

The following table outlines the factors that were considered, their levels, and how they are associated. Originally tray position was not considered as a factor, however, when putting the trays into the oven, only one tray would fit on the top rack so the difference in top and bottom racks was added after the fact.

Factor	Levels	Fixed?	Nested/Crossed	
Butter (b)	Melted (M), Creamed (C)	Fixed	Crossed with Dough & Tray	
Dough Temp (d)			Crossed with Butter & Tray	
	NOT Refrigerated (N)			
Tray Position (t)	Top (T), Bottom (B)	Fixed	Crossed with Butter & Dough	

Using the possible combinations of butter and dough temperature, R was used draw 2 samples for position assignment for each tray. The following is the output from this procedure.

```
1 > tray1
2 [1] "CN" "CN" "MR" "CN" "MR" "CR" "CR" "MR" "MN" "MN" "CR" "MN"
3 > tray2
4 [1] "CN" "CN" "CR" "CR" "MR" "MN" "CN" "MN" "MR" "MR" "MN" "CR"
```

Listing 1: Randomized Tray Locations

**DATA PLOTS** 

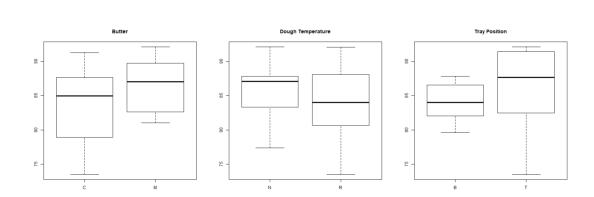


Figure 1: Individual Factor Effects on Cookie Size

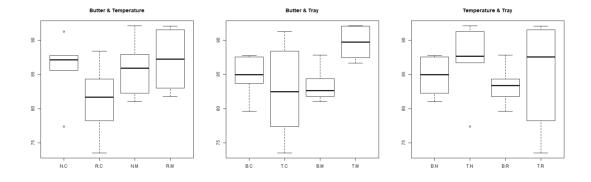


Figure 2: Pairwise Factor Effects on Cookie Size

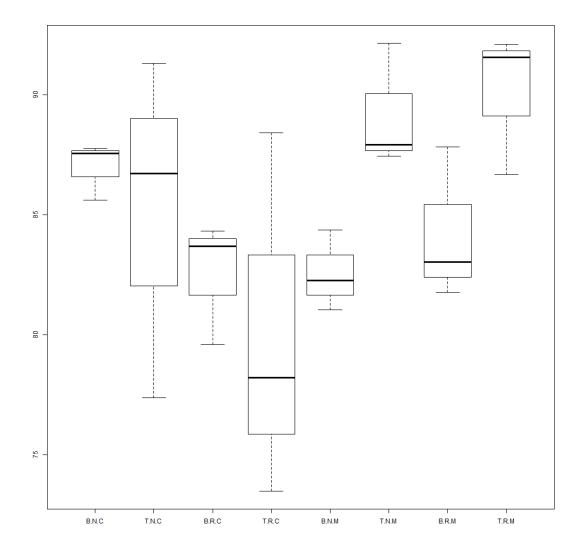


Figure 3: Full Factor Effects on Cookie Size

Model \_\_\_\_

Using the full model with all interactions, we can obtain the following model:

$$\begin{split} Y_{b,d,t,c} &= \alpha_b + \beta_d + \gamma_t + \left(\alpha\beta\right)_{b,d} + \left(\alpha\gamma\right)_{b,t} + \left(\beta\gamma\right)_{dt} + \epsilon_{b,d,t,c} \\ \epsilon_{b,d,t,c} &\sim N(0,\sigma^2) \end{split}$$

If one were to only examine the main effects, the ME model is as follows:

$$\begin{aligned} Y_{b,d,t,c} &= \alpha_b + \beta_d + \gamma_t + \epsilon_{b,d,t,c} \\ \epsilon_{b,d,t,c} &\sim N(0,\sigma^2) \end{aligned}$$

R ANALYSIS

Looking at the ANOVA table for the full model, we can see that the only truly significant factor is the interaction between the type of butter used and the tray position. The chilled dough and butter type interaction is significant if we relax our alpha value to 0.1.

```
1 > cookieFullModel = aov(size ~ tray + chilled + butter + tray:chilled + tray:butter +
       chilled:butter, data=cookies)
2 > anova(cookieFullModel)
3 Analysis of Variance Table
4
5 Response: size
6
                Df Sum Sq Mean Sq F value Pr(>F)
7
                 1 25.133 25.133 1.4696 0.24198
  trav
8 chilled
                 1 18.131
                            18.131
                                    1.0602 0.31760
9 butter
                  1 48.621
                            48.621
                                     2.8431 0.11003
10 tray: chilled
                 1
                     0.680
                             0.680
                                     0.0398 0.84430
11 tray:butter
                 1 106.597 106.597
                                    6.2332 0.02311
12 chilled:butter 1 55.085
                            55.085
                                     3.2211 0.09050 .
               17 290.726
13 Residuals
                            17.102
14 -
15 Signif. codes: 0 Ś***Š 0.001 Ś**Š 0.01 Ś*Š 0.05 Ś.Š 0.1 Ś Š 1
```

Listing 2: Full Model ANOVA Table

For robustness, examining the full model yields the same result that the individual factors are not enough to result in a difference in the size of the cookies.

```
1 > cookieMainModel = aov(size ~ tray + chilled + butter, data=cookies)
2 > anova (cookieMainModel)
3 Analysis of Variance Table
4
5 Response: size
6
            Df Sum Sq Mean Sq F value Pr(>F)
           1 25.13 25.133 1.1094 0.3048
7 tray
8 chilled
           1 18.13 18.131 0.8003 0.3816
9 butter
            1 48.62 48.621 2.1462 0.1585
10 Residuals 20 453.09 22.654
11
12 Signif. codes: 0 Ś***Š 0.001 Ś**Š 0.01 Ś*Š 0.05 Ś.Š 0.1 Ś Š 1
```

Listing 3: Main Effects Model ANOVA Table

Moving to check our normality assumptions, the below Q-Q and Residual vs Fitted Plots. The residual vs fitted plot shows relatively constant variance and there is nothing significantly out of place in the Q-Q plot to indicate that our normality assumptions are violated. The tails are both a bit skewed but the majority of the data is within a reasonable variance. Performing a log and square-root transformation on the data yielded minimal change in the normality plots, so the unaltered model was used.

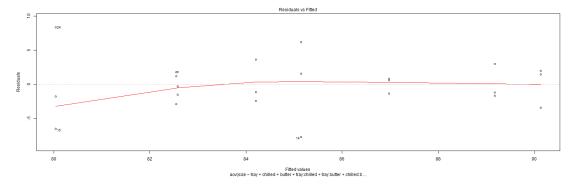


Figure 4: Residual vs Fitted Plot for Full Model

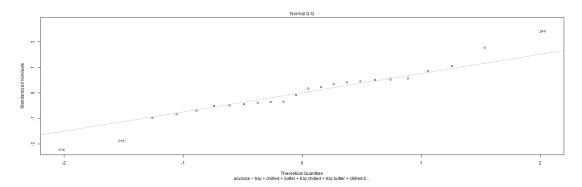


Figure 5: Q-Q Plot for Full Model

Finally, because the only significant terms are interaction terms, an interaction plot was created for the two interaction pairs. These plots are below:

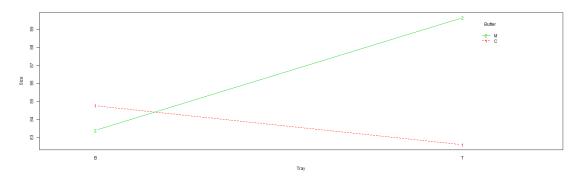


Figure 6: (Tray Position:Butter Type) Interaction Plot

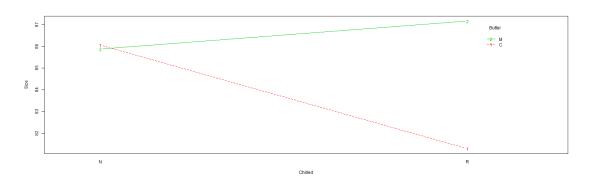


Figure 7: (Dough Temperature:Butter Type) Interaction Plot

## DATA APPENDIX

Size (mm)	Butter	Dough Temperature	Tray Position
85.61	С	N	В
87.56	С	N	В
83.03	M	R	В
87.78	С	N	В
81.78	M	R	В
83.70	С	R	В
84.32	С	R	В
87.83	M	R	В
82.28	M	N	В
81.06	M	N	В
79.60	С	R	В
84.38	M	N	В
91.32	С	N	T
77.38	С	N	Т
73.49	С	R	T
78.23	С	R	T
86.69	M	R	T
87.93	M	N	T
86.72	С	N	Т
87.45	M	N	T
91.57	M	R	T
92.12	M	R	T
92.17	M	N	T
88.42	С	R	Т

Table of Collected Data

## **CODE APPENDIX**

```
2 #### Setup
4 ## Install and load libraries
5 # ipak function taken from: https://gist.github.com/stevenworthington/3178163
6 ipak = function(pkg) {
   new.pkg = pkg[!(pkg %in% installed.packages()[, "Package"])]
8
   if (length (new.pkg))
9
     install.packages(new.pkg, dependencies = TRUE)
10
  sapply(pkg, require, character.only = TRUE)
11 }
12 packages = c("ggplot2", "ggplotify", "reshape2", "gridExtra", "TSA", "astsa",
            "orcutt", "nlme", "fGarch", "vars", "lsmeans", "multcompView",
13
           "base2grob", "lme4", "lmerTest")
14
15 ipak (packages)
16
18 #### Randomly assign 3 of each pair of treatments to spots on the tray
20 options = c(rep("MR",3), rep("MN",3), rep("CR",3), rep("CN",3))
21 tray1 = sample(options)
22 tray2 = sample(options)
23 trav1
24 tray2
25
29 cookies=read.table("cookies.txt",header=TRUE)
30
32 ## Plot Data in Boxplots
34 plotWidth=512;
35 plotHeight=512;
37 ######################
38 ## Individual Plots
39 #######################
41 png("./figures/boxplots/boxplot-1-butter.png", width = plotWidth, height = plotHeight
   boxplot(size ~ butter, data=cookies, main = "Butter")
42
43 dev. off()
44
45 png("./figures/boxplots/boxplot-1-chilled.png", width = plotWidth, height =
     plotHeight)
46
   boxplot(size ~ chilled, data=cookies, main = "Dough Temperature")
47 dev. off()
49 png("./figures/boxplots/boxplot-1-tray.png", width = plotWidth, height = plotHeight)
boxplot(size ~ tray, data=cookies, main = "Tray Position")
51 dev. off ()
53 ######################
54 ## Pair Plots
55 #####################
56 png("./figures/boxplots/boxplot-2-butter-chilled.png", width = plotWidth, height =
     plotHeight)
  boxplot(size ~ chilled + butter, data=cookies, main = "Butter & Temperature")
58 dev. off ()
60 png("./figures/boxplots/boxplot-2-butter-tray.png", width = plotWidth, height =
  plotHeight)
```

```
61 boxplot(size ~ tray + butter, data=cookies, main = "Butter & Tray")
62 dev. off()
63
64 png("./figures/boxplots/boxplot-2-chilled-tray.png", width = plotWidth, height =
     boxplot(size ~ tray + chilled, data=cookies, main = "Temperature & Tray")
65
66 dev. off ()
67
68 ####################
69 ## Full Plot
70 ####################
71 png("./figures/boxplot-full.png", width = 2*plotWidth, height = 2*plotHeight)
72 boxplot(size ~ tray + chilled + butter, data=cookies)
74
75 #####################
76 ## Compile Plots
77 #####################
78 singleBoxplots = lapply(sprintf("./figures/boxplots/boxplot-1-%s.png", c("butter","
       chilled","tray")), png::readPNG)
79 singleBoxGrid = lapply(singleBoxplots, grid::rasterGrob)
80
81 doubleBoxPlots = lapply(sprintf("./figures/boxplots/boxplot-2-%s.png", c("butter-
       chilled","butter-tray","chilled-tray")), png::readPNG)
82 doubleBoxGrid = lapply(doubleBoxPlots, grid::rasterGrob)
84 png("./figures/boxplot-individuals.png", width = 3*plotWidth, height = plotHeight)
85 gridExtra::grid.arrange(ncol=3, grobs=singleBoxGrid)
86 dev. off ()
88 png("./figures/boxplot-pairs.png", width = 3*plotWidth, height = plotHeight)
89 gridExtra::grid.arrange(ncol=3, grobs=doubleBoxGrid)
90 dev. off()
95 cookieFullModel = aov(size ~ tray + chilled + butter + tray:chilled + tray:butter +
       chilled:butter, data=cookies)
96 anova (cookieFullModel)
97
98 cookieMainModel = aov(size ~ tray + chilled + butter, data=cookies)
99 anova (cookieMainModel)
101 #######################
102 # Check Normality
103 ######################
104 png("./figures/normality-residuals.png", width = 3*plotWidth, height = plotHeight)
plot (cookieFullModel, 1)
106 dev. off ()
107
108 png("./figures/normality-qq.png", width = 3*plotWidth, height = plotHeight)
109 plot (cookieFullModel, 2)
110 dev. off ()
112 ########################
113 # Examine Interactions
114 ######################
115 png("./figures/interaction-tray-butter.png", width = 3*plotWidth, height = plotHeight
116
     interaction.plot(x.factor = cookies$tray, trace.factor = cookies$butter,
                     response = cookies$size, type ="b",col = 2:3,
117
                     xlab ="Tray", ylab ="Size", trace.label ="Butter")
118
119 dev. off ()
120
```