

# Discrete Maths

3

set of symbols  $\rightarrow$  Alphabet (A)

word: an ordered set

phrase/sentence/para:

sequence of symbols

Language  $\bullet \bullet A^*$  (regular expression  
\* means one or more occurrences)

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Can you perform set operations?

YES

Here, a person speaking mixed languages  
can be understood by a person who  
knows them all

$\rightarrow$  While DB query, certain problem might  
be easily solved by set operations.

# Phrase Structure Grammar

① A set of terminals  $T$  (alphabet)

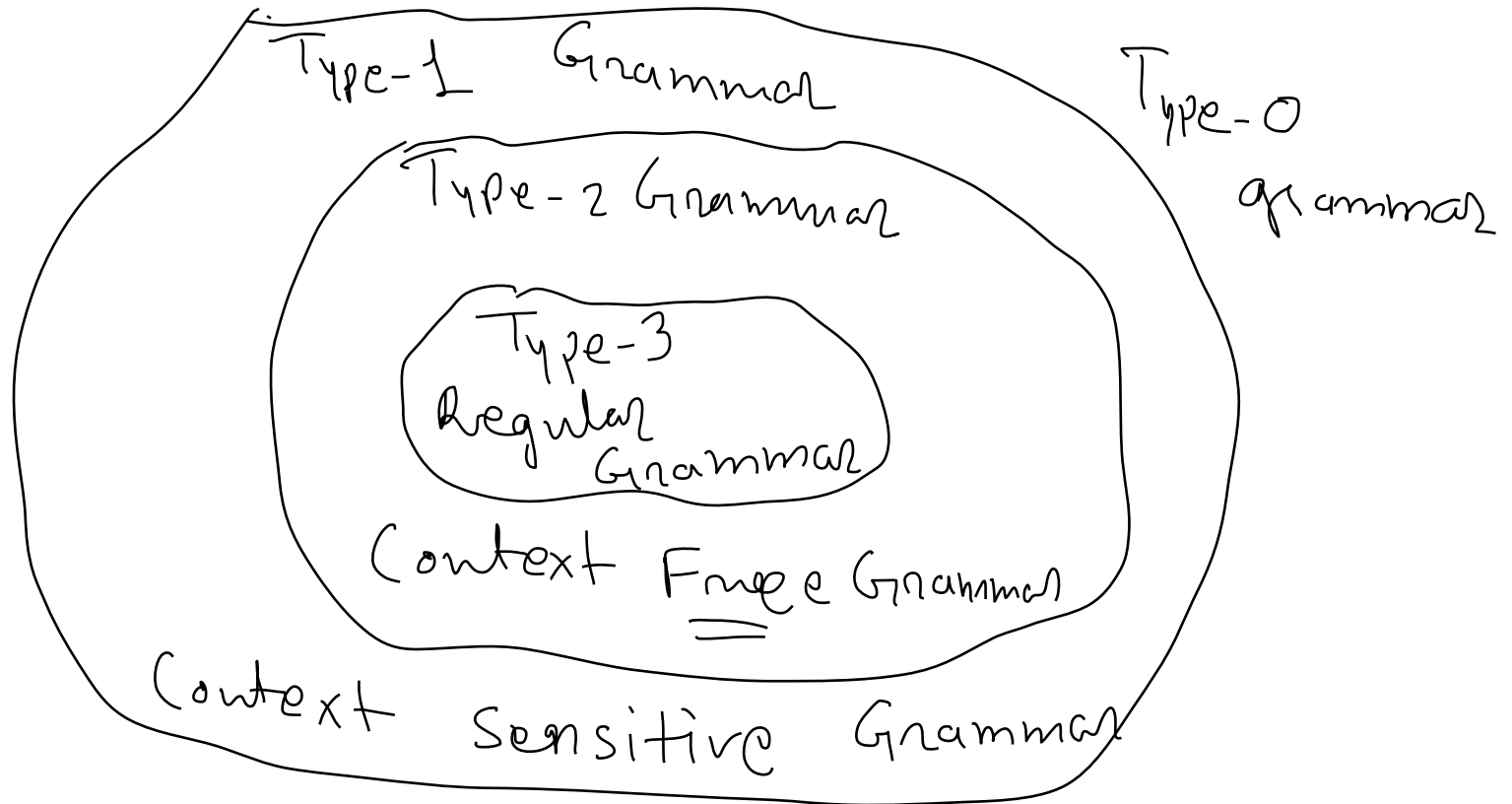
② A set of non-terminal  $N$

③ A set of productions  $P$

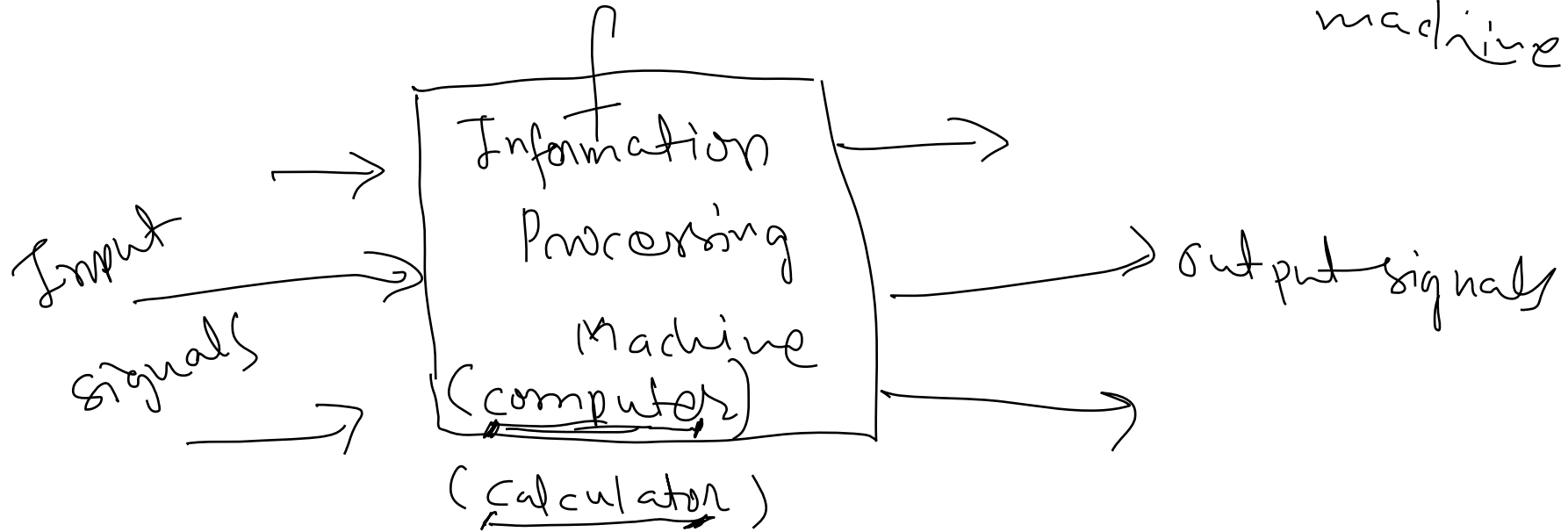
④ Among all the non-terminals in  $N$ , there is a special NT that is referred as the starting

It is Symbol  $S \in N$  (for starting)  
NOT a set. Element. mostly its gonna be single.

# Relationship among different types of Grammar



# Basic concepts of information processing machine



i.e. convert input  
from upper case to lower

Box  
diagram before  
programming.

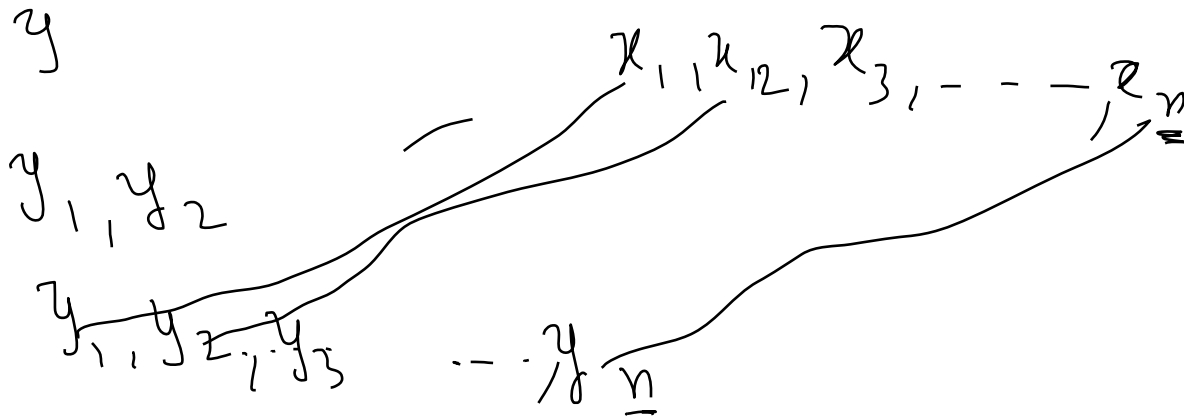
Case

Observe relation  
of input to output

$f$

$$y = f(x)$$

Think of  
one to one  
|  
Many to many.



# Application

## Vending Machine

Currency cent	1	(penny)
Nickel	5	
Dime	10	
Quarter	25	
Dollar	100	(1 bill)

? will it revert the  
extra change

? will it carry forward / credit extra  
change for next transaction?  
..... V1 or V2 or V3 . . .

# Finite State machine

## Abstract model

1. A finite set of states

$$S = \{s_0, s_1, s_2, \dots, s_n\}$$

2. A special element of set  $S$ , " $s_0$ " referred to as the initial state.

3. A finite set of input letters

$$\underline{I} = \{i_1, i_2, i_3, \dots\}$$



4. A finite set of output letters

$$O = \{o_1, o_2, \dots\}$$

5.

A function  $f$  from  $S \times I$  to  $S$  // same as  $P$  in grammar

referred to as transition function.

6.

A function  $g$  from  $S$  to  $O$ ,

referred to as the output function.

# Equivalent machines

How do you tell  
two or more machines  
exactly same?

i.e.

There might be solutions to  
2 or more same style problem.

- If there are extra states?  
Removing them will make it  
efficient.