# Package 'cxr'

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Type Package
Title A Toolbox for Modelling Species Coexistence in R
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Description Recent developments in modern coexistence theory has advanced our understanding on how species are able to persist and co-occur with other species at varying abundances. However, applying this mathematical framework to empirical data is still challenging, precluding a larger adoption of the theoretical tools developed by empiricists. This package provides a complete toolbox for modelling competitive effects between species, calculate fitness and niche differences, and calculate coexistence regions.  The functions are flexible and can include covariates and different fitting algorithms can be used.
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### Description

A dataset containing abundances for each plant species, where each species was sampled at its developmental peak.

### Usage

data(abundance)

### **Format**

A data frame with 5832 rows and 7 variables

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#### **Details**

· year: year

• month: month of sampling

• day: day of sampling

• plot: plot

subplot: subplot code species: plant species

• individuals: number of individuals

#### Note

For details, see Lanuza et al. 2018 Ecology Letters.

AvgFitnessRatio

Average fitness differences between a pair of species

### **Description**

Calculates the product of (1) the demographic ratio, and (2) the competitive response ratio between two species according to their vital rates and competition coefficients. First species in the parameters is numerator (j in eq. 4 of Godoy et al. 2014). If germ.rate and survival.rate are provided, it calculates the ratio according to eq. 4 of Godoy et al. (2014), for annual plants. Otherwise, if only lambda is provided, it returns the general version of the demographic ratio, where nu = lambda

#### Usage

```
AvgFitnessRatio(lambda, germ.rate = NULL, survival.rate = NULL,
pair.matrix)
```

#### **Arguments**

lambda vector of length 2, per capita fecundity of the species in the absence of compe-

tition

germ. rate optional vector of length 2, germination rate of the two species

survival.rate optional vector of length 2, annual survival of ungerminated seed in the soil pair.matrix 2x2 matrix, competition coefficients between the two species and intraspecific

terms

#### Value

list with three numeric values, giving 1) the demographic ratio, 2) the competitive response ratio, and 3) the average fitness ratio between the two species

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competition

Competition measurements

### **Description**

A dataset containing fitness and neighbours for each plant individual

### Usage

```
data(competition)
```

#### **Format**

A data frame with 42948 rows and 11 variables

#### **Details**

- year: year
- month: month
- day: day
- plot: plot
- subplot: subplot code
- focal: focal plant species identity
- individual\_ID: unique identifier for each individual focal plant
- fruit: total fruits produced by the focal individual
- seed: total seeds produced by the focal individual
- competitor: competitor identity
- number: number of competitors

#### Note

For details, see Lanuza et al. 2018 Ecology Letters.

cxr cxr

### Description

Tools and functions for evaluating multi-species coexistence.

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cxr_er_bootstrap	standard error estimates for effect and response parameters
	j = ijj = i = i

#### **Description**

Computes bootstrap standard errors for a given effect/response function

### Usage

```
cxr_er_bootstrap(effect.response.model, optim.method, sp.data, init.par,
  lower.bounds, upper.bounds, covariates, optimize.lambda, lambda.vector,
  nsamples)
```

### **Arguments**

effect.response.model

effect/response function

optim.method optimization method to use. One of the following: "optim\_NM","optim\_L-

BFGS-B","nloptr\_CRS2\_LM", "nloptr\_ISRES","nloptr\_DIRECT\_L\_RAND","GenSA","hydroPSO","D

sp. data dataframe with all the necessary information in long format. It should have the

following columns: - site: character ID - focal: character ID of the focal species. Any number of focal species is allowed, but the number of focal species must match the number of initial parameters (one lambda, e, and r per species). - fitness: numeric, a fitness metric - competitor: character, ID of a competitor for that observation. The set of competitors must be, for now, the same as the set of focal species. - number: number of neighbouring/competitor individuals from the associated species. Observations without competitors of a given species

must be explicit, i.e. setting number to zero.

init.par 1d vector of initial parameters

lower.bounds 1d vector of lower bounds

upper.bounds 1d vector of upper bounds

covariates dataframe/matrix with observations in rows and covariates in columns. Each

cell is the value of a covariate from an observation.

optimize.lambda

boolean, whether to optimize the values of lambda or not.

lambda.vector in case lambda is not to be optimized, fixed values for it.

nsamples how many bootstrap samples to compute.

### Value

1d vector, the standard error of each parameter in init.par

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cxr\_init\_params

Join parameters in a 1d vector

#### **Description**

Generate a 1d vector from a series of parameters in a certain order. It also returns the same vector for lower and upper bounds. This function is intended to work with parameters for a single species (i.e. a single lambda value, etc). Note that lambda.cov and alpha.cov must be consistent with num.covariates.

### Usage

```
cxr_init_params(init.lambda = NULL, init.sigma = 0,
  init.alpha = NULL, init.lambda.cov = NULL, init.alpha.cov = NULL,
  lower.lambda = 1, upper.lambda = 1e+05, lower.sigma = 1e-05,
  upper.sigma = 1e+05, lower.alpha = 1e-05, upper.alpha = 1e+05,
  lower.lambda.cov = 1e-05, upper.lambda.cov = 1e+05,
  lower.alpha.cov = 1e-05, upper.alpha.cov = 1e+05, num.competitors,
  num.covariates)
```

### **Arguments**

```
init.lambda
                 numeric, lambda
init.sigma
                 numeric, sigma
init.alpha
                  1d vector, interaction coefficients over the species
init.lambda.cov
                  1d vector, initial values for lambda.cov
init.alpha.cov 1d vector, initial values for alpha.cov
lower.lambda
                 lower bound for lambda
upper.lambda
                 upper bound for lambda
lower.sigma
                 lower bound for sigma
upper.sigma
                 upper bound for sigma
lower.alpha
                 lower bound for alpha
upper.alpha
                 upper bound for alpha
lower.lambda.cov
                 lower bound for lambda.cov
upper.lambda.cov
                 upper bound for lambda.cov
lower.alpha.cov
                 lower bound for alpha.cov
upper.alpha.cov
                 upper bound for alpha.cov
num.competitors
                 number of competitors
num.covariates number of covariates
```

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### Value

list with three 1d vectors, ready for passing to the optim methods, consistent with the functions  $model\_BH1-5$ 

cxr\_pm\_bootstrap Standard error estimates for model parameters

### Description

Computes bootstrap standard errors for a given population dynamics model.

### Usage

```
cxr_pm_bootstrap(fitness.model, optim.method, param.list, fixed.terms,
  log.fitness, init.par, lower.bounds, upper.bounds, focal.comp.matrix,
  focal.covariates, nsamples)
```

#### **Arguments**

fitness.model	function returning a single value to minimize, given a set of parameters and a fitness metric		
optim.method	optimization method to use. One of the following: "optim_NM","optim_L-BFGS-B","nloptr_CRS2_LM", "nloptr_ISRES","nloptr_DIRECT_L_RAND","GenSA","hydroPSO","D		
param.list	string vector giving the parameters that are to be optimized for the fitness model.		
fixed.terms	string vector giving the parameters that are NOT optimized for the fitness model.		
log.fitness	1d vector, log of the fitness metric for every observation		
init.par	1d vector of initial parameters		
lower.bounds	1d vector of lower bounds		
upper.bounds	1d vector of upper bounds		
focal.comp.matr	rix		
	matrix with observations in rows and neighbours in columns. Each cell is the number of neighbours of a given species in a given observation.		
focal.covariates			
	optional matrix with observations in rows and covariates in columns. Each cell is the value of a covariate in a given observation.		
nsamples	how many bootstrap samples to compute.		

#### Value

1d vector, the standard error of each parameter in init.par

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cxr_retrieve_params Retrieve parameters from the vector returned by the optimization pro- cedures	cxr_retrieve_params	Retrieve parameters from the vector returned by the optimization procedures
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### **Description**

Retrieve parameters from the vector returned by the optimization procedures

#### Usage

```
cxr_retrieve_params(optim.params, param.list, alpha.length,
  alpha.cov.length, num.competitors, num.covariates)
```

### Arguments

optim.params 1d vector, the result of an optimization method

param.list character vector, which parameters are present. Possible elements are "lambda",
 "lambda.cov", "alpha", "alpha.cov".

alpha.length if alpha is to be retrieved, its length
 alpha.cov.length
 if alpha.cov is to be retrieved, its length

num.competitors
 how many competitor species

#### Value

num.covariates how many covariates

list with elements "lambda", "alpha", "lambda.cov", "alpha.cov", "sigma". If one of these elements is not present, returns NULL.

er_optim	Estimate competition effects and responses for a set of species

### **Description**

This function is similar in spirit to pm\_optim, in that it optimizes a set of parameters via maximum likelihood. See vignette 'Obtain competitive responses and effects' for an example of its use.

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### Usage

```
er_optim(lambda.vector, e.vector, r.vector, lambda.cov = NULL,
    e.cov = NULL, r.cov = NULL, sigma, lower.lambda = 0,
    upper.lambda = 1000, lower.e, upper.e, lower.r, upper.r,
    lower.lambda.cov = NULL, upper.lambda.cov = NULL,
    lower.e.cov = NULL, upper.e.cov = NULL, lower.r.cov = NULL,
    upper.r.cov = NULL, lower.sigma, upper.sigma, effect.response.model,
    optim.method, sp.data, covariates = NULL, optimize.lambda = FALSE,
    generate.errors = FALSE, bootstrap.samples = 0)
```

### Arguments

lambda.vector	1d vector of lambda estimates/initial values (depending on whether lambda values are optimized or not)
e.vector	1d vector of competitive effect initial values
r.vector	1d vector of competitive response initial values
lambda.cov	numeric matrix of num.sp x num.covariates, effect of every covariate on species' lambda. Discarded if covariates are not passed.
e.cov	numeric matrix of num.sp x num.covariates, effect of every covariate on species' competitive effect. Discarded if covariates are not passed.
r.cov	numeric matrix of num.sp x num.covariates, effect of every covariate on species' competitive response. Discarded if covariates are not passed.
sigma	initial value for variation estimate.
lower.lambda	lower bound for lambda, in case it is optimized. Either length 1 or same length as lambda.vector
upper.lambda	upper bound for lambda, in case it is optimized. Either length 1 or same length as lambda.vector
lower.e	lower bound for competitive effects. Either length 1 or same length as e.vector
upper.e	upper bound for competitive effects. Either length 1 or same length as e.vector
lower.r	lower bound for competitive responses. Either length 1 or same length as r.vector
upper.r	upper bound for competitive responses. Either length 1 or same length as r.vector
lower.lambda.c	
	lower bound for covariate effects on lambda. Either length 1 or same length as lambda.cov. Discarded if covariates are not passed.
upper.lambda.c	
	upper bound for covariate effects on lambda. Either length 1 or same length as lambda.cov. Discarded if covariates are not passed.
lower.e.cov	lower bound for covariate effects on e. Either length 1 or same length as e.cov. Discarded if covariates are not passed.
upper.e.cov	upper bound for covariate effects on e. Either length 1 or same length as e.cov. Discarded if covariates are not passed.
lower.r.cov	lower bound for covariate effects on r. Either length 1 or same length as r.cov. Discarded if covariates are not passed.

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upper.r.cov upper bound for covariate effects on r. Either length 1 or same length as r.cov.

Discarded if covariates are not passed.

lower.sigma lower bound for sigma. Length 1. upper.sigma upper bound for sigma. Length 1.

effect.response.model

function returning a value to optimize over, e.g. maximum likelihood

optim.method optimization method to use. One of the following: "optim\_NM","optim\_L-

BFGS-B","nloptr\_CRS2\_LM", "nloptr\_ISRES","nloptr\_DIRECT\_L\_RAND","GenSA","hydroPSO","D

sp. data dataframe with all the necessary information in long format. It should have the

following columns: - site: character ID - focal: character ID of the focal species. Any number of focal species is allowed, but the number of focal species must match the number of initial parameters (one lambda, e, and r per species). - fitness: numeric, a fitness metric - competitor: character, ID of a competitor for that observation. The set of competitors must be, for now, the same as the set of focal species. - number: number of neighbouring/competitor individuals from the associated species. Observations without competitors of a given species

must be explicit, i.e. setting number to zero.

covariates optional matrix/dataframe with as many rows as the sp.data dataframe, and co-

variates in columns.

optimize.lambda

boolean, whether we want to optimize lambda values or not.

generate.errors

boolean, whether to compute bootstrap errors for the fitted parameters. Note that, depending on the data and optimization method, this may be computationally expensive.

bootstrap.samples

how many bootstrap samples to compute.

### Value

list with estimated species values for e, r, lambda (optional), and if covariates are given, the effects of covariates on lambda, r, and e.

GenerateTestData

Generate simulated competition data

### **Description**

Generate simulated competition data

#### Usage

```
GenerateTestData(focal.sp = 1, num.sp = 2, num.cov = 2,
num.obs = 10, fitness.model = 1, focal.lambda, alpha,
alpha.cov = NULL, lambda.cov = NULL)
```

#### **Arguments**

focal.sp number of focal species

num. sp total number of species, including focal ones

num.cov number of covariates

num. obs number of observations/sites

fitness.model scalar representing the model to generate data from, from BH1 to BH5 in in-

creasing levels of complexity.

focal.lambda 1d vector with lambdas of the focal sp alpha interaction matrix, num.sp x num.sp

alpha.cov list of dimension num.cov. Each component of the list is a matrix of different di-

mensions depending on fitness.model. If fitness.model is 4, each component should be a single value, giving the effect of each covariate over every interaction; if fitness.model is 5, each component should be a matrix num.sp x num.sp, giving the effect of the covariate in question over each element of the interaction

matrix.

lambda.cov matrix of num.sp x num.cov giving the effect of each covariate over the fecun-

dity (lambda) of each species

#### Value

dataset with a fitness metric calculated for each focal species and observation, according to the fitness model selected

model\_abundBH1 Project abundance of individuals according to the Beverton-Holt fist model

#### **Description**

Project abundance of individuals according to the Beverton-Holt fist model

#### Usage

```
model_abundBH1(sp.par, init.abund, cov.values, alpha.matrix,
lambda.cov.matrix, alpha.cov.matrix, return.seeds = TRUE)
```

#### **Arguments**

sp.par dataframe with species in rows, and the following columns: lambda: fecundity

term germ.rate: seed germination rate survival.rate: annual survival of ungermi-

nated seed

init.abund number of individuals at time t cov.values Not used in BH\_abundances\_1

alpha.matrix Not used in BH\_1

#### Value

1d vector with number of individuals of each species at time t+1

model_abundBH2	Project abundance of individuals according to the Beverton-Holt second model

### **Description**

Project abundance of individuals according to the Beverton-Holt second model

### Usage

```
model_abundBH2(sp.par, init.abund, cov.values, alpha.matrix,
  lambda.cov.matrix, alpha.cov.matrix, return.seeds = TRUE)
```

### **Arguments**

sp.par	dataframe with species in rows, and the following columns: lambda: fecundity term germ.rate: seed germination rate survival.rate: annual survival of ungerminated seed				
init.abund	number of individuals at time t				
cov.values	Not used in model_abundBH2				
alpha.matrix	competition value, same for all interactions				
lambda.cov.matı	rix				
	Not used in model_abundBH2				
alpha.cov.matrix					
	Not used in model_abundBH2				
return.seeds	boolean flag, whether the prediction should return number of seeds (i.e. $N_{i,t+1}$ , eq. 1 of Lanuza et al. 2018), or number of adult individuals, (i.e. $N_{i,t+1} * g$ )				

#### Value

1d vector with number of individuals of each species at time t+1

Project abundance of individuals according to the Beverton-Holt third model
·

### **Description**

Project abundance of individuals according to the Beverton-Holt third model

#### Usage

```
model_abundBH3(sp.par, init.abund, cov.values, alpha.matrix,
lambda.cov.matrix, alpha.cov.matrix, return.seeds = TRUE)
```

#### **Arguments**

sp.par dataframe with species in rows, and the following columns: lambda: fecundity

term germ.rate: seed germination rate survival.rate: annual survival of ungermi-

nated seed

init.abund number of individuals at time t cov.values Not used in model abundBH3

alpha.matrix competition matrix

lambda.cov.matrix

Not used in model\_abundBH3

alpha.cov.matrix

Not used in model abundBH3

return. seeds boolean flag, whether the prediction should return number of seeds (i.e.  $N_{i,t+1}$ ,

eq. 1 of Lanuza et al. 2018), or number of adult individuals, (i.e.  $N_{i,t+1} * g$ )

#### Value

1d vector with number of individuals of each species at time t+1

model_abundBH4	Project fourth r	of	individuals	according	to	the	Beverton-Holt	

#### **Description**

Project abundance of individuals according to the Beverton-Holt fourth model

#### Usage

```
model_abundBH4(sp.par, init.abund, cov.values, alpha.matrix,
lambda.cov.matrix, alpha.cov.matrix, return.seeds = TRUE)
```

#### **Arguments**

sp.par dataframe with species in rows, and the following columns: lambda: fecundity

term germ.rate: seed germination rate survival.rate: annual survival of ungermi-

nated seed

init.abund number of individuals at time t

cov. values 1d vector with values of each covariate

alpha.matrix competition matrix

lambda.cov.matrix

matrix of num.sp x num.cov giving the effect of each covariate over the fecun-

dity (lambda) of each species

alpha.cov.matrix

list of dimension number of covariates. Each component of the list is a single

value, giving the effect of the covariate in question over the interaction matrix.

return. seeds boolean flag, whether the prediction should return number of seeds (i.e.  $N_{i,t+1}$ ,

eq. 1 of Lanuza et al. 2018), or number of adult individuals, (i.e.  $N_{i,t+1} * g$ )

#### Value

1d vector with number of individuals of each species at time t+1

model_abundBH5	Project abundance of individuals according to the Beverton-Holt fifth
	model

#### **Description**

Project abundance of individuals according to the Beverton-Holt fifth model

### Usage

```
model_abundBH5(sp.par, init.abund, cov.values, alpha.matrix,
lambda.cov.matrix, alpha.cov.matrix, return.seeds = TRUE)
```

#### **Arguments**

sp.par dataframe with species in rows, and the following columns: lambda: fecundity

term germ.rate: seed germination rate survival.rate: annual survival of ungermi-

nated seed

init.abund number of individuals at time t

cov.values 1d vector with values of each covariate

alpha.matrix competition matrix

lambda.cov.matrix

matrix of num.sp x num.cov giving the effect of each covariate over the fecun-

dity (lambda) of each species

```
alpha.cov.matrix
```

list of dimension number of covariates. Each component of the list is a matrix of num.sp x num.sp, giving the effect of the covariate in question over the interaction matrix.

return.seeds

boolean flag, whether the prediction should return number of seeds (i.e.  $N_{i,t+1}$ , eq. 1 of Lanuza et al. 2018), or number of adult individuals, (i.e.  $N_{i,t+1} * g$ )

#### Value

1d vector with number of individuals of each species at time t+1

model\_BH1

Title Beverton-Holt fecundity, first model

### Description

These functions return the negative log-likelihood of the data given the model and parameters. model\_BH1 is  $F_i=\lambda_i$ 

#### Usage

```
model_BH1(par, param.list = NULL, log.fitness,
  focal.comp.matrix = NULL, num.covariates = NULL,
  num.competitors = NULL, focal.covariates = NULL,
  fixed.terms = NULL)
```

#### Arguments

```
param.list not used in model_BH1
log.fitness log of fitness value
focal.comp.matrix
not used in model_BH1
num.covariates not used in model_BH1
num.competitors
not used in model_BH1
focal.covariates
not used in model_BH1
fixed.terms not used in model_BH1
```

#### Value

model\_BH2

Title Beverton-Holt fecundity, second model

#### **Description**

These functions return the negative log-likelihood of the data given the model and parameters. model\_BH2 is  $F_i = \frac{\lambda_i}{1+\alpha\sum_i N_j}$ 

### Usage

```
model_BH2(par, param.list = c("lambda", "alpha"), log.fitness,
  focal.comp.matrix, num.covariates = NULL, num.competitors = NULL,
  focal.covariates = NULL, fixed.terms = NULL)
```

#### **Arguments**

par

vector of variable length, with the following order: first, lambda of focal sp; second alpha, single interaction coefficient; last, sigma value. If any element is not to be optimized, it must not be present in this vector, but rather in the "fixed.terms" list

param.list

string listing parameters to optimize. Possible elements are lambda, lambda.cov, alpha, alpha.cov.

log.fitness

log of fitness value

focal.comp.matrix

dataframe with as many rows as observations, and one column for each competitor sp. Values of the dataframe are number of competitors of each sp per observation.

num.covariates not used in model\_BH2

num.competitors

not used in model\_BH2

focal.covariates

not used in model\_BH2.

fixed.terms

list with elements lambda, lambda.cov, alpha, alpha.cov. It contains parameters not to be optimized. Each element of the list must be of its appropriate length. Note that adding an element in "param.list" will force the function to look for it in par, and will not consider it here. In this model, lambda.cov and alpha.cov are not considered.

#### Value

model\_BH3

Title Beverton-Holt fecundity, third model

#### **Description**

These functions return the negative log-likelihood of the data given the model and parameters. model\_BH3 is  $F_i = \frac{\lambda_i}{1+\sum_j \alpha_{ij} N_j}$ 

#### Usage

```
model_BH3(par, param.list = c("lambda", "alpha"), log.fitness,
  focal.comp.matrix, num.covariates = NULL, num.competitors = NULL,
  focal.covariates = NULL, fixed.terms = NULL)
```

#### Arguments

par

vector of variable length, with the following order: first, lambda of focal sp; second alpha, interaction coefficients with every species; last, sigma value. If any element is not to be optimized, it must not be present in this vector, but rather in the fixed.terms list

param.list

string listing parameters to optimize. Possible elements are lambda, lambda.cov, alpha, alpha.cov.

log.fitness

log of fitness value

focal.comp.matrix

dataframe with as many rows as observations, and one column for each competitor sp. Values of the dataframe are number of competitors of each sp per observation.

num.covariates not used in model\_BH3

num.competitors

number of competitor species

focal.covariates

not used in model\_BH3.

fixed.terms

list with elements lambda, lambda.cov, alpha, alpha.cov. It contains parameters not to be optimized. Each element of the list must be of its appropriate length. Note that adding an element in "param.list" will force the function to look for it in par, and will not consider it here. In this model, lambda.cov and alpha.cov are not considered.

#### Value

model\_BH4

Title Beverton-Holt fecundity, fourth model

#### **Description**

These functions return the negative log-likelihood of the data given the model and parameters. model\_BH4 is  $F_i = \frac{\lambda_i + \sum_k b_k \Theta_{i,k}}{1 + \sum_j (\alpha_{ij} + \sum_k b_k \phi_k) N_j}$ 

#### Usage

model\_BH4(par, param.list, log.fitness, focal.comp.matrix, num.covariates,
num.competitors, focal.covariates, fixed.terms)

### **Arguments**

par

vector of variable length, with the following order: first, lambda of focal sp; second lambda.cov, effects of every covariate on lambda; third alpha, interaction coefficients with every species; fourth alpha.cov, effects of every covariate on alpha values (single effect for each covariate); last, sigma value. If any element is not to be optimized, it must not be present in this vector, but rather in the fixed.terms list

param.list

string listing parameters to optimize. Possible elements are lambda, lambda.cov, alpha, alpha.cov.

log.fitness

log of fitness value

focal.comp.matrix

dataframe with as many rows as observations, and one column for each competitor sp. Values of the dataframe are number of competitors of each sp per observation.

num.covariates number of covariates

 $\verb"num.competitors"$ 

number of competitor species

focal.covariates

dataframe/matrix with as many rows as observationes, and one column for each covariate. Values of the dataframe are covariate values for every observation.

fixed.terms

list with elements lambda, lambda.cov, alpha, alpha.cov. It contains parameters not to be optimized. Each element of the list must be of its appropriate length. Note that adding an element in "param.list" will force the function to look for it in par, and will not consider it here. In this model, lambda.cov and alpha.cov are not considered.

#### Value

model\_BH5

Title Beverton-Holt fecundity, fifth model

#### **Description**

These functions return the negative log-likelihood of the data given the model and parameters. model\_BH5 is  $F_i = \frac{\lambda_i + \sum_k b_k \Theta_{i,k}}{1 + \sum_j (\alpha_{ij} + \sum_k b_k \phi_{i,j,k}) N_j}$ 

#### Usage

model\_BH5(par, param.list, log.fitness, focal.comp.matrix, num.covariates,
num.competitors, focal.covariates, fixed.terms)

### **Arguments**

par vector of variable length, with the following order: first, lambda of focal sp;

second lambda.cov, effects of every covariate on lambda; third alpha, interaction coefficients with every species; fourth alpha.cov, effects of every covariate on alpha values (varying effect of every covariate over every interaction coefficient); last, sigma value. If any element is not to be optimized, it must not be

present in this vector, but rather in the fixed. terms list

param.list string listing parameters to optimize. Possible elements are lambda, lambda.cov,

alpha, alpha.cov.

log.fitness log of fitness value

focal.comp.matrix

dataframe with as many rows as observations, and one column for each competitor sp. Values of the dataframe are number of competitors of each sp per observation.

num.covariates number of covariates

num.competitors

number of competitor species

focal.covariates

dataframe with as many rows as observationes, and one column for each covariate. Values of the dataframe are covariate values for every observation.

fixed.terms

list with elements lambda, lambda.cov, alpha, alpha.cov. It contains parameters not to be optimized. Each element of the list must be of its appropriate length. Note that adding an element in "param.list" will force the function to look for it in par, and will not consider it here. In this model, lambda.cov and alpha.cov are not considered.

#### Value

20 model\_ER\_lambda

model_ER	Estimation of competitive effects and responses

#### **Description**

Calculates the log-likelihood of a Beverton-Holt model parameterized with given values with respect to a fitness metric. The function for calculating fecundity given effect and response values is taken from Godoy et al. (2014). Note that, as e and r are not pair-specific, all species parameters are fit in the same function. In this version, lambda values are fixed.

#### Usage

```
model_ER(init.par, lambda, target_all, density_all, log.fitness,
  covariates = NULL)
```

### Arguments

init.par	1d vector of initial parameters: r values, e values, and single sigma term. If covariates are given, this vector must include also lambda.cov, response.cov, and effect.cov terms, after the e values and before the sigma term.
lambda	1d vector of lambda values
target_all	matrix giving which species is calculated with which values. See er_optim
density_all	matrix giving the densities of each species at each observation. See er_optim
log.fitness	log of the fitness metric
covariates	if present, it is a dataframe/matrix with as many rows as observationes, and one column for each covariate. Values are covariate values for every observation.

#### Value

single numeric value giving the sum of negative log-likelihoods

model_ER_lambda	Estimation of competitive effects and responses
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### **Description**

Calculates the log-likelihood of a Beverton-Holt model parameterized with given values with respect to a fitness metric. The function for calculating fecundity given effect and response values is taken from Godoy et al. (2014). Note that, as e is not pair-specific, all species parameters are fit in the same function. In this version, lambda values are also fit.

#### Usage

```
model_ER_lambda(init.par, target_all, density_all, log.fitness,
  covariates = NULL)
```

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#### **Arguments**

init.par	1d vector of initial parameters: lambda values, r values, e values, and single sigma term. If covariates are given, this vector must include also lambda.cov, response.cov, and effect.cov terms, after the e values and before the sigma term.
target_all	matrix giving which species is calculated with which values. See er_optim
density_all	matrix giving the densities of each species at each observation. See er_optim
log.fitness	log of the fitness metric
covariates	if present, it is a dataframe/matrix with as many rows as observationes, and one column for each covariate. Values are covariate values for every observation.

#### Value

single numeric value giving the sum of negative log-likelihoods

NicheOverlap Niche overlap between two species
--

### **Description**

quoting Godoy et al. (2014): reflects the average degree to which species limit individuals of their own species relative to competitors. Low niche overlap causes species to have greater per capita growth rates when rare than when common. If species limit individuals of their own species and their competitors equally, then niche overlap is 1, and coexistence is not possible unless species are otherwise identical. At the other extreme, if species have no interspecific effects, then niche overlap is 0.

### Usage

```
NicheOverlap(pair.matrix)
```

### **Arguments**

pair.matrix 2x2 matrix with competition coefficients between the two species, and intraspecific terms

### Value

niche overlap value, in the range 0-1.

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param\_estimates

Population model parameters

### Description

A dataset containing estimated parameters for the competition dataset The dataset is generated by code similar to that of the vignette Multi-species parameter optimization. It is structured as a nested list with three levels, of the form: param\_estimates[[species]][[fecundity model]][[optimization method]] In the provided dataset, we include models 1 to 5, estimated with optimization method "optim\_L-BFGS-B" For each combination of species, model, and method, all model parameters are given. If a parameter is not estimated (e.g. upper/lower errors), the value stored is NA.

#### Usage

data(param\_estimates)

#### **Format**

A nested list with three levels

#### **Details**

- · lambda: per germinant fecundity
- lambda.lower.error:
- lambda.upper.error:
- sigma:
- alpha: effect of every competitor species on the focal species
- alpha.lower.error:
- · alpha.upper.error:
- lambda.cov: effect of every covariate on lambda
- lambda.cov.lower.error:
- lambda.cov.upper.error:
- alpha.cov: effect of every covariate on alpha
- alpha.cov.lower.error:
- alpha.cov.upper.error:
- log.likelihood: log-likelihood of the fitted parameters and model

### Note

For details, see vignette Multi-species parameter optimization

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pm\_optim

General optimization for population models

### **Description**

Wrapper for optimization procedures. It accepts a population dynamics model, defined as a function, and a series of parameters. It returns the optimal value for the parameters given a fitness metric and an optimization method. Optionally, bootstrap confidence intervals can also be computed.

### Usage

```
pm_optim(fitness.model, optim.method, param.list, log.fitness,
  init.lambda = NULL, lower.lambda = 1, upper.lambda = 1e+05,
  init.sigma = NULL, lower.sigma = 1e-10, upper.sigma = 1e+05,
  init.alpha = 1e-04, lower.alpha = 0, upper.alpha = 1e+05,
  init.lambda.cov = 0.001, lower.lambda.cov = 1e-04,
  upper.lambda.cov = 1e+05, init.alpha.cov = 0.001,
  lower.alpha.cov = 1e-04, upper.alpha.cov = 1e+05, focal.comp.matrix,
  focal.covariates = NULL, generate.errors = FALSE,
  bootstrap.samples = 0, verbose = FALSE)
```

#### **Arguments**

init.lambda.cov

fitness.model	function giving the population dynamics model. Any functional form is allowed, but the model must be constrained to free parameters lambda (fecundity of each
	sp in absence of competition), alpha (interaction coefficients), lambda.cov (effect of covariates on lambda), alpha.cov (effect of covariates on alpha)
optim.method	optimization method to use. One of the following: "optim_NM","optim_L-BFGS-B","nloptr_CRS2_LM", "nloptr_ISRES","nloptr_DIRECT_L_RAND","GenSA","hydroPSO","D
param.list	string vector giving the parameters that are to be optimized for the fitness model (to choose among "lambda", "alpha", "lambda.cov", and "alpha.cov").
log.fitness	1d vector, log of the fitness metric for every observation
init.lambda	1d vector, initial value of lambda
lower.lambda	lower bound for lambda
upper.lambda	upper bound for lambda
init.sigma	initial value for sigma (standard deviation)
lower.sigma	lower bound for sigma
upper.sigma	upper bound for sigma
init.alpha	initial value for the alpha vector/matrix
lower.alpha	lower bound for alpha
upper.alpha	upper bound for alpha

initial value for the lambda.cov matrix. Discarded if no covariates are given.

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lower.lambda.cov

lower bound for lambda.cov

upper.lambda.cov

upper bound for lambda.cov

init.alpha.cov initial value for the alpha.cov matrix. Discarded if no covariates are given.

lower.alpha.cov

lower bound for alpha.cov

upper.alpha.cov

upper bound for alpha.cov

focal.comp.matrix

matrix with observations in rows and neighbours in columns. Each cell is the number of neighbours of a given species in a given observation.

focal.covariates

optional matrix with observations in rows and covariates in columns. Each cell is the value of a covariate in a given observation.

generate.errors

boolean, whether to compute bootstrap errors for the fitted parameters. Note that, depending on the data, model, and optimization method, this may be computationally expensive.

bootstrap.samples

how many bootstrap samples to compute.

verbose

work in progress

### Value

list with the fitted parameters, and the loglikelihood of the fit. If a parameter is taken as a constant, the list will return the original value given.

pollinators

Pollinators measurments

#### **Description**

A dataset containing the overall pollinator visitation over the season for each plant species.

### Usage

data(pollinators)

#### **Format**

A data frame with x rows and 9 variables

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#### **Details**

• plot: plot number

• subplot: subplot code

• plant\_species: plant species

· year: year of measurement

· bees: total bee visits recieved

· flies: total flies visits recieved

· beetles: total beetles visits recieved

• butterflies: total butterflies visits recieved

· other: total other visits recieved

#### Note

For details, see Lanuza et al. 2018 Ecology Letters.

PredictAbundances

Project abundances according to specified models and parameters

#### Description

Project abundances according to specified models and parameters

#### **Usage**

PredictAbundances(par, timesteps, abundance.model, return.seeds = TRUE)

#### Arguments

par

list with the following components:

- dataframe sp.par, with the parameters to be passed to the predictive model
- dataframe initial.values, with fields "site", "species", "abundance"
- covariates, either 0 if there are no covariates, or a dataframe with fields "site", "timestep", "covariate", "value"
- list other.par, other parameters to abundance model, such as alpha.matrix, lambda.cov.matrix, alpha.cov.matrix.

Note that the fields "species", "site", and "covariate" should be unique identifiers, character or numeric.

timesteps

number of timesteps to project

abundance.model

a function that accepts parameters from sp.par, a set of initial abundances, and optionally other parameters. The function returns the projected abundances at t+1

return.seeds

boolean flag, whether the prediction should return number of seeds (i.e.  $N_{i,t+1}$ , eq. 1 of Lanuza et al. 2018), or number of adult individuals, (i.e.  $N_{i,t+1} * g$ )

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#### Value

dataframe with fields "timestep", "site", "sp", "abundance", giving the expected abundance for each species, timestep, and site.

salinity

Salinity measurements

### **Description**

A dataset containing the integrated salinity over the season for each plant species.

### Usage

```
data(salinity)
```

#### **Format**

A data frame with 324 rows and 5 variables

#### **Details**

- plot: plot number
- subplot: subplot code
- · year: year of measurement
- precip: anual precipitation
- sum\_salinity: summatory of the salinity values integrated through the species lifespan.

### Note

For details, see Lanuza et al. 2018 Ecology Letters.

SpeciesFitness

Fitness of a species

### Description

Calculates the fitness of a species following eq. S2 of Godoy et al. (2014). If germ.rate and survival.rate are provided, it calculates nu according to eq. 4 of Godoy et al. (2014), for annual plants. Otherwise, if only lambda is provided, nu = lambda

#### Usage

```
SpeciesFitness(lambda, germ.rate = NULL, survival.rate = NULL,
  competitive.response)
```

species\_rates 27

### **Arguments**

lambda per capita fecundity of the species in the absence of competition

germ.rate optional, germination rate of the species

survival.rate optional, annual survival of ungerminated seed in the soil

competitive.response

parameter reflecting the species' sensitivity to competition

### Value

single numeric value, species fitness

species\_rates

Species germination and survival rates

#### **Description**

A dataset containing germination and survival rates for each plant species. It also includes a column with the scientific names, and their associated codes.

### Usage

```
data(species_rates)
```

### **Format**

A data frame with 20 rows and 4 variables

#### **Details**

• species: binomial name

• code: four-letter code used in other datasets

• germination: germination rate

• seed.survival: annual survival of ungerminated seed in the soil

#### Note

For details, see Lanuza et al. 2018 Ecology Letters.

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