

Handheld VESAD Analysis

March 20, 2018

The analysis of the experiment data is also accessible online:
<https://github.com/NormandErwan/master-thesis-analysis/blob/master/Handled%20VESAD%20Analysis.ipynb>.

1 1. Data preparation

Configuration :

```
In [1]: import numpy as np
import pandas as pd
from pandas.api.types import CategoricalDtype
import itertools

import seaborn as sns
import matplotlib.pyplot as plt
import matplotlib.ticker as ticker
import matplotlib.patches as patches

from scipy import stats
import statsmodels.api as sm
from statsmodels.formula.api import ols
from statsmodels.stats.multicomp import (MultiComparison, pairwise_tukeyhsd)
from statsmodels.stats.multitest import multipletests
from statsmodels.stats.libqsturng import psturng

from ast import literal_eval
from os import listdir
from os.path import join
```

```
C:\Users\Erwan\Miniconda\envs\master-thesis\lib\site-packages\statsmodels\compat\pandas.py:56: FutureWarning:
from pandas.core import datetools
```

```
In [2]: %matplotlib inline

# Style and size of the figures
legend_fontsize = sns.plotting_context('notebook')['axes.labelsize']
legend_title_fontsize = sns.plotting_context('notebook')['axes.titlesize']+1

sns.set(context='notebook', style='whitegrid', font_scale=1.25,\
        rc={'legend.fontsize': legend_fontsize})
subplotsize = (5,4)
```

```

# Render the plots with this language
#language = 'English'
language = 'Français'

```

Data are loaded in the following variables: - Participants information, from the questionnaire before the trials: participants - The summary of the trials of the participants: trials - The detailed measures of the trials: trial_details - The ranks of the participants from the post-questionnaire: ranks

```

In [3]: participants = pd.read_csv('participants.csv')
        trials = pd.read_csv('participant_trials.csv')
        trials_for_anova = pd.read_csv('participant_trials.csv')
        ranks = pd.read_csv('participant_ranks.csv')

```

```

In [4]: # Detailed trials are long to load, keep commented if unused

```

```

#trial_details = []
#for file in listdir('.'):
#    if file.endswith('details.csv'): # The trial files end with *-details.csv
#        details.append(pd.read_csv(file))
#trial_details = pd.concat(details, ignore_index=True)

```

Creates independent variables lists (participants_ivs, trials_ivs) and dependent variables lists (ranks_dvs, trials_dvs) to make easier to use algorithms and to plot figures.

```

In [5]: # Participants IVs
        if language == 'Français':
            participants_iv_labels = ['Numéro participant', 'Sexe', 'Porte des lunettes', \
                                     'Porte des lentilles', 'Est daltonien', \
                                     'Intervalle d\'âge', 'Main dominante', \
                                     'Main utilisée pour la souris', 'Activité principale', \
                                     'Utilisation de l\'ordinateur (heures/jours)', \
                                     'Logiciels 3D utilisés', 'Visiocasques RV/RA utilisés', \
                                     'Techniques d\'interactions RV/RA utilisées']
        else:
            participants_iv_labels = ['Participant Id', 'Sex', 'Has Glasses', \
                                     'Has Contact Lenses', 'Is Color Blind', \
                                     'Age Class', 'Dominant Hand', \
                                     'Hand Used for Mouse', 'Activity', \
                                     'Computer Hours per Day', '3D Softwares Used', \
                                     'HMD Used', 'Known Interactions Techniques on HMD']

        participants_ivs = pd.Series(data=participants_iv_labels, index=participants.columns)

In [6]: # Trials IVs
        if language == 'Français':
            trials_iv_labels = ['Technique', 'Taille du texte', 'Distance', 'Groupe', \
                               'Méthode d\'entrée', 'Méthode d\'affichage']
        else:
            trials_iv_labels = ['Technique', 'Text Size', 'Distance', 'Ordering', \
                               'Technique Input', 'Technique Output']

        trials_ivs = ['technique', 'text_size', 'distance', 'ordering', 'input', 'output']

```

```

    trials_ivs = pd.DataFrame(columns=trials_ivs, index=['label', 'categorical', 'palette'])

    default_palette = sns.color_palette('Set2', 8)

    for iv_index, iv_label in zip(trials_ivs.columns, trials_iv_labels):
        iv_categories = trials.sort_values([iv_index + '_id']).drop_duplicates(iv_index)[iv_index]
        iv_categorical = pd.Categorical(iv_categories, iv_categories, ordered=True)
        trials_ivs[iv_index] = [iv_label, iv_categorical, default_palette]

    trials_ivs.at['palette', 'technique'] = [default_palette[1], default_palette[0], default_palette[2]]
    trials_ivs.at['palette', 'text_size'] = sns.light_palette(default_palette[6], 3)[1:3] # Pink palette
    trials_ivs.at['palette', 'distance'] = sns.light_palette(default_palette[4], 3)[1:3] # Green palette
    trials_ivs.at['palette', 'ordering'] = sns.light_palette(default_palette[3], 4)[1:4] # Brown palette
    trials_ivs.at['palette', 'input'] = [default_palette[5], default_palette[2]]
    trials_ivs.at['palette', 'output'] = [default_palette[0], sns.color_palette('muted')[5]]

In [7]: # Trials DVs
    if language == 'Français':
        trials_dv_labels = ['Temps de complétion (s)', 'Sélections', 'Temps en sélection',\
                             'Distance 3D en sélection', 'Distance en sélection',\
                             'Désélections', 'Erreurs', 'Disques classés', 'Défilements',\
                             'Temps de défilement', 'Distance 3D de défilement',\
                             'Distance de défilement', 'Zooms', 'Temps de zoom', 'Distance 3D de zoom',\
                             'Distance de zoom', 'Mouvements tête-téléphone',\
                             'Distance relative tête-téléphone']
    else:
        trials_dv_labels = ['Task Completion Time (s)', 'Selections', 'Selection Time',\
                             'Selection Distance', 'Selection Distance on Grid',\
                             'Deselections', 'Errors', 'Items Classified', 'Pans', 'Pan Time',\
                             'Pan Distance', 'Pan Distance on Grid',\
                             'Zooms', 'Zoom Time', 'Zoom Distance',\
                             'Zoom Distance on Grid', 'Phone-Head Motion',\
                             'Signed Phone-Head Motion']

    trials_dvs = trials.loc[:, 'total_time':'signed_head_phone_distance'].columns
    trials_dvs = pd.Series(data=trials_dv_labels, index=trials_dvs)

In [8]: # Ranks DVs
    if language == 'Français':
        ranks_dv_labels = ['Facile à comprendre', 'Mentalement facile à utiliser',\
                             'Physiquement facile à utiliser', 'Rapidité', 'Réussite',\
                             'Frustration', 'Préférence']
    else:
        ranks_dv_labels = ['Easy to Understand', 'Mentally Easy to Use',\
                             'Physically Easy to Use', 'Subjective Speed',\
                             'Subjective Performance', 'Frustration', 'Preference']

    ranks_dv_scales = [pd.Categorical(list(range(1,6)), list(range(1,6)), ordered=True)] * len(ranks_dv_labels)
    ranks_dv_palettes = [sns.color_palette('RdYlBu', 5)] * len(ranks_dv_labels)

    ranks_dvs = ranks.loc[:, 'easy_understand':'preference'].columns
    ranks_dvs = pd.DataFrame(data=[ranks_dv_labels, ranks_dv_scales, ranks_dv_palettes],\
                              columns=ranks_dvs, index=['label', 'scale', 'palette'])

```

```
ranks_dvs.at['scale', 'preference'] = pd.Categorical(list(range(1,4)), list(range(1,4)), ordered=True)
ranks_dvs.at['palette', 'preference'] = [sns.color_palette('RdYlBu', 5)[i] for i in range(4,-1,-1)]
```

In [9]: # Shortcuts

```
technique, text_size, distance = trials_ivs['technique'], trials_ivs['text_size'], trials_ivs['distance']
ordering, iv_input, iv_output = trials_ivs['ordering'], trials_ivs['input'], trials_ivs['output']
```

Clean the data:

In [10]: # Set better and translated columns to participants, trials and ranks

```
participants.columns = participants_ivs
```

```
columns = []
for column in trials.columns:
    if (column in participants_ivs.index):
        columns.append(participants_ivs[column])
    elif (column in trials_ivs.columns):
        columns.append(trials_ivs[column]['label'])
    elif (column in trials_dvs.index):
        columns.append(trials_dvs[column])
    else:
        columns.append(column)
```

```
trials.columns = columns
```

```
ranks.columns = [participants_ivs['participant_id'], trials_ivs['ordering']['label'], trials_ivs['distance']['label']]
+ ranks_dvs.loc['label', :].tolist()
```

In [11]: # Set the participant_id column as the index in participants

```
participants.set_index(participants_ivs['participant_id'], inplace=True)
```

In [12]: # Some participants are non valid or don't have complete measures

```
non_valid_participants = [0, 4]
participants = participants[~participants.index.isin(non_valid_participants)]
ranks = ranks[~ranks[participants_ivs['participant_id']].isin(non_valid_participants)]

incomplete_trials_participant_ids = [0, 4]
trials = trials[~trials[participants_ivs['participant_id']].isin(incomplete_trials_participant_ids)]
trials_for_anova = trials_for_anova[~trials_for_anova['participant_id'].isin(incomplete_trials_participant_ids)]
```

In [13]: # Some participants have wrong head phone measures

```
for head_distance_column in ['absolute_head_phone_distance', 'signed_head_phone_distance']:
    trials.loc[trials[trials_dvs[head_distance_column]] == 0, trials_dvs[head_distance_column]] = np.nan
    trials_for_anova.loc[trials_for_anova[head_distance_column] == 0, head_distance_column] = np.nan
```

In [14]: # Setup categorical columns participants, trials and ranks

```
participants[trials_ivs['ordering']['label']] = ranks.groupby(participants_ivs['participant_id']).apply(lambda x: x.technique)
participants[trials_ivs['ordering']['label']] = participants[trials_ivs['ordering']['label']]

for iv_index in trials_ivs.columns:
    iv = trials_ivs[iv_index]
    trials_for_anova[iv_index] = trials[iv['label']] = trials[iv['label']].astype(iv['category'])

ranks[technique['label']] = ranks[technique['label']].astype(technique['category'])
```

```

ranks[ordering['label']] = ranks[ordering['label']].astype(ordering['categorical'])

# Rename categories
if language == 'Français':
    technique['categorical'].categories = ['Téléphone', 'VESAD tactile', 'VESAD']
    text_size['categorical'].categories = ['Grand', 'Petit']
    distance['categorical'].categories = ['Proche', 'Loin']
    ordering['categorical'].categories = ['Groupe 1', 'Groupe 2', 'Groupe 3']
    iv_input['categorical'].categories = ['Tactile', 'Autour du téléphone']
    iv_output['categorical'].categories = ['Téléphone seul', 'Téléphone étendu']
else:
    ordering['categorical'].categories = ['Group 1', 'Group 2', 'Group 3']

# Set renamed categories to data
participants[trials_ivs['ordering']]['label']].cat.categories = ordering['categorical'].categories

for iv_index in trials_ivs.columns:
    iv = trials_ivs[iv_index]
    trials[iv['label']].cat.categories = iv['categorical'].categories

ranks[technique['label']].cat.categories = technique['categorical'].categories
ranks[ordering['label']].cat.categories = ordering['categorical'].categories

```

```

In [15]: # Eval the arrays in some dvs
def eval_if_str(data):
    return literal_eval(data) if isinstance(data, str) else data

trials['grid_config'] = trials['grid_config'].apply(eval_if_str)

```

Utilities:

```

In [16]: labels = pd.Series()

if language == 'Français':
    labels['category'] = 'Catégorie'
    labels['count'] = 'Nombre total'
    labels['distance'] = 'Distance moyenne (m)'
    labels['dv'] = 'Variable dépendante'
    labels['iv'] = 'Variable indépendante'
    labels['iv_value'] = 'Valeur variable indépendante'
    labels['mean_difference'] = 'Différence des moyennes'
    labels['mean_difference_percentage'] = 'Différence des moyennes (%)'
    labels['mean_rank'] = 'Note moyenne'
    labels['preferences'] = ['Premier', 'Deuxième', 'Troisième']
    labels['p_value'] = 'Valeur p'
    labels['question'] = 'Question'
    labels['rank'] = 'Note'
    labels['time'] = 'Temps moyen (s)'
    labels['t_statistic'] = 'Statistique T'
    labels['votes'] = 'Votes'
else:
    labels['category'] = 'Category'
    labels['count'] = 'Count'
    labels['distance'] = 'Mean Distance (m)'

```

```

labels['dv'] = 'Dependent Variable'
labels['iv'] = 'Independent Variable'
labels['iv_value'] = 'Independent Variable Value'
labels['mean_difference'] = 'Mean Difference'
labels['mean_difference_percentage'] = 'Mean Difference Percentage'
labels['mean_rank'] = 'Mean Rank'
labels['preferences'] = ['First', 'Second', 'Third']
labels['p_value'] = 'p-value'
labels['question'] = 'Question'
labels['rank'] = 'Rank'
labels['time'] = 'Mean Time (s)'
labels['t_statistic'] = 'T statistic'
labels['votes'] = 'Votes'

```

```

In [17]: def mask(df, f):
         return df[f(df)]

```

```

pd.DataFrame.mask = mask

```

```

In [18]: def p_values_correction(data, alpha=0.05, correction_method='fdr_bh'):
         if correction_method != None:
             reject, p_values_corrected, a1, a2 = multipletests(data[labels['p_value']].tolist(), alpha=alpha,
                                                                 method=correction_method)
             data[labels['p_value']] = p_values_corrected

```

```

In [19]: def subplots(nsubplots, ncols_max=2, subplotsize=subplotsize, *plt_args):
         ncols = min(ncols_max, nsubplots)
         nrows = ((nsubplots - 1) // ncols) + 1
         fig, axs = plt.subplots(nrows=nrows, ncols=ncols, figsize=(subplotsize[0] * ncols, subplotsize[1]),
                                 *plt_args)

         if nrows == 1 and ncols == 1:
             axs = [axs]
         elif nrows >= 2 and ncols >= 2:
             axs = [ax for ax_row in axs for ax in ax_row]

         for ax in axs[::-1][0:len(axs) - nsubplots]:
             fig.delaxes(ax)

         return (fig, axs)

```

```

In [20]: def fix_legend_fontsize(ax_legend, fontsize=legend_title_fontsize):
         plt.setp(ax_legend.get_title(), fontsize=fontsize)

```

2. Participant ranks

Some functions for the analysis:

```

In [21]: def get_ranks_count(iv_index, dv_index):
         iv, dv = trials_ivs[iv_index], ranks_dvs[dv_index]

         ranks_counts_index = pd.MultiIndex.from_product([iv['categorical'], dv['scale']],
                                                         names=[iv['label'], labels['rank']])

```

```

zero_ranks_counts = pd.Series(0, index=ranks_counts_index) # Zero counts by default
ranks_counts = ranks.groupby([iv['label'], dv['label']]).size() # Gets the counts

ranks_counts = pd.concat([ranks_counts, zero_ranks_counts]) # Merge counts with the default
ranks_counts = ranks_counts[~ranks_counts.index.duplicated(keep='first')] # Keeps the counts
ranks_counts.sort_index(inplace=True)
ranks_counts.index = ranks_counts_index # Restore the index
return ranks_counts

In [22]: def cumulated_barplot(data, palette, **args):
    for row_index, row in data.iloc[:,-1].iterrows():
        sns.barplot(y=data.columns, x=row, label=row_index, color=palette[row_index-1], orient=

In [23]: def plot_ranks_distributions(iv_index, dv_indexes):
    iv = trials_ivs[iv_index]

    fig, axs = subplots(len(dv_indexes))
    for dv_index, ax in zip(dv_indexes, axs):

        dv = ranks_dvs[dv_index]

        cumulated_ranks_count = get_ranks_count(iv_index, dv_index).unstack(level=0).cumsum()
        cumulated_barplot(cumulated_ranks_count, palette=dv['palette'], ax=ax)
        ax.set(xlabel=labels['votes'], xlim=(0, cumulated_ranks_count.max()[0]))
        ax.xaxis.set_major_locator(ticker.MultipleLocator(2)) # Fix the axis ticks

        ax_handles, ax_labels = ax.get_legend_handles_labels()
        legend = ax.legend(ax_handles[:-1], ax_labels[:-1], frameon=True, loc='lower center',
                           bbox_to_anchor=(0.5, 1), mode=None, ncol=len(dv['scale']), title=dv
                           fontsize=legend_fontsize-2)
        fix_legend_fontsize(legend)

    fig.tight_layout(h_pad=4) # Add padding to avoid legend and labels overlap
    return (fig, axs)

In [24]: def plot_ranks(iv_index, dv_indexes):
    iv = trials_ivs[iv_index]

    fig, axs = subplots(len(dv_indexes))
    for dv_index, ax in zip(dv_indexes, axs):
        dv = ranks_dvs[dv_index]

        sns.barplot(x=iv['label'], y=dv['label'], palette=iv['palette'], data=ranks, ax=ax)
        ax.set(ylim=(0, dv['scale'][-1]))
        ax.yaxis.set_major_locator(ticker.MultipleLocator(1)) # Fix the axis ticks

    return (fig, axs)

In [25]: def test_ranks(iv_index, dv_indexes, **args):
    iv = trials_ivs[iv_index]

    results = []
    for dv_index in dv_indexes:
        dv = ranks_dvs[dv_index]

```

```

        samples = [ranks[ranks[iv['label']] == iv_value][dv['label']] for iv_value in iv['catego

        kruskal_H, p_value = stats.kruskal(*samples) # Compare the samples
        results.append([iv['label'], dv['label'], kruskal_H, p_value])

    results = pd.DataFrame(results, columns=[labels['iv'], labels['dv'], 'Kruskal-Wallis H', l
    p_values_correction(results, **args)
    return results

In [26]: def test_pairwise_ranks(iv_index, dv_indexes, **args):
    iv = trials_ivs[iv_index]
    iv_category_ids = range(len(iv['categorical']))

    results = []
    for dv_index in dv_indexes:
        dv = ranks_dvs[dv_index]
        samples = [ranks[ranks[iv['label']] == iv_value][dv['label']] for iv_value in iv['catego

        for iv_value_ids in itertools.combinations(iv_category_ids, 2): # Test each pair
            U, p_value = stats.mannwhitneyu(samples[iv_value_ids[0]], samples[iv_value_ids[1]])
            results.append([iv['label'], iv['categorical'][iv_value_ids[0]], iv['categorical']
                            dv['label'], U, p_value])

    results = pd.DataFrame(results, columns=[labels['iv'], labels['iv_value'] + ' (1)', \
                                            labels['iv_value'] + ' (2)', labels['dv'], \
                                            'Mann-Whitney U', labels['p_value']])

    p_values_correction(results, **args)
    return results

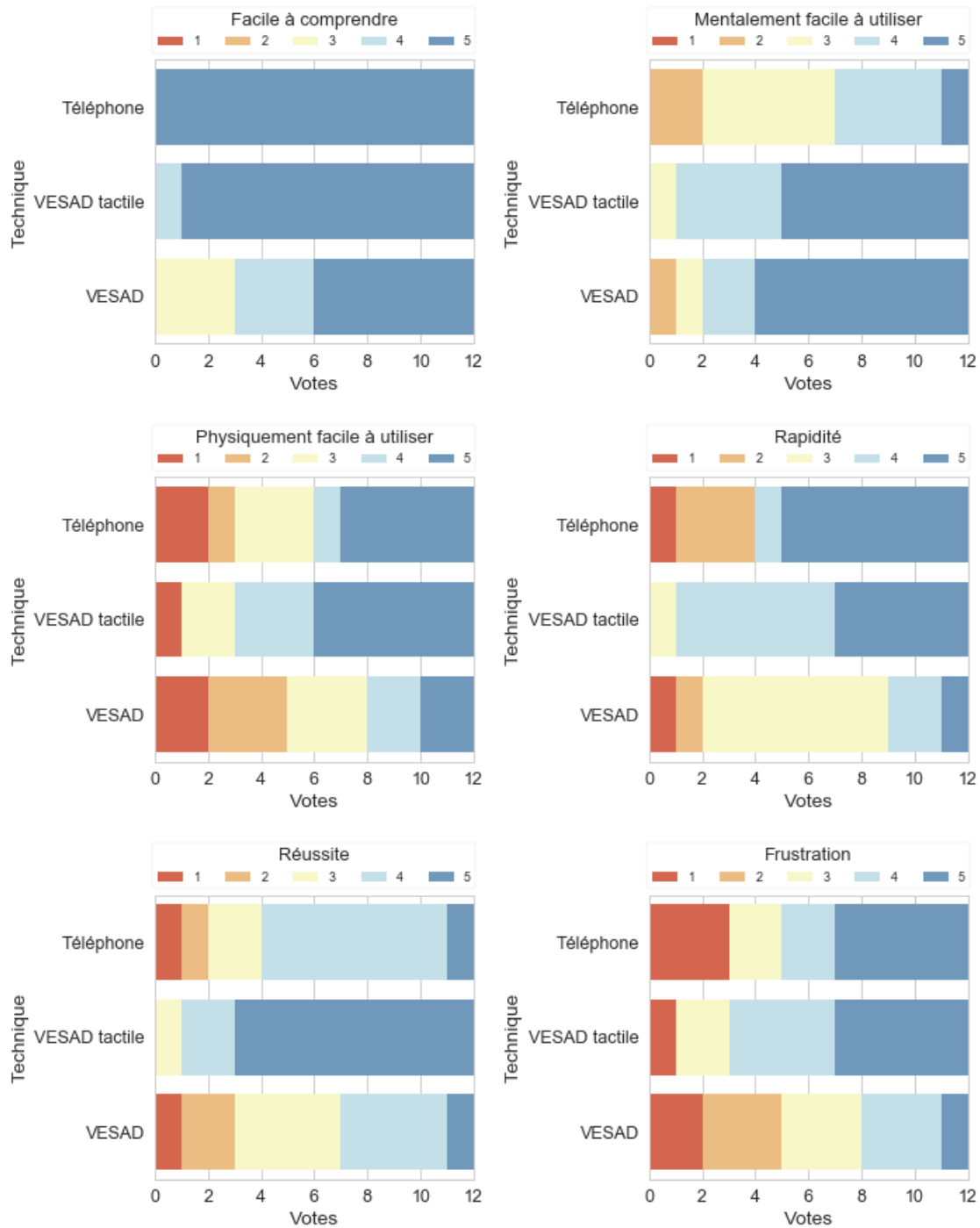
```

Display the note distributions for each question and each technique.

```

In [27]: (fig, axs) = plot_ranks_distributions('technique', ranks_dvs.columns[0:-1])
    fig.savefig('ranks_distributions.png', dpi=300, bbox_inches='tight')

```

We use Kruskal-Wallis test (Benjamini–Hochberg correction) on each question to check if there is significative differences between the ranks among TECHNIQUE:

```
In [28]: test_ranks('technique', ranks_dvs, correction_method='fdr_bh')
```

```
Out[28]:  Variable indépendante      Variable dépendante  Kruskal-Wallis H  \
          0      Technique          Facile à comprendre      11.001420
```

1	Technique	Mentalement facile à utiliser	10.905742
2	Technique	Physiquement facile à utiliser	4.148121
3	Technique	Rapidité	7.130846
4	Technique	Réussite	13.784269
5	Technique	Frustration	4.500057
6	Technique	Préférence	12.638889

	Valeur p
0	0.007497
1	0.007497
2	0.125674
3	0.039599
4	0.006303
5	0.122962
6	0.006303

All the questions, except Physically Easy to Use and Frustration, have significant ranks among TECHNIQUES : Easy to Understand (p=0.0078), Mentally Easy to Use (p=0.0042), Subjective Speed (p=0.025), Subjective Performance (p=0.0018), Preference (p=0.0018).

We use then pairwise Mann-Whitney test (Benjamini–Hochberg correction) for the significant question above:

```
In [29]: test_pairwise_ranks('technique', ['easy_understand', 'mentally_easy_use', 'could_go_fast', \
                                           'subjective_performance', 'preference'], correction_method='')
```

```
Out[29]:  Variable indépendante Valeur variable indépendante (1)  \
0          Technique Téléphone
1          Technique Téléphone
2          Technique VESAD tactile
3          Technique Téléphone
4          Technique Téléphone
5          Technique VESAD tactile
6          Technique Téléphone
7          Technique Téléphone
8          Technique VESAD tactile
9          Technique Téléphone
10         Technique Téléphone
11         Technique VESAD tactile
12         Technique Téléphone
13         Technique Téléphone
14         Technique VESAD tactile

      Valeur variable indépendante (2)      Variable dépendante  \
0          VESAD tactile      Facile à comprendre
1          VESAD      Facile à comprendre
2          VESAD      Facile à comprendre
3          VESAD tactile      Mentalement facile à utiliser
4          VESAD      Mentalement facile à utiliser
5          VESAD      Mentalement facile à utiliser
6          VESAD tactile      Rapidité
7          VESAD      Rapidité
8          VESAD      Rapidité
9          VESAD tactile      Réussite
10         VESAD      Réussite
```

11	VESAD	Réussite
12	VESAD tactile	Préférence
13	VESAD	Préférence
14	VESAD	Préférence

	Mann-Whitney U	Valeur p
0	66.0	0.215732
1	36.0	0.008605
2	40.5	0.020977
3	23.0	0.005031
4	28.5	0.010151
5	69.5	0.475027
6	70.5	0.475027
7	48.5	0.126838
8	21.0	0.004655
9	22.5	0.004655
10	57.0	0.215732
11	17.5	0.003904
12	16.0	0.003904
13	56.0	0.215732
14	32.0	0.013011

Significant results are:

- Easy to Understand : *PhoneOnly* (5.00 ± 0.00) is significantly better than *MidAirInArOut* (4.25 ± 0.83 , $p=0.009$);
- Mentally Easy to Use : *PhoneOnly* (3.33 ± 0.85) is significantly worst than *PhoneInArOut* (4.50 ± 0.65 , $p=0.005$) and *MidAirInArOut* (4.42 ± 0.95 , $p=0.01$);
- Subjective Speed : *PhoneInArOut* (4.33 ± 0.62) is significantly better than *MidAirInArOut* (3.08 ± 0.95 , $p=0.05$);
- Subjective Performance : *PhoneInArOut* (4.67 ± 0.62) is significantly better than *PhoneOnly* (3.50 ± 1.04 , $p=0.005$) and *MidAirInArOut* (3.17 ± 1.07 , $p=0.004$);
- Preference: *PhoneInArOut* (1.33 ± 0.47) is significantly preferred to *PhoneOnly* (2.50 ± 0.65 , $p=0.004$) or *MidAirInArOut* (2.17 ± 0.80 , $p=0.01$).

Display the mean of the ranks with the standard deviation for each question among TECHNIQUE:

```
In [30]: ranks.groupby([trials_ivs['technique']['label']])\
        .aggregate(lambda x : '{:.2f}±{:.2f}'.format(np.mean(x), np.std(x)))\
        .loc[:, ranks_dvs.loc['label', :]]
```

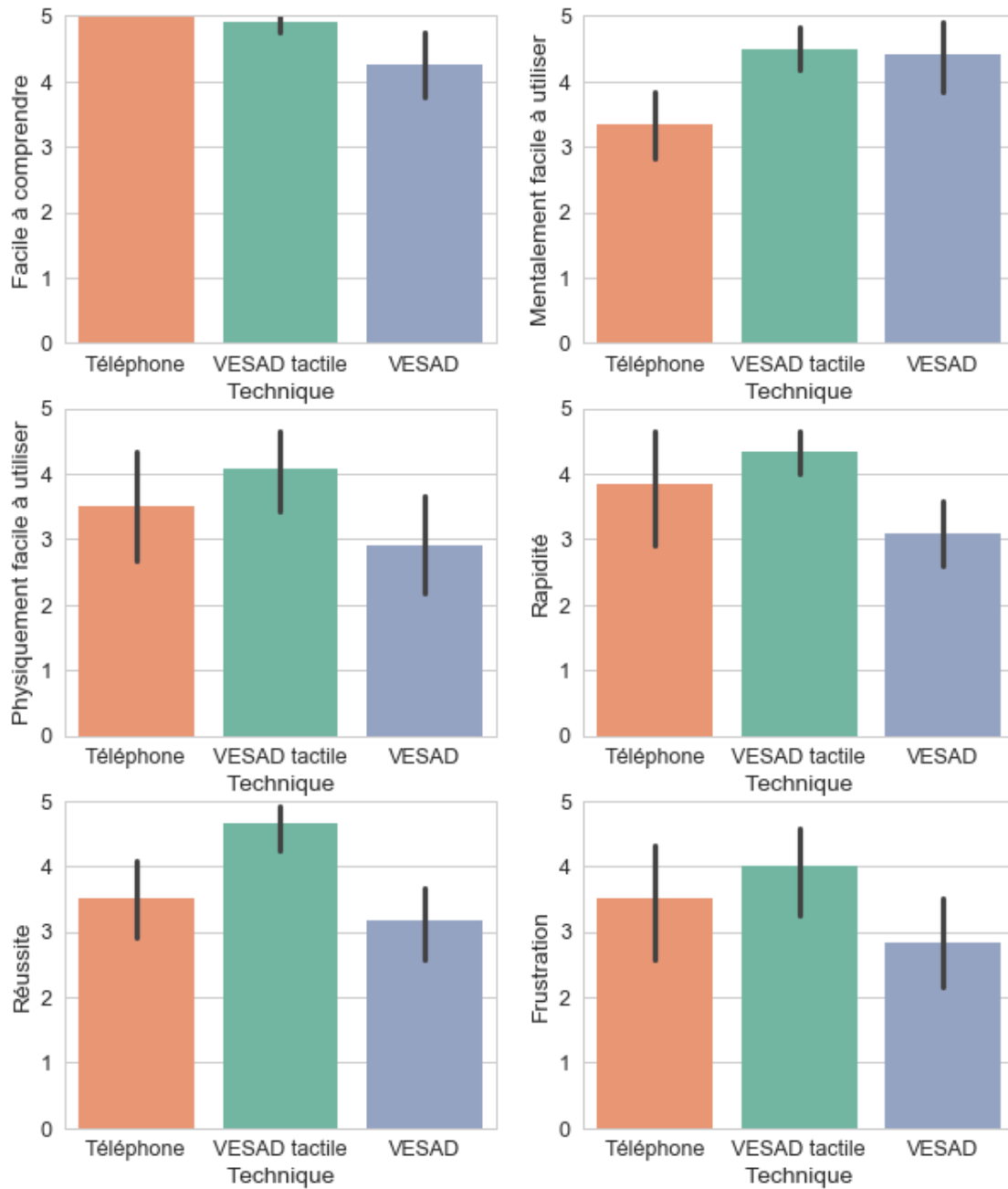
```
Out[30]:
```

	Facile à comprendre	Mentalement facile à utiliser	
Technique			
Téléphone	5.00±0.00	3.33±0.85	
VESAD tactile	4.92±0.28	4.50±0.65	
VESAD	4.25±0.83	4.42±0.95	

	Physiquement facile à utiliser	Rapidité	Réussite	
Technique				
Téléphone	3.50±1.50	3.83±1.52	3.50±1.04	
VESAD tactile	4.08±1.19	4.33±0.62	4.67±0.62	
VESAD	2.92±1.32	3.08±0.95	3.17±1.07	

Frustration Préférence			
Technique			
Téléphone	3.50±1.61	2.50±0.65	
VESAD tactile	4.00±1.15	1.33±0.47	
VESAD	2.83±1.21	2.17±0.80	

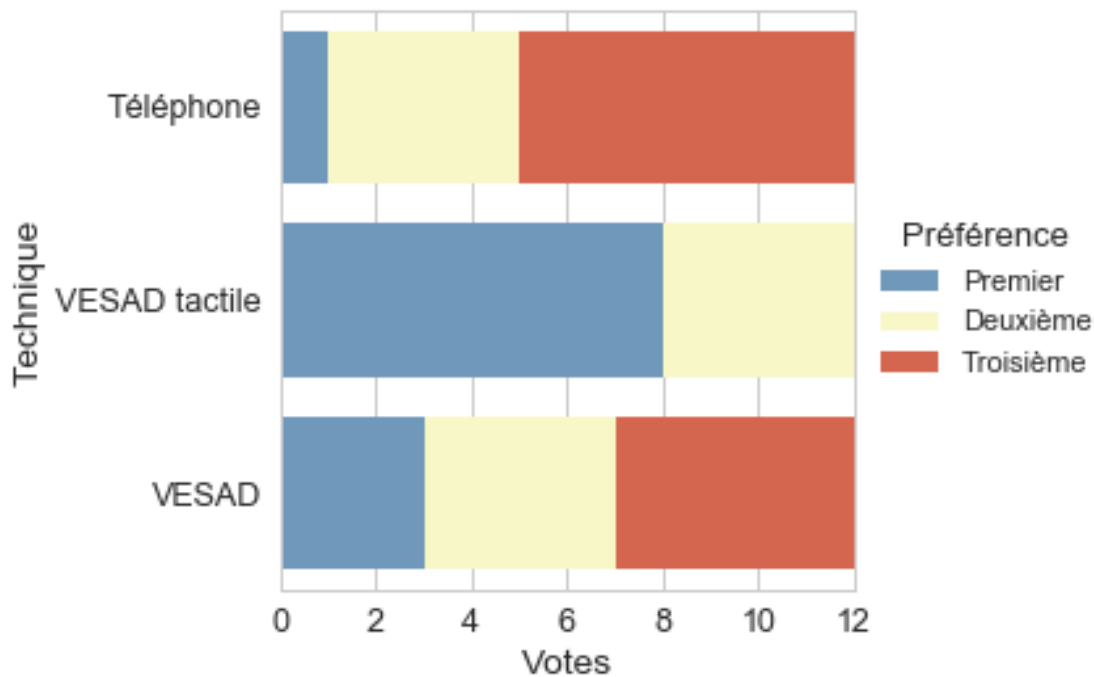
```
In [31]: (fig, axs) = plot_ranks('technique', ranks_dvs.columns[0:-1])
fig.savefig('ranks.png', dpi=300, bbox_inches='tight')
```



```
In [32]: (fig, axs) = plot_ranks_distributions('technique', ['preference'])

ax_handles, ax_labels = axs[0].get_legend_handles_labels()
legend = axs[0].legend(ax_handles[:-1], labels['preferences'], loc='center left',\
                      bbox_to_anchor=(1, 0.5), title=ranks_dvs['preference']['label'])
fix_legend_fontsize(legend)

fig.savefig('preferences.png', dpi=300, bbox_inches='tight')
```



3. Participant rates

Some functions for the analysis:

```
In [33]: def melt_trials(value_vars, var_name, value_name, data=trials):
         return pd.melt(data, id_vars=trials_ivs.loc['label', :], value_vars=value_vars, var_name=var_name)

In [34]: def filter_trials_outliers(dv_index, data=trials, nth_percentile_trimed=5):
         dv = trials_dvs[dv_index]
         pmin, pmax = np.nanpercentile(data[dv], [nth_percentile_trimed, 100 - nth_percentile_trimed])
         return data[(np.isnan(data[dv]) == False) & (pmin < data[dv]) & (data[dv] < pmax)]

In [35]: def test_pairwise_trials(dv_index, iv_index, data=trials, **args):
         results = []
         iv, dv = trials_ivs[iv_index], trials_dvs[dv_index]
         iv_category_ids = range(len(iv['categorical']))

         samples = [data[data[iv['label']] == iv_value][dv] for iv_value in iv['categorical']]
```

```

for iv_value_ids in itertools.combinations(iv_category_ids, 2):
    T, p_value = stats.ttest_ind(samples[iv_value_ids[0]], samples[iv_value_ids[1]])

    mean_diff = np.mean(samples[iv_value_ids[0]]) - np.mean(samples[iv_value_ids[1]])
    mean_diff_percentage = mean_diff / np.mean(samples[iv_value_ids[1]]) * 100

    results.append([iv['label'], iv['categorical'][iv_value_ids[0]], iv['categorical'][iv_value_ids[1]],
                    dv, mean_diff, mean_diff_percentage, T, p_value])

results = pd.DataFrame(results, columns=[labels['iv'], labels['iv_value'] + ' (1)', \
                                       labels['iv_value'] + ' (2)', labels['dv'], \
                                       labels['mean_difference'], labels['mean_difference_percentage'], \
                                       labels['t_statistic'], labels['p_value']])

p_values_correction(results, **args)
return results

In [36]: def test_pairwise_trial_conditions(dv_index, iv_index, condition_iv_indexes, data=trials, **args):
    condition_ivs = [trials_ivs[iv_index] for iv_index in condition_iv_indexes]
    condition_iv_cats = [iv['categorical'] for iv in condition_ivs]

    results_list = []
    for condition_iv_values in itertools.product(*condition_iv_cats):
        sample = data
        for condition_iv, condition_iv_value in zip(condition_ivs, condition_iv_values):
            sample = sample[sample[condition_iv['label']] == condition_iv_value]

        r = test_pairwise_trials(dv_index, iv_index, data=sample, correction_method=None)
        r['Condition'] = [condition_iv_values] * len(r)
        results_list.append(r)

    results = results_list[0]
    for result in results_list[1:]:
        results = results.append(result)

    p_values_correction(results, **args)
    results.reset_index(inplace=True, drop=True)
    return results

In [37]: def test_non_normal_trials(dv_indexes, iv_indexes, data=trials, **args):
    results = []

    for dv_index in dv_indexes:
        dv = trials_dvs[dv_index]

        for iv_index in iv_indexes:
            iv = trials_ivs[iv_index]
            samples = [data[data[iv['label']] == iv_value][dv] for iv_value in iv['categorical']]

            kruskal_H, p_value = stats.kruskal(*samples)
            results.append([iv['label'], dv, kruskal_H, p_value])

    results = pd.DataFrame(results, columns=[labels['iv'], labels['dv'], \
                                           'Kruskal-Wallis H', labels['p_value']])

```

```

p_values_correction(results, **args)
return results

In [38]: def test_pairwise_non_normal_trials(dv_indexes, iv_indexes, data=trials, **args):
    results = []

    for dv_index in dv_indexes:
        dv = trials_dvs[dv_index]

        for iv_index in iv_indexes:
            iv = trials_ivs[iv_index]
            samples = [data[data[iv['label']] == iv_value][dv] for iv_value in iv['categorical']]

            iv_category_ids = range(len(iv['categorical']))
            for iv_value_ids in itertools.combinations(iv_category_ids, 2): # Test each pair
                U, p_value = stats.mannwhitneyu(samples[iv_value_ids[0]], samples[iv_value_ids[1]])
                results.append([iv['label'], iv['categorical'][iv_value_ids[0]], iv['categorical'][iv_value_ids[1]],
                               dv, U, p_value])

    results = pd.DataFrame(results, columns=[labels['iv'], labels['iv_value'] + ' (1)', \
                                             labels['iv_value'] + ' (2)', labels['dv'], \
                                             'Mann-Whitney U', labels['p_value']])

    p_values_correction(results, **args)
    return results

In [39]: def plot_trials(dv_index, iv_indexes_list=[], data=trials, kind='bar'):
    dv = trials_dvs[dv_index]

    if (len(iv_indexes_list) == 0):
        iv_indexes_list = [[iv_index] for iv_index in trials_ivs.columns]

    fig, axs = subplots(len(iv_indexes_list))

    for iv_indexes, ax in zip(iv_indexes_list, axs):
        ivs = [trials_ivs[iv_index] for iv_index in iv_indexes]

        if (len(ivs) == 1):
            iv = ivs[0]

            if (kind == 'bar'):
                sns.barplot(x=iv['label'], y=dv, data=data, palette=iv['palette'], ax=ax)

            elif (kind == 'box'):
                sns.boxplot(x=iv['label'], y=dv, data=data, palette=iv['palette'], ax=ax)

            elif (kind == 'count'):
                sns.countplot(hue=iv['label'], x=dv, data=data, palette=iv['palette'], ax=ax)
                ax.set(ylabel='Count')
                ax.legend(loc='upper right', title=labels['count'], frameon=True)

        elif (len(ivs) == 2):
            if (kind == 'bar'):
                sns.barplot(x=ivs[1]['label'], y=dv, hue=ivs[0]['label'], data=data, palette=ivs[0]['palette'], ax=ax)
                ax.legend(frameon=True, loc='upper left', bbox_to_anchor=(1, 1))

```

```
return (fig, axs)
```

3.1 3.1. Task completion time

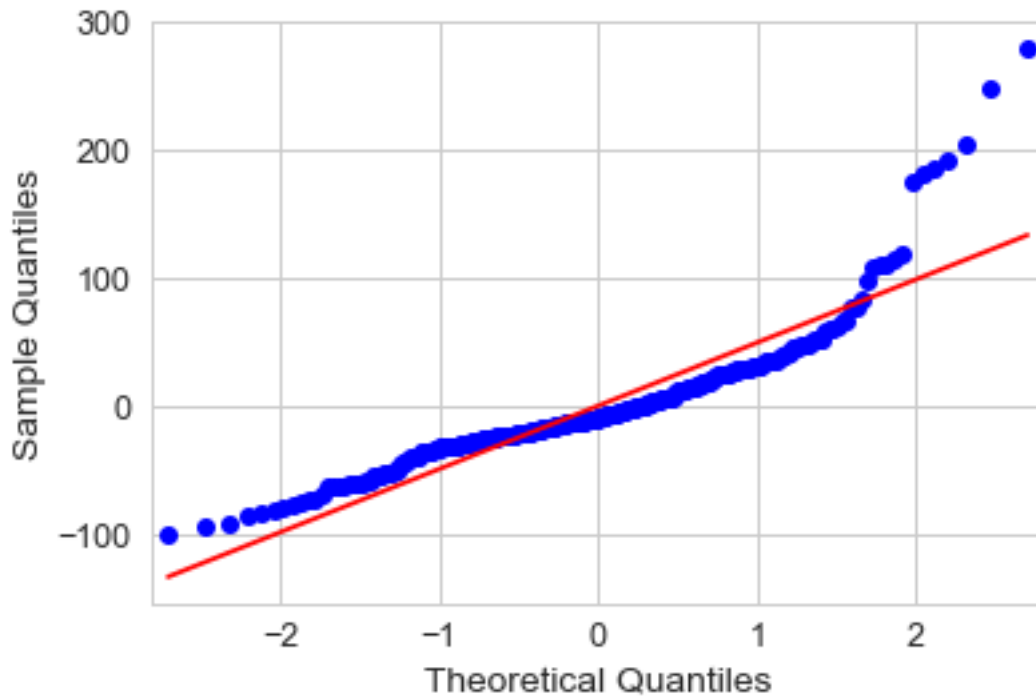
We should test all the assumptions of an ANOVA (independence of measure points, normality, homogeneity of variance). The trials are independent from each other, since they are generated randomly. The data is non-normal, but the ANOVA can tolerate non-normal data with skewed distribution. The homogeneity of variance is less important when the sample sizes are equal.

We perform a full factorial ANOVA with the model: $TCT \sim TECHNIQUE \times TEXT_SIZE \times DISTANCE + ORDERING$.

```
In [40]: tct_model = ols('total_time ~ technique * text_size * distance + ordering', data=trials_for_anova)
tct_model_anova = sm.stats.anova_lm(tct_model, typ=2)
```

```
fig = sm.qqplot(tct_model.resid, line='s')
fig.savefig('tct_anova.png', dpi=300, bbox_inches='tight')
plt.show()
```

```
tct_model_anova
```



```
Out[40]:
```

	sum_sq	df	F	PR(>F)
technique	256284.863291	2.0	49.887481	3.343713e-19
text_size	6524.396184	1.0	2.540031	1.121455e-01
distance	273.284406	1.0	0.106393	7.445375e-01
ordering	12606.272262	2.0	2.453891	8.784569e-02

technique:text_size	10779.057863	2.0	2.098212	1.246423e-01
technique:distance	1129.444917	2.0	0.219854	8.027777e-01
text_size:distance	10418.141005	1.0	4.055915	4.499418e-02
technique:text_size:distance	17350.562563	2.0	3.377397	3.556339e-02
Residual	703804.357932	274.0	NaN	NaN

The main significant effect on TCT is TECHNIQUE ($p < 0.0001$). There is also interaction effects: TEXT_SIZE x DISTANCE ($p = 0.046$) and TECHNIQUE x TEXT_SIZE x DISTANCE ($p = 0.037$). TEXT_SIZE, DISTANCE and ORDERING have no significant effects on TCT.

Also, we verify that the ANOVA residuals are roughly normal with the QQ-plot above.

We compare TCT for the three TECHNIQUE with pairwise t-tests (Benjamini–Hochberg correction) first. Then we compare TCT for the three TECHNIQUE for all TEXT_SIZE x DISTANCE conditions with pairwise t-tests (Benjamini–Hochberg correction).

```
In [41]: results = test_pairwise_trials('total_time', 'technique', correction_method=None)
         results['Condition'] = [''] * len(results)

         r = test_pairwise_trial_conditions('total_time', 'technique', ['text_size', 'distance'], correction_method=None)
         results = results.append(r)
         results.reset_index(inplace=True, drop=True)

         p_values_correction(results, correction_method='fdr_bh')
         results
```

```
Out[41]:
```

	Variable indépendante	Valeur variable indépendante (1)	\
0	Technique	Téléphone	
1	Technique	Téléphone	
2	Technique	VESAD tactile	
3	Technique	Téléphone	
4	Technique	Téléphone	
5	Technique	VESAD tactile	
6	Technique	Téléphone	
7	Technique	Téléphone	
8	Technique	VESAD tactile	
9	Technique	Téléphone	
10	Technique	Téléphone	
11	Technique	VESAD tactile	
12	Technique	Téléphone	
13	Technique	Téléphone	
14	Technique	VESAD tactile	

	Valeur variable indépendante (2)	Variable dépendante	\
0	VESAD tactile	Temps de complétion (s)	
1	VESAD	Temps de complétion (s)	
2	VESAD	Temps de complétion (s)	
3	VESAD tactile	Temps de complétion (s)	
4	VESAD	Temps de complétion (s)	
5	VESAD	Temps de complétion (s)	
6	VESAD tactile	Temps de complétion (s)	
7	VESAD	Temps de complétion (s)	
8	VESAD	Temps de complétion (s)	
9	VESAD tactile	Temps de complétion (s)	
10	VESAD	Temps de complétion (s)	

11	VESAD	Temps de complétion (s)
12	VESAD tactile	Temps de complétion (s)
13	VESAD	Temps de complétion (s)
14	VESAD	Temps de complétion (s)

	Différence des moyennes	Différence des moyennes (%)	Statistique T \
0	21.840362	32.666819	4.600061
1	-49.467731	-35.803106	-5.669051
2	-71.308093	-51.610437	-8.608496
3	24.168476	36.724278	2.549015
4	-77.353492	-46.227392	-3.835002
5	-101.521968	-60.670769	-5.199072
6	26.892856	41.152781	2.379929
7	-43.047900	-31.819082	-2.450544
8	-69.940756	-51.697078	-4.614999
9	9.832919	13.926232	1.170723
10	-26.990175	-25.123437	-2.028633
11	-36.823094	-34.276275	-2.721200
12	26.467198	40.306314	2.970482
13	-50.479357	-35.396365	-3.005064
14	-76.946555	-53.955290	-4.776990

	Valeur p	Condition
0	2.887821e-05	
1	3.951549e-07	
2	4.178800e-14	
3	1.936788e-02	(Grand, Proche)
4	8.149009e-04	(Grand, Proche)
5	2.246879e-05	(Grand, Proche)
6	2.482784e-02	(Grand, Loin)
7	2.265802e-02	(Grand, Loin)
8	7.898347e-05	(Grand, Loin)
9	2.477394e-01	(Petit, Proche)
10	5.175809e-02	(Petit, Proche)
11	1.372939e-02	(Petit, Proche)
12	7.855825e-03	(Petit, Loin)
13	7.855825e-03	(Petit, Loin)
14	5.551087e-05	(Petit, Loin)

PhoneInArOut is 22 s faster than *PhoneOnly* ($p < 0.0001$, 33% faster) and 71 s faster than *MidAirInArOut* ($p < 0.0001$, 52% faster) faster than *MidAirInArOut*. Also, *PhoneOnly* is 50 s faster than *MidAirInArOut* ($p < 0.0001$, 36% faster). I hypothesed this TCT difference order between the three techniques.

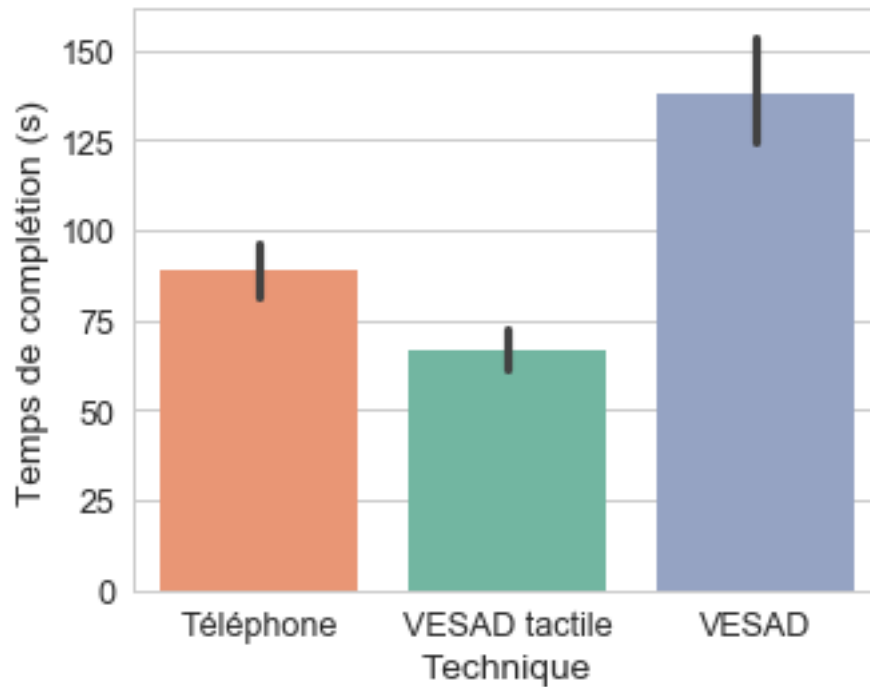
However this is not the case for all TEXT_SIZE x DISTANCE condition:

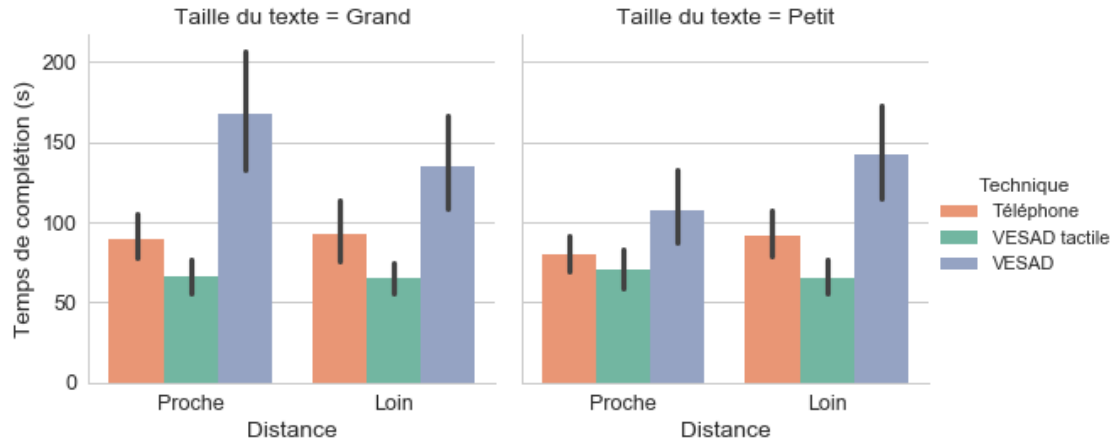
- For *Big* text size and *Near* distance:
 - *PhoneInArOut* is 24 s faster than *PhoneOnly* ($p < 0.019$, 37% faster);
 - *PhoneInArOut* is 102 s faster than *MidAirInArOut* ($p < 0.0001$, 61% faster);
 - *PhoneOnly* is 77 s faster than *MidAirInArOut* ($p = 0.0008$, 46% faster).
- For *Big* text size and *Far* distance:
 - *PhoneInArOut* is 27 s faster than *PhoneOnly* ($p < 0.022$, 41% faster);

- *PhoneInArOut* is 70 s faster than *MidAirInArOut* ($p < 0.0001$, 52% faster);
- *PhoneOnly* is 43 s faster than *MidAirInArOut* ($p = 0.023$, 32% faster).
- For *Small* text size and *Near* distance:
 - There is no significant difference between *PhoneInArOut* and *PhoneOnly*;
 - *PhoneInArOut* is 70 s faster than *MidAirInArOut* ($p = 0.0003$, 52% faster);
 - There is no significant difference between nor *PhoneOnly* and *MidAirInArOut*.
- For *Small* text size and *Far* distance:
 - *PhoneInArOut* is 26 s faster than *PhoneOnly* ($p < 0.0079$, 40% faster);
 - *PhoneInArOut* is 77 s faster than *MidAirInArOut* ($p < 0.0001$, 54% faster);
 - *PhoneOnly* is 50 s faster than *MidAirInArOut* ($p = 0.0079$, 35% faster).

```
In [42]: (fig, axs) = plot_trials('total_time', [['technique']])
fig.savefig('tct.png', dpi=300, bbox_inches='tight')

g = sns.factorplot(x=distance['label'], y=trials_dvs['total_time'], col=text_size['label'], hue=technique['label'],
                  data=trials, palette=technique['palette'], kind='bar')
g.savefig('tct_2.png', dpi=300, bbox_inches='tight')
```





3.2 Error rate

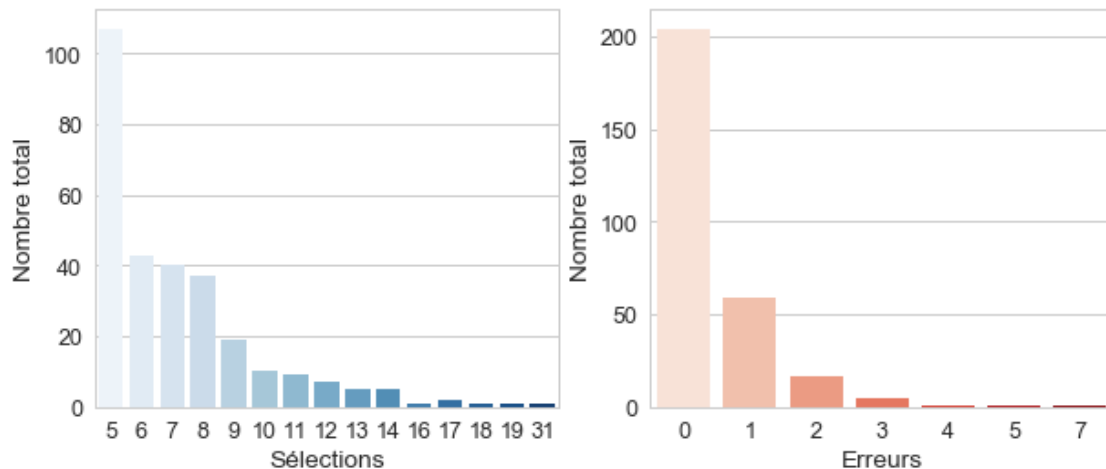
Visualize the SELECTIONS and ERRORS distributions:

```
In [43]: (fig, axs) = subplots(2)

sns.countplot(x=trials_dvs['selections_count'], data=trials, palette='Blues', ax=axs[0])
axs[0].set(ylabel=labels['count'])

sns.countplot(x=trials_dvs['errors'], data=trials, palette='Reds', ax=axs[1])
axs[1].set(ylabel=labels['count'])

fig.savefig('selections_errors_distributions.png', dpi=300, bbox_inches='tight')
```



We can't use ANOVA as for both SELECTIONS and ERRORS variables as their distributions are exponential. We use Kruskal-Wallis test (Benjamini-Hochberg correction) on SELECTIONS

and ERRORS to check if there is significative differences among TECHNIQUE, TEXT_SIZE, DISTANCE or ORDERING.

```
In [44]: test_non_normal_trials(['selections_count', 'errors'], ['technique', 'text_size', 'distance'],
```

```
Out[44]:
```

	Variable indépendante	Variable dépendante	Kruskal-Wallis H	Valeur p
0	Technique	Sélections	20.015292	0.000217
1	Taille du texte	Sélections	0.000810	0.977297
2	Distance	Sélections	0.329777	0.754387
3	Groupe	Sélections	19.648369	0.000217
4	Technique	Erreurs	6.510257	0.077152
5	Taille du texte	Erreurs	0.063506	0.915472
6	Distance	Erreurs	0.437007	0.754387
7	Groupe	Erreurs	10.200291	0.016256

Only TECHNIQUE ($p=0.0002$) and ORDERING ($p=0.0002$) have a significant effect on SELECTIONS. Identically, only TECHNIQUE ($p=0.077$) and ORDERING ($p=0.016$) have a significant effect on ERRORS.

We compare SELECTIONS and ERRORS among TECHNIQUE with pairwise Mann-Whitney tests (Benjamini–Hochberg correction):

```
In [45]: test_pairwise_non_normal_trials(['selections_count', 'errors'], ['technique'])
```

```
Out[45]:
```

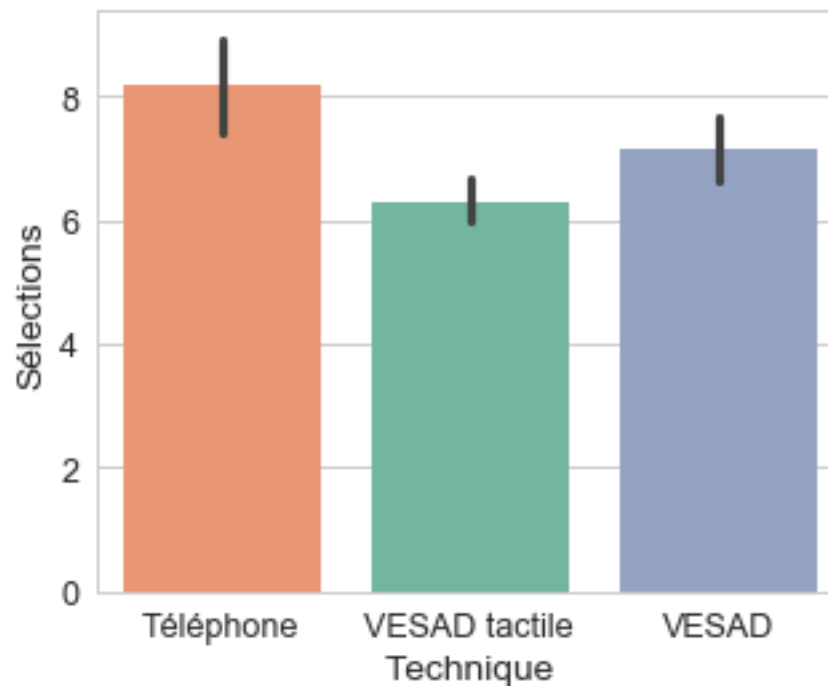
	Variable indépendante	Valeur variable indépendante (1)	Valeur variable indépendante (2)	Variable dépendante	Mann-Whitney U	Valeur p
0	Technique	Téléphone	VESAD tactile	Sélections	2923.0	0.000020
1	Technique	Téléphone	VESAD	Sélections	3733.5	0.020678
2	Technique	VESAD tactile	VESAD	Sélections	3850.5	0.028448
3	Technique	Téléphone	VESAD tactile	Erreurs	4502.5	0.358201
4	Technique	Téléphone	VESAD	Erreurs	4006.5	0.034230
5	Technique	VESAD tactile	VESAD	Erreurs	3869.0	0.020678

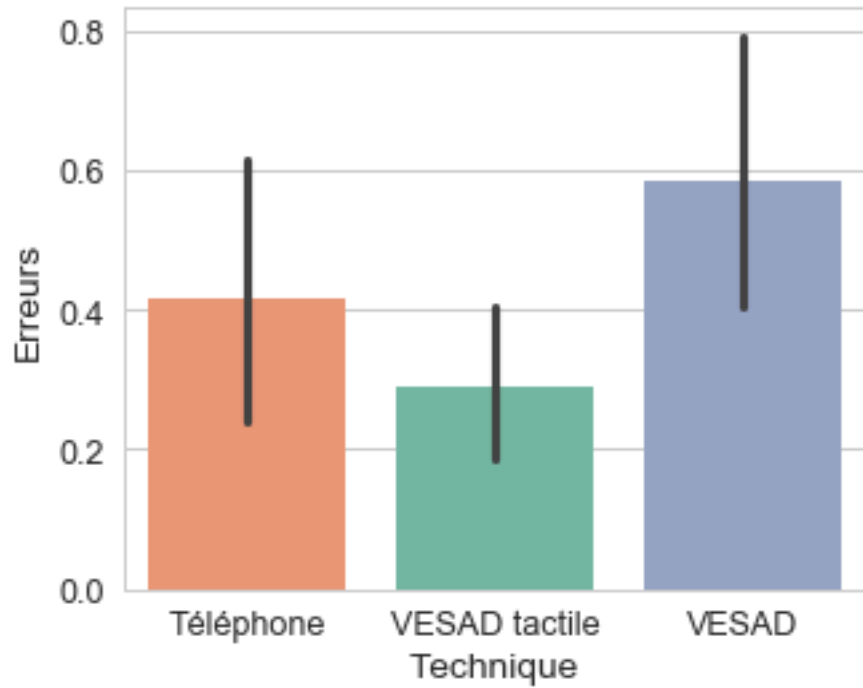
- Participants made a significant different number of selections between the three TECHNIQUE : *PhoneOnly* yielded the most selections ($p=0.021$) and *PhoneInArOut* the least selections ($p=0.028$). When using *PhoneOnly*, we observed that users sometimes forgot what they had selected or changed their mind during the drop operation, increasing the number of selections.

- Participants made significant more errors with *MidAirInArOut* rather than *PhoneOnly* ($p=0.034$) or *PhoneInArOut* ($p=0.021$), but these latter two do not differ significantly. With *MidAirInArOut*, users sometimes dropped items in the wrong container, not voluntarily but because they were too zoomed out and/or the sensing limitations of the Leap Motion made it difficult to successfully aim at targets, especially when arms were crossed.

```
In [46]: (fig, axes) = plot_trials('selections_count', [['technique']])
fig.savefig('selections.png', dpi=300, bbox_inches='tight')

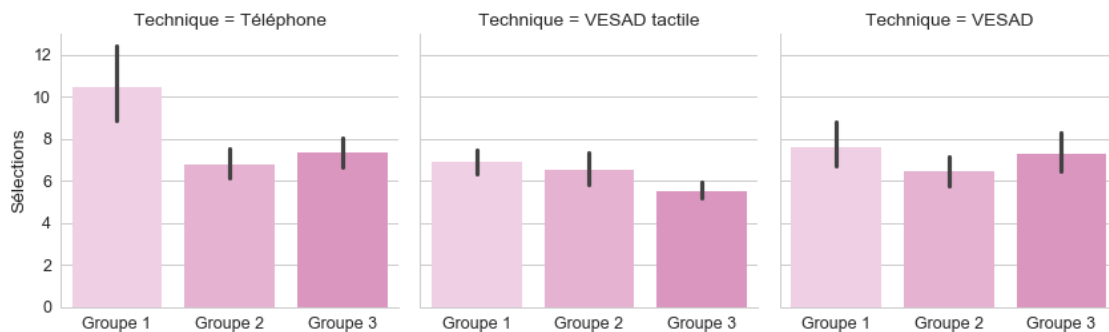
(fig, axes) = plot_trials('errors', [['technique']])
fig.savefig('errors.png', dpi=300, bbox_inches='tight')
```

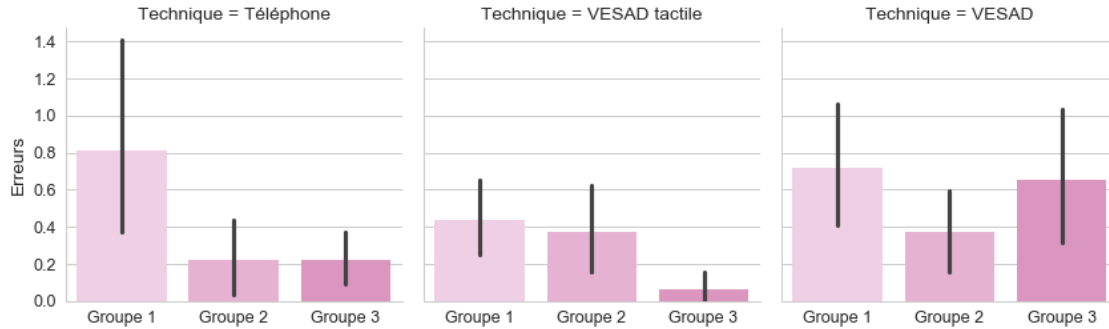




```
In [47]: g = sns.factorplot(x=ordering['label'], y=trials_dvs['selections_count'], col=technique['label'],\
                             palette=ordering['palette'], kind='bar', data=trials)
g.set_axis_labels('')
g.savefig('selections_ordering.png', dpi=300, bbox_inches='tight')

g = sns.factorplot(x=ordering['label'], y=trials_dvs['errors'], col=technique['label'],\
                   palette=ordering['palette'], kind='bar', data=trials)
g.set_axis_labels('')
g.savefig('errors_ordering.png', dpi=300, bbox_inches='tight')
```





PhoneOnly seems to be more sensitive in terms of ERRORS to being the first technique tested by users.

3.3. Navigation

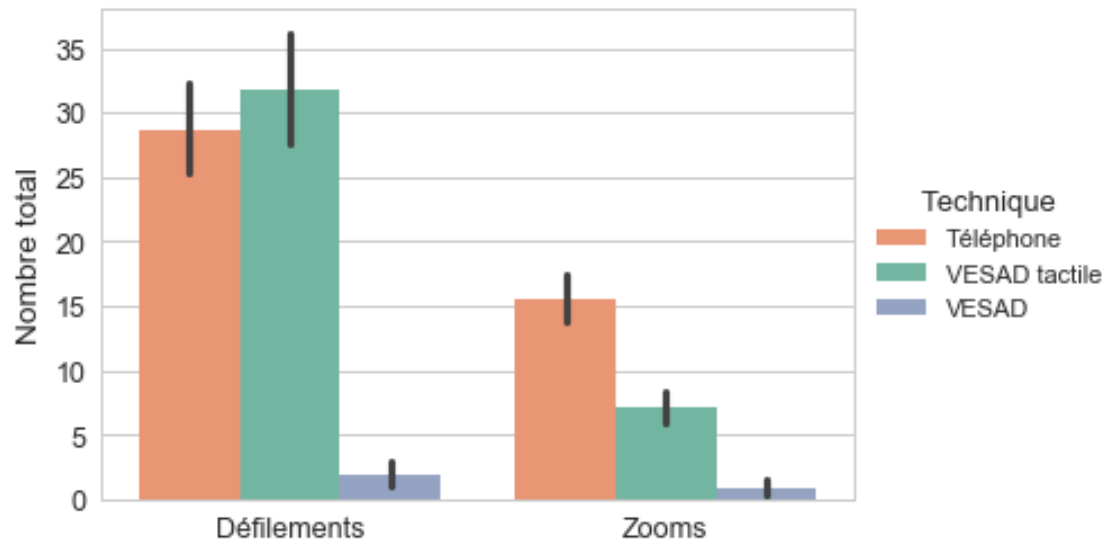
```
In [48]: trial_counts = melt_trials(var_name=labels['category'], value_name=labels['count'],\
                                     value_vars=[trials_dvs['pan_count'], trials_dvs['zoom_count']])

fig = plt.figure(figsize=(6,4))

ax = sns.barplot(x=labels['category'], y=labels['count'], hue=technique['label'],\
                 palette=technique['palette'], data=trial_counts)
legend = ax.legend(loc='center left', bbox_to_anchor=(1, 0.5), title=technique['label'])
fix_legend_fontsize(legend)
ax.set(xlabel='')

plt.show()
fig.savefig('navigation_count.png', dpi=300, bbox_inches='tight')

trial_counts.groupby([technique['label'], labels['category']], sort=False)\
    .aggregate(lambda x : '{:.2f}±{:.2f}'.format(np.mean(x), np.std(x)))\
    .unstack(level=1)
```

```
Out[48]:
```

Catégorie	Défilements	Zooms
Téléphone	28.70±18.56	15.53±8.63
VESAD tactile	31.81±20.82	7.14±6.19
VESAD	1.83±4.79	0.83±3.20

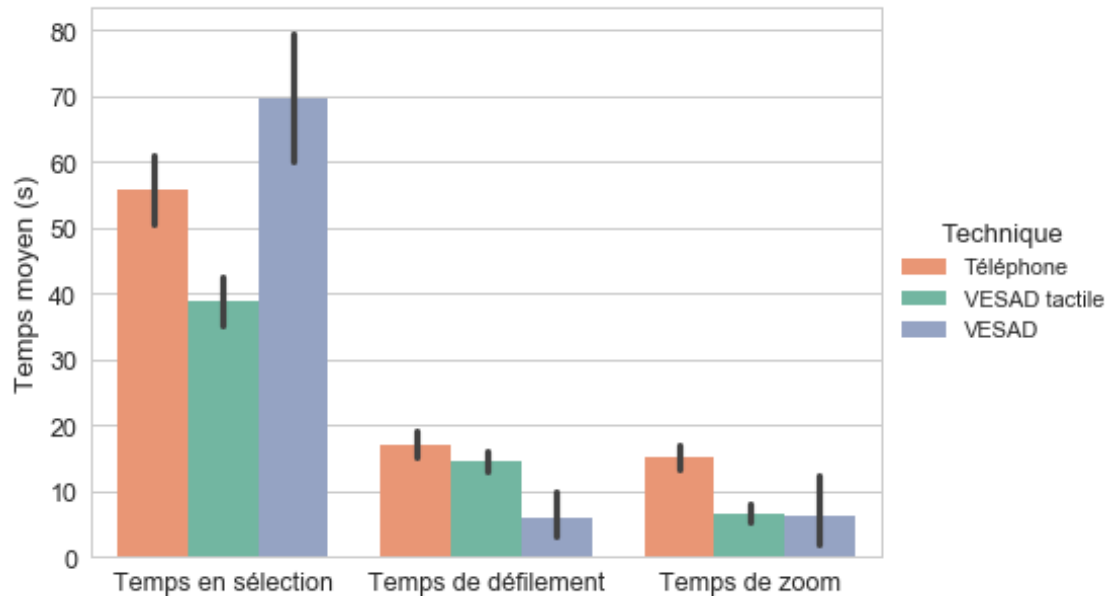
```
In [49]: trial_times = melt_trials(var_name=labels['category'], value_name=labels['time'],\
                                   value_vars=[trials_dvs['selections_time'], trials_dvs['pan_time'], t

fig = plt.figure(figsize=(7,5))

ax = sns.barplot(x=labels['category'], y=labels['time'], hue=technique['label'], palette=technique,
                 data=trial_times)
legend = ax.legend(loc='center left', bbox_to_anchor=(1, 0.5), title=technique['label'])
fix_legend_fontsize(legend)
ax.set(xlabel='')

plt.show()
fig.savefig('navigation_time.png', dpi=300, bbox_inches='tight')

trial_times.groupby([technique['label'], labels['category']], sort=False)\
    .aggregate(lambda x : '{:.2f}±{:.2f}'.format(np.mean(x), np.std(x)))\
    .unstack(level=1)
```



```
Out[49]:
```

	Temps moyen (s)		
Catégorie	Temps en sélection	Temps de défilement	Temps de zoom
Technique			
Téléphone	55.74±27.54	17.12±10.66	15.18±9.00
VESAD tactile	38.98±19.21	14.53±8.10	6.70±6.83
VESAD	69.68±47.17	5.97±16.56	6.24±26.31

```
In [50]: trial_distances = melt_trials(var_name=labels['category'], value_name=labels['distance'],\
                                         value_vars=[trials_dvs['selections_projected_distance'],\
                                                         trials_dvs['pan_projected_distance'],\
                                                         trials_dvs['zoom_projected_distance'],\
                                                         trials_dvs['absolute_head_phone_distance']])

g = sns.factorplot(x=technique['label'], y=labels['distance'], col=labels['category'], data=trials_dvs,\
                   palette=technique['palette'], kind='bar', col_wrap=2)

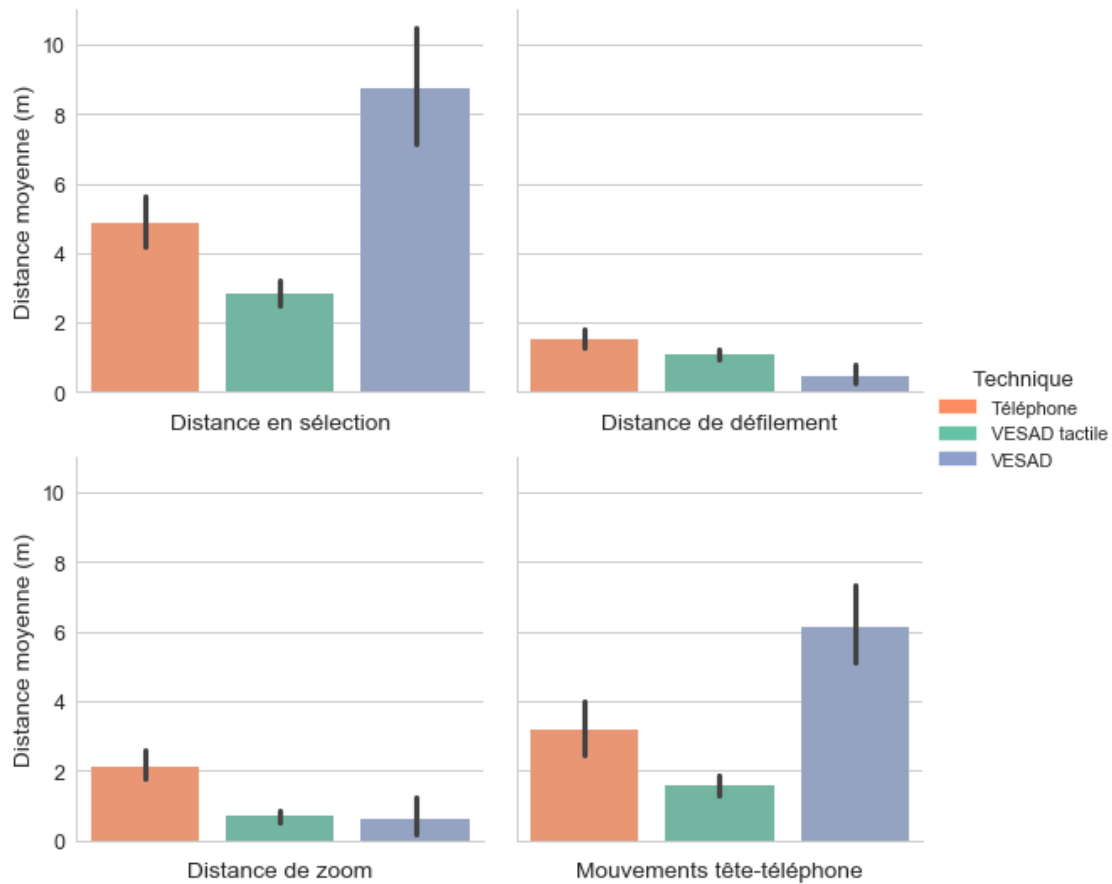
g.set_titles('{col_name}') # Replace subplot titles
for ax in g.axes:
    ax.title.set_position([0.5, -0.12])

g.set_axis_labels('') # Custom legend
g.set_xticklabels([])
legend_handles = [patches.Patch(color=color, label=value)\
                  for value, color in zip(technique['categorical'], technique['palette'])]
legend = plt.legend(handles=legend_handles, loc='center left', bbox_to_anchor=(1, 1.1), title=labels['category'],\
                    fix_legend_fontsize(legend))

plt.show()
g.savefig('navigation_distance.png', dpi=300, bbox_inches='tight')

trial_distances.groupby([technique['label'], labels['category']], sort=False)\
```

```
.aggregate(lambda x : '{:.2f}±{:.2f}'.format(np.mean(x), np.std(x)))\
.unstack(level=1)
```



```
Out[50]:
```

	Distance moyenne (m)	
Catégorie	Distance en sélection	Distance de défilement
Technique		Distance de zoom
Téléphone	4.87±3.74	1.50±1.31
VESAD tactile	2.83±1.89	1.09±0.76
VESAD	8.72±7.89	0.47±1.30

Catégorie	Mouvements tête-téléphone
Technique	
Téléphone	3.18±3.55
VESAD tactile	1.57±1.37
VESAD	6.12±5.05

Variable meanings:

- Selection Time = time spent looking for where to drop an item that had been picked
- Selection Distance = distance travelled by the finger with an item selected

- Head Phone Distance = sum of the distance between the head and the phone

Results are:

- Both for *PhoneInArOut* and *PhoneOnly*, participants used pans more than zooms : in count, in time and in distance.
- Participants were the most effective in **selection time** for *PhoneInArOut* (38.98 ± 19.21 s) rather than for *PhoneOnly* (55.74 ± 27.54 s). We observed that the screen size in *PhoneInArOut* helped to make decisions on items to select or where to drop the selected items.
- Participants used as much **pans** in *PhoneInArOut* as in *PhoneOnly* ($\sim 30 \pm 19$). But it seems they were slightly more effective with in *PhoneInArOut* rather than *PhoneOnly* both in time (14.53 ± 8.10 s / 17.12 ± 10.66 s) and distance (1.09 ± 0.76 m / 1.50 ± 1.31 m).
- Participants used less **zooms** in *PhoneInArOut* (7.14 ± 6.19) rather than *PhoneOnly* (15.53 ± 8.63). They were also more effective with zooms in *PhoneInArOut* rather than *PhoneOnly* both in time (6.70 ± 6.83 s / 15.18 ± 9.00 s) and distance (0.69 ± 0.74 m / 2.11 ± 1.99 m).
- In terms of **physical navigation**, the head-phone distance is the lowest for *PhoneInArOut* (1.57 ± 1.37), the greatest for *MidAirInArOut* (6.12 ± 5.05). *PhoneOnly* is between the two (3.18 ± 3.55). In *MidAirInArOut*, participants moved in conjunction the hand and the phone to select the item: for items at the grid's extremities, it could be easier to rotate the phone to bring the item closer to the head. It seemed that people using both their hands were more effective. Also, both for *PhoneOnly* and *MidAirInArOut*, participants preferred to bring closer the phone if they had trouble to read an item's letter. *PhoneInArOut* required less head-phone movement because participants could let the grid zoomed in and do only pans and drag'n'drop with items to complete the task without many virtual zoom nor physical zoom.