

2017-07-25

Signature Inference for Functional Property Discovery

Signature Inference for Functional Property
Discovery
or: How never to come up with tests manually anymore(*)

Tom Sydney Kerckhove
ETH Zurich
<https://cs-syd.eu/>
<https://github.com/NorfairKing>
27 July 2017

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or: How never to come up with tests manually anymore(*)

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27 July 2017

1. The presentation should take about one hour.
2. I have been working on this for the last four and a half months, so if I forget to explain anything, please ask me immediately.

Long term vision: A future in which ...

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└ Long term vision

└ Long term vision: A future in which ...

Long term vision: A future in which ...

1. I am not happy with the state of software today.
2. Maybe I'm just an annoying user, but I find that software very often doesn't work.
3. The reason, I think, is that it is often cheaper to make software that only sort of works, at least in the short term.

Long term vision: A future in which ...

Software works

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- └ Long term vision
 - └ Long term vision: A future in which ...

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Long term vision: A future in which ...

Software works

Long term vision: A future in which ...

Software works because is cheaper to make software that works

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└ Long term vision

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Long term vision: A future in which ...

Software works because is cheaper to make software that works

Long term vision: A future in which ...

Software works because is cheaper to make software that works,
even in the short term.

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└ Long term vision

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Long term vision: A future in which ...

Software works because is cheaper to make software that works,
even in the short term.

Long term goal:

We never come up with tests manually.

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- └ Long term vision
 - └ Long term goal:

1. Spoiler: we are well on our way, and I'm going to show you a significant step in that direction.

Long term goal:

We never come up with tests manually.

Motivation

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└ Motivation

└ Motivation

Motivation

1. So why would we want to not want to come up with tests manually?

Motivation

Writing correct software is hard for humans.

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└ Motivation

└ Motivation

Motivation

Writing correct software is hard for humans.

1. So why would we want to not want to come up with tests manually?



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└ Motivation

└ Idea

Idea



1. Here is an idea:

Motivation

Make machines do it!

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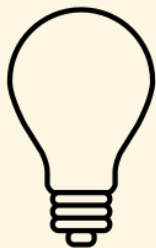
└ Motivation

└ Motivation

Motivation

Make machines do it!

1. It turns out that making machines write software is hard.
2. I read on hacker news: One day we will only have to give the machine a precise description of what we want code to do, and the machine will write it for us.
3. Well, we are already there. This precise description is called the code.



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└ Motivation

└ Idea

Idea



1. Alright, so maybe we cannot make machines write the code. New idea then.

Motivation

I will write the code myself, and get the machine to prove that it is correct.

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└ Motivation

└ Motivation

Motivation

I will write the code myself, and get the machine to prove that it is correct.

1. There are a few problems with this.
2. First of all, you will run into Rice's theorem at some point.
3. Second, you have to already know exactly what it means for your code to be correct.
4. I argue that, in practice, formal methods will not solve the problem that writing correct code is expensive in the short term.

Idea



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- └ Motivation
- └ Idea

Idea



Motivation

I will write the code myself, and get the machine to test that it works.

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└ Motivation

└ Motivation

Motivation

I will write the code myself, and get the machine to test that it works.

1. When formal methods are too expensive, what do we turn to? Testing!

Making machines test that my code works

```
sort
  [4, 1, 6]
  ==
  [1, 4, 6]
```

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- Signature Inference for Functional Property Discovery
 - └ Motivation
 - └ Making machines test that my code works

```
Making machines test that my code works

sort
  [4, 1, 6]
  ==
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Making machines test that my code works

sort

[4, 1, 6]

==

[1, 4, 6]

Top Level Definitions			Alternatives			Expressions		
%	covered / total		%	covered / total		%	covered / total	
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40%	6/15	<div><div></div></div>	-	0/0		100%	38/38	<div><div></div></div>
42%	500/1165	<div><div></div></div>	74%	331/442	<div><div></div></div>	79%	8077/10171	<div><div></div></div>

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└ Motivation

└ Making machines test that my code works

Making machines test that my code works

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Making machines test that my code works

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==

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Fixing the coverage problem

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- └ Motivation
- └ Fixing the coverage problem

Fixing the coverage problem

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Property testing

```
forall
  arbitrary
    $ \ls ->
      isSorted (sort ls)
```

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- Signature Inference for Functional Property Discovery
 - └ Motivation
 - └ Property testing

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Signature Inference for Functional Property Discovery

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Property testing

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forall
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Property testing

```
forAll  
  arbitrary  
    $ \ls ->  
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```



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Signature Inference for Functional Property Discovery

└ Motivation

└ Property testing

Property testing

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forall  
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Fixing the cost problem



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└ Motivation

└ Fixing the cost problem

Fixing the cost problem



Property Discovery

```
forall
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    $ \ls ->
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└ Property Discovery
└ Property Discovery

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Signature Inference for Functional Property Discovery
└ Property Discovery

Property Discovery with QuickSpec

Property Discovery with QuickSpec

Example code

```
module MySort where
```

```
mySort :: Ord a => [a] -> [a]
```

```
mySort [] = []
```

```
mySort (x:xs) = insert (mySort xs)
```

```
  where
```

```
    insert [] = [x]
```

```
    insert (y:ys)
```

```
      | x <= y = x : y : ys
```

```
      | otherwise = y : insert ys
```

```
myIsSorted :: Ord a => [a] -> Bool
```

```
myIsSorted [] = True
```

```
myIsSorted [_] = True
```

```
myIsSorted (x:y:ls) = x <= y && myIsSorted (y : ls)
```

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└ Property Discovery

└ Example code

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Property discovery using QuickSpec

```
== Signature ==
  True  :: Bool
  (<=)  :: Ord a => a -> a -> Bool
  (:)   :: a -> [a] -> [a]
  mySort :: Ord a => [a] -> [a]
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Signature Inference for Functional Property Discovery

└ Property Discovery

└ Property discovery using QuickSpec

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Property discovery using QuickSpec

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```

1. Explain how would you use this
2. Before I go on:
3. This is Really cool!
4. Really good at what it does
5. Great foundation for what comes next

Property discovery using QuickSpec

```
== Signature ==
  True :: Bool
  (<=) :: Ord a => a -> a -> Bool
  (:) :: a -> [a] -> [a]
  mySort :: Ord a => [a] -> [a]
  myIsSorted :: Ord a => [a] -> Bool

== Laws ==
  1. y <= y = True
  2. y <= True = True
  3. True <= x = x
  4. myIsSorted (mySort xs) = True
  5. mySort (mySort xs) = mySort xs
  6. xs <= mySort xs = myIsSorted xs
  7. mySort xs <= xs = True
  8. myIsSorted (y : (y : xs)) = myIsSorted (y : xs)
  9. mySort (y : mySort xs) = mySort (y : xs)
```

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Signature Inference for Functional Property Discovery

└ Property Discovery

└ Property discovery using QuickSpec

Property discovery using QuickSpec

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Signature Inference for Functional Property Discovery

└ Property Discovery

└ Property discovery using QuickSpec

Property discovery using QuickSpec

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```

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QuickSpec Code

```
{-# LANGUAGE ScopedTypeVariables #-}
{-# LANGUAGE ConstraintKinds #-}
{-# LANGUAGE RankNTypes #-}
{-# LANGUAGE FlexibleContexts #-}

module MySortQuickSpec where

import Control.Monad
import MySort
import QuickSpec

main :: IO ()
main =
  void $
    quickSpec
      signature
      { constants =
        [ constant "True" (True :: Bool)
        , constant "<=" (mkDict (<=) :: Dict (Ord A) -> A -> A -> Bool)
        , constant ":" ((:) :: A -> [A] -> [A])
        , constant "mySort" (mkDict mySort :: Dict (Ord A) -> [A] -> [A])
        , constant
            "myIsSorted"
            (mkDict myIsSorted :: Dict (Ord A) -> [A] -> Bool)
        ]
      }

mkDict ::
  (c =>
   a
  -> Dict c
  -> a
  )
mkDict x Dict = x
```

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Signature Inference for Functional Property Discovery

- Property Discovery
- QuickSpec Code

```
QuickSpec Code
{-# LANGUAGE ScopedTypeVariables #-}
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main =
  void $
    quickSpec
      signature
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        [ constant "True" (True :: Bool)
        , constant "<=" (mkDict (<=) :: Dict (Ord A) -> A -> A -> Bool)
        , constant ":" ((:) :: A -> [A] -> [A])
        , constant "mySort" (mkDict mySort :: Dict (Ord A) -> [A] -> [A])
        , constant
            "myIsSorted"
            (mkDict myIsSorted :: Dict (Ord A) -> [A] -> Bool)
        ]
      }

mkDict ::
  (c =>
   a
  -> Dict c
  -> a
  )
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Problems with QuickSpec: Monomorphisation

Only for monomorphic functions

```
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  (mkDict (<) :: Dict (Ord A) -> A -> A -> Bool)
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Signature Inference for Functional Property Discovery

└ Property Discovery

└ Problems with QuickSpec: Monomorphisation

```
Only for monomorphic functions  
constant "<"  
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```

Problems with QuickSpec: Code

Programmer has to write code for all functions of interest
15 lines of subject code.
33 lines of QuickSpec code.

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- Signature Inference for Functional Property Discovery
 - Property Discovery
 - Problems with QuickSpec: Code

Problems with QuickSpec: Code

Programmer has to write code for all functions of interest
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33 lines of QuickSpec code.

Problems with QuickSpec: Speed

Dumb version of the QuickSpec approach:

1. Generate all possible terms
2. Generate all possible equations (tuples) of terms
3. Type check them to make sure the equation makes sense
4. Check that the input can be generated and the output compared for equality
5. Run QuickCheck to see if the equation holds

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Signature Inference for Functional Property Discovery

└ Property Discovery

└ Problems with QuickSpec: Speed

Problems with QuickSpec: Speed

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1. Generate all possible terms
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4. Check that the input can be generated and the output compared for equality
5. Run QuickCheck to see if the equation holds

Pause slide with a joke

```
strictId :: a -> a
strictId !x = x
```

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Signature Inference for Functional Property Discovery

└ Property Discovery

└ Pause slide with a joke

Pause slide with a joke

```
strictId :: a -> a
strictId !x = x
```

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Signature Inference for Functional Property Discovery
└ Property Discovery

Property Discovery with EasySpec

Property Discovery with EasySpec

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Signature Inference for Functional Property Discovery
└ Automation

Step 1: Automation

Step 1: Automation

Signatures

```
{-# LANGUAGE ScopedTypeVariables #-}  
{-# LANGUAGE ConstraintKinds #-}  
{-# LANGUAGE RankNTypes #-}  
{-# LANGUAGE FlexibleContexts #-}
```

```
module MySortQuickSpec where
```

```
import Control.Monad  
import MySort  
import QuickSpec
```

```
main :: IO ()  
main =  
  void $  
    quickSpec  
      signature  
      { constants =  
        [ constant "True" (True :: Bool)  
        , constant "<=" (mkDict (<=) :: Dict (Ord A) -> A -> A -> Bool)  
        , constant ":" ((:) :: A -> [A] -> [A])  
        , constant "mySort" (mkDict mySort :: Dict (Ord A) -> [A] -> [A])  
        , constant  
          "myIsSorted"  
          (mkDict myIsSorted :: Dict (Ord A) -> [A] -> Bool)  
        ]  
      }
```

```
mkDict ::  
  (c =>  
   a)  
  -> Dict c  
  -> a  
mkDict x Dict = x
```

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Signature Inference for Functional Property Discovery

- Automation
- Signatures

```
Signatures  
  
{-# LANGUAGE ScopedTypeVariables #-}  
{-# LANGUAGE ConstraintKinds #-}  
{-# LANGUAGE RankNTypes #-}  
{-# LANGUAGE FlexibleContexts #-}  
  
module MySortQuickSpec where  
  
import Control.Monad  
import MySort  
import QuickSpec  
  
main :: IO ()  
main =  
  void $  
    quickSpec  
      signature  
      { constants =  
        [ constant "True" (True :: Bool)  
        , constant "<=" (mkDict (<=) :: Dict (Ord A) -> A -> A -> Bool)  
        , constant ":" ((:) :: A -> [A] -> [A])  
        , constant "mySort" (mkDict mySort :: Dict (Ord A) -> [A] -> [A])  
        , constant  
          "myIsSorted"  
          (mkDict myIsSorted :: Dict (Ord A) -> [A] -> Bool)  
        ]  
      }
```

Signatures

```
{-# LANGUAGE ScopedTypeVariables #-}  
{-# LANGUAGE ConstraintKinds #-}  
{-# LANGUAGE RankNTypes #-}  
{-# LANGUAGE FlexibleContexts #-}
```

```
module MySortQuickSpec where
```

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import Control.Monad  
import MySort  
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main :: IO ()  
main =  
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    quickSpec  
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      { constants =  
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        , constant ":" ((:) :: A -> [A] -> [A])  
        , constant "mySort" (mkDict mySort :: Dict (Ord A) -> [A] -> [A])  
        , constant  
          "myIsSorted"  
          (mkDict myIsSorted :: Dict (Ord A) -> [A] -> Bool)  
        ]  
      }
```

```
mkDict ::  
  (c =>  
   a)  
  -> Dict c  
  -> a  
mkDict x Dict = x
```

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Signature Inference for Functional Property Discovery

- Automation
- Signatures

```
Signatures  
{-# LANGUAGE ScopedTypeVariables #-}  
{-# LANGUAGE ConstraintKinds #-}  
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module MySortQuickSpec where  
  
import Control.Monad  
import MySort  
import QuickSpec  
  
main :: IO ()  
main =  
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    quickSpec  
      signature  
      { constants =  
        [ constant "True" (True :: Bool)  
        , constant "<=" (mkDict (<=) :: Dict (Ord A) -> A -> A -> Bool)  
        , constant ":" ((:) :: A -> [A] -> [A])  
        , constant "mySort" (mkDict mySort :: Dict (Ord A) -> [A] -> [A])  
        , constant  
          "myIsSorted"  
          (mkDict myIsSorted :: Dict (Ord A) -> [A] -> Bool)  
        ]  
      }
```

A QuickSpec Signature

```
data Signature =  
  Signature {  
    constants      :: [Constant],  
    instances      :: [[Instance]],  
    [...]          :: [...],  
    background     :: [Prop],  
    [...]          :: [...],  
  }  
  
quickSpec :: Signature -> IO Signature
```

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Signature Inference for Functional Property Discovery

└ Automation

└ A QuickSpec Signature

A QuickSpec Signature

```
data Signature =  
  Signature {  
    constants      :: [Constant],  
    instances      :: [[Instance]],  
    [...]          :: [...],  
    background     :: [Prop],  
    [...]          :: [...],  
  }  
  
quickSpec :: Signature -> IO Signature
```

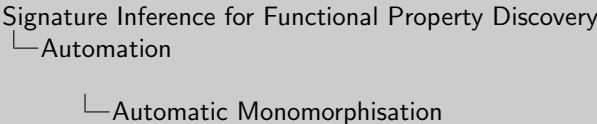
Automatic Monomorphisation

```
filter :: (a -> Bool) -> [a] -> [a]
```

becomes

```
filter :: (A -> Bool) -> [A] -> [A]
```

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```
filter :: (a -> Bool) -> [a] -> [a]
      becomes
filter :: (A -> Bool) -> [A] -> [A]
```


Automatic Monomorphisation

```
filter :: (a -> Bool) -> [a] -> [a]
```

becomes

```
filter :: (A -> Bool) -> [A] -> [A]
```

```
sort :: Ord a => [a] -> [a]
```

becomes

```
sort :: Dict (Ord A) -> [A] -> [A]
```

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Signature Inference for Functional Property Discovery

└ Automation

└ Automatic Monomorphisation

Automatic Monomorphisation

```
filter :: (a -> Bool) -> [a] -> [a]
```

becomes

```
filter :: (A -> Bool) -> [A] -> [A]
```

```
sort :: Ord a => [a] -> [a]
```

becomes

```
sort :: Dict (Ord A) -> [A] -> [A]
```

Signature Expression Generation

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- Signature Inference for Functional Property Discovery
 - Automation
 - Signature Expression Generation

Signature Expression Generation

```
sort :: Ord a => [a] -> [a]
```

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- Signature Inference for Functional Property Discovery
 - Automation
 - Signature Expression Generation

Signature Expression Generation

sort :: Ord a => [a] -> [a]

Signature Expression Generation

```
sort :: Ord a => [a] -> [a]
sort :: Dict (Ord A) => [A] -> [A]
```

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Signature Inference for Functional Property Discovery

- Automation
 - Signature Expression Generation

Signature Expression Generation

```
sort :: Ord a => [a] -> [a]
sort :: Dict (Ord A) => [A] -> [A]
```

Signature Expression Generation

```
sort :: Ord a => [a] -> [a]

sort :: Dict (Ord A) => [A] -> [A]

constant "sort"
  (mkDict sort :: Dict (Ord A) -> [A] -> [A])
```

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Signature Inference for Functional Property Discovery

└ Automation

└ Signature Expression Generation

Signature Expression Generation

```
sort :: Ord a => [a] -> [a]
sort :: Dict (Ord A) => [A] -> [A]
constant "sort"
  (mkDict sort :: Dict (Ord A) -> [A] -> [A])
```

Signature Expression Generation

```
sort :: Ord a => [a] -> [a]

sort :: Dict (Ord A) => [A] -> [A]

constant "sort"
  (mkDict sort :: Dict (Ord A) -> [A] -> [A])

signature { constants = [...] }
```

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Signature Inference for Functional Property Discovery

└ Automation

└ Signature Expression Generation

Signature Expression Generation

```
sort :: Ord a => [a] -> [a]
sort :: Dict (Ord A) => [A] -> [A]
constant "sort"
  (mkDict sort :: Dict (Ord A) -> [A] -> [A])
signature { constants = [...] }
```

Current situation

```
$ cat Reverse.hs
```

```
{-# LANGUAGE NoImplicitPrelude #-}
```

```
module Reverse where
```

```
import Data.List (reverse, sort)
```

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Signature Inference for Functional Property Discovery

└ Automation

└ Current situation

Current situation

```
$ cat Reverse.hs
{-# LANGUAGE NoImplicitPrelude #-}

module Reverse where

import Data.List (reverse, sort)
```

Current situation

```
$ cat Reverse.hs
```

```
{-# LANGUAGE NoImplicitPrelude #-}
```

```
module Reverse where
```

```
import Data.List (reverse, sort)
```

```
$ easyspec discover Reverse.hs
```

```
reverse (reverse xs) = xs
```

```
sort (reverse xs) = sort xs
```

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Signature Inference for Functional Property Discovery

└ Automation

└ Current situation

Current situation

```
$ cat Reverse.hs
{-# LANGUAGE NoImplicitPrelude #-}

module Reverse where

import Data.List (reverse, sort)

$ easyspec discover Reverse.hs
reverse (reverse xs) = xs
sort (reverse xs) = sort xs
```


Pause slide with a joke

```
safePerformIO :: IO a -> IO a
safePerformIO ioa = ioa >>= return
```

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Signature Inference for Functional Property Discovery

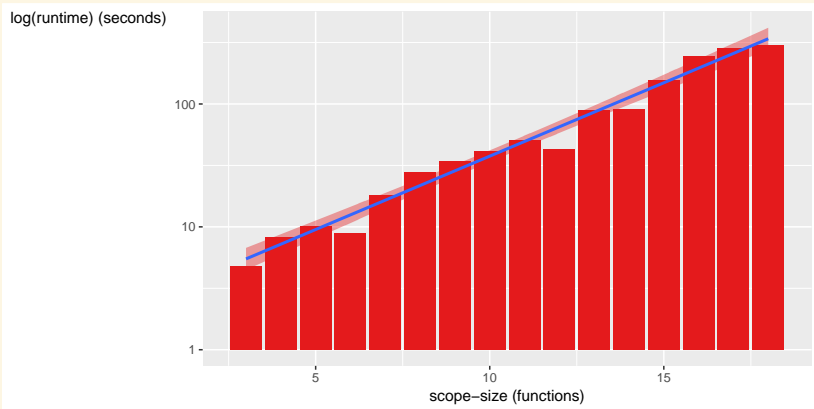
└ Automation

└ Pause slide with a joke

Pause slide with a joke

```
safePerformIO :: IO a -> IO a
safePerformIO ioa = ioa >>= return
```

Automated, but still slow



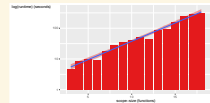
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Signature Inference for Functional Property Discovery

└ Signature Inference

└ Automated, but still slow

Automated, but still slow



1. Now we have automated QuickSpec, but it still slow

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Definitions

Definitions: Property

Example:

```
reverse (reverse ls) = ls
```

Short for:

```
(\ls -> reverse (reverse ls)) = (\ls -> ls)
```

In general:

```
(f :: A -> B) = (g :: A -> B)
```

for some A and B with

```
instance Arbitrary A
```

```
instance Eq B
```

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Signature Inference for Functional Property Discovery

└ Signature Inference

└ Definitions: Property

Definitions: Property

Example:

```
reverse (reverse ls) = ls
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Short for:

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```

In general:

```
(f :: A -> B) = (g :: A -> B)
```

for some A and B with

```
instance Arbitrary A
```

```
instance Eq B
```

Definitions: Size of property

Example:

```
xs <= mySort xs = myIsSorted xs
```

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- Signature Inference for Functional Property Discovery
 - Signature Inference
 - Definitions: Size of property

Definitions: Size of property

Example:
xs <= mySort xs = myIsSorted xs

Definitions: Size of property

Example:

```
xs <= mySort xs = myIsSorted xs
```

Size: 4

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- Signature Inference for Functional Property Discovery
 - Signature Inference
 - Definitions: Size of property

Definitions: Size of property

Example:
xs <= mySort xs = myIsSorted xs
Size: 4

Definitions: Size of property

Example:

```
xs <= mySort xs = myIsSorted xs
```

Size: 4

In general: It's complicated

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- Signature Inference for Functional Property Discovery
 - Signature Inference
 - Definitions: Size of property

Definitions: Size of property

Example:
xs <= mySort xs = myIsSorted xs
Size: 4

In general: It's complicated

Definitions: Property of a function

Functions:

$f = (*\ 2)$

$g = (*\ 3)$

$z = 0$

Properties of f :

$f\ (g\ x) = g\ (f\ x)$

$f\ z = z$

Not properties of f :

$g\ z = z$

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Signature Inference for Functional Property Discovery

└ Signature Inference

└ Definitions: Property of a function

Definitions: Property of a function

Functions:

$f = (*\ 2)$

$g = (*\ 3)$

$z = 0$

Properties of f :

$f\ (g\ x) = g\ (f\ x)$

$f\ z = z$

Not properties of f :

$g\ z = z$

Definitions: Relevant function

Functions:

$f = (*\ 2)$

$g = (*\ 3)$

$z = 0$

$h = \text{id}$

Properties:

$f\ (g\ x) = g\ (f\ x)$

$f\ z = z$

$g\ z = z$

$h\ x = x$

g and z are relevant to f but h is not.

relevant property = property of focus function

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Signature Inference for Functional Property Discovery

└ Signature Inference

└ Definitions: Relevant function

Definitions: Relevant function

Functions:

$f = (*\ 2)$

$g = (*\ 3)$

$z = 0$

$h = \text{id}$

Properties:

$f\ (g\ x) = g\ (f\ x)$

$f\ z = z$

$g\ z = z$

$h\ x = x$

g and z are relevant to f but h is not.

relevant property = property of focus function

Definitions: Scope

Scope: Functions in scope

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- Signature Inference for Functional Property Discovery
 - Signature Inference
 - Definitions: Scope

Definitions: Scope

Scope: Functions in scope

Definitions: Scope

Scope: Functions in scope

Size of scope: Number of functions in scope

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Signature Inference for Functional Property Discovery
└ Signature Inference
└ Definitions: Scope

Definitions: Scope

Scope: Functions in scope

Size of scope: Number of functions in scope

Definitions: Scope

Scope: Functions in scope

Size of scope: Number of functions in scope

Size of signature: Number of functions in signature

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Signature Inference for Functional Property Discovery
└ Signature Inference
└ Definitions: Scope

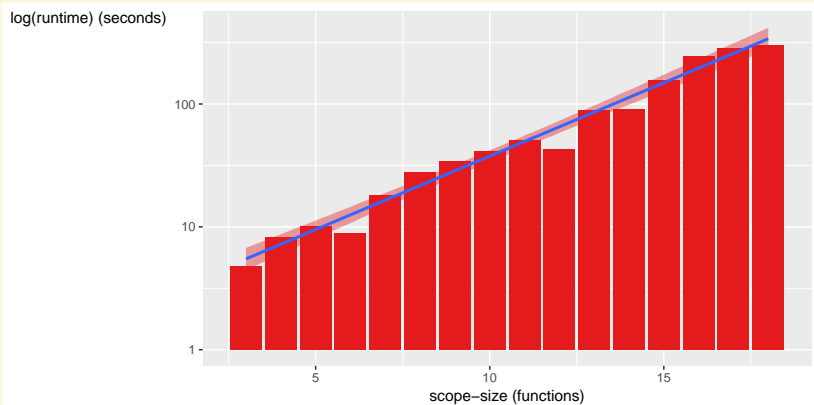
Definitions: Scope

Scope: Functions in scope

Size of scope: Number of functions in scope

Size of signature: Number of functions in signature

Automated, but still slow



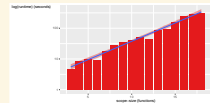
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Signature Inference for Functional Property Discovery

└ Signature Inference

└ Automated, but still slow

Automated, but still slow



1. We set out to find eighty percent of the properties in twenty percent of the time.
2. Of course, later we realised that even twenty percent does not change the time complexity and therefore is too slow in practice.

Why is this slow?

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Signature Inference for Functional Property Discovery

└ Signature Inference

└ Why is this slow?

Why is this slow?

1. Maximum size of the discovered properties

- 1. Maximum size of the discovered properties

Why is this slow?

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Signature Inference for Functional Property Discovery

└ Signature Inference

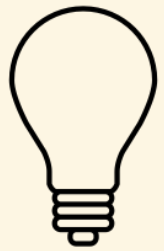
└ Why is this slow?

Why is this slow?

- 1. Maximum size of the discovered properties
- 2. Size of the signature

- 1. Maximum size of the discovered properties
- 2. Size of the signature

Idea



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Signature Inference for Functional Property Discovery
└ Signature Inference
└ Idea

Idea



Critical insight

We are not interested in the entire codebase.

We are interested in a relatively small amount of code.

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- Signature Inference for Functional Property Discovery
 - Signature Inference
 - Critical insight

1. This means that we have an entirely different goal than QuickSpec
2. Comparisons with QuickSpec are not really fair, but we have nothing else to compare to

Critical insight

We are not interested in the entire codebase.
We are interested in a relatively small amount of code.

Reducing the size of the signature

```
inferSignature
  :: [Function] -- Focus functions
  -> [Function] -- Functions in scope
  -> [Function] -- Chosen functions
```

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Signature Inference for Functional Property Discovery

└ Signature Inference

└ Reducing the size of the signature

Reducing the size of the signature

```
inferSignature
  :: [Function] -- Focus functions
  -> [Function] -- Functions in scope
  -> [Function] -- Chosen functions
```

Full background and empty background

```
inferFullBackground _ scope = scope
inferEmptyBackground focus _ = focus
```

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Signature Inference for Functional Property Discovery

└─ Signature Inference

└─ Full background and empty background

Full background and empty background

inferFullBackground _ scope = scope

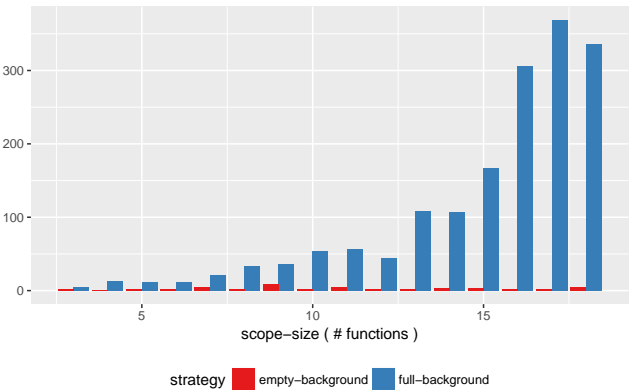
inferEmptyBackground focus _ = focus

Full background and empty background

`inferFullBackground _ scope = scope`

`inferEmptyBackground focus _ = focus`

runtime (time seconds)



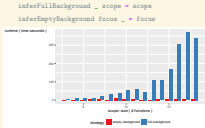
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Signature Inference for Functional Property Discovery

Signature Inference

Full background and empty background

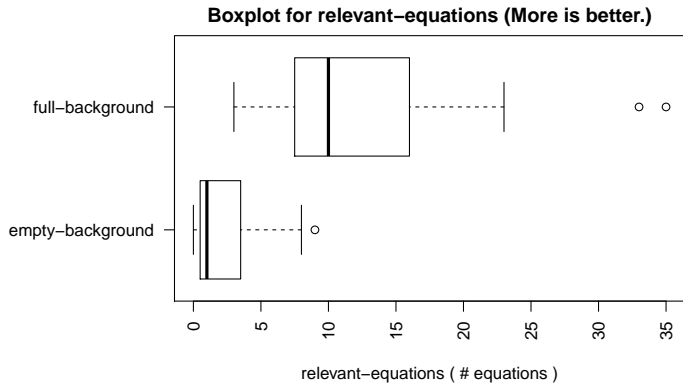
Full background and empty background



Full background and empty background

```
inferFullBackground _ scope = scope
```

```
inferEmptyBackground focus _ = focus
```



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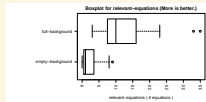
Signature Inference for Functional Property Discovery

└ Signature Inference

└ Full background and empty background

Full background and empty background

```
inferFullBackground _ scope = scope  
inferEmptyBackground focus _ = focus
```



Pause slide with a joke

```
safeCoerce :: a ~ b => a -> b
safeCoerce x = x
```

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Signature Inference for Functional Property Discovery

- Signature Inference

- Pause slide with a joke

Pause slide with a joke

```
safeCoerce :: a ~ b => a -> b
safeCoerce x = x
```

Syntactic similarity: Name

```
inferSyntacticSimilarityName [focus] scope
  = take 5 $ sortOn
    (\sf ->
      hammingDistance
        (name focus) (name sf))
    scope
```

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Signature Inference for Functional Property Discovery

└ Signature Inference

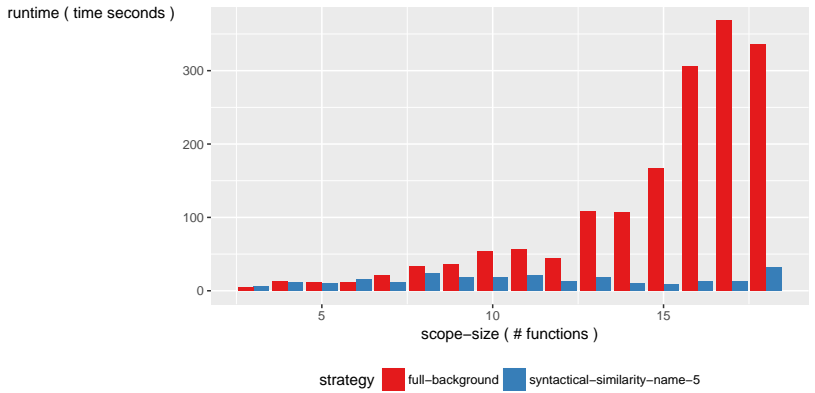
└ Syntactic similarity: Name

Syntactic similarity: Name

```
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```

Syntactic similarity: Name

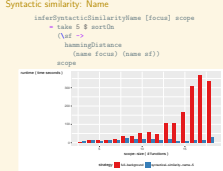
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  (\sf ->
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  scope
```



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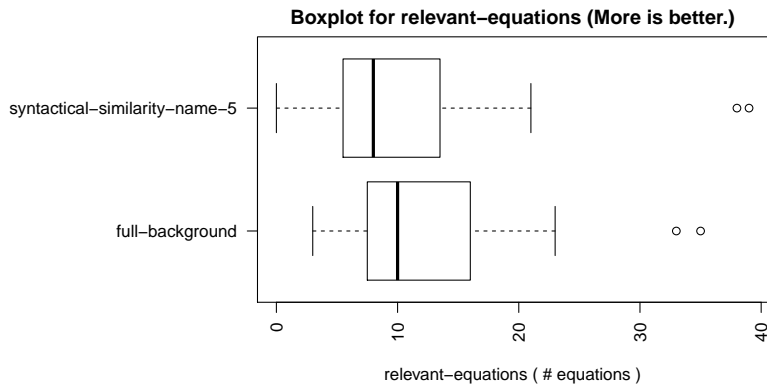
Signature Inference for Functional Property Discovery

- Signature Inference
 - Syntactic similarity: Name



Syntactic similarity: Name

```
inferSyntacticSimilarityName [focus] scope  
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```



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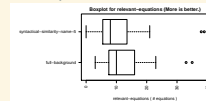
Signature Inference for Functional Property Discovery

└ Signature Inference

└ Syntactic similarity: Name

Syntactic similarity: Name

```
inferSyntacticSimilarityName [focus] scope  
  = take 5 $ sortOn  
    (\sf ->  
      hammingDistance  
        (name focus) (name sf))  
    scope
```



Syntactic similarity: Implementation

```
inferSyntacticSimilaritySymbols i [focus] scope
  = take i $ sortOn
    (\sf ->
      hammingDistance
        (symbols focus) (symbols sf))
    scope
```

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Signature Inference for Functional Property Discovery

└ Signature Inference

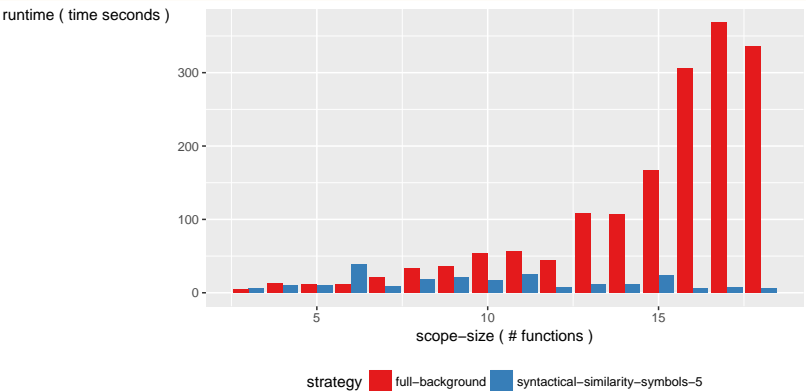
└ Syntactic similarity: Implementation

Syntactic similarity: Implementation

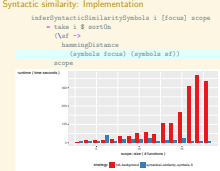
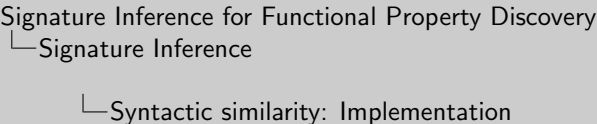
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inferSyntacticSimilaritySymbols i [focus] scope
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    scope
```

Syntactic similarity: Implementation

```
inferSyntacticSimilaritySymbols i [focus] scope
= take i $ sortOn
  (\sf ->
    hammingDistance
      (symbols focus) (symbols sf))
  scope
```

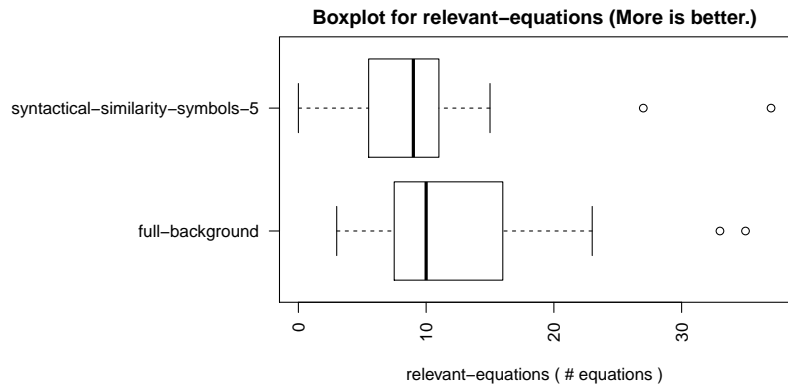


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Syntactic similarity: Implementation

```
inferSyntacticSimilaritySymbols i [focus] scope
= take i $ sortOn
  (\sf ->
    hammingDistance
      (symbols focus) (symbols sf))
  scope
```



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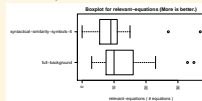
Signature Inference for Functional Property Discovery

└ Signature Inference

└ Syntactic similarity: Implementation

Syntactic similarity: Implementation

```
inferSyntacticSimilaritySymbols i [focus] scope
= take i $ sortOn
  (\sf ->
    hammingDistance
      (symbols focus) (symbols sf))
  scope
```



Syntactic similarity: Type

```
inferSyntacticSimilarityType i [focus] scope
  = take i $ sortOn
    (\sf ->
      hammingDistance
        (getTypeParts focus) (getTypeParts sf))
    scope
```

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Signature Inference for Functional Property Discovery

└ Signature Inference

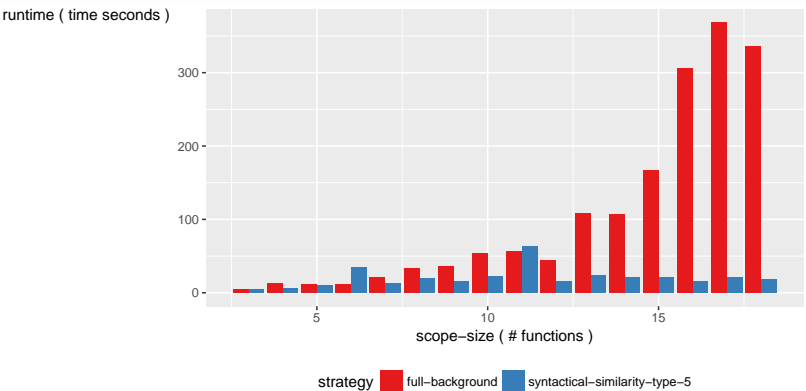
└ Syntactic similarity: Type

Syntactic similarity: Type

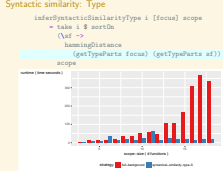
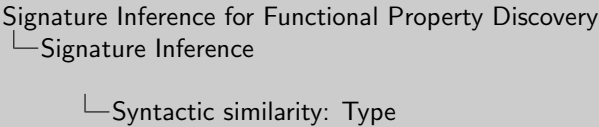
```
inferSyntacticSimilarityType i [focus] scope
  = take i $ sortOn
    (\sf ->
      hammingDistance
        (getTypeParts focus) (getTypeParts sf))
    scope
```

Syntactic similarity: Type

```
inferSyntacticSimilarityType i [focus] scope
= take i $ sortOn
  (\sf ->
    hammingDistance
      (getTypeParts focus) (getTypeParts sf))
  scope
```

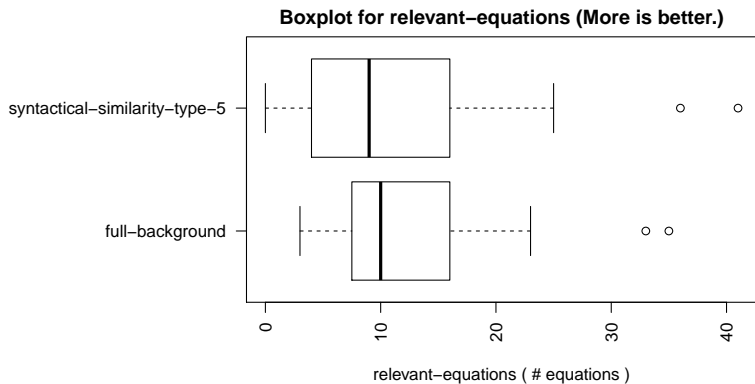


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Syntactic similarity: Type

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inferSyntacticSimilarityType i [focus] scope
= take i $ sortOn
  (\sf ->
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      (getTypeParts focus) (getTypeParts sf))
  scope
```



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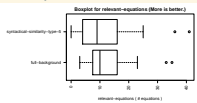
Signature Inference for Functional Property Discovery

└ Signature Inference

└ Syntactic similarity: Type

Syntactic similarity: Type

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      (getTypeParts focus) (getTypeParts sf))
  scope
```



Other things we tried

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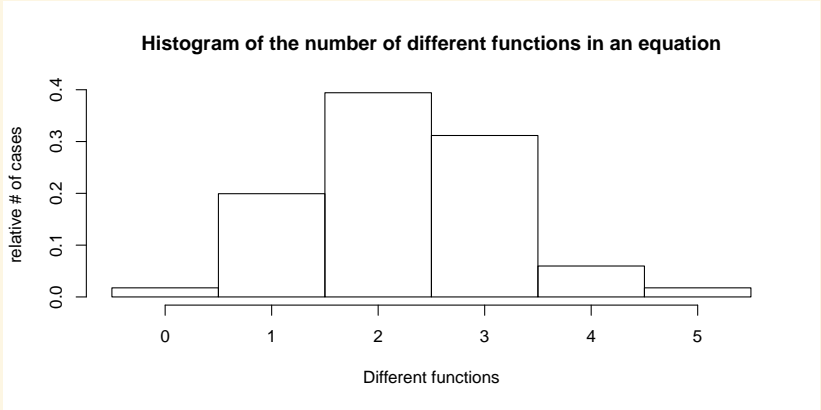
└ Signature Inference

└ Other things we tried

- Other things we tried
- 1. Similarity using a different metric: edit distance
 - 2. Unions of the previous strategies

- 1. Similarity using a different metric: edit distance
- 2. Unions of the previous strategies

Breakthrough

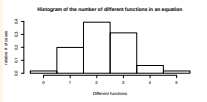


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Signature Inference for Functional Property Discovery

- Signature Inference
 - Breakthrough

Breakthrough



Idea



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- Signature Inference for Functional Property Discovery
 - Signature Inference
 - Idea

Idea



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Signature Inference for Functional Property Discovery

└ Signature Inference

We can run QuickSpec more than
once!

We can run QuickSpec more than
once!

Inferred Signature

```
type SignatureInferenceStrategy
  = [Function] -> [Function] -> InferredSignature
```

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Signature Inference for Functional Property Discovery

- Signature Inference
 - Inferred Signature

```
Inferred Signature

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Inferred Signature

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type SignatureInferenceStrategy
  = [Function] -> [Function] -> InferredSignature
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Combine the results of multiple runs:

```
type InferredSignature = [Signature]
```

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Signature Inference for Functional Property Discovery

└ Signature Inference

└ Inferred Signature

Inferred Signature

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Combine the results of multiple runs:

```
type InferredSignature = [Signature]
```

User previous results as background properties:

```
type InferredSignature = Forest Signature
```

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Signature Inference for Functional Property Discovery

└ Signature Inference

└ Inferred Signature

Inferred Signature

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```

User previous results as background properties:

```
type InferredSignature = Forest Signature
```

Share previous runs:

```
type InferredSignature = DAG Signature
```

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Signature Inference for Functional Property Discovery

└ Signature Inference

└ Inferred Signature

Inferred Signature

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Combine the results of multiple runs:
type InferredSignature = [Signature]

User previous results as background properties:
type InferredSignature = Forest Signature

Share previous runs:
type InferredSignature = DAG Signature
```

Chunks

```
chunks :: SignatureInferenceStrategy
```

```
> chunks
> [sort :: Ord a => [a] -> [a]]
> [reverse :: [a] -> [a], id :: a -> a]

[sort, reverse]
  |
  v
-> [sort]
  |
  |
[sort, id]
```

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Signature Inference for Functional Property Discovery

└ Signature Inference

└ Chunks

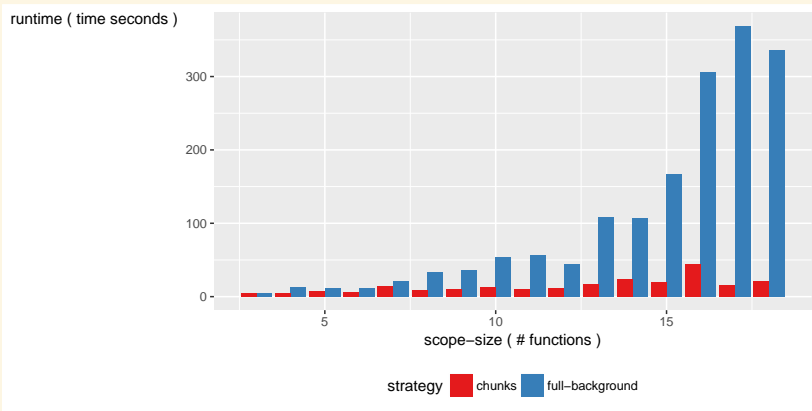
Chunks

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  |
  |
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```


The runtime of chunks



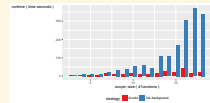
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Signature Inference for Functional Property Discovery

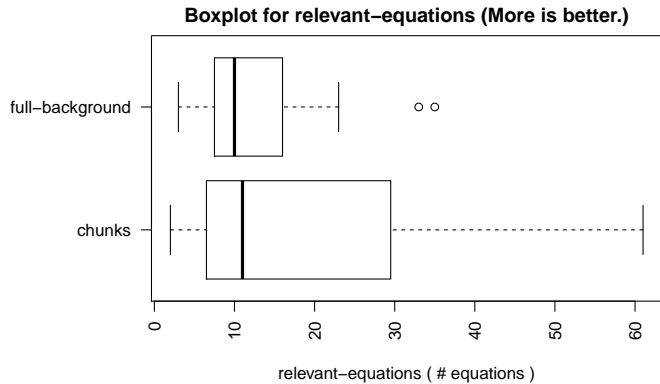
└ Signature Inference

└ The runtime of chunks

The runtime of chunks



The outcome of chunks: Relevant equations



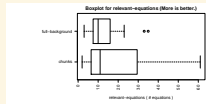
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Signature Inference for Functional Property Discovery

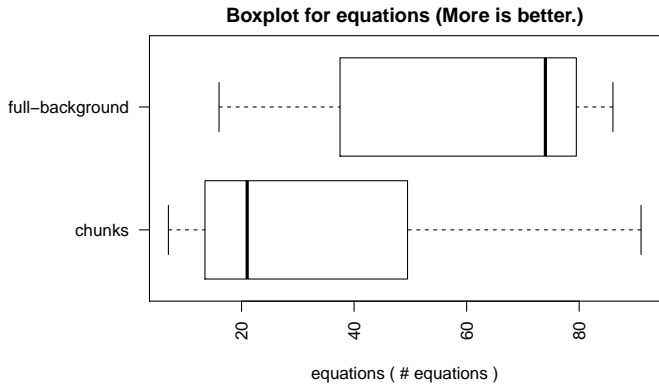
└ Signature Inference

└ The outcome of chunks: Relevant equations

The outcome of chunks: Relevant equations



Why does chunks find more relevant equations?



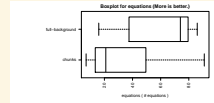
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Signature Inference for Functional Property Discovery

└ Signature Inference

└ Why does chunks find more relevant equations?

Why does chunks find more relevant equations?



Why does chunks find more relevant equations?

Scope:

- i = (+ 1)
- j = (+ 2)
- k = (+ 3)
- l = (+ 4)
- m = (+ 5)
- n = (+ 6)
- o = (+ 7)
- p = (+ 8)
- q = (+ 9)
- r = (+ 10)

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Signature Inference for Functional Property Discovery

└ Signature Inference

└ Why does chunks find more relevant equations?

Why does chunks find more relevant equations?

```
Signature
i = (+ 1)
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m = (+ 5)
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o = (+ 7)
p = (+ 8)
q = (+ 9)
r = (+ 10)

Full background:

i (i x) = j x
i (j x) = k x
i (k x) = l x
i (l x) = m x
i (m x) = n x
i (n x) = o x
i (o x) = p x
i (p x) = q x
i (q x) = r x

Relevant to r:

i (q x) = r x

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Signature Inference for Functional Property Discovery

└ Signature Inference

└ Why does chunks find more relevant equations?

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Scope

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i (o x) = p x
i (p x) = q x
i (q x) = r x

Relevant to r:

i (q x) = r x

Chunks for r:

q (i x) = r x
q (q x) = p (r x)
q (q (q x)) = o (r (r x))
q (q (q (q (q x)))) = m (r (r (r (r x))))
q (q (q (q (q (q x))))) = l (r (r (r (r (r x)))))

All relevant

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Signature Inference for Functional Property Discovery

Signature Inference

Why does chunks find more relevant equations?

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Scope

i = (+ 1)
j = (+ 2)
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Full background

i (i x) = j x
i (j x) = k x
i (k x) = l x
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i (n x) = o x
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i (p x) = q x
i (q x) = r x

Chunks for r

q (i x) = r x
q (q x) = p (r x)
q (q (q x)) = o (r (r x))
q (q (q (q (q x)))) = m (r (r (r (r x))))
q (q (q (q (q (q x))))) = l (r (r (r (r (r x)))))

All relevant

i (q x) = r x

Inferred Signature

```
type SignatureInferenceStrategy  
  = [Function] -> [Function] -> InferredSignature
```

```
type InferredSignature =  
  DAG ([[Signature, [Equation]]] -> Signature)
```

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Signature Inference for Functional Property Discovery

└ Signature Inference

└ Inferred Signature

Inferred Signature

```
type SignatureInferenceStrategy  
  = [Function] -> [Function] -> InferredSignature
```

```
type InferredSignature =  
  DAG ([[Signature, [Equation]]] -> Signature)
```

Inferred Signature

```
type SignatureInferenceStrategy
  = [Function] -> [Function] -> InferM ()
```

```
data InferM a where
  InferPure  :: a -> InferM a
  InferFmap  :: (a -> b) -> InferM a -> InferM b
  InferApp   :: InferM (a -> b) -> InferM a -> InferM b
  InferBind  :: InferM a -> (a -> InferM b) -> InferM b
```

```
InferFrom
  :: [EasyNamedExp]
  -> [OptiToken]
  -> InferM (OptiToken, [EasyEq])
```

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Signature Inference for Functional Property Discovery

└ Signature Inference

└ Inferred Signature

Inferred Signature

```
type SignatureInferenceStrategy
  = [Function] -> [Function] -> InferM ()

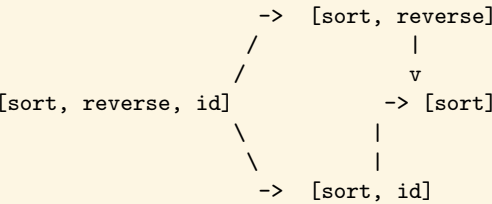
data InferM a where
  InferPure  :: a -> InferM a
  InferFmap  :: (a -> b) -> InferM a -> InferM b
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  InferBind  :: InferM a -> (a -> InferM b) -> InferM b

  InferFrom
    :: [EasyNamedExp]
    -> [OptiToken]
    -> InferM (OptiToken, [EasyEq])
```


Chunks Plus

chunksPlus :: SignatureInferenceStrategy

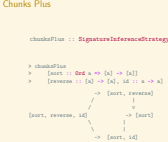
```
> chunksPlus
> [sort :: Ord a => [a] -> [a]]
> [reverse :: [a] -> [a], id :: a -> a]
```



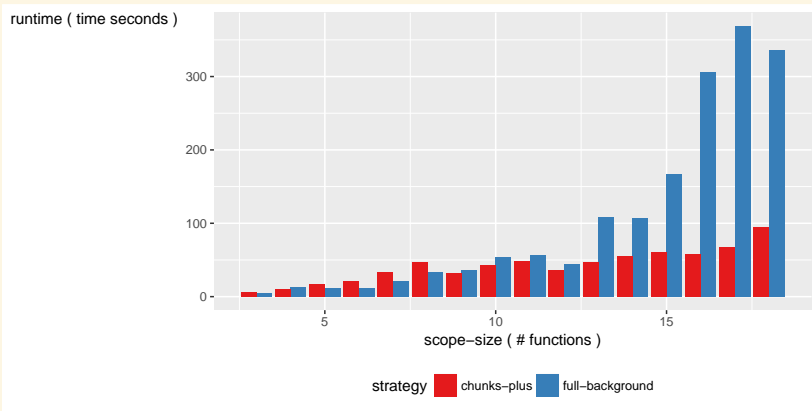
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Signature Inference for Functional Property Discovery

- Signature Inference
 - Chunks Plus



The runtime of chunks plus



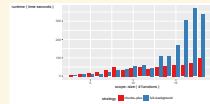
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Signature Inference for Functional Property Discovery

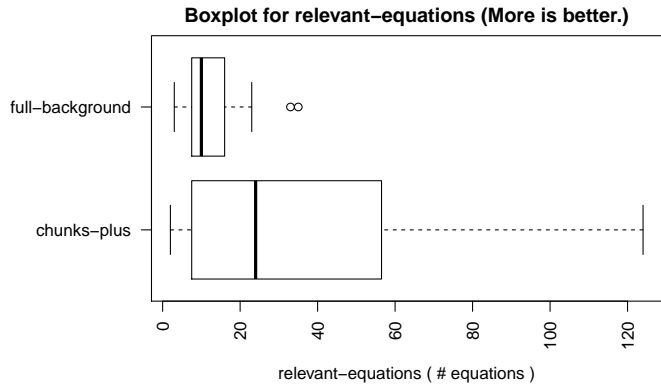
└ Signature Inference

└ The runtime of chunks plus

The runtime of chunks plus



The outcome of chunks plus: Relevant equations



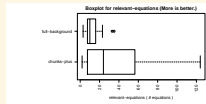
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Signature Inference for Functional Property Discovery

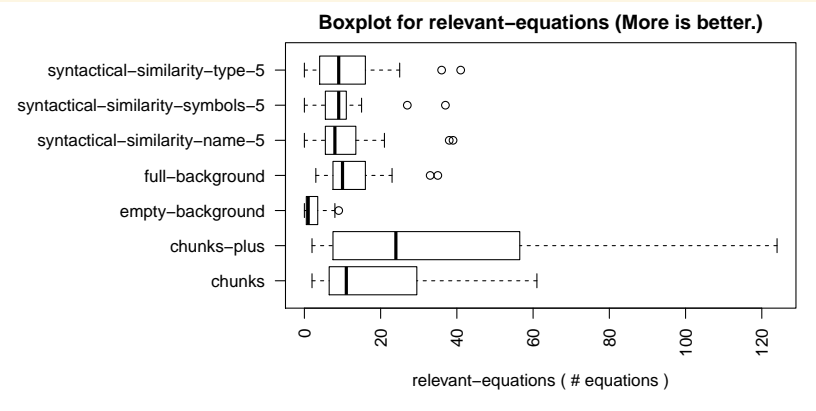
└ Signature Inference

└ The outcome of chunks plus: Relevant equations

The outcome of chunks plus: Relevant equations



All strategies

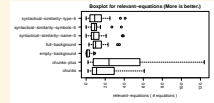


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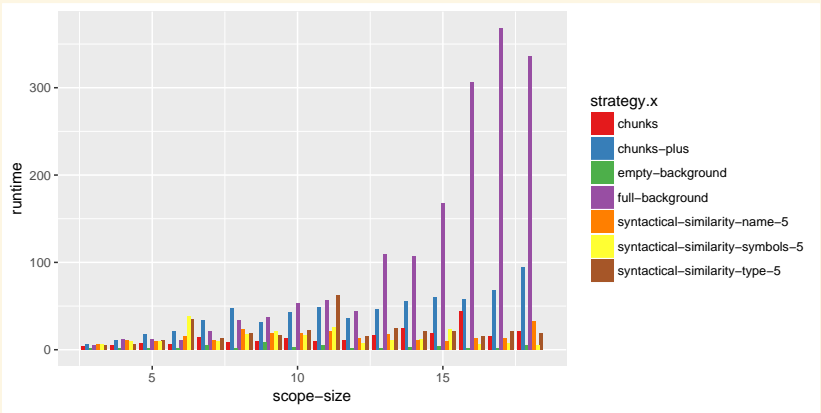
Signature Inference for Functional Property Discovery

- Signature Inference
- All strategies

All strategies



All strategies



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Signature Inference for Functional Property Discovery

- Signature Inference
- All strategies



```
$ time stack exec easyspec \  
  -- discover MySort.hs MySort.mySort
```

```
xs <= mySort xs = myIsSorted xs  
mySort xs <= xs = True  
myIsSorted (mySort xs) = True  
mySort (mySort xs) = mySort xs
```

```
3.61s user 1.14s system 193% cpu 2.450 total
```

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Signature Inference for Functional Property Discovery

└ Signature Inference

└ Neat

Neat

```
$ time stack exec easyspec \  
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```

Great promise, but ...

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- Signature Inference for Functional Property Discovery
 - Signature Inference
 - Great promise, but ...

Great promise, but ...

Great promise, but ...

- 1. Only works for functions in scope of which the type is in scope too.

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- Signature Inference for Functional Property Discovery
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1. Only works for functions in scope of which the type is in scope too.

Great promise, but ...

- 1. Only works for functions in scope of which the type is in scope too.
- 2. Crashes on partial functions.

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Signature Inference for Functional Property Discovery

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Great promise, but ...

1. Only works for functions in scope of which the type is in scope too.
2. Crashes on partial functions.
3. Only works with built in instances.

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Signature Inference for Functional Property Discovery

└ Signature Inference

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Great promise, but ...

1. Only works for functions in scope of which the type is in scope too.
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3. Only works with built in instances.
4. Data has to have an *Arbitrary* instance in scope.

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Signature Inference for Functional Property Discovery

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Signature Inference for Functional Property Discovery

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Signature Inference for Functional Property Discovery

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All technical problems, not theoretical problems!

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Signature Inference for Functional Property Discovery

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Further Research

- 1. Can we go faster?

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- Signature Inference for Functional Property Discovery
 - Signature Inference
 - Further Research

- Further Research
 - 1. Can we go faster?

Further Research

2017-07-25

Signature Inference for Functional Property Discovery

└ Signature Inference

└ Further Research

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- 1. Can we go faster?
 - 2. Which constants do we choose for built in types?

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Further Research

- 1. Can we go faster?
- 2. Which constants do we choose for built in types?
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- Signature Inference for Functional Property Discovery
 - Signature Inference
 - Further Research

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Further Research

- 1. Can we go faster?
- 2. Which constants do we choose for built in types?
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- 4. Relative importance of equations

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- Signature Inference for Functional Property Discovery
 - Signature Inference
 - Further Research

Further Research

- 1. Can we go faster?
- 2. Which constants do we choose for built in types?
- 3. Can we apply this to effectful code?
- 4. Relative importance of equations

Call to action

Proofs of concept:

`https://github.com/nick8325/quickcheck`

`https://github.com/nick8325/quickspec`

`https://github.com/NorfairKing/easyspec`

Now we need to make it production ready!

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Signature Inference for Functional Property Discovery

└ Signature Inference

└ Call to action

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About Me

Student at ETH
This is my master thesis
Wrote Haskell in open source
Taught Haskell at ETH
Wrote Haskell in industry
Looking for a job!

`https://cs-syd.eu/`
`https://cs-syd.eu/cv`
`https://github.com/NorfairKing`

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Signature Inference for Functional Property Discovery
└ Signature Inference
└ About Me

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