Handheld VESAD Analysis

June 21, 2018

The analysis of the experiment data is also accessible online: https://github.com/NormandErwan/HandheldVesadAnalysis/blob/master/Handheld%20VESAD%20Analysis.ipynb.

0.1 1. Data preparation

Configuration:

```
In [1]: # Imports
       import numpy as np
       import pandas as pd
       from pandas.api.types import CategoricalDtype
       import itertools
       import seaborn as sns
        import matplotlib as mpl
        import matplotlib.pyplot as plt
        import matplotlib.ticker as ticker
        import matplotlib.patches as patches
       from scipy import stats
       import statsmodels.api as sm
       from statsmodels.formula.api import ols
       from statsmodels.stats.multicomp import (MultiComparison, pairwise_tukeyhsd)
       from statsmodels.stats.multitest import multipletests
       from statsmodels.stats.libqsturng import psturng
       from ast import literal_eval
       from os import listdir
       from os.path import join
       from IPython.html.services.config import ConfigManager
In [2]: # Notebook configuration
       %matplotlib inline
        # Ruler
       ip = get_ipython()
        cm = ConfigManager(parent=ip)
        cm.update('notebook', {"ruler_column": [80]})
```

Data are loaded in the following variables: - Participants information, from the questionary before the trials: participants - The summary of the trials of the participants: raw_trials - Trials averaged so that each participants ends up with a single observation (there was two trials per condition per participant) (Tip 9 of Dragicevic (2016)): trials - The detailed measures of the trials: trial_details - The ranks of the participants from the post-questionary: ranks

Creates independent variables lists (participants_ivs, trials_ivs) and dependent variables lists (ranks_dvs, trials_dvs) to make easier to use algorithms and to plot figures.

```
In [5]: # Participants IVs
        if language == 'Français':
            participants_iv_labels = ['Numéro participant', 'Sexe',
                                       'Porte des lunettes', 'Porte des lentilles',
                                       'Est daltonien', 'Intervalle d\'âge',
                                       'Main dominante', 'Main utilisée pour la souris',
                                       'Activité principale',
                                       'Utilisation de l\'ordinateur (heures/jours)',
                                       'Logiciels 3D utilisés',
                                       'Visiocasques RV/RA utilisés',
                                       'Techniques d\'interactions RV/RA utilisées']
        else:
            participants_iv_labels = ['Participant Id', 'Sex', 'Has Glasses',
                                       'Has Contact Lenses', 'Is Color Blind',
                                       'Age Class', 'Dominant Hand',
                                       'Hand Used for Mouse', 'Activity',
                                       'Computer Hours per Day', '3D Softwares Used',
```

```
'HMD Used'.
                                      'Known Interactions Techniques on HMD']
       participants_ivs = pd.Series(data=participants_iv_labels,
                                     index=participants.columns)
In [6]: # Trials IVs
        if language == 'Français':
            trials_iv_labels = ['Technique', 'Taille du texte', 'Distance', 'Groupe',
                                'Méthode d\'entrée', 'Méthode d\'affichage']
        else:
           trials_iv_labels = ['Technique', 'Text Size', 'Distance', 'Ordering',
                                'Technique Input', 'Technique Output']
       trials_ivs = ['technique', 'text_size',
                      'distance', 'ordering', 'input', 'output']
       trials_ivs = pd.DataFrame(columns=trials_ivs,\)
                                  index=['label', 'categorical', 'palette'])
       default_palette = sns.color_palette('Set2', 8)
       for iv_index, iv_label in zip(trials_ivs.columns, trials_iv_labels):
            iv_categories = raw_trials.sort_values([iv_index + '_id'])\
            .drop_duplicates(iv_index)[iv_index]
            iv_categorical = pd.Categorical(iv_categories, iv_categories, ordered=True)
            trials_ivs[iv_index] = [iv_label, iv_categorical, default_palette]
       technique_palette = [default_palette[1], default_palette[0], default_palette[2]]
       trials_ivs.at['palette', 'technique'] = technique_palette
       trials_ivs.at['palette', 'text_size'] = sns.light_palette(
            default_palette[6], 3)[1:3] # Brown paired colors
       trials_ivs.at['palette', 'distance'] = sns.light_palette(
            default_palette[4], 3)[1:3] # Green paired colors
        trials_ivs.at['palette', 'ordering'] = technique_palette
        trials_ivs.at['palette', 'input'] = [default_palette[5], default_palette[2]]
       trials_ivs.at['palette', 'output'] = [default_palette[0],
                                              sns.color_palette('muted')[5]]
In [7]: # Trials DVs
        if language == 'Français':
            trials_dv_labels = ['Temps de complétion (s)', 'Sélections',
                                'Temps en sélection', 'Distance 3D en sélection',
                                'Distance en sélection', 'Déselections', 'Erreurs',
                                'Disques classés', 'Défilements', 'Temps de défilement',
                                'Distance 3D de défilement', 'Distance de défilement',
                                'Zooms', 'Temps de zoom', 'Distance 3D de zoom',
                                'Distance de zoom', 'Mouvements tête-téléphone',
                                'Distance relative tête-téléphone']
        else:
           trials_dv_labels = ['Task Completion Time (s)', 'Selections',
                                'Selection Time', 'Selection Distance',
```

```
'Selection Distance on Grid', 'Deselections', 'Errors',
                                'Items Classified', 'Pans', 'Pan Time', 'Pan Distance',
                                'Pan Distance on Grid', 'Zooms', 'Zoom Time',
                                'Zoom Distance', 'Zoom Distance on Grid',
                                'Phone-Head Motion', 'Signed Phone-Head Motion']
       trials_dvs = raw_trials.loc[:, 'total_time':'signed_head_phone_distance'].columns
       trials_dvs = pd.Series(data=trials_dv_labels, index=trials_dvs)
In [8]: # Ranks DVs
        if language == 'Français':
            ranks_dv_labels = ['Facile à comprendre', 'Mentalement facile à utiliser',
                               'Physiquement facile à utiliser', 'Rapidité', 'Réussite',
                               'Frustration', 'Préférence']
        else:
            ranks_dv_labels = ['Easy to Understand', 'Mentally Easy to Use',
                               'Physically Easy to Use', 'Subjective Speed',
                               'Subjective Performance', 'Frustration', 'Preference']
       ranks_dv_scales = [pd.Categorical(list(range(1, 6)), list(
            range(1, 6)), ordered=True)] * len(ranks_dv_labels)
       RdYlBu = sns.color_palette('RdYlBu', 5)
       ranks_dv_palettes = [sns.color_palette('RdYlBu', 5)] * len(ranks_dv_labels)
       ranks_dvs = ranks.loc[:, 'easy_understand':'preference'].columns
       ranks_dvs = pd.DataFrame(data=[ranks_dv_labels, ranks_dv_scales,
                                       ranks_dv_palettes],
                                 columns=ranks_dvs, index=['label', 'scale', 'palette'])
       ranks_dvs.at['scale', 'preference'] = pd.Categorical(
            list(range(1, 4)), list(range(1, 4)), ordered=True)
       ranks_dvs.at['palette', 'preference'] = [RdYlBu[4], RdYlBu[2], RdYlBu[0]]
In [9]: # Shortcuts
       participant_id = participants_ivs['participant_id']
       technique = trials ivs['technique']
       text_size = trials_ivs['text_size']
       distance = trials_ivs['distance']
        ordering = trials_ivs['ordering']
       iv_input = trials_ivs['input']
       iv_output = trials_ivs['output']
       total_time = trials_dvs['total_time']
   Clean the data:
In [10]: # Set better and translated columns to participants, trials and ranks
         participants.columns = participants_ivs
         columns = []
```

```
for column in raw_trials.columns:
             if (column in participants_ivs.index):
                 columns.append(participants_ivs[column])
             elif (column in trials_ivs.columns):
                 columns.append(trials_ivs[column]['label'])
             elif (column in trials_dvs.index):
                 columns.append(trials_dvs[column])
             else:
                 columns.append(column)
         raw_trials.columns = columns
         ranks.columns = [participant_id, ordering['label'],
                          technique['label']] + ranks_dvs.loc['label', :].tolist()
In [11]: # Set the participant_id column as the index in participants
         participants.set_index(participants_ivs['participant_id'], inplace=True)
In [12]: # Some participants are non valid or don't have complete measures
         non_valid_participants = [0, 4]
         participants = participants[~participants.index.isin(non_valid_participants)]
         ranks = ranks[~ranks[participants_ivs['participant_id']]
                       .isin(non_valid_participants)]
         incomplete_trials_participant_ids = [0, 4]
         raw_trials = raw_trials[~raw_trials[participants_ivs['participant_id']]
                                 .isin(incomplete_trials_participant_ids)
                                 ].reset_index(drop=True)
         trials_for_anova = trials_for_anova[~trials_for_anova['participant_id']
                                             .isin(incomplete_trials_participant_ids)
                                             ].reset_index(drop=True)
In [13]: # Some participants have wrong head phone mesures
         for head_distance_column in ['absolute_head_phone_distance',
                                      'signed_head_phone_distance']:
             raw_trials.loc[raw_trials[trials_dvs[head_distance_column]] == 0,
                            trials_dvs['absolute_head_phone_distance']] = np.nan
             trials_for_anova.loc[trials_for_anova[head_distance_column] == 0,
                                  head_distance_column] = np.nan
In [14]: # Setup categorical columns participants, trials and ranks
         participants[ordering['label']] = ranks.groupby(
             participant_id) [ordering['label']].first()
         participants[ordering['label']] = participants[ordering['label']].astype(
             ordering['categorical'])
         for iv_index in trials_ivs.columns:
             iv = trials_ivs[iv_index]
             raw_trials[iv['label']] = raw_trials[iv['label']].astype(iv['categorical'])
             trials_for_anova[iv_index] = raw_trials[iv['label']]
```

```
ranks[technique['label']] = ranks[technique['label']].astype(
             technique['categorical'])
         ranks[ordering['label']] = ranks[ordering['label']].astype(
             ordering['categorical'])
         # Rename categories
         if language == 'Français':
             technique['categorical'].categories = ['Téléphone', 'VESAD tactile', 'VESAD']
             text_size['categorical'].categories = ['Grand', 'Petit']
             distance['categorical'].categories = ['Proche', 'Loin']
             ordering['categorical'].categories = ['Groupe 1', 'Groupe 2', 'Groupe 3']
             iv_input['categorical'].categories = ['Tactile', 'Autour du téléphone']
             iv_output['categorical'].categories = ['Téléphone seul', 'Téléphone étendu']
         else:
             ordering['categorical'].categories = ['Group 1', 'Group 2', 'Group 3']
         # Set renamed categories to data
         participants[trials_ivs['ordering']['label']
                      ].cat.categories = ordering['categorical'].categories
         for iv_index in trials_ivs.columns:
             iv = trials_ivs[iv_index]
             raw_trials[iv['label']].cat.categories = iv['categorical'].categories
         ranks[technique['label']].cat.categories = technique['categorical'].categories
         ranks[ordering['label']].cat.categories = ordering['categorical'].categories
In [15]: # Eval the arrays in some dvs
         def eval_if_str(data):
             return literal_eval(data) if isinstance(data, str) else data
         raw_trials['grid_config'] = raw_trials['grid_config'].apply(eval_if_str)
In [16]: # Create trials
         trials_groupby_ivs = [participants_ivs['participant_id']]\
                              + trials_ivs.loc['label', :].tolist()
         trials = raw_trials.groupby(trials_groupby_ivs, observed=True)\
                  .mean().reset_index()
   Utilities:
In [17]: # Figure labels in the selected language
         labels = pd.Series()
         if language == 'Français':
             labels['category'] = 'Catégorie'
             labels['count'] = 'Nombre total'
             labels['distance'] = 'Distance moyenne (m)'
             labels['dv'] = 'VD'
             labels['iv'] = 'VI'
             labels['iv_value'] = 'Valeur VI'
```

```
labels['mean_difference'] = 'Différence des moyennes'
             labels['mean_difference_percentage'] = 'Différence des moyennes (%)'
             labels['mean_rank'] = 'Note moyenne'
             labels['preferences'] = ['Premier', 'Deuxième', 'Troisième']
             labels['p_value'] = 'Valeur p'
             labels['question'] = 'Question'
             labels['rank'] = 'Note'
             labels['time'] = 'Temps moyen (s)'
             labels['t_statistic'] = 'Statistique T'
             labels['votes'] = 'Participants'
         else:
             labels['category'] = 'Category'
             labels['count'] = 'Count'
             labels['distance'] = 'Mean Distance (m)'
             labels['dv'] = 'DV'
             labels['iv'] = 'IV'
             labels['iv_value'] = 'IV Value'
             labels['mean_difference'] = 'Mean Difference'
             labels['mean_difference_percentage'] = 'Mean Difference Percentage'
             labels['mean_rank'] = 'Mean Rank'
             labels['preferences'] = ['First', 'Second', 'Third']
             labels['p_value'] = 'p-value'
             labels['question'] = 'Question'
             labels['rank'] = 'Rank'
             labels['time'] = 'Mean Time (s)'
             labels['t_statistic'] = 'T statistic'
             labels['votes'] = 'Participants'
In [18]: def mean_ci(x, which=95, n_boot=1000):
             """Returns the confidence interval of the mean"""
             x2 = [i for i in x if not np.isnan(i)]
             boots = sns.algorithms.bootstrap(x2, n_boot=n_boot)
             return sns.utils.ci(boots, which=which)
In [19]: def print_mean_ci(x, ci_which=95):
             """Returns a string containing the mean with the CI of x"""
             ci1, ci2 = mean_ci(x, which=ci_which)
             return '{:.2f} [{:.2f}, {:.2f}]'.format(np.mean(x), ci1, ci2)
In [20]: def exp_mean(x):
             return np.exp(np.mean(x))
In [21]: def print_exp_mean_ci(x, ci_which=95):
             ci1, ci2 = np.exp(mean_ci(x, which=ci_which))
             return '{:.2f} [{:.2f}, {:.2f}]'.format(np.exp(np.mean(x)), ci1, ci2)
In [22]: def mean_difference(a, b):
             """Returns the mean difference value and percentage between a and b"""
             mean_diff = np.mean(a) - np.mean(b)
             mean_diff_percentage = mean_diff / np.mean(b) * 100
             return (mean_diff, mean_diff_percentage)
```

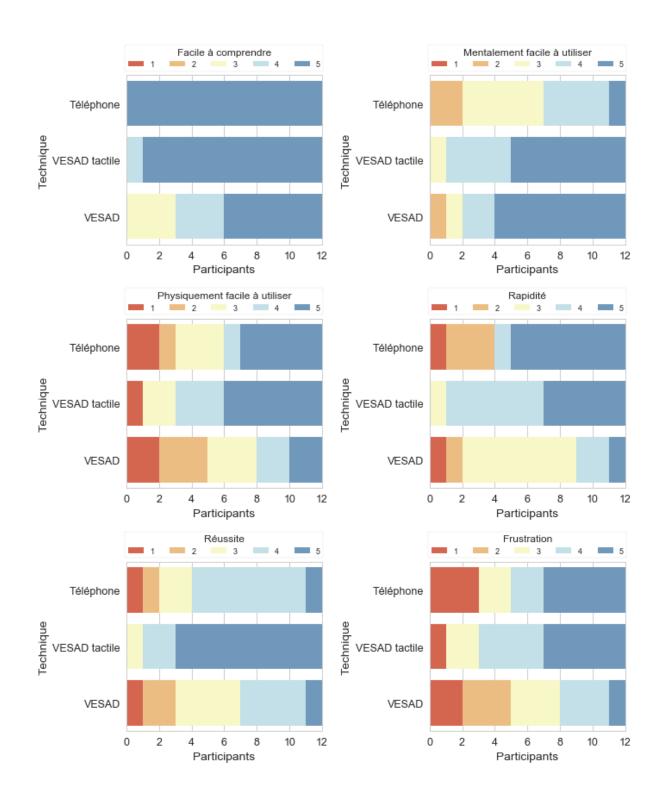
```
In [23]: def p_values_correction(data, alpha=0.05, correction_method='fdr_bh'):
             if correction_method != None:
                 reject, p_values_corrected, a1, a2 =\
                     multipletests(data[labels['p_value']].tolist(), alpha=alpha,
                                   method=correction_method)
                 data[labels['p_value']] = p_values_corrected
In [24]: def subplots(nsubplots, ncols_max=2, subplotsize=subplotsize, *plt_args):
             ncols = min(ncols_max, nsubplots)
             nrows = ((nsubplots - 1) // ncols) + 1
             fig, axs = plt.subplots(nrows=nrows, ncols=ncols,\
                                     figsize=(subplotsize[0]*ncols, subplotsize[1]*nrows),
             if nrows == 1 and ncols == 1:
                 axs = [axs]
             elif nrows >= 2 and ncols >= 2:
                 axs = [ax for ax_row in axs for ax in ax_row]
             for ax in axs[::-1][0:len(axs) - nsubplots]:
                 fig.delaxes(ax)
             return (fig, axs)
In [25]: def fix_legend_fontsize(ax_legend, fontsize=legend_title_fontsize):
             plt.setp(ax_legend.get_title(), fontsize=fontsize)
In [26]: def config_legend(ax, iv_id, fontsize=legend_title_fontsize):
             legend = ax.legend(title=trials_ivs.at['label', iv_id], frameon=True,
                                loc='center left', bbox_to_anchor=(1, 0.5))
             fix_legend_fontsize(legend)
             return legend
```

0.2 2. Participant ranks

Some functions for the analysis:

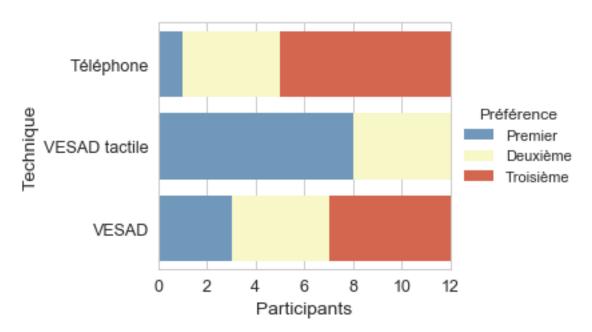
```
ranks_counts.sort_index(inplace=True)
             ranks_counts.index = ranks_counts_index # Restore the index
             return ranks_counts
In [28]: def cumulated_barplot(data, palette, **args):
             for row_id, row in data.iloc[::-1].iterrows():
                 sns.barplot(y=data.columns, x=row, label=row_id,
                             color=palette[row_id-1], orient='h', **args)
In [29]: def plot_ranks_distributions(iv_id, dv_ids):
             iv = trials_ivs[iv_id]
             fig, axs = subplots(len(dv_ids))
             for dv_id, ax in zip(dv_ids, axs):
                 dv = ranks_dvs[dv_id]
                 cumulated_ranks_count = get_ranks_count(iv_id, dv_id).unstack(level=0)\
                                         .cumsum()
                 cumulated_barplot(cumulated_ranks_count, palette=dv['palette'], ax=ax)
                 ax.set(xlabel=labels['votes'], xlim=(0, cumulated_ranks_count.max()[0]))
                 ax.xaxis.set_major_locator(ticker.MultipleLocator(2)) # Fix the axis ticks
                 ax_handles, ax_labels = ax.get_legend_handles_labels()
                 legend = ax.legend(ax_handles[::-1], ax_labels[::-1], frameon=True,
                                    loc='lower center', bbox_to_anchor=(0.5, 1),
                                    mode=None, ncol=len(dv['scale']), title=dv['label'],
                                    fontsize=legend_fontsize-2)
                 fix_legend_fontsize(legend)
             fig.tight_layout(h_pad=1) # Add padding to avoir legend and labels overlap
             return (fig, axs)
In [30]: def plot_ranks(iv_id, dv_ids, estimator=np.mean):
             iv = trials_ivs[iv_id]
             fig, axs = subplots(len(dv_ids))
             for dv_id, ax in zip(dv_ids, axs):
                 dv = ranks_dvs[dv_id]
                 sns.barplot(x=iv['label'], y=dv['label'], palette=iv['palette'],
                             data=ranks, ax=ax, estimator=estimator)
                 ax.set(ylim=(0, dv['scale'][-1]))
                 ax.yaxis.set_major_locator(ticker.MultipleLocator(1)) # Fix the axis ticks
             return (fig, axs)
In [31]: def rank_samples(iv_id, dv_id):
             """Returns the list of ranks (DV) for each IV value"""
             samples = []
             iv = trials ivs[iv id]
```

```
for iv_value in iv['categorical']:
                 dv_label = ranks_dvs[dv_id]['label']
                 sample = ranks[ranks[iv['label']] == iv_value][dv_label] \
                          .reset_index(drop=True)
                 samples.append(sample)
             return samples
In [32]: def test_ranks(iv_id, dv_ids, **args):
             results = []
             iv = trials_ivs[iv_id]
             for dv_id in dv_ids:
                 dv = ranks_dvs[dv_id]
                 samples = rank_samples(iv_id, dv_id)
                 H, p = stats.kruskal(*samples)
                 results.append([iv['label'], dv['label'], H, p])
             results = pd.DataFrame(results, columns=[labels['iv'], labels['dv'],
                                                       'Kruskal-Wallis H',
                                                       labels['p_value']])
             p_values_correction(results, **args)
             return results
In [33]: def test_pairwise_ranks(iv_id, dv_ids, **args):
             iv = trials_ivs[iv_id]
             iv_category_ids = range(len(iv['categorical']))
             results = []
             for dv_id in dv_ids:
                 dv = ranks_dvs[dv_id]
                 samples = rank_samples(iv_id, dv_id)
                 sample_pairs = itertools.combinations(iv_category_ids, 2)
                 for id1, id2 in sample_pairs:
                     U, p = stats.mannwhitneyu(samples[id1], samples[id2])
                     mean_diff, mean_diff_per = mean_difference(samples[id1], samples[id2])
                     results.append([iv['label'], iv['categorical'][id1],
                                     iv['categorical'][id2], dv['label'],
                                     mean_diff, mean_diff_per, U, p])
             columns = [labels['iv'], labels['iv_value'] + ' 1',
                        labels['iv_value'] + ' 2', labels['dv'],
                        labels['mean_difference'], labels['mean_difference_percentage'],
                        'Mann-Whitney U', labels['p_value']]
             results = pd.DataFrame(results, columns=columns)
             p_values_correction(results, **args)
             return results
   We display the rank and preference distributions:
In [34]: (fig, axs) = plot_ranks_distributions('technique', ranks_dvs.columns[0:-1])
         fig.savefig('ranks_distributions.png')
```



fix_legend_fontsize(legend)

fig.savefig('preferences_distribution.png')



We use the Kruskal-Wallis test (Benjamini–Hochberg correction) on each question to check if there is statistical significative differences between the ranks among TECHNIQUE:

```
In [36]: test_ranks('technique', ranks_dvs, correction_method='fdr_bh')
Out [36]:
                                                   VD Kruskal-Wallis H Valeur p
                   VI
         0
           Technique
                                  Facile à comprendre
                                                              11.001420 0.007497
                        Mentalement facile à utiliser
         1
           Technique
                                                              10.905742 0.007497
           Technique
                       Physiquement facile à utiliser
                                                               4.148121 0.125674
         3 Technique
                                             Rapidité
                                                               7.130846 0.039599
         4
           Technique
                                             Réussite
                                                              13.784269
                                                                         0.006303
           Technique
                                          Frustration
                                                               4.500057
                                                                         0.122962
         5
                                           Préférence
           Technique
                                                              12.638889
                                                                         0.006303
```

All the questions, except Physically Easy to Use and Frustration, are statistically significants: Easy to Understand (p = 0.007), Mentally Easy to Use (p = 0.007), Subjective Speed (p = 0.04), Subjective Performance (p = 0.006), Preference (p = 0.006).

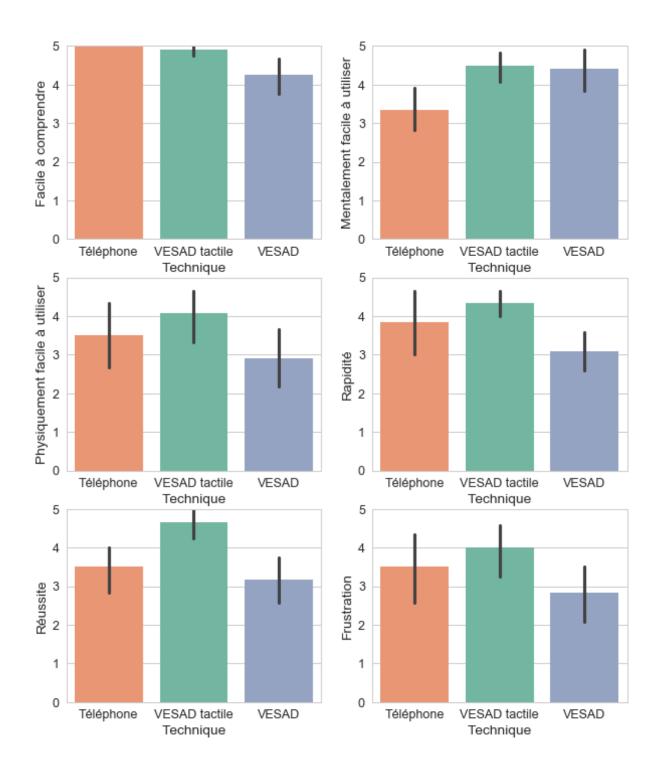
We use then pairwise Mann-Whitney tests (Benjamini–Hochberg correction) for the significant questions above:

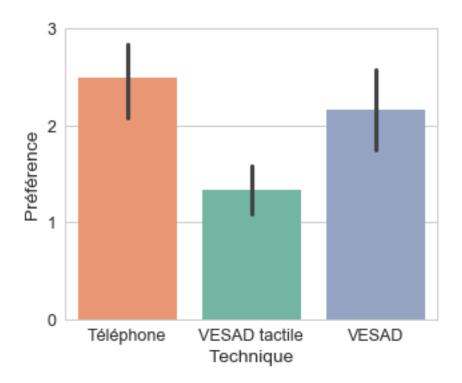
```
2
    Technique
               VESAD tactile
                                        VESAD
                                                           Facile à comprendre
3
    Technique
                               VESAD tactile
                                                Mentalement facile à utiliser
                    Téléphone
4
    Technique
                    Téléphone
                                        VESAD
                                                Mentalement facile à utiliser
    Technique
5
               VESAD tactile
                                        VESAD
                                                Mentalement facile à utiliser
6
    Technique
                    Téléphone
                               VESAD tactile
                                                                       Rapidité
7
    Technique
                    Téléphone
                                        VESAD
                                                                       Rapidité
8
    Technique
               VESAD tactile
                                        VESAD
                                                                       Rapidité
    Technique
9
                    Téléphone
                               VESAD tactile
                                                                       Réussite
    Technique
                    Téléphone
                                                                       Réussite
10
                                        VESAD
11
    Technique
                VESAD tactile
                                        VESAD
                                                                       Réussite
    Technique
12
                    Téléphone
                                                                     Préférence
                                VESAD tactile
    Technique
13
                    Téléphone
                                        VESAD
                                                                     Préférence
    Technique
                VESAD tactile
                                        VESAD
                                                                     Préférence
                               Différence des moyennes (%)
                                                              Mann-Whitney U
    Différence des moyennes
0
                    0.083333
                                                   1.694915
                                                                         66.0
                    0.750000
1
                                                  17.647059
                                                                         36.0
2
                    0.666667
                                                  15.686275
                                                                         40.5
3
                                                                         23.0
                   -1.166667
                                                 -25.925926
4
                   -1.083333
                                                 -24.528302
                                                                         28.5
5
                    0.083333
                                                   1.886792
                                                                         69.5
6
                                                 -11.538462
                   -0.500000
                                                                         70.5
7
                    0.750000
                                                  24.324324
                                                                         48.5
8
                    1.250000
                                                  40.540541
                                                                         21.0
9
                                                 -25.000000
                                                                         22.5
                   -1.166667
10
                    0.333333
                                                  10.526316
                                                                         57.0
11
                    1.500000
                                                  47.368421
                                                                         17.5
12
                    1.166667
                                                  87.500000
                                                                         16.0
13
                    0.333333
                                                  15.384615
                                                                         56.0
14
                   -0.833333
                                                 -38.461538
                                                                         32.0
    Valeur p
0
    0.215732
1
    0.008605
2
    0.020977
3
    0.005031
4
    0.010151
5
    0.475027
6
    0.475027
7
    0.126838
8
    0.004655
9
    0.004655
10
   0.215732
11
    0.003904
    0.003904
12
13
    0.215732
    0.013011
```

We display the mean and 95% CI of each question:

```
In [38]: ranks.groupby([trials_ivs['technique']['label']])\
```

```
.aggregate(print_mean_ci).loc[:, ranks_dvs.loc['label', :]].transpose()
Out[38]: Technique
                                                 Téléphone
                                                               VESAD tactile \
        Facile à comprendre
                                        5.00 [5.00, 5.00] 4.92 [4.75, 5.00]
        Mentalement facile à utiliser
                                        3.33 [2.83, 3.83] 4.50 [4.17, 4.83]
         Physiquement facile à utiliser 3.50 [2.58, 4.33] 4.08 [3.33, 4.67]
         Rapidité
                                        3.83 [2.92, 4.59] 4.33 [4.00, 4.67]
                                        3.50 [2.83, 4.00] 4.67 [4.25, 5.00]
        Réussite
         Frustration
                                        3.50 [2.50, 4.33] 4.00 [3.25, 4.58]
                                        2.50 [2.17, 2.83]
                                                           1.33 [1.08, 1.58]
        Préférence
         Technique
                                                    VESAD
         Facile à comprendre
                                        4.25 [3.75, 4.67]
        Mentalement facile à utiliser 4.42 [3.83, 4.83]
         Physiquement facile à utiliser 2.92 [2.25, 3.67]
         Rapidité
                                        3.08 [2.50, 3.67]
                                        3.17 [2.58, 3.75]
         Réussite
                                        2.83 [2.17, 3.50]
         Frustration
         Préférence
                                        2.17 [1.75, 2.67]
In [39]: (fig, axs) = plot_ranks('technique', ranks_dvs.columns[0:-1])
         fig.savefig('ranks.png')
```





Overall significant results are:

- **Easy to Understand**: *PhoneOnly* is significantly better than MidAirInArOut (p = 0.009), and seems a little better than *PhoneInArOut*.
- **Physically Easy to Use**: There is no significant differences due to TECHNIQUE; they seem scored similar.
- **Mentally Easy to Use**: *PhoneOnly* is statistically and practically worst than *PhoneInArOut* (p = 0.005) and *MidAirInArOut* (p = 0.01).
- **Subjective Speed**: *PhoneInArOut* is significantly better than MidAirInArOut (p = 0.05).
- **Subjective Performance**: *PhoneInArOut* is statistically better than *PhoneOnly* (p = 0.005) and *MidAirInArOut* (p = 0.004).
- Frustration: There is no significant differences due to TECHNIQUE; they seem scored similar.
- **Preference**: *PhoneInArOut* is significantly preferred to *PhoneOnly* (p = 0.004) and *MidAirInArOut* (p = 0.01).

0.3 3. Participant trials

Some functions for the analysis:

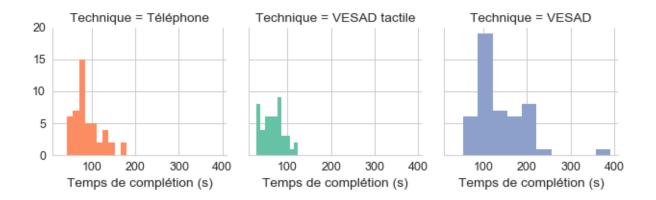
```
In [43]: def melt_trials(value_vars, var_name, value_name, data=trials):
             return pd.melt(data, id_vars=trials_ivs.loc['label', :],
                            value_vars=value_vars, var_name=var_name,
                            value_name=value_name)
In [44]: def test_normality(iv_ids, dv_ids, data=trials, **args):
             results = []
             for dv_id in dv_ids:
                 for iv_id in iv_ids:
                     iv = trials_ivs[iv_id]
                     samples = trial_samples(iv_id, dv_id, data)
                     for iv_value, sample in zip(iv['categorical'], samples):
                         W, p = stats.shapiro(sample)
                         results.append([iv['label'], iv_value, trials_dvs[dv_id], W, p])
             results = pd.DataFrame(results, columns=[labels['iv'], labels['iv_value'],
                                                      labels['dv'], 'Shapiro W',
                                                      labels['p_value']])
             p_values_correction(results, **args)
             return results
In [45]: def test_equal_variances(iv_ids, dv_ids, data=trials, levene_center='mean',
                                  **args):
             results = []
             for dv_id in dv_ids:
                 for iv_id in iv_ids:
                     samples = trial_samples(iv_id, dv_id, data)
                     W, p = stats.levene(*samples)
                     results.append([trials_ivs.at['label', iv_id], trials_dvs[dv_id],
                                     W, p])
             results = pd.DataFrame(results, columns=[labels['iv'], labels['dv'],
                                                      'Levene W', labels['p_value']])
             p_values_correction(results, **args)
             return results
In [46]: def test_pairwise_trials(iv_id, dv_id, data=trials, log_data=False, **args):
             results = []
             iv, dv = trials_ivs[iv_id], trials_dvs[dv_id]
             iv_category_ids = range(len(iv['categorical']))
             samples = trial_samples(iv_id, dv_id, data)
             sample_pairs = itertools.combinations(iv_category_ids, 2)
             for id1, id2 in sample_pairs:
                 T, p = stats.ttest_ind(samples[id1], samples[id2])
                 mean_diff, mean_diff_per = mean_difference(np.exp(samples[id1]),
                                                             np.exp(samples[id2]))\
                     if log_data else mean_difference(samples[id1], samples[id2])
```

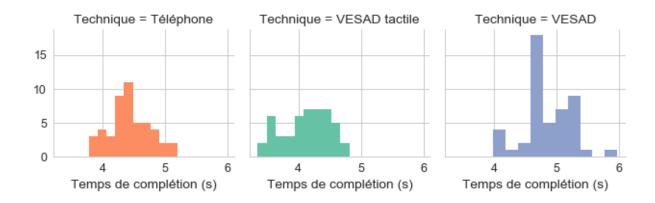
```
results.append([iv['label'], iv['categorical'][id1],
                                 iv['categorical'][id2], dv, mean_diff,
                                 mean_diff_per, T, p])
             columns = [labels['iv'], labels['iv_value'] + ' 1',
                        labels['iv_value'] + ' 2', labels['dv'],
                        labels['mean_difference'], labels['mean_difference_percentage'],
                        labels['t_statistic'], labels['p_value']]
             results = pd.DataFrame(results, columns=columns)
             p_values_correction(results, **args)
             return results
In [47]: def test_non_normal_trials(iv_ids, dv_ids, data=trials, **args):
             results = []
             for dv_id in dv_ids:
                 for iv_id in iv_ids:
                     samples = trial_samples(iv_id, dv_id, data)
                     H, p = stats.kruskal(*samples)
                     results.append([trials_ivs.at['label', iv_id], trials_dvs[dv_id],
                                     H, p])
             results = pd.DataFrame(results, columns=[labels['iv'], labels['dv'],
                                                       'Kruskal-Wallis H',
                                                       labels['p_value']])
             p_values_correction(results, **args)
             return results
In [48]: def test_pairwise_non_normal_trials(iv_ids, dv_ids, data=trials, **args):
             results = []
             for dv_id in dv_ids:
                 for iv_id in iv_ids:
                     iv, dv = trials_ivs[iv_id], trials_dvs[dv_id]
                     samples = trial_samples(iv_id, dv_id, data)
                     iv_category_ids = range(len(iv['categorical']))
                     sample_pairs = itertools.combinations(iv_category_ids, 2)
                     for id1, id2 in sample_pairs:
                         U, p = stats.mannwhitneyu(samples[id1], samples[id2])
                         mean_diff, mean_diff_per = mean_difference(samples[id1],
                                                                     samples[id2])
                         results.append([iv['label'], iv['categorical'][id1],
                                         iv['categorical'][id2], dv, mean_diff,
                                         mean_diff_per, U, p])
             columns = [labels['iv'], labels['iv_value'] + ' 1',
                        labels['iv_value'] + ' 2', labels['dv'],
                        labels['mean_difference'], labels['mean_difference_percentage'],
```

```
'Mann-Whitney U', labels['p_value']]
             results = pd.DataFrame(results, columns=columns)
             p_values_correction(results, **args)
             return results
In [49]: def plot_trials(iv_ids_list, dv_id, data=trials, kind='bar', **args):
             dv = trials_dvs[dv_id]
             if (len(iv_ids_list) == 0):
                 iv_ids_list = [[iv_id] for id_id in trials_ivs.columns]
             fig, axs = subplots(len(iv_ids_list))
             for id_ids, ax in zip(iv_ids_list, axs):
                 ivs = [trials_ivs[id_id] for id_id in id_ids]
                 if (len(ivs) == 1):
                     iv = ivs[0]
                     if (kind == 'bar'):
                         sns.barplot(x=iv['label'], y=dv, data=data,
                                     palette=iv['palette'], ax=ax, **args)
                     elif (kind == 'box'):
                         sns.boxplot(x=iv['label'], y=dv, data=data,
                                     palette=iv['palette'], ax=ax, **args)
                     elif (kind == 'count'):
                         sns.countplot(hue=iv['label'], x=dv, data=data,
                                       palette=iv['palette'], ax=ax, **args)
                         ax.set(ylabel='Count')
                         ax.legend(loc='upper right', title=labels['count'],
                                   frameon=True)
                 elif (len(ivs) == 2):
                     if (kind == 'bar'):
                         sns.barplot(x=ivs[1]['label'], y=dv, hue=ivs[0]['label'],
                                     data=data, palette=ivs[0]['palette'], ax=ax, **args)
                     ax.legend(frameon=True, loc='upper left', bbox_to_anchor=(1, 1))
             return (fig, axs)
```

0.3.1 3.1. Task completion time

We first apply a log transform to TCT to approximate a normal distribution.





We test the normality of TCT distributions for each TECHNIQUE and their equality of variances, since it's the main factor of interest.

```
In [53]: test_normality(['technique'], ['total_time'])
Out [53]:
                  VI
                          Valeur VI
                                                          VD Shapiro W Valeur p
                          Téléphone Temps de complétion (s)
        0 Technique
                                                              0.983679
                                                                        0.735995
        1 Technique VESAD tactile Temps de complétion (s)
                                                              0.971828
                                                                        0.446912
        2 Technique
                              VESAD Temps de complétion (s)
                                                              0.966510 0.446912
In [54]: test_equal_variances(['technique'], ['total_time'])
Out [54]:
                  VI
                                           VD Levene W Valeur p
        O Technique Temps de complétion (s) 0.756269 0.471309
```

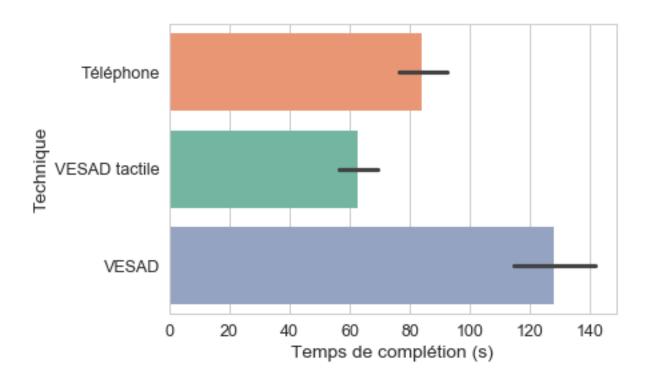
We meet all the assumptions of an ANOVA. Trials were done independently, TCT distributions are normal and their variances are equal.

We perform a full factorial ANOVA with the model: TCT ~ TECHNIQUE x TEXT_SIZE x DISTANCE + TECHNIQUE x ORDERING.

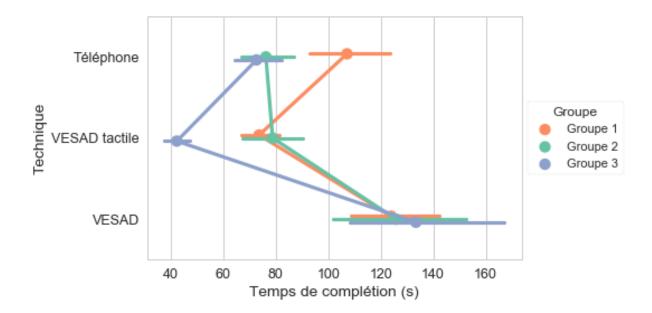
```
In [55]: tct_model = ols('total_time ~ technique * text_size * distance'
                        + '+ technique * ordering', data=trials_for_anova).fit()
        sm.stats.anova_lm(tct_model, typ=2)
Out [55]:
                                                   df
                                                               F
                                                                        PR(>F)
                                         sum_sq
                                                   2.0 76.430298 4.982920e-27
        technique
                                      22.333355
        text_size
                                       0.252107
                                                  1.0 1.725548 1.900955e-01
        distance
                                       0.035125
                                                  1.0 0.240415 6.243050e-01
                                                  2.0 13.835474 1.904089e-06
        ordering
                                       4.042802
        technique:text_size
                                       0.650853
                                                   2.0 2.227382 1.097877e-01
        technique:distance
                                       0.098190
                                                   2.0 0.336030 7.149003e-01
        text_size:distance
                                       0.559213
                                                  1.0 3.827533 5.144784e-02
        technique:ordering
                                                   4.0 10.261184 9.495336e-08
                                       5.996749
        technique:text_size:distance
                                                        2.924364 5.540194e-02
                                      0.854515
                                                   2.0
        Residual
                                      39.447745 270.0
                                                             {\tt NaN}
                                                                           NaN
```

The main significant effect on TCT is TECHNIQUE (F = 76.4, p < 0.0001), then ORDERING (F = 13.8, p < 0.0001). There is also an significant interaction effect: TECHNIQUE x ORDERING (F = 2.9, p < 0.0001).

We display mean TCT values with 95% CI for these conditions:



```
In [58]: trial_means(['ordering', 'technique'], ['total_time'],
                     aggregate=print_exp_mean_ci).unstack()
Out[58]:
                   Temps de complétion (s)
                                 Téléphone
                                                   VESAD tactile
         Technique
         Groupe
         Groupe 1
                    107.14 [91.84, 123.42] 73.63 [66.95, 81.19]
                      76.22 [66.67, 87.00] 78.79 [68.79, 90.48]
         Groupe 2
         Groupe 3
                      72.64 [64.44, 81.78] 42.27 [37.47, 47.37]
         Technique
                                      VESAD
         Groupe
         Groupe 1
                    124.00 [109.18, 141.63]
         Groupe 2
                    125.91 [102.74, 154.53]
         Groupe 3
                    133.41 [108.55, 167.96]
In [59]: ax = sns.pointplot(x=trials_dvs['total_time'], y=technique['label'],
                           hue=ordering['label'], palette=ordering['palette'],
                           data=trials, dodge=True, estimator=exp_mean)
         config_legend(ax, 'ordering')
         ax.get_figure().savefig('tct_ordering.png')
```



It seems that participants who started with *PhoneOnly* were slower with this technique than the other groups. Similarly, participants who finished with *PhoneInArOut* were faster with this technique. It indicates there is a learning curve on the task, but interestingly participants from all groups performed equally with *MidAirInArOut* technique.

We compare the TCT for the three techniques only with pairwise t-tests (Benjamini–Hochberg correction).

```
In [60]: test_pairwise_trials('technique', 'total_time', correction_method='fdr_bh',
                                  log_data=True)
Out[60]:
                    VΙ
                                          Valeur VI 2
                                                                              VD
                          Valeur VI 1
                                                                                 \
            Technique
                            Téléphone
                                       VESAD tactile
                                                       Temps de complétion (s)
         0
         1
            Technique
                            Téléphone
                                                VESAD
                                                       Temps de complétion (s)
            Technique
                       VESAD tactile
                                                VESAD
                                                       Temps de complétion (s)
            Différence des moyennes
                                      Différence des moyennes (%)
                                                                     Statistique T
         0
                           21.840362
                                                         32.666819
                                                                          4.090635
         1
                          -49.467731
                                                         -35.803106
                                                                         -5.615875
         2
                          -71.308093
                                                         -51.610437
                                                                         -9.032751
                Valeur p
            9.077859e-05
         0
         1
            2.966612e-07
         2
            6.282833e-14
```

- *PhoneInArOut* is 71s (+52%) faster than *MidAirInArOut* (p < 0.0001).
- *PhoneOnly* is 49s (+36%) faster than *MidAirInArOut* (p < 0.0001).
- *PhoneInArOut* is 22s (+33%) faster than *PhoneOnly* (p < 0.0001).

0.3.2 3.2. Errors

We visualize first the SELECTIONS and ERRORS distributions:

```
In [61]: g = sns.pairplot(trials, hue=technique['label'], kind='reg',
                              vars=[trials_dvs['selections_count'], trials_dvs['errors']],
                              palette=technique['palette'], size=4);
          g.savefig('selections_errors_distributions.png')
        22.5
        20.0
        17.5
     Sélections
        15.0
        12.5
        10.0
         7.5
         5.0
                                                                                        Technique
                                                                                         Téléphone
                                                                                         VESAD tactile
           5
                                                                                         VESAD
           4
           3
        Erreurs
           1
           0
```

It seems that a user makes as much errors as she makes selections. The relation is almost the same for each technique, even if users seems to make more selections for the same number of errors with PhoneOnly.

3

Erreurs

5

Sélections

We can't use ANOVA on SELECTIONS and ERRORS variables as their distributions are exponentials. We use instead the Kruskal-Wallis test (Benjamini–Hochberg correction) to check if there is significative differences due to TECHNIQUE, TEXT_SIZE, DISTANCE or ORDERING.

```
In [62]: test_non_normal_trials(['technique', 'text_size', 'distance', 'ordering'],
                                 ['selections_count', 'errors'])
Out[62]:
                         VI
                                     VD
                                         Kruskal-Wallis H Valeur p
         0
                  Technique
                             Sélections
                                                 15.125918
                                                            0.004155
            Taille du texte
                             Sélections
                                                  0.003897
                                                            0.950224
         1
         2
                   Distance
                             Sélections
                                                  0.052701 0.935347
         3
                     Groupe
                             Sélections
                                                 11.510535 0.010095
```

4	Technique	Erreurs	5.201541	0.148433
5	Taille du texte	Erreurs	0.103661	0.935347
6	Distance	Erreurs	0.201599	0.935347
7	Groupe	Erreurs	11.153096	0.010095

Only TECHNIQUE (p = 0.004) and ORDERING (p = 0.01) have a significant effect on SELECTIONS. But, only ORDERING (p = 0.01) have a significant effect on ERRORS.

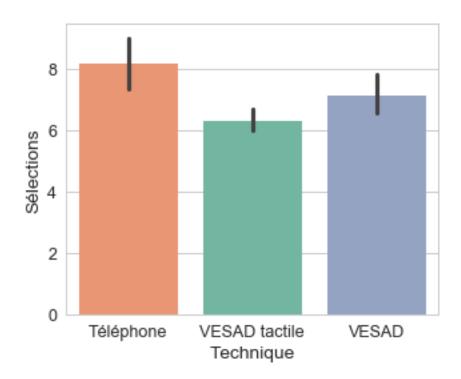
We use then pairwise Mann-Whitney tests (Benjamini–Hochberg correction) for the significant questions above:

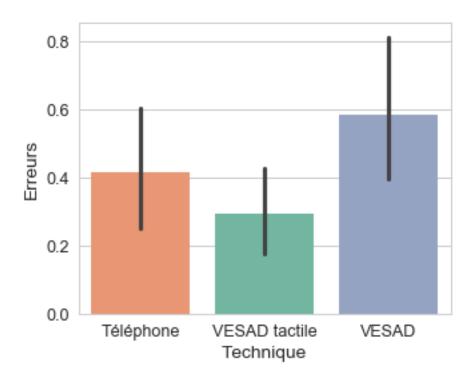
```
In [63]: test_pairwise_non_normal_trials(['technique', 'ordering'],
                                             ['selections_count', 'errors'])
Out [63]:
                     VΙ
                            Valeur VI 1
                                            Valeur VI 2
                                                                   VD
         0
              Technique
                              Téléphone
                                          VESAD tactile
                                                           Sélections
         1
              Technique
                              Téléphone
                                                   VESAD
                                                           Sélections
         2
              Technique
                          VESAD tactile
                                                   VESAD
                                                           Sélections
         3
                               Groupe 1
                 Groupe
                                                Groupe 2
                                                           Sélections
         4
                 Groupe
                               Groupe 1
                                                Groupe 3
                                                           Sélections
         5
                 Groupe
                               Groupe 2
                                                Groupe 3
                                                           Sélections
              Technique
         6
                              Téléphone
                                          VESAD tactile
                                                              Erreurs
         7
              Technique
                              Téléphone
                                                   VESAD
                                                              Erreurs
         8
              Technique
                          VESAD tactile
                                                   VESAD
                                                              Erreurs
         9
                 Groupe
                               Groupe 1
                                                Groupe 2
                                                              Erreurs
         10
                 Groupe
                               Groupe 1
                                                Groupe 3
                                                              Erreurs
         11
                 Groupe
                               Groupe 2
                                                Groupe 3
                                                              Erreurs
              Différence des moyennes
                                         Différence des moyennes (%)
                                                                         Mann-Whitney U
         0
                              1.864583
                                                             29.537954
                                                                                   627.0
         1
                              1.041667
                                                             14.598540
                                                                                   864.5
         2
                             -0.822917
                                                            -11.532847
                                                                                   915.0
         3
                                                             26.265823
                                                                                   755.0
                              1.729167
         4
                              1.583333
                                                             23.529412
                                                                                   755.0
         5
                             -0.145833
                                                             -2.167183
                                                                                  1136.0
         6
                              0.125000
                                                             42.857143
                                                                                  1083.5
         7
                             -0.166667
                                                            -28.571429
                                                                                   957.0
         8
                             -0.291667
                                                            -50.000000
                                                                                   873.0
         9
                              0.333333
                                                            103.225806
                                                                                  846.5
         10
                              0.343750
                                                            110.000000
                                                                                   761.5
         11
                              0.010417
                                                              3.333333
                                                                                  1039.0
              Valeur p
         0
              0.000635
              0.029356
         1
         2
              0.059881
         3
              0.005196
         4
              0.005196
         5
              0.454285
         6
              0.312007
         7
              0.083050
              0.026306
```

```
9 0.020183
10 0.005196
11 0.205336
```

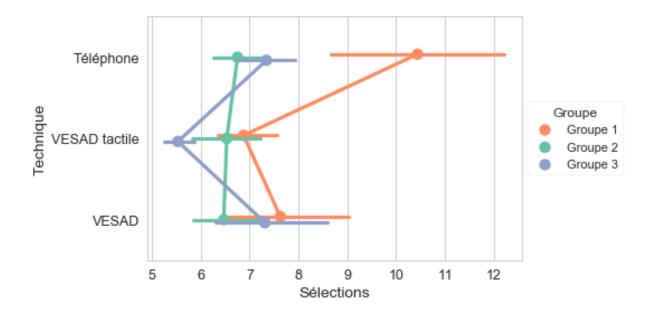
```
In [64]: trial_means(['technique'], ['selections_count', 'errors'])
```

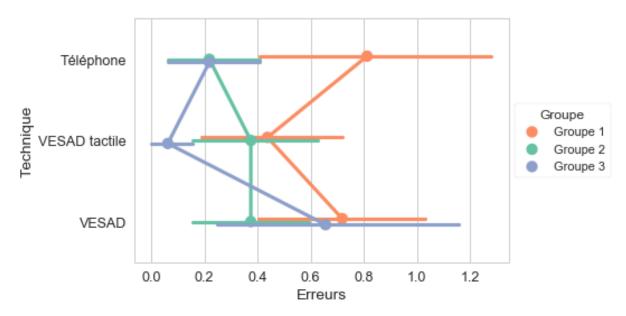
Out[64]:		Sélections			Erreurs	
	Technique					
	Téléphone	8.18	[7.42, 8.97]	0.42	[0.25, 0.59]	
	VESAD tactile	6.31	[5.99, 6.66]	0.29	[0.18, 0.42]	
	VESAD	7.14	[6.53, 7.78]	0.58	[0.40, 0.82]	





```
In [67]: trial_means(['ordering', 'technique'], ['selections_count', 'errors'])
Out[67]:
                                          Sélections
                                                                Erreurs
         Groupe
                  Technique
         Groupe 1 Téléphone
                                 10.44 [8.62, 12.38] 0.81 [0.38, 1.31]
                                   6.88 [6.38, 7.56] 0.44 [0.19, 0.69]
                  VESAD tactile
                  VESAD
                                   7.62 [6.53, 9.00] 0.72 [0.41, 1.03]
                                   6.75 [6.25, 7.28] 0.22 [0.06, 0.41]
         Groupe 2 Téléphone
                  VESAD tactile
                                   6.53 [5.84, 7.19]
                                                      0.38 [0.16, 0.62]
                                   6.47 [5.81, 7.19]
                  VESAD
                                                      0.38 [0.19, 0.62]
         Groupe 3 Téléphone
                                   7.34 [6.72, 8.00]
                                                     0.22 [0.06, 0.41]
                  VESAD tactile
                                   5.53 [5.22, 5.84]
                                                      0.06 [0.00, 0.16]
                  VESAD
                                   7.31 [6.22, 8.50]
                                                      0.66 [0.25, 1.12]
In [68]: ax = sns.pointplot(x=trials_dvs['selections_count'], y=technique['label'],
                            hue=ordering['label'], palette=ordering['palette'],
                            data=trials, dodge=True)
         config_legend(ax, 'ordering')
         ax.get_figure().savefig('selections_ordering.png')
```





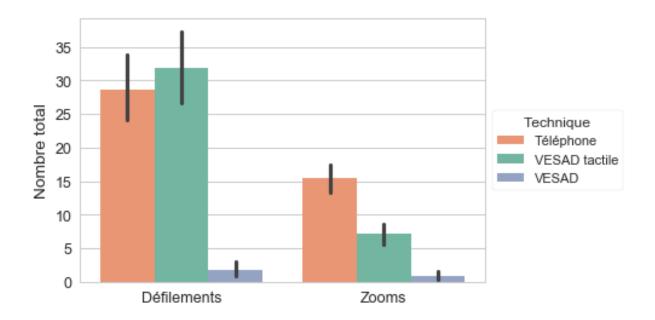
0.3.3 3.3. Navigation

Variable meanings:

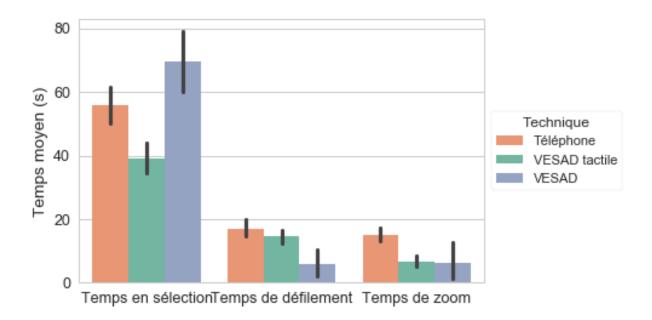
• Selection Time = time spent looking for where to drop an item that had been picked

- Selection Distance = distance travelled by the finger with an item selected
- Head Phone Distance = sum of the distance between the head and the phone

```
In [70]: # Data preparation
         trial_counts = melt_trials(var_name=labels['category'],
                                    value_name=labels['count'],
                                    value_vars=[trials_dvs['pan_count'],
                                               trials_dvs['zoom_count']])
         trial_times = melt_trials(var_name=labels['category'],
                                   value_name=labels['time'],
                                   value_vars=[trials_dvs['selections_time'],
                                               trials_dvs['pan_time'],
                                               trials_dvs['zoom_time']])
         trial_distances_dvs = [trials_dvs['selections_projected_distance'],
                                trials_dvs['pan_projected_distance'],
                                trials_dvs['zoom_projected_distance'],
                                trials_dvs['absolute_head_phone_distance']]
         trial_distances = melt_trials(var_name=labels['category'],
                                       value_name=labels['distance'],
                                       value_vars=trial_distances_dvs)
In [71]: trial_means(['technique'], ['pan_count', 'zoom_count'])
Out[71]:
                                 Défilements
                                                             Zooms
         Technique
         Téléphone
                       28.70 [23.96, 34.15]
                                             15.53 [13.66, 17.48]
         VESAD tactile 31.81 [26.84, 37.13]
                                                 7.14 [5.73, 8.60]
         VESAD
                           1.83 [0.81, 2.93]
                                                 0.83 [0.27, 1.49]
In [72]: ax = sns.barplot(x=labels['category'], y=labels['count'],
                          hue=technique['label'], palette=technique['palette'],
                          data=trial_counts)
         config_legend(ax, 'technique')
         ax.set(xlabel='')
         ax.get_figure().savefig('navigation_count.png')
```



```
In [73]: trial_means(['technique'], ['selections_time', 'pan_time', 'zoom_time'])
Out [73]:
                          Temps en sélection
                                                Temps de défilement \
         Technique
                        55.74 [50.09, 61.69]
                                              17.12 [14.59, 19.82]
         Téléphone
         VESAD tactile 38.98 [34.28, 44.09]
                                              14.53 [12.71, 16.61]
                        69.68 [61.40, 78.83]
         VESAD
                                                 5.97 [2.18, 10.12]
                               Temps de zoom
         Technique
         Téléphone
                        15.18 [13.28, 17.19]
         VESAD tactile
                           6.70 [5.06, 8.61]
         VESAD
                          6.24 [1.56, 12.10]
In [74]: ax = sns.barplot(x=labels['category'], y=labels['time'], data=trial_times,
                          hue=technique['label'], palette=technique['palette'])
         config_legend(ax, 'technique')
         ax.set(xlabel='')
         ax.get_figure().savefig('navigation_time.png')
```



```
In [75]: trial_means(['technique'], ['selections_projected_distance',
                                      'pan_projected_distance',
                                      'zoom_projected_distance',
                                      'absolute_head_phone_distance'])
Out [75]:
                       Distance en sélection Distance de défilement
                                                                       Distance de zoom \
         Technique
                           4.87 [4.06, 5.74]
                                                   1.50 [1.20, 1.83]
                                                                      2.11 [1.75, 2.56]
         Téléphone
         VESAD tactile
                           2.83 [2.38, 3.28]
                                                   1.09 [0.90, 1.28]
                                                                      0.69 [0.51, 0.87]
         VESAD
                          8.72 [7.21, 10.56]
                                                   0.47 [0.19, 0.80]
                                                                      0.62 [0.13, 1.21]
                       Mouvements tête-téléphone
         Technique
         Téléphone
                               3.18 [2.35, 4.16]
         VESAD tactile
                               1.57 [1.26, 1.92]
         VESAD
                               6.12 [4.90, 7.48]
In [76]: g = sns.factorplot(x=technique['label'], y=labels['distance'],
                            col=labels['category'], data=trial_distances,
                            palette=technique['palette'], kind='bar', col_wrap=2)
         g.set_titles('{col_name}') # Replace subplot titles
         for ax in g.axes:
             ax.title.set_position([0.5, -0.12])
         g.set_axis_labels('') # Custom legend
         g.set_xticklabels([])
         legend_handles = [patches.Patch(color=color, label=value)\
                           for value, color in zip(technique['categorical'],
                                                    technique['palette'])]
```

g.savefig('navigation_distance.png')

