

A **proof by induction** consists of **two** cases.

The **first**, the **base case** (or **basis**), proves the statement for  $n = 0$  without assuming any knowledge of other cases.

The **second** case, the **induction step**, proves that *if* the statement holds for any given case  $n = k$ , *then* it must also hold for the next case  $n = k + 1$ . These two steps establish that the statement holds for every natural number  $n$ .

The base case does **not necessarily** begin with  $n = 0$ , but often with  $n = 1$ , and possibly with any fixed natural number  $n = N$ , establishing the truth of the statement for all natural numbers  $n \geq N$ .