1
       0.56483
                                       0.46745
2
       0.34764
                                       0.44929
3
                                       0.42082
       0.51693
4
       0.51468
                                       0.55375
5
       0.74356
                                       0.36602
6
                                       0.56743
       0.45670
7
       0.50063
                                       0.44934
8
       0.35404
                                       0.44647
9
       0.45950
                                       0.57172
                                  0.010000
Variance
Bias
                                  0.100000
Prior Model MAE
                                 0.516278
ABC pre-generator MAE
                                 0.530005
Skip Node weight
                                 0.274691
ABC GAN MAE
                                 0.507653
ABC_GAN MAE (skip connection) 0.449316
dtype: float64
  Variance Bias Prior Model MAE ABC pre-generator MAE Skip Node weight \
0
          1 0.01
                           0.62588
                                                   1.18596
                                                                     0.35418
1
          1 0.01
                           0.52304
                                                   1.01815
                                                                     0.33965
2
          1 0.01
                           0.74975
                                                   1.05210
                                                                      0.29646
3
          1 0.01
                           0.52429
                                                   0.95581
                                                                      0.32946
4
          1 0.01
                           0.48338
                                                   1.00998
                                                                      0.32076
5
          1 0.01
                           0.58723
                                                   1.14215
                                                                      0.32050
6
          1 0.01
                           0.58388
                                                   1.15237
                                                                     0.47708
7
          1 0.01
                           0.49451
                                                   0.76121
                                                                     0.34719
8
          1 0.01
                           0.50876
                                                   1.05500
                                                                     0.41988
9
          1 0.01
                           0.67886
                                                   1.39967
                                                                     0.35270
  ABC GAN MAE ABC GAN MAE (skip connection)
0
       0.54323
                                       0.46617
1
       0.61959
                                       0.49882
2
       0.58510
                                       0.72495
3
                                       0.46782
       0.45701
4
       0.32568
                                       0.35579
5
       0.57248
                                       0.59535
6
       0.48084
                                       0.44876
7
       0.29037
                                       0.42110
8
       0.40448
                                       0.41576
9
       0.66499
                                       0.71340
                                  1.000000
Variance
```

Bias

```
Prior Model MAE
                              0.554083
ABC pre-generator MAE
                             1.053550
Skip Node weight
                              0.343423
ABC GAN MAE
                             0.512035
ABC GAN MAE (skip connection) 0.466998
dtype: float64
  Variance Bias Prior Model MAE ABC pre-generator MAE Skip Node weight \
       0.1 0.01
                  0.52713
0
                                              0.53239
                                                               0.24743
1
       0.1 0.01
                       0.60158
                                              0.58374
                                                               0.15920
2
       0.1 0.01
                       0.63817
                                              0.62046
                                                               0.20914
3
       0.1 0.01
                       0.56911
                                              0.56816
                                                               0.18413
4
      0.1 0.01
                        0.64806
                                             0.61719
                                                              0.16301
5
      0.1 0.01
                       0.61426
                                             0.61155
                                                              0.21559
6
      0.1 0.01
                                             0.53986
                                                              0.21552
                       0.52819
7
      0.1 0.01
                       0.43284
                                             0.40754
                                                              0.32789
8
      0.1 0.01
                       0.47584
                                            0.48683
                                                              0.21928
9
       0.1 0.01
                        0.41747
                                              0.39251
                                                              0.20267
  ABC GAN MAE ABC_GAN MAE (skip connection)
0
      0.49321
                                   0.52259
1
      0.48550
                                   0.52312
2
      0.55401
                                   0.54453
3
      0.38670
                                   0.46995
4
      0.36521
                                   0.36476
5
    0.67290
                                   0.44144
6
      0.65886
                                   0.39668
7
      0.27239
                                   0.27265
8
      0.51177
                                   0.46258
      0.43027
                                   0.39745
Variance
                              0.100000
Bias
                              0.010000
Prior Model MAE
                              0.548651
ABC pre-generator MAE
                             0.554013
Skip Node weight
                             0.212334
ABC GAN MAE
                             0.489353
ABC_GAN MAE (skip connection)
                             0.452011
dtype: float64
  Variance Ping Drier Model MAE ADC nr
```

|   | Variance | Bias | Prior Model MAE | ABC pre-generator MAE | Skip Node weight |
|---|----------|------|-----------------|-----------------------|------------------|
| 0 | 0.01     | 0.01 | 0.31832         | 0.32375               | 0.19151          |
| 1 | 0.01     | 0.01 | 0.54027         | 0.53400               | 0.17197          |
| 2 | 0.01     | 0.01 | 0.43639         | 0.43214               | 0.17381          |
| 3 | 0.01     | 0.01 | 0.49849         | 0.49781               | 0.19117          |
| 4 | 0.01     | 0.01 | 0.61684         | 0.61271               | 0.13287          |
| 5 | 0.01     | 0.01 | 0.58378         | 0.57790               | 0.20367          |

```
7
            0.01 0.01
                                0.54218
                                                      0.53840
                                                                         0.17850
     8
            0.01 0.01
                                0.58031
                                                      0.57566
                                                                        0.21411
     9
            0.01 0.01
                                0.51799
                                                      0.51483
                                                                        0.21570
        ABC GAN MAE
                    ABC_GAN MAE (skip connection)
     0
            0.30129
     1
            0.43375
                                           0.50622
     2
            0.46646
                                           0.39244
     3
            0.36862
                                           0.46545
     4
            0.87588
                                           0.57286
     5
            0.53713
                                           0.35204
     6
            0.46122
                                           0.39844
     7
            0.56682
                                           0.58491
     8
            0.52019
                                           0.54366
     9
            0.42981
                                         108.15121
     Variance
                                      0.010000
     Bias
                                      0.010000
     Prior Model MAE
                                      0.529130
     ABC pre-generator MAE
                                      0.524417
     Skip Node weight
                                      0.187100
     ABC GAN MAE
                                      0.463838
     ABC_GAN MAE (skip connection)
                                     0.485838
     dtype: float64
[10]: # Display Stats Summary Tables
     data = np.array(data)
     catboostData = []
     for i in range(9):
          catboostData.append([gan_median,stats,paramVal[i][0],__
       →paramVal[i][1],median(data[i][:,3]),median(data[i][:,5]),median(data[i][:
       →,6]),median(data[i][:,4])])
     df = pd.DataFrame(catboostData, columns =
       →['GAN','Stats','Variance','Bias','Prior Model','mGAN','skipGAN','Weight'])
     display(df.round(5))
            GAN
                   Stats Variance Bias Prior Model
                                                         mGAN
                                                                skipGAN
                                                                         Weight
     0 0.44772 0.48174
                              1.00 1.00
                                                               0.45948 0.99327
                                              1.39160 0.49185
     1 0.44772 0.48174
                              0.10 1.00
                                              0.92834 0.45461
                                                               0.43823 0.99851
     2 0.44772 0.48174
                              0.01 1.00
                                                      0.53092 0.54546 0.99755
                                              0.87969
                              1.00 0.10
     3 0.44772 0.48174
                                              1.09603
                                                      0.50607
                                                               0.42450 0.66578
     4 0.44772 0.48174
                              0.10 0.10
                                              0.54435
                                                      0.55939 0.49485 0.48871
     5 0.44772 0.48174
                              0.01 0.10
                                              0.53001 0.50765 0.44932 0.27469
     6 0.44772 0.48174
                              1.00 0.01
                                              1.05355 0.51204
                                                               0.46700 0.34342
     7 0.44772 0.48174
                              0.10 0.01
                                              0.55401 0.48935 0.45201 0.21233
     8 0.44772 0.48174
                              0.01 0.01
                                              0.52442 0.46384 0.48584 0.18710
```

6

0.01 0.01

0.48061

0.48210