

Relative Motion Threshold for Rejection in ICP Registration

François Pomerleau, Francis Colas, François Ferland and François Michaud

Abstract One of the most applied techniques in autonomous robotics for navigation is Simultaneous Localization and Mapping (SLAM). SLAM iteratively builds a map of the environment by putting each new observation in relation with the current map. This relation is usually done by scan matching algorithms such as Iterative Closest Point (ICP) where two sets of features are paired. However as ICP is sensitive to outliers, methods have been proposed to reject them. In this article, we present a new rejection technique called Relative Motion Threshold (RMT). In combination with multiple pairing rejection, RMT identifies outliers based on error produced by paired points instead of a distance measurement, which makes it more applicable to point-to-plane error. The rejection threshold is calculated with a simulated annealing ratio which follows the convergence rate of the algorithm. Experiments demonstrate that RMT performs 20% better than former techniques for outliers created by dynamical obstacles. Those results were achieved without reducing convergence speed of the overall ICP algorithm.

Key words: ICP, kd-tree, registration, scan matching, rejection, robot, SLAM.

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1 Introduction

Simultaneous Localization And Mapping (SLAM) algorithms use a motion model and an observation probabilistic model to incrementally correct positioning problems. The mechanism of transforming different observation models into the same coordinate system is called registration (also known as data association or scan matching). Proposed SLAM solutions based on Maximum Likelihood (ML) present fast capabilities to minimize global positioning errors [7], but it still needs to rely on efficient and robust registration algorithms to be stable in real robotic applications.

Registration can be done using landmarks (e.g., lines, circles, arcs, corners) [1], [16]. When applied to the registration processes, landmarks confer the advantage of accelerating calculation by summing up information. However, landmark registrations can be sensitive to unstructured environments where landmarks are difficult to detect. A second type of registration is called Normal Distribution Transform (NDT). NDT segments spatial information and works on the first and second statistical moments to reduce the computational cost [9] while avoiding to define specific landmarks. However, NDT is still very sensitive to segmentation because large spatial cells filter out relevant details, whereas small cells augment the computational cost.

Another strategy is to directly use point clouds derived from exteroceptive data. One technique to find such matches is known as Iterative Closest Point (ICP) [2]. This method pairs points of both scans by finding for each point of the first scan the nearest point in the other one. From these pairs a motion vector is estimated to cope for their misalignment. This process is iterated until convergence. ICP variants were first developed for applications involving 3D model reconstructions [14], [4], [6],[5], [8]. When used in SLAM by an autonomous robot, these algorithms need to be adapted in several ways: 1) they must work in real-time [11], [3]; 2) they must be adapted to the sensors to be able to use 2D and 3D spatial information [12], and to cope with sensor fusion (range, laser reflectivity [17], color [15], etc.); 3) they must be able to deal with occlusion and partially overlapping scans that frequently arise in a dynamic environment explored by a mobile platform.

This paper addresses the issue of occlusions and partially overlapping scans by using an adaptive rejection technique called Relative Motion Threshold (RMT). For SLAM, changes in the environment and occlusions caused by the motion of the mobile robot are sources of outliers (i.e., points with no match). Fig. 1 presents an example for which an optimal rotation and translation of the blue point cloud (p_i) must be applied to align it with the reference red point cloud (q_j), with i and j being point indexes. Even after a small displacement of the robot between t_1 and t_2 , maps can largely differ due to sensor occlusion. For example, in Fig. 1(b), 50% of the blue points are outliers when compared to the red point cloud. Also, the disambiguation of points obtained from obstacle 1 and obstacle 2 must be resolved to make ICP robust to initial positioning errors and overlapping. Removing outliers from

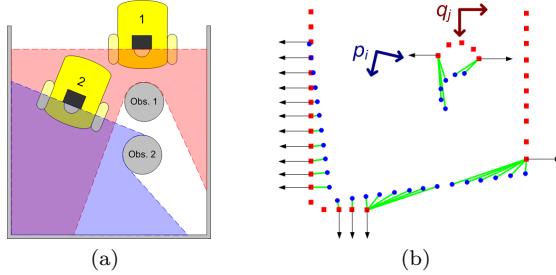


Fig. 1 Map registration example for SLAM, with misalignment caused by odometry error. The green lines represent the alignment error minimized by ICP algorithms. Obs.: Obstacle. (a) Two laser scans taken at time t_1 and t_2 . (b) Point cloud p_i (blue) taken at t_2 is represented in the coordinate system of point cloud q_j (red) taken at t_1 .

the paired points is done during the rejection step of ICP, where it minimizes misalignment errors for the determination of the motion vector between two point clouds.

The paper is organized as follows. Section 2 presents an overview of rejection techniques. Section 3 describes the RMT rejection technique we propose. Section 4 presents experimental results that evaluate performance of each rejection technique in terms of matching and convergence rate of ICP in simulated and real-world applications.

2 Rejection Techniques

Rejection techniques can be categorized as follows:

- *Fix*: Manual setting of the maximum distance d authorized between paired points. Then, all paired points with a distance higher than d are systematically rejected. This method is simple but does not adapt well to different conditions that would require different thresholds.
- *Iterative*: Strategy based on statistical moments of the distribution of the distances between the paired points (*Zhang* method [18]). Four conditions are needed to adapt the threshold d :

$$d = \begin{cases} \mu + 3\sigma, & \text{if } 0 \leq \mu < \eta \\ \mu + 2\sigma, & \text{if } \eta < \mu \leq 3\eta \\ \mu + \sigma, & \text{if } 3\eta < \mu \leq 6\eta \\ \rho, & \text{otherwise} \end{cases} \quad (1)$$

where ρ is a fixed maximal distance. This method can be adjusted to different statistical distributions of the distances but still lacks generality.

- *Mean*: Technique proposed in [5], d starts equal to 20 times the map resolution η for the first iteration, and then uses to $\mu + \sigma$ for each following iteration, where μ and σ are respectively the mean and the standard deviation of the distances between paired points. This method has no parameter, is flexible to different type of outliers. However it filters outliers on the assumption that the distribution of distances is Gaussian, which is not a good assumption in the case of a dynamic environment where several local minima can emerge.
- *Trim*: Overlapping parameter ξ defined by [4] is used to reject a percentage of outliers:

$$N_{\text{trimmed}} = \xi N_{\text{total}} \quad (2)$$

where N is the number of paired points. This approach is less dependent on the shape of the distribution. However, it requires to sort all paired points based on their distances at each iteration, which increases computation time, and can be misleading in case of a large change in the overlap that can occur with a moving platform due to occlusions.

In addition to these techniques, it is also possible to reject multiple pairing to a single point [19], [3], as shown in the lower right part of Figure 1(b) where multiple green lines connect to the same red points. Instead of authorizing all pairs, only the one with the smallest distance is kept. This criterion has been shown to improve the performance of all standard rejection techniques, and thus all results presented here use this additional criterion.

3 Relative Motion Threshold Technique for Rejection

Existing rejection techniques rely mostly on distances between paired points. Those distances have a direct impact on point-to-point error metric but this hypothesis does not hold in the case of point-to-plane error metric (i.e., projecting the distance between matched points on a vector corresponding to the surface orientation of the destination point q_j of Figure 1(b), surface orientation being represented by black arrows). We introduce a new, more general rejection technique called Relative Motion Threshold (RMT). RMT is an adaptive rejection technique that progressively identifies outliers that create most of the error during ICPs iterative process. Adaptation is based directly on errors created by paired points against distances: when multiple points in p_i connect to the same point in q_j , the one with the smallest error on translation components is selected instead of the one with the smallest distance. The maximum authorized error e for iteration t is evaluated by:

$$e_t = \begin{cases} \lambda e_{t-1}, & \text{if } \lambda < 1 \\ e_{t-1}, & \text{otherwise} \end{cases} \quad (3)$$

with λ being a simulated annealing ratio defined by:

$$\lambda = \frac{\|m_{t-1}\|}{\|m_{t-2}\|} \quad (4)$$

This ratio uses past motion information to determine if the point cloud is converging to a local minima, where $\|m\|$ is the Euclidean norm of the motion vector minimizing the alignment error of p_i at iteration t . A ratio smaller than 1 means that the position of p_i is stabilizing. All points with a translation error larger than $e_t + \epsilon$ are identified as outliers and rejected during the iteration t . If the ratio λ is larger than 1, the point cloud p_i is accelerating due to new appearing constraints. The maximum authorized error e_t is then kept stable until the point cloud start to converge again.

The minimum error ϵ is the only parameter needed for our rejection technique. It represents random sensors reading noises. A simple way to evaluate this parameter is to take two scans of a static environment and look at the distribution of translation errors created by the error metric used. This translation error should be centered on zero and can be estimated by a Gaussian distribution. The parameter ϵ can be estimated using the standard deviation of this distribution, making the parameter sensor-dependent instead of situation-dependent.

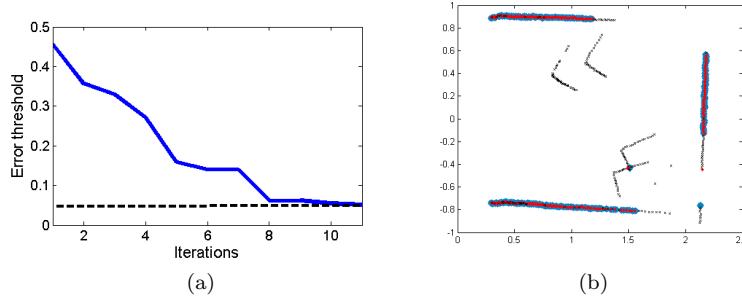


Fig. 2 (a) A generic example of maximal authorized error based on RMT in function of iterations. (b) Final position of the registered point clouds used in the generic example.

Figure 2(a) presents an example of the relative motion threshold in function of iterations. During the two first iterations, only the rejection of multiple pairings is active to initialize a value for m_{t-2} and apply the simulated annealing ratio. e_2 is then initialized to the maximum Euclidean norm on translation error created of all points in p_i . The simulated annealing ratio reduces this error until the point cloud p_i stops to move. The ratio λ is higher than one between iteration 6 and 7, forcing a constant error threshold until the point cloud p_i start converging again. The final threshold error is reduced until iteration 11 where it equals the minimum error ϵ represented by the dashed line. Figure 2(b) shows the two point clouds used in this exam-

ple at iteration 11. The point clouds were taken in a room where two boxes were moved in different directions. The thick points in light blue represent p_i which converge to the right position even with outliers caused by dynamic obstacles (i.e., boxes). Small black cross represent outliers detected by RMT.

4 Experimental Results

Experiments were conducted in simulation and real settings using the following ICP algorithm consisting in five steps [13]:

1. *Selection* reduces the number of points in p_i by selecting a representative subset of points p_s , where $s < i$. This step is a compromise between computation speed and robustness. Even if using a smaller number of points results in faster computation time, the result may diverge if not enough points are used, or if the selection process filters out necessary constraints.
2. *Matching* pairs each point of p_s in the point cloud q_j . This corresponds to a closest point search problem. One data structure often used to solve this problem is the k-d tree. It is a data structure that partitions the space into k dimensions, with the property of accelerating the nearest neighbor search. Recently, utilization of the approximate k-d tree [8] has shown to give faster results without altering ICP precision.
3. *Weighting* improves impacts of pairing point on the error matrix by using criteria such as distance, normal compatibilities and scanner noise. However, results suggest that weighting is data-dependent and does not increase convergence rate significantly [13].
4. *Rejection* uses techniques described in Section 2 and Section 3.
5. *Error and minimization* use all the remaining matched points to evaluate the misalignment error and a create a motion vector $m = [T, \Omega]'$ minimizing this error where T is the translation components and Ω the orientation components. This motion vector is applied to the point cloud q_i . Point-to-plan error function is shown to have a faster convergence rate than point-to-point error [13].

Steps 2 to 5 are repeated until any of the ending condition is reached. Several ending conditions have been proposed, e.g. number of iterations, error, relative motion between two iterations [4], [19], stabilization of mean and standard deviation of distances between paired points, number of registered pairs [5]. Our complete ICP algorithm uses all of those.

4.1 Evaluation method

To test RMT rejection technique while dealing with outliers or occlusion caused by moving objects, we enriched the test protocol described in [10]. More specifically, we recorded data taken by a SICK LMS 200 laser range finder in a U-shaped room. Without moving the sensor, we added or moved boxes in its field of view. This way we generated 10 pairs of different scans with an overlapping ratio around 75%. For each trial, one of the two scans was transformed with a rotation and a translation vector drawn randomly according to Gaussian distributions in order to fit the uncertainty of the localization of standard SLAM techniques. The standard deviations were 0.2 m for each translation component and 0.2 rad for the angle. Figure 3a) shows an example of two scans as well as the distribution of displacement of the second scan. We can see that in the second scan, one of the boxes moved while the other disappeared altogether. As the sensor is fixed between the scans, the result of the registration algorithm is exactly the inverse of this transformation. Figure 3b) shows the results for each rejection techniques. A correct registration is defined by an estimation error or the position of the robot of less than 0.01 m and an error in angle of less than 0.1° . The percentage is computed over 500 trials. For rejection techniques that require the setting of parameters, optimal values were derived by sampling the parameter space and computing the percentage of good registration over a training set. The final performances were evaluated using the remaining configurations. These optimal parameters are presented in Table 1. RMT provides a large improvement over the other rejection techniques, while others tends to easily miscategorize points as outliers and converge towards local minima.

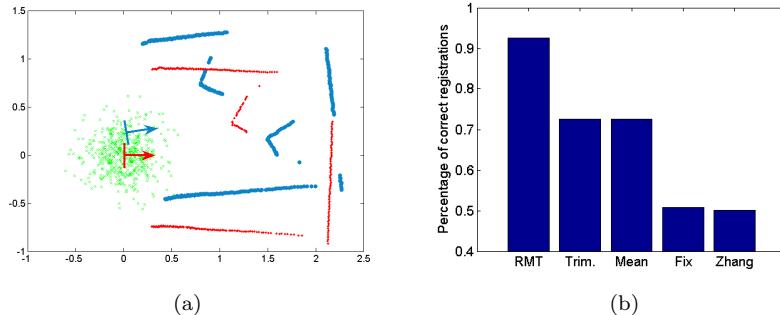


Fig. 3 (a)Two scans to be matched. The first scan is in red, whereas the second scan, after translation and rotation, is in thick blue. The green crosses show the distribution of displacement error used in our test with a standard deviation of 0.2 on x-axis and y-axis. (b) Comparison of the performance of several rejection methods. The performance is measured by the percentage of correct registrations.

	Fix	Zhang	Mean	Trim.	RMT
Parameter	0.3 m	0.02 m	none	76%	0.05

Table 1 Parameters used for each rejection techniques during comparison test.

In terms of speed, ICP is an iterative algorithm known to converge in a small number of iterations. RMT rejection method does not impair the convergence rate of the matching algorithm. The mean and covariance on the number of iterations for the trimmed and RMT are respectively ($\mu = 10.4$, $\sigma = 2.4$) and ($\mu = 9.5$, $\sigma = 3.6$). Those results were obtained keeping registration converging to the right value for 500 trials. No significant differences exist between the all rejection techniques.

Looking at how rejection techniques perform with shifting initial positions, Table 2 presents the correct registration computed for 500 trials of each rejection technique for various standard deviations on the initial error. RMT rejection technique performs better than the others for all conditions. Moreover, an increase in the initial variance decreases the performance for every method, as expected. However, RMT rejection method is more robust as performance loss occurs at a higher variance than with other techniques.

Std	Fix	Zhang	Mean	Trim.	RMT
0.05	50%	69%	78%	75%	100%
0.10	50%	60%	77%	75%	98%
0.20	51%	50%	73%	73%	93%
0.30	58%	48%	62%	65%	75%
0.40	64%	53%	58%	60%	67%

Table 2 Robustness of the rejection techniques with respect to initial error. The performance is measured in percentage of good registration.

4.2 Real-world application

The last section described experiments with outliers mainly due to dynamical obstacles. Another main source of outliers can be created by low overlapping percentage of scans. The Canadian Space Agency (CSA) uses a rotating laser range finder installed on a robot to test Mars exploration algorithms which is showed in figure 4 (a). The robot typically moves few meters on a simulated Martian terrain, takes a 3D scan and decides where to go next. In this kind of application, overlapping between scans can vary between 50% and 90% and few 3D features are available, making the registration very sensible to outliers. The RMT was used on 3D point clouds extract in this context of application. Figure 4 presents the result of one registration with a distance

of 15 meters between the two scans. The grayscale surface correspond to the section used for the registration. The maximum height of the surface is about 1 meter. Points on both side of the surface represent outliers removed during the registration. This demonstrate that the RMT can also deals with outliers created by low overlapping scans. Moreover, the algorithm is currently used by the Space Technologies Research Program of the CSA for complete mapping of the Martian terrain.

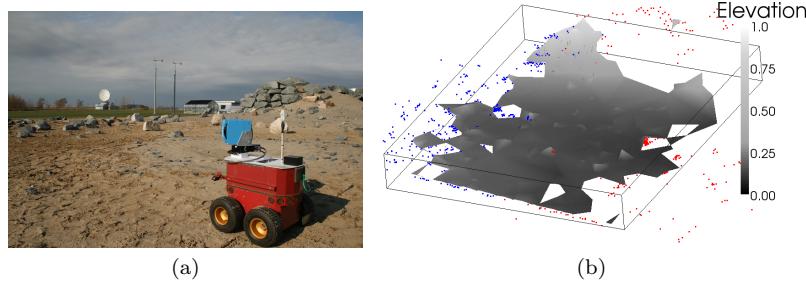


Fig. 4 (a) Robot and environment of the Canadian Space Agency for the Mars exploration project. (b) RMT applied to scans with low overlapping. In grayscale, the surface recovered from match points. In red and blue, the outliers of each scan.

5 Conclusion and Future Work

This paper presents a novel rejection technique called RMT in the context of ICP registration applied to SLAM in mobile robotics. Results show promising performance, making RMT a very interesting alternative to other rejection techniques. In particular, RMT allows better registration in case of larger initial misalignment of the point clouds. RMT demonstrates its applicability in a Mars exploration context with low overlapping percentages. It also presents good results for identifying dynamical obstacles. In future work, we plan to characterize the stability of the approach in a complete SLAM algorithm, and to further extend the range of initial error that ICP can resolve.

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