lecture 3

view transformations

model transformations

GL_MODELVIEW transformation

view transformations:

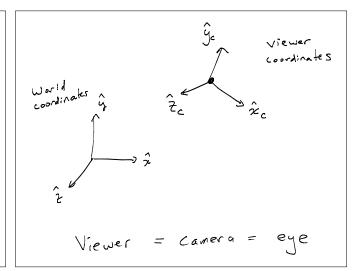
How do we map from world coordinates to camera/view/eye coordinates?

model transformations:

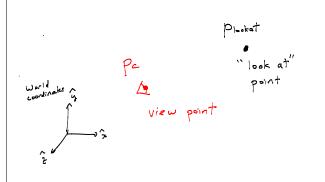
How do we map from object coordinates to world coordinates ?

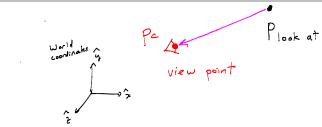
GL_MODELVIEW transformation

How do we map from object (to world) to view coordinates?

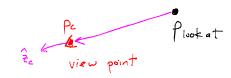


How can we specify the viewer's coordinate system?





Define the z axis of the viewer by a vector from the 'look at' point to the viewer.

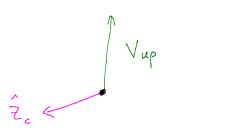


The z coordinate axis of the viewer is a unit vector in the direction is from the 'look at' point to the viewer.

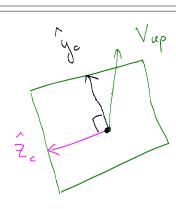
To specify the viewer's x and y coordinate axes, we need to choose from 360 degrees of possibilities.

Which way is up?

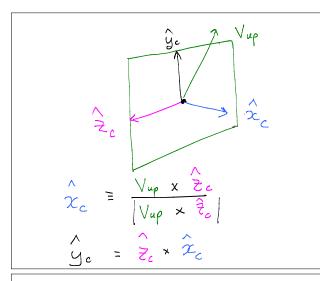
Define any 3D vector **Vup** such $\bigvee_{up} \cdot \stackrel{\wedge}{\rightleftharpoons} \neq \emptyset$ that



This defines a plane, containing Vup and z_c .



will be defined to lie in this plane.



Example

Viewer =
$$(2,1,1)$$

 $|a|$ $|a$

See lecture notes for the calculation.

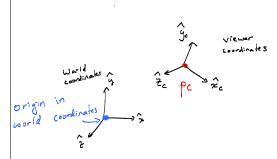
As a programmer using OpenGL, you don't have to compute these vectors. Instead you just define:

gluLookAt(eye[0], eye[1], eye[2],

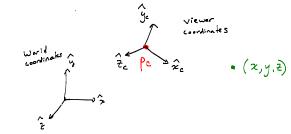
lookat[0], lookat[1], lookat[2],

up[0], up[1], up[2])

What does this definition do ("under the hood")? Coming soon...



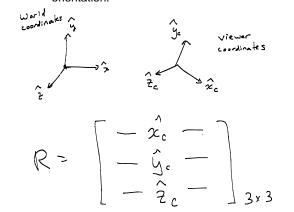
What is the relationship between the world coordinate system and the viewer's coordinate system?



To re-map a general scene point (x,y,z) from world coordinates to viewer coordinates, we translate and rotate.

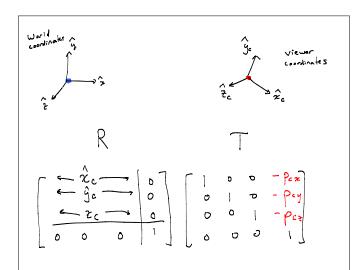
Let the viewer's position be expressed in world coordinates. The matrix T translates the viewer's position to the origin.

R rotates into the viewer's orientation.



Recall slide 7 from lecture 2.

R maps to a new coordinate system by projecting onto new axes.



view transformations:

How do we map from world coordinates to camera/view/eye coordinates?

model transformations:

How do we map from object coordinates to world coordinates?

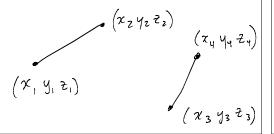
GL_MODELVIEW transformation

How do we map from object (to world) to view coordinates?

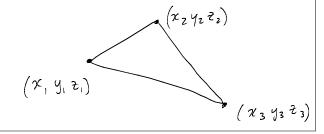
glBegin(GL_LINES) glVertex3f(x1, y1, z1) glVertex3f(x2, y2, z2) glVertex3f(x3, y3, z3) glVertex3f(x4, y4, z4)

// more vertex pairs gives more lines

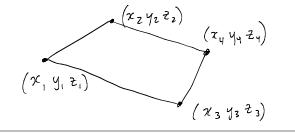
glEnd()



glBegin(GL_TRIANGLES)
glVertex3f(x1, y1, z1)
glVertex3f(x2, y2, z2)
glVertex3f(x3, y3, z3)
// more vertex triples gives more triangles
glEnd()



glBegin(GL_POLYGON)
glVertex3f(x1, y1, z1)
glVertex3f(x2, y2, z2)
glVertex3f(x4, y4, z4)
glVertex3f(x3, y3, z3)
glEnd()



"Quadric" (Quadratic) Surfaces: examples

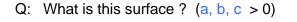
ellipsoid
$$a (x-x_0)^2 + b(y-y_0)^2 + c(z-z_0)^2 = 1$$
Cone
$$a (x-x_0)^2 + b(y-y_0)^2 = c(z-z_0)^2$$
paraboloid
$$0 x = b(y-y_0)^2 + c(z-z_0)^2$$

Quadric Surfaces: General

$$ax^2+by^2+cz^2+dxy+eyz+fxz+gx+hy+iz+j=0$$

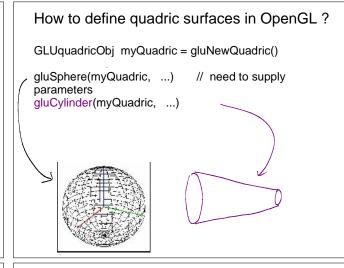
$$\begin{bmatrix} x & y & z & 1 \end{bmatrix} \qquad Q \qquad \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} = 0$$

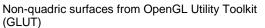
Recall homogeneous coordinates. Same quadric surface is represented if we scale 4D vector by a constant.



$$\begin{bmatrix}
R T \begin{pmatrix} x \\ y \\ \frac{7}{2} \end{pmatrix} & T \begin{bmatrix} a & 6 & 0 & 0 \\ 0 & b & 0 & 0 \\ 0 & 0 & c & 0 \\ 0 & 0 & 0 & -1 \end{bmatrix}
R T \begin{pmatrix} x \\ y \\ \frac{7}{2} \end{pmatrix} = 0$$

A: rotated and translated ellipsoid.





glutSolidCube() glutWireCube()





glutSolidTorus() glutWireTorus()





glutSolidTeapot() glutWireTeapot()





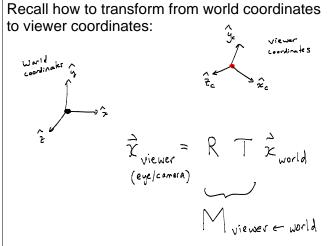
How to transform objects in OpenGL?

 $\begin{array}{lll} \text{glRotatef}(&\text{vx, vy, vz, angle }) \\ \text{glTranslatef}(&\text{x, y, z}) \\ \text{glScalef}(&\text{sx, sy, sz}) \end{array}$

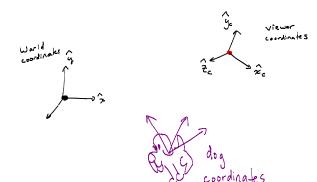
The parameters of each of these calls specify a 4x4 matrix.

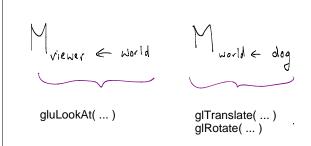
These transformations are not associated with (bound to) any particular object, however.

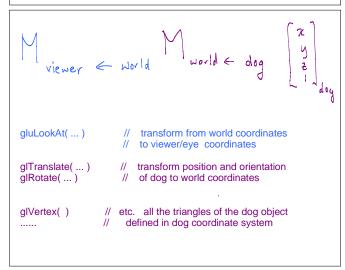
We'll see how this works next.



How to transform from dog (object) coordinates to viewer coordinates?



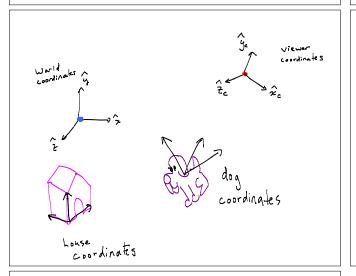






OpenGL is a "state machine". One of its states is the GL_MODELVIEW matrix. This is a 4x4 matrix that transforms a vertex into eye coordinates.

We would like:



Summary of Today

viewer coordinate systems

view transformations : gluLookAt()

model transformations: glRotate(), glTranslate(),

glScale()

GL MODELVIEW transformation

```
glMatrixMode(GL_MODELVIEW) glLoadIdentity()
```

initializes:

ASIDE: How to examine the GL_MODELVIEW matrix ? (python)

```
m = (GLfloat * 16)()
glGetFloatv(GL_MODELVIEW_MATRIX,m)
glModelViewMatrix = [ [ ],[],[],[] ]
for i in range(16):
glModelViewMatrix[i % 4].append(m[i]) # OpenGL stores in column major order
print 'GL_MODELVIEW', glModelViewMatrix
```

<u>Problem:</u> the GL_MODELVIEW matrix only keeps track of one (model to view) transformation. But we may have hundreds of object models.

How do we keep track of all these transformations?

```
Q: What happens when you make these calls?

Gl_MODELVIEW

Answer:

G
```

```
Solution: use a stack of GL_MODELVIEW transformations.

glMatrixMode(GL_MODELVIEW)
glLoadIdentity()
gluLookAt( eye ... , lookat..., up ...)

glPushMatrix()
glTranslate( ...)
glRotate(...)
drawDog()
glPopMatrix()

glPushMatrix()
glTranslate( ...)
glRotate(...)
glRotate(...)
glRotate(...)
drawHouse()
glPopMatrix()
```