## **Basic Jupyter Notebook Tutorial**

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Modified from Berkeley Python Bootcamp 2013 <a href="https://github.com/profjsb/python-bootcamp">https://github.com/profjsb/python-bootcamp</a> (<a href="https://github.com/profjsb/python-bootcamp">https://github.com/profjsb/python-bootcamp</a>)

and Python for Signal Processing <a href="http://link.springer.com/book/10.1007%2F978-3-319-01342-8">http://link.springer.com/book/10.1007%2F978-3-319-01342-8</a> (<a href="http://link.springer.com/book/10.1007%2F978-3-319-01342-8">http://link.springer.com/book/10.1007%2F978-3-319-01342-8</a>)

and EE 123 iPython Tutorial <a href="http://inst.eecs.berkeley.edu/~ee123/sp14/lab/python\_tutorial.ipynb">http://inst.eecs.berkeley.edu/~ee123/sp14/lab/python\_tutorial.ipynb</a> (<a href="http://inst.eecs.berkeley.edu/~ee123/sp14/lab/python\_tutorial.ipynb">http://inst.eecs.berkeley.edu/~ee123/sp14/lab/python\_tutorial.ipynb</a>).

This lab serves as a quick overview of Jupyter Notebooks, numpy, matplotlib, and simulations in Python, which we will use throughout the course. If you are unfamiliar with these, you should carefully read through all of the examples. You are only required to answer the two questions at the bottom for credit.

# General Jupyter Notebook Usage Instructions (Overview)

- Start by clicking Help >> User Interface Tour to get yourself familiar with the Jupyter Notebook environment.
- Click the Play button to run and advance a cell. The short-cut for it is Shift-Enter.
- To add a new cell, either select "Insert >> Insert New Cell Below" or click the Plus button.
- You can change the cell mode from code to text in the pulldown menu. Use Markdown for writing text.
- You can change the text in Markdown cells by double-clicking it. The short-cut for this is enter.
- To save your notebook, either select "File >> Save and Checkpoint" or hit Command-s for Mac and Ctrl-s for Windows.
- To undo edits within a cell, hit Command-z for Mac and Ctrl-z for Windows.
- Help >> Keyboard Shortcuts has a list of all useful keyboard shortcuts.
- The Help menu also has links to many reference docs you may find useful this semester (e.g. Markdown, Python, NumPy, Matplotlib, SciPy).

### **Tab Completion**

One useful feature of iPython is tab completion:

```
In [1]: x = 1
y = 2
x_plus_y = x + y

# Type `x_` then hit TAB to auto-complete the variable and then press St
# Enter to run the cell.
print(x_plus_y)
3
```

## Help

Another useful feature is the help command. Type any function followed by ? and run the cell to return a help window. Hit the x button to close it.

## Floats and Integers

Doing math in Python is easy, but note that there are int and float types in Python. In Python 3, integer division returns the same results as floating point division.

```
In [3]: 59 / 87
Out[3]: 0.6781609195402298
In [4]: 59 / 87.0
Out[4]: 0.6781609195402298
```

## **Strings**

- Double quotes and single quotes are the same thing.
- '+' concatenates strings.

```
In [5]: # This is a comment.
   "Hi " + 'Bye'
Out[5]: 'Hi Bye'
```

## **Printing**

Here are some fancy ways of printing:

#### Lists

A list is a mutable array of data, i.e. it can constantly be modified. See <a href="http://stackoverflow.com/questions/8056130/immutable-vs-mutable-types-python">http://stackoverflow.com/questions/8056130/immutable-vs-mutable-types-python</a>) for more info. If you are not careful, using mutable data structures can lead to bugs in code that passes common data to many different functions.

Important functions:

- Created a list by using square brackets [ ].
- '+' appends lists.
- len(x) gets the length of list x.

## **Tuples**

A tuple is an immutable list. They can be created using round brackets ( ).

They are usually used as inputs and outputs to functions.

## Arrays (NumPy)

A NumPy array is like a list with multidimensional support and more functions. We will be using it a lot.

Arithmetic operations on NumPy arrays correspond to elementwise operations.

Important functions:

- . shape returns the dimensions of the array.
- .ndim returns the number of dimensions.
- .size returns the number of entries in the array.
- len() returns the first dimension.

To use functions in NumPy, we have to import NumPy to our workspace. This is done by the command import numpy. By convention, we rename numpy as np for convenience.

```
In [14]: # by convention, import numpy as np
import numpy as np

x = np.array([[1, 2, 3], [4, 5, 6]])

print(x)

[[1 2 3]
  [4 5 6]]
```

```
In [15]: print("Number of Dimensions:", x.ndim)
         Number of Dimensions: 2
In [16]: print("Dimensions:", x.shape)
         Dimensions: (2, 3)
In [17]: print("Size:", x.size)
         Size: 6
In [18]: print("Length:", len(x))
         Length: 2
In [19]: a = np.array([1, 2, 3])
         print("a = ", a)
         # elementwise arithmetic
         print("a * a = ", a * a)
         a = [1 2 3]
         a * a = [1 4 9]
In [20]: b = np.array(np.ones((3, 3))) * 2
         print("b = \n", b)
         c = np.array(np.ones((3, 3)))
         print("c = \n", c)
         b =
          [[2. 2. 2.]
          [2. 2. 2.]
          [2. 2. 2.]]
          c =
          [[1. 1. 1.]
          [1. 1. 1.]
          [1. 1. 1.]]
         Multiply elementwise:
In [21]: print("b * c = \n", b * c)
         b * c =
          [[2. 2. 2.]
          [2. 2. 2.]
          [2. 2. 2.]]
```

Now multiply as matrices (not arrays):

```
In [22]: print("b * c =\n", np.dot(b, c))

b * c =
    [[6. 6. 6.]
    [6. 6. 6.]]
[6. 6. 6.]
```

With Python3, you can also use the "@" operator for the dot product

```
In [23]: print("b * c =\n", b @ c)

b * c =
   [[6. 6. 6.]
   [6. 6. 6.]
   [6. 6. 6.]]
```

Alternatively, we can just convert to or create a matrix instead of an array and then use normal multiplication:

```
In [24]: print("b * c =\n", np.matrix(b) * np.matrix(c))

d = np.matrix([[1, 1j, 0], [1, 2, 3]])
e = np.matrix([[1], [1j], [0]])

print("d * e =\n", d * e)

b * c =
   [[6. 6. 6.]
   [6. 6. 6.]
   [6. 6. 6.]]
   d * e =
   [[0.+0.j]
   [1.+2.j]]
```

## **Slicing for NumPy Arrays**

NumPy uses pass-by-reference semantics so it creates views into the existing array, without implicit copying. This is particularly helpful with very large arrays because copying can be slow.

[1 2 3 4]

Since slicing does not copy the array, changing y changes x:

```
In [27]: y[0] = 7
print(x)
print(y)

[7 2 3 4 5 6]
[7 2 3 4]

To actually copy x, we should use .copy:

In [28]: x = np.array([1, 2, 3, 4, 5, 6])
y = x.copy()
y[0] = 7
print(x)
print(y)

[1 2 3 4 5 6]
[7 2 3 4 5 6]
```

## **Plotting**

In this class we will use matplotlib.pyplot to plot signals and images.

To begin with, we import matplotlib.pyplot as plt (again for convenience).

```
In [29]: import numpy as np
# by convention, we import pyplot as plt
import matplotlib.pyplot as plt
# import r_ function from numpy
from numpy import r_

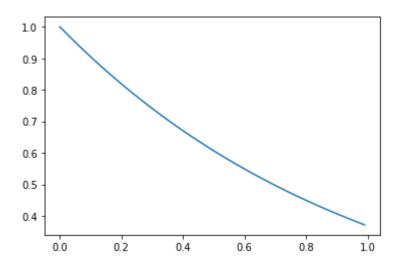
# if you don't specify a number before the colon, the starting index den
# to 0
x = r_[:1:0.01]
a = np.exp(-x)
b = np.sin(x * 10.0) / 4.0 + 0.5

# plot in browser instead of opening new windows
%matplotlib inline
```

plt.plot(x, a) plots a against x.

```
In [30]: plt.figure()
plt.plot(x, a)
```

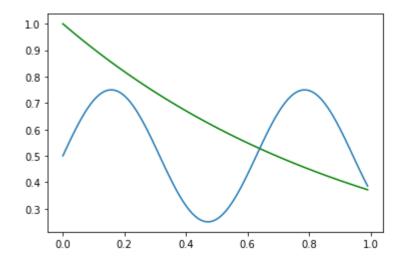
Out[30]: [<matplotlib.lines.Line2D at 0x115232e50>]



Once you started a figure, you can keep plotting to the same figure.

```
In [31]: plt.figure()
  plt.plot(x, a, "green")
  plt.plot(x, b)
```

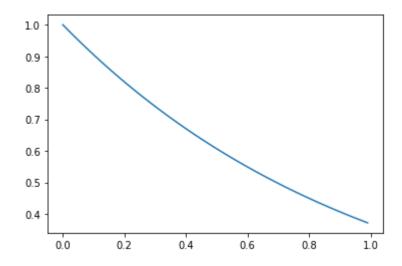
Out[31]: [<matplotlib.lines.Line2D at 0x114b48a10>]

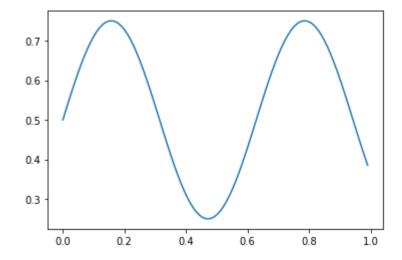


To plot different plots, you can create a second figure.

```
In [32]: plt.figure()
  plt.plot(x, a)
  plt.figure()
  plt.plot(x, b)
```

Out[32]: [<matplotlib.lines.Line2D at 0x11573b610>]



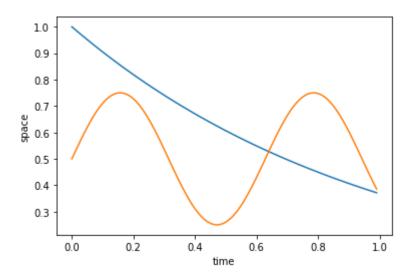


To label the axes, use plt.xlabel() and plt.ylabel().

```
In [33]: plt.figure()
  plt.plot(x, a)
  plt.plot(x, b)

plt.xlabel("time")
  plt.ylabel("space")
```

#### Out[33]: Text(0, 0.5, 'space')



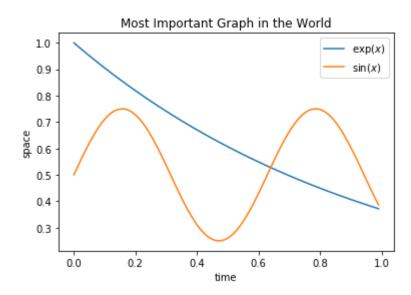
You can also add title and legends using plt.title() and plt.legend().

```
In [34]: plt.figure()
plt.plot(x, a)
plt.plot(x, b)
plt.xlabel("time")
plt.ylabel("space")

plt.title("Most Important Graph in the World")

plt.legend(("$\exp(x)$", "$\sin(x)$"))
```

Out[34]: <matplotlib.legend.Legend at 0x11584c490>



There are many options you can specify in plot(), such as color and linewidth. You can also change the axis using plt.axis.

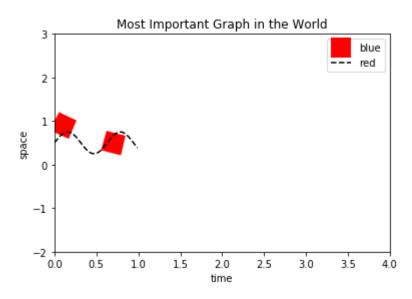
```
In [35]: plt.figure()
   plt.plot(x, a, ":r", linewidth=20)
   plt.plot(x, b , "--k")
   plt.xlabel("time")
   plt.ylabel("space")

plt.title("Most Important Graph in the World")

plt.legend(("blue", "red"))

plt.axis([0, 4, -2, 3])
```

#### Out[35]: [0, 4, -2, 3]

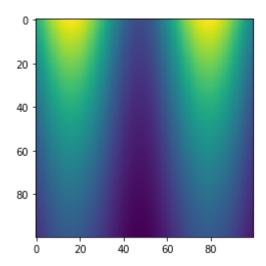


There are many other plotting functions. For example, we will use plt.imshow() for showing images and plt.stem() for plotting discretized signals.

```
In [36]: # image
plt.figure()

# plotting the outer product of a and b
data = np.outer(a, b)
plt.imshow(data)
```

Out[36]: <matplotlib.image.AxesImage at 0x115c17510>

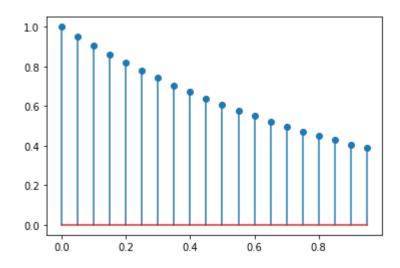


```
In [37]: # stem plot
    plt.figure()
    # subsample by 5
    plt.stem(x[::5], a[::5])
```

/Users/wjgan/anaconda3/lib/python3.7/site-packages/ipykernel\_launcher. py:4: UserWarning: In Matplotlib 3.3 individual lines on a stem plot w ill be added as a LineCollection instead of individual lines. This sig nificantly improves the performance of a stem plot. To remove this war ning and switch to the new behaviour, set the "use\_line\_collection" ke yword argument to True.

after removing the cwd from sys.path.

Out[37]: <StemContainer object of 3 artists>

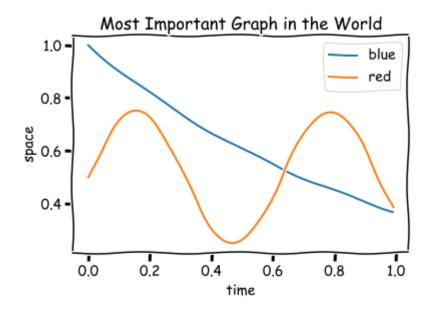


```
In [38]: # xkcd style plots
# Note: Requires matplotlib version 1.3.1 or higher
plt.xkcd()
plt.plot(x, a)
plt.plot(x, b)
plt.xlabel("time")
plt.ylabel("space")

plt.title("Most Important Graph in the World")

plt.legend(("blue", "red"))
```

Out[38]: <matplotlib.legend.Legend at 0x115c9ee50>



To turn off xkcd style plotting, restart the kernel or run the command plt.rcdefaults().

## Logic

#### For Loop

Indentation matters in Python. Everything indented belongs to the loop:

#### If-Else

Same goes for If-Else:

## **Random Library**

The NumPy random library should be your resource for all Monte Carlo simulations which require generating instances of random variables.

The documentation for the library can be found here:

http://docs.scipy.org/doc/numpy/reference/routines.random.html (http://docs.scipy.org/doc/numpy/reference/routines.random.html)

The function rand can be used to generates a uniform random number in the range [0, 1).

```
In [42]: from numpy import random

# random number
print(random.rand())
# random vector
print(random.rand(5))
# random matrix
print(random.rand(3, 3))

0.30827390446658687
[0.43193358 0.89712897 0.25453753 0.6048372 0.78784836]
[[0.38848219 0.3484001 0.67090501]
[0.2018519 0.61155685 0.04911921]
[0.67024566 0.3083388 0.6769348 ]]
```

Let's see how we can use this to generate a fair coin toss (i.e. a discrete Bernoulli(1/2) random variable).

```
In [43]: # Bernoulli(1/2) random variable
x = round(random.rand())
print(x)
```

Now let's generate several fair coin tosses and plot a histogram of the results.

```
k = 100
In [44]:
         x1 = [round(random.rand()) for _ in range(k)]
         plt.figure()
         plt.hist(x1)
         # we could also use NumPy's round function to elementwise round the vect
         x2 = np.round(random.rand(k))
         plt.figure()
         plt.hist(x2)
Out[44]:
          (array([42.,
                        0., 0., 0., 0., 0., 0.,
                                                        0.,
                                                             0., 58.]),
          array([0., 0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, 1.]),
          <a list of 10 Patch objects>)
          50 -
          40 •
          30 -
          20 •
           10 -
                      0.2
                              0.4
                                             8.0
               0.0
                                      0.6
                                                     1.0
          60 -
          50 •
          40 •
          30 -
          20 -
           10 -
                      0.2
```

0.4

0.6

We can do something similar for several other distributions, and allow the histogram to give us a sense of what the distribution looks like. As we increase the number of samples we take from the distribution k, the more and more our histogram looks like the actual distribution.

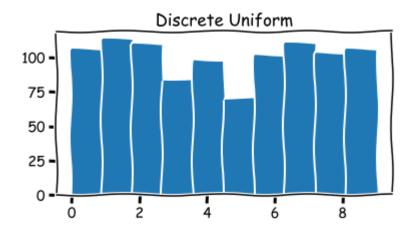
8.0

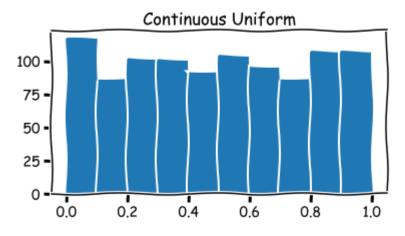
1.0

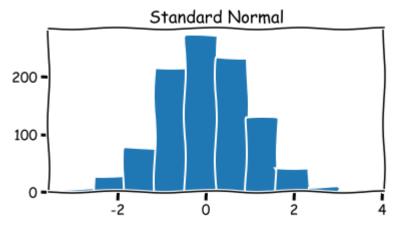
0.0

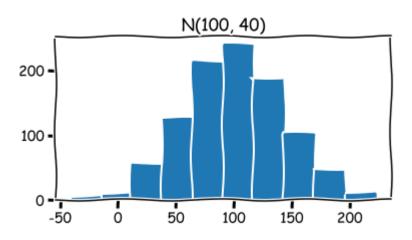
```
In [45]: k = 1000
         # k discrete uniform random variables between 0 and 9
         discrete uniform = random.randint(0, 10, size=k)
         plt.figure(figsize=(6, 3))
         plt.hist(discrete uniform)
         plt.title("Discrete Uniform")
         continuous uniform = random.rand(k)
         plt.figure(figsize=(6, 3))
         plt.hist(continuous uniform)
         plt.title("Continuous Uniform")
         # randn generates elements from the standard normal
         std normal = random.randn(k)
         plt.figure(figsize=(6, 3))
         plt.hist(std_normal)
         plt.title("Standard Normal")
         # To generate a normal distribution with mean mu and standard deviation
         # we must mean shift and scale the variable
         mu = 100
         sigma = 40
         normal_mu_sigma = mu + random.randn(k) * sigma
         plt.figure(figsize=(6, 3))
         plt.hist(normal mu sigma)
         plt.title("N({}, {})".format(mu, sigma))
```

#### Out[45]: Text(0.5, 1.0, 'N(100, 40)')









<sup>^</sup> We could do this all day with all sorts of distributions. I think you get the point.

## Specifying a Discrete Probability Distribution for Monte Carlo Sampling

The following function takes n sample from a discrete probability distribution specified by the two arrays distribution and values .

As an example, let us suppose a random variable X follows the following distribution:

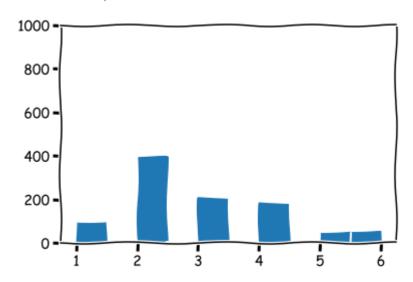
```
X = \begin{cases} 1 \text{ w/ probability } 0.1\\ 2 \text{ w/ probability } 0.4\\ 3 \text{ w/ probability } 0.2\\ 4 \text{ w/ probability } 0.2\\ 5 \text{ w/ probability } 0.05\\ 6 \text{ w/ probability } 0.05 \end{cases}
```

Then we would have: distribution = [0.1, 0.4, 0.2, 0.2, 0.05, 0.05] and values = [1, 2, 3, 4, 5, 6].

```
In [46]: def n sample(distribution, values, n):
              if sum(distribution) != 1:
                  distribution = [distribution[i] / sum(distribution) \
                      for i in range(len(distribution))]
              rand = [random.rand() for i in range(n)]
              rand.sort()
              samples = []
              sample_pos, dist_pos, cdf = 0, 0, distribution[0]
             while sample pos < n:</pre>
                  if rand[sample_pos] < cdf:</pre>
                      sample pos += 1
                      samples.append(values[dist pos])
                  else:
                      dist pos += 1
                      cdf += distribution[dist pos]
              return samples
```

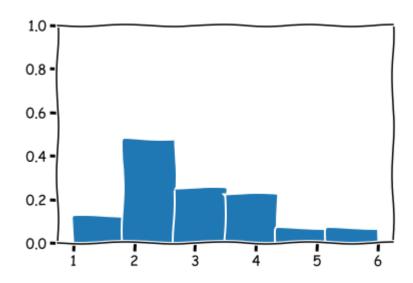
```
In [47]: # collect k samples from X and plot the histogram
    samples_from_x = n_sample(
            [0.1, 0.4, 0.2, 0.2, 0.05, 0.05], [1, 2, 3, 4, 5, 6], k)
    plt.hist(samples_from_x)
    plt.ylim((0, 1000))
    print("Wow, if we normalized the y-axis that would be a PMF. Incredible
    print("I should try that.")
```

Wow, if we normalized the y-axis that would be a PMF. Incredible! I should try that.



In [49]: # Normalize the samples from X to plot the probability mass function being plt.hist(samples\_from\_x, bins=6, density=True)
 plt.ylim((0, 1))

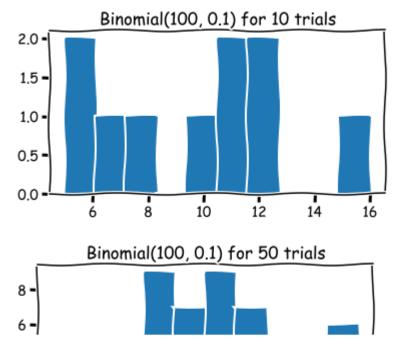




**Question 1: Sampling and Plotting a Binomial Random Variable** 

A binomial random variable  $X \sim \operatorname{Binomial}(n,p)$  can be thought of as the number of heads in n coin flips where each flip has probability p of coming up heads. We can equivalently think of it as the sum of n Bernoulli random variables:  $X = \sum_{i=1}^{n} X_i$  where  $X_i \sim \operatorname{Bernoulli}(p)$ .

In this question, you will put your new plotting skills to work and sample the values of a binomial random variable.



Now that you have plotted many values of a few different binomial random variables, do the results coincide with what you expect them to?

## Question 2: Monte Carlo Method for Estimating Pi

After going through this tutorial, you might wonder: why should we bother with NumPy at all?

While many of you may not have used NumPy previously, or not see the purpose in learning this library, we strongly urge you to force yourself to use NumPy as much as possible while doing virtual labs.

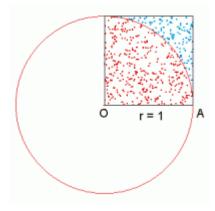
NumPy (and using matrix operations rather than loops) is your friend when it comes to efficiently dealing with lots of data or doing elaborate simulations. If you find yourself using many loops or list comprehensions to process data, think about using NumPy. Furthermore, NumPy is widely used in industry and academic research, and so it will benefit you greatly to become comfortable with it this semester!

Let's work through an example to see the usefulness of NumPy.

#### Estimate the value of $\pi$ using a Monte Carlo method.

Monte Carlo methods are algorithms that use probability and randomness to solve problems that would be difficult otherwise. Here, we will use a Monte Carlo simulation to estimate the value of  $\pi$ .

Suppose we have a one meter by one meter square dartboard with a quarter circle inscribed in it, as shown below:



If we throw darts at the dartboard such that they are equally likely to land anywhere in the square, then as we throw more and more darts, the fraction of them that will land in the quarter circle will approach

$$\frac{\text{Area of quarter circle}}{\text{Area of square}} = \frac{\pi}{4}$$

Therefore, after simulating this process, we can take the fraction of darts that landed within the circle, and multiply this value by 4 to use as our estimate for  $\pi$ .

A version of the simulation that does not use NumPy at all is given. Your job is to reimplement the simulation using NumPy to speed it up. For reference, the staff solution is > 10x better.

```
import time
In [1]:
        import numpy as np
        import random
        def monte carlo pi(num points):
            # num points is the number of random points to choose
            count = 0
            for in range(num points):
                randx, randy = random.random(), random.random()
                if (randx ** 2 + randy ** 2 < 1):
                    count += 1
            estimate = (count * 4.0 / num_points)
            return estimate
        def monte_carlo_pi_numpy(num_points):
            # num points is the number of random points to choose
            # Your beautiful code here... #
            x, y = np.random.rand(num points), np.random.rand(num points)
            dists = np.add(np.square(x), np.square(y))
            in circle = np.less equal(dists, 1)
            return np.count nonzero(in circle) / num points * 4
```

To see the effectiveness of using NumPy, let's run both implementations of the simulation, with and without NumPy, and compare their speeds.

```
In [2]: num points = 10000000 # number of random points to choose
        start = time.perf counter()
In [3]:
        print("Estimate of Pi:", monte carlo pi(num points))
        print ("Actual value of Pi:", np.pi)
        end = time.perf counter()
        total1 = end - start
        Estimate of Pi: 3.141812
        Actual value of Pi: 3.141592653589793
In [4]:
        start = time.perf counter()
        print("Estimate of Pi:", monte_carlo_pi_numpy(num_points))
        print ("Actual value of Pi:", np.pi)
        end = time.perf counter()
        total2 = end - start
        Estimate of Pi: 3.141036
        Actual value of Pi: 3.141592653589793
In [5]: print("w/o NumPy:\t %f s\nw/ NumPy:\t %f s" %(total1, total2))
        print("Total Speedup: " + str(total1 / total2) + "x")
        w/o NumPy:
                         3.121263 s
        w/ NumPy:
                         0.167935 s
        Total Speedup: 18.586183257367896x
```

In [ ]: