

**Theorem 1.** *Let  $\mathcal{C}$  be an abelian category. Then  $K(\mathcal{C})$  (also  $K^+, K^-, K^b$ ) with standard translation functor and distinguished triangles is triangulated.*

**Remark 2.**  $C(U)$  fits as  $Z$  in TR1.

**Definition 3** (cohomological functor). *Assume  $\mathcal{C}$  is triangulated,  $\mathcal{A}$  is abelian. Let  $F : \mathcal{C} \rightarrow \mathcal{A}$  be an additive functor. We call it cohomological if for any distinguished triangle  $X \xrightarrow{u} Y \xrightarrow{v} Z \xrightarrow{w} T(X)$  we have an exact sequence*

$$\dots \rightarrow F(T^i(X)) \rightarrow F(T^i(Y)) \rightarrow F(T^i(Z)) \rightarrow F(T^{i+1}(X)) \rightarrow \dots$$

**Definition 4.** *Let  $\mathcal{C}$  be a triangulated category,  $S$  a localizing class of morphisms in  $\mathcal{C}$ . We say that  $S$  is compatible with triangulation if*

- $s \in S \iff T(s) \in S$ ,
- in TR3,  $f, g \in S \implies h \in S$  for any  $h$ .

**Theorem 5.** *Let  $\mathcal{C}$  and  $S$  be as above. On  $\mathcal{C}[S^{-1}]$  we can define*

- $T_S : \mathcal{C}[S^{-1}] \rightarrow \mathcal{C}[S^{-1}]$ ,  $T_S = T$  on objects and morphisms, i.e.  $T(X \xleftarrow{s} Z \xrightarrow{f} Y) = T(X) \xleftarrow{T(s)} T(Z) \xrightarrow{T(f)} T(Y)$ .
- $X \xrightarrow{u} Y \xrightarrow{v} Z \xrightarrow{w} T(X)$  is distinguished in  $\mathcal{C}[S^{-1}]$  if it is isomorphic to a distinguished triangle coming from  $\mathcal{C}$ .

*Then  $\mathcal{C}[S^{-1}]$  with the structure defined above is triangulated.*

**Corollary 6.** *Derived category of an abelian category inherits the triangulated structure from the homotopy category of complexes.*