# The senskernel package. User Manual.

# Introduction

The package **senskernel-1.0** provides the following opportunity for users working at Linux-based computers:

- Calculation of multi-modal surface wave dispersion and eigenfunctions in flat isotropic elastic Earth model consisting of homogeneous layers. Options for sphericity and attenuation corrections are included.
- Calculation of phase velocity sensitivity kernels for the same model.
- Calculation of group velocity sensitivity kernels for the same model.

Package includes three programs: SURF\_PERTURB, PHV\_SENS\_KERNEL ,GRV\_SENS\_KERNEL and C-shell script KERNELS.csh.

The program **SURF\_PERTURB** is based on original R. Herrmann's code [1] with many modifications, introduced by A. Levshin and B. Bukchin. It can be used as a part of package for obtaining dispersion curves, ellipticity, eigenfunctions for the given set of Rayleigh and Love modes and the given set of periods. It also may be used outside of package for the same goals.

The program PHV\_SENS\_KERNEL (written by A. Levshin) can be used as a part of package for obtaining the set of phase-velocity sensitivity kernels for the range of modes and periods using the outputs of SURF\_PERTURB. The theory behind these calculations presented in many books (e.g., Aki and Richards [2], Levshin et al. [3]). It can be used outside this package following the execution of SURF\_PETURB.

The program **GRV\_SENS\_KERNEL** (written by A. Levshin) is used only at this package for obtaining group velocity sensitivity kernels. The computational algorithm is described in Rodi et al.[4].

# 1. SURF\_PERTURB program

#### Command line

SURF PERTURB MODEL PREF rl kmin kmax tmin tmax tstep [-f] [-a] [-s depth step] [-p perturb]

#### **Description**

**SURF\_PERTURB** reads the named input MODEL with radial profile (1-D shear velocities model) of the elastic and nonelastic parameters and computes phase and group velocity dispersion curves and the set of eigenfunctions of the fundamental and higher modes of Rayleigh/Love surface waves. Program includes special algorithm to produce perturbed eigenvalues and eigenfunctions for further sensitivity kernel computation. Program **SURF\_PERTURB** uses argument **PREF** as the prefix to tree output files. In the case of Rayleigh waves, **rl** = R, the names are PREF.R.grv and PREF.R.phv where

PREF.R file consists of complete set of eigenfunctions for all modes and all periods, file

PREF.R.grv consists of group velocity dispersion curves for all modes, and file PREF.R.phv consists of phase velocity dispersion curves for all modes. For Love case,  $\mathbf{rl} = \mathbf{L}$ , output files have the names PREF.L.grv and PREF.L.phv. The files keeps the same types of information computed for Love waves. See more details below in **Input/Output** data sections.

### Parameters and options

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rl - character "R" or "L". Define type of waves: "R" - Rayleigh, "L" - Love kmin - minimal mode number. Modes numbered from 0 by 1. Mode 0 is fundamental kmax - maximal mode number tmin - minimal period, in sec tmax - maximal period, in sec tstep - step by periods, in sec - f apply correction for sphericity - a apply attenuation correction - s depth_step

Define step by depth in eigenfunctions as depth_step, in km. By default depth_step = 1.0 km - p perturb

Insert small perturbation ε= perturb-1.0 into periods as T<sub>pert</sub>=T · perturb. ?

By default perturb = 1.0
```

### Input data

**MODEL file.** The model file is a plain ASCII file given in tabular form. Each line in the file describes single layer of some thickness with constant parameters inside layer. The layers start from free surface downward to the center of the Earth. It is possible to set up the first layer only as the water layer.

The line fields are: h, vp, vs,  $\rho$ , Q

where,

h - layer thickness, (km)
 vp - velocity of P waves, (km/s)
 vs - velocity of S waves, (km/s)
 ρ - density, (g/cm³)
 Q - intrinsic shear Q

An example of model file **eus\_model** is stored under **test1** directory.

NOTE: The last field Q in the MODEL file might be omitted. In this case do not use  $-\mathbf{a}$  option in command line. It leads to wrong results.

Format: informatted

### Output data, Rayleigh case

**PREF.R.phv** file. This plain ASCII file contains in the sequential order **m** phase velocity dispersion curves (**m** = **kmax-kmin+1**) of Rayleigh waves in mode range **kmin÷kmax**. Each dispersion curve is the set of lines ended with two empty lines.

The line fields are: *T*, *Cr*, *Cv* where,

T - period, (s)

*Cr* - phase velocity, (km/s), found as a root of the equation for the boundary conditions at the surface

*Cv* - phase velocity, (km/s), found from integral relations based on variational formulas.

The period range is defined as  $T_i$ =tmin+i×tstep, where i=0, ...,n and n=[(tmax-tmin)/tstep].

**PREF.R.grv file.** This plain ASCII file contains in the sequential order **m** group velocity dispersion curves of Rayleigh waves in mode range **kmax÷kmin**. Each dispersion curve is the set of lines ended with two empty lines.

The line fields are: T, U

where,

T - period, (s)

U - group velocity, (km/s)

The period range is defined as  $T_i$ =tmin+i×tstep, where i=0, ...,n and n=[(tmax-tmin)/tstep].

**PREF.R** file. This plain ASCII file consists of eigenfunctions grouped in m mode-sections.

Mode-sections placed in PREF.R file in increasing mode number order. Each mode-section consists of header – the first line, separator "@", and body – rest of lines. The header is the text line form of "Rayleigh mode **k**"

where, **k** is mode number plus one. The line separator is the text line of 48 characters "@" followed by the space character, namely,

The body includes n+1 eigenfunctions values computed for corresponding eigenvalues  $T_i$ .

Eigenfuctions are divided by separator "(a)", and stored in increasing order by period  $T_i$ .

Each eigenfunction consists of the header – two lines, horizontal component of eigenfuncton, separator "\$", and vertical component. The separator "\$" is the text line of 47 characters "\$" followed by space, namely,

# Header of eigenfunction.

Line 1. The line fields are: T, C, U, k, ampf, ellip, QRapp

Where,

*T* - period, (sec)

C - phase velocity, (km/s)
U - group velocity, (km/s)
k - wavenumber, (km<sup>-1</sup>)

Ampf - ampf= $1/(2*C*U*sumi0)/sqrt(2*\pi)*10^{-15}$ 

Ellip - ratio Vhoriz./Vvert components at the surface

*QRapp* - apparent Rayleigh wave Quality factor for given period

**NOTE:** If option "-a" is absent,  $QRapp = 20{,}000$  by default. If option "-f" is present,  $k = \operatorname{sqrt}((2\pi/CT)^2 - 1/R_0^2)$ , where  $R_0$  is the Earth radius.

Line 2. The line fields are: sumi0, sumi1, sumi2, sumi3, flagr

sumi0- sumi3 - integrals related to the potential and kinetic energy for given period and mode number;

- Lagrangian of this mode, which should be close to 0 if the roots of period equation are found accurately

Horizontal component of eigenfuncton. Each line consists of three field: h, Vhor, dVhordh

Where, h depth, (km)

Vhor - horizontal eigenfunction component, normalized to be ellipticity value at the

surface, nondimensional.

*dVhordh* - derivative of *Vhor* by depth *h*, *dVhor/dh* (km<sup>-1</sup>)

Vertical component of eigenfuncton. Each line consists of three field: h, Vver, dVver/dh

Where,

*h* - depth, (km)

*Vver* - vertical component of eigenfunction normalized to be 1 for h=0

dVverdh - derivative of Vver by h, dVver/dh,  $(km^{-1})$ 

See examples of PREF. R file in test1 directory of distribution set.

# Output data, Love case

The output files PREF.L.phv and PREF.L.grv have the same structure as in Rayleigh case, but contains of phase and group velocity dispersion curves of different modes for Love waves. See examples in **test1** directory of distribution set.

**PREF.L.phv file.** This plain ASCII file consists of eigenfunctions grouped in m mode-sections. Mode-sections placed in PREF.L file in increasing mode number order. Each mode-section consists of header – the first line, separator "@", and body – rest of lines. The header is the text line form of Love mode  $\mathbf{k}$ "

where, **k** is mode number plus one. The line separator is the text line of 41 characters "@" followed by the space character, namely,

The body includes n+1 eigenfunctions computed for corresponding eigenvalues  $T_i$ . Eigenfunctions are devided by separator "@", and stored in increasing order by period  $T_i$ .

Each eigenfunction consists of the header – two lines and eigenfuncton component.

#### Header of eigenfunction.

```
Line 1. The line fields are: T, C, U, k, ampf, QLapp
```

Where,

T - period, (sec)

C - phase velocity, (km/s)
U - group velocity, (km/s)
k - wavenumber, (km<sup>-1</sup>)

Ampf - ampf= $1/(2*C*U*sumi0)/sqrt(2*\pi)*10^{-15}$ 

*OLapp* - apparent Love wave Quality factor for given period

**NOTE:** If option "-a" is absent, QLapp = 20000 by default. If option "-f" is present,  $k = \operatorname{sqrt}((2\pi/CT)^2 - 1/R_0^2)$ , where  $R_0$  is the Earth radius.

Line 2. The line fields are: sumi0, sumi1, sumi2, flagr

sumi0- sumi2 - integrals related to the potential and kinetic energy for given period and mode number;

flagr - Lagrangian of this mode, which should be close to 0 if the roots of period equation

are found accurately

**Eigenfuncton.** Each line consists of three field: h, V, dVdh

Where,

*h* - depth, (km)

V - eigenfunction value, normalized to be 1 at the surface,

dVdh - derivative of V by depth h, dV/dh, (km<sup>-1</sup>)

# 2. PHV\_SENS\_KERNEL program

#### **Command line**

PHV\_SENS\_KERNEL MODEL PREF rl SENS

# **Description**

PHV\_SENS\_KERNEL reads the named input MODEL and files PREF.R, PREF.R.grv, PREF.R.phv (Rayleigh case) or PREF.L, PREF.L.grv, PREF.L.phv (Love case) created by SURF\_PERTURB program and described in the previous section. PHV\_SENS\_KERNEL outputs files with normalized partial derivatives of phase velocity for all requested modes and all requested periods. Each file has name form of SENS.phv.rl\_mode\_period. Arguments rl is the character "R" or "L", it defines the type of wave Rayleigh or Love correspondingly. For example, test.phv.R\_0\_60, test.phv.L\_1\_40.

#### **Output data**

**Rayleigh case**. Each output file has 4 fields: h,  $(\delta C/C)/(\delta b/b)$ ,  $(\delta C/C)/(\delta a/a)$ ,  $(\delta C/C)/(\delta \rho/\rho)$  Where, h is depth, (km), C is phase velocity, a is P velocity, b is S velocity, and  $\rho$  is density. The first line contains additional fields with values of period, T, (s), phase velocity, C (km/s), group velocity, C (km/s), and mode number  $\mathbf{k}$ .

**Love case.** Each output file has 3 fields: h,  $(\delta C/C)/(\delta b/b)$ ,  $(\delta C/C)/(\delta \rho/\rho)$ ,

where h is depth, (km), C is phase velocity, b is S velocity, and  $\rho$  is density. The first line contains additional fields with values of period, T(s), phase velocity, C(km/s), group velocity, U(km/s), and mode number k.

# 3. GRV\_SENS\_KERNEL program

#### **Command line**

GRV SENS KERNEL PREF rl

#### **Description**

This program calculates group velocity sensitivity kernels for the MODEL used in SURF\_PERTURB and PHV\_SENS\_KERNEL. The program uses output files of PHV\_SENS\_KERNEL corresponding to

the given wave type  $\mathbf{rl}$ , mode  $\mathbf{k}$  and period T for three values of *perturb* parameter  $(1-\varepsilon, 1, 1+\varepsilon)$  where  $\varepsilon=0.01$  and creates corresponding files of group velocity sensitivity kernels.

**GRV\_SENS\_KERNEL** outputs files with normalized partial derivatives of group velocity for all requested modes and all requested periods. Each file has name form of **SENS.grv.rl\_mode\_period**. Arguments  $\mathbf{rl}$  is the character "R" or "L", it defines the type of wave Rayleigh or Love correspondingly. For Love case you have to perform everything described above with  $\mathbf{rl} = \mathbf{L}$ . See for more details script **KERNERLS.**csh in bin directory of the distribution set.

# **Output data**

**Rayleigh case**. Each output file has 4 fields: h,  $(\partial U/U)/(\partial b/b)$ ,  $(\partial U/U)/(\partial a/a)$ ,  $(\partial U/U)/(\partial \rho/\rho)$  Where, h is depth, (km), U is group velocity, a is share P velocity, b is shared S velocity, and  $\rho$  is density. The first line contains has additional fields with values of period, T, (s), phase velocity, C, (km/s), group velocity, U, (km/s), and mode number **k**.

**Love case.** Each output file has 3 fields: h,  $(\partial U/U)/(\partial b/b)$ ,  $(\partial U/U)/(\partial \rho/\rho)$ 

Where, h is depth, (km), U is group velocity, b is shared S velocity, and  $\rho$  is density. The first line contains has additional fields with values of period, T, (s), phase velocity, C, (km/s), group velocity, U, (km/s), and mode number  $\mathbf{k}$ .

# 4. KERNELS.csh script

#### **Command line**

KERNELS.sh MODEL PREF rl kmin kmax tmin tmax tstep -s depth\_step -a

### **Description**

**KERNELS**.csh script provides the complete set of program calls to evaluate sensitivity kernels for phase and group velocity curves of Rayleigh/Love surface waves. The meaning of input arguments had been described before in Section 1. Note, that the script deletes some intermediate files. To get full file set of files comment two \rm commands at the end of script.

## References

- [1] R.B. Herrmann, Computer programs in seismology, http://www.eas.slu.edu/eqc/eqccps.html
- [2] Aki, K., Richards P.G., 1980. Quantitative seismology, W. H.Freeman and Co.
- [3] Levshin, A.L., Yanovskaya, T.B., Lander, A.V., Bukchin B.G., Barmin, M.P., Ratnikova L.I., Its E.N., 1989. Seismic Surface Waves in Laterally Inhomogeneous Earth. (Ed. V.I.Keilis-Borok), Kluwer Publ. House, Dordrecht/Boston/ London.
- [4] Rodi, W., Glover, P., Li, T.M.C., Alexander, S.S., 1975. A fast, accurate method for computing group-velocity partial derivatives for Rayleigh and Love waves. Bull. Seismol. Soc. Am. 65 (5), 1105-1114.