

# Discrete Maths

5

Based on type of production (categories)

rules that is how does terminals and non-terminals are arranged

there are types of grammar observed by

Chomsky =

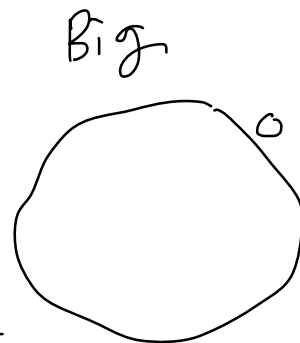
He actually is looking for "Universal Grammar"

hypothetically,

humans and alien can also communicate.

Rules :

~~##~~ (no restrictions) type-0



Type-1

i.e  $aA \rightarrow a$  X  
 $aAb \rightarrow aBcb$

$\alpha \rightarrow \beta$

length of  $\alpha \leq$  length of  $\beta$

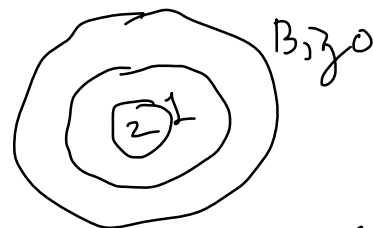
i.e  $A \rightarrow ab$   
 $A \rightarrow aA$   
 $aAb \rightarrow aBcb, 3 < 4$

$\alpha, \beta$  arbitrary

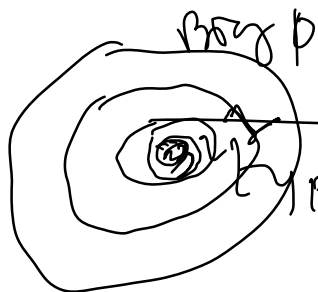
Type-2

$A \rightarrow \alpha$

left always NT single



terminally  
 strings of  
 and non-terminally



Type-3

$A \rightarrow a | aB$  } same  $a \in T$   
 $A \rightarrow a | Ba$  }  $B \in N$

A language is said to be a type-i

( $\{0,1,2\}$ ) language if it can be  
represented by a type-i grammar.  
(specified)



BUT  
Can NOT be specified by  
a type (i+1) grammar,

i.e.  $L = \{ a^i b^k \mid i \geq k \}$

$A \rightarrow aAb$

$A \rightarrow ab$

$A \rightarrow \alpha$

Type-2 language  $\left\{ \begin{array}{l} S \rightarrow aA \\ S \rightarrow Aa \end{array} \right.$

but not type-3 (regular)

bcz right hand more than 2 lengths

Phrase structure grammar <sup>is based on</sup> constituency relation. PSG

---

~~is~~ type-0 grammar.

"Flexible" / open

Type-0 language can be  
utilized / represents

Turing Machine

constituency  
vs  
Dependency  
relation

Turing machine

~ A computer that is capable  
of ~~running~~ program  
storage + processing

\_\_\_\_ Type-3 / Regular language  
is for FSA

Grammar:

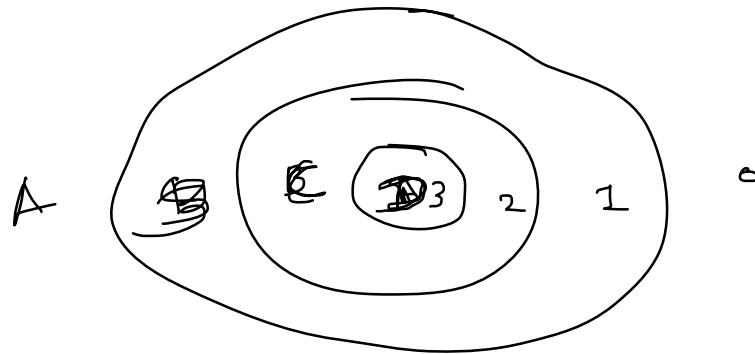
Specific rules that determine  
input strings are accepted  
(part of language) or  
rejected (not part of language)



All type-0 grammar  
are also  
type 1, 2, 3. ?

All type-3 grammar are also  
type 2, 1, 0 ?





A contains ~~data~~ B, ~~1~~, 0

B contains ~~data~~ ~~1~~, 0

C contains 0



All type-0 are 1, 2, 3

~~All~~ type-1 are 2, 3

All type-2 are 3

All type-3 are 2, 1, 0

All type-2 are 1, 0

All type-1 are 0

OR

~~type-0 grammar are~~  
~~used by Turing machine~~  
"General purpose"

type-1  
~~context sensitive grammar~~

It there is a production of the form  
 $\alpha \rightarrow \beta$   ~~$A \rightarrow$~~   $L \rightarrow R$  (~~different~~  $A \rightarrow$  ~~than~~)

Observe context sensitivity

A can be replaced by  $\alpha$  only

when it is having context exact  
that is it is surrounded by

the strings  $L$  and  $R$ , where  $L$  is left  
context,  $R$  is right side context.

~~Context free grammar (type-2)~~

are used in defining the

Syntax of almost all programming

languages. (context free grammar)

Regular grammars (type-3) can be

used to search text / pattern matching.

p.s. regular expressions

Example

30 cents vending machine

Total Deposits	New			merchandise delivered	
	5¢	10¢	25¢	↓ NOTHING	Total deposit of
0¢	0+5⇒5	0+10⇒10	0+25⇒25		0¢
5¢			30 or more	NOTHING	5¢
10¢			30 or more	NOTHING	10¢
15¢			30 or more	NOTHING	15¢
20¢		30 or more	35¢ or more	NOTHING	20¢
25¢	30¢ or more	30¢ or more	30¢ or more	NOTHING	25¢
30¢ or more	5¢	10¢	25¢	Bubble Gum	30¢ or more

state (a) New total deposit Input

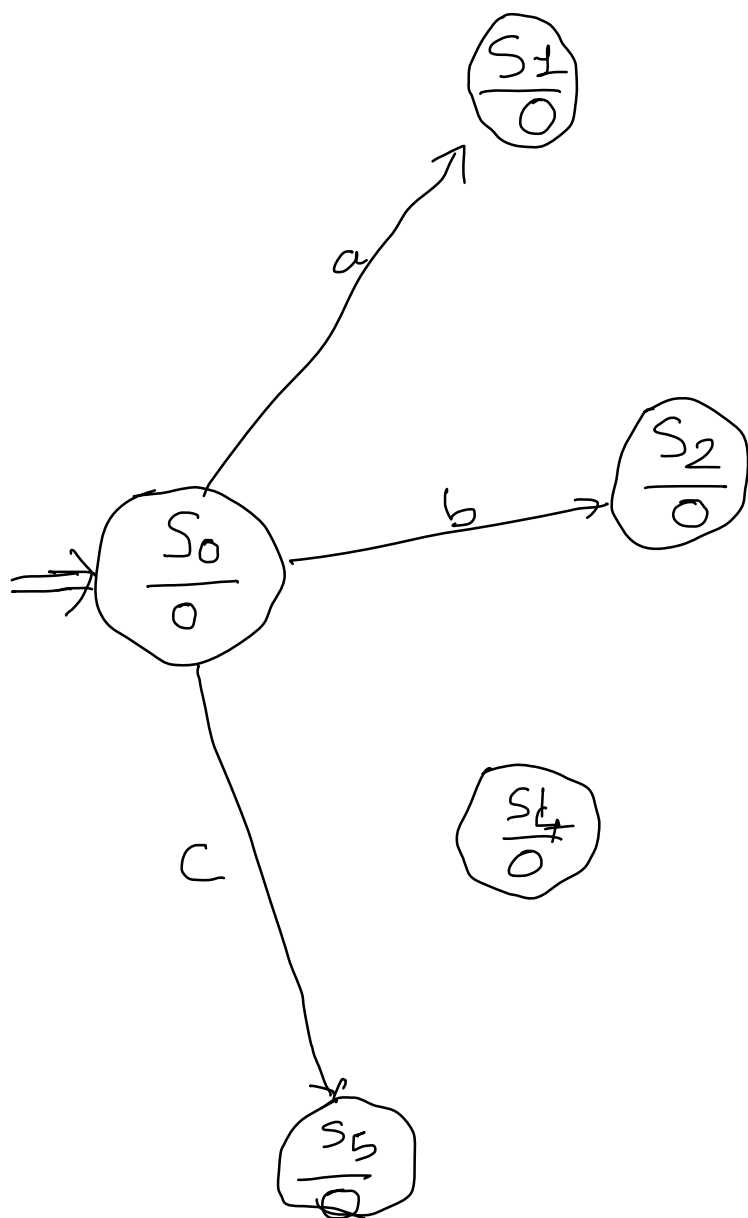
(b) output State

output is attached with state  
and not transition.

indicate start  $\Rightarrow$

State	Input			Output
	a	b	c	
$S_0$	$S_1$	$S_2$	$S_5$	0
$S_1$	$S_2$	$S_3$	$S_6$	0
$S_2$	$S_3$	$S_4$	$S_6$	0
$S_3$	$S_4$	$S_5$	$S_6$	0
$S_4$	$S_5$	$S_6$	$S_6$	0
$S_5$	$S_6$	$S_6$	$S_6$	0
$S_6$	$S_1$	$S_2$	$S_5$	1

If you reach to state 6, you receive bubble gum.



\ . . . .

# FSTN as models of physical systems

---

Example:

Design a modulo 3 counter

Input: sequence of 0's & 1's & 2's

Output: sequence of 0s, 1s and 2s

Such that at any instant

~~The output is~~

equal to the modulo 3,

sum of the digits in

the input sequence.

State A :

Situation that

modulo 3 sum of all input  
digits is  $\emptyset$

State B :

~~modulo 3 sum of all input~~  
digits is 1

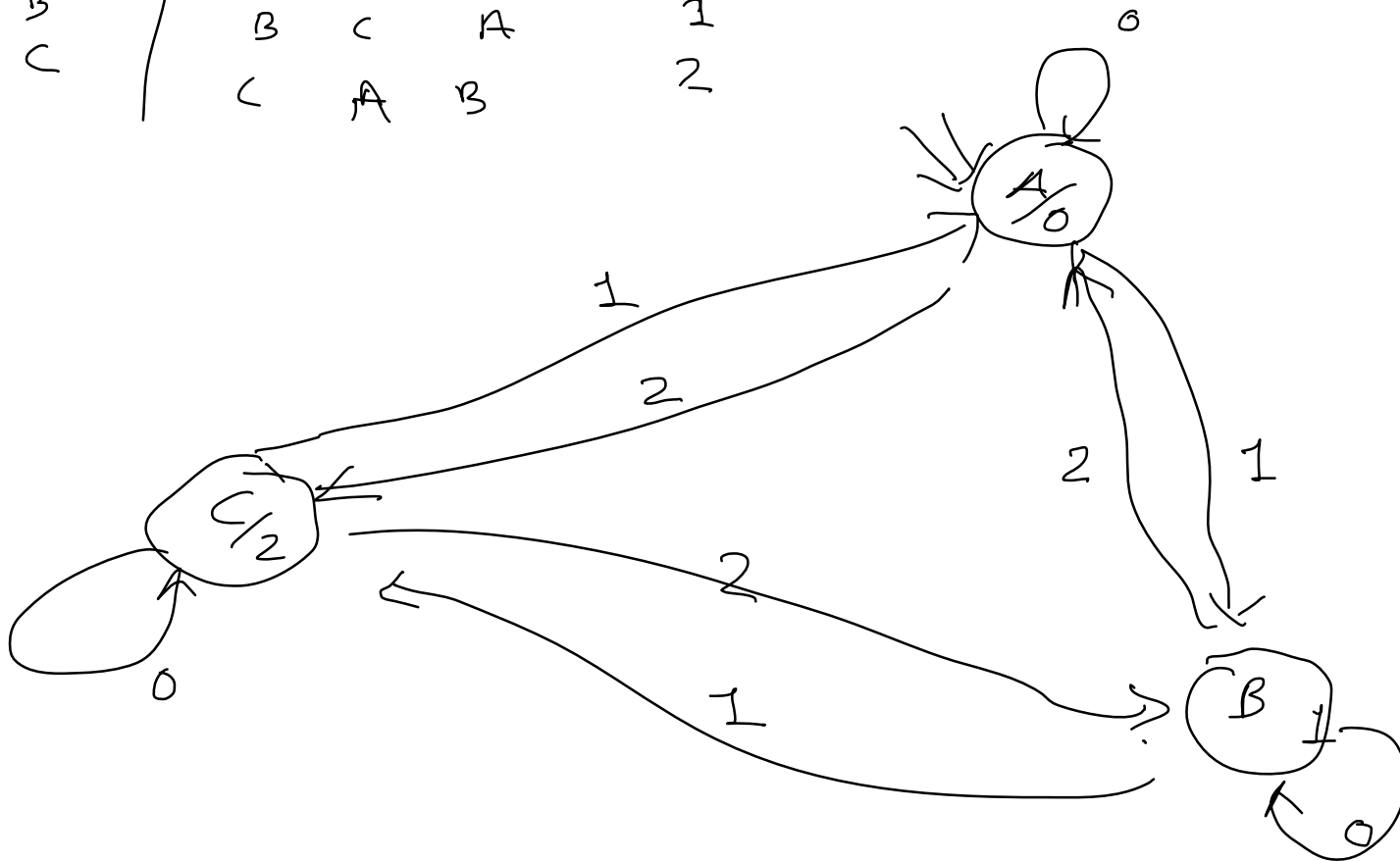
State C :

modulo 3 sum of all digits  
is 2



	Sum	output	
0	0	0	
0	0	0	
1	1	1	
1	2	2	
1	3	0	$\therefore 3 \% 3 \Rightarrow 0$
2	5	2	$\therefore 5 \% 3 \Rightarrow 2$
2	7	1	
0	7	1	$7 \% 3 \Rightarrow 1$
1	8	2	
2	10	1	
0	10	1	
0	10	1	
1	11	2	
1	12	0	

State	Input			Output
	0	1	2	
⇒ A	A	B	C	0
B	B	C	A	1
C	C	A	B	2



This can be used in real

i.e      A                  B                  C  
            0                  1                  2  
            Equal          Large          Small

Happy	Angry	<del>depressed</del>
Sing	Curse	Sleep

state	Input			output
	Homework	Party	Poor exam	
<del>A (Happy)</del>	A	A	B	SING
B (Angry)	C	A	B	CURSE
<del>C (depressed)</del>	C	A	C	SLEEP