

Robustness of Deep Neural Networks against white-box adversarial attacks

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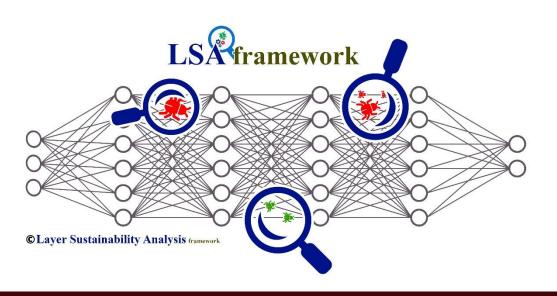






- Review on prev. presentations
- Paper review
 - Layer-wise Regularized Adversarial Training (AT-LR)

using Layers Sustainability Analysis (LSA) framework







• Attack

$$\boldsymbol{x}^* = \boldsymbol{x} + \epsilon \cdot \operatorname{sign}\left(\nabla_{\boldsymbol{x}} J(\boldsymbol{x}, y)\right)$$

$$L_{\infty}$$
 norm $||x^* - x||_{\infty} \le \varepsilon$

$$\operatorname*{arg\,min}_{\delta} \|\delta\|_p + c \cdot J(x+\delta,y)$$
 s.t. $x+\delta \in [0,1]^n$



"panda"
57.7% confidence



 $sign(\nabla_{\boldsymbol{x}}J(\boldsymbol{\theta},\boldsymbol{x},y))$ "nematode" 8.2% confidence



 $x + \epsilon sign(\nabla_x J(\theta, x, y))$ "gibbon"

99.3 % confidence

• Defense

- Data manipulation
- Architecture manipulation
- Loss manipulation

$$\min_{\theta} \rho(\theta), \quad \text{where} \quad \rho(\theta) = \mathbb{E}_{(x,y) \sim \mathcal{D}} \left[\max_{\delta \in \mathcal{S}} L(\theta, x + \delta, y) \right]$$



• Adversarial Training (AT)

A method for learning robust deep networks
It is typically assumed to be **more expensive** than **traditional training**constructing adversarial examples via a first-order method like projected gradient decent (PGD)

$$\min_{\theta} \sum_{i} \max_{\delta \in \Delta} \ell(f_{\theta}(x_i + \delta), y_i)$$

robust optimization problem

$$\Delta = \{\delta : \|\delta\|_{\infty} \le \epsilon\} \quad \epsilon > 0$$

Madry et al. (2017)

$$\delta^{\star} = \epsilon \cdot \operatorname{sign}(\nabla_x \ell(f(x), y))$$

Goodfellow et al. (2014)

A better approximation of the inner maximization is to take multiple

$$\ell$$
 Loss function

$$f_{\theta}$$
 Network

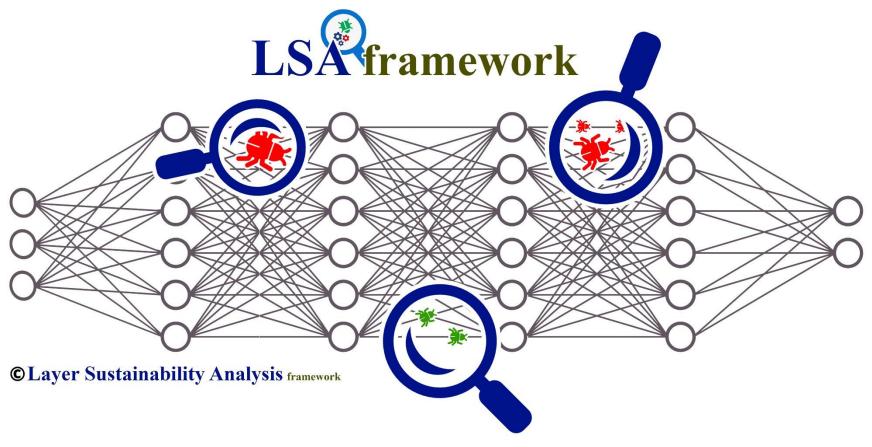
$$\theta$$
 Parameters



Latest work



• Layer-wise Regularized Adversarial Training using Layers Sustainability Analysis (LSA) framework

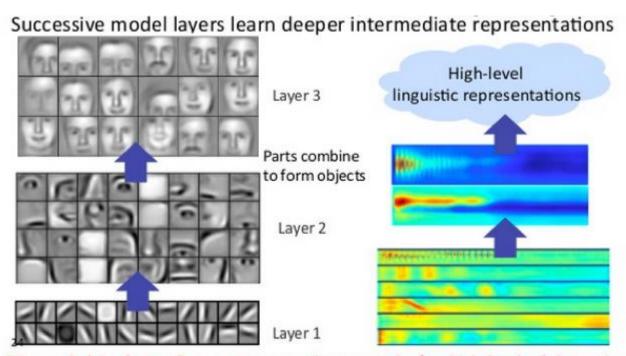


https://github.com/khalooei/LSA



Latest work: Motivation





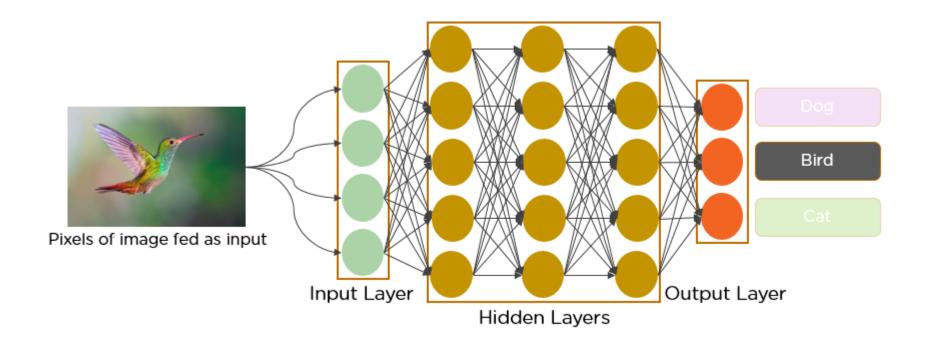
Prior: underlying factors & concepts compactly expressed w/ multiple levels of abstraction

https://wiki.pathmind.com/neural-network



Latest work: Motivation







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• Layer-wise Regularized Adversarial Training using Layers Sustainability Analysis (LSA) framework

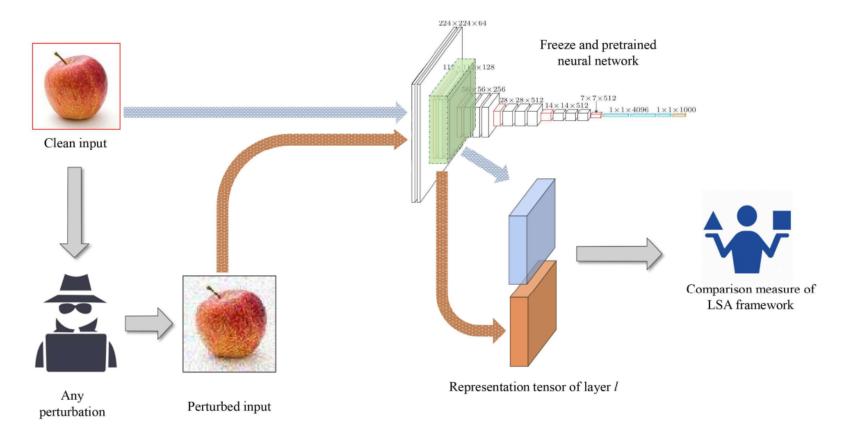


Fig. 1. Diagram of the Layer Sustainability Analysis (LSA) framework

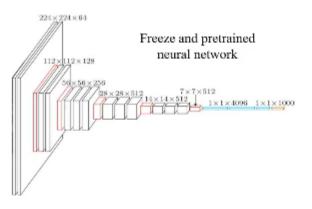


Latest work: idea



• Layer-wise Regularized Adversarial Training using Layers Sustainability Analysis (LSA) framework





Layer Sustainability Analysis (LSA) framework



Latest work: idea



• Layer-wise Regularized Adversarial Training using Layers Sustainability Analysis (LSA) framework

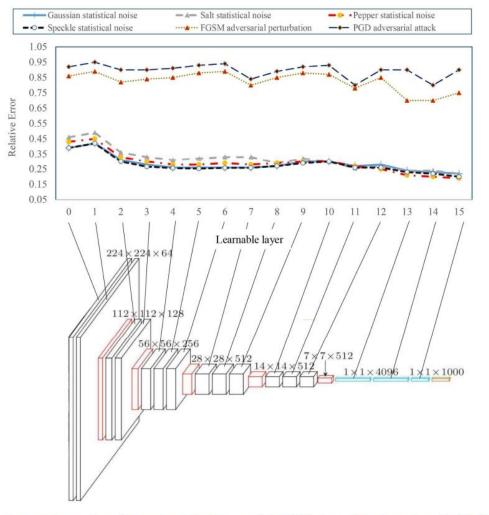


Fig. 2. Comparison measure values for corresponding layers of the VGG network in the proposed LSA framework

Lipschitz condition



Lipschitz condition

Definition: function f(t, y) satisfies a **Lipschitz condition** in the variable y on a set $D \subset \mathbb{R}^2$ if a constant L > 0 exists with

$$|f(t, y_1) - f(t, y_2)| \le L|y_1 - y_2|,$$

whenever $(t, y_1), (t, y_2)$ are in D. L is Lipschitz constant.

$$||F(x_1) - F(x_2)|| \le \psi ||x_1 - x_2||$$
 s.t. $x_1, x_2 \subset X$.

Latest work: Lipschitz condition



$$||F(x_1) - F(x_2)|| \le \psi ||x_1 - x_2||$$
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$$\|\phi_l(x_1) - \phi_l(x_2)\| \le \psi \|x_1 - x_2\|.$$

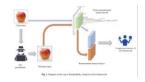


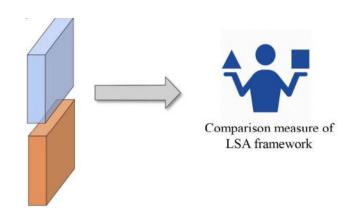
$$\|\phi_l(x) - \phi_l(\hat{x})\| \le \psi \|x - \hat{x}\|.$$



Latest work: proposed method







$$CM\big(\phi_l(x),\phi_l(\hat{x})\big) = \frac{\|\phi_l(x)-\phi_l(\hat{x})\|_F}{\|\phi_l(x)\|_F},$$

$$\mu = \frac{1}{M \times Ly} \sum_{m=0}^{M-1} \sum_{l=0}^{Ly-1} CM(\phi_l(x_m), \phi_l(\hat{x}_m)),$$

$$\sigma = \sqrt{\frac{1}{M \times Ly} \sum_{m=0}^{M-1} \sum_{l=0}^{Ly-1} \left(CM \left(\phi_l(x_m), \phi_l(\hat{x}_m) \right) - \mu \right)^2},$$



Latest work: proposed method



Algorithm 1. Algorithm to find the most vulnerable layers in the layer sustainability analysis (LSA) framework

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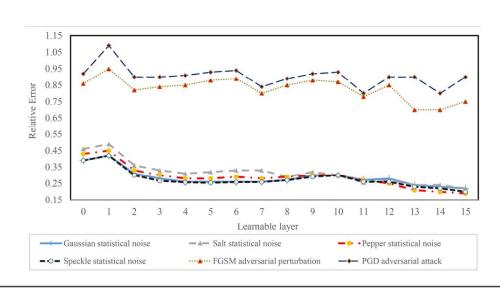
Input: Output representation tensors $\phi_l(x)$ and $\phi_l(\hat{x})$ of layer l for clean input x and the corresponding perturbed sample \hat{x}

Output: list of most vulnerable layers

Algorithm steps:

for trained model m, constant η , average μ and standard deviation σ as calculated in equation (12).

- 1. LSA_MVL_list = []
- 2. for l in range(0, Ly)
- 3. if $(CM(\phi_l(x), \phi_l(\hat{x})) \mu) > \eta \sigma$
- 4. LSA_MVL_list.append(*l*)
- 5. LSA_MVL_list = sort(LSA_MVL_list)





Latest work: proposed method



Algorithm 2. Layer sustainability analysis (LSA) framework's algorithm

Algorithm 2 Layer Sustainability Analysis (LSA) framework

Input: model m, train data D_{train} , test data D_{test} , attack method and its parameters

Output: list of vulnerable layers

Algorithm steps:

- 1. Standard training of model m using D_{train} samples
- 2. Execute attack on the trained model m and obtain adversarial examples by perturbing D_{test} samples
- 3. Run Algorithm 1 and tune the proper cut-off threshold η of Algorithm 1 to find out the MVL list
- 4. Return the MVL list of Algorithm 1





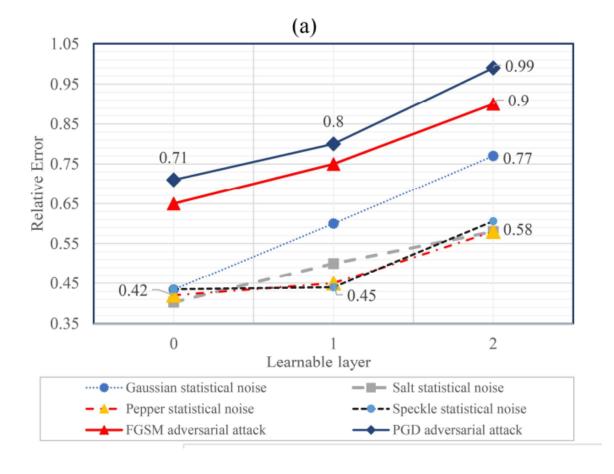
• Experiment architectures

Table 1 Experiment architectures A, B, C, and D

Model A	$linear(100) \Rightarrow ELU \Rightarrow Linear(100) \Rightarrow ELU \Rightarrow Linear(100) \Rightarrow ELU \Rightarrow Linear(1)$
Model B	$Conv2D(16, (5 \times 5)) \Rightarrow ReLU() \Rightarrow Conv2D(32, (5 \times 5)) \Rightarrow ReLU() \Rightarrow MaxPool2D(2,2)$
Wiodel B	$\Rightarrow Conv2D(64,(5\times5)) \Rightarrow ReLU() \Rightarrow MaxPool2D(2,2) \Rightarrow Linear(100) \Rightarrow ReLU() \Rightarrow Linear(10)$
Model C	VGG-19 architecture [63]
Model D	WideResNet [68]







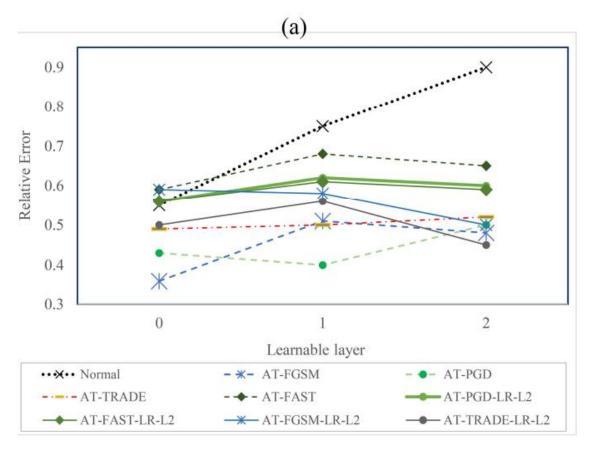






Table 2. Evaluation of model A on Moon dataset with different loss functions against FGSM adversarial attack.

	Accuracy of model A against FGSM with different epsilon values						
Training type	0	0.1	0.2	0.3	0.4	0.5	R&G Score
Normal	97.07	93.63	82.5	76.83	63.79	52.35	466.17
AT-FGSM	95.86	91.98	87.88	81.33	70.54	58.69	486.28
AT-PGD	86.5	83.89	80.87	76.61	72.57	60.02	460.46
AT-TRADE	96.17	93.06	85.78	74.2	68.62	59.68	477.51
AT-FAST	94.32	89.72	84.91	78.35	70.18	61.65	479.13
AT-FGSM-LR-L0	92.81	90.25	85.36	80.74	68.21	58.74	476.11
AT-FGSM-LR-L1	91.87	89.77	86.95	81.51	69.15	59.59	478.84
AT-FGSM-LR-L2	93.98	93.01	89.12	84.01	75.15	63.25	498.52
AT-PGD-LR-L0	87.02	84.02	80.64	76.22	71.12	65.87	464.89
AT-PGD-LR-L1	86.2	82.94	79.23	75.16	70.5	65.04	459.07
AT-PGD-LR-L2	88.78	86.93	81.25	77.01	72.81	66.58	473.36
AT-FAST-LR-L0	86.86	83.85	80.33	76.34	71.34	65.79	464.51
AT-FAST-LR-L1	87.91	85.43	82.44	77.38	70.01	62.25	465.42
AT-FAST-LR-L2	92.91	90.31	86.26	81.53	75.09	67.65	493.75
AT-TRADE-LR-L0	86.84	82.38	80.55	76.37	71.58	64.07	461.79
AT-TRADE-LR-L1	87.25	84.22	81.25	76.98	71.14	63.25	464.09
AT-TRADE-LR-L2	96.67	93.2	86.56	81.25	79.5	68.65	505.83





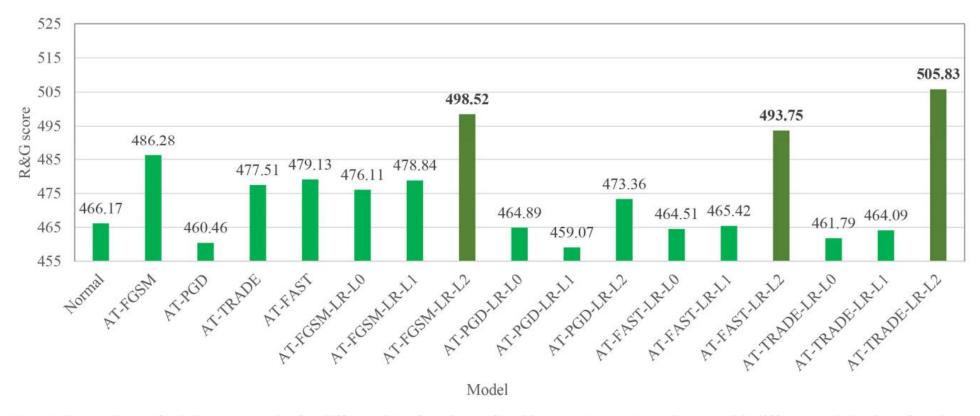


Fig. 6. Comparison of R&G score results for different loss functions of architecture A on Moon dataset with different training loss functions.





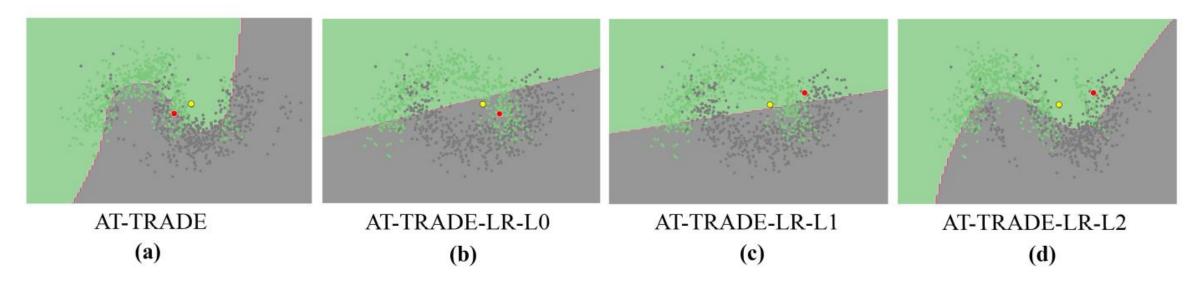
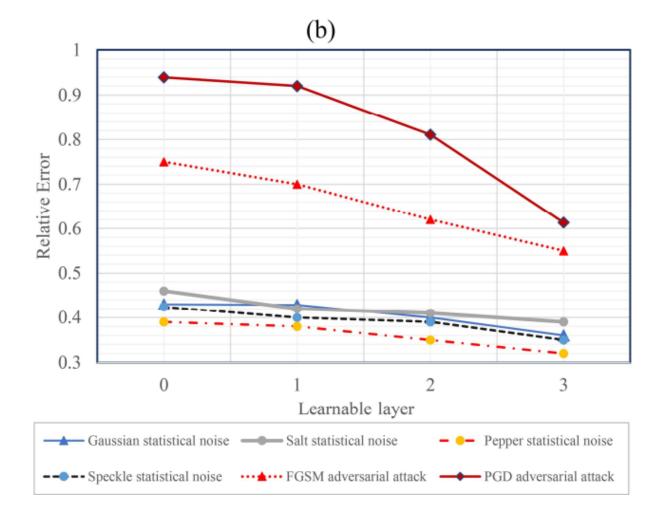


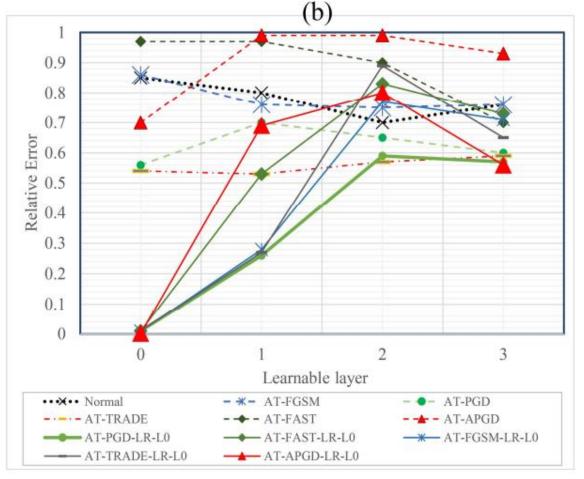
Fig. 7. Decision boundary of adversarial training with different loss functions on Model A.





• MNIST Dataset // model B (CNN)









• MNIST Dataset // model B (CNN)

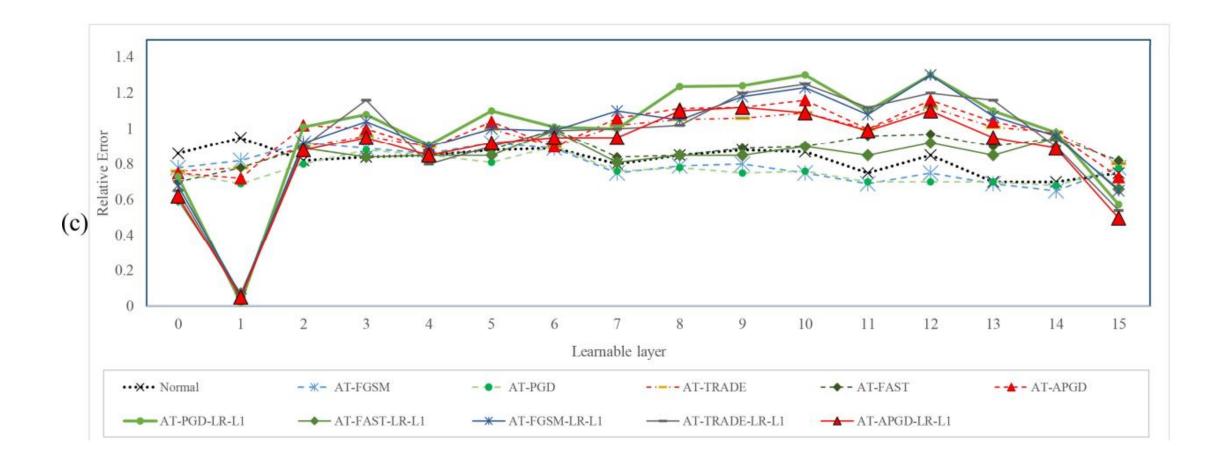
Table 3. Evaluation of model B on MNIST dataset with different loss functions against FGSM adversarial attack.

	Accuracy of model A against FGSM with different epsilon values						
Training type	0	0.1	0.2	0.3	0.4	0.5	R&G Score
Normal	98.82	82.1	47.2	17.87	6.96	4.25	257.2
AT-APGD	99.36	98.54	97.67	96.97	71.72	33.73	497.99
AT-APGD-LR-L0	98.97	98.11	97.36	97.17	94.6	55.52	541.73





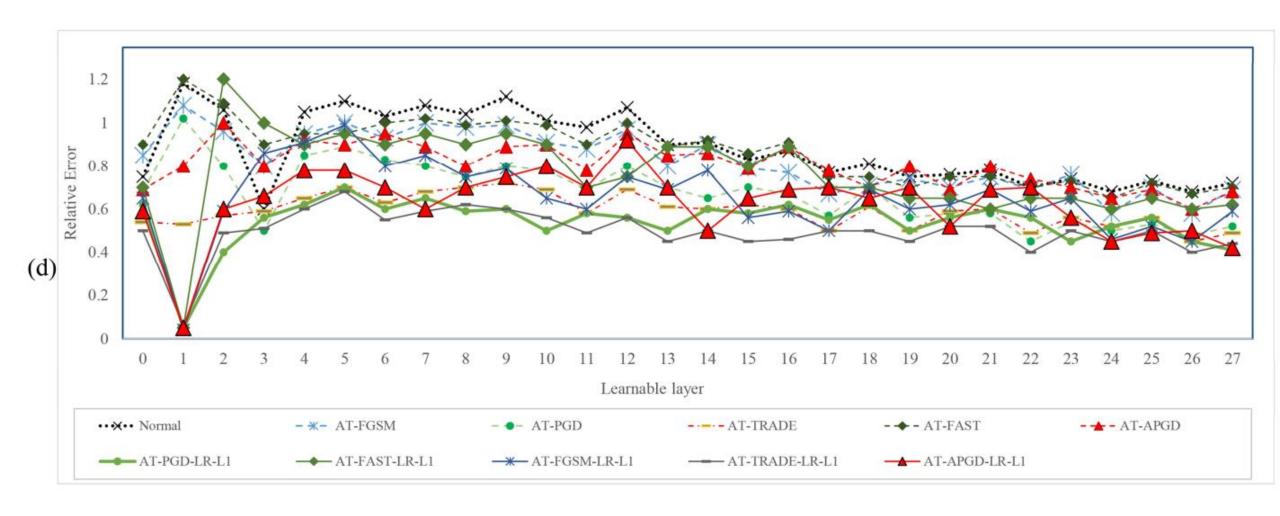
• CIFAR10 Dataset // model C (VGG19)







• CIFAR10 Dataset // model D (WideResnet)







• CIFAR10 Dataset // model D (WideResnet)

Table 4. Evaluation of models C and D on CIFAR-10 with different loss functions against FGSM adversarial attack.

		Accuracy of model C and D against FGSM with different epsilon values					
Architecture	Training type	0	0.01	0.03	0.1	0.2	R&G Score
	Normal	90.53	48.91	43.91	31.5	22.29	237.14
Model C	AT-APGD	83.68	74.69	72.21	50.04	41.45	322.07
	AT-APGD-LR-L1	83.55	75.32	73.35	52.36	46.01	330.59
	Normal	90.01	40.01	36.35	22.3	16.2	204.87
Model D	AT-APGD	82.60	50.12	47.11	41.46	40.01	261.3
	AT-APGD-LR-L1	81.81	53.21	48.17	43.01	42.65	268.85











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