

**OLLSCOIL NA hEIREANN, CORCAIGH**  
THE NATIONAL UNIVERSITY OF IRELAND, CORK

**COLAISTE NA hOLLSCOILE, CORCAIGH**  
UNIVERSITY COLLEGE, CORK

**Midterm Examination**

**Fourth Science Computer Science**

**CS4407 : Algorithms**

**Sample Final Exam**

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Professor G. Provan

**(Instructions –Answer all Questions.)**

**Time 60 minutes**

## CS4407 : Algorithms

### Sample MidTerm, Period 2

Please answer all questions; Total marks: 100  
Points for each question are indicated by [xx]

1. [25] Consider the *BubbleSort* algorithm.
  - (a) [15] Use the loop invariance approach to analyse this algorithm.
  - (b) [5] Use this approach to specify the complexity of the algorithm.
2. [25] Assume that Not All Equal 3SAT (a variant of 3SAT) is NP-Complete. Prove that Not All Equal 3SAT can be reduced to Set Splitting, thus proving that Set Splitting is NP-complete.

#### Not All Equal 3SAT

INSTANCE: Set  $U$  of variables, collection  $C$  of clauses over  $U$  such that each clause has 3 variables.

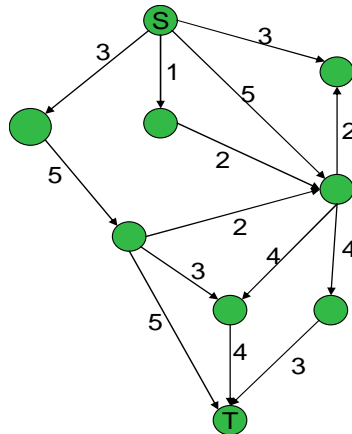
QUESTION: Is there a truth assignment for  $U$  such that each clause in  $C$  has at least one true literal and at least one false literal?

#### Set Splitting

INSTANCE: Collection  $C$  of subsets of a finite set  $S$ .

QUESTION: Is there a partition of  $S$  into two subsets  $S_1$  and  $S_2$  such that no subset in  $C$  is entirely contained in either  $S_1$  or  $S_2$ ?

3. [25] Consider the Travelling Salesman Problem on a complete undirected graph  $G$  with a length  $L(i,j) \geq 0$  for each edge  $(i,j)$ . Suppose the lengths satisfy  $L(i,j) \leq L(i,k) + 2 L(k,j)$  for all  $i, j, k$ .
  - (a) [10] Provide an approximation algorithm for  $G$ .
  - (b) [10] What is the approximation ratio?
4. [25] Consider a graph  $G(V,E)$ , with source node  $S$  and sink node  $T$ .



For the instance of a flow network shown below, compute the maximum flow. Give the actual flow as well as its value. Justify your answer.