

## Revised Effective Ionic Radii and Systematic Studies of Interatomic Distances in Halides and Chalcogenides

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The effective ionic radii of Shannon & Prewitt [*Acta Cryst.* (1969), B25, 925–945] are revised to include more unusual oxidation states and coordinations. Revisions are based on new structural data, empirical bond strength–bond length relationships, and plots of (1) radii *vs* volume, (2) radii *vs* coordination number, and (3) radii *vs* oxidation state. Factors which affect radii additivity are polyhedral distortion, partial occupancy of cation sites, covalence, and metallic character. Mean Nb<sup>5+</sup>–O and Mo<sup>6+</sup>–O octahedral distances are linearly dependent on distortion. A decrease in cation occupancy increases mean Li<sup>+</sup>–O, Na<sup>+</sup>–O, and Ag<sup>+</sup>–O distances in a predictable manner. Covalence strongly shortens Fe<sup>2+</sup>–X, Co<sup>2+</sup>–X, Ni<sup>2+</sup>–X, Mn<sup>2+</sup>–X, Cu<sup>+</sup>–X, Ag<sup>+</sup>–X, and M–H<sup>–</sup> bonds as the electronegativity of X or M decreases. Smaller effects are seen for Zn<sup>2+</sup>–X, Cd<sup>2+</sup>–X, In<sup>3+</sup>–X, Pb<sup>2+</sup>–X, and Tl<sup>+</sup>–X. Bonds with delocalized electrons and therefore metallic character, *e.g.* Sm–S, V–S, and Re–O, are significantly shorter than similar bonds with localized electrons.

### Introduction

A thorough and systematic knowledge of the relative sizes of ions in halides and chalcogenides is rapidly being developed by crystal chemists as a result of (1) extensive synthesis within certain structure types, *e.g.* rocksalt, spinel, perovskite and pyrochlore; (2) preparation of new compounds with unusual oxidation states and coordination numbers; and (3) the abundance of accurate crystal structure refinements of halides, chalcogenides, and molecular inorganic compounds. A set of effective ionic radii which showed a number of systematic trends with valence, electronic spin state, and coordination was recently developed (Shannon & Prewitt, 1969, hereafter referred to as SP 69). This work has since been supplemented and improved by studies of certain groups of ions: rare earth and actinide ions (Peterson & Cunningham, 1967, 1968); tetrahedral oxyanions (Kálmán, 1971); tetravalent ions in perovskites (Fukunaga & Fujita, 1973); rare earth ions (Greis & Petzel, 1974); and tetravalent cations (Knop & Carlow, 1974).

Further, the relative sizes of certain ions or ion pairs were studied by Khan & Baur (1972): NH<sub>4</sub><sup>+</sup>; Ribbe & Gibbs (1971): OH<sup>–</sup>; Wolfe & Newnham (1969): Bi<sup>3+</sup>–La<sup>3+</sup>; McCarthy (1971): Eu<sup>2+</sup>–Sr<sup>2+</sup>; Silva, McDowell, Keller & Tarrant (1974): No<sup>2+</sup>. These authors' results have been incorporated here into a comprehensive modification of the Shannon–Prewitt radii.

In this paper the revised list of effective ionic radii, along with the relations between radii, coordination number, and valence is presented. The factors responsible for the deviation of radii sums from additivity such as polyhedral distortion, partial occupancy of cation sites, covalence, and metallic behavior (electron delocalization) will be discussed.

### Procedure

The same basic methods used in SP 69 were employed in preparing the revised list of effective ionic radii (Table 1). Some of the same assumptions were made:

(1) Additivity of both cation and anion radii to reproduce interatomic distances is valid if one considers coordination number (CN), electronic spin, covalency, repulsive forces, and polyhedral distortion.\*

(2) With these limitations, radii are independent of structure type.

(3) Both cation and anion radii vary with coordination number.

(4) With a constant anion, unit-cell volumes of isostructural series are proportional (but not necessarily linearly) to the cation volumes.

Other assumptions made in SP 69 have been modified:

(1) The effects of covalency on the shortening of M–F and M–O bonds are *not* comparable.

(2) Average interatomic distances in similar polyhedra in one structure are *not* constant but vary in a predictable way with the degree of polyhedral distortion (and anion CN). Both of these modified assumptions will be discussed in detail later.

The anion radii used in SP 69 were subtracted from available average distances. Approximately 900 distances from oxide and fluoride structures were used, and Table 2 lists their references according to CN and spin. These references generally cover from 1969 to 1975. The cation radii were derived to a first approximation from these distances, and then adjusted to be consistent with both the experimental interatomic distances and radii–unit cell volume (*r*<sup>3</sup> *vs* *V*) plots, as in

\* Polyhedral distortion was not considered in SP 69.

SP 69. Although such  $r^3$  vs  $V$  plots are not always linear (Shannon, 1975), their regular curvilinear nature still allows prediction of radii. This system is particularly accurate for radii in the middle of a series, and least reliable for large polarizable cations like  $\text{Cs}^+$ ,  $\text{Ba}^{2+}$ , and  $\text{Tl}^{3+}$ . Radii-volume plots were used by Knop & Carlow (1974) and Fukunaga & Fujita (1973) to derive radii of tetravalent cations. These radii were used along with experimental interatomic distances in deriving the final radii. Greis & Petzel (1974) derived rare earth radii in eight- and nine-coordination using accurate cell dimensions for rare earth trifluorides and distances calculated using the structural parameters of  $\text{YF}_3$  and  $\text{LaF}_3$ . These radii were used in Table 1 after applying small corrections ( $+0.030 \text{ \AA}$  to  $\text{IXLa}^{3+}$ ,  $\text{IXCe}^{3+}$ ,  $\text{IXPr}^{3+}$ , and  $\text{IXNd}^{3+}$ ;  $+0.025 \text{ \AA}$  to all other Greis & Petzel  $\text{IXRE}^{3+}$  radii, and  $0.015 \text{ \AA}$  to all

$\text{VIII RE}^{3+}$  radii) for consistency with experimental interatomic distances and radii-CN plots.

Where structural data were not available or not accurate, plots of (1) radii vs unit cell volumes, (2) radii vs CN and (3) radii vs oxidation state, or combinations of these were used to obtain estimated values. Fig. 1 shows examples of radii-valence plots used to provide consistency between experimental radii and those anticipated from the regular nature of these plots. Cations whose final radii values were derived from both estimated values and experimental interatomic distances are:  $\text{VI Os}^{3+}$ ,  $\text{VI Os}^{6+}$ ,  $\text{VI Os}^{7+}$ ,  $\text{VI Re}^{4+}$ ,  $\text{VI Re}^{5+}$ ,  $\text{VI Re}^{6+}$ ,  $\text{VI Re}^{7+}$ ,  $\text{VI Rh}^{4+}$ ,  $\text{VII U}^{4+}$ ,  $\text{VII U}^{5+}$ , and  $\text{VII U}^{6+}$ .

Fig. 2(a)-(e) shows plots of radii vs CN. Generally, it was assumed that radii-CN plots for two different ions do not cross. Radii for  $\text{IV Cu}^+$ ,  $\text{VI Cu}^+$ ,  $\text{IX Rb}^+$ ,  $\text{VNi}^{2+}$ ,  $\text{VII Er}^{3+}$ ,  $\text{VII Yb}^{3+}$ ,  $\text{VII Tb}^{3+}$ ,  $\text{XII Nd}^{3+}$ ,  $\text{IV Cr}^{4+}$ ,

Table 1. *Effective ionic radii*

CR crystal radius, IR effective ionic radius, R from  $r^3$  vs  $V$  plots, C calculated, E estimated, ? doubtful, \* most reliable, M from metallic oxides.

| ION             | EC | CN | SP    | CR    | *IR* | ION             | EC | CN | SP    | CR    | *IR* | ION             | EC | CN | SP    | CR    | *IR* |
|-----------------|----|----|-------|-------|------|-----------------|----|----|-------|-------|------|-----------------|----|----|-------|-------|------|
| AC+3 6P 6 VI    |    |    | 1.26  | 1.12  | R    | CL-1 3P 6 VI    |    |    | 1.67  | 1.81  | P    | GD+3 4F 7 VII   |    |    | 1.14  | 1.00  |      |
| AG+1 4D10 II    |    |    | .81   | .67   |      | CL+5 3S 2 IIIPY |    |    | .26   | .12   |      | GE+2 4S 2 VI    |    |    | 1.193 | 1.053 | R    |
| IV              |    |    | 1.14  | 1.00  | C    | CL+7 2P 6 IV    |    |    | .22   | .08   | *    | GE+4 3D10 IV    |    |    | 1.247 | 1.107 | RC   |
| IVSQ            |    |    | 1.16  | 1.02  |      | VI              |    |    | .41   | .27   | A    | VI              |    |    | .87   | .73   | A    |
| V               |    |    | 1.23  | 1.09  | C    | CM+3 5F 7 VI    |    |    | 1.11  | .97   | R    | VI              |    |    | .930  | .390  | *    |
| VI              |    |    | 1.29  | 1.15  | C    | CM+4 5F 6 VI    |    |    | .99   | .85   | R    | VI              |    |    | .670  | .530  | R*   |
| VII             |    |    | 1.36  | 1.22  |      | VIII            |    |    | 1.09  | .95   | R    | H +1 1S 0 I     |    |    | -.24  | -.38  |      |
| VIII            |    |    | 1.42  | 1.28  |      | CD+2 3D 7 IV    | HS |    | .72   | .58   |      | II              |    |    | -.04  | -.18  |      |
| AG+2 4D 9 IVSQ  |    |    | .93   | .79   |      | V               |    |    | .81   | .67   | C    | HF+4 4F14 IV    |    |    | .72   | .58   | R    |
| VI              |    |    | 1.08  | .94   |      | VI              | LS |    | .79   | .65   | R    | VI              |    |    | .85   | .71   | R    |
| AG+3 4D 8 IVSQ  |    |    | .81   | .67   |      | HS              |    |    | .885  | .745  | R*   | VII             |    |    | .90   | .76   |      |
| VI              |    |    | .89   | .75   | R    | CD+3 3D 6 VI    | LS |    | 1.04  | .90   |      | VIII            |    |    | .97   | .83   |      |
| AL+3 2P 6 IV    |    |    | .53   | .39   | *    | VI              |    |    | .685  | .565  | R*   | HG+1 6S 1 III   |    |    | 1.11  | .97   |      |
| VI              |    |    | .62   | .48   |      | HS              |    |    | .75   | .61   |      | II              |    |    | 1.33  | 1.19  |      |
| V               |    |    | .675  | .535  | R*   | CD+4 3D 5 IV    | HS |    | .54   | .40   |      | HG+2 5D10 VI    |    |    | .83   | .69   |      |
| AM+2 5F 7 VII   |    |    | 1.35  | 1.21  |      | VI              |    |    | .67   | .53   | R    | IV              |    |    | 1.10  | .96   |      |
| VIII            |    |    | 1.40  | 1.26  |      | LS              |    |    | .87   | .73   | E    | VI              |    |    | 1.16  | 1.02  |      |
| IX              |    |    | 1.45  | 1.31  |      | HS              |    |    | .94   | .80   | R    | VIII            |    |    | 1.28  | 1.14  | R    |
| AM+3 5F 6 VI    |    |    | 1.115 | .975  | R    | CR+3 3D 3 VI    |    |    | .755  | .615  | R*   | HO+3 4F10 VI    |    |    | 1.041 | .901  | R    |
| VIII            |    |    | 1.23  | 1.09  |      | CR+4 3D 2 IV    |    |    | .55   | .41   |      | VIII            |    |    | 1.155 | 1.015 | R    |
| AM+4 5F 5 VI    |    |    | .99   | .85   | R    | VI              |    |    | .69   | .55   | R    | IX              |    |    | 1.212 | 1.072 | R    |
| VIII            |    |    | 1.09  | .95   |      | CR+5 3D 1 IV    |    |    | .485  | .345  | R    | X               |    |    | 1.26  | 1.12  |      |
| AS+3 4S 2 VI    |    |    | .72   | .58   | A    | VI              |    |    | .63   | .49   | EA   | I -1 5P 6 VI    |    |    | 2.06  | 2.20  | A    |
| AS+5 3D10 IV    |    |    | .675  | .535  | R*   | VIII            |    |    | .71   | .57   |      | I +5 5S 2 IIIPY |    |    | .58   | .44   | *    |
| VI              |    |    | .60   | .46   | C*   | CR+6 3P 6 IV    |    |    | .40   | .26   |      | VI              |    |    | 1.09  | .95   |      |
| AT+7 5D10 VI    |    |    | .76   | .62   | A    | VI              |    |    | .58   | .44   | C    | I +7 4D10 IV    |    |    | .56   | .42   |      |
| AU+1 5D10 VI    |    |    | 1.51  | 1.37  | A    | CS+1 5P 6 VIII  |    |    | 1.81  | 1.67  |      | VI              |    |    | .67   | .53   |      |
| AU+3 5D 8 IVSQ  |    |    | .82   | .68   |      | IX              |    |    | 1.88  | 1.74  |      | IN+3 4D10 IV    |    |    | .76   | .62   |      |
| VI              |    |    | .99   | .85   | A    | IX              |    |    | 1.92  | 1.78  |      | VI              |    |    | .940  | .800  | R*   |
| AU+5 5D 6 VI    |    |    | .71   | .57   |      | X               |    |    | 1.95  | 1.81  |      | VIII            |    |    | 1.06  | .92   | RC   |
| 8 +3 1S 2 III   |    |    | .55   | .41   | *    | XI              |    |    | 1.99  | 1.85  |      | IR+3 5D 6 VI    |    |    | .82   | .68   | E    |
| IV              |    |    | .55   | .41   | *    | XII             |    |    | 2.02  | 1.88  |      | IR+4 5D 5 VI    |    |    | .765  | .625  | R    |
| VI              |    |    | .41   | .27   | C    | CU+1 3D10 II    |    |    | .60   | .46   |      | IR+5 5D 4 VI    |    |    | .71   | .57   | EM   |
| BA+2 5P 6 VI    |    |    | 1.49  | 1.35  |      | IV              |    |    | .74   | .60   | E    | K +1 3P 6 IV    |    |    | 1.51  | 1.37  |      |
| VII             |    |    | 1.52  | 1.38  |      | VI              |    |    | .91   | .77   | E    | VI              |    |    | 1.52  | 1.38  |      |
| VIII            |    |    | 1.56  | 1.42  | C    | CU+2 3D 9 IV    |    |    | .71   | .57   |      | VII             |    |    | 1.60  | 1.46  |      |
| IX              |    |    | 1.61  | 1.47  |      | IVSQ            |    |    | .71   | .57   | *    | VIII            |    |    | 1.65  | 1.51  |      |
| X               |    |    | 1.66  | 1.52  |      | V               |    |    | .79   | .65   | *    | IX              |    |    | 1.69  | 1.55  |      |
| XI              |    |    | 1.71  | 1.57  |      | VI              |    |    | .87   | .73   |      | X               |    |    | 1.73  | 1.59  |      |
| XII             |    |    | 1.75  | 1.61  | C    | CU+3 3D 8 VI    | LS |    | .68   | .54   |      | XI              |    |    | 1.78  | 1.64  |      |
| BE+2 1S 2 III   |    |    | .30   | .16   |      | D +1 1S 0 II    |    |    | .04   | -.10  |      | LA+3 4D10 VI    |    |    | 1.172 | 1.032 | R    |
| IV              |    |    | .41   | .27   | *    | DY+2 4F10 VI    |    |    | 1.21  | 1.07  |      | VII             |    |    | 1.24  | 1.10  |      |
| VI              |    |    | .59   | .45   | C    | VIII            |    |    | 1.27  | 1.13  |      | VIII            |    |    | 1.300 | 1.160 | R    |
| BI+3 6S 2 V     |    |    | 1.10  | .96   | C    | VI              |    |    | 1.33  | 1.19  |      | IX              |    |    | 1.356 | 1.216 | R    |
| VI              |    |    | 1.17  | 1.03  | R*   | UY+3 4F 9 VI    |    |    | 1.052 | .912  | R    | X               |    |    | 1.41  | 1.27  |      |
| VII             |    |    | 1.31  | 1.17  | R    | VII             |    |    | .11   | .97   |      | XI              |    |    | 1.50  | 1.36  | C    |
| BI+5 5D10 VII   |    |    | .90   | .76   | E    | VIII            |    |    | 1.167 | 1.027 | R    | LI+1 1S 2 IV    |    |    | .730  | .590  | *    |
| BK+3 5F 8 VI    |    |    | 1.10  | .96   | R    | IX              |    |    | 1.223 | 1.083 | R    | VI              |    |    | .90   | .76   | *    |
| BK+4 5F 7 VI    |    |    | .97   | .83   | R    | ER+3 4F11 VI    |    |    | 1.030 | .890  | R    | VIII            |    |    | 1.06  | .92   | C    |
| VIII            |    |    | 1.07  | .93   | R    | VII             |    |    | 1.085 | .945  |      | LU+3 4F14 VI    |    |    | 1.001 | .861  | R    |
| BR-1 4P 6 VI    |    |    | 1.82  | 1.66  | P    | VIII            |    |    | 1.144 | 1.004 | R    | VII             |    |    | 1.117 | .977  | R    |
| BR+3 4P 2 IVSQ  |    |    | .73   | .59   |      | IX              |    |    | 1.202 | 1.062 | R    | IX              |    |    | 1.172 | 1.032 | R    |
| BR+5 4S 2 IIIPY |    |    | .45   | .31   |      | EU+2 4F 7 VI    |    |    | 1.31  | 1.17  |      | VI              |    |    | .71   | .57   |      |
| BR+7 3D10 IV    |    |    | .39   | .25   |      | V               |    |    | 1.34  | 1.20  | V    | VI              |    |    | .80   | .66   |      |
| VI              |    |    | .53   | .39   | A    | VIII            |    |    | 1.39  | 1.25  |      | VII             |    |    | .860  | .720  | *    |
| C +4 1S 2 III   |    |    | .06   | -.08  |      | IX              |    |    | 1.44  | 1.30  |      | VIII            |    |    | 1.03  | .89   | C    |
| IV              |    |    | .29   | .15   | P    | X               |    |    | 1.49  | 1.35  |      | HS              |    |    | .80   | .66   |      |
| VI              |    |    | .16   | .02   |      | EU+3 4F 6 VI    |    |    | 1.087 | .947  | R    | VI              | HS |    | .89   | .75   | C    |
| CA+2 3P 6 VI    |    |    | 1.14  | 1.00  |      | VII             |    |    | 1.15  | 1.01  |      | LS              |    |    | .81   | .67   | E    |
| VII             |    |    | 1.20  | 1.06  | *    | VIII            |    |    | 1.206 | 1.066 | R    | HS              |    |    | .970  | .830  | R*   |
| VIII            |    |    | 1.26  | 1.12  | *    | IX              |    |    | 1.260 | 1.120 | R    | VI              |    |    | 1.04  | .90   | C    |
| IX              |    |    | 1.32  | 1.18  |      | F -1 2P 6 VI    |    |    | 1.145 | 1.005 |      | VIII            |    |    | 1.10  | .96   | R    |
| X               |    |    | 1.37  | 1.23  | C    | III             |    |    | 1.16  | 1.30  |      | MN+3 3D 4 V     |    |    | .72   | .58   |      |
| XII             |    |    | 1.48  | 1.34  | C    | IV              |    |    | 1.17  | 1.31  |      | VI              | LS |    | .72   | .58   | R    |
| CD+2 4D10 IV    |    |    | .92   | .78   |      | VI              |    |    | 1.19  | 1.33  |      | HS              |    |    | .785  | .645  | R*   |
| V               |    |    | 1.01  | .87   |      | F +7 1S 2 VI    |    |    | .22   | .08   | A    | MN+4 3D 3 IV    |    |    | .53   | .39   | R    |
| VI              |    |    | 1.09  | .95   |      | FE+2 3D 6 IV    | HS |    | .77   | .63   |      | VI              |    |    | .670  | .530  | R*   |
| VII             |    |    | 1.17  | 1.03  | C    | IVSQ            |    |    | .78   | .64   |      | MN+5 3D 2 IV    |    |    | .47   | .33   | R    |
| VIII            |    |    | 1.24  | 1.10  | C    | VI              | LS |    | .75   | .61   | E    | MN+6 3D 1 IV    |    |    | .75   | .61   | R    |
| IX              |    |    | 1.45  | 1.31  |      | HS              |    |    | .920  | .780  | R*   | MN+7 3P 6 IV    |    |    | .39   | .25   |      |
| CE+3 6S 1 VI    |    |    | 1.15  | 1.01  | R    | VIII            |    |    | 1.06  | .92   | C    | VI              |    |    | .60   | .46   | A    |
| VII             |    |    | 1.21  | 1.07  | E    | FE+3 3D 5 IV    | HS |    | .63   | .49   | *    | VI              |    |    | .83   | .69   | E    |
| VIII            |    |    | 1.283 | 1.143 | R    | V               |    |    | .72   | .58   |      | MO+4 4D 2 VI    |    |    | .790  | .650  | RM   |
| IX              |    |    | 1.336 | 1.196 | R    | VI              | LS |    | .69   | .55   | R    | MO+5 4D 1 IV    |    |    | .60   | .46   | R    |
| X               |    |    | 1.39  | 1.25  | C    | HS              |    |    | .785  | .645  | R*   | VI              |    |    | .75   | .61   | R    |
| XI              |    |    | 1.48  | 1.34  | C    | FE+4 3D 4 VI    | HS |    | .92   | .78   | C    | MO+6 4P 6 IV    |    |    | .55   | .41   | R*   |
| CE+4 5P 6 VI    |    |    | 1.01  | .87   | R    | VI              |    |    | .725  | .585  | R    | V               |    |    | .64   | .50   |      |
| VIII            |    |    | 1.11  | .97   | R    | FE+6 3D 2 IV    |    |    | .39   | .25   | R    | VI              |    |    | .73   | .59   | R*   |
| X               |    |    | 1.21  | 1.07  |      | FR+1 6P 6 VI    |    |    | 1.94  | 1.80  | A    | VII             |    |    | .87   | .73   |      |
| XII             |    |    | 1.14  | .99   |      | GA+3 3D10 IV    |    |    | .61   | .47   | *    | N -3 2P 6 VI    |    |    | 1.32  | 1.18  |      |
| CF+3 6D 1 VI    |    |    | 1.09  | .95   | R    | VI              |    |    | .69   | .55   |      | N +3 2S 2 VI    |    |    | .30   | .16   | A    |
| CF+4 5F 8 VI    |    |    | .961  | .821  | R    | VI              |    |    | .760  | .620  | R*   | N +5 1S 2 III   |    |    | .044  | -.104 | A    |
| VIII            |    |    | 1.06  | .92   |      | GD+3 4F 7 VI    |    |    | 1.078 | .938  | R    | VI              |    |    | .27   | -.13  | A    |

Table 1 (cont.)

| ION            | EC | CN | SP | CR    | 'IR'     | ION            | EC | CN | SP | CR    | 'IR'    | ION           | EC | CN | SP | CR    | 'IR'     |
|----------------|----|----|----|-------|----------|----------------|----|----|----|-------|---------|---------------|----|----|----|-------|----------|
| Na+1 2P 6 IV   |    |    |    | 1.13  | .99      | PR+3 4F 2 VI   |    |    |    | 1.13  | .99 R   | TC+4 4D 3 VI  |    |    |    | .785  | .645 RM  |
| V              |    |    |    | 1.14  | 1.00     | VIII           |    |    |    | 1.266 | 1.126 R | TC+5 4D 2 VI  |    |    |    | .74   | .60 ER   |
| VI             |    |    |    | 1.16  | 1.02     | IX             |    |    |    | 1.317 | 1.179 R | TC+7 4P 6 VI  |    |    |    | .51   | .37      |
| VII            |    |    |    | 1.26  | 1.12     | PR+4 4F 1 VI   |    |    |    | .99   | .85 R   | TE-2 5P 6 VI  |    |    |    | 2.07  | 2.21 P   |
| VIII           |    |    |    | 1.32  | 1.18     | VIII           |    |    |    | 1.10  | .96 R   | TE+4 5S 2 VII |    |    |    | .66   | .52      |
| IX             |    |    |    | 1.38  | 1.24 C   | PT+2 5D 8 IVSQ |    |    |    | .74   | .60     | VI            |    |    |    | .80   | .66      |
| X              |    |    |    | 1.53  | 1.39     | IX             |    |    |    | .94   | .80 A   | VI            |    |    |    | 1.11  | .97      |
| NB+3 4D 2 VI   |    |    |    | .86   | .72      | PT+4 5D 6 VI   |    |    |    | .765  | .625 R  | TE+6 4D10 IV  |    |    |    | .57   | .43 C    |
| NB+4 4D 1 VI   |    |    |    | .82   | .68 RE   | PT+5 5D 5 VI   |    |    |    | .71   | .57 ER  | VI            |    |    |    | .70   | .56 *    |
| VIII           |    |    |    | .93   | .79      | PU+3 5F 5 VI   |    |    |    | 1.14  | 1.00 R  | TH+4 6P 6 VI  |    |    |    | 1.08  | .94 C    |
| NB+5 4P 6 VI   |    |    |    | .78   | .64 C    | PU+4 5F 4 VI   |    |    |    | 1.00  | .86 R   | VIII          |    |    |    | 1.19  | 1.05 RC  |
| VII            |    |    |    | .83   | .69 C    | PU+5 5F 3 VI   |    |    |    | .88   | .74 E   | IX            |    |    |    | 1.23  | 1.09 *   |
| VIII           |    |    |    | .88   | .74      | PU+6 5F 2 VI   |    |    |    | .85   | .71 R   | X             |    |    |    | 1.27  | 1.13 E   |
| ND+2 4F 4 VIII |    |    |    | 1.43  | 1.29     | RA+2 6P 6 VIII |    |    |    | 1.62  | 1.48 R  | XI            |    |    |    | 1.32  | 1.18 C   |
| IX             |    |    |    | 1.49  | 1.35     | XII            |    |    |    | 1.84  | 1.70 R  | XII           |    |    |    | 1.35  | 1.21 C   |
| ND+3 4F 3 VI   |    |    |    | 1.123 | .983 R   | RB+1 4P 6 VI   |    |    |    | 1.66  | 1.52    | TI+2 3D 2 VI  |    |    |    | 1.00  | .86 E    |
| VIII           |    |    |    | 1.249 | 1.109 R* | VII            |    |    |    | 1.70  | 1.56 E  | TI+3 3D 1 VI  |    |    |    | .810  | .670 RM  |
| IX             |    |    |    | 1.303 | 1.163 R  | VIII           |    |    |    | 1.75  | 1.61    | TI+4 3P 6 IV  |    |    |    | .56   | .42 C    |
| XII            |    |    |    | 1.41  | 1.27 E   | IX             |    |    |    | 1.77  | 1.63 E  | V             |    |    |    | .65   | .51 C    |
| NI+2 3D 8 IV   |    |    |    | .69   | .55      | X              |    |    |    | 1.80  | 1.66    | VI            |    |    |    | .745  | .605 R*  |
| IVSQ           |    |    |    | .63   | .49      | XI             |    |    |    | 1.83  | 1.69    | VIII          |    |    |    | .88   | .74 C    |
| V              |    |    |    | .77   | .63 E    | XII            |    |    |    | 1.86  | 1.72    | TL+1 6S 2 VI  |    |    |    | 1.64  | 1.50 R   |
| VI             |    |    |    | .830  | .690 R*  | XIV            |    |    |    | 1.97  | 1.83    | VIII          |    |    |    | 1.73  | 1.59 R   |
| NI+3 3U 7 VI   | LS |    |    | .70   | .56 R*   | RE+4 5D 3 VI   |    |    |    | .77   | .63 RM  | XII           |    |    |    | 1.84  | 1.70 RE  |
| HS             |    |    |    | .74   | .60 E    | RE+5 5D 2 VI   |    |    |    | .72   | .58 E   | TL+3 5D10 IV  |    |    |    | .89   | .75      |
| LS             |    |    |    | .62   | .48 R    | RE+6 5D 1 VI   |    |    |    | .69   | .55 E   | VI            |    |    |    | 1.025 | .885 R   |
| NI+4 3D 6 VI   |    |    |    | 1.24  | 1.1 E    | RE+7 5P 6 IV   |    |    |    | .52   | .38     | VIII          |    |    |    | 1.12  | .98 C    |
| ND+2 5F14 VI   |    |    |    | 1.24  | 1.10     | VI             |    |    |    | .67   | .53     | TM+2 4F13 VII |    |    |    | 1.17  | 1.03     |
| NP+2 5F 5 VI   |    |    |    | 1.01  | .87 R    | RH+3 4D 6 VI   |    |    |    | .805  | .665 R  | VII           |    |    |    | 1.23  | 1.09     |
| NP+3 5F 4 VI   |    |    |    | 1.24  | 1.01     | RH+4 4D 5 VI   |    |    |    | .74   | .60 RM  | TM+3 4F12 VI  |    |    |    | 1.020 | .880 R   |
| NP+4 5F 3 VI   |    |    |    | 1.12  | .98 R    | RH+5 4D 4 VI   |    |    |    | .69   | .55     | VIII          |    |    |    | 1.134 | .994 R   |
| NP+5 5F 2 VI   |    |    |    | .89   | .75      | RU+3 4D 5 VI   |    |    |    | .82   | .68     | IX            |    |    |    | 1.192 | 1.05 R   |
| NP+6 5F 1 VI   |    |    |    | .86   | .72 R    | RU+4 4D 4 VI   |    |    |    | .760  | .620 RM | U +3 5F 3 VI  |    |    |    | 1.165 | 1.025 R  |
| NP+7 6P 6 VI   |    |    |    | .85   | .71 A    | RU+5 4D 3 VI   |    |    |    | .705  | .565 ER | U +4 5F 2 VI  |    |    |    | 1.03  | .89      |
| O -2 2P 6 II   |    |    |    | 1.21  | 1.35     | RU+7 4D 1 IV   |    |    |    | .52   | .38     | VII           |    |    |    | 1.09  | .95 E    |
| II             |    |    |    | 1.22  | 1.36     | RU+8 4P 6 IV   |    |    |    | .50   | .36     | IV            |    |    |    | 1.14  | 1.00 R*  |
| III            |    |    |    | 1.24  | 1.38     | S -2 3P 6 VI   |    |    |    | 1.70  | 1.84 P  | IX            |    |    |    | 1.19  | 1.05     |
| IV             |    |    |    | 1.26  | 1.40     | S +4 3S 2 VI   |    |    |    | .51   | .37 A   | XII           |    |    |    | 1.31  | 1.17 E   |
| V              |    |    |    | 1.28  | 1.42     | S +6 2P 6 IV   |    |    |    | .26   | .12 *   | U +5 5F 1 VI  |    |    |    | .90   | .76      |
| VI             |    |    |    | 1.18  | 1.32     | VI             |    |    |    | .63   | .29 C   | VI            |    |    |    | .98   | .84 E    |
| VII            |    |    |    | 1.20  | 1.34     | SB+3 5S 2 IVPV |    |    |    | .90   | .76     | U +6 6P 6 II  |    |    |    | .59   | .45      |
| VIII           |    |    |    | 1.21  | 1.35 E   | V              |    |    |    | .94   | .80     | IV            |    |    |    | .66   | .52      |
| IX             |    |    |    | 1.23  | 1.37 E   | VI             |    |    |    | .90   | .76 A   | VI            |    |    |    | .87   | .73 *    |
| OS+4 5D 4 VI   |    |    |    | .770  | .630 RM  | SB+5 4D10 VI   |    |    |    | .74   | .60 *   | VII           |    |    |    | .95   | .81 E    |
| OS+5 5D 3 VI   |    |    |    | .715  | .575 E   | SC+3 3P 6 VI   |    |    |    | .885  | .745 R* | VIII          |    |    |    | 1.00  | .86      |
| OS+6 5D 2 V    |    |    |    | .63   | .49      | VIII           |    |    |    | 1.010 | .870 R* | V +2 3D 3 VI  |    |    |    | .93   | .79      |
| OS+7 5D 1 VI   |    |    |    | .685  | .545 E   | SE-2 4P 6 VI   |    |    |    | 1.84  | 1.98 P  | V +3 3D 2 VI  |    |    |    | .70   | .56 RM   |
| OS+8 5P 6 IV   |    |    |    | .53   | .39      | SE+4 4S 2 VI   |    |    |    | .64   | .50 A   | V +4 3D 1 V   |    |    |    | .67   | .53      |
| P +3 3S 2 VI   |    |    |    | .58   | .44 A    | SE+6 3D10 IV   |    |    |    | .42   | .28 *   | VI            |    |    |    | .72   | .58 R*   |
| P +5 2P 6 IV   |    |    |    | .31   | .17 *    | SI+4 2P 6 VI   |    |    |    | .56   | .42 C   | VIII          |    |    |    | .86   | .72 E    |
| V              |    |    |    | .29   | .15      | VI             |    |    |    | .60   | .46 *   | V +5 3P 6 IV  |    |    |    | .495  | .355 RM  |
| VI             |    |    |    | .52   | .38 C    | SM+2 4F 6 VII  |    |    |    | 1.36  | 1.22    | V             |    |    |    | .60   | .46 *    |
| PA+3 5F 2 VI   |    |    |    | 1.18  | 1.04 E   | VIII           |    |    |    | 1.41  | 1.27    | VI            |    |    |    | .68   | .54      |
| PA+4 6D 1 VI   |    |    |    | 1.04  | .90 R    | IX             |    |    |    | 1.32  | 1.18    | W +4 5D 2 VI  |    |    |    | .80   | .66 RM   |
| VII            |    |    |    | 1.15  | 1.01     | SM+3 4F 5 VI   |    |    |    | 1.098 | .958 R  | W +5 5D 1 VI  |    |    |    | .76   | .62 R    |
| PA+5 6P 6 VI   |    |    |    | .92   | .78      | VII            |    |    |    | 1.16  | 1.02 E  | W +6 5P 6 IV  |    |    |    | .56   | .42 *    |
| VIII           |    |    |    | 1.05  | .91      | VIII           |    |    |    | 1.219 | 1.079 R | VI            |    |    |    | .65   | .51      |
| IX             |    |    |    | 1.09  | .95      | IX             |    |    |    | 1.272 | 1.132 R | VI            |    |    |    | .74   | .60 A    |
| PB+2 6S 2 IVPV |    |    |    | 1.12  | .98 C    | XII            |    |    |    | 1.38  | 1.24 C  | XE+8 4D10 IV  |    |    |    | .54   | .40      |
| VI             |    |    |    | 1.33  | 1.19     | SN+4 4D10 IV   |    |    |    | .69   | .55 R   | VI            |    |    |    | .62   | .48      |
| VII            |    |    |    | 1.37  | 1.23 C   | V              |    |    |    | .76   | .62 C   | Y +3 4P 6 VI  |    |    |    | 1.040 | .900 R*  |
| VIII           |    |    |    | 1.43  | 1.29 C   | VI             |    |    |    | .830  | .690 R* | VII           |    |    |    | 1.159 | 1.019 R* |
| IX             |    |    |    | 1.49  | 1.35 C   | VII            |    |    |    | .89   | .75     | IX            |    |    |    | 1.215 | 1.075 R  |
| X              |    |    |    | 1.54  | 1.40 C   | VIII           |    |    |    | .95   | .81 C   | YB+2 4F14 VI  |    |    |    | 1.16  | 1.02     |
| XI             |    |    |    | 1.59  | 1.45 C   | SR+2 4P 6 VII  |    |    |    | 1.32  | 1.18    | VII           |    |    |    | 1.22  | 1.08 E   |
| XII            |    |    |    | 1.63  | 1.49     | VIII           |    |    |    | 1.35  | 1.21    | VIII          |    |    |    | 1.28  | 1.14     |
| PB+4 5D10 IV   |    |    |    | .79   | .65 E    | IX             |    |    |    | 1.40  | 1.26    | YB+3 4F13 VI  |    |    |    | 1.008 | .868 R*  |
| V              |    |    |    | .87   | .73 E    | IX             |    |    |    | 1.45  | 1.31    | VII           |    |    |    | 1.065 | .925 E   |
| VI             |    |    |    | .915  | .775 R   | X              |    |    |    | 1.50  | 1.36 C  | VIII          |    |    |    | 1.125 | .985 R   |
| VIII           |    |    |    | 1.08  | .94 R    | XII            |    |    |    | 1.58  | 1.44 C  | IX            |    |    |    | 1.182 | 1.042 R  |
| PD+1 4D 9 II   |    |    |    | .73   | .59      | TA+3 5D 2 VI   |    |    |    | .86   | .72 E   | ZN+2 3D10 IV  |    |    |    | .74   | .60 *    |
| PD+2 4D 8 IVSQ |    |    |    | .78   | .64      | TA+4 5D 1 VI   |    |    |    | .82   | .68 E   | V             |    |    |    | .82   | .68 *    |
| PD+3 4D 7 VI   |    |    |    | 1.00  | .86      | TA+5 5P 6 VI   |    |    |    | .78   | .64     | VI            |    |    |    | .880  | .740 R*  |
| PD+4 4D 6 VI   |    |    |    | .90   | .76      | VII            |    |    |    | .83   | .69     | VIII          |    |    |    | 1.04  | .90 C    |
| PD+5 4D 5 VI   |    |    |    | .755  | .615 R   | VIII           |    |    |    | .88   | .74     | ZR+4 4P 6 IV  |    |    |    | .73   | .59 R    |
| PD+6 4F 4 VI   |    |    |    | 1.11  | .97 R    | IX             |    |    |    | 1.063 | .923 R  | V             |    |    |    | .80   | .66 C    |
| PD+7 4F 3 VI   |    |    |    | 1.233 | 1.093 R  | TI+3 4F 8 VI   |    |    |    | 1.12  | .98 E   | VI            |    |    |    | .86   | .72 R*   |
| IX             |    |    |    | 1.284 | 1.144 R  | VII            |    |    |    | 1.180 | 1.040 R | VII           |    |    |    | .92   | .78 *    |
| PD+4 6S 2 VI   |    |    |    | 1.08  | .94 R    | VIII           |    |    |    | 1.235 | 1.095 R | VIII          |    |    |    | .98   | .84 *    |
| VIII           |    |    |    | 1.22  | 1.08 R   | IX             |    |    |    | .90   | .76 R   | IX            |    |    |    | 1.03  | .89      |
| PD+6 5D10 VI   |    |    |    | .81   | .67 A    | TI+4 4F 7 VIII |    |    |    | 1.02  | .88     |               |    |    |    |       |          |

$\text{VIII V}^{4+}$ ,  $\text{IV Pb}^{4+}$ , and  $\text{X Th}^{4+}$  obtained from these plots were used to help determine the values in Table 1. The first estimate of  $\text{VIII V}^{4+}$  was made from distances in  $\text{C}_{32}\text{H}_{28}\text{S}_8\text{V}$  (Bonamico, Dessy, Fares & Scaramuzza, 1974).

Another method used to estimate radii was based on the empirical relationship between interatomic distances and bond strengths. Brown & Shannon (1973) derived these relationships for the cations in the first three rows of the periodic table from a large number of experimental interatomic distances. These curves can be used to calculate hypothetical distances for cations in any coordination (Brown & Shannon, 1973; Shannon, 1975; Brown, 1975). Examples of cations whose radii were calculated in this way are:  $\text{IV Mn}^{2+}$ ,  $\text{VI Be}^{2+}$ ,  $\text{VI B}^{3+}$ ,  $\text{VI P}^{5+}$ ,  $\text{VI S}^{6+}$ ,  $\text{VIII Mg}^{2+}$ , and  $\text{VIII Fe}^{2+}$ . These are marked with a C in Table 1. In certain cases, these values were combined with known structural data (see Table 2) to obtain the radii in Table 1. Although the

majority of radii were derived from oxides and fluorides,\* some were taken from chlorides, bromides, iodides, and sulfides. For large electropositive cations with highly ionic bonds, very little covalent shortening is believed to occur and radii derived from these other compounds should differ only slightly from those derived from fluorides and oxides. Examples are divalent rare earths such as  $\text{Yb}^{2+}$ ,  $\text{Tm}^{2+}$ ,  $\text{Dy}^{2+}$ ,  $\text{Sm}^{2+}$ ,  $\text{Nd}^{2+}$  and the ions  $\text{Am}^{2+}$ ,  $\text{Ac}^{3+}$ ,  $\text{Np}^{3+}$ , and  $\text{U}^{4+}$ .

Another useful scheme for estimation of radii is the comparison of unit-cell volumes of compounds containing cations of similar size. McCarthy (1971) prepared a number of isotopic  $\text{Sr}^{2+}$  and  $\text{Eu}^{2+}$  ternary oxides and generally found the unit cells of the  $\text{Sr}^{2+}$

\* Because of covalency differences in M-O and M-F bonds, oxide distances were emphasized. Therefore the radii in Table 1 are more applicable to oxides than fluorides. This subject is treated further in the discussion *Effects of covalence*.

Table 2. References for Table 1

The references here and in Tables 4, 5, 6 and 8 are abbreviated according to *Codens for Periodic Titles* (1966).

|            |                        |      |                                      |
|------------|------------------------|------|--------------------------------------|
| AG+3 VI    | 68 JINCA               | 30   | 823 AC CL3                           |
| AG+1 II    | 71 INDOCA              | 10   | 719 AG FE 02                         |
| 72 ZAACA   | 393                    | 246  | 58 AG 04                             |
| 73 ZENBA   | 288                    | 263  | BA AG 04                             |
| AG+1 IV    | 71 JSSCB               | 3    | 364 AG 02 CR 04                      |
| AG+1 IVS0  | 42 JACSA               | 64   | 354 AG 03 AS 04                      |
| 69 ACSAA   | 23                     | 2261 | AG 2 S 03                            |
| AG+1 V     | 70 JSSCB               | 1    | 484 AG 06 MO10 033                   |
| AG+1 V     | 32 ZKKA                | 82   | 161 AG 02 S04                        |
| 47 JACSA   | 69                     | 222  | AG 03 P04                            |
| 71 JSSCB   | 3                      | 364  | AG 02 CR 04                          |
| 69 ACABA   | 25                     | 5116 | AG 02 CR 07                          |
| 70 JSSCB   | 1                      | 484  | AG 02 MO 04                          |
| AG+1 VII   | 70 JSSCB               | 1    | 484 AG 06 MO10 033                   |
| 69 ACABA   | 25                     | 5116 | AG 02 CR 07                          |
| AG+1 VII   | 65 ACCRA               | 19   | 180 AG 7 N 011                       |
| AG+2 IVS0  | 71 JPCSA               | 32   | 543 AG F2                            |
| AG+2 VI    | 71 JPCSA               | 32   | 543 AG F2                            |
| AG+3 IVS0  | 65 ACCRA               | 19   | 180 AG 7 N 011                       |
| AL+3 V     | 67 ACCRA               | 23   | 754 NA T12 AL5 012                   |
| 68 NJMBA   | 1968                   | 80   | CA AL B 04                           |
| 70 AGABA   | 26                     | 1230 | CA AL B 04                           |
| 70 NJMBA   | 1970                   | 547  | CA12 AL10 033                        |
| 71 SPMDA   | 15                     | 905  | CA AL 010 (OH)6                      |
| 71 SPMDA   | 15                     | 905  | CA AL 010 (OH)6                      |
| 71 SPMDA   | 15                     | 905  | CA AL 010 (OH)6                      |
| 72 JACSA   | 27                     | 1826 | BE14 AL2 03                          |
| 72 JSSCB   | 4                      | 60   | AG AL11 017                          |
| AL+3 V     | 68 ACABA               | 24   | 1518 (MG,FE) AL3 S1 B 09             |
| 68 AMNIA   | 53                     | 1096 | AL2 P04 (OH)3                        |
| AL+3 VI    | 71 AMNIA               | 56   | 18 NA3 AL2 L13 F12                   |
| 72 JSSCB   | 4                      | 11   | ND AL 03                             |
| 72 JSSCB   | 4                      | 11   | ND AL 03                             |
| 58 ACABA   | 5                      | 684  | MG AL2 04                            |
| 72 ACABA   | 28                     | 1899 | AL2 BE3 S10 D18                      |
| 68 JACSA   | 80                     | 22   | AL1AC1A                              |
| 73 ACABA   | 29                     | 2291 | AL P 0412 H2 0                       |
| 67 ZKKA    | 125                    | 1423 | CS BE4 B12-X1 AL4 O28 H2             |
| 74 ACABA   | 30                     | 1311 | NA AL 1P 0412 IO H14                 |
| 74 ACABA   | 139                    | 125  | AL IO H13                            |
| AM+2 VII   | 72 JINCA               | 34   | 3427 AM 12                           |
| AM+2 VIII  | 73 JINCA               | 35   | 483 AM BR2                           |
| AM+2 IX    | 73 JINCA               | 35   | 483 AM CL2                           |
| AM+3 VIII  | 72 JINCA               | 11   | 2233 AM2 (S 04)3.0H2 0               |
| AM+4 VI    | 67 ACABA               | 71   | 228 BA AM 03                         |
| 67 INUCA   | 3                      | 327  | R (BK+)                              |
| AS+5 IV    | 69 ZKKA                | 130  | 231 ZH2 CU AS2 08                    |
| 68 CJCHA   | 46                     | 917  | CU3 AS2 08                           |
| 63 BAPCA   | 11                     | 361  | MG AS2 07                            |
| 69 ACABA   | 25                     | 1544 | CA H AS 04.2 H2 0                    |
| 69 ACABA   | 25                     | 2658 | R H AS 04.2 H2 0                     |
| 68 AMNIA   | 53                     | 1841 | MN2 0 H AS 04                        |
| 63 CARIA   | 7                      | 561  | CA CU AS 04 0 H                      |
| 70 ACABA   | 24                     | 1584 | NA2 H AS 04.7 H2 0                   |
| 69 ACABA   | 26                     | 1574 | NA2 H AS 04.7 H2 0                   |
| 69 CHUCA   | 268                    | 1694 | BA H12 AS2 08                        |
| 70 AMNIA   | 55                     | 2023 | MN2 IO H19 (H2 012                   |
| 70 ACABA   | 26                     | 1809 | IN H12 H AS 04                       |
| 70 ACABA   | 24                     | 1711 | LI H 02 AS 04                        |
| 70 INUCA   | 9                      | 2259 | CA2 AS 04 CL                         |
| 69 ACABA   | 18                     | 777  | CU3 AS 04 IO H13                     |
| 70 CJCHA   | 48                     | 801  | CU3 AS2 08                           |
| 71 CJCHA   | 49                     | 1036 | CA AS 04                             |
| 70 AMNIA   | 55                     | 1409 | MN2 H AS 012                         |
| 71 ACABA   | 27                     | 2124 | NA3 AS 04.12 H2 0                    |
| 73 ACABA   | 29                     | 2611 | MG AS2 08                            |
| 61 AMNIA   | 46                     | 1077 | CA2 B AS 04 (OH)4                    |
| 73 CJCHA   | 51                     | 2082 | NA4 AS2 07                           |
| 68 ZAACA   | 347                    | 133  | CR H AS 04 H2 0                      |
| 66 ZAACA   | 347                    | 140  | SR H AS 04 H2 0                      |
| 71 AMNIA   | 56                     | 1167 | ZNA AS2 08 (OH)2.2H2 0               |
| 70 ACABA   | 26                     | 403  | CA H AS 04                           |
| 70 ZKKA    | 132                    | 332  | CU3 AS2 08                           |
| 73 ACABA   | 29                     | 141  | LU AS 04                             |
| 73 ACABA   | 29                     | 2121 | MN4 H AS 04                          |
| AS+5 VI    | 71 CJCHA               | 49   | 2539 CL F2 AS F6                     |
| 73 JSSCB   | 6                      | 80   | MGAS AS3 016                         |
| 70 CJCHA   | 48                     | 3124 | CUB AS3 016                          |
| 73 ACABA   | 29                     | 266  | CALCULATED                           |
| 74 INDOCA  | 13                     | 780  | XL AS F11.4E2 AS F9                  |
| 74 ACABA   | 30                     | 250  | K AS F6                              |
| AU+3 IVS0  | 69 JPCSA               | 1969 | 1936 R AU F4                         |
| 70 ZAACA   | 375                    | 43   | L13 AU O3.4 AU O2.8B AU O2           |
| 70 JCSIA   | 1970                   | 1092 | R AU INDO34                          |
| AU+5 VI    | 74 INUCA               | 13   | 775 RE2 AU F17                       |
| D+3 III    | 68 NJMBA               | 1968 | 80 CA AL B 04                        |
| 71 SPMDA   | 15                     | 902  | R BE2 B 03 F2                        |
| 71 ACABA   | 27                     | 672  | ZN B4 07                             |
| 70 ACABA   | 26                     | 1189 | B 02                                 |
| 71 ACABA   | 27                     | 904  | L13 B 03                             |
| 70 ZKKA    | 132                    | 241  | CA B3 05 (OH)1                       |
| 71 JACSA   | 4                      | 284  | LU B 04                              |
| 74 JPCSA   | 60                     | 1899 | MN B4 07                             |
| 74 MRBUA   | 9                      | 1661 | ND AL3 (B 03)4                       |
| B+3 IV     | 68 ACABA               | 24   | 869 B2 J3 I1                         |
| 68 ACABA   | 24                     | 1703 | NA B F4                              |
| 68 CJCHA   | 47                     | 2579 | R B F4                               |
| 71 ACABA   | 27                     | 677  | CU B2 04                             |
| 71 ACABA   | 132                    | 241  | CA B3 05 0 H                         |
| 63 ACABA   | 16                     | 1233 | NA B IO H14.2 H2 0                   |
| 74 JPCSA   | 60                     | 1899 | MN B4 07                             |
| 71 AMNIA   | 56                     | 1553 | MG (NO 07 IO H16) .2 H2 0            |
| 73 AMNIA   | 58                     | 909  | CA B S1 UN 0 H                       |
| 71 ACABA   | 27                     | 672  | ZN B4 07                             |
| B+3 VI     | 73 ACABA               | 29   | 266 CALCULATED                       |
| BA+2 VI    | 70 ZKKA                | 131  | 161 BA3 V2 08                        |
| 73 ZENBA   | 288                    | 263  | BA AG 04                             |
| BA+2 VII   | 71 ACABA               | 27   | 1263 BA FE2 04                       |
| 73 ACABA   | 29                     | 2009 | BA2 TI 04                            |
| BA+2 VIII  | 58 ZKKA                | 110  | 231 CU B42 IC 0 H16.4 H2 0           |
| 69 JPCSA   | 51                     | 428  | BA MN F4                             |
| 70 JPCSA   | 53                     | 3279 | BA CU F4                             |
| 71 JPCSA   | 55                     | 1093 | BA W 04                              |
| 71 AMNIA   | 56                     | 758  | BA C 03                              |
| 71 ZAACA   | 386                    | 1    | BA2 C 04                             |
| 73 ACABA   | 29                     | 2009 | BA2 TI 04                            |
| BA+2 IX    | 71 ZAACA               | 386  | 1 BA2 C 04                           |
| 73 ACABA   | 27                     | 1653 | BA TE (S2 03)2.2 H2 0                |
| 73 ACABA   | 27                     | 1653 | BA TE (S2 03)2.2 H2 0                |
| BA+2 X     | 70 ZKKA                | 131  | 161 BA3 IV 0412                      |
| 70 ACABA   | 26                     | 105  | BA3 S14 NB6 026                      |
| 67 BUFGA   | 90                     | 24   | BA P2 06                             |
| BA+2 XI    | 71 ACABA               | 27   | 1263 BA FE2 04                       |
| BA+2 XII   | 70 ACABA               | 26   | 102 BA5 TA 015                       |
| 72 CSCMC   | 1                      | 1    | BA T16 013                           |
| 71 MRBUA   | 6                      | 725  | BA CA FE4 08                         |
| 69 CHUCA   | 280                    | 1694 | BA H12 AS2 08                        |
| 75 ACABA   | 31                     | 596  | K2 BA CU (IN 02)6                    |
| BE+2 III   | 69 ACABA               | 25   | 1647 SR BE3 04                       |
| 66 ACABA   | 20                     | 295  | CA12 BE17 029                        |
| BE+2 IV    | 68 SPMDA               | 6    | 733 NA BE P 04                       |
| 68 ACABA   | 24                     | 672  | L42 BE2 05                           |
| 68 ACABA   | 24                     | 607  | CS BE F3                             |
| 69 ACABA   | 25                     | 1647 | SR BE3 04                            |
| 71 SPMDA   | 15                     | 909  | FE3 BE S13 09 (F,OH)2                |
| 72 SPMDA   | 16                     | 1021 | BE2 S14 0 H                          |
| 73 ACABA   | 28                     | 1899 | AL2 BE3 S16 018                      |
| 73 ACABA   | 229                    | 2976 | NA3 BE TH10 F45                      |
| 69 ACABA   | 12                     | 634  | BE AR F4T1                           |
| 67 ZKKA    | 125                    | 423  | CA BE4 B12-X1 AL4 O28 H2             |
| 74 ACABA   | 30                     | 396  | NA6 (S116 AL2)BE10H2 0391            |
| 74 ACABA   | 30                     | 2434 | L12 BE S1 04                         |
| 74 AMNIA   | 59                     | 1267 | CA BE2 P2 08                         |
| BI+3 V     | 69 JSCDA               | 7    | 1797 B12 M 06                        |
| 70 ACABA   | 24                     | 384  | B12 03 ALPHA                         |
| BI+3 VI    | 70 ACABA               | 24   | 384 B12 03 ALPHA                     |
| 71 JPCSA   | 32                     | 1315 | BI FE 03                             |
| BI+3 VIII  | 72 MRBUA               | 7    | 1025 BI TITANATES                    |
| BI+5 VI    | R3 VS V (BA2 LA B1 06) |      |                                      |
| BR+4 VI    | 67 INUCA               | 3    | 327 R (BK+)                          |
| BR+4 IV S0 | 71 JPCSA               | 1969 | 1936 K AR F4                         |
| BR+5 III   | 69 ACABA               | 25   | 421 SR (BR 03)3.9H2 0                |
| 67 ACABA   | 21                     | 2834 | MG BR 03                             |
| BR+7 IV    | 71 JCSIA               | 1971 | 1857 BR(+7)0                         |
| C+4 III    | 65 ACCRA               | 18   | 689 CA C 03                          |
| 71 JINCA   | 35                     | 27   | CA C 03                              |
| 73 AMNIA   | 58                     | 1029 | MG C 03                              |
| 67 PRALIA  | 92                     | 125  | MN C 03                              |
| 75 ACABA   | 31                     | 890  | NA2 C 03.2H2 0                       |
| CA+2 VI    | 68 NJMBA               | 1968 | 80 CA AL B 04                        |
| 69 ACABA   | 25                     | 1933 | CA IN2 BE P 0213                     |
| 57 JPCSA   | 26                     | 563  | CA IO H12                            |
| 55 ACABA   | 18                     | 689  | CA C 03                              |
| CA+2 VII   | 71 CJCHA               | 49   | 1036 CA3 AS2 08                      |
| 71 ACABA   | 27                     | 2311 | CA2 AL FE 05                         |
| 73 MRBUA   | 8                      | 593  | CA CR F5                             |
| 69 ACABA   | 25                     | 1534 | CA10 (P 04)6 IO H12                  |
| CA+2 VIII  | 71 INDOCA              | 7    | 1345 CA2 P2 07                       |
| 74 CJCHA   | 52                     | 1155 | CA18 MG2 H2 (P 04)14                 |
| CA+2 IX    | 71 JINCA               | 35   | 27 CA C 03                           |
| 69 ACABA   | 25                     | 1534 | CA10 (P 04)6 IO H12                  |
| CA+2 X     | 69 ACABA               | 25   | 955 CA B2 04 I11                     |
| CA+2 XII   | 69 ACABA               | 25   | 965 CA B2 04 IV                      |
| 74 AMNIA   | 59                     | 41   | CA AL3 IO H16                        |
| 74 JACSA   | 98                     | 6606 | K2 CA CU (IN 02)16                   |
| CD+2 IV    | 59 ACABA               | 12   | 1049 CO IN2 04                       |
| 71 ZAACA   | 382                    | 27   | K2 CO2 04                            |
| CD+2 V     | 69 CJCHA               | 47   | 3409 CO2 P2 07                       |
| 70 ZKKA    | 132                    | 332  | CU3 AS2 08                           |
| 69 CJCHA   | 47                     | 3409 | CO2 P2 07                            |
| 70 ZKKA    | 132                    | 332  | CU3 AS2 08                           |
| 66 SPMDA   | 11                     | 11   | CO W 04                              |
| 67 HCAGA   | 50                     | 2023 | CO2 MN3 08                           |
| 74 JCSIA   | 1974                   | 674  | CO CA H6 06                          |
| 74 ACABA   | 30                     | 1880 | CO2 C4 H12 012                       |
| CD+2 VII   | 74 ACABA               | 28A  | 119 CO D1C H2 C 0 D12.3 1/2 H2 0     |
| 74 JCSIA   | 1974                   | 1922 | CO D1C H2 C 0 U12.3 H2 0             |
| CD+2 VIII  | 55 PRVBA               | 98   | 903 CO2 N82 07                       |
| 69 ACABA   | 25                     | 1804 | CO IN 03)2.4 D2 0                    |
| 74 JCSIA   | 1974                   | 674  | CO CA H6 06                          |
| CE+3 VIII  | 74 ZAACA               | 403  | 1 R3 VS V (CE F3)                    |
| 74 JCSIA   | 1974                   | 1165 | C41 H24 CE F12 N DB 54               |
| CE+3 IX    | 67 SPMDA               | 12   | 214 CE B S1 05                       |
| 74 ZAACA   | 403                    | 1    | R3 VS V (CE F3)                      |
| CE+3 X     | 60 AMNIA               | 45   | 1 CE4 ME NE2 T12 S14 022             |
| CE+4 VI    | 72 ACABA               | 28   | 956 BA CE 03                         |
| 73 JSSCB   | 8                      | 331  | R (CE+4)                             |
| CE+4 VII   | 69 INUCA               | 8    | 33 IN H612 CE F6                     |
| 74 JCSIA   | 1974                   | 2021 | NA6 CE M10 D36.2H02 0                |
| 74 JCSIA   | 15                     | 397  | CE15 OH12                            |
| 74 ACABA   | 28                     | 1079 | AC CE (ACAC)4                        |
| CE+4 XII   | 68 JACSA               | 90   | 3589 (HMH)2 H6 ICE MD12 0421.12 H2 0 |
| CF+3 VI    | 71 JINCA               | 36   | 2023 R3 VS V (CF2 S 04)3             |
| CL+5 III   | 73 MRBUA               | 8    | 791 RB CL 03                         |
| CL+7 IV    | 72 ACABA               | 28   | 839 TMPO CL 04                       |
| 62 ZKKA    | 84                     | 65   | K CL 04                              |
| 60 ACABA   | 13                     | 855  | N U2 CL 04.8 CL 04                   |
| 59 JPCSA   | 63                     | 270  | H CL 04.2 H2 0                       |
| 59 JACSA   | 80                     | 5075 | CA H6 MG CL 04                       |
| 57 PISAA   | 50                     | 134  | N H CL 04                            |
| 57 PISAA   | 50                     | 143  | R CL 04                              |
| 62 ACABA   | 15                     | 1201 | N H CL 04                            |
| 71 JCSIA   | 1971                   | 1371 | CU (CL10 H9 N312 ICL 04)2            |
| 70 ACABA   | 26                     | 1928 | N2 H5 CL 04                          |
| 71 ACABA   | 27                     | 898  | H CL 04 IO 1/2 H2 0                  |
| 73 INCAH   | 7                      | 477  | IC N12-TRILEN-CU CL 04               |
| 71 ACABA   | 27                     | 898  | H CL 04.2 1/2 H2 0                   |
| 72 MRBUA   | 7                      | 1281 | CL1(+7) -0                           |
| 71 JCSIA   | 1971                   | 1857 | CL1(+7) -0                           |
| 62 ACABA   | 15                     | 18   | H3 O CL 04 (1-80 C1                  |
| 59 ACABA   | 25                     | 1875 | H3 O H CL 04                         |
| 73 ACASA   | 27                     | 2309 | (P84 IO H14)3 C 03 ICL 04110         |
| 73 ACASA   | 27                     | 3523 | CU (C3 H4 N214 ICL 04)2              |
| LM+4 VI    | 67 INUCA               | 3    | 327 R (CH+4)                         |
| CO+2 IV    | 69 ZAACA               | 369  | 306 CO V2 04                         |
| CO+2 V     | 72 SCBCA               | 28   | 2883 CO2 P2 07 ALPHA                 |
| CO+2 VI    | 68 ZAACA               | 358  | 125 CO SE 04                         |
| 68 ZKKA    | 126                    | 298  | CO GE 03                             |
| 70 CJCHA   | 48                     | 881  | CO3 AS2 08                           |
| 70 JPCSA   | 53                     | 3279 | BA CO F4                             |
| 70 PERIA   | 3                      | 181  | CO2 S1 04                            |
| 73 ACABA   | 29                     | 2304 | CO3 V2 08                            |
| 71 HCAGA   | 54                     | 1621 | CO3 IO H12 (S 04)2.2 H2 0            |
| REF 1      | CO2 S1 04              |      |                                      |
| 72 ACABA   | 28                     | 2883 | CO2 P2 07                            |
| 70 INDOCA  | 9                      | 151  | CO (OHMA)3 ICL 0412                  |
| 73 ACABA   | 29                     | 2741 | CO S1 F4.6 H2 0                      |
| 74 AMNIA   | 59                     | 475  | CO2 S1 04                            |
| 74 JCLMB   | 4                      | 55   | C16 H18 CO 06                        |
| CO+2 VIII  | 66 INDOCA              | 5    | 1208 (AS1C6 H514)2(COIN 03)3         |
| CO+3 VI    | 68 CJCHA               | 1968 | 871 CO (IN 03)3                      |
| 68 CJCHA   | 46                     | 3472 | CO3 04                               |
| 68 JACSA   | 88                     | 2951 | CO (C5 H7 02)3                       |
| 74 ACABA   | 30                     | 822  | CO (H7 02)3                          |
| 69 JACSA   | 91                     | 6881 | IN H416 (H4 CO2 MO10 0381            |
| 74 ZAACA   | 408                    | 97   | K CO2 04                             |
| CO+4 IV    | 71 ZAACA               | 386  | 1 BA2 CO 04                          |
| 73 ZAACA   | 398                    | 54   | L18 CO 06                            |
| 74 ZAACA   | 408                    | 75   | CS2 CO 03                            |
| 74 ZAACA   | 409                    | 152  | K6 CO2 07                            |
| CO+4 VI    | 67 STGBA               | 3    | 1 R3 VS V (FLUORIDES)                |
| 67 STGBA   | 408                    | 97   | K CO2 04                             |
| CR+2 VI    | 71 ANCPA               | 6    | 41 TA2 CR 06                         |
| 69 ACABA   | 25                     | 925  | R VS D ELECTRONS                     |
| CR+3 VI    | 69 MRBUA               | 4    | 621 NA3 CR F6                        |
| 70 INDOCA  | 9                      | 2289 | NA3 ICR MO 06 024 H61.8 H2 0         |
| 70 SPMDA   | 15                     | 902  | NA2 CR3 08 0 H                       |
| 73 MRBUA   | 8                      | 593  | CA CR F5                             |
| 65 ACABA   | 19                     | 131  | CR (C5 H7 02)3                       |
| CR+4 IV    | 74 ZAACA               | 407  | 129 BA2 CR 04                        |
| CR+4 VI    | 72 MRBUA               | 7    | 157 CR 02                            |
| CR+5 VI    | 67 STGBA               | 3    | 1 R3 VS V (FLUORIDES)                |
| CR+6 IV    | 68 CJCHA               | 46   | 935 K2 CR2 07                        |
| 70 ACABA   | 26                     | 222  | CR 03                                |
| 69 JCSIA   | 1969                   | 1857 | (HMH)2 CR 04                         |
| 69 ACABA   | 25                     | 1516 | AG2 CR2 07                           |
| 70 SPMDA   | 15                     | 930  | K2 CR 013                            |
| 70 AMNIA   | 55                     | 784  | P82 CR2 05                           |
| 70 ACASA   | 24                     | 3627 | NA2 CR3 08 0 H                       |
| 71 SPMDA   | 15                     | 820  | NA2 CR2 07.2 H2 0                    |
| 7          |                        |      |                                      |

[illegible]

Table 2 (cont.)

|           |      |      |            |           |              |                              |                        |      |
|-----------|------|------|------------|-----------|--------------|------------------------------|------------------------|------|
| 70 ACBCA  | 26   | 105  | BA3        | S14       | NB6          | D26                          |                        |      |
| 71 ACSAA  | 25   | 3347 | L1         | NB3       | 08           |                              |                        |      |
| 59 SPHCA  | 4    | 796  | LY         | YB1       | NB           | 04                           |                        |      |
| 73 JSSCA  | 4    | 150  | BI         | NB        | 04           |                              |                        |      |
| 66 ACSAA  | 20   | 72   | NB         | P         | 05           |                              |                        |      |
| 74 BUCFA  | 97   | 3    | NA3        | NB        | 04           |                              |                        |      |
| NB+5 VI   |      |      |            |           |              |                              |                        |      |
| 70 JSSCB  | 1    | 454  | NA2        | NB        | 011          |                              |                        |      |
| 71 JSSCB  | 3    | 89   | NA12       | NB        | 054          |                              |                        |      |
| 71 ACBCA  | 27   | 1610 | (NH4)3     | NB        | 0            | IC2 0413.H2 O                |                        |      |
| 75 ACBCA  | 31   | 673  | NB2        | 05        |              |                              |                        |      |
| ND+2 VII  |      |      |            |           |              |                              |                        |      |
| UNPUL     |      |      |            |           |              | NO 12                        |                        |      |
| ND+2 IX   |      |      |            |           |              | NO CL2, NO BR2               |                        |      |
| ND+3 VI   |      |      |            |           |              |                              |                        |      |
| 71 INDOCA | 10   | 922  | BA2        | NO        | MD           | 06                           |                        |      |
| 74 MRBUA  | 9    | 1661 | NO         | AL3       | BA           | 012                          |                        |      |
| ND+3 VII  |      |      |            |           |              |                              |                        |      |
| 69 JCPFA  | 50   | 86   | ND2        | MO3       | 012          |                              |                        |      |
| 71 JSSCB  | 3    | 458  | ND         | V         | 04           |                              |                        |      |
| 70 SPHCA  | 14   | 518  | R          | ND        | M2           | 08                           |                        |      |
| 70 ACBCA  | 26   | 1484 | ND2        | T12       | 07           |                              |                        |      |
| 70 ACSAA  | 24   | 3408 | ND4        | RE2       | 011          |                              |                        |      |
| 71 SPHDA  | 15   | 636  | ND2        | M         | 06           |                              |                        |      |
| 71 SPHCA  | 15   | 991  | ND4        | M5        | 015          |                              |                        |      |
| 74 MRBUA  | 9    | 129  | ND         | P5        | 014          |                              |                        |      |
| 74 ZAACA  | 403  | 1    | R3         | VS        | V            | (ND F3)                      |                        |      |
| 74 ACBCA  | 30   | 468  | ND         | P3        | 09           |                              |                        |      |
| ND+3 IX   |      |      |            |           |              |                              |                        |      |
| 70 ACSAA  | 24   | 2969 | ND2        | IC2       | 0413.10.H2 O |                              |                        |      |
| 71 SPHCA  | 29   | 2743 | ND2        | IC3       | 0413.10.H2 O |                              |                        |      |
| 73 ACSAA  | 27   | 2441 | ND2        | IC3       | H2           | 0413.10.H2 O                 |                        |      |
| 74 ZAACA  | 403  | 1    | R3         | VS        | V            | (ND F3)                      |                        |      |
| 73 ACSAA  | 27   | 2815 | ND2        | IC3       | H2           | 0413.10.H2 O                 |                        |      |
| 73 ACSAA  | 27   | 2973 | ND         | 04        | C            | 03                           |                        |      |
| 74 AMHIA  | 59   | 1277 | ND4        | MG2       | T13          | S14                          | O22                    |      |
| ND+3 XII  |      |      |            |           |              |                              |                        |      |
| 72 JSSCB  | 4    | 11   | NO         | AL        | 03           |                              |                        |      |
| NI+2 IV   |      |      |            |           |              |                              |                        |      |
| 61 JAPFA  | 32   | 685  | NI         | CR2       | 04           |                              |                        |      |
| 65 BSCFA  | 1965 | 1085 | SPINELS    |           |              |                              |                        |      |
| NI+2 V    |      |      |            |           |              |                              |                        |      |
| 66 INDOCA | 5    | 1200 | NI         | (DPH)2    |              |                              |                        |      |
| NI+2 V    |      |      |            |           |              |                              |                        |      |
| 67 BAPCA  | 15   | 47   | NI2        | P2        | 07           |                              |                        |      |
| NI+2 VI   |      |      |            |           |              |                              |                        |      |
| 74 AMHIA  | 59   | 486  | NI2        | S1        | 04           |                              |                        |      |
| 74 ACBCA  | 30   | 1686 | NI         | (PY N     | D16          | 1B F412                      |                        |      |
| 68 ZAACA  | 358  | 125  | NI         | SE        | 04           |                              |                        |      |
| 67 BAPCA  | 15   | 47   | NI2        | P2        | 07           |                              |                        |      |
| 70 ACBCA  | 26   | 1464 | R8         | NI        | F3           |                              |                        |      |
| 70 ZAACA  | 378  | 129  | SR2        | NI        | TE           | 04                           |                        |      |
| 70 JSSCB  | 2    | 416  | R8         | NI        | F3           |                              |                        |      |
| 71 PHSSA  | 438  | 125  | NI         | (O        | H12          |                              |                        |      |
| 70 REF    | 1    |      |            |           |              |                              |                        |      |
| 64 ACBCA  | 17   | 1481 | NI         | (C5       | MT           | 0212.2H2 O                   |                        |      |
| 73 ACBCA  | 29   | 2743 | NI         | (F6       | 0H2          | 0                            |                        |      |
| 63 ZKKA   | 118  | 291  | NI         | (H        | C            | 0                            | 012.2H2 O              |      |
| 74 JCPFA  | 61   | 852  | NI         | (C4       | 04           | 04.2H2 O                     |                        |      |
| 73 JCHLS  | 9    |      |            |           |              |                              |                        |      |
| 73 ACBCA  | 29   | 2304 | NI3        | V2        | 08           |                              |                        |      |
| NI+3 VI   |      |      |            |           |              |                              |                        |      |
| 74 ZAACA  | 405  | 167  | M2         | N1        | F6           |                              |                        |      |
| 71 CHDOCA | 272  | 2163 | HO         | NI        | 03           |                              |                        |      |
| NI+3 VI   |      |      |            |           |              |                              |                        |      |
| 54 JACSA  | 76   | 1499 | NA         | NI        | 02           |                              |                        |      |
| NI+4 VI   |      |      |            |           |              |                              |                        |      |
| 67 STGBA  | 3    | 1    | R3         | VS        | V            | (FLUORIDES)                  |                        |      |
| 74 JINCA  | 36   | 1561 | K2         | NI        | TE           | 04                           |                        |      |
| ND+2 VI   |      |      |            |           |              |                              |                        |      |
| 74 INDOCA | 13   | 2233 | ESTIMATED  |           |              |                              |                        |      |
| NP+3 VI   |      |      |            |           |              |                              |                        |      |
| 68 JINCA  | 30   | 823  | NP         | CL3       |              |                              |                        |      |
| NP+4 VI   |      |      |            |           |              |                              |                        |      |
| 67 INUCA  | 3    | 327  | ESTIMATED  |           |              |                              |                        |      |
| 74 CJCHA  | 52   | 2175 | R3         | VS        | V            |                              |                        |      |
| NP+6 VI   |      |      |            |           |              |                              |                        |      |
|           |      |      |            |           |              | R3 VS V (BA2 SR NP 06)       |                        |      |
| OH-1 III  |      |      |            |           |              |                              |                        |      |
| 71 AMHIA  | 56   | 1155 | MG6.6      | FE4       | S13          | O12 F O H, R10H-11(RF-11)+04 |                        |      |
| OH-1 III  |      |      |            |           |              |                              |                        |      |
| 71 AMHIA  | 56   | 1155 | MG6.6      | FE4       | S13          | O12 F O H, R10H-11(RF-11)+04 |                        |      |
| OH-1 IV   |      |      |            |           |              |                              |                        |      |
|           |      |      |            |           |              | R10H-11(RF-11)+04            |                        |      |
| OH-1 VI   |      |      |            |           |              |                              |                        |      |
|           |      |      |            |           |              | R10H-11(RF-11)+04            |                        |      |
| OS+4 VI   |      |      |            |           |              |                              |                        |      |
| 69 JCDOA  | 17   | 459  | OS         | 02        |              |                              |                        |      |
| 70 ACSAA  | 24   | 123  | OS         | 04        |              |                              |                        |      |
| OS+5 VI   |      |      |            |           |              |                              |                        |      |
| 71 JCSIA  | 1971 | 2789 | OS         | F5        |              |                              |                        |      |
| 74 SSCOA  | 14   | 357  | R3         | VS        | V            | (CD2 052 07)                 |                        |      |
| OS+6 VI   |      |      |            |           |              |                              |                        |      |
| 65 JINCA  | 2    | 79   | K          | OS        | F6           |                              |                        |      |
| OS+7 VI   |      |      |            |           |              |                              |                        |      |
|           |      |      |            |           |              | R3 VS V (PEROVSKITES)        |                        |      |
| OS+8 IV   |      |      |            |           |              |                              |                        |      |
|           |      |      |            |           |              | R3 VS V (PEROVSKITES)        |                        |      |
| OS+8 IV   |      |      |            |           |              |                              |                        |      |
| 66 ACSAA  | 20   | 395  | OS         | 04        |              |                              |                        |      |
| 73 ACBCA  | 29   | 1983 | OS         | 04        |              |                              |                        |      |
| 65 ACBCA  | 19   | 157  | OS         | 05        |              |                              |                        |      |
| 71 JCSIA  | 1971 | 1857 | OS(8+)     | -0        |              |                              |                        |      |
| PA+5 IV   |      |      |            |           |              |                              |                        |      |
| 72 ACBCA  | 28   | 2883 | CO2        | P2        | 07           |                              |                        |      |
| 68 CJCHA  | 46   | 605  | CO2        | P2        | 07           |                              |                        |      |
| 65 CJCHA  | 43   | 1159 | MO2        | P2        | 07           |                              |                        |      |
| 68 INDOCA | 7    | 1345 | CA2        | P2        | 07           |                              |                        |      |
| 71 BSCFA  | 1971 | 426  | 2R         | P2        | 07           |                              |                        |      |
| 70 ACBCA  | 26   | 1826 | M3         | P         | 04.1/2       | H2 O                         |                        |      |
| 71 NJMMA  | 1971 | 241  | SR         | AL3       | (P           | 0412 IO H15.H2 O             |                        |      |
| 69 ZKKA   | 130  | 148  | R          | ZR2       | (P           | 0413                         |                        |      |
| 71 ACBCA  | 27   | 2124 | NA3        | P         | 04.12H2 O    |                              |                        |      |
| 68 ACSAA  | 22   | 1822 | NA         | R2        | P1           | 012                          |                        |      |
| 68 ZKKA   | 127  | 21   | AL3        | P2        | 08.5H2 O     |                              |                        |      |
| 68 CJCHA  | 46   | 290  | LI         | FE        | 04           |                              |                        |      |
| 70 ACBCA  | 26   | 1826 | M3         | P         | 04           |                              |                        |      |
| 72 AMHIA  | 57   | 45   | NA45       | FE        | 35           | P                            | 04                     |      |
| 72 ACBCA  | 28   | 2005 | (H         | NH4)2     | M            | P                            | 04                     |      |
| 73 ACBCA  | 29   | 141  | LU         | P         | 04           |                              |                        |      |
| 71 ACBCA  | 27   | 2247 | CA         | 1H2       | P            | 0412.H2 U                    |                        |      |
| 73 ACBCA  | 29   | 2242 | AL         | P         | 04.2H2 O     |                              |                        |      |
| 71 ACSAA  | 25   | 512  | K          | H5        | (P           | 0412                         |                        |      |
| 70 JSSCB  | 1    | 120  | ZN2        | P2        | 07           |                              |                        |      |
| PA+5 V    |      |      |            |           |              |                              |                        |      |
| 67 JACSA  | 89   | 2268 | C23        | H29       | OS           | P                            |                        |      |
| 67 JACSA  | 89   | 2270 | C23        | H29       | OS           | P                            |                        |      |
| PA+5 VI   |      |      |            |           |              |                              |                        |      |
| 71 ZAACA  | 380  | 51   | P          | CL5       |              |                              |                        |      |
| 72 CCJDA  | 1972 | 676  | ET3        | M         | (C6          | HA                           | 0213 P                 |      |
| 74 ACBCA  | 29   | 246  | CALCULATED |           |              |                              |                        |      |
| PA+4 VI   |      |      |            |           |              |                              |                        |      |
| 67 INUCA  | 3    | 327  | R          | (PU+4)    |              |                              |                        |      |
| 74 CJCHA  | 52   | 2175 | R3         | VS        | V            |                              |                        |      |
| PA+5 VI   |      |      |            |           |              |                              |                        |      |
| 71 ACBCA  | 27   | 731  | R          | PA        | 03           |                              |                        |      |
| PA+5 IX   |      |      |            |           |              |                              |                        |      |
| 67 JCSIA  | 1967 | 1429 | K2         | PA        | F7           |                              |                        |      |
| PB+2 IV   |      |      |            |           |              |                              |                        |      |
| 68 ZKKA   | 126  | 98   | P8         | S1        | 03           |                              |                        |      |
| PB+2 VI   |      |      |            |           |              |                              |                        |      |
| 70 ACACB  | 26   | 501  | PB2        | 03        |              |                              |                        |      |
| PB+2 VII  |      |      |            |           |              |                              |                        |      |
| 69 ZKKA   | 128  | 213  | PB         | CA2       | S13          | 09                           |                        |      |
| 64 ACBCA  | 17   | 1539 | PB         | P2        | 06           |                              |                        |      |
| PB+2 VIII |      |      |            |           |              |                              |                        |      |
| 71 SPHCA  | 15   | 928  | PB         | M         | 04           |                              |                        |      |
| 64 ACBCA  | 17   | 1539 | PB         | P2        | 06           |                              |                        |      |
| 73 CJCHA  | 51   | 70   | PB2        | V2        | 07           |                              |                        |      |
| 72 MRBUA  | 7    | 1025 | B1         | TITANATES |              |                              |                        |      |
| PB+2 IX   |      |      |            |           |              |                              |                        |      |
| 67 ACBCA  | 22   | 744  | PB         | F2        |              |                              |                        |      |
| 73 CJCHA  | 51   | 70   | PB2        | V2        | 07           |                              |                        |      |
| 74 ZKKA   | 139  | 215  | PB         | C         | 03           |                              |                        |      |
| 74 CJCHA  | 52   | 2701 | PB         | V2        | 06           |                              |                        |      |
| PB+2 X    |      |      |            |           |              |                              |                        |      |
| 70 ZKKA   | 132  | 228  | PB3        | P2        | 08           |                              |                        |      |
| PB+2 XII  |      |      |            |           |              |                              |                        |      |
| 57 ACBCA  | 10   | 103  | PB         | (N        | O312         |                              |                        |      |
|           |      |      |            |           |              | R3 VS V (BA S                | 04)                    |      |
| 70 ZKKA   | 132  | 228  | PB3        | P2        | 08           |                              |                        |      |
| 71 INDOCA | 10   | 1264 | K2         | PB        | CU           | 1N                           | 0216                   |      |
| PB+4 IV   |      |      |            |           |              |                              |                        |      |
| 72 JCSIA  | 1972 | 2448 | R3         | VS        | V            | (NA4                         | PB                     | 04)  |
| PB+4 V    |      |      |            |           |              |                              |                        |      |
| 70 ZAACA  | 375  | 255  | R82        | PB        | 03           |                              |                        |      |
| PB+4 VI   |      |      |            |           |              |                              |                        |      |
| 65 ACBCA  | 26   | 501  | PB2        | 03        |              |                              |                        |      |
| 65 JINCA  | 27   | 1509 | PB3        | 04        |              |                              |                        |      |
| 74 CJCHA  | 52   | 2175 | R3         | VS        | V            |                              |                        |      |
| PD+4 VII  |      |      |            |           |              |                              |                        |      |
| 68 MRBUA  | 3    | 153  | PB         | 02        |              |                              |                        |      |
| PD+2 IV   |      |      |            |           |              |                              |                        |      |
| 67 INDOCA | 6    | 730  | PD         | (C6       | H5           | CH3                          | CH1C                   | 0212 |
| 68 JSTCA  | 9    | 166  | PD         | (IC6      | HS12         | CH                           | CH2                    | 0212 |
| PD+4 VI   |      |      |            |           |              |                              |                        |      |
| 68 MRBUA  | 3    | 699  | R3         | VS        | V            | (M2                          | PD2                    | 07)  |
| 73 INDOCA | 12   | 1726 | KE         | PD        | F11          |                              |                        |      |
| 61 JCSIA  | 1961 | 3728 | K2         | PD        | F6           |                              |                        |      |
| PM+3 VI   |      |      |            |           |              |                              |                        |      |
| PM+3 VIII |      |      |            |           |              |                              |                        |      |
| 74 ZAACA  | 403  | 1    | R3         | VS        | V            | (PM                          | F3)                    |      |
| PM+3 IX   |      |      |            |           |              |                              |                        |      |
| 74 ZAACA  | 403  | 1    | R3         | VS        | V            | (PM                          | F3)                    |      |
| PD+4 VI   |      |      |            |           |              |                              |                        |      |
| 74 CJCHA  | 52   | 2175 | R3         | VS        | V            |                              |                        |      |
| PD+4 VIII |      |      |            |           |              |                              |                        |      |
|           |      |      |            |           |              |                              | R3 VS V (FLUORITE)     |      |
| PR+3 VI   |      |      |            |           |              |                              |                        |      |
| 71 MRBUA  | 6    | 545  | R3         | VS        | V            | (PR2                         | MO3                    | 012) |
| PR+3 VIII |      |      |            |           |              |                              |                        |      |
| 70 SPHCA  | 15   | 28   | PR2        | M2        | 09           |                              |                        |      |
| 74 ZAACA  | 403  | 1    | R3         | VS        | V            | (PR                          | F3)                    |      |
| PR+3 IX   |      |      |            |           |              |                              |                        |      |
| 70 SPHCA  | 15   | 28   | PR2        | M2        | 09           |                              |                        |      |
| 59 ZKKA   | 112  | 362  | PR         | (C2       | H5           | S                            | 0413.2H2 O             |      |
| 74 ZAACA  | 403  | 1    | R3         | VS        | V            | (PR                          | F3)                    |      |
| PR+4 VI   |      |      |            |           |              |                              |                        |      |
| 72 ACBCA  | 26   | 956  | BA         | PR        | 03           |                              |                        |      |
| 75 ACBCA  | 31   | 971  | PR2        | 012       |              |                              |                        |      |
| 73 JSSCB  | 8    | 331  | R          | (PR+4)    |              |                              |                        |      |
| 74 CJCHA  | 52   | 2175 | R3         | VS        | V            |                              |                        |      |
| PT+2 IV   |      |      |            |           |              |                              |                        |      |
| 72 REF    | 5    |      |            |           |              |                              |                        |      |
| PT+2 V    |      |      |            |           |              |                              |                        |      |
| 69 JINCA  | 31   | 3803 | PT         | 02        |              |                              |                        |      |
| 74 CJCHA  | 52   | 2175 | R3         | VS        | V            |                              |                        |      |
| PT+2 VI   |      |      |            |           |              |                              |                        |      |
| 67 STGBA  | 3    | 1    | R3         | VS        | V            | (FLUORIDES)                  |                        |      |
| 67 JCSIA  | 1967 | 478  | KE         | PT        | F11          |                              |                        |      |
| PUR+3 VI  |      |      |            |           |              |                              |                        |      |
| 67 INUCA  | 3    | 327  | R          | (PU+3)    |              |                              |                        |      |
| 75 JINCA  | 37   | 743  | R          | (PU+3)    |              |                              |                        |      |
| PUR+4 VI  |      |      |            |           |              |                              |                        |      |
| 67 INUCA  | 3    | 327  | R          | (PU+4)    |              |                              |                        |      |
| 73 JSSCB  | 8    | 331  | R          | (PU+4)    |              |                              |                        |      |
| 74 CJCHA  | 52   | 2175 | R3         | VS        | V            |                              |                        |      |
| PUR+6 VI  |      |      |            |           |              |                              |                        |      |
|           |      |      |            |           |              |                              | R3 VS V (BA2 SR PU 04) |      |
| RB+1 VI   |      |      |            |           |              |                              |                        |      |
| 70 ZAACA  | 375  | 255  | R82        | PB        | 03           |                              |                        |      |
| RB+1 IX   |      |      |            |           |              |                              |                        |      |
| 74 ACBCA  | 30   | 1640 | R82        | S         | 04           |                              |                        |      |
| RB+1 XI   |      |      |            |           |              |                              |                        |      |
| 74 ACBCA  | 30   | 1640 | R82        | S         | 04           |                              |                        |      |
| RB+1 XII  |      |      |            |           |              |                              |                        |      |
| 70 ACBCA  | 26   | 1464 | R8         | NI        | F3           |                              |                        |      |
| 70 JSSCB  | 2    | 416  | R8         | NI        | F3           |                              |                        |      |
| 70 JSSCB  | 2    | 582  | R8         | NI        | F3           |                              |                        |      |
| RB+1 XIV  |      |      |            |           |              |                              |                        |      |
| 65 ACBCA  | 19   | 205  | RB         | U         | 02           | IN                           | 0312                   |      |
| RE+4 VI   |      |      |            |           |              |                              |                        |      |
| 68 INDOCA | 7    | 108  | LA4        | RE        | 019          |                              |                        |      |
| 74 CJCHA  | 52   | 2175 | R3         | VS        | V            |                              |                        |      |
| RE+5 VI   |      |      |            |           |              |                              |                        |      |
| 70 ACSAA  | 24   | 3406 | ND4        | RE2       | 011          |                              |                        |      |
| UNPUL     |      |      |            |           |              |                              |                        |      |

Table 2 (cont.)

|   |   |   |
|---|---|---|
| 72 ACBCA 28 956 BA T8 03  | 71 JINCA 33 2867 CR2 U 06                     | 69 PHSSA 32 K91 ZN FE2 04   |
| TC+5 VI 67 STBGA 3 1 R3 VS V (FLUORIDES)                          | 72 ACBCA 28 3609 U 02 0 H12                   | 73 ACSCA 27 1541 ZN S 03.2 1/2H2 U  |
| TC+7 IV 69 ACIEA 8 381 T62 07                                     | 73 ACBCA 29 7 U F6                            | 64 INDOA 3 245 ZN 0PMH2   |
| 71 ZAACA 380 146 T62 07   | U6+ VII 72 ACBCA 28 3609 U 03                 | ZN+2 V 70 JSSCB 1 120 ZN2 P2 07   |
| TE+4 IV 69 ACBCA 25 1551 H3 FE2 TE4 012 CL                        | U6+ VIII 69 ACBCA 25 787 CA U 04              | 73 CJCHA 51 1004 ZN2 V2 07  |
| 71 ACBCA 27 602 T1 TE3 08, 3N TE3 08, TE 02, HF TE3 08, ZR TE3 08 | 69 ACCRA 19 205 RB U 02 (IN 0313)             | 71 ANMIA 56 1147 ZN4 AS2 08 0 H12.2H2 0   |
| 71 ACBCA 27 608 U TE3 09  | V+2 VI UNPUS V F2                             | ZN+2 VI 65 CJCHA 43 1147 ZN2 P2 07  |
| TE+4 VI 61 ZKKA 116 345 TE 02                                     | V+3 VI 70 PRBBA 2 3771 V2 03                  | 68 SPHCA 13 127 ZN 04   |
| 71 ACBCA 27 602 M TE3 08  | 69 ACBCA 25 1354 V IC5 H7 0213                | 70 JSSCB 1 120 ZN2 P2 07  |
| 71 ACBCA 27 608 U TE3 09  | 69 ZAACA 369 306 M V2 04                      | 71 CJCHA 49 3056 ZN3 V2 08  |
| TE+6 IV 71 JCSCA 1971 1857 TE(+6)+0                               | 74 MRBBA 9 1091 UVO-99 CR0.0112 03            | 71 ANMIA 56 1147 ZN4 AS2 08 0 H12.2H2 0   |
| TE+6 VI 69 ZENBA 24 647 L16 TE 06                                 | 70 JCPCA 31 2569 V2 03                        | 73 ACSCA 27 1541 ZN S 03.2 1/2H2 0  |
| 70 NBUBA 5 109 M63 TE 06  | V4+ V 65 ACBCA 19 432 L1 V2 05                | 75 JSSCB 13 275 R3 VS V (M4 ZR 04)  |
| 69 ACSCA 23 3062 NA2 KA TE2 08 0 H12 IH2 0114                     | 61 JCPSA 35 55 V 0 IC5 H7 0212                | ZR+4 V 69 CCJDA 1969 727 K2 ZR 03   |
| 64 INDOA 3 634 K TE 0 10 H15.2H2 0                                | 73 ACBCA 29 269 CA V3 07                      | 70 JSSCB 2 410 K2 ZR 03   |
| 64 NATMA 51 552 K TE 0 H  | 73 ACBCA 29 1335 CA V4 09                     | ZR+4 VI 69 ACBCA 25 2658 ZR IH AS 0412.H2 0   |
| 66 ACSCA 20 2138 K4 TE2 06 0 H14.H2 0                             | V4+ VI 72 JSSCB 5 446 CU V 03                 | 69 ZAACA 371 306 L12 ZR 03  |
| 70 NATMA 57 393 M63 TE 06   | 61 JSSCB 6 419 V4 07                          | 70 JSSCB 1 478 K2 ZR2 05  |
| 70 ZAACA 378 129 SR2 NI TE 06                                     | 72 PRBBA 5 2541 V 02 CR                       | 68 ACSCA 22 1822 NA ZR2 P3 012  |
| 70 ACSCA 24 3178 TE 10 H16  | 74 ACBCA 30 2644 V3 07                        | 73 ACBCA 29 2294 L12 ZR F6  |
| 68 ACSCA 20 1535 TE F6  | 71 ACSCA 25 2675 V6 013                       | 71 ACBCA 27 1944 RB5 ZR F21   |
| 71 ACBCA 27 615 M63 TE 06   | 70 ACSCA 24 420 V02                           | 74 CJCHA 52 2175 R3 VS V  |
| 65 ZAACA 334 225 K TE 02 0 H13                                    | 74 PRBBA 10 490 V02                           | ZR+4 VII 69 ACBCA 25 2164 NA2 ZR F6   |
| 68 CHODA 267 1435 O2 TE 06  | V5+ IV 68 ACBCA 24 292 Y V 04                 | 70 ACBCA 26 417 IH M413 ZR F7   |
| 69 MOCBM 100 1809 AG2 TE 02 0 H14                                 | 68 CHPLB 2 47 ER V 04                         | 70 JACTA 53 126 ZR 02   |
| 71 BUFGA 94 172 TE 10 H16   | 67 ACSCA 25 250 H7 H2 07                      | 73 ACSCA 27 177 ZR4 0 H16 (CR 0415.H2 0   |
| 73 ACBCA 29 643 TE 06   | 70 ZKKA 131 161 BA3 (V 0412                   | 73 ACSCA 27 2614 ZR 10 H12 S 04.H2 0  |
| 73 ACBCA 29 956 H2 TE2 06   | 71 JSSCB 3 458 ND V 04                        | 71 ACBCA 27 1944 RB5 ZR F21   |
| 73 ACSCA 27 85 TE 10 H16  | 27 71 ACBCA 29 2259 CAZ V 04 CL               | ZR+4 VIII 69 ACBCA 25 1558 ZR2 IS 0414 IH2 018.6H2 0                                  |
| 74 ACBCA 29 2976 NA3 BE TH10 P45                                  | 71 CJCHA 49 1629 MG3 V2 08                    | 69 ACBCA 25 1566 ZR2 IS 0414 IH2 018.2H2 0  |
| 74 ACBCA 30 2095 IN H416 (TE M06 024) TE (H016 7H2 0              | 71 ACBCA 49 1629 MG3 V2 08                    | 69 ACBCA 25 1572 ZR2 IS 0414.5H2 0  |
|   | 72 JSSCB 4 29 FE V 04                         | 71 ANMIA 56 782 ZR 51 04  |
| TH+4 VI 74 CJCHA 52 2175 R3 VS V                                  | 73 CJCHA 51 1004 ZN2 V2 07                    | 63 INDOA 2 243 ZR IACAC14   |
| TH+4 VIII 71 ACBCA 27 629 K5 TH F9                                | 71 CJCHA 49 1629 MG3 V2 08                    | 63 INDOA 27 1944 RB5 ZR F21   |
| 71 ACBCA 27 2290 K7 TH F31  | 73 JSSCB 6 518 L13 V 04                       | 63 INDOA 2 250 NA4 ZR IC2 0414.3H2 0  |
| 74 ICHAA 8 273 K TH P3 010  | 72 CJCHA 50 3944 C03 V2 07                    |   |
| TH+4 IX 68 CCJDA 1968 990 IN H414 TH F8                           | 71 CJCHA 51 1004 ZN2 V2 07                    | HEF 1 G. E. BROWN, PH.D. THESIS, VIRGINIA   |
| 69 ACBCA 25 1958 IN H414 TH F8                                    | 73 ACBCA 29 141 Y V 04                        | POLYTECH. INST., UNIV. MICROFILMS, 78-498   |
| 68 CCACA 40 147 K TH2 P3 012                                      | 73 ACBCA 29 1338 CUS V2 010                   | REF 2 R.W.C. WYCKOFF, CRYSTAL STRUCTURES, WILEY, N.Y., 1965                           |
| 70 ICHAA 4 571 NA TM2 (P 0413                                     | 74 ACBCA 30 1678 NA V 03                      | REF 3 H.BARNIGHAUSEN ET AL., PROD. 10TH R.E. RES. CONF. CAREER, ARIZ. 1973, 490       |
| 71 ACBCA 27 1823 RB TH F13  | 74 ACBCA 30 1678 NA V 03                      | REF 4 C.BRANDLE, STEINFINK, PROD. 7TH R.E. RES. CONF., CORONADO, CALIF. OCT. 28, 1968 |
| 71 ACBCA 29 2976 NA3 BE TH10 P45                                  | 74 NJMMA 5 2110 CS IV 0413 0 H                | REF 5 R.D. SHANNON, U.S. PAT. 3,663,181, MAY 16, 1972                                 |
| 70 ACBCA 26 1185 K NA TH F6                                       | V4+ V 50 ACSCA 4 1119 V2 05                   | REF 6 W.H. BAUR, NITROGEN, HANDBOOK OF GEUECHEM, SPRINGER-VERLAG, N.Y., 1974          |
| 71 ACBCA 27 2279 IN H413 TH F7                                    | 71 RVCAZ 4 509 ND V 05                        | REF 7 A.W. SLEIGHT, U.S. PAT. 3,869,954, NOV. 19, 1974                                |
| TH+4 X 73 ACBCA 29 2687 TH IN 0314 (IG6 H513 P 012                | 74 ACBCA 30 2644 V3 07                        | UNPUB. H.BARNIGHAUSEN, PERSONAL COMMUNICATION   |
| TH+4 XI 60 ACBCA 20 842 TH IN 0314.5H2 0                          | 74 ACBCA 30 2644 V3 07                        | UNPUB. A.W. SLEIGHT, PERSONAL COMMUNICATION   |
| 66 ACBCA 20 836 TH IN 0314.5H2 0                                  | 70 CHODA 270 952 CA V2 06                     | UNPUB. C. CALVO, PERSONAL COMMUNICATION   |
| TH+4 XII 65 ACBCA 18 698 MG TH IN 0316.6H2 0                      | V4+ VI 50 ACSCA 4 1119 V2 05                  | UNPUB. C.T. PREWITT, PERSONAL COMMUNICATION   |
| TI+3 VI 73 JSSCB 6 213 TH 07                                      | 71 ACSCA 25 2675 V6 013                       | UNPUB. W.H. BAUR, PERSONAL COMMUNICATION  |
| 63 PHRVA 130 2230 T12 03  | 72 CJCHA 50 3619 MG V2 06                     | ACACB ACTA CRYST. SECT. A   |
| 74 JSSCB 9 255 T12 03   | 73 CJCHA 51 2184 K3 V 02 C2 04.3H2 0          | ACBCA ACTA CRYST. SECT. B   |
| 74 ACBCA 30 662 CS T1 15 0412.12H2 0                              | 73 ACBCA 29 1743 CU V2 06                     | ACSCA ACTA CRYST. SECT. C   |
| TI+4 IV 67 STBGA 3 1 R3 VS V (FLUORIDES)                          | V5+ VI 67 STBGA 3 1 R3 VS V (FLUORIDES)       | ACSCA ACTA CRYST. SECT. D   |
| 73 ACBCA 29 2009 BA2 T1 04  | M4+ IV 25 1704 K2 M 04                        | ACSCA ACTA CRYST. SECT. E   |
| 61 ACBCA 14 875 BA2 T1 04   | 69 ACBCA 15 636 ND2 M 06                      | ACSCA ACTA CRYST. SECT. F   |
| 71 JCSCA 1971 1857 T1(+4)+0                                       | 71 SPHCA 15 928 RB M 04                       | ACSCA ACTA CRYST. SECT. G   |
| 74 ZAACA 408 60 RB2 T1 03   | 72 ACBCA 28 3174 SN 04                        | ACSCA ACTA CRYST. SECT. H   |
| TI+4 V 68 ACBCA 24 1327 V2 T1 05                                  | 71 JCPCA 55 1093 SR M 04.8A M 04              | ACSCA ACTA CRYST. SECT. I   |
| TI+4 VI 70 ZKKA 131 278 V2 T12 07                                 | 71 JCSCA 1971 1857                            | ACSCA ACTA CRYST. SECT. J   |
| 71 ACBCA 27 635 NE M6 T1 F6                                       | 74 ACBCA 30 1872 NA2 M 04                     | ACSCA ACTA CRYST. SECT. K   |
| 71 JSSCB 3 340 T14 07   | 74 ACBCA 30 1878 AL2 IN 0413                  | ACSCA ACTA CRYST. SECT. L   |
| 70 ACBCA 28 336 BA T1 03  | M5+ V 74 ACBCA 30 2587 CA3 M 05 CL2           | ACSCA ACTA CRYST. SECT. M   |
| 64 ACBCA 17 240 CO T1 03  | M6+ VI 69 ACBCA 13 933 MG M 04                | ACSCA ACTA CRYST. SECT. N   |
| 71 JCPCA 55 3266 T1 02  | 69 SSCDA 7 1797 B12 M 06                      | ACSCA ACTA CRYST. SECT. O   |
| 72 CSCMC 1 1 BA T16 013   | 70 SPHCA 14 518 K ND IN 0412                  | ACSCA ACTA CRYST. SECT. P   |
| 72 ZKKA 136 273 T1 02   | 70 SPHCA 14 515 L12 FE M 0412                 | ACSCA ACTA CRYST. SECT. Q   |
| 74 ZKKA 139 103 K T1 P 05   | 70 SPHCA 15 28 PR2 M2 09                      | ACSCA ACTA CRYST. SECT. R   |
| 72 INDOA 11 2989 (T1 01C5 H7 021212                               | 70 ACBCA 26 1020 CU M 04                      | ACSCA ACTA CRYST. SECT. S   |
| 74 ICHAA 11 243 INH412 T1 01C2 0412.H2 0                          | 70 JSSCB 2 278 L1 FE M 0412                   | ACSCA ACTA CRYST. SECT. T   |
| 74 ACBCA 30 2894 BA T12 05  | 66 ACSCA 20 2698 M F6 IGAS1                   | ACSCA ACTA CRYST. SECT. U   |
| 74 CJCHA 52 2175 R3 VS V  | 72 ZENBA 27 203 SN M 04                       | ACSCA ACTA CRYST. SECT. V   |
| TI+4 VIII 66 JCSCA 1966 1496 T1 IN 0314                           | 71 SPHCA 15 991 ND4 M3 015                    | ACSCA ACTA CRYST. SECT. W   |
| TL+1 VI R3 VS V (MF)  | 74 JSSCB 10 5 FE2 M 06                        | ACSCA ACTA CRYST. SECT. X   |
| TL+1 VIII 75 ACBCA 31 365 TL N 03                                 | X ACBCA 30 2069 BA M 04                       | ACSCA ACTA CRYST. SECT. Y   |
| TL+3 IV 71 JCPCA 52 812 XE 04                                     | XE+0 IV 71 JCPCA 52 812 XE 04                 | ACSCA ACTA CRYST. SECT. Z   |
| 71 ZAACA 381 129 L15 TL 04  | 71 JCSCA 1971 1857 XE(+8)+0                   |   |
| 71 ZAACA 396 113 SR4 TL2 07                                       | XE+0 VI 64 INDOA 3 1412 NA4 XE 06.0H2 0       |   |
| 71 ZAACA 405 197 BA2 TL2 05                                       | 64 INDOA 3 1417 NA4 XE 06.0H2 0               |   |
| TL+3 VI 68 ZKKA 126 143 TL2 03                                    | Y+3 VI 67 ACBCA 22 354 V2 BE 04               |   |
| 74 ZAACA 405 197 BA2 TL2 05                                       | 68 ZAACA 358 138 SR Y2 04                     |   |
| 75 ZAACA 412 37 RB TL F4  | 67 SPHCA 11 583 NA Y 51 04                    |   |
| TL+3 VIII 72 ZAACA 393 223 TL F3                                  | 69 ACBCA 25 2140 Y2 03                        |   |
| TM+2 VI UNPUB TM 12   | 71 SPHCA 15 806 Y2 51 05                      |   |
| TM+2 VII UNPUB TM CL2, TM BRZ                                     | 71 JCSCA 1974 229 C66 H72 13 N12 06 Y         |   |
| TM+2 VIII 63 PHSSA 3 K446 TM2 03                                  | Y+3 VII 68 INDOA 7 1777 YIC65C0CCH313.H20     |   |
| TM+3 VIII 70 SSCDA 8 1749 TM3 FE5 012                             | Y4+ VIII 68 ACBCA 24 292 Y V 04               |   |
| 74 ZAACA 403 1 K3 VS V (TM F3)                                    | 57 ACBCA 10 239 Y3 FE5 012                    |   |
| TM+3 IX 74 ZAACA 403 1 K3 VS V (TM F3)                            | 68 SPHCA 12 1095 K Y ND2 08                   |   |
| UN+3 VI 74 ZAACA 403 1 K3 VS V (TM F3)                            | 69 SPHCA 13 420 K Y W2 08                     |   |
| UN+3 VII 68 JINCA 30 823 R (U+3)                                  | 70 ZKKA 131 278 V2 T12 07                     |   |
| UN+3 VIII 73 JSSCB 8 331 R3 VS V                                  | 67 ACBCA 23 939 Y T4 04                       |   |
| 67 CJCHA 52 2175 R3 VS V  | 74 ZAACA 403 1 R3 VS V (Y F3)                 |   |
| UN+3 IX 70 ACBCA 26 38 IN H414 U F6                               | Y+3 IX 69 ZKKA 112 362 Y IC2 H5 S 0413.9H2 0  |   |
| 73 ACBCA 29 1442 U CL4  | 74 ZAACA 403 1 R3 VS V (Y F3)                 |   |
| UN+3 X 69 ACBCA 25 1919 K U2 F6                                   | YB+2 VI 74 ZAACA 386 221 YB BR2 YB 12         |   |
| 69 ACBCA 25 2103 K2 U F6  | YB+2 VII 74 ZAACA 386 221 YB CL2              |   |
| 71 ACBCA 27 245 CS U6 F25   | 74 ACBCA 386 221 YB BR2                       |   |
| 72 CS U2 F9   | YB+2 VIII 74 ACBCA 386 221 YB F2              |   |
| 74 ACBCA 30 1906 B - NHA U F5                                     | YB+2 IX 70 SPHCA 14 854 YB2 S1 05             |   |
| UN+3 XI 67 ACBCA 23 805 CS U F6                                   | 70 ACBCA 26 1020 CU M 04                      |   |
| 70 JINCA 32 3701 NA U 03  | 70 ZAACA 377 70 CA YB2 04, SR YB2 04          |   |
| 65 BUFGA 80 214 U CR 04   | 74 ACBCA 30 1857 YB P3 09                     |   |
| 67 BUFGA 50 257 U FE 04   | YB+3 VII 70 SPHCA 14 854 YB2 S1 05            |   |
| UN+3 XII 73 SPHCA 18 323 U2 RD 08                                 | 69 INDOA 8 22 YB IC5 H7 0213 (H2 0)           |   |
| UN+3 VI 68 ACBCA 24 967 CU U 04                                   | 69 INDOA 8 29 YB IC5 H7 0213 (H2 0) 1/2 C6 H6 |   |
| 69 ACBCA 25 787 SR U 04, BA U 04, CAZ U 05                        | YB+3 VIII 9 1096 YB L1 F4                     |   |
| UN+3 VII 68 ACBCA 25 787 SR U 04, BA U 04, CAZ U 05               | 70 SSCDA 8 1745 YB3 FE5 012                   |   |
| UN+3 VIII 68 ACBCA 25 787 SR U 04, BA U 04, CAZ U 05              | 74 MRBBA 9 179 YB P5 014                      |   |
| UN+3 IX 68 ACBCA 25 787 SR U 04, BA U 04, CAZ U 05                | 74 ZAACA 403 1 R3 VS V (YB F3)                |   |
| UN+3 X 68 ACBCA 25 787 SR U 04, BA U 04, CAZ U 05                 | YB+3 IX 74 ZAACA 403 1 R3 VS V (YB F3)        |   |
| UN+3 XI 68 ACBCA 25 787 SR U 04, BA U 04, CAZ U 05                | ZN+4 68 SPHDA 12 987 NA2 ZN2 S12 07           |   |
| UN+3 XII 68 ACBCA 25 787 SR U 04, BA U 04, CAZ U 05               | 69 ACBCA 25 1233 ZN 03                        |   |

compounds to be slightly larger than those of the  $\text{Eu}^{2+}$  compounds. This difference was assumed to exist for all  $\text{Sr}^{2+}$  and  $\text{Eu}^{2+}$  coordinations. Because compounds of  $\text{Am}^{2+}$  and  $\text{Sr}^{2+}$  have similar cell volumes, the radius of  $\text{Am}^{2+}$  was made equal to that of  $\text{Sr}^{2+}$ .

Wolfe & Newnham (1969) studied  $\text{Bi}_{4-x}\text{RE}_x\text{Ti}_3\text{O}_{12}$  and concluded that  $\text{Bi}^{3+}$  and  $\text{La}^{3+}$  have nearly equal radii. From a study of  $\text{BiTaO}_4$  Sleight & Jones (1975) have concluded that although  $\text{Bi}^{3+}$  and  $\text{La}^{3+}$  have essentially equal radii, the size of  $\text{Bi}^{3+}$  depends on the degree of the  $6s^2$  lone-pair character. When  $\text{BiTaO}_4$  transforms from a structure where the lone-pair character is dominant to the  $\text{LaTaO}_4$  structure, it undergoes a volume reduction. Table 3 shows a comparison of isotypic  $\text{Bi}^{3+}$  and  $\text{La}^{3+}$  compounds where the lone-pair character of  $\text{Bi}^{3+}$  is (1) constrained and (2) dominant. Bi pyrochlores such as  $\text{Bi}_2\text{Ru}_2\text{O}_7$ ,  $\text{Bi}_2\text{Ir}_2\text{O}_7$  and  $\text{Bi}_2\text{Pt}_2\text{O}_7$  were omitted from the table because no corresponding La pyrochlore exists, but they have unit-cell volumes close to those of the Sm or Nd pyrochlores and thus have smaller volumes than those of La. When  $\text{Bi}^{3+}$  is forced into high symmetry, a  $\text{Bi}^{3+}$  compound has a smaller volume than that of  $\text{La}^{3+}$ , but when the lone-pair character is dominant, the  $\text{Bi}^{3+}$  compound is distorted and  $\text{Bi}^{3+}$  and  $\text{La}^{3+}$  compounds have approximately equal volumes. This behavior was also noted in the highly symmetric garnet structure where the hypothetical  $\text{Bi}_3\text{Fe}_3\text{O}_{12}$  was estimated to have cell dimensions between those of the hypothetical  $\text{Nd}_3\text{Fe}_3\text{O}_{12}$  and  $\text{Pr}_3\text{Fe}_3\text{O}_{12}$  (Geller, Williams, Espinosa, Sherwood & Gilleo, 1963). For practical purposes,  $\text{Bi}^{3+}$  is listed as slightly smaller than  $\text{La}^{3+}$  but this dependence on lone-pair character must be kept in mind when comparing the volumes of  $\text{Bi}^{3+}$  and  $\text{La}^{3+}$  compounds. Similar behavior may also exist for  $\text{Pb}^{2+}$  and  $\text{Sr}^{2+}$ , but this relationship was not investigated.

Table 3. Cell volumes of isotypic  $\text{Bi}^{3+}$  and  $\text{La}^{3+}$  compounds

(a) Lone pair character of  $\text{Bi}^{3+}$  constrained

| Compound                      | Cell volume | Ratio |
|-------------------------------|-------------|-------|
| $\text{BiLi}(\text{MoO}_4)_2$ | 314.7       | 0.96  |
| $\text{LaLi}(\text{MoO}_4)_2$ | 328.7       |       |
| $\text{BiNa}(\text{MoO}_4)_2$ | 320.5       |       |
| $\text{LaNa}(\text{MoO}_4)_2$ | 332.1       | 0.97  |
| $\text{BiOF}$                 | 87.6        |       |
| $\text{LaOF}$                 | 97.7        |       |
| $\text{BiOCl}$                | 110.7       | 0.95  |
| $\text{LaOCl}$                | 116.8       |       |
| $\text{BiOBr}$                | 123.8       |       |
| $\text{LaOBr}$                | 126.4       | 0.98  |
| $\text{BiPO}_4$               | 293.0       |       |
| $\text{LaPO}_4$               | 304.7       |       |

(b) Lone pair character of  $\text{Bi}^{3+}$  dominant

|                                    |                       |      |
|------------------------------------|-----------------------|------|
| $\text{Bi}_2\text{MoO}_6$          | 268.5 ( $\times 8$ )  | 1.00 |
| $\text{La}_2\text{MoO}_6$          | 267.3                 |      |
| $\text{BiFeO}_3$                   | 62.49 ( $\times 6$ )  | 1.03 |
| $\text{LaFeO}_3$                   | 60.77 ( $\times 4$ )  |      |
| $\text{Bi}_2\text{Sn}_2\text{O}_7$ | 1219.9 ( $\times 8$ ) | 1.00 |
| $\text{La}_2\text{Sn}_2\text{O}_7$ | 1225.3                |      |

A similar study of relative cell volumes of isotypic compounds involving the pairs  $\text{Cu}^+-\text{Li}^+$ ,  $\text{Ag}^+-\text{Na}^+$ ,  $\text{Tl}^+-\text{Rb}^+$ , and  $\text{Pb}^{2+}-\text{Sr}^{2+}$  was used to obtain more reliable estimates of the radii of  $\text{Cu}^+$ ,  $\text{Ag}^+$ ,  $\text{Tl}^+$ , and  $\text{Pb}^{2+}$  (Shannon & Gummerman, 1975).

The nature of  $\text{Sn}^{2+}$ ,  $\text{NH}_4^+$ , and  $\text{H}^-$  made it impossible to define their ionic radii. The coordination of  $\text{Sn}^{2+}$  by oxygen or fluorine is always extremely irregular,\* leading to average distances which depend on the degree of distortion. Since this distortion varies widely from one compound to another, it is not meaningful to define an ionic radius.

Khan & Baur (1972) derived an apparent radius of the  $\text{NH}_4^+$  ion by analyzing the N-O distances in a large number of ammonium salts. They concluded that  $\text{NH}_4^+$  has an octahedral radius of 1.61 Å, between that of  $\text{Rb}^+$  (1.52 Å) and  $\text{Cs}^+$  (1.67 Å). Alternatively, cell volumes of  $\text{NH}_4^+$  and  $\text{Rb}^+$  fluorides, chlorides, bromides, iodides and oxides may be compared. This leads to the conclusion that  $\text{NH}_4^+$  is not significantly different in size from  $\text{Rb}^+$ . No explanation is offered for this inconsistency and therefore the radius of  $\text{NH}_4^+$  is not included.

The radius of the hydride ion,  $\text{H}^-$ , has been the subject of some controversy. A number of different radii have been proposed: 2.08 (Pauling, 1960); 1.40 (Gibb, 1962); and 1.53 Å (Morris & Reed, 1965). Gibb studied interatomic distances in many hydrides and concluded that good agreement between observed and calculated distances could be obtained using  $r(\text{VIH}^-) = 1.40$  Å if corrected for cation and anion coordination. The value of  $r(\text{IVH}^-)$  was taken to be 1.22 Å.

Morris & Reed (1965) concluded that differences in observed distances in hydrides were caused by the large  $\text{H}^-$  polarizability. Because of such wide variations in the apparent  $\text{H}^-$  radius, it was omitted. However, an explanation for the variations based on covalence differences will be discussed later.

\* Although cell dimensions of  $\text{Sn}_2\text{M}_2\text{O}_7$  pyrochlores were used in SP 69 to derive  $r(\text{VIIISn}^{2+})$ , Stewart, Knop, Meads & Parker (1973) and Birchall & Sleight (1975) recently found that the pyrochlore A site in  $\text{Sn}_2\text{Ta}_2\text{O}_7$  is not fully occupied. Thus, even this example of apparently regular  $\text{Sn}^{2+}$  polyhedra is not valid.

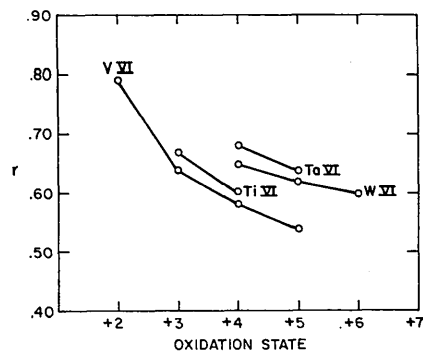


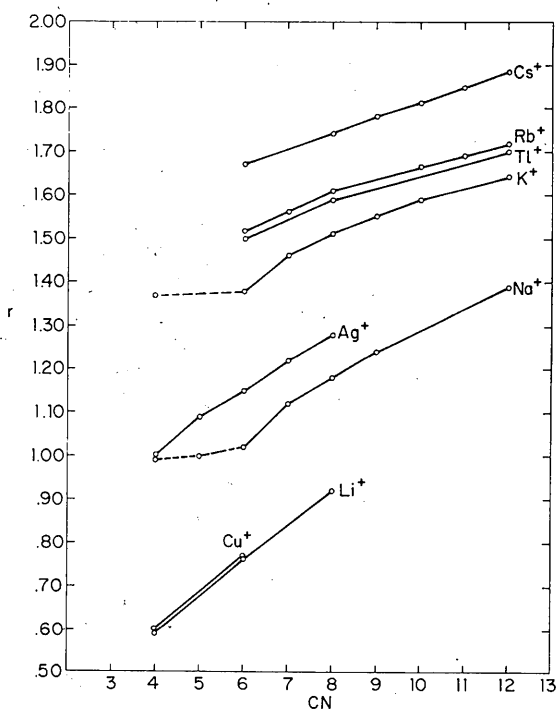
Fig. 1. Effective ionic radius (Å) vs oxidation state.



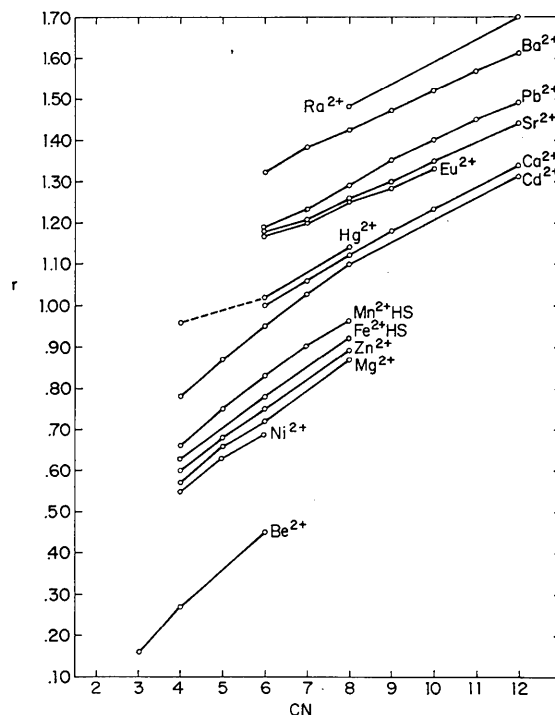
## Results and discussion

In Table 1 two sets of radii are included. The first is a set of traditional radii based on  $r(\text{VI}\text{O}^{2-}) = 1.40 \text{ \AA}$ . The

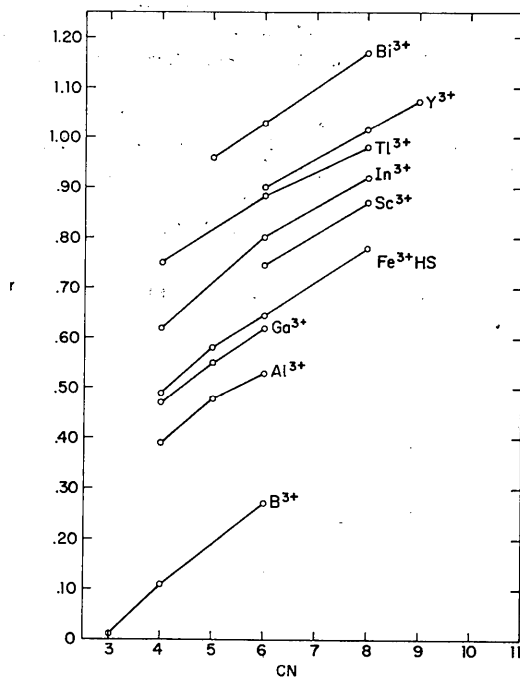
other set is based on  $r(\text{VI}\text{O}^{2-}) = 1.26$  and  $r(\text{VI}\text{F}^-) = 1.19 \text{ \AA}$ , and corresponds to crystal radii as defined by Fumi & Tosi (1964). As pointed out in SP 69, crystal radii differ from traditional radii only by a constant factor



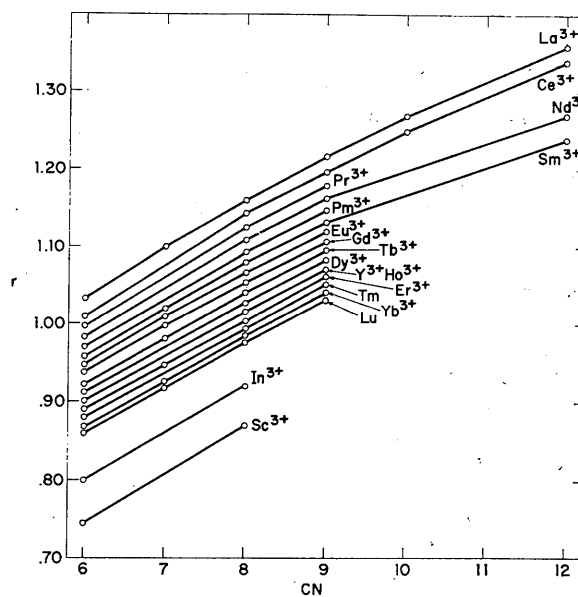
(a)



(b)

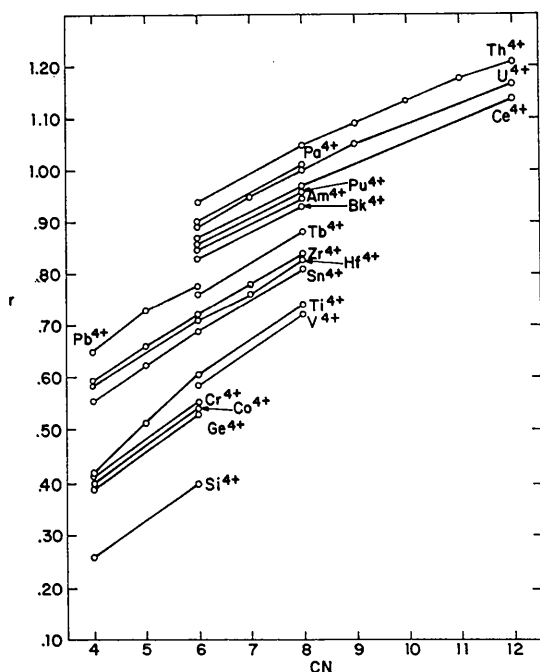


(c)



(d)

Fig. 2. (a)–(e) Effective ionic radius ( $\text{\AA}$ ) vs CN for some common cations.



(e)

Fig. 2. (cont.)

of 0.14 Å. Although their inclusion in Table 1 may seem superfluous, it is felt that crystal radii correspond more closely to the physical size of ions in a solid. They should be used, for example, in discussions of closest packing of spheres, structure field maps (Muller & Roy, 1974), and diffusion in solids (Flygare & Huggins, 1973). Traditional radii have been retained because of their familiarity to crystal chemists and physicists. They will probably continue to be used for comparison of unit-cell volumes and interatomic distances. In the table, the ion is followed by electron configuration (EC), coordination number (CN), spin state (SP), crystal radius (CR), and effective ionic radius (IR), and in the last column, a symbol indicating the derivation of the radii and their reliability. Those with a question mark are doubtful because of: uncertainty in CN, or deviation from radii *vs* CN, or radii *vs* valence plots. Where at least five structural determinations resulted in radii differing by no more than  $\pm 0.01$  Å, the values are marked with an asterisk.

When the choice of a radius was influenced by any of the various correlations described earlier, it is indicated by the following: *R* – from  $r^3$  *vs* unit cell volume plots; *C* – calculated from bond length–bond strength equations; *E* – estimated from one or more plots of *r vs* valence, *r vs* CN, and *r vs* cell volume. *E* implies poor or nonexistent structural data. Radii in this category include  $^{VI}\text{Fe}^{2+}\text{LS}$ ,  $^{VI}\text{Mn}^{2+}\text{LS}$ ,  $^{VI}\text{Cr}^{2+}\text{LS}$ ,  $^{VI}\text{V}^{2+}$ ,  $^{VI}\text{Ni}^{3+}\text{HS}$ ,  $^{VI}\text{Ir}^{3+}$ ,  $^{VI}\text{Mo}^{3+}$ ,  $^{VI}\text{Ta}^{3+}$ ,  $^{VI}\text{Pa}^{3+}$ ,  $^{VI}\text{Ta}^{4+}$ ,  $^{IV}\text{Pb}^{4+}$ ,  $^{VI}\text{Ir}^{5+}$ ,  $^{VI}\text{Os}^{5+}$ ,  $^{VI}\text{Re}^{5+}$ ,  $^{VI}\text{Pu}^{5+}$ ,  $^{VI}\text{Bi}^{5+}$ ,

$^{VI}\text{Os}^{6+}$ ,  $^{VI}\text{Re}^{6+}$ , and  $^{VI}\text{Os}^{7+}$ . The symbol *A* means that Ahrens (1952) ionic radius was used whereas *P* means Pauling's (1960) crystal radius was used. The symbol *M* means that the radius was derived from a compound having metallic conductivity. Distances calculated from these radii may be too small for use in compounds having localized electrons. (See discussion *Effects of electron delocalization*.)

In addition, the sources of the radii are indicated in Table 2.

Fig. 2(a)–(e) shows that *r*–CN plots are reasonably regular. Notable exceptions are  $^{IV}\text{Na}^+$ ,  $^{V}\text{Na}^+$ , and  $^{IV}\text{K}^+$ . It is apparent that Na–O and K–O distances do not decrease as much as anticipated from the *r*–CN curve\* when the CN falls below six. Typical distances and corresponding radii in Table 4 show that Na–O distances in four-coordination are only slightly less than in six-coordination. The reduction in interatomic distances is caused primarily by the decreased repulsive forces due to fewer ligands according to the expression of Pauling (1960):

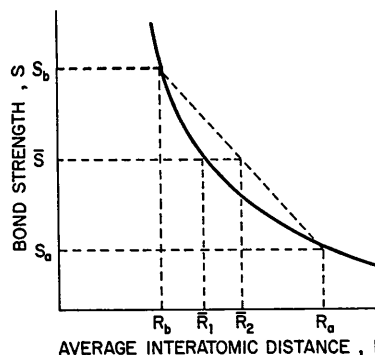
$$\frac{R_{\text{CsCl}}}{R_{\text{NaCl}}} = \left[ \frac{A_{\text{NaCl}}}{A_{\text{CsCl}}} \frac{B_{\text{CsCl}}}{B_{\text{NaCl}}} \right]^{1/(n-1)}$$

where *R*=interatomic distance, *A*=Madelung constant, *B*=the cation CN and *n*=Born repulsion coefficient. It appears that this equation is not valid for four-coordinated  $\text{Na}^+$  or  $\text{K}^+$ .

There are a few small irregularities in *r*–CN plots probably caused by poor or insufficient data, *e.g.* curves for  $\text{Ti}^{3+}$  *vs*  $\text{Y}^{3+}$ . The differences in slopes of  $\text{Ti}^{4+}$  *vs*  $\text{Cr}^{4+}$  and  $\text{V}^{5+}$  *vs*  $\text{As}^{5+}$  are probably caused by  $\text{Ti}^{4+}$ –O and  $\text{V}^{5+}$ –O octahedra being generally more distorted, which leads to greater average interatomic distances.

It is also interesting to compare distances in square planar coordination *versus* tetrahedral coordination. Radii of square planar  $\text{Cu}^{2+}$  and  $\text{Ag}^+$  are equal to or slightly greater than corresponding tetrahedral radii, consistent with the trend anticipated from anion

\* Extrapolation of the Na curve gives  $r(^{IV}\text{Na}^+)=0.90$  Å.

Fig. 3. Typical bond length *vs* bond strength plot.

repulsion effects. A similar comparison with  $\text{Fe}^{2+}$  and  $\text{Ni}^{2+}$  cannot be made because of electron distribution changes from tetrahedral to square planar coordination.

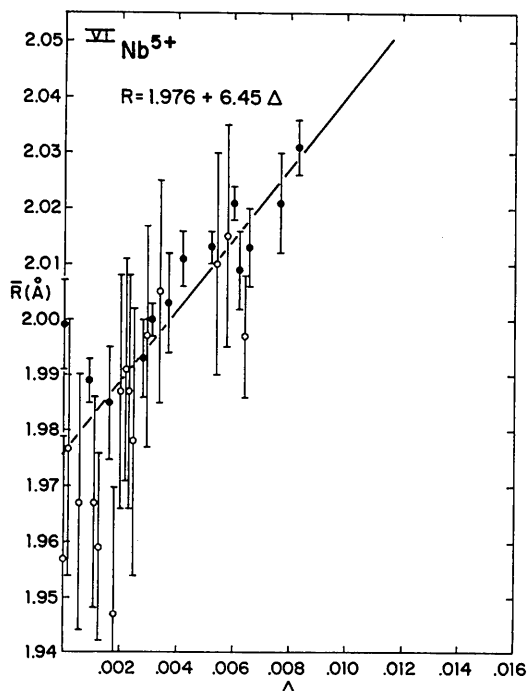


Fig. 4. Mean  $\text{Nb}^{5+}$ -O bond length *vs* distortion. Vertical bars represent average e.s.d.'s quoted by the authors. Solid circles represent more accurate data.

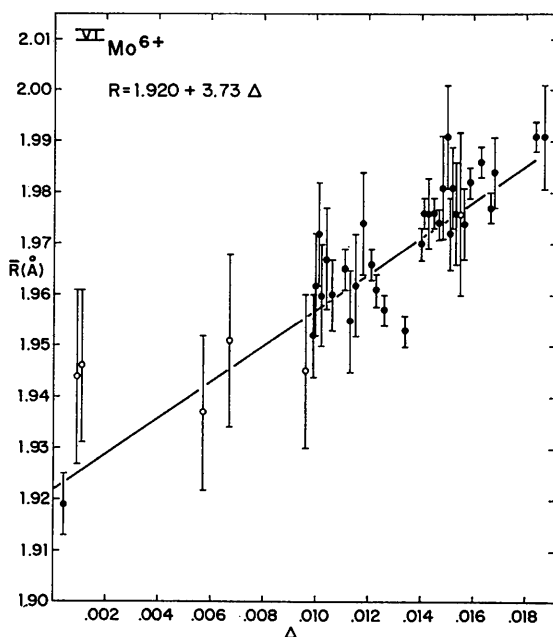


Fig. 5. Mean  $\text{Mo}^{6+}$ -O bond length *vs* distortion.

Table 4. *Interatomic distances in some compounds containing tetrahedral and octahedral  $\text{Na}^+$*

| Compound   | $\bar{R}$ (Å) | $r$ (Å) | Reference         |
|--|---------------|---------|-------------------|
| (a) $\text{IVNa}^+$  |               |         |                   |
| $\text{Na}_2\text{O}$  | 2.40          | 1.02    |                   |
| $\text{Na}_3\text{P}_3\text{O}_{10}$   | 2.37          | 0.99    | 60 ACCRA 13 263   |
| $\text{NaOH} \cdot \text{H}_2\text{O}$   | 2.36          | 1.00    | 57 ACCRA 10 462   |
| $\text{Na}_6\text{ZnO}_4$  | 2.39          | 0.99    | 69 ZAACA409 69    |
| Mean   | 2.38          | 1.00    |                   |
| (b) $\text{VI Na}^+$   |               |         |                   |
| $\text{Na}_2\text{WO}_4$   | 2.38          | 1.00    | 74 ACBCA 30 1872  |
| $\text{NaC}_6\text{O}_7\text{H}_7$   | 2.37          | 1.01    | 65 ACCRA 19 561   |
| $\text{Na}_4\text{Sn}_2\text{Ge}_4\text{O}_{12}(\text{OH})_4$                        | 2.39          | 1.02    | 70 ACSAA 24 1287  |
| $\text{Na}_2\text{P}_2\text{O}_7 \cdot 10\text{H}_2\text{O}$                         | 2.48          | 1.10    | 64 ACCRA 17 672   |
| $\text{NaHCO}_3$   | 2.44          | 1.06    | 65 ACCRA 18 818   |
| $\text{Na}_2\text{B}_4\text{O}_6(\text{OH})_2 \cdot 3\text{H}_2\text{O}$             | 2.41          | 1.04    | 67 SCIEA 154 1453 |
| $\text{Na}_4\text{P}_4\text{O}_{12} \cdot 4\text{H}_2\text{O}$                       | 2.415         | 1.05    | 61 ACCRA 14 555   |
| $\text{NaAl}(\text{SO}_4)_2 \cdot 12\text{H}_2\text{O}$                              | 2.45          | 1.10    | 67 ACCRA 22 182   |
| $\text{NaB}(\text{OH})_4 \cdot 2\text{H}_2\text{O}$                                  | 2.460         | 1.09    | 63 ACCRA 16 1233  |
| $\text{NaU acetate}$   | 2.375         | 1.025   | 59 ACCRA 12 526   |
| $\text{C}_{10}\text{H}_{13}\text{N}_5\text{NaO}_6\text{P} \cdot 6\text{H}_2\text{O}$ | 2.406         | 1.046   | 75 ACBCA 31 19    |
| Mean   | 2.42          | 1.05    |                   |

### Factors affecting mean interatomic distances

Additivity of radii to give mean interatomic distances is not so important to the synthetic chemist who is primarily interested in ionic radii for predicting substitution in crystal structures. Crystallographers and physicists, however, are concerned with comparing calculated and experimental interatomic distances and predicting distances, *e.g.* for distance least-squares (DLS) structure refinements (Baur, 1972; Tillmanns, Gebert & Baur, 1973; Dempsey & Strens, 1975). The effective ionic radii in Table 1 can be used to reproduce moderately well most average interatomic distances in oxides and fluorides. However, certain deviations do occur. Some of these are unexplained but others can be attributed to (1) polyhedral distortion, (2) covalence, (3) partial occupancy of cation sites, or (4) electron delocalization.

#### 1. Polyhedral distortion

To see the effects of polyhedral distortion consider the relationship between bond length ( $R$ ) and Pauling bond strength ( $s$ ) (Brown & Shannon, 1973). The analytical expression  $s = s_0(R/R_0)^{-N}$ , where  $s_0$  is an ideal bond strength associated with  $R_0$ , and  $R_0$  and  $N$  are fitted parameters, was evaluated for cation-oxygen pairs for the first three rows of the periodic table. Using these relationships, the sums of bond strengths about cations and anions were found to equal the valences with a mean deviation of about 5%. Accepting the approximate validity of Pauling's second rule,  $p = \sum s$  where  $p$  = valence, it is possible to derive the effects of distortion of various polyhedra on their mean bond distances. Fig. 3 shows a typical  $R$ - $s$  curve. An undistorted octahedron results in an average bond strength  $\bar{s}$  and a mean distance  $\bar{R}_1$ . A distorted octahedron with three bonds of length  $R_a$  and three of length  $R_b$  results in the same average bond strength,  $\bar{s}$ , but a mean distance  $\bar{R}_2 > \bar{R}_1$ .

The effects of distortion on mean bond lengths in numerous polyhedra have been determined. Although distortions in tetrahedra are not as important as in octahedra, they can contribute to variations in mean tetrahedral distances (Baur, 1974; Hawthorne, 1973). Strongly distorted octahedra like those containing  $V^{5+}$ ,  $Cu^{2+}$ , and  $Mn^{3+}$  show a significant variation in mean distance with distortion,  $\Delta^*$  (Brown & Shannon, 1973; Shannon & Calvo, 1973a; Shannon, Gurnerman & Chenavas, 1975). Octahedra containing  $Mg^{2+}$ ,  $Zn^{2+}$ ,  $Co^{2+}$ , and  $Li^+$  are generally less distorted than those of  $V^{5+}$ ,  $Cu^{2+}$ , and  $Mn^{3+}$  and show a less pronounced dependence on mean bond length (Brown & Shannon, 1973).

The effects of distortion on mean bond lengths in  $Nb^{5+}$ -O and  $Mo^{6+}$ -O octahedra are illustrated in Figs. 4 and 5. Tables 5 and 6 list the data used to derive the figures.

Table 7 lists the results of linear regression analyses of mean bond length on distortion for all octahedra studied. It is clear from Fig. 4 that undistorted  $Nb^{5+}$  octahedra in pyrochlores have a distinctly smaller mean value than in compounds like  $NbOPO_4$ ,  $CaNb_2O_6$ , and  $Na_3NbO_4$ . Most of the accurately refined molybdates have relatively distorted octahedra. However, certain ordered perovskites with no octahedral distortion such as  $Ba_2CaMoO_6$  would be expected to have much smaller mean  $Mo^{6+}$ -O distances than a typical molyb-

date. In fact, the  $Mo^{6+}$ -O octahedra in  $Mo_2(O_2C_6Cl_4)_6$  with a very small distortion have the short mean distance of 1.919 Å.

Table 7 also lists the results of regression analyses for  $Ta^{5+}$ -O and  $W^{6+}$ -O octahedra but they are only approximate because of the scarcity of accurate structural data. Analysis of  $Ti^{4+}$ -O octahedra was unsuccessful because of scatter in the data. Distances in  $Ba_6Ti_{17}O_{40}$  (Tillmanns & Baur, 1970) and  $BaTiO_3$  (Evans, 1951) deviated significantly from a linear relation.

Relations between mean distance and distortion should be particularly useful to help determine oxidation states in mixed valence compounds with such combinations as  $Mo^{5+}$ - $Mo^{6+}$ ,  $W^{5+}$ - $W^{6+}$ ,  $V^{4+}$ - $V^{5+}$ ,  $Nb^{4+}$ - $Nb^{5+}$  and  $Mn^{3+}$ - $Mn^{4+}$ . Such considerations helped rationalize Mn-O distances in  $NaMn_7O_{12}$  and the mineral pinakolite (Shannon, Gurnerman & Chenavas, 1975).

The radii in Table 1 are generally derived for an average degree of distortion. Thus, interatomic distances calculated from these radii may be inaccurate if the distortion in a particular compound is much less or greater than usual. This applies particularly to cations whose polyhedra frequently show a large distortion, e.g.  $Mo^{6+}$ ,  $Nb^{5+}$ ,  $V^{5+}$ ,  $Ba^{2+}$ , and the alkali ions.

## 2. Effects of partial occupancy of cation sites on mean cation-anion distances

In compounds with partially occupied sites, abnormally large cation-anion distances are usually found, as expected if the anions surrounding unoc-

\* Octahedral distortion is defined by  $\Delta = \frac{1}{6} \sum (R_i - \bar{R})^2$  where  $\bar{R}$  = average bond length and  $R_i$  = an individual bond length.

Table 5. Comparison of mean octahedral  $Nb^{5+}$ -O distances with distortion

Only structures with e.s.d.'s for Nb-O distances of <0.025 Å were used.

| Compound                         | $\bar{R}$ (Å) | Distortion<br>$\Delta = \langle (\Delta R/R)^2 \rangle \times 10^4$ | Reference |          |
|----------------------------------|---------------|---|-----------|----------|
| $Hg_2Nb_2O_7$                    | 1.999         | 0   | 68 INOCA  | 7 1704   |
| $Cd_2Nb_2O_7$                    | 1.957         | 0   | 72 CJCHA  | 50 3648  |
| $Na_2Nb_4O_{11}$                 | 1.977         | 1   | 70 JSSCB  | 1 454    |
| $Ba_{0.27}Sr_{0.73}Nb_2O_{5.78}$ | 1.967         | 6   | 61 JCPSA  | 48 5048  |
| $Na_{13}Nb_{35}O_{94}$           | 1.965         | 7   | 71 JSSCB  | 3 89     |
| $Ba_3Si_4Nb_6O_{26}$             | 1.989         | 9   | 70 ACBCA  | 26 102   |
| $Na_{13}Nb_{35}O_{94}$           | 1.967         | 11  | 71 JSSCB  | 3 89     |
| $Na_{13}Nb_{35}O_{94}$           | 1.959         | 12  | 71 JSSCB  | 3 89     |
| $Na_{13}Nb_{35}O_{94}$           | 1.964         | 12  | 71 JSSCB  | 3 89     |
| $NaNbO_3$                        | 1.985         | 16  | 69 ACBCA  | 25 851   |
| $Na_{13}Nb_{35}O_{94}$           | 1.947         | 18  | 71 JSSCB  | 3 89     |
| $Na_{13}Nb_{35}O_{94}$           | 1.991         | 22  | 71 JSSCB  | 3 89     |
| $Na_{13}Nb_{35}O_{94}$           | 1.987         | 22  | 71 JSSCB  | 3 89     |
| $Na_{13}Nb_{35}O_{94}$           | 1.978         | 24  | 71 JSSCB  | 3 89     |
| $LiNb_2O_8$                      | 1.993         | 28  | 71 ACSAA  | 25 3337  |
| $LiNbO_3$                        | 2.000         | 31  | 66 JPCSA  | 27 997   |
| $Ca_2Nb_2O_7$                    | 1.997         | 31  | 74 JINCA  | 36 1965  |
| $Ca_2Nb_2O_7$                    | 2.005         | 34  | 74 JINCA  | 36 1965  |
| $SbNbO_4$                        | 2.003         | 37  | 65 CCJDA  | 1965 611 |
| $KNbO_3$                         | 2.011         | 42  | 67 ACACA  | 22 639   |
| $Na_3NbO_4$                      | 2.013         | 52  | 74 BUFCA  | 97 3     |
| $Ca_2Nb_2O_7$                    | 2.010         | 53  | 74 JINCA  | 36 1965  |
| $Ca_2Nb_2O_7$                    | 2.015         | 58  | 74 JINCA  | 36 1965  |
| $Na_3NbO_4$                      | 2.021         | 60  | 74 BUFCA  | 97 3     |
| $CaNb_2O_6$                      | 2.021         | 76  | 70 AMMIA  | 55 90    |
| $GaNbO_4$                        | 2.031         | 83  | 65 ACACA  | 18 874   |

Table 6. Comparison of mean octahedral  $\text{Mo}^{6+}$ -O distances with distortionOnly structures with e.s.d.'s for Mo-O distances of  $<0.025$  Å were used.

| Compound   | $\bar{R}$ (Å) | Distortion  |          | Reference |      |
|--|---------------|---|----------|-----------|------|
|  |               | $\Delta = \langle (\Delta R/R)^2 \rangle \times 10^4$ |          |           |      |
| $\text{Mo}_2(\text{O}_2\text{C}_6\text{Cl}_4)_6$   | 1.919         | 5   | 75 JACSA | 97        | 2123 |
| $\text{Mo}_4\text{O}_{11}$ orthorhombic  | 1.944         | 9   | 63 ARKEA | 21        | 365  |
| $\text{Mo}_4\text{O}_{11}$ monoclinic  | 1.946         | 10  | 63 ARKEA | 21        | 365  |
| $\text{Mo}_4\text{O}_{11}$ monoclinic  | 1.937         | 56  | 63 ARKEA | 21        | 365  |
| $\text{Mo}_4\text{O}_{11}$ orthorhombic  | 1.951         | 67  | 63 ARKEA | 21        | 365  |
| $\text{Mo}_4\text{O}_{11}$ orthorhombic  | 1.911         | 96  | 63 ARKEA | 21        | 365  |
| $\text{Mo}_4\text{O}_{11}$ monoclinic  | 1.945         | 96  | 63 ARKEA | 21        | 365  |
| $(\text{C}_{15}\text{H}_{11}\text{O}_2)_2\text{MoO}_2$   | 1.952         | 99  | 74 ACBCA | 30        | 300  |
| $(\text{NH}_4)_6[\text{Mo}_7\text{O}_{24}] \cdot 4\text{H}_2\text{O}$                                | 1.962         | 99  | 75 JCSIA | 1975      | 505  |
| $(\text{NH}_4)_6[\text{Mo}_7\text{O}_{24}] \cdot 4\text{H}_2\text{O}$                                | 1.972         | 101   | 75 JCSIA | 1975      | 505  |
| $(\text{NH}_4)_6[\text{Mo}_7\text{O}_{24}] \cdot 4\text{H}_2\text{O}$                                | 1.960         | 104   | 75 JCSIA | 1975      | 505  |
| $\text{LiMoO}_2\text{AsO}_4$   | 1.967         | 104   | 70 ACSAA | 24        | 3711 |
| $(\text{NH}_4)_6\text{Mo}_8\text{O}_{27} \cdot 4\text{H}_2\text{O}$                                  | 1.960         | 106   | 74 ACBCA | 30        | 48   |
| $\text{HgMoO}_4$   | 1.965         | 111   | 73 ACBCA | 29        | 869  |
| $(\text{NH}_4)_6[\text{Mo}_7\text{O}_{24}] \cdot 4\text{H}_2\text{O}$                                | 1.955         | 113   | 75 JCSIA | 1975      | 505  |
| $(\text{NH}_4)_6[\text{Mo}_7\text{O}_{24}] \cdot 4\text{H}_2\text{O}$                                | 1.962         | 115   | 75 JCSIA | 1975      | 505  |
| $(\text{NH}_4)_6[\text{Mo}_7\text{O}_{24}] \cdot 4\text{H}_2\text{O}$                                | 1.974         | 118   | 68 JACSA | 90        | 3275 |
| $\text{MoO}_3 \cdot 2\text{H}_2\text{O}$   | 1.966         | 121   | 72 ACBCA | 28        | 2222 |
| $\text{MoO}_3 \cdot 2\text{H}_2\text{O}$   | 1.961         | 123   | 72 ACBCA | 28        | 2222 |
| $\text{MoO}_3 \cdot 2\text{H}_2\text{O}$   | 1.957         | 126   | 72 ACBCA | 28        | 2222 |
| $\text{MoO}_3 \cdot 2\text{H}_2\text{O}$   | 1.953         | 134   | 72 ACBCA | 28        | 2222 |
| $(\text{NH}_4)_5[\text{MoO}_3]_5(\text{PO}_4)(\text{HPO}_4) \cdot 3\text{H}_2\text{O}$               | 1.970         | 140   | 74 JCSIA | 1974      | 941  |
| $\text{Na}_3(\text{CrMo}_6\text{O}_{24}\text{H}_6) \cdot 8\text{H}_2\text{O}$                        | 1.976         | 141   | 70 INOCA | 9         | 2228 |
| $(\text{NH}_4)_6\text{Mo}_8\text{O}_{27} \cdot 4\text{H}_2\text{O}$                                  | 1.976         | 141   | 74 ACBCA | 30        | 48   |
| $\text{Na}_3\text{CrMo}_6\text{O}_{24}\text{H}_6 \cdot 8\text{H}_2\text{O}$                          | 1.976         | 143   | 70 INOCA | 9         | 2228 |
| $(\text{NH}_4)_5[(\text{MoO}_3)_5(\text{PO}_4)(\text{HPO}_4)] \cdot 3\text{H}_2\text{O}$             | 1.974         | 145   | 74 JCSIA | 1974      | 941  |
| $(\text{NH}_4)_6[\text{TeMo}_6\text{O}_{24}] \cdot \text{Te}(\text{OH})_6 \cdot 7\text{H}_2\text{O}$ | 1.981         | 147   | 74 ACBCA | 30        | 2095 |
| $\text{CoMoO}_4$   | 1.991         | 150   | 65 ACACA | 19        | 269  |
| $(\text{NH}_4)_6\text{Mo}_8\text{O}_{27} \cdot 4\text{H}_2\text{O}$                                  | 1.972         | 151   | 74 ACBCA | 30        | 48   |
| $\text{MoO}_3$   | 1.981         | 151   | 63 ARKEA | 21        | 357  |
| $(\text{NH}_4)_6[\text{Mo}_7\text{O}_{24}] \cdot 4\text{H}_2\text{O}$                                | 1.976         | 152   | 68 JACSA | 90        | 3275 |
| $\text{K}_2\{[\text{MoO}_2(\text{C}_2\text{O}_4)(\text{H}_2\text{O})]_2\text{O}\}$                   | 1.976         | 152   | 64 INOCA | 3         | 1603 |
| $(\text{NH}_4)_6\text{Mo}_8\text{O}_{27} \cdot 4\text{H}_2\text{O}$                                  | 1.974         | 152   | 74 ACBCA | 30        | 48   |
| $(\text{NH}_4)_5[(\text{MoO}_3)_5(\text{PO}_4)(\text{HPO}_4)] \cdot 3\text{H}_2\text{O}$             | 1.982         | 159   | 74 JCSIA | 1974      | 941  |
| $\text{Na}_3\text{CrMo}_6\text{O}_{24}\text{H}_6 \cdot 8\text{H}_2\text{O}$                          | 1.986         | 163   | 70 INOCA | 9         | 2228 |
| $(\text{NH}_4)_5[(\text{MoO}_3)_5(\text{PO}_4)(\text{HPO}_4)] \cdot 3\text{H}_2\text{O}$             | 1.977         | 167   | 74 JCSIA | 1974      | 941  |
| $\text{MoO}_3 \cdot \text{H}_2\text{O}$  | 1.984         | 167   | 74 ACBCA | 30        | 1795 |
| $(\text{NH}_4)_5[(\text{MoO}_3)_5(\text{PO}_4)(\text{HPO}_4)] \cdot 3\text{H}_2\text{O}$             | 1.991         | 186   | 74 JCSIA | 1974      | 941  |
| $(\text{NH}_4)_6[\text{Mo}_7\text{O}_{24}] \cdot 4\text{H}_2\text{O}$                                | 1.991         | 189   | 75 JCSIA | 1975      | 505  |
| $(\text{NH}_4)_6[\text{Mo}_7\text{O}_{24}] \cdot 4\text{H}_2\text{O}$                                | 2.008         | 197   | 75 JCSIA | 1975      | 505  |

Table 7. Variation of mean M-O distance and effective ionic radius in octahedral environments as a function of distortion

| Ion              | Maximum<br>$\Delta \times 10^4$ | $N^*$ | $R_0^\dagger$ | $r_0^\ddagger$ | $m$   | Correlation<br>coefficient | Goodness<br>of fit ( $\times 10^3$ ) |
|------------------|---------------------------------|-------|---------------|----------------|-------|----------------------------|--------------------------------------|
| $\text{Mo}^{6+}$ | 212                             | 38    | 1.920         |                | 3.73  | 0.74                       | 67                                   |
|                  |                                 |       |               | 0.572          | 3.01  | 0.63                       | 70                                   |
| $\text{W}^{6+}$  | 122                             | 7     | 1.925         |                | 3.30  | 0.75                       | 19                                   |
|                  |                                 |       |               | 0.565          | 3.28  | 0.66                       | 24                                   |
| $\text{V}^{5+}$  | 576                             | 16    | 1.887         |                | 2.62  | 0.98                       | 8                                    |
| $\text{Nb}^{5+}$ | 83                              | 29    | 1.976         |                | 6.45  | 0.69                       | 71                                   |
|                  |                                 |       |               | 0.599          | 6.83  | 0.44                       | 99                                   |
| $\text{Ta}^{5+}$ | 79                              | 6     | 1.984         |                | 6.70  | 0.81                       | 18                                   |
|                  |                                 |       |               | 0.617          | 3.79  | 0.15                       | 46                                   |
| $\text{Mn}^{3+}$ | 71                              | 15    | 1.994         |                | 7.08  | 0.82                       | 30                                   |
|                  |                                 |       |               | 0.624          | 6.15  | 0.54                       | 50                                   |
| $\text{Cu}^{2+}$ | 316                             | 26    | 2.085         |                | 3.99  | 0.82                       | 77                                   |
| $\text{Mg}^{2+}$ | 156                             | 28    | 2.094         |                | 8.31  | 0.72                       | 21                                   |
|                  |                                 |       |               | 0.728          | 8.86  | 0.77                       | 18                                   |
| $\text{Co}^{2+}$ | 46                              | 15    | 2.106         |                | 7.38  | 0.42                       | 19                                   |
|                  |                                 |       |               | 0.734          | 11.70 | 0.70                       | 16                                   |
| $\text{Zn}^{2+}$ | 71                              | 16    | 2.099         |                | 7.70  | 0.64                       | 21                                   |
|                  |                                 |       |               | 0.736          | 8.20  | 0.74                       | 16                                   |
| $\text{Li}^+$    | 148                             | 11    | 2.159         |                | 8.42  | 0.81                       | 30                                   |
|                  |                                 |       |               | 0.784          | 9.02  | 0.79                       | 35                                   |

\*  $N$  = number of independent octahedra $^\dagger R = R_0 + m\Delta$ . $^\ddagger r = r_0 + m\Delta$ .

cupied sites relax toward their bonded cation neighbors. Therefore average distances should increase as the occupancy factor decreases. In general, partial occupancy seems to be more prevalent for cations which are weakly bonded to oxygen like  $\text{Cu}^+$ ,  $\text{Ag}^+$ , alkali ions, and large alkaline earths. The most prominent examples are Li and Na compounds. Table 8 summarizes the existent data on some structures with partial cation occupancy. Fig. 6 shows the dependence of mean Li–O bond length on the degree of occupancy. Although the data are not extensive, it is apparent that mean distance increases as occupancy factor decreases. Extrapolation of the Li curve in Fig. 6 to zero occupancy, *i.e.* a tetrahedral Li vacancy, gives 2.10–2.15 Å, which is close to the 2.11 Å found for  $\alpha\text{-Li}_5\text{GaO}_4$  by Stewner & Hoppe (1971) and for  $\beta$  eucryptite by Tscherry, Schulz & Laves (1972).

Another example of the effects of partial occupancy can be found in the non-stoichiometric feldspar  $\text{Sr}_{0.84}\text{Na}_{0.03}\text{Al}_{1.69}\text{Si}_{2.29}\text{O}_8$  reported by Grundy & Ito (1974). The mean Sr–O distance in this compound is 0.03 Å greater than in the stoichiometric  $\text{SrAl}_2\text{Si}_2\text{O}_8$  (Chiari, Calleri, Bruno & Ribbe, 1975).

The relation between mean distance and occupancy probably cannot be quantified precisely because the relaxation of oxygen ions will depend on the nature and number of other cation neighbors.

### 3. Effects of covalence

Changes in interatomic distances due to covalence effects are anticipated in compounds with (1) anions less electronegative than fluorine or oxygen, *i.e.* chlor-

ides, bromides, sulfides, selenides, *etc.* and (2) tetrahedral oxyanions such as the  $\text{VO}_4^{3-}$  and  $\text{AsO}_4^{3-}$  groups. The effects of covalence show up as a lack of additivity of the radii and are generally referred to as 'covalent shortening'.

(a) *Halides and chalcogenides.* Covalence effects can be observed by comparing the relative contraction of cation–anion distances in two different isotypic compounds as the anion becomes less electronegative, *e.g.*  $\text{Fe}^{2+}$  in  $\text{Fe}_2\text{GeO}_4$  and  $\text{Fe}_2\text{GeS}_4$  vs  $\text{Mg}^{2+}$  in  $\text{Mg}_2\text{GeO}_4$  and  $\text{Mg}_2\text{GeS}_4$ . Covalence shortens both Fe–S and Mg–S bonds relative to Fe–O and Mg–O bonds, but because of the greater electronegativity of  $\text{Fe}^{2+}$  (1.8) compared to  $\text{Mg}^{2+}$  (1.2), the Fe–S bonds are shortened to a greater extent. Thus a 'covalency contraction' parameter (Shannon & Vincent, 1974) can be defined:

$$R_d = \frac{d(\text{Fe-X})^3}{d(\text{Mg-X})^3}$$

where  $d(\text{Fe-X})$  = mean Fe–X distance.

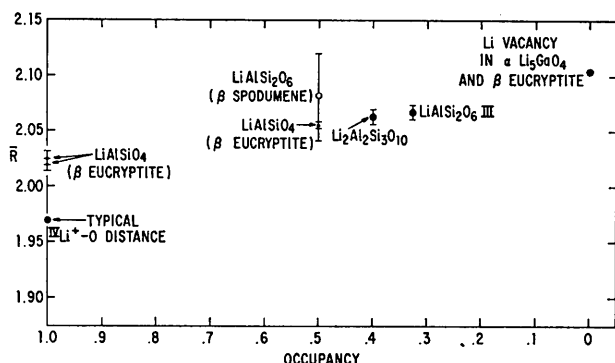
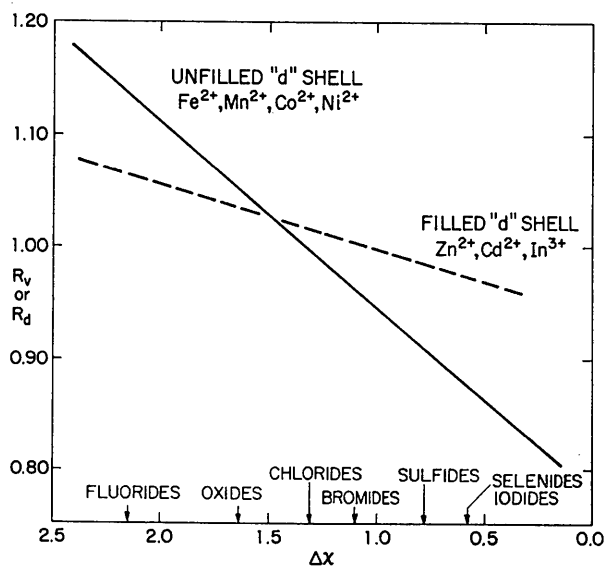
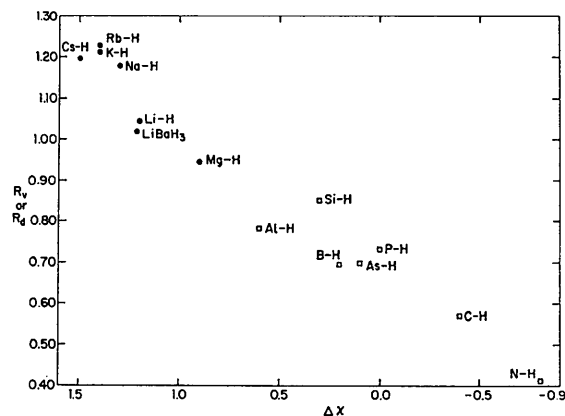
A similar parameter

$$R_v = \frac{V(\text{Fe}_m\text{X}_n)}{V(\text{Mg}_m\text{X}_n)}$$

compares the volume of an  $\text{Fe}^{2+}$  compound with that of an isotypic  $\text{Mg}^{2+}$  compound. To see the effects of covalence on the Fe–X distance relative to the Mg–X distance, the ratio  $R_v$  or  $R_d$  may be plotted against the difference in electronegativity of the Fe–X bond,  $\Delta\chi_{\text{Fe-X}}$ . Such schematic  $R_v$ – $\Delta\chi$  plots are shown in Fig. 7. The reference ions for  $\text{Cd}^{2+}$  and  $\text{In}^{3+}$  are  $\text{Ca}^{2+}$  and  $\text{Sc}^{3+}$  respectively. Such plots usually show a strong

Table 8. Mean distances in structures with partially occupied cation sites

| Compound   | Occupancy factor | $\bar{R}$ | Reference |     |      |
|--|------------------|-----------|-----------|-----|------|
| (a) $^{\text{IV}}\text{Li}^+$  |                  |           |           |     |      |
| Typical  | 1.00             | 1.97      | Table 1   |     |      |
| $\text{LiAlSiO}_4$ ( $\beta$ eucryptite)   | 1.00             | 2.020 (4) | 73 AMMIA  | 58  | 681  |
|  |                  | 2.025 (7) | 72 ZKKKA  | 135 | 175  |
| $\text{LiAlSi}_2\text{O}_6$ II ( $\beta$ spodumene)                                | 0.50             | 2.08 (4)  | 68 ZKKKA  | 126 | 46   |
|  |                  | 2.085 (9) | 69 ZKKKA  | 130 | 420  |
| $\text{LiAlSiO}_4$ ( $\beta$ eucryptite)   | 0.50             | 2.056 (2) | 72 ZKKKA  | 135 | 161  |
| $\text{Li}_2\text{Al}_2\text{Si}_3\text{O}_{10}$                                   | 0.40             | 2.064 (4) | 70 ZKKKA  | 132 | 118  |
| $\text{LiAlSi}_2\text{O}_6$ III  | 0.33             | 2.068 (5) | 68 ZKKKA  | 127 | 327  |
| $\alpha\text{-Li}_5\text{GaO}_4$   | 0.00             | 2.11      | 71 ACBCA  | 27  | 616  |
| $\text{LiAlSiO}_4$   | 0.00             | 2.11      | 72 ZKKKA  | 135 | 175  |
| (b) $^{\text{VI}}\text{Na}^+$  |                  |           |           |     |      |
| Typical  | 1.00             | 2.42      | Table 1   |     |      |
| $\text{Na}_2\text{Fe}_2\text{Al}(\text{PO}_4)_3$ (wylieite)                        | 0.91             | 2.533 (6) | 74 AMMIA  | 59  | 280  |
| $\text{NaSbO}_3$   | 0.82             | 2.74      | 74 JSSCB  | 9   | 345  |
| $\text{Na}_2\text{Fe}_2\text{Al}(\text{PO}_4)_3$ (wylieite)                        | 0.70             | 2.723 (6) | 74 AMMIA  | 59  | 280  |
| $\text{NaAlSi}_3\text{O}_8$ (high albite)  | 0.50             | 2.600 (9) | 69 ACBCA  | 25  | 1503 |
| $\text{NaAl}_{11}\text{O}_{17}$ ( $\beta\text{-Al}_2\text{O}_3$ )                  | 0.35             | 2.839 (1) | 68 ZKKKA  | 127 | 94   |
| $\text{NaSbO}_3$   | 0.29             | 2.65      | 74 JSSCB  | 9   | 345  |
| $\text{Na}_{2.58}\text{Al}_{21.81}\text{O}_{34}$ ( $\beta\text{-Al}_2\text{O}_3$ ) | 0.25             | 2.88      | 71 ACBCA  | 27  | 1826 |
| (c) $^{\text{VI}}\text{Ag}^+$  |                  |           |           |     |      |
| Typical  | 1.00             | 2.50      | Table 1   |     |      |
| $\text{AgSbO}_3$   | 0.44             | 2.64      | 74 JSSCB  | 9   | 345  |
| $\text{AgSbO}_3$   | 0.33             | 2.75      | 74 JSSCB  | 9   | 345  |
| $\text{Ag}_{2.4}\text{Al}_{22}\text{O}_{34.2}$                                     | 0.22             | 2.83      | 72 JSSCB  | 4   | 60   |

Fig. 6. Mean  $\text{Li}^+\text{-O}$  bond length vs partial occupancy.Fig. 7. Covalency contraction parameter,  $R_v$  or  $R_d$ , vs  $\Delta\chi$  for filled and unfilled  $d$  shell cations.Fig. 8. Covalency contraction parameter,  $R_v$  or  $R_d$ , vs  $\Delta\chi$  for hydrides. Solid circles represent ratios of cell volumes of isotopic compounds. Squares represent ratios of the cubed  $\text{M-H}$  distances to the cubed  $\text{M-F}$  distances.

dependence of  $R_v$  on  $\Delta\chi$ . For  $\text{Fe}^{2+}\text{-Mg}^{2+}$  the  $\text{Fe}^{2+}$  fluoride volumes are  $\sim 110\%$  of the corresponding  $\text{Mg}^{2+}$  fluoride volumes whereas the  $\text{Fe}^{2+}$  sulfide volumes are  $\sim 96\%$  of the corresponding  $\text{Mg}^{2+}$  sulfide volumes. Plots for the cations with filled ' $d$ ' shells show a markedly smaller dependence on  $\Delta\chi$ . This appears to be due to the difference in covalence of hybrid orbitals formed from metal ' $d$ ' orbitals vs metal ' $s$ - $p$ ' orbitals.

These relations show that effective ionic radii derived primarily from oxides are not strictly applicable to fluorides – note the change in  $R_v$  for  $\text{Fe}^{2+}$ ,  $\text{Co}^{2+}$ ,  $\text{Ni}^{2+}$ , and  $\text{Mn}^{2+}$  from fluorides to oxides. This effect is particularly noticeable in  $R_v\text{-}\Delta\chi$  plots for the pairs  $\text{Cu}^+\text{-Li}^+$  and  $\text{Ag}^+\text{-Na}^+$  (Shannon & Gurneman, 1975). The  $\text{Cu}^+\text{-Li}^+$  and  $\text{Ag}^+\text{-Na}^+$  plots are very steep, e.g. the volume of  $\text{AgF}$  is 120% of the volume of  $\text{NaF}$ , whereas the volume of  $\text{Ag}_2\text{Se}$  is only 72% of the volume of  $\text{Na}_2\text{Se}$ . Although most of this change arises from covalency, double repulsion effects present in the Li and Na halides described by Pauling (1960) may also play a role.

Covalence effects are useful in explaining certain differences between the effective ionic radii of Table 1 and the ionic radii of Pauling (1927) and Ahrens (1952). Pauling's radii for  $\text{Cu}^+$  (0.96 Å) and  $\text{Ag}^+$  (1.26 Å) are considerably larger than those in Table 1 (0.77 and 1.15 Å respectively). Since these radii were derived from comparison of alkali halide distances, using an equation relating effective nuclear charge and screening constants (Pauling, 1927), they are valid in primarily ionic crystals. The smaller radii in Table 1 are applicable in the more covalent oxides. Extrapolation of  $R$  vs  $\Delta\chi$  curves such as in Fig. 7 leads to values of 0.91 Å and 1.23 Å for fluorides, which are close to Pauling's ionic values.

A final example of covalence effects concerns  $\text{M}^+\text{-H}^-$  distances. According to Gibb (1962), the radius of the hydride ion is slightly larger than the radius of the fluoride ion. To rationalize the behavior of the hydride ion, the  $\text{M-H}$  bond has been treated as covalent. Therefore, it is useful to make  $R_v$  vs  $\Delta\chi$  plots similar to those just discussed for  $\text{Fe}^{2+}$ ,  $\text{Cu}^+$ , etc. In this case, the reference ion is  $\text{F}^-$  and volumes of certain hydrides are compared to those of isotopic fluorides. The results of this analysis are shown in Fig. 8. The solid circles represent volume ratios,  $R_v = V(\text{M}_m\text{H}_n)/V(\text{M}_m\text{F}_n)$ ; open squares represent ratios of typical distances  $R_d = d(\text{M-H})^3/d(\text{M-F})^3$ . In the more ionic hydrides of Cs, Rb, K, and Na, hydride volumes are considerably larger than those of the fluorides. For the Li and Mg compounds, hydride and fluoride volumes are approximately equal, whereas the more covalent hydrides have increasingly smaller relative volumes than the corresponding fluorides. Fig. 8 partly explains the differences in reported radii. The Morris & Reed (1965) value of 1.53 Å was derived essentially from the large alkali halides, while Gibb's value of 1.40 Å was derived primarily from hydrides of the more electronegative

metals such as: Sc, Ti, Y, Zr, Hf, Nb, Ta, and Th. Because of this strong dependence of M–H distances on cation electronegativity, it does not seem very useful to quote a unique radius for  $H^-$ .

(b) *Tetrahedral oxyanions.* Lack of additivity also appears in most small tetrahedral groups and is particularly noticeable for the ions  $^{IV}B^{3+}$ ,  $^{IV}Fe^{3+}$ ,  $^{IV}Ge^{4+}$ ,  $^{IV}As^{5+}$ ,  $^{IV}V^{5+}$ ,  $^{IV}S^{6+}$ ,  $^{IV}Se^{6+}$ , and  $^{IV}Cl^{7+}$ . The deviations in vanadates have been studied in detail (Shannon & Calvo, 1973b). Assuming that the V–O bond is strongly covalent, and that relatively electronegative cations such as  $Cu^{2+}$ ,  $Ni^{2+}$ , and  $Co^{2+}$  tend to remove electron density from the V–O bond, a V–O bond length increase in Cu, Ni, and Co vanadates is anticipated. Plots of mean radii ( $\bar{r}$ ) *vs* mean cation electronegativity ( $\bar{\chi}$ ) show a marked slope with a gradual increase in  $\bar{r}(^{IV}V^{5+})$  from vanadates of the alkali and alkaline earth ions to those of Cu, Ni, and Co. Similar plots for other ions,  $P^{5+}$ ,  $As^{5+}$  (Shannon & Calvo, 1973b),  $B^{3+}$ ,  $Si^{4+}$ ,  $Se^{6+}$  (Shannon, 1975), showed the same behavior. The statistical data on the tetrahedra of  $B^{3+}$ ,  $Si^{4+}$ ,  $Ge^{4+}$ ,  $P^{5+}$ ,  $As^{5+}$ ,  $S^{6+}$ ,  $Se^{6+}$ ,  $Cr^{6+}$ ,  $Mo^{6+}$ ,  $W^{6+}$ , and  $Cl^{7+}$  have been summarized by Shannon (1975). The slopes of the  $\bar{r}$  *vs*  $\bar{\chi}$  plots were greatest for  $V^{5+}$ ,  $Se^{6+}$ , and  $Cl^{7+}$ , and least for  $Si^{4+}$ . Although the evidence for covalence as the origin of these effects in the above systems is only indirect, this behavior is consistent with accepted ideas of ‘covalent shortening’ of bonds.

The evidence for covalent shortening of  $^{IV}Fe^{3+}$ –O bonds is more direct. Jeitschko, Sleight, McClellan & Weiher (1976) have found a good correlation between (1) the Fe Mössbauer isomer shift and mean Fe–O distance and (2)  $\bar{\chi}$  and mean Fe–O distance ( $\bar{R}$ ). Thus, in  $\beta$ - $NaFeO_2$   $\bar{R}=1.86$  Å and  $\delta=0.18$  mm  $s^{-1}$  relative to  $\alpha$  Fe whereas in  $Bi_3(FeO_4)(MoO_4)_2$   $\bar{R}=1.909$  Å and  $\delta=0.282$  mm  $s^{-1}$ .

#### 4. Effects of electron delocalization

At a pressure of 6.5 kbar SmS (NaCl structure) undergoes a semiconductor to metal transition and a reduction in cell edge from 5.97 to 5.70 Å (Jayaraman, Narayanamurti, Bucher & Maines, 1970). The reduction in cell volume was attributed to a partial conversion of  $Sm^{2+}$  to  $Sm^{3+}$ ; some of the electrons presumably go into a conduction band.

Electron delocalization effects can also be seen by comparing the volumes of the conducting V sulfides VS,  $V_7S_8$ ,  $V_3S_4$  and  $V_5S_8$  with the corresponding Cr sulfides which have localized ‘*d*’ electrons (de Vries & Jellinek, 1974). The V compounds have volumes ~5% smaller than the corresponding chromium compounds. This does not agree with the relative sizes of V and Cr in oxides and fluorides, *e.g.*  $r(^{IV}V^{3+})=0.64$  and  $r(^{VI}Cr^{3+})=0.615$  Å. For the sulfides, this unit-cell volume anomaly is not simply attributable to metallic *vs* semiconducting behavior. While  $Cr_3S_4$ ,  $Cr_5S_6$ , and  $Cr_7S_8$  show a positive temperature dependence of resistivity typical of a metal, magnetic susceptibility

measurements indicate Curie–Weiss behavior and therefore nearly localized electrons (van Bruggen, 1969). This is in contrast to the Pauli paramagnetic behavior of the corresponding V sulfides (de Vries & Haas, 1973) characteristic of delocalized electrons. Thus, in SmS and the sulfides of V metallic character accompanied by electron delocalization appears to be associated with reduced bond distances.

A further example of delocalization effects occurs in the compound  $NaVS_2$  (Weigers, van der Meer, van Heinigen, Kloosterboer & Alberink, 1974). The molecular volume of Pauli paramagnetic  $NaVS_2$  I ( $67.9$  Å<sup>3</sup>) is significantly less than that of  $NaVS_2$  II ( $72.7$  Å<sup>3</sup>).  $NaVS_2$  II is characterized by localized electrons (Jellinek, 1975) and its molecular volume is consistent with that of isotypic  $NaCrS_2$  ( $71.1$  Å<sup>3</sup>).

If electron delocalization in oxides results in reduced metal–oxygen distances and thereby an effective increase in valence, radii derived for the ions  $Mo^{4+}$ ,  $Tc^{4+}$ ,  $Ru^{4+}$ ,  $Rh^{4+}$ ,  $W^{4+}$ ,  $Re^{4+}$ ,  $Os^{4+}$ , and  $Ir^{5+}$  from metallic oxides may not be reliable when applied to insulating oxides. Thus, radii obtained from distances in the metallic phases, *e.g.*  $RhO_2$ ,  $ReO_2$ , and  $Cd_2Ir_2O_7$ , will be smaller than radii obtained from semiconducting or insulating compounds.\* When both types of compounds have been studied, a significant difference in distances is generally found. The mean octahedral  $Re^{4+}$ –O distance in insulating  $K_4[Re_2O_2(C_2O_4)_4] \cdot 3H_2O$  (Lis, 1975) of  $2.021$  (10) Å ( $r=0.671$  Å) is greater than the estimated mean distance in metallic  $ReO_2$  of  $1.99$  Å ( $r=0.63$  Å). Knop & Carlow’s (1974) value of  $r=0.662$  Å derived from cell volumes of the insulating  $Cs_2ReF_6$  phases is consistent with the radius of  $Re^{4+}$  from  $K_4[Re_2O_2(C_2O_4)_4] \cdot 3H_2O$ . The  $Re^{5+}$ –O distance in  $Nd_4Re_2O_{11}$  (Wilhelmi, Lagervall & Muller, 1970) of  $1.987$  (12) Å ( $r=0.607$  Å) is significantly greater than the distance in metallic  $Cd_2Re_2O_7$  (Sleight, 1975) of  $1.93$  (2) Å ( $r=0.55$  Å). The radii of  $0.58$  Å derived from  $XeF_2RuF_6$  and  $0.60$  Å from  $XeFRuF_6$  (Bartlett, Gennis, Gibler, Morrell & Zalkin, 1973) are greater than the radius of  $0.565$  Å derived from the  $r^3$ – $V$  plot for metallic  $Cd_2Ru_2O_7$ . In contrast, however, the  $Mo^{4+}$  radius of  $0.64$  Å derived from insulating  $Li_2MoF_6$  (Brunton, 1971) is not greatly different from the radius of  $0.65$  Å derived from metallic  $MoO_2$  (Brandt & Skapski, 1967).

Although there appears to be ample evidence to show that M–O bond distances in compounds with localized electrons are greater than M–O distances in compounds with delocalized electrons, the data are not yet sufficient to derive a reliable set of radii for semiconducting compounds containing  $Mo^{4+}$ ,  $Tc^{4+}$ ,  $Ru^{4+}$ ,  $Rh^{4+}$ ,  $W^{4+}$ ,  $Re^{4+}$ ,  $Os^{4+}$ , and  $Ir^{5+}$ . This will become possible as additional accurate structure refinements of fluorides, molecular inorganic compounds, and semiconducting oxides containing these ions become available.

\* This assumes that metallic character can be equated with delocalized electron behavior in these compounds.



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