

Assignment

1 Sorting Techniques

1.1 Implement Quick Sort using first/last/any random element as pivot.

Ans:

```

#include <iostream>
#include <cstdlib>
#include <ctime>
#define MAX 100

int size[20], x=0, n, s=0;
float x2[20];
using namespace std;

void swap(int* a, int* b)
{
    int t = *a;
    *a = *b;
    *b = t;
}

int partition(int arr[], int low, int high)
{
    int pivot = arr[high];
    int i = (low - 1);
    for (int j = low; j <= high - 1; j++)
    {
        if (arr[j] < pivot)
        {
            i++;
            swap(&arr[i], &arr[j]);
        }
    }
    swap(&arr[i+1], &arr[high]);
    return (i+1);
}

```

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```
void quicksort ( int arr [ ], int low, int high )
{
    if ( low < high )
    {
        int pi = partition ( arr, low, high );
        quicksort ( arr, low, pi - 1 );
        quicksort ( arr, pi + 1, high );
    }
    int end_clock = clock ();
    size [ S ] = n;
    S++;
}

void printArray ( int arr [ ], int size )
{
    int i;
    for ( i = 0; i < size; i++ )
        cout << " " << arr [ i ];
    cout << endl;
}

int main()
{
    int a [ 1000 ], n = 3;
    while ( n > 0 )
    {
        cout << "\n Enter the number of elements in the array : ";
        cin >> n;
        int a [ n ];
        for ( int i = 0; i < n; i++ )
        {
            int random = rand () % 100;
            a [ i ] = random;
        }
        cout << " Randomly generated array : ";
        int start_clock = clock ();
        quicksort ( a, 0, n - 1 );
        cout << " Sorted array : ";
        printArray ( a, n );
    }
}
```

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```
int end_clock = clock();
cout << "Time taken:" << (end_clock - start_clock) / double
    (CLOCKS_PER_SEC) * 1000 << "second" << endl;
}
return 0;
```

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partha@partha-pratim-sarmah:~

```
partha@partha-pratim-sarmah:~$ g++ quick_sort.cpp  
partha@partha-pratim-sarmah:~$ ./a.out
```

```
Enter the number of elements in the array: 3  
Randomly generated array:  
Sorted array: 77 83 86  
Time taken:0.046second
```

```
Enter the number of elements in the array: 2  
Randomly generated array:  
Sorted array: 15 93  
Time taken:0.026second
```

```
Enter the number of elements in the array: 1  
Randomly generated array:  
Sorted array: 35  
Time taken:0.019second
```

```
Enter the number of elements in the array: 0  
Randomly generated array:  
Sorted array:  
Time taken:0.015second
```

```
partha@partha-pratim-sarmah:~$ █
```

Q.2. Implement the ascending and descending order using Quick Sort.

Ans:-

```
#include <stdio.h>
int partition (int a[], int low, int high) // for ascending
{
    int pivot;
    int i, j, t;
    pivot = a[high];
    i = (low - 1);
    for (j = low; j <= high - 1; j++)
    {
        if (a[j] < pivot)
        {
            i++;
            t = a[i];
            a[i] = a[j];
            a[j] = t;
        }
    }
    t = a[i + 1];
    a[i + 1] = a[high];
    a[high] = t;
    return i + 1;
}
```

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```

int quicksort ( int a [20], int low, int high)
{
    int pivot;
    if (low < high)
    {
        pivot = partition (a, low, high);
        quicksort (a, low, pivot - 1);
        quicksort (a, pivot + 1, high);
    }
    return 0;
}

void swap (int arr [ ], int one, int two) "for descending
{
    int temp = Array [one];
    Array [one] = Array [two];
    Array [two] = temp;
} // for descending order

int partition1 (int Array [ ], int left, int right)
{
    int pivot = Array [right];
    int leftPointer = left - 1;
    int rightPointer = right;
    for (i)
    {
        while (Array [++leftPointer] > pivot)
        {
            while (rightPointer > 0 && Array [--rightPointer] < pivot)
        }
        if (leftPointer >= rightPointer) { break; }
        else { swap (Array, leftPointer, right); }
        return leftPointer;
    }
}

```

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```

void Quicksort (int Array[ ], int left , int right )
{
    if (left < right)
    {
        int Partition1 Point = partition1 (Array, left, right),
            Quicksort (Array, left, Partition1 Point - 1),
            Quicksort (Array, Partition1 Point + 1, right);
    }
}

int main()
{
    int a[20], i, j, low, high, n;
    printf ("Enter the size of the array : ");
    scanf ("%d", &n);
    printf ("Enter the elements in the array : ");
    for (i=0; i<n; i++)
        scanf ("%d", &a[i]);
    quicksort (a, 0, n-1);
    printf ("After quicksort the arrays is in ascending order : ");
    for (i=0; i<n; i++)
        printf ("%d", a[i]);
    quicksort (a, 0, n-1);
    printf ("After quicksort the arrays is in descending order : ");
    for (i=0; i<n; i++)
        printf ("%d", a[i]);
    printf ("\n");
    return 0;
}

```

Output →

Enter the size of the array: 6

Enter the elements in the array: 5 1 3 2 9 10

After quick sort the arrays is in ascending order: 1 2 3 5 9 10

After quick sort the arrays is in descending order: 10 9 5 3 2 1

```
After quick sort the arrays is in ascending order: 1 2 3 5 9 10
partha@partha-pratim-sarmah:~/Documents$ ./a.out
Enter the size of the array: 6
Enter the elements in the array: 5 1 3 2 9
10
After quick sort the arrays is in ascending order: 1 2 3 5 9 10
After quick sort the arrays is in descending order: 10 9 5 3 2 1
partha@partha-pratim-sarmah:~/Documents$ █
```

1.3. Implement Quick Sort with duplicate numbers in a given array/elements.

Answer :-

```
#include <bits/stdc++.h>
```

```
using namespace std;
```

```
void partition ( int a[], int l, int r, int &i, int &j )
```

{

```
    i = l - 1, j = r;
```

```
    int p = l - 1, q = r;
```

```
    int v = a[r];
```

```
    while (true)
```

```
    { while (a[++l] < v),
```

```
        while (v < a[--j])
```

```
            if (j == l)
```

```
                break;
```

```
            if (i >= j) break;
```

```
            swap(a[i], a[j]);
```

```
            if (a[i] == v)
```

```
            { p++;
```

```
                swap(a[p], a[i]);
```

```
}
```

```
            if (a[j] == v)
```

```
            { q--;
```

```
                swap(a[j], a[q]);
```

```
        }
```

```
        swap(a[i], a[r]);
```

```
        j = i - 1;
```

```
        for (int k = l; k < p; k++, j--)
```

```
            swap(a[k], a[j]);
```

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```
i = i + 1;  
for (int k = n - 1; k > q; k--, i++)  
    swap(a[i], a[k]);  
}  
void quicksort (int a[], int l, int r)  
{  
    if (r <= l) return;  
    int i, j;  
    partition (a, l, r, i, j);  
    quicksort (a, l, j);  
    quicksort (a, i, r);  
}  
void printarr (int a[], int n)  
{  
    for (int i = 0; i < n; ++i)  
        printf ("%d", a[i]);  
    printf ("\n");  
}  
int main()  
{  
    printf (" Given Arrays elements are : \n ");  
    int a[] = { 4, 9, 4, 4, 1, 9, 4, 4, 9, 4, 4, 1, 4 };  
    int size = sizeof (a) / sizeof (int);  
    printarr (a, size);  
    quicksort (a, 0, size - 1);  
    printf (" In sorted Arrays elements are : \n ");  
    printarr (a, size);  
    return 0;  
}
```

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Output →

Given Arrays elements are :

4 9 4 4 1 9 4 4 9 4 4 1 4

Sorted arrays elements are :

1 1 4 4 4 4 4 4 4 4 9 9 9

```
partha@partha-pratim-sarmah:~$ g++ 1.3.3.3
partha@partha-pratim-sarmah:~$ ./a.out
```

Given Arrays elements are:

4 9 4 4 1 9 4 4 9 4 4 1 4

Sorted arrays elements are:

1 1 4 4 4 4 4 4 4 4 9 9 9

```
partha@partha-pratim-sarmah:~$ █
```

1.4 Finding Kth minimum and maximum element in heap.

```

Ans #include <iostream>
using namespace std;
void swap (int &x, int &y)
{
    int temp = x;
    x = y;
    y = temp;
}

class MinHeap
{
    int size;
    int* arr;
public:
    MinHeap (int size, int input[]);
    void heapify (int i);
    void buildHeap();
};

MinHeap :: MinHeap (int size, int input[])
{
    this->size = size;
    this->arr = input;
    buildHeap();
}

void MinHeap :: heapify (int i)
{
    if (i >= size / 2)
        return;
    int smallest;
    int left = 2 * i + 1;
    int right = 2 * i + 2;
    smallest = arr [left] < arr [i] ? left : i;
}

```

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```

if (smallest != i)
{
    swap (arr[i], arr[smallest]),
    heapify (smallest);
}
}

void MinHeap::buildHeap()
{
    for (int i = size / 2 - 1; i >= 0; i--)
        heapify(i);
}

void FirstKelements (int arr[], int size, int k)
{
    MinHeap* m = new MinHeap (k, arr);
    for (int i = k; i < size; i++)
    {
        if (arr[0] > arr[i])
            continue;
        else
        {
            arr[0] = arr[i];
            m->heapify(0);
        }
    }

    for (int i = 0; i < k; i++)
        cout << arr[i] << " ";
}

int main()
{
    int arr[] = {11, 3, 2, 1, 15, 5, 4, 45, 88, 96, 50, 45};
    int size = sizeof(arr) / sizeof(arr[0]);
    int K = 3;
    FirstKelements (arr, size, K);
    cout << "\n";
    return 0;
}

```

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Output →

50 88 96

```
partha@partha-pratin-sarmah:  
50 88 96  
partha@partha-pratin-sarmah:
```

1.5 Build Min heap, Max heap and sort the given elements

Ans

```
#include <iostream>
using namespace std;
```

```
void heapify(int arr[], int n, int i)
```

```
{ int largest = i;
```

```
    int l = 2 * i + 1;
```

```
    int r = 2 * i + 2;
```

```
    if (l < n && arr[i] > arr[largest])
```

```
        largest = l;
```

```
    if (r < n && arr[r] > arr[largest])
```

```
        largest = r;
```

```
    if (largest != i)
```

```
        swap(arr[i], arr[largest]);
```

```
        heapify(arr, n, largest);
```

```
}
```

```
}
```

```
void buildHeap(int arr[], int n)
```

```
{ int startIdx = (n/2) - 1;
```

```
for (int i = startIdx; i >= 0; i--)
```

```
    heapify(arr, n, i);
```

```
}
```

```
void printHeap(int arr[], int n)
```

```
{ cout << "Array representation of heap is: \n";
```

```
for (int i = 0; i < n; i++)
```

```
    cout << arr[i] << " ";
```

```
}
```

```
int main()
```

```
{ int arr[] = {1, 3, 5, 4, 6, 13, 10, 9, 8, 15, 17};
```

```
int n = sizeof(arr) / sizeof(arr[0]);
```

```
buildHeap(arr, n); printHeap(arr, n);
```

```
} return 0;
```

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Output →

Array representation of Heap is :

17 15 13 9 6 5 10 4 8 3 1

1.5.cpp

1.5(1).cpp

```
partha@partha-pratim-sarmah:~$ g++ 1.5.cpp
partha@partha-pratim-sarmah:~$ ./a.out
Array representation of Heap is:
17 15 13 9 6 5 10 4 8 3 1
partha@partha-pratim-sarmah:~$
```

1.6 Delete Kth indexed element in Min Heap and Max Heap.

Ans:-

```
#include <iostream>
using namespace std;
void heapify( int arr[ ], int n, int i )
{
    int largest = i;
    int l = 2 * i + 1;
    int r = 2 * i + 2;
    if ( l < n && arr[ l ] > arr[ largest ] )
        largest = l;
    if ( r < n && arr[ r ] > arr[ largest ] )
        largest = r;
    if ( largest != i ) {
        swap( arr[ i ], arr[ largest ] );
        heapify( arr, n, largest );
    }
}
void deleteRoot( int arr[ ], int & n )
{
    int lastElement = arr[ n - 1 ];
    arr[ 0 ] = lastElement;
    n = n - 1;
    heapify( arr, n, 0 );
}
void printArray( int arr[ ], int n )
{
    for ( int i = 0; i < n; ++i )
        cout << arr[ i ] << " ";
    cout << endl;
}
int main()
{
    int arr[ ] = { 10, 5, 3, 2, 4 };
    int n = sizeof( arr ) / sizeof( arr[ 0 ] );
    deleteRoot( arr, n );
    printArray( arr, n );
    return 0;
}
```

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```
partha@partha-pratin-sarmah:~$ g++ 1.6  
partha@partha-pratin-sarmah:~$ ./a.out  
5 4 3 2  
partha@partha-pratin-sarmah:~$ █
```

Output → 5 4 3 2

2 Greedy Algorithms

2.1 Implement the job sequencing with deadlines problem using the fixed tuple size formulation.

Ans

```
#include <iostream>
#include <algorithm>
using namespace std;
```

struct Job

```
{ char id;
  int dead;
  int profit;
};
```

```
bool compare (Job a, Job b)
{
    return (a.profit > b.profit);
}
```

```
void jobschedule (Job arr[], int n)
{
    sort (arr, arr+n, compare);
    int result[n];
    bool slot[n];
    for (int i=0; i<n; i++)
        slot[i] = false;
    for (int i=0; i<n; i++)
    {
        for (int j=min(n, arr[i].dead)-1; j>=0; j--)
        {
            if (slot[j] == false)
            {
                result[j] = i;
                slot[j] = true;
                break;
            }
        }
    }
}
```

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```
for (int i=0 ; i<n ; i++)
    if (slot[i])
        cout << arr[result[i]].id << " ";
}

int main()
{
    Job arr[] = { {'a', 2, 20}, {'b', 2, 15}, {'c', 1, 10},
                  {'d', 3, 5}, {'e', 3, 1} };
    int n = 5;
    cout << "Maximum profit sequence of jobs is -> ";
    jobschedule(arr, n);
    cout << endl;
}
```

Output →

maximum profit sequence of jobs is $\rightarrow b \ a \ d$

Q

partha@partha-pratim-sarmah:~

partha@partha-pratim-sarmah:~\$ g++ 2.1.cpp

partha@partha-pratim-sarmah:~\$./a.out

maximum profit sequence of jobs is $\rightarrow b \ a \ d$

partha@partha-pratim-sarmah:~\$ █

2.2 Implement Knapsack problem.

Ans #include <bits/stdc++.h>

using namespace std;

struct Item

{ int value, weight;

Item (int value, int weight) : value(value), weight(weight)

{}
};

bool cmp (struct Item a, struct Item b)

{

double r1 = (double)a.value / a.weight;

double r2 = (double)b.value / b.weight;

return r1 > r2;

}

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```

double fractionalKnapsack (int w, struct Item arr[], int n)
{
    sort (arr, arr + n, cmp);
    int curWeight = 0;
    double finalValue = 0.0;
    for (int i=0; i<n; i++)
    {
        if (curWeight + arr[i].weight <= w)
        {
            curWeight += arr[i].weight;
            finalValue += arr[i].value;
        }
        else
        {
            int remain = w - curWeight;
            finalValue += arr[i].value * ((double)remain / arr[i].weight);
            break;
        }
    }
    return finalValue;
}

int main()
{
    int w = 50;
    Item arr[] = {{60, 10}, {100, 20}, {120, 30}};
    int n = sizeof(arr) / sizeof(arr[0]);
    cout << "Maximum value we can obtain = "
        << fractionalKnapsack (w, arr, n) << endl;
    return 0;
}

```

```
Q partha@partha-pratim-s... F E - D X
partha@partha-pratim-sarmah:~$ g++ 2.2.cpp
partha@partha-pratim-sarmah:~$ ./a.out
Maximum value we can obtain = 240
partha@partha-pratim-sarmah:~$ █
```

Output →

Maximum value we can obtain = 240

2.3 Implement the file or code compression using Huffman's algorithm.

Ans

```

#include <iostream>
#include <cstdlib>
using namespace std;
#define MAX-TREE-HT 100
struct MinHeapNode
{
    char data;
    unsigned freq;
    struct MinHeapNode *left, *right;
};
struct MinHeap
{
    unsigned size;
    unsigned capacity;
    struct MinHeapNode** array;
};

struct MinHeapNode* newNode (char data, unsigned freq)
{
    struct MinHeapNode* temp = (struct MinHeapNode*)malloc(
        sizeof(struct MinHeapNode));
    temp->left = temp->right = NULL;
    temp->data = data;
    temp->freq = freq;
    return temp;
}

struct MinHeap* createMinHeap (unsigned capacity)
{
    struct MinHeap* minHeap = (struct MinHeap*)
        malloc (sizeof(struct MinHeap));
    minHeap->size = 0;
    minHeap->capacity = capacity;
}

```

```

mintleap → array = (struct MinHeapNode**) malloc (mintleap →
    capacity * sizeof (struct MinHeapNode *));
return mintleap;
}

void swapMinHeapNode (struct MinHeapNode** a, struct
    MinHeapNode** b)
{
    struct MinHeapNode* t = *a;
    *a = *b;
    *b = t;
}

void minHeapify (struct MinHeap* mintleap, int idx)
{
    int smallest = idx;
    int left = 2 * idx + 1;
    int right = 2 * idx + 2;
    if (left < mintleap → size && mintleap → array [left] → freq
        < mintleap → array [smallest] → freq)
    {
        smallest = left;
    }
    if (right < mintleap → size && mintleap → array [right] →
        freq < mintleap → array [smallest] → freq)
    {
        smallest = right;
    }
    if (smallest != idx) {
        swapMinHeapNode (& mintleap → array [smallest],
            & mintleap → array [idx]);
        minHeapify (mintleap, smallest);
    }
}

```

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```

int isSizeOne ( struct MinHeap * mintHeap )
{
    return ( mintHeap -> size == 1 );
}

struct MinHeapNode* extractMin ( struct MinHeap * mintHeap )
{
    struct MinHeapNode* temp = mintHeap -> array [ 0 ];
    mintHeap -> array [ 0 ] = mintHeap -> array [ mintHeap -> size - 1 ];
    -- mintHeap -> size;
    minHeapify ( mintHeap, 0 );
    return temp;
}

void insertMinHeap ( struct MinHeap * mintHeap, struct MinHeapNode * mintHeapNode )
{
    ++ mintHeap -> size;
    int i = mintHeap -> size - 1;
    while ( i && mintHeapNode -> freq < mintHeap -> array [ ( i - 1 ) / 2 ] -> freq )
    {
        mintHeap -> array [ i ] = mintHeap -> array [ ( i - 1 ) / 2 ];
        i = ( i - 1 ) / 2;
    }
    mintHeap -> array [ i ] = mintHeapNode;
}

void buildMinHeap( struct MinHeap * mintHeap )
{
    int n = mintHeap -> size - 1;
    int i;
    for ( i = ( n - 1 ) / 2 ; i >= 0 ; -- i )
        minHeapify ( mintHeap, i );
}

```

```

void printArr (int arr[], int n)
{
    int i;
    for (i=0; i<n; ++i)
        cout << arr[i];
    cout << "\n";
}

int isLeaf (struct MintleapNode* root)
{
    return !(root->left) && !(root->right);
}

struct Mintleap* createAndBuildMintleap (char data[], int freq[],
                                         int size)
{
    struct Mintleap* mintleap = createMintleap (size);
    for (int i=0; i< size; ++i)
        mintleap->arr[i] = newNode (data[i], freq[i]);
    mintleap->size = size;
    buildMintleap (mintleap);
    return mintleap;
}

struct MintleapNode* buildHuffmanTree (char data[], int freq[],
                                       int size)
{
    struct MintleapNode *left, *right, *top;
    struct Mintleap* mintleap = createAndBuildMintleap (data, freq,
                                                       size);
    while (!isSizeOne (mintleap))
    {
        left = extractMin (mintleap);
        right = extractMin (mintleap);
        top = newNode ('$', left->freq + right->freq);
        top->left = left;
        top->right = right;
        insertMin (mintleap, top);
    }
}

```

```

top->left = left;
top->right = right;
insertMinHeap (minHeap, top);
}
return extractMin (minHeap);
void printCodes (struct MinHeapNode* root, int arr[], int top)
{
    if (root->left)
    {
        arr[top] = 0;
        printCodes (root->left, arr, top + 1);
    }
    if (root->right)
    {
        arr[top] = 1;
        printCodes (root->right, arr, top + 1);
    }
    if (isLeaf (root))
    {
        cout << root->data << ":" ;
        printArr (arr, top);
    }
}
void HuffmanCodes (char data[], int freq[], int size)
{
    struct MinHeapNode* root = buildHuffmanTree (data, freq, size);
    int arr [MAX-TREE-HT], top=0;
    printCodes (root, arr, top);
}
int main()
{
    char arr[] = { 'a', 'b', 'c', 'd', 'e', 'f' };
    int freq[] = { 5, 9, 12, 13, 16, 45 };
    int size = sizeof (arr) / sizeof (arr[0]);
    HuffmanCodes (arr, freq, size);
    return 0;
}

```

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```
partha@partha-pratin  
partha@partha-pratin  
Maximum value we can  
partha@partha-pratin  
partha@partha-pratin  
f: 0  
c: 100  
d: 101  
a: 1100  
b: 1101  
e: 111  
partha@partha-pratin
```

Output → f: 0
c: 100
d: 101
a: 1100
b: 1101
e: 111

2.4 Implement the minimisation of records movement using Optimal Merge Pattern Algorithm.

Ans

```
#include <iostream>
using namespace std;

int main()
{
    int i, k, a[10], c[10], n, l;
    cout << "Enter the no. of elements: ";
    cin >> n;
    cout << "Enter the sorted elements for optimal merge pattern: ";
    for (i = 0; i < n; i++)
        cin >> a[i];
    i = 0;
    k = 0;
    c[k] = a[i] + a[i + 1];
    i = 2;
    while (i < n)
    {
        k++;
        if ((c[c[k - 1]] + a[i]) <= (a[i] + a[i + 1]))
            c[k] = c[k - 1] + a[i];
        else
        {
            c[k] = a[i] + a[i + 1];
            i = i + 2;
            while (i < n)
            {
                k++;
                if ((c[c[k - 1]] + a[i]) <= (c[c[k - 2]] + a[i]))
                    c[k] = c[k - 1] + a[i];
                else
                    c[k] = c[k - 2] + a[i];
                i++;
            }
        }
    }
}
```

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}

k++

c[k] = c[k-1] + c[k-2];

cout << "The optimal sum are as follows \n";

for (k=0; k<n-1; k++)

{ cout << c[k] << "\t";

}

l=0;

for (k=0; k<n-1; k++)

l = l + c[k];

cout << "The external path length is . . . " << l;

return 0;

}

The external path length is33
partha@partha-pratin-sarmah:~\$./a.out
Enter the no. of elements: 5

Enter the sorted elements for optimal merge pattern: 5 6 7 8 9 10

The optimal sum are as follows.....

11 15 20 35

The external path length is81
partha@partha-pratin-sarmah:~\$

```
l=0; f[0]=5; f[1]=6; f[2]=7; f[3]=8; f[4]=9; f[5]=10;
for(k=0;k<n-1;k++)
{
```

Output →

Enter the no. of elements: 5

Enter the sorted elements for optimal merge
pattern: 5 6 7 8 9 10

The optimal sum are as follows

11 15 20 35

The external path length is81

3. Graph Algorithm

3.1 Find Minimum Cost Spanning Tree of a given undirected graph using Kruskal's algorithm.

Ans

```
#include <stdlib.h>
#include <cstring>
#include <iostream>
using namespace std;
struct Edge
{
    int src, dest, weight;
};
struct Graph
{
    int V, E;
    struct Edge* edge;
};
```

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```

struct Graph* createGraph (int V, int E)
{
    struct Graph* graph = (struct Graph*) malloc (sizeof
        (struct Graph));
    graph->V = V;
    graph->E = E;
    graph->edge = (struct Edge*) malloc (graph->E *
        sizeof (struct Edge));
    return graph;
}

struct subset
{
    int parent;
    int rank;
};

int find (struct subset subsets[], int i)
{
    if (subsets[i].parent != i)
        subsets[i].parent = find (subsets, subsets[i].parent);
    return subsets[i].parent;
}

void Union (struct subset subsets[], int x, int y)
{
    int xroot = find (subsets, x);
    int yroot = find (subsets, y);
    if (subsets[xroot].rank < subsets[yroot].rank)
        subsets[xroot].parent = yroot;
    else if (subsets[xroot].rank > subsets[yroot].rank)
        subsets[yroot].parent = xroot;
    else {
        subsets[yroot].parent = xroot;
        subsets[xroot].rank++;
    }
}

```

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```

int myComp ( const void* a, const void* b )
{
    struct Edge* a1 = (struct Edge*) a;
    struct Edge* b1 = (struct Edge*) b;
    return a1->weight > b1->weight;
}

void KruskalMST (struct Graph* graph)
{
    int V = graph->V;
    struct Edge result[V];
    int e = 0;
    int i = 0;
    qsort (graph->edge, graph->E, sizeof(graph->Edge[0]),
            myComp);
    struct subset *subsets = (struct subset*) malloc
        (V * sizeof(struct subset));
    for (int v = 0; v < V; ++v)
    {
        subsets[v].parent = v;
        subsets[v].rank = 0;
    }
    while (e < V - 1)
    {
        struct Edge next_edge = graph->edge[i++];
        int x = find (subsets, next_edge.src);
        int y = find (subsets, next_edge.dest);
        if (x != y)
        {
            result[e++] = next_edge;
            union (subsets, x, y);
        }
    }
}

```

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```

cout << " Following are the edges in the constructed MST \n";
for(i=0; i<e; ++i)
{
    cout << result[i].src << " -- " << result[i].dest << " == "
        << result[i].weight << endl;
}
return;
}

```

```

int main()
{
    int V = 4;
    int E = 5;
    struct Graph* graph = createGraph(V, E);

    graph->edge[0].src = 0;
    graph->edge[0].dest = 1;
    graph->edge[0].weight = 10;

    graph->edge[1].src = 0;
    graph->edge[1].dest = 2;
    graph->edge[1].weight = 6;

    graph->edge[2].src = 0;
    graph->edge[2].dest = 3;
    graph->edge[2].weight = 5;

    graph->edge[3].src = 1;
    graph->edge[3].dest = 3;
    graph->edge[3].weight = 15;

    graph->edge[4].src = 2;
    graph->edge[4].dest = 3;
    graph->edge[4].weight = 4;

    KruskalMST(graph);
    return 0;
}

```

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```
partha@partha-pratim-sarmah:~$ g++ 3.1.cpp
partha@partha-pratim-sarmah:~$ ./a.out
Following are the edges in the constructed MST
2 -- 3 == 4
0 -- 3 == 5
0 -- 1 == 10
partha@partha-pratim-sarmah:~$
```

Output →

Following are the edges in the constructed MST

2 -- 3 == 4
0 -- 3 == 5.
0 -- 1 == 10

3.2 Find Minimum Cost Spanning Tree of a given undirected graph using Prim's algorithm.

Aim #include <iostream>

#include <cstring>

using namespace std;

define INF 9999999

define V 5

int G[V][V] = {

{ 0, 9, 75, 0, 0 },

{ 9, 0, 95, 19, 42 },

{ 75, 95, 0, 51, 66 },

{ 0, 19, 51, 0, 31 },

{ 0, 42, 66, 31, 0 }

};

int main()

{ int no-edge;

int selected[V];

memset(selected, false, sizeof(selected));

no-edge = 0;

selected[0] = true;

int x, y;

cout << "Edge" << ":" << " weight";

cout << endl;

while (no-edge < V - 1)

{ int min = INF;

x = 0;

y = 0;

for (int i = 0; i < V; i++)

{ if (selected[i])

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```
{  
    for (int j = 0; j < v; j++)  
        {  
            if (!selected[j] && G[i][j])  
                {  
                    if (min > G[i][j])  
                        {  
                            min = G[i][j];  
                            x = i;  
                            y = j;  
                        }  
                }  
        }  
}
```

```
cout << x << " - " << y << ":" << G[x][y],
```

```
cout << endl;
```

```
selected[y] = true;
```

```
no_edge++;
```

```
}
```

```
return 0;
```

```
y
```

```
partha@partha-pr
Edge : weight
0 - 1 : 9
1 - 3 : 19
3 - 4 : 31
3 - 2 : 51
partha@partha-pr
```

Output →

Edge : weight

0 - 1	:	9
1 - 3	:	19
3 - 4	:	31
3 - 2	:	51

4. Shortest Path Finding in Graph

4.1 From a given vertex in a weighted connected graph, find shortest paths to other vertices using Dijkstra's algorithm.

Ans

```
#include <iostream>
#include <limits.h>
#include <stdio.h>
#define v 9
int minDistance ( int dist[], bool sptSet[] )
```

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```

for ( int v=0; v<V; v++ )
{
    if ( sptSet[v] == false && dist[v] <= min )
    {
        min = dist[v], min_index = v;
    }
}
return min_index;
}

void printSolution ( int dist[])
{
    printf ("vertex \t\t Distance from source\n");
    for ( int i=0; i<V; i++)
        printf (" %d \t\t %d\n", i, dist[i]);
}

void dijkstra ( int graph[V][V], int src)
{
    int dist [V];
    bool sptSet [V];
    for ( int i=0; i<V; i++)
        dist[i] = INT_MAX, sptSet[i] = false;
    dist[src] = 0;
    for ( int count = 0; count < V-1; count++)
    {
        int u = minDistance (dist, sptSet);
        sptSet[u] = true;
        for ( int v=0; v<V; v++)
        {
            if ( !sptSet[v] && graph[u][v] && dist[u] != INT_MAX && dist[u] + graph[u][v] < dist[v])
            {
                dist[v] = dist[u] + graph[u][v];
            }
        }
    }
    printSolution (dist);
}

```

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int main()

```
{ int graph[V][V] = { { 0, 4, 0, 0, 0, 0, 0, 8, 0 },
    { 4, 0, 8, 0, 0, 0, 0, 11, 0 },
    { 0, 8, 0, 7, 0, 4, 0, 0, 2 },
    { 0, 0, 7, 0, 9, 14, 0, 0, 0 },
    { 0, 0, 0, 9, 0, 10, 0, 0, 0 },
    { 0, 0, 4, 14, 10, 0, 2, 0, 0 },
    { 0, 0, 0, 0, 0, 2, 0, 1, 6 },
    { 8, 11, 0, 0, 0, 0, 1, 0, 7 },
    { 0, 0, 2, 0, 0, 0, 6, 7, 0 } };
}
```

dijkstra(graph, 0);

return 0;

}

—o—

```
partha@partha-pratim-sarmah:~$ g++ 4.1.cpp
partha@partha-pratim-sarmah:~$ ./a.out
/* L
int Vertex      Distance from Source
 0            0
 1            4
 2           12
 3           19
 4           21
 5           11
 6            9
 7            8
 8           14
partha@partha-pratim-sarmah:~$ █
ijkstra(graph, 0);
```

4.2 Draw simple, connected weighted graph with 8 vertices and 16 edges, each with unique edge weight. Identify one vertex as a start vertex and obtain shortest path using Dijkstra's algorithm.

```

Am #include <bits/stdc++.h>
using namespace std;
#define INF 0x3f3f3f3f
typedef pair<int, int> iPair;
class Graph {
    int V;
    list<iPair*>* adj;
public:
    Graph(int V);
    void addEdgeRev(int u, int v, int w);
    void shortestPath(int s);
};

Graph::Graph(int V) {
    this->V = V;
    adj = new list<iPair*>[V];
}

void Graph::addEdgeRev(int u, int v, int w) {
    adj[u].push_back(make_pair(v, w));
}

void Graph::shortestPath(int dest) {
    priority_queue<iPair, vector<iPair>, greater<iPair>> pq;
    vector<int> dist(V, INF);
    pq.push(make_pair(0, dest));
    dist[dest] = 0;
}

```

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```

while (!pq.empty())
{
    int u = pq.top().second;
    pq.pop();
    list<pair<int, int>>::iterator i;
    for (i = adj[u].begin(); i != adj[u].end(); ++i)
    {
        int v = (*i).first;
        int weight = (*i).second;
        if (dist[v] > dist[u] + weight)
        {
            dist[v] = dist[u] + weight;
            pq.push(make_pair(dist[v], v));
        }
    }
}
printf ("Destination Vertex Distance"
        " from all vertex \n");
for (int i = 0; i < v; ++i)
    printf ("%d \t\t %d \n", i, dist[i]);
}

int main()
{
    int v = 5;
    Graph g(v);
    g.addEdgeRev(0, 2, 1);
    g.addEdgeRev(0, 4, 5);
    g.addEdgeRev(1, 4, 1);
    g.addEdgeRev(2, 0, 10);
    g.addEdgeRev(2, 3, 5);
    g.addEdgeRev(3, 1, 1);
}

```

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```
g.addEdgeRev(4, 0, 5);  
g.addEdgeRev(4, 2, 100);  
g.addEdgeRev(4, 3, 5);  
g.shortestPath(0);  
return 0;
```

}

Output →

Destination	Vertex Distance from all vertex
0	0
1	6
2	10
3	7
4	5

C:\Users\ASUS\AppData\Local\Temp\main 4-2.exe

Destination Vertex Distance from all vertex

0	0
1	6
2	10
3	7
4	5

Process exited after 0.04501 seconds with return value 0
Press any key to continue . . .

4.3 Find the k-th shortest path between two given nodes of a graph.

Answer: —

```
#include <iostream>
#include <stdio.h>
using namespace std;
#define INFINITY 999
#define max 5
void dijkstra ( int G[max][max] , int n , int startnode );
int main()
{
    int G[max][max] = {{0,1,0,3,10},{1,0,5,0,0},{0,5,0,2,1},{3,0,2,0,6},{10,0,1,6,0}},
```

```
    int n=5, u=0;
```

```
    dijkstra ( G,n,u );
```

```
    return 0;
```

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```

void dijkstra ( int G[max][max], int n, int startnode )
{
    int cost[max][max], distance[max], pred[max];
    int visited[max], count, mindistance, nextnode, i, j;
    for ( i=0; i<n; i++ )
        for ( j=0; j<n; j++ )
            if ( G[i][j] == 0 )
                cost[i][j] = INFINITY;
            else
                cost[i][j] = G[i][j];
    for ( i=0; i<n, i++ )
    {
        distance[i] = cost[startnode][i];
        pred[i] = startnode;
        visited[i] = 0;
    }
    distance[startnode] = 0;
    visited[startnode] = 1;
    count = 1;
    while ( count < n-1 )
    {
        mindistance = INFINITY;
        for ( i=0; i<n; i++ )
            if ( distance[i] < mindistance && !visited[i] )
            {
                mindistance = distance[i];
                nextnode = i;
            }
        visited[nextnode] = 1;
        for ( i=0; i<n; i++ )
            if ( !visited[i] )

```

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```
if (mindistance + cost [nextnode][i] < distance[i])  
{  
    distance[i] = mindistance + cost [nextnode][i];  
    pred[i] = nextnode;  
}  
count++;  
}  
for (i=0; i<n; i++)  
if (i != startnode)  
{  
    cout << "In Distance of node " << i << "=" << distance[i];  
    cout << " In Path = " << i;  
    j = i;  
    do  
    {  
        j = pred[j];  
        cout << " - " << j;  
    }  
    while (j != startnode);  
}
```

Output →

Distance of node 1 = 1

Path = 1 <- 0

Distance of node 2 = 5

Path = 2 <- 3 <- 0

Distance of node 3 = 3

Path = 3 <- 0

Distance of node 4 = 6

Path = 4 <- 2 <- 3 <- 0

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Distance of node1=1

Path=1<-0

Distance of node2=5

Path=2<-3<-0

Distance of node3=3

Path=3<-0

Distance of node4=6

Path=4<-2<-3<-0

Process exited after 0.0405

Press any key to continue .

5 Dynamic Programming

5.1 Implement the Bottom Up Dynamic Programming Approach for matrix chain multiplication.

```
Ans:- #include <iostream>
#include <limits.h>
using namespace std;

int MatrixChainMultiplication ( int dims[ ], int i, int j )
{
    if ( j <= i + 1 )
        return 0;
    int min = INT_MAX;
    for ( int k = i + 1; k <= j - 1; k++ )
    {
        int cost = MatrixChainMultiplication(dims, i, k);
        cost += MatrixChainMultiplication(dims, k, j);
        cost += dims[i] * dims[k] * dims[j];
        if ( cost < min )
            min = cost;
    }
    return min;
}

int main()
{
    int dims[ ] = { 10, 30, 5, 60 };
}
```

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```
int n = sizeof(dims) / sizeof( dims[0]);  
cout << " Minimum cost is " << MatrixChainMultiplication(dims,0,n-1);  
return 0;  
}
```

C:\Users\ASUS\AppData\Local\Temp\main 5-1.exe

Minimum cost is 4500

Process exited after 0.1087 seconds with return value 0
Press any key to continue . . .

Output - Minimum cost is 4500

5.3 Implement the Top Down Dynamic Programming Memoization Approach for matrix chain multiplication.

Ans:

```
#include <bits/stdc++.h>
using namespace std;
int MatrixChainOrder (int P[], int i, int j)
{
    if (i == j)
        return 0;
    int k;
    int min = INT_MAX;
    int count;
    for (k = i; k < j; k++)
    {
        count = MatrixChainOrder (P, i, k)
            + MatrixChainOrder (P, k+1, j)
            + P[i-1] * P[k] * P[j];
        if (count < min)
            min = count;
    }
    return min;
}
int main()
{
    int arr[] = {1, 2, 3, 4, 3};
    int n = sizeof(arr)/sizeof(arr[0]);
    cout << "Minimum number of multiplication is "
        << MatrixChainOrder (arr, 1, n-1);
}
```

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```
C:\Users\ASUS\AppData\Local\Temp\main 5-2.exe
Minimum number of multiplications is 30
-----
Process exited after 0.1144 seconds with re
Press any key to continue . . .
```

5.2 Output →

minimum number of multiplication is 30

5.3 Implement the Bottom Up Dynamic Programming Approach
for longest common subsequence.

Ans

```
#include <iostream>
#include <string>
using namespace std;

int LCSLength (string X, string Y)

{
    int m = X.length(), n = Y.length();
    int lookup[m+1][n+1];
    for (int i=0; i<=m; i++)
        lookup[i][0] = 0;
    for (int j=0; j<=n; j++)
        lookup[0][j] = 0;
    for (int i=1; i<=m; i++)
    {
        for (int j=1; j<=n; j++)
        {
            if (X[i-1] == Y[j-1])
                lookup[i][j] = lookup[i-1][j-1] + 1;
            else
                lookup[i][j] = max(lookup[i-1][j],
                                    lookup[i][j-1]);
        }
    }
    return lookup[m][n];
}

int main()
{
    string X = "XMJYAUZ", Y = "MZJAWXU";
    cout << "The length of LCS is " << LCSLength(X, Y);
    return 0;
}
```

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Output → The length of LCS is 4

C:\Users\ASUS\AppData\Local\Temp\main 5-3.exe

The length of LCS is 4

Process exited after 0.1129 seconds with return code 0.
Press any key to continue . . .