

Handheld VESAD Analysis

June 20, 2018

The analysis of the experiment data is also accessible online: <https://github.com/NormandErwan/HandheldVesadAnalysis/blob/master/Handheld%20VESAD%20Analysis.ipynb>.

0.1 1. Data preparation

Configuration :

```
In [1]: # Imports
import numpy as np
import pandas as pd
from pandas.api.types import CategoricalDtype
import itertools

import seaborn as sns
import matplotlib as mpl
import matplotlib.pyplot as plt
import matplotlib.ticker as ticker
import matplotlib.patches as patches

from scipy import stats
import statsmodels.api as sm
from statsmodels.formula.api import ols
from statsmodels.stats.multicomp import (MultiComparison, pairwise_tukeyhsd)
from statsmodels.stats.multitest import multipletests
from statsmodels.stats.libqsturng import psturng

from ast import literal_eval
from os import listdir
from os.path import join

from IPython.html.services.config import ConfigManager

C:\Users\Erwan\Miniconda\envs\master-thesis\lib\site-packages\IPython\html.py:14: ShimWarning: The
"IPython.html.widgets" has moved to "ipywidgets"., ShimWarning)

In [2]: # Notebook configuration
%matplotlib inline

# Ruler
```

```

ip = get_ipython()
cm = ConfigManager(parent=ip)
cm.update('notebook', {"ruler_column": [80]})

# Style and size of the figures
subplotsize = (5, 4)
legend_fontsize = sns.plotting_context('notebook')['axes.labelsize']
legend_title_fontsize = legend_fontsize + 1
sns.set(context='notebook', style='whitegrid', font_scale=1.25,
        rc={'legend.fontsize': legend_fontsize, 'savefig.dpi': 300,
            'savefig.bbox': 'tight'})

# Render the plots with this language
#language = 'English'
language = 'Français'

```

Data are loaded in the following variables: - Participants information, from the questionnaire before the trials: participants - The summary of the trials of the participants: raw_trials - Trials averaged so that each participants ends up with a single observation (there was two trials per condition per participant) (Tip 9 of Dragicevic (2016)): trials - The detailed measures of the trials: trial_details - The ranks of the participants from the post-questionary: ranks

```

In [3]: participants = pd.read_csv('participants.csv')
raw_trials = pd.read_csv('participant_trials.csv')
trials_for_anova = pd.read_csv('participant_trials.csv')
ranks = pd.read_csv('participant_ranks.csv')

```

```

In [4]: # Detailled trials are long to load, keep commented if unused

```

```

#trial_details = []
#for file in listdir('.'):
#    if file.endswith('details.csv'): # The trial files end with *-details.csv
#        details.append(pd.read_csv(file))
#trial_details = pd.concat(details, ignore_index=True)

```

Creates independent variables lists (participants_ivs, trials_ivs) and dependent variables lists (ranks_dvs, trials_dvs) to make easier to use algorithms and to plot figures.

```

In [5]: # Participants IVs
if language == 'Français':
    participants_iv_labels = ['Numéro participant', 'Sexe',
                             'Porte des lunettes', 'Porte des lentilles',
                             'Est daltonien', 'Intervalle d\'âge',
                             'Main dominante', 'Main utilisée pour la souris',
                             'Activité principale',
                             'Utilisation de l\'ordinateur (heures/jours)',
                             'Logiciels 3D utilisés',
                             'Visiocasques RV/RA utilisés',
                             'Techniques d\'interactions RV/RA utilisées']
else:
    participants_iv_labels = ['Participant Id', 'Sex', 'Has Glasses',

```

```

        'Has Contact Lenses', 'Is Color Blind',
        'Age Class', 'Dominant Hand',
        'Hand Used for Mouse', 'Activity',
        'Computer Hours per Day', '3D Softwares Used',
        'HMD Used',
        'Known Interactions Techniques on HMD']

participants_ivs = pd.Series(data=participants_iv_labels,
                             index=participants.columns)

In [6]: # Trials IVs
if language == 'Français':
    trials_iv_labels = ['Technique', 'Taille du texte', 'Distance', 'Groupe',
                        'Méthode d\'entrée', 'Méthode d\'affichage']
else:
    trials_iv_labels = ['Technique', 'Text Size', 'Distance', 'Ordering',
                        'Technique Input', 'Technique Output']

trials_ivs = ['technique', 'text_size',
              'distance', 'ordering', 'input', 'output']
trials_ivs = pd.DataFrame(columns=trials_ivs,
                           index=['label', 'categorical', 'palette'])

default_palette = sns.color_palette('Set2', 8)

for iv_index, iv_label in zip(trials_ivs.columns, trials_iv_labels):
    iv_categories = raw_trials.sort_values([iv_index + '_id'])\
        .drop_duplicates(iv_index)[iv_index]
    iv_categorical = pd.Categorical(iv_categories, iv_categories, ordered=True)
    trials_ivs[iv_index] = [iv_label, iv_categorical, default_palette]

technique_palette = [default_palette[1], default_palette[0], default_palette[2]]
trials_ivs.at['palette', 'technique'] = technique_palette
trials_ivs.at['palette', 'text_size'] = sns.light_palette(
    default_palette[6], 3)[1:3] # Brown paired colors
trials_ivs.at['palette', 'distance'] = sns.light_palette(
    default_palette[4], 3)[1:3] # Green paired colors
trials_ivs.at['palette', 'ordering'] = technique_palette
trials_ivs.at['palette', 'input'] = [default_palette[5], default_palette[2]]
trials_ivs.at['palette', 'output'] = [default_palette[0],
                                       sns.color_palette('muted')[5]]

In [7]: # Trials DVs
if language == 'Français':
    trials_dv_labels = ['Temps de complétion (s)', 'Sélections',
                        'Temps en sélection', 'Distance 3D en sélection',
                        'Distance en sélection', 'Déselections', 'Erreurs',
                        'Disques classés', 'Défilements', 'Temps de défilement',
                        'Distance 3D de défilement', 'Distance de défilement',
                        'Zooms', 'Temps de zoom', 'Distance 3D de zoom',
                        'Distance de zoom', 'Mouvements tête-téléphone',

```

```

        'Distance relative tête-téléphone']
else:
    trials_dv_labels = ['Task Completion Time (s)', 'Selections',
                        'Selection Time', 'Selection Distance',
                        'Selection Distance on Grid', 'Deselections', 'Errors',
                        'Items Classified', 'Pans', 'Pan Time', 'Pan Distance',
                        'Pan Distance on Grid', 'Zooms', 'Zoom Time',
                        'Zoom Distance', 'Zoom Distance on Grid',
                        'Phone-Head Motion', 'Signed Phone-Head Motion']

trials_dvs = raw_trials.loc[:, 'total_time':'signed_head_phone_distance'].columns
trials_dvs = pd.Series(data=trials_dv_labels, index=trials_dvs)

```

```

In [8]: # Ranks DVs
if language == 'Français':
    ranks_dv_labels = ['Facile à comprendre', 'Mentalement facile à utiliser',
                      'Physiquement facile à utiliser', 'Rapidité', 'Réussite',
                      'Frustration', 'Préférence']
else:
    ranks_dv_labels = ['Easy to Understand', 'Mentally Easy to Use',
                      'Physically Easy to Use', 'Subjective Speed',
                      'Subjective Performance', 'Frustration', 'Preference']

ranks_dv_scales = [pd.Categorical(list(range(1, 6)), list(
    range(1, 6))), ordered=True] * len(ranks_dv_labels)

RdYlBu = sns.color_palette('RdYlBu', 5)
ranks_dv_palettes = [sns.color_palette('RdYlBu', 5)] * len(ranks_dv_labels)

ranks_dvs = ranks.loc[:, 'easy_understand':'preference'].columns
ranks_dvs = pd.DataFrame(data=[ranks_dv_labels, ranks_dv_scales,
                              ranks_dv_palettes],
                        columns=ranks_dvs, index=['label', 'scale', 'palette'])

ranks_dvs.at['scale', 'preference'] = pd.Categorical(
    list(range(1, 4)), list(range(1, 4)), ordered=True)
ranks_dvs.at['palette', 'preference'] = [RdYlBu[4], RdYlBu[2], RdYlBu[0]]

```

```

In [9]: # Shortcuts
participant_id = participants_ivs['participant_id']
technique = trials_ivs['technique']
text_size = trials_ivs['text_size']
distance = trials_ivs['distance']
ordering = trials_ivs['ordering']
iv_input = trials_ivs['input']
iv_output = trials_ivs['output']

```

Clean the data:

```

In [10]: # Set better and translated columns to participants, trials and ranks
participants.columns = participants_ivs

```

```

columns = []
for column in raw_trials.columns:
    if (column in participants_ivs.index):
        columns.append(participants_ivs[column])
    elif (column in trials_ivs.columns):
        columns.append(trials_ivs[column]['label'])
    elif (column in trials_dvs.index):
        columns.append(trials_dvs[column])
    else:
        columns.append(column)

raw_trials.columns = columns

ranks.columns = [participant_id, ordering['label'],
                 technique['label']] + ranks_dvs.loc['label', :].tolist()

```

```

In [11]: # Set the participant_id column as the index in participants
participants.set_index(participants_ivs['participant_id'], inplace=True)

```

```

In [12]: # Some participants are non valid or don't have complete measures
non_valid_participants = [0, 4]
participants = participants[~participants.index.isin(non_valid_participants)]
ranks = ranks[~ranks[participants_ivs['participant_id']]
               .isin(non_valid_participants)]

incomplete_trials_participant_ids = [0, 4]
raw_trials = raw_trials[~raw_trials[participants_ivs['participant_id']]
                        .isin(incomplete_trials_participant_ids)
                        ].reset_index(drop=True)
trials_for_anova = trials_for_anova[~trials_for_anova['participant_id']
                                     .isin(incomplete_trials_participant_ids)
                                     ].reset_index(drop=True)

```

```

In [13]: # Some participants have wrong head phone measures
for head_distance_column in ['absolute_head_phone_distance',
                             'signed_head_phone_distance']:
    raw_trials.loc[raw_trials[trials_dvs[head_distance_column]] == 0,
                  trials_dvs['absolute_head_phone_distance']] = np.nan
    trials_for_anova.loc[trials_for_anova[head_distance_column] == 0,
                        head_distance_column] = np.nan

```

```

In [14]: # Setup categorical columns participants, trials and ranks
participants[ordering['label']] = ranks.groupby(
    participant_id)[ordering['label']].first()
participants[ordering['label']] = participants[ordering['label']].astype(
    ordering['categorical'])

for iv_index in trials_ivs.columns:
    iv = trials_ivs[iv_index]
    raw_trials[iv['label']] = raw_trials[iv['label']].astype(iv['categorical'])

```

```

    trials_for_anova[iv_index] = raw_trials[iv['label']]

ranks[technique['label']] = ranks[technique['label']].astype(
    technique['categorical'])
ranks[ordering['label']] = ranks[ordering['label']].astype(
    ordering['categorical'])

# Rename categories
if language == 'Français':
    technique['categorical'].categories = ['Téléphone', 'VESAD tactile', 'VESAD']
    text_size['categorical'].categories = ['Grand', 'Petit']
    distance['categorical'].categories = ['Proche', 'Loin']
    ordering['categorical'].categories = ['Groupe 1', 'Groupe 2', 'Groupe 3']
    iv_input['categorical'].categories = ['Tactile', 'Autour du téléphone']
    iv_output['categorical'].categories = ['Téléphone seul', 'Téléphone étendu']
else:
    ordering['categorical'].categories = ['Group 1', 'Group 2', 'Group 3']

# Set renamed categories to data
participants[trials_ivs['ordering']]['label']
    ].cat.categories = ordering['categorical'].categories

for iv_index in trials_ivs.columns:
    iv = trials_ivs[iv_index]
    raw_trials[iv['label']].cat.categories = iv['categorical'].categories

ranks[technique['label']].cat.categories = technique['categorical'].categories
ranks[ordering['label']].cat.categories = ordering['categorical'].categories

```

```

In [15]: # Eval the arrays in some dvs
def eval_if_str(data):
    return literal_eval(data) if isinstance(data, str) else data

raw_trials['grid_config'] = raw_trials['grid_config'].apply(eval_if_str)

```

```

In [16]: # Create trials
trials_groupby_ivs = [participants_ivs['participant_id']] \
    + trials_ivs.loc['label', :].tolist()
trials = raw_trials.groupby(trials_groupby_ivs, observed=True) \
    .mean().reset_index()

```

Utilities:

```

In [17]: # Figure labels in the selected language
labels = pd.Series()

if language == 'Français':
    labels['category'] = 'Catégorie'
    labels['count'] = 'Nombre total'
    labels['distance'] = 'Distance moyenne (m)'
    labels['dv'] = 'Variable dépendante'

```

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labels['iv'] = 'Variable indépendante'
labels['iv_value'] = 'Valeur VI'
labels['mean_difference'] = 'Différence des moyennes'
labels['mean_difference_percentage'] = 'Différence des moyennes (%)'
labels['mean_rank'] = 'Note moyenne'
labels['preferences'] = ['Premier', 'Deuxième', 'Troisième']
labels['p_value'] = 'Valeur p'
labels['question'] = 'Question'
labels['rank'] = 'Note'
labels['time'] = 'Temps moyen (s)'
labels['t_statistic'] = 'Statistique T'
labels['votes'] = 'Participants'
else:
    labels['category'] = 'Category'
    labels['count'] = 'Count'
    labels['distance'] = 'Mean Distance (m)'
    labels['dv'] = 'Dependent Variable'
    labels['iv'] = 'Independent Variable'
    labels['iv_value'] = 'IV Value'
    labels['mean_difference'] = 'Mean Difference'
    labels['mean_difference_percentage'] = 'Mean Difference Percentage'
    labels['mean_rank'] = 'Mean Rank'
    labels['preferences'] = ['First', 'Second', 'Third']
    labels['p_value'] = 'p-value'
    labels['question'] = 'Question'
    labels['rank'] = 'Rank'
    labels['time'] = 'Mean Time (s)'
    labels['t_statistic'] = 'T statistic'
    labels['votes'] = 'Participants'

```

```

In [18]: def mean_ci(x, which=95, n_boot=1000):
    """Returns the confidence interval of the mean"""
    x2 = [i for i in x if not np.isnan(i)]
    boots = sns.algorithms.bootstrap(x2, n_boot=n_boot)
    return sns.utils.ci(boots, which=which)

```

```

In [19]: def print_mean_ci(x, ci_which=95):
    """Returns a string containing the mean with the CI of x"""
    ci1, ci2 = mean_ci(x, which=ci_which)
    return '{:.2f} [{:.2f}, {:.2f}'].format(np.mean(x), ci1, ci2)

```

```

In [20]: def mean_difference(a, b):
    """Returns the mean difference value and percentage between a and b"""
    mean_diff = np.mean(a) - np.mean(b)
    mean_diff_percentage = mean_diff / np.mean(b) * 100
    return (mean_diff, mean_diff_percentage)

```

```

In [21]: def p_values_correction(data, alpha=0.05, correction_method='fdr_bh'):
    if correction_method != None:
        reject, p_values_corrected, a1, a2 =\
            multipletests(data[labels['p_value']].tolist(), alpha=alpha,

```

```

        method=correction_method)
    data[labels['p_value']] = p_values_corrected

In [22]: def subplots(nsubplots, ncols_max=2, subplotsize=subplotsize, *plt_args):
    ncols = min(ncols_max, nsubplots)
    nrows = ((nsubplots - 1) // ncols) + 1
    fig, axs = plt.subplots(nrows=nrows, ncols=ncols,\
        figsize=(subplotsize[0]*ncols, subplotsize[1]*nrows),
        *plt_args)

    if nrows == 1 and ncols == 1:
        axs = [axs]
    elif nrows >= 2 and ncols >= 2:
        axs = [ax for ax_row in axs for ax in ax_row]

    for ax in axs[:-1][0:len(axs) - nsubplots]:
        fig.delaxes(ax)

    return (fig, axs)

In [23]: def fix_legend_fontsize(ax_legend, fontsize=legend_title_fontsize):
    plt.setp(ax_legend.get_title(), fontsize=fontsize)

In [24]: def config_legend(ax, iv_id, fontsize=legend_title_fontsize):
    legend = ax.legend(title=trials_ivs.at['label', iv_id], frameon=True,
        loc='center left', bbox_to_anchor=(1, 0.5))
    fix_legend_fontsize(legend)
    return legend

In [25]: def log_mean(x):
    return np.exp(np.mean(np.log(x)))

```

0.2 2. Participant ranks

Some functions for the analysis:

```

In [26]: def get_ranks_count(iv_index, dv_index):
    iv, dv = trials_ivs[iv_index], ranks_dvs[dv_index]

    ranks_counts_index = pd.MultiIndex.from_product([iv['categorical'],
        dv['scale']],
        names=[iv['label'],
            labels['rank']])

    # Zero counts by default and gets the counts
    default_counts = pd.Series(0, index=ranks_counts_index)
    ranks_counts = ranks.groupby([iv['label'], dv['label']]).size()

    # Merge and remove duplicated defaults
    ranks_counts = pd.concat([ranks_counts, default_counts])
    ranks_counts = ranks_counts[~ranks_counts.index.duplicated(keep='first')]

    ranks_counts.sort_index(inplace=True)

```



```

ranks_counts.index = ranks_counts_index # Restore the index
return ranks_counts

```

```

In [27]: def cumulated_barplot(data, palette, **args):
    for row_id, row in data.iloc[:, :-1].iterrows():
        sns.barplot(y=data.columns, x=row, label=row_id,
                    color=palette[row_id-1], orient='h', **args)

```

```

In [28]: def plot_ranks_distributions(iv_id, dv_ids):
    iv = trials_ivs[iv_id]

    fig, axs = subplots(len(dv_ids))
    for dv_id, ax in zip(dv_ids, axs):
        dv = ranks_dvs[dv_id]

        cumulated_ranks_count = get_ranks_count(iv_id, dv_id).unstack(level=0)\
                                .cumsum()
        cumulated_barplot(cumulated_ranks_count, palette=dv['palette'], ax=ax)
        ax.set(xlabel=labels['votes'], xlim=(0, cumulated_ranks_count.max()[0]))
        ax.xaxis.set_major_locator(ticker.MultipleLocator(2)) # Fix the axis ticks

        ax_handles, ax_labels = ax.get_legend_handles_labels()
        legend = ax.legend(ax_handles[:, :-1], ax_labels[:, :-1], frameon=True,
                           loc='lower center', bbox_to_anchor=(0.5, 1),
                           mode=None, ncol=len(dv['scale']), title=dv['label'],
                           fontsize=legend_fontsize-2)
        fix_legend_fontsize(legend)

    fig.tight_layout(h_pad=1) # Add padding to avoid legend and labels overlap
    return (fig, axs)

```

```

In [29]: def plot_ranks(iv_id, dv_ids, estimator=np.mean):
    iv = trials_ivs[iv_id]

    fig, axs = subplots(len(dv_ids))
    for dv_id, ax in zip(dv_ids, axs):
        dv = ranks_dvs[dv_id]

        sns.barplot(x=iv['label'], y=dv['label'], palette=iv['palette'],
                    data=ranks, ax=ax, estimator=estimator)
        ax.set(ylim=(0, dv['scale'][-1]))
        ax.yaxis.set_major_locator(ticker.MultipleLocator(1)) # Fix the axis ticks

    return (fig, axs)

```

```

In [30]: def rank_samples(iv_id, dv_id):
    """Returns the list of ranks (DV) for each IV value"""
    samples = []
    iv = trials_ivs[iv_id]
    for iv_value in iv['categorical']:
        dv_label = ranks_dvs[dv_id]['label']

```

```

        sample = ranks[ranks[iv['label']] == iv_value][dv_label]\
            .reset_index(drop=True)
        samples.append(sample)
    return samples

In [31]: def test_ranks(iv_id, dv_ids, **args):
    results = []
    iv = trials_ivs[iv_id]

    for dv_id in dv_ids:
        dv = ranks_dvs[dv_id]
        samples = rank_samples(iv_id, dv_id)
        H, p = stats.kruskal(*samples)
        results.append([iv['label'], dv['label'], H, p])

    results = pd.DataFrame(results, columns=[labels['iv'], labels['dv'],
                                            'Kruskal-Wallis H',
                                            labels['p_value']])

    p_values_correction(results, **args)
    return results

In [32]: def test_pairwise_ranks(iv_id, dv_ids, **args):
    iv = trials_ivs[iv_id]
    iv_category_ids = range(len(iv['categorical']))

    results = []
    for dv_id in dv_ids:
        dv = ranks_dvs[dv_id]
        samples = rank_samples(iv_id, dv_id)
        sample_pairs = itertools.combinations(iv_category_ids, 2)
        for id1, id2 in sample_pairs:
            U, p = stats.mannwhitneyu(samples[id1], samples[id2])
            mean_diff, mean_diff_per = mean_difference(samples[id1], samples[id2])
            results.append([iv['label'], iv['categorical'][id1],
                            iv['categorical'][id2], dv['label'],
                            mean_diff, mean_diff_per, U, p])

    columns = [labels['iv'], labels['iv_value'] + ' 1',
                labels['iv_value'] + ' 2', labels['dv'],
                labels['mean_difference'], labels['mean_difference_percentage'],
                'Mann-Whitney U', labels['p_value']]
    results = pd.DataFrame(results, columns=columns)
    p_values_correction(results, **args)
    return results

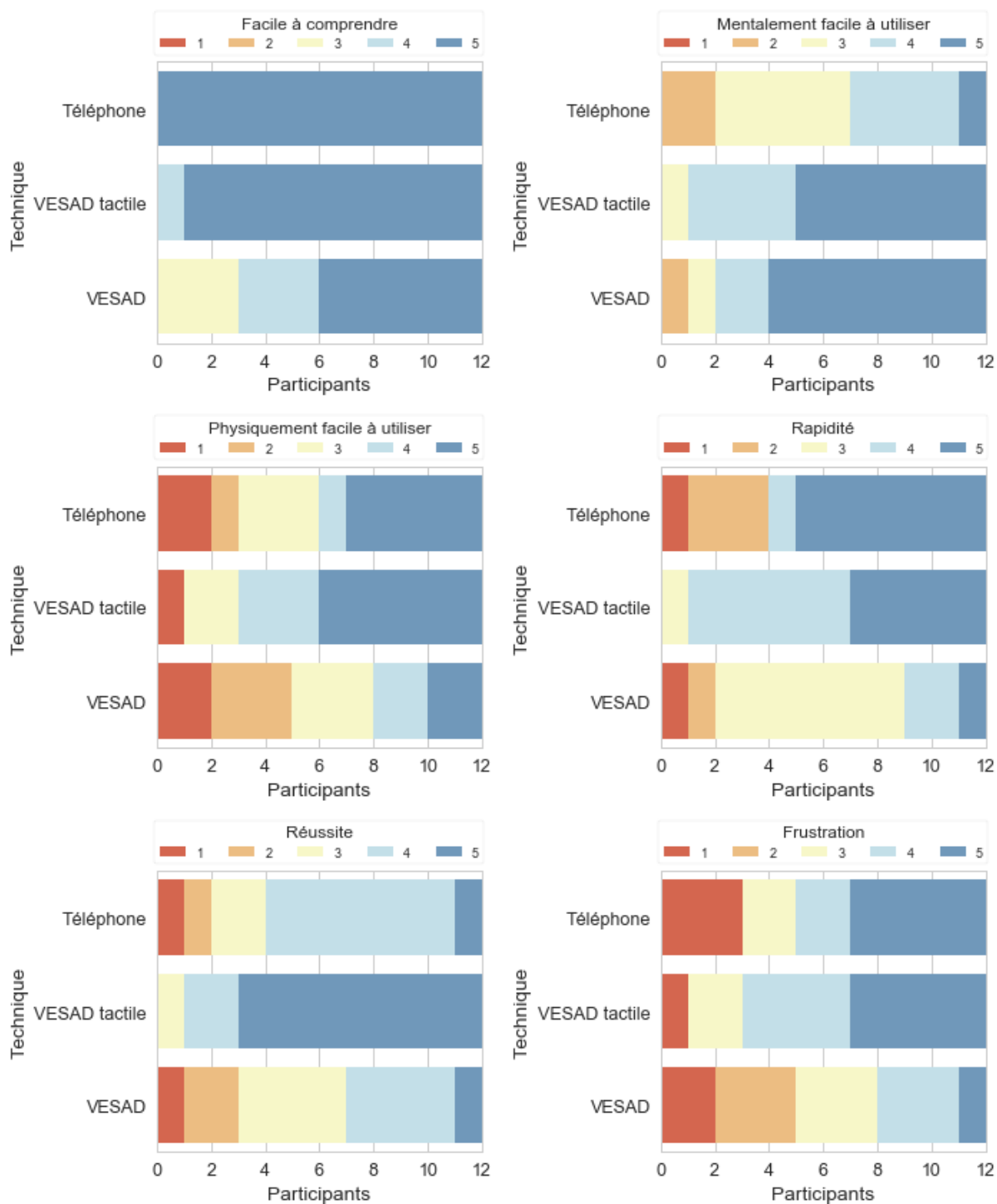
```

We display the rank and preference distributions:

```

In [33]: (fig, axs) = plot_ranks_distributions('technique', ranks_dvs.columns[0:-1])
    fig.savefig('ranks_distributions.png')

```

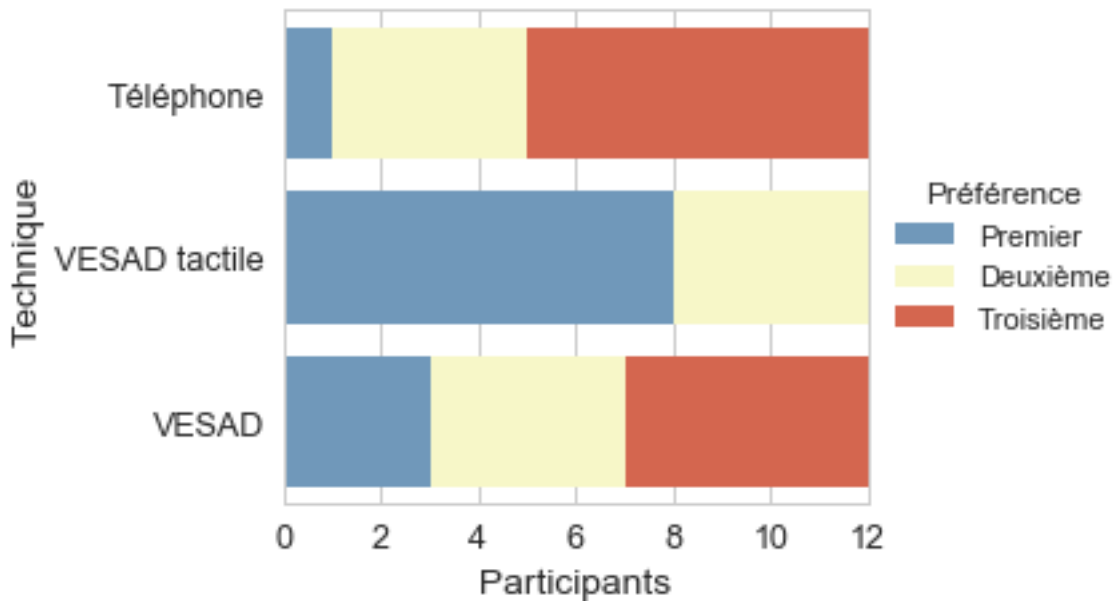


```
In [34]: (fig, axs) = plot_ranks_distributions('technique', ['preference'])
```

```
ax_handles, ax_labels = axs[0].get_legend_handles_labels()
legend = axs[0].legend(ax_handles[::-1], labels['preferences'],
                      loc='center left', bbox_to_anchor=(1, 0.5),
                      title=ranks_dvs['preference']['label'])
```

```
fix_legend_fontsize(legend)

fig.savefig('preferences_distribution.png')
```



We use the Kruskal-Wallis test (Benjamini–Hochberg correction) on each question to check if there is statistical significant differences between the ranks among TECHNIQUE:

```
In [35]: test_ranks('technique', ranks_dvs, correction_method='fdr_bh')
```

```
Out[35]:
```

	Variable indépendante	Variable dépendante	Kruskal-Wallis H \
0	Technique	Facile à comprendre	11.001420
1	Technique	Mentalement facile à utiliser	10.905742
2	Technique	Physiquement facile à utiliser	4.148121
3	Technique	Rapidité	7.130846
4	Technique	Réussite	13.784269
5	Technique	Frustration	4.500057
6	Technique	Préférence	12.638889

	Valeur p
0	0.007497
1	0.007497
2	0.125674
3	0.039599
4	0.006303
5	0.122962
6	0.006303

All the questions, except Physically Easy to Use and Frustration, are statistically significant: Easy to Understand ($p = 0.007$), Mentally Easy to Use ($p = 0.007$), Subjective Speed ($p = 0.04$), Subjective Performance ($p = 0.006$), Preference ($p = 0.006$).

We use then pairwise Mann-Whitney tests (Benjamini–Hochberg correction) for the significant questions above:

```
In [36]: test_pairwise_ranks('technique', ['easy_understand', 'mentally_easy_use',
      'could_go_fast', 'subjective_performance',
      'preference'], correction_method='fdr_bh')
```

```
Out[36]:
```

	Variable indépendante	Valeur VI 1	Valeur VI 2 \
0	Technique	Téléphone	VESAD tactile
1	Technique	Téléphone	VESAD
2	Technique	VESAD tactile	VESAD
3	Technique	Téléphone	VESAD tactile
4	Technique	Téléphone	VESAD
5	Technique	VESAD tactile	VESAD
6	Technique	Téléphone	VESAD tactile
7	Technique	Téléphone	VESAD
8	Technique	VESAD tactile	VESAD
9	Technique	Téléphone	VESAD tactile
10	Technique	Téléphone	VESAD
11	Technique	VESAD tactile	VESAD
12	Technique	Téléphone	VESAD tactile
13	Technique	Téléphone	VESAD
14	Technique	VESAD tactile	VESAD

	Variable dépendante	Différence des moyennes \
0	Facile à comprendre	0.083333
1	Facile à comprendre	0.750000
2	Facile à comprendre	0.666667
3	Mentalement facile à utiliser	-1.166667
4	Mentalement facile à utiliser	-1.083333
5	Mentalement facile à utiliser	0.083333
6	Rapidité	-0.500000
7	Rapidité	0.750000
8	Rapidité	1.250000
9	Réussite	-1.166667
10	Réussite	0.333333
11	Réussite	1.500000
12	Préférence	1.166667
13	Préférence	0.333333
14	Préférence	-0.833333

	Différence des moyennes (%)	Mann-Whitney U	Valeur p
0	1.694915	66.0	0.215732
1	17.647059	36.0	0.008605
2	15.686275	40.5	0.020977
3	-25.925926	23.0	0.005031
4	-24.528302	28.5	0.010151
5	1.886792	69.5	0.475027
6	-11.538462	70.5	0.475027
7	24.324324	48.5	0.126838
8	40.540541	21.0	0.004655
9	-25.000000	22.5	0.004655
10	10.526316	57.0	0.215732
11	47.368421	17.5	0.003904

12	87.500000	16.0	0.003904
13	15.384615	56.0	0.215732
14	-38.461538	32.0	0.013011

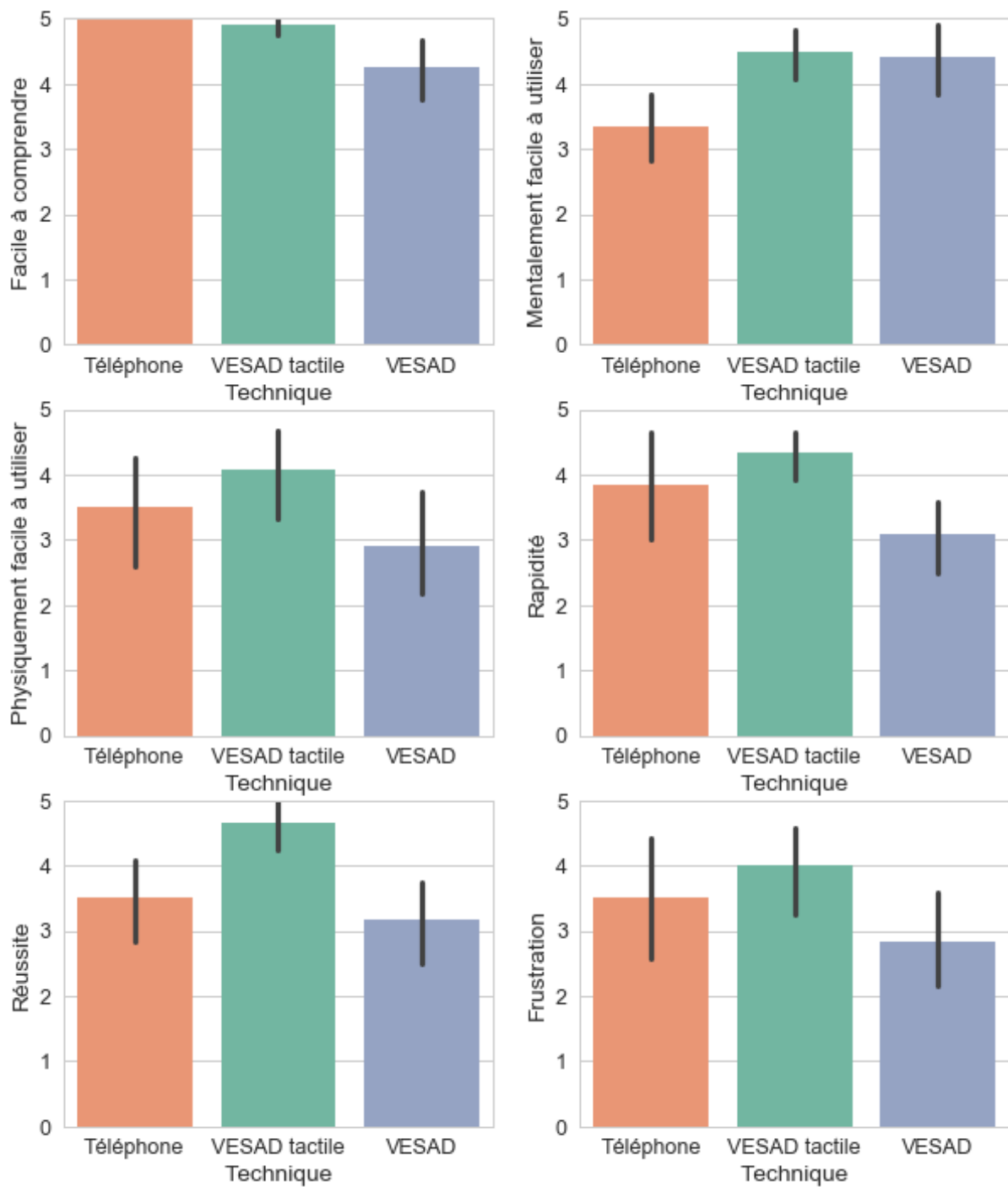
We display the mean and 95% CI of each question:

```
In [37]: ranks.groupby([trials_ivs['technique'] ['label']])\
        .aggregate(print_mean_ci).loc[:, ranks_dvs.loc['label', :]].transpose()
```

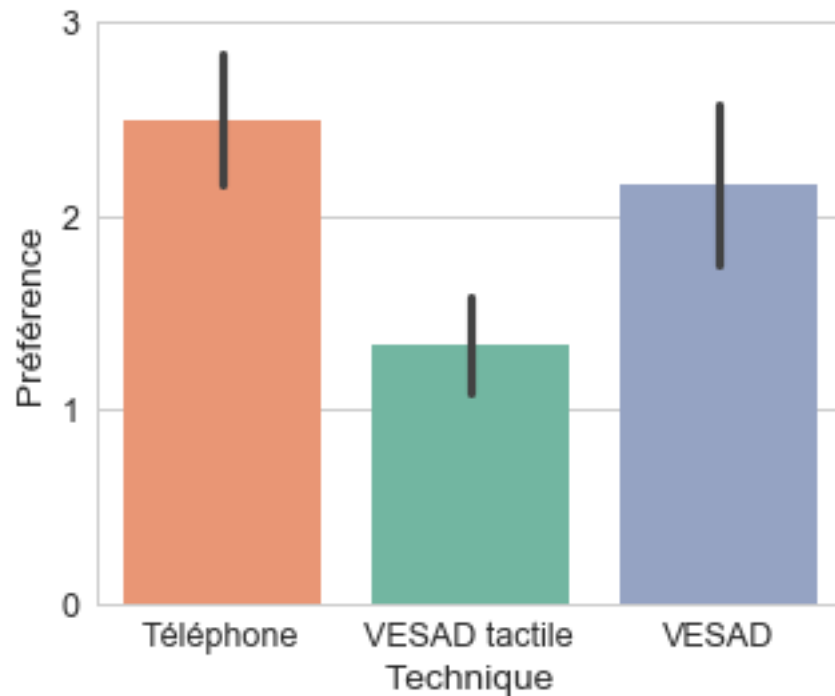
```
Out[37]: Technique          Téléphone          VESAD tactile \
Facile à comprendre      5.00 [5.00, 5.00]  4.92 [4.75, 5.00]
Mentalement facile à utiliser  3.33 [2.83, 3.83]  4.50 [4.08, 4.83]
Physiquement facile à utiliser  3.50 [2.67, 4.33]  4.08 [3.42, 4.67]
Rapidité                  3.83 [2.92, 4.67]  4.33 [4.00, 4.67]
Réussite                  3.50 [2.83, 4.00]  4.67 [4.25, 5.00]
Frustration               3.50 [2.67, 4.33]  4.00 [3.33, 4.58]
Préférence                2.50 [2.17, 2.83]  1.33 [1.08, 1.58]
```

Technique	VESAD
Facile à comprendre	4.25 [3.75, 4.67]
Mentalement facile à utiliser	4.42 [3.83, 4.92]
Physiquement facile à utiliser	2.92 [2.17, 3.67]
Rapidité	3.08 [2.50, 3.58]
Réussite	3.17 [2.58, 3.75]
Frustration	2.83 [2.17, 3.42]
Préférence	2.17 [1.75, 2.58]

```
In [38]: (fig, axs) = plot_ranks('technique', ranks_dvs.columns[0:-1])
fig.savefig('ranks.png')
```



```
In [39]: (fig, axs) = plot_ranks('technique', ['preference'])
fig.savefig('preferences.png')
```



Overall significant results are:

- **Easy to Understand:** *PhoneOnly* is significantly better than *MidAirInArOut* ($p = 0.009$), and seems a little better than *PhoneInArOut*.
- **Physically Easy to Use:** There is no significant differences due to TECHNIQUE; they seem scored similar.
- **Mentally Easy to Use:** *PhoneOnly* is statistically and practically worst than *PhoneInArOut* ($p = 0.005$) and *MidAirInArOut* ($p = 0.01$).
- **Subjective Speed:** *PhoneInArOut* is significantly better than *MidAirInArOut* ($p = 0.05$).
- **Subjective Performance:** *PhoneInArOut* is statistically better than *PhoneOnly* ($p = 0.005$) and *MidAirInArOut* ($p = 0.004$).
- **Frustration:** There is no significant differences due to TECHNIQUE; they seem scored similar.
- **Preference:** *PhoneInArOut* is significantly preferred to *PhoneOnly* ($p = 0.004$) and *MidAirInArOut* ($p = 0.01$).

0.3 3. Participant trials

Some functions for the analysis:

```
In [40]: def trial_samples(iv_id, dv_id, data=trials):
         iv, dv = trials_ivs[iv_id], trials_dvs[dv_id]
         return [data[data[iv['label']] == iv_value][dv]\
                 for iv_value in iv['categorical']]
```

```
In [41]: def trial_means(iv_ids, dv_ids, data=trials):
         iv_labels = [trials_ivs.at['label', iv_id] for iv_id in iv_ids]
         dv_labels = [trials_dvs[dv_id] for dv_id in dv_ids]
         return data.groupby(iv_labels).aggregate(print_mean_ci).loc[:, dv_labels]
```



```

In [42]: def melt_trials(value_vars, var_name, value_name, data=trials):
    return pd.melt(data, id_vars=trials_ivs.loc['label', :],
                    value_vars=value_vars, var_name=var_name,
                    value_name=value_name)

In [43]: def filter_trials_outliers(dv_id, data=trials, nth_percentile_trimed=5):
    dv = trials_dvs[dv_id]
    pmin, pmax = np.nanpercentile(data[dv], [nth_percentile_trimed,
                                              100 - nth_percentile_trimed])
    return data[(np.isnan(data[dv]) == False) & (pmin < data[dv])\
                & (data[dv] < pmax)]

In [44]: def test_pairwise_trials(iv_id, dv_id, data=trials, **args):
    results = []
    iv, dv = trials_ivs[iv_id], trials_dvs[dv_id]
    iv_category_ids = range(len(iv['categorical']))

    samples = trial_samples(iv_id, dv_id, data)
    sample_pairs = itertools.combinations(iv_category_ids, 2)
    for id1, id2 in sample_pairs:
        T, p = stats.ttest_ind(samples[id1], samples[id2])
        mean_diff, mean_diff_per = mean_difference(samples[id1], samples[id2])
        results.append([iv['label'], iv['categorical'][id1],
                        iv['categorical'][id2], dv, mean_diff,
                        mean_diff_per, T, p])

    columns = [labels['iv'], labels['iv_value'] + ' 1',
                labels['iv_value'] + ' 2', labels['dv'],
                labels['mean_difference'], labels['mean_difference_percentage'],
                labels['t_statistic'], labels['p_value']]
    results = pd.DataFrame(results, columns=columns)

    p_values_correction(results, **args)
    return results

In [45]: def test_non_normal_trials(iv_ids, dv_ids, data=trials, **args):
    results = []

    for dv_id in dv_ids:
        for iv_id in iv_ids:
            samples = trial_samples(iv_id, dv_id, data)
            H, p = stats.kruskal(*samples)
            results.append([trials_ivs.at['label', iv_id], trials_dvs[dv_id],
                            H, p])

    results = pd.DataFrame(results, columns=[labels['iv'], labels['dv'],
                                              'Kruskal-Wallis H',
                                              labels['p_value']])
    p_values_correction(results, **args)
    return results

```

```

In [46]: def test_pairwise_non_normal_trials(iv_ids, dv_ids, data=trials, **args):
    results = []

    for dv_id in dv_ids:
        for iv_id in iv_ids:
            iv, dv = trials_ivs[iv_id], trials_dvs[dv_id]
            samples = trial_samples(iv_id, dv_id, data)

            iv_category_ids = range(len(iv['categorical']))
            sample_pairs = itertools.combinations(iv_category_ids, 2)
            for id1, id2 in sample_pairs:
                U, p = stats.mannwhitneyu(samples[id1], samples[id2])
                mean_diff, mean_diff_per = mean_difference(samples[id1],
                                                            samples[id2])
                results.append([iv['label'], iv['categorical'][id1],
                               iv['categorical'][id2], dv, mean_diff,
                               mean_diff_per, U, p])

    columns = [labels['iv'], labels['iv_value'] + ' 1',
               labels['iv_value'] + ' 2', labels['dv'],
               labels['mean_difference'], labels['mean_difference_percentage'],
               'Mann-Whitney U', labels['p_value']]
    results = pd.DataFrame(results, columns=columns)
    p_values_correction(results, **args)
    return results

In [47]: def plot_trials(iv_ids_list, dv_id, data=trials, kind='bar', **args):
    dv = trials_dvs[dv_id]
    if (len(iv_ids_list) == 0):
        iv_ids_list = [[iv_id] for id_id in trials_ivs.columns]

    fig, axs = subplots(len(iv_ids_list))
    for id_ids, ax in zip(iv_ids_list, axs):

        ivs = [trials_ivs[id_id] for id_id in id_ids]
        if (len(ivs) == 1):
            iv = ivs[0]

            if (kind == 'bar'):
                sns.barplot(x=iv['label'], y=dv, data=data,
                           palette=iv['palette'], ax=ax, **args)

            elif (kind == 'box'):
                sns.boxplot(x=iv['label'], y=dv, data=data,
                           palette=iv['palette'], ax=ax, **args)

            elif (kind == 'count'):
                sns.countplot(hue=iv['label'], x=dv, data=data,
                             palette=iv['palette'], ax=ax, **args)
                ax.set(ylabel='Count')
                ax.legend(loc='upper right', title=labels['count'],

```

```

        frameon=True)

    elif (len(ivs) == 2):
        if (kind == 'bar'):
            sns.barplot(x=ivs[1]['label'], y=dv, hue=ivs[0]['label'],
                        data=data, palette=ivs[0]['palette'], ax=ax, **args)
            ax.legend(frameon=True, loc='upper left', bbox_to_anchor=(1, 1))

    return (fig, axs)

```

0.3.1 3.1. Task completion time

We perform a full factorial ANOVA with the model: $TCT \sim \text{TECHNIQUE} \times \text{TEXT_SIZE} \times \text{DISTANCE} + \text{TECHNIQUE} \times \text{ORDERING}$.

We should test all the assumptions of an ANOVA : independence of measure points, normality, homogeneity of variance. The trials are independent from each other, since they are generated randomly. The data is non-normal, but the ANOVA can tolerate non-normal data with skewed distribution. The homogeneity of variance is less important when the sample sizes are equal.

```

In [48]: tct_model = ols('total_time ~ technique * text_size * distance'
                        + '+ technique * ordering', data=trials_for_anova).fit()
sm.stats.anova_lm(tct_model, typ=2)

```

```

Out[48]:

```

	sum_sq	df	F	PR(>F)
technique	256284.863291	2.0	52.727496	4.664381e-20
text_size	6524.396184	1.0	2.684630	1.024855e-01
distance	273.284406	1.0	0.112450	7.376324e-01
ordering	12606.272262	2.0	2.593587	7.661302e-02
technique:text_size	10779.057863	2.0	2.217660	1.108428e-01
technique:distance	1129.444917	2.0	0.232370	7.928115e-01
text_size:distance	10418.141005	1.0	4.286812	3.935962e-02
technique:ordering	47629.511187	4.0	4.899597	7.897650e-04
technique:text_size:distance	17350.562563	2.0	3.569667	2.950225e-02
Residual	656174.846745	270.0	NaN	NaN

The main significant effect on TCT is TECHNIQUE ($F = 52.7$, $p < 0.0001$). There is also interaction effects: TEXT_SIZE x DISTANCE ($F = 4.3$, $p = 0.04$), TECHNIQUE x ORDERING ($F = 4.9$, $p = 0.0007$) and TECHNIQUE x TEXT_SIZE x DISTANCE ($F = 3.0$, $p = 0.03$).

We display mean TCT values with 95% CI for these conditions:

```

In [49]: trial_means(['technique'], ['total_time'])

```

```

Out[49]:

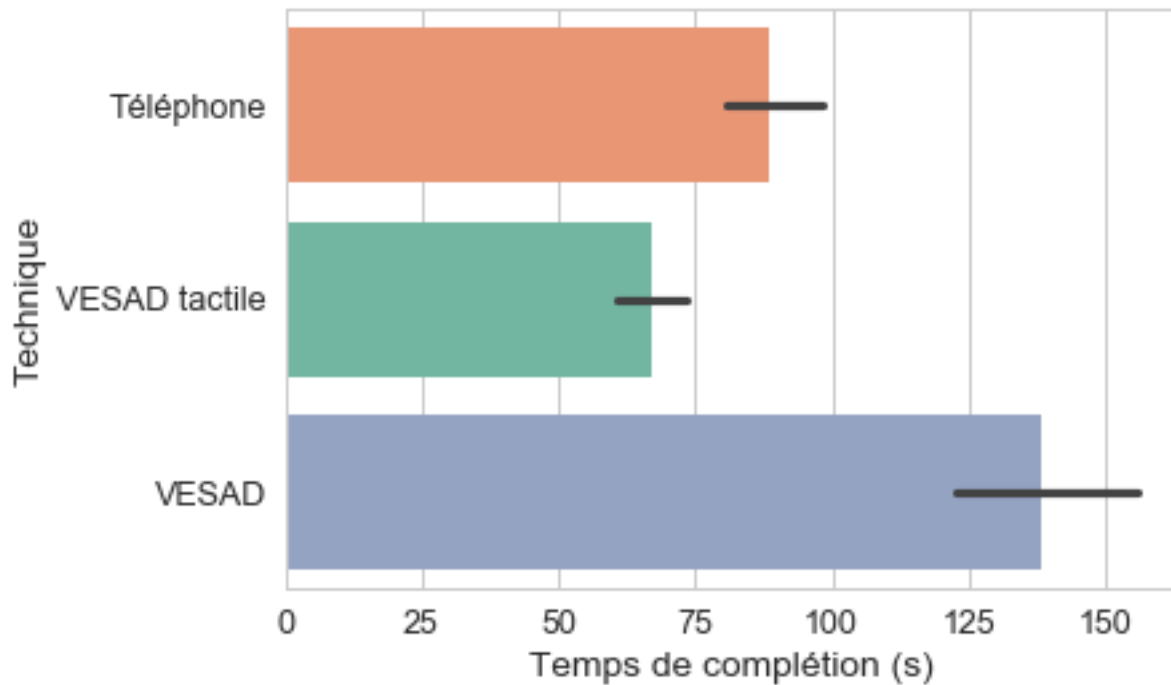
```

	Temps de complétion (s)
Technique	
Téléphone	88.70 [79.44, 97.51]
VESAD tactile	66.86 [60.82, 73.78]
VESAD	138.17 [121.86, 156.24]

```

In [50]: ax = sns.barplot(x=trials_dvs['total_time'], y=technique['label'],
                        palette=technique['palette'], data=trials)
ax.get_figure().savefig('tct.png')

```



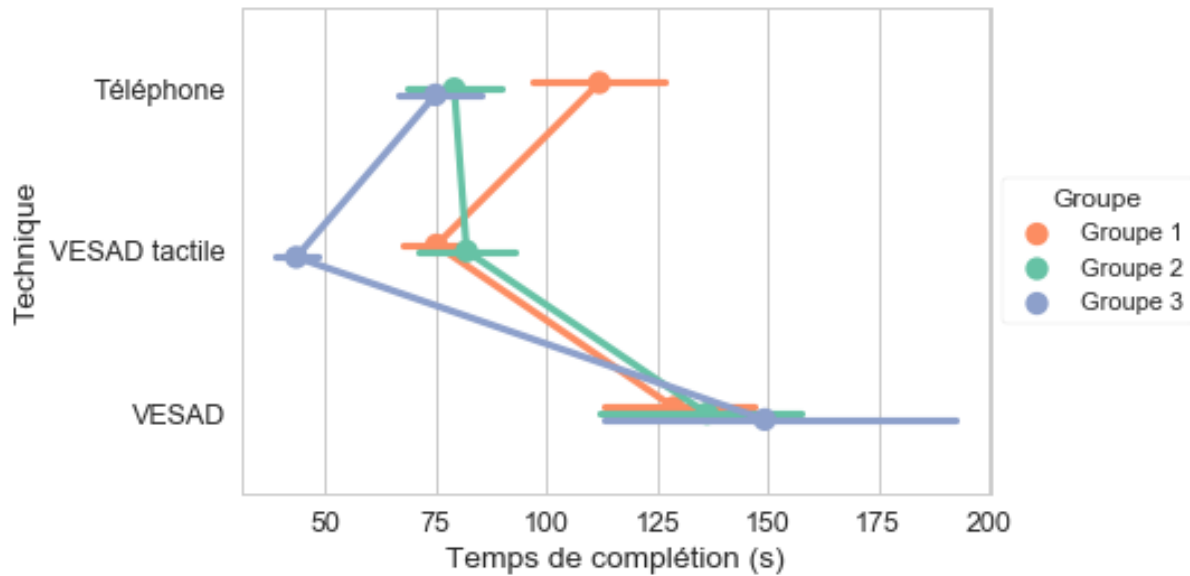
```
In [51]: trial_means(['ordering', 'technique'], ['total_time']).unstack()
```

```
Out[51]:
```

		Temps de complétion (s)		
Technique		Téléphone	VESAD tactile	\
Groupe				
Groupe 1		111.98 [95.69, 129.01]	75.15 [67.83, 82.57]	
Groupe 2		79.19 [69.86, 90.43]	81.97 [71.06, 92.69]	
Groupe 3		74.93 [66.13, 85.17]	43.46 [38.51, 48.20]	

Technique	VESAD
Groupe	
Groupe 1	128.82 [111.16, 146.32]
Groupe 2	136.32 [112.82, 157.68]
Groupe 3	149.36 [114.44, 190.34]

```
In [52]: ax = sns.pointplot(x=trials_dvs['total_time'], y=technique['label'],
                             hue=ordering['label'], palette=ordering['palette'],
                             data=trials, dodge=True)
config_legend(ax, 'ordering')
ax.get_figure().savefig('tct_ordering.png')
```



It seems that participants who started with *PhoneOnly* were slower with this technique than the other groups. Similarly, participants who finished with *PhoneInArOut* were faster with this technique. It indicates there is a learning curve on the task, but interestingly participants from all groups performed equally with *MidAirInArOut* technique.

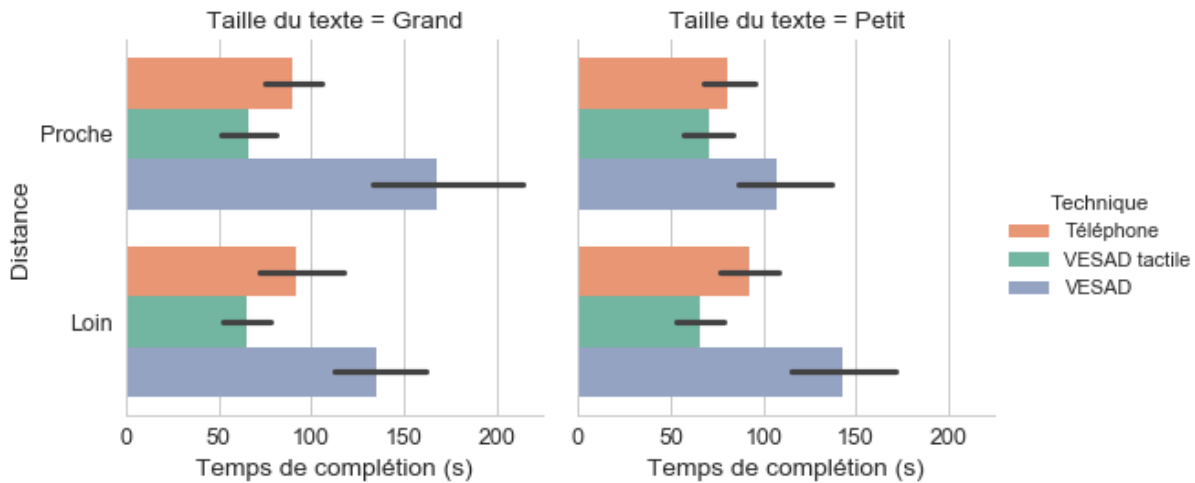
```
In [53]: trial_means(['text_size', 'distance', 'technique'], ['total_time']).unstack()
```

```
Out[53]:
```

Technique		Temps de complétion (s)		
				\
		Téléphone	VESAD tactile	
Taille du texte	Distance			
	Grand	Proche 89.98 [73.86, 105.05]	65.81 [52.90, 80.86]	
		Loin 92.24 [71.66, 114.40]	65.35 [52.55, 77.78]	
	Petit	Proche 80.44 [67.00, 94.63]	70.61 [58.01, 83.72]	
	Loin 92.13 [76.62, 110.48]	65.67 [53.22, 79.23]		

Technique		VESAD	
Taille du texte	Distance		
	Grand	Proche 167.33 [131.76, 216.83]	
		Loin 135.29 [111.80, 162.08]	
	Petit	Proche 107.43 [84.19, 136.76]	
	Loin 142.61 [115.30, 169.66]		

```
In [54]: g = sns.factorplot(x=trials_dvs['total_time'], y=distance['label'],
                             col=text_size['label'], hue=technique['label'],
                             data=trials, palette=technique['palette'], kind='bar')
g.savefig('tct_2.png')
```



Interactions on TCT due to TEXT_SIZE x DISTANCE don't seem important.

We compare the TCT for the three techniques only with pairwise t-tests (Benjamini–Hochberg correction).

```
In [55]: test_pairwise_trials('technique', 'total_time', correction_method='fdr_bh')
```

```
Out[55]:
```

Variable indépendante	Valeur VI 1	Valeur VI 2	
0	Technique	Téléphone	VESAD tactile
1	Technique	Téléphone	VESAD
2	Technique	VESAD tactile	VESAD

Variable dépendante	Différence des moyennes	
0 Temps de complétion (s)	21.840362	
1 Temps de complétion (s)	-49.467731	
2 Temps de complétion (s)	-71.308093	

	Différence des moyennes (%)	Statistique T	Valeur p
0	32.666819	3.891218	1.862003e-04
1	-35.803106	-5.143480	2.201995e-06
2	-51.610437	-7.746559	3.247150e-11

Results:

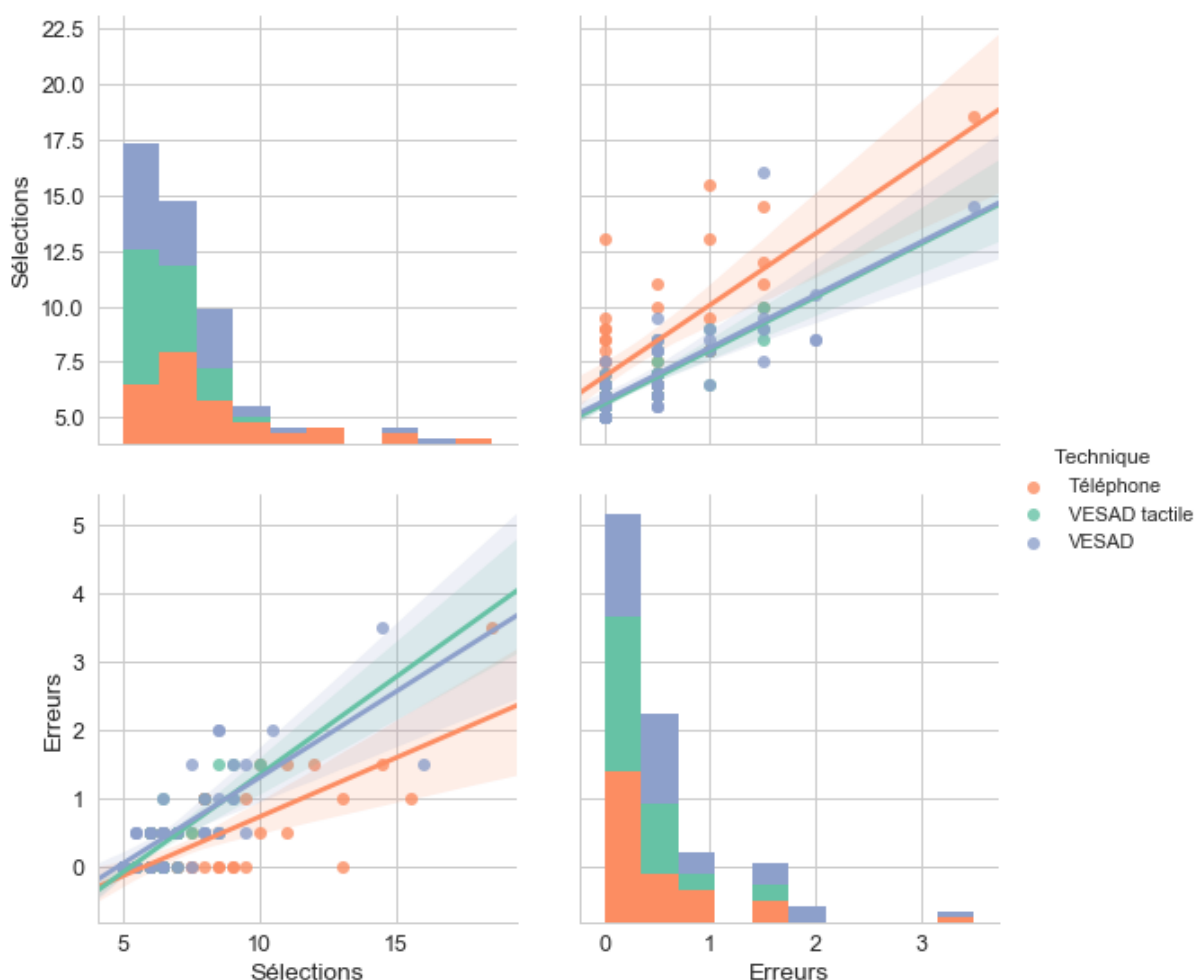
- *PhoneInArOut* is 71s (+52%) faster than *MidAirInArOut* ($p < 0.0001$).
- *PhoneOnly* is 49s (+36%) faster than *MidAirInArOut* ($p < 0.0001$).
- *PhoneInArOut* is 22s (+33%) faster than *PhoneOnly* ($p = 0.0004$).

Differences due to interactions don't seem important.

0.3.2 3.2. Errors

We visualize first the SELECTIONS and ERRORS distributions:

```
In [56]: g = sns.pairplot(trials, hue=technique['label'], kind='reg',
                          vars=[trials_dvs['selections_count'], trials_dvs['errors']],
                          palette=technique['palette'], size=4);
g.savefig('selections_errors_distributions.png')
```



It seems that a user makes as much errors as she makes selections. The relation is almost the same for each technique, even if users seems to make more selections for the same number of errors with PhoneOnly.

We can't use ANOVA on SELECTIONS and ERRORS variables as their distributions are exponentials. We use instead the Kruskal-Wallis test (Benjamini–Hochberg correction) to check if there is significative differences due to TECHNIQUE, TEXT_SIZE, DISTANCE or ORDERING.

```
In [57]: test_non_normal_trials(['technique', 'text_size', 'distance', 'ordering'],
                                ['selections_count', 'errors'])
```

```
Out[57]:
```

	Variable indépendante	Variable dépendante	Kruskal-Wallis H	Valeur p
0	Technique	Sélections	15.125918	0.004155
1	Taille du texte	Sélections	0.003897	0.950224
2	Distance	Sélections	0.052701	0.935347
3	Groupe	Sélections	11.510535	0.010095
4	Technique	Erreurs	5.201541	0.148433
5	Taille du texte	Erreurs	0.103661	0.935347
6	Distance	Erreurs	0.201599	0.935347
7	Groupe	Erreurs	11.153096	0.010095

Only TECHNIQUE ($p = 0.004$) and ORDERING ($p = 0.01$) have a significant effect on SELECTIONS. But, only ORDERING ($p = 0.01$) have a significant effect on ERRORS.

We use then pairwise Mann-Whitney tests (Benjamini–Hochberg correction) for the significant questions above:

```
In [58]: test_pairwise_non_normal_trials(['technique', 'ordering'],
                                         ['selections_count', 'errors'])
```

```
Out[58]:
```

	Variable indépendante	Valeur VI 1	Valeur VI 2	Variable dépendante \
0	Technique	Téléphone	VESAD tactile	Sélections
1	Technique	Téléphone	VESAD	Sélections
2	Technique	VESAD tactile	VESAD	Sélections
3	Groupe	Groupe 1	Groupe 2	Sélections
4	Groupe	Groupe 1	Groupe 3	Sélections
5	Groupe	Groupe 2	Groupe 3	Sélections
6	Technique	Téléphone	VESAD tactile	Erreurs
7	Technique	Téléphone	VESAD	Erreurs
8	Technique	VESAD tactile	VESAD	Erreurs
9	Groupe	Groupe 1	Groupe 2	Erreurs
10	Groupe	Groupe 1	Groupe 3	Erreurs
11	Groupe	Groupe 2	Groupe 3	Erreurs

	Différence des moyennes	Différence des moyennes (%)	Mann-Whitney U \
0	1.864583	29.537954	627.0
1	1.041667	14.598540	864.5
2	-0.822917	-11.532847	915.0
3	1.729167	26.265823	755.0
4	1.583333	23.529412	755.0
5	-0.145833	-2.167183	1136.0
6	0.125000	42.857143	1083.5
7	-0.166667	-28.571429	957.0
8	-0.291667	-50.000000	873.0
9	0.333333	103.225806	846.5
10	0.343750	110.000000	761.5
11	0.010417	3.333333	1039.0

	Valeur p
0	0.000635
1	0.029356
2	0.059881
3	0.005196
4	0.005196
5	0.454285
6	0.312007
7	0.083050
8	0.026306
9	0.020183
10	0.005196
11	0.205336

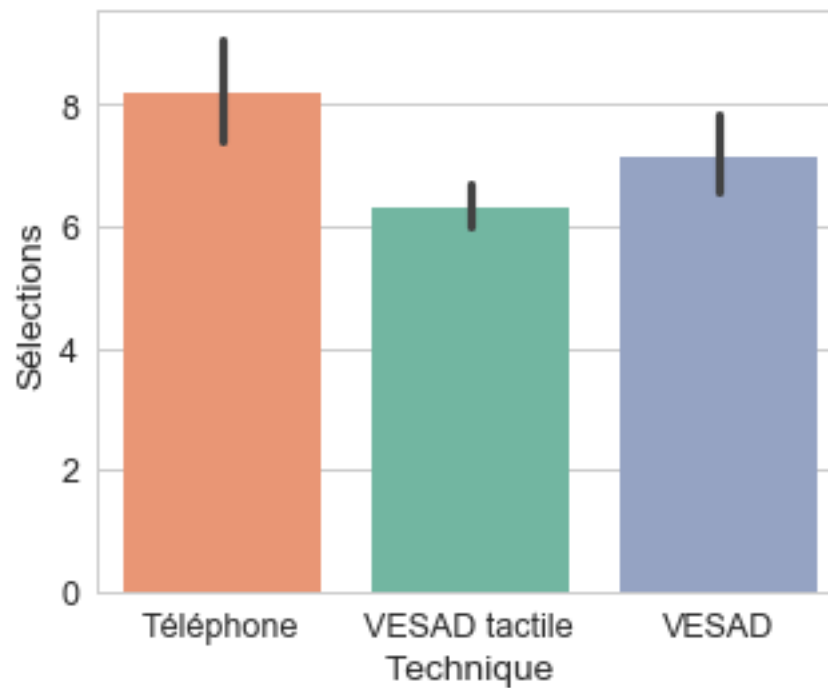
```
In [59]: trial_means(['technique'], ['selections_count', 'errors'])
```

```
Out[59]:
```

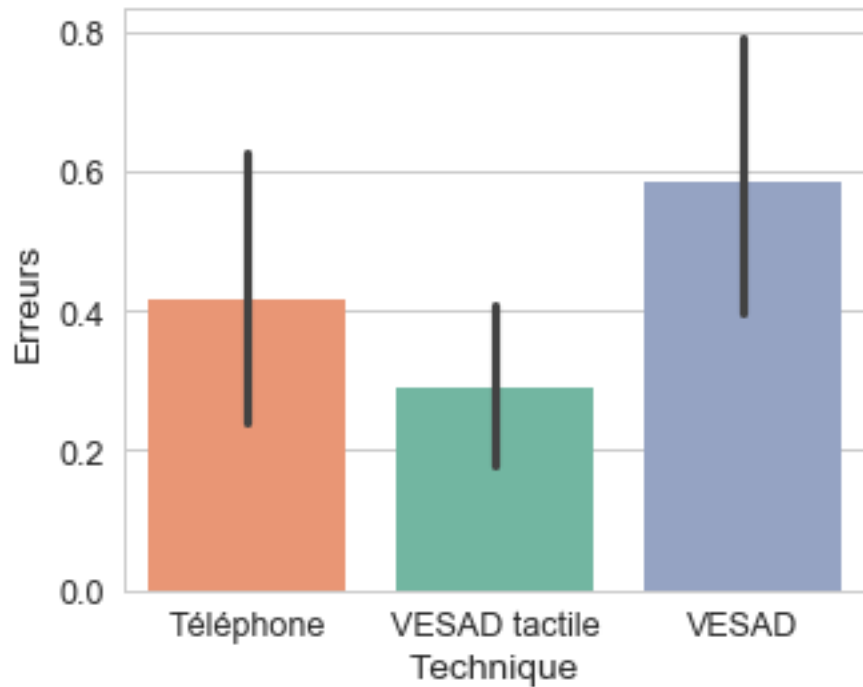
	Sélections	Erreurs
Technique		

Téléphone	8.18 [7.46, 9.03]	0.42 [0.24, 0.61]
VESAD tactile	6.31 [5.98, 6.68]	0.29 [0.18, 0.41]
VESAD	7.14 [6.54, 7.83]	0.58 [0.39, 0.81]

```
In [60]: (fig, axs) = plot_trials([['technique']], 'selections_count')
fig.savefig('selections.png')
```



```
In [61]: (fig, axs) = plot_trials([['technique']], 'errors')
fig.savefig('errors.png')
```

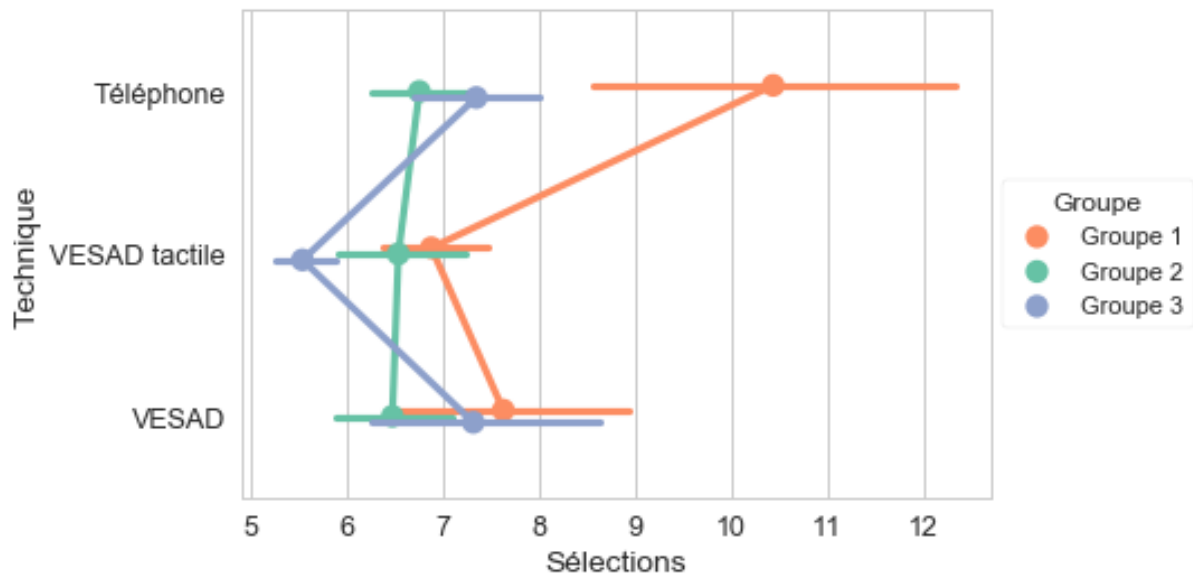


```
In [62]: trial_means(['ordering', 'technique'], ['selections_count', 'errors'])
```

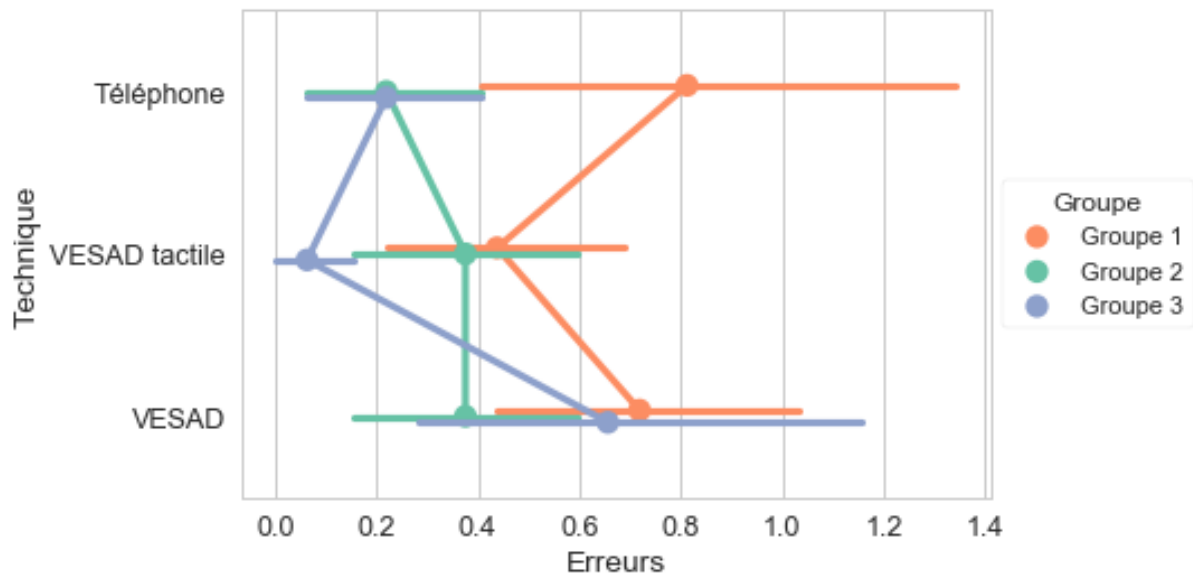
```
Out[62]:
```

		Sélections	Erreurs
Groupe 1	Téléphone	10.44 [8.75, 12.34]	0.81 [0.44, 1.31]
	VESAD tactile	6.88 [6.38, 7.47]	0.44 [0.22, 0.69]
	VESAD	7.62 [6.50, 9.12]	0.72 [0.41, 1.03]
Groupe 2	Téléphone	6.75 [6.25, 7.31]	0.22 [0.06, 0.41]
	VESAD tactile	6.53 [5.88, 7.25]	0.38 [0.16, 0.62]
	VESAD	6.47 [5.84, 7.19]	0.38 [0.16, 0.62]
Groupe 3	Téléphone	7.34 [6.75, 8.06]	0.22 [0.06, 0.41]
	VESAD tactile	5.53 [5.25, 5.88]	0.06 [0.00, 0.16]
	VESAD	7.31 [6.22, 8.62]	0.66 [0.25, 1.19]

```
In [63]: ax = sns.pointplot(x=trials_dvs['selections_count'], y=technique['label'],
                             hue=ordering['label'], palette=ordering['palette'],
                             data=trials, dodge=True)
config_legend(ax, 'ordering')
ax.get_figure().savefig('selections_ordering.png')
```



```
In [64]: ax = sns.pointplot(x=trials_dvs['errors'], y=technique['label'],
                             hue=ordering['label'], palette=ordering['palette'],
                             data=trials, dodge=True)
config_legend(ax, 'ordering')
ax.get_figure().savefig('errors_ordering.png')
```



0.3.3 3.3. Navigation

Variable meanings:

- Selection Time = time spent looking for where to drop an item that had been picked

- Selection Distance = distance travelled by the finger with an item selected
- Head Phone Distance = sum of the distance between the head and the phone

In [65]: *# Data preparation*

```
trial_counts = melt_trials(var_name=labels['category'],
                           value_name=labels['count'],
                           value_vars=[trials_dvs['pan_count'],
                                       trials_dvs['zoom_count']])

trial_times = melt_trials(var_name=labels['category'],
                          value_name=labels['time'],
                          value_vars=[trials_dvs['selections_time'],
                                      trials_dvs['pan_time'],
                                      trials_dvs['zoom_time']])

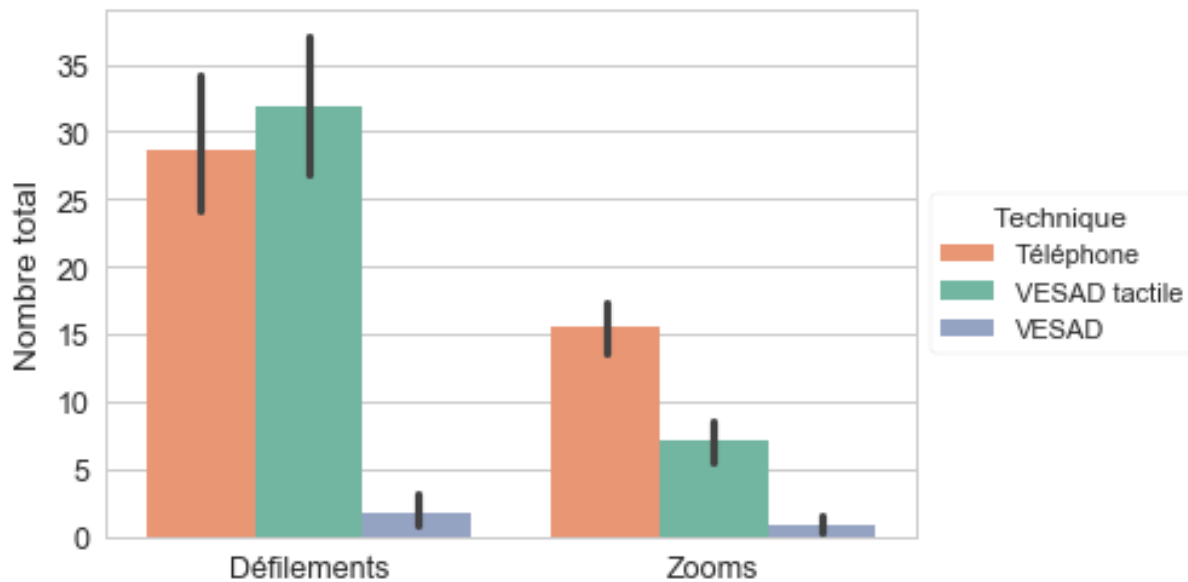
trial_distances_dvs = [trials_dvs['selections_projected_distance'],
                      trials_dvs['pan_projected_distance'],
                      trials_dvs['zoom_projected_distance'],
                      trials_dvs['absolute_head_phone_distance']]
trial_distances = melt_trials(var_name=labels['category'],
                              value_name=labels['distance'],
                              value_vars=trial_distances_dvs)
```

In [66]: trial_means(['technique'], ['pan_count', 'zoom_count'])

Out[66]:

	Défilements	Zooms
Technique		
Téléphone	28.70 [24.02, 33.95]	15.53 [13.68, 17.50]
VESAD tactile	31.81 [26.34, 36.75]	7.14 [5.71, 8.78]
VESAD	1.83 [0.82, 3.04]	0.83 [0.29, 1.52]

```
In [67]: ax = sns.barplot(x=labels['category'], y=labels['count'],
                          hue=technique['label'], palette=technique['palette'],
                          data=trial_counts)
config_legend(ax, 'technique')
ax.set(xlabel='')
ax.get_figure().savefig('navigation_count.png')
```



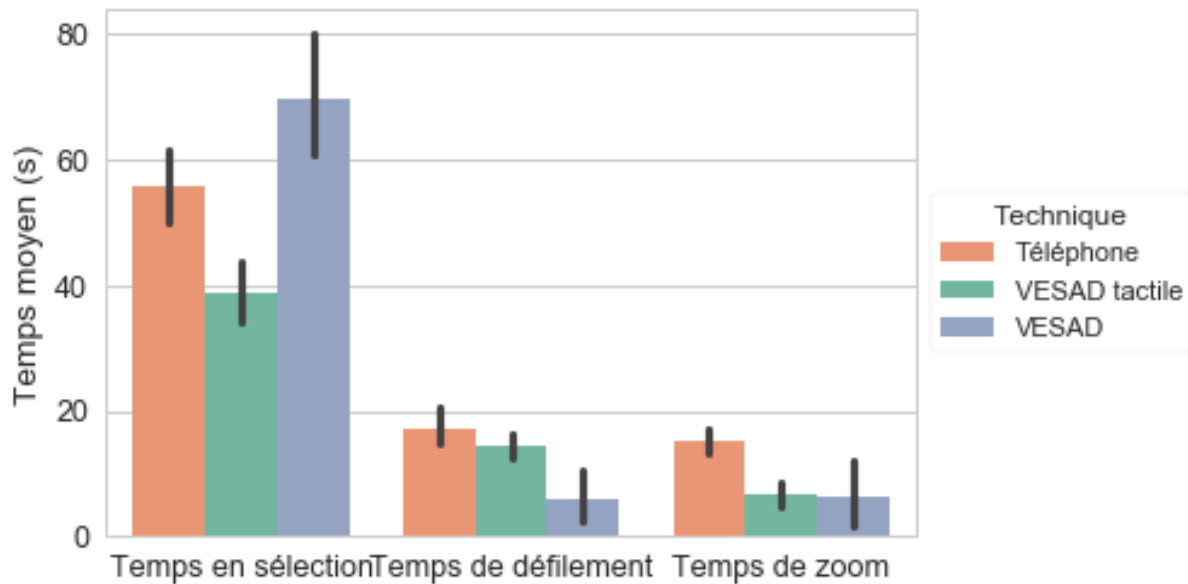
```
In [68]: trial_means(['technique'], ['selections_time', 'pan_time', 'zoom_time'])
```

```
Out[68]:
```

	Temps en sélection		Temps de défilement \	
Technique				
Téléphone	55.74	[49.67, 62.01]	17.12	[14.76, 19.92]
VESAD tactile	38.98	[34.49, 43.86]	14.53	[12.59, 16.69]
VESAD	69.68	[60.93, 79.01]	5.97	[2.43, 10.61]

	Temps de zoom	
Technique		
Téléphone	15.18	[13.08, 17.17]
VESAD tactile	6.70	[4.99, 8.57]
VESAD	6.24	[1.57, 12.36]

```
In [69]: ax = sns.barplot(x=labels['category'], y=labels['time'], data=trial_times,
                           hue=technique['label'], palette=technique['palette'])
config_legend(ax, 'technique')
ax.set(xlabel='')
ax.get_figure().savefig('navigation_time.png')
```



```
In [70]: trial_means(['technique'], ['selections_projected_distance',
                                     'pan_projected_distance',
                                     'zoom_projected_distance',
                                     'absolute_head_phone_distance'])
```

```
Out[70]:
```

	Distance en sélection	Distance de défilement	Distance de zoom \
Technique			
Téléphone	4.87 [4.03, 5.72]	1.50 [1.20, 1.85]	2.11 [1.74, 2.54]
VESAD tactile	2.83 [2.36, 3.29]	1.09 [0.91, 1.29]	0.69 [0.51, 0.89]
VESAD	8.72 [7.16, 10.37]	0.47 [0.19, 0.86]	0.62 [0.16, 1.19]

```
Mouvements tête-téléphone
```

Technique	
Téléphone	3.18 [2.34, 4.07]
VESAD tactile	1.57 [1.25, 1.92]
VESAD	6.12 [4.86, 7.61]

```
In [71]: g = sns.factorplot(x=technique['label'], y=labels['distance'],
                             col=labels['category'], data=trial_distances,
                             palette=technique['palette'], kind='bar', col_wrap=2)
```

```
g.set_titles('{col_name}') # Replace subplot titles
for ax in g.axes:
    ax.title.set_position([0.5, -0.12])
```

```
g.set_axis_labels('') # Custom legend
g.set_xticklabels([])
legend_handles = [patches.Patch(color=color, label=value)\
                   for value, color in zip(technique['categorical'],
                                           technique['palette'])]
```

```

legend = plt.legend(handles=legend_handles, loc='center left',
                    bbox_to_anchor=(1, 1.1), title=technique['label'])
fix_legend_fontsize(legend)

g.savefig('navigation_distance.png')

```

