

# Chasing Snoopy's Tail

Roger Twank

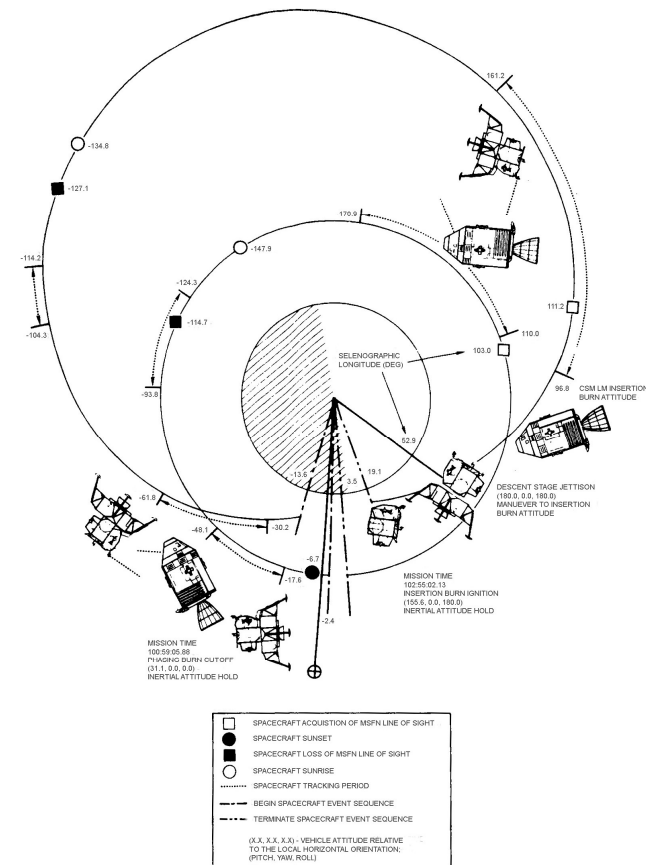
January, 2020

# Introduction

- Apollo 10 jettisoned its Lunar Module descent stage into an elliptic, low-inclination lunar orbit in May, 1969
- It is widely assumed that this orbit was unstable, and that the stage impacted the moon soon after it was jettisoned
- Simulations indicate that the orbit is actually quasi-stable, and that the stage might still be in orbit today

# About the Phasing Orbit

- In order to run a lunar Descent Orbit Insertion (DOI) followed after one orbit by an Ascent Orbit Insertion (AOI), with no intervening landing, it was necessary to perform a unique (to Apollo missions) “Phasing” maneuver
- The Phasing maneuver raised the LM apolune to 190.1 n.m. (352 km) allowing the CSM to overtake the LM
- The LM Descent Stage was jettisoned into this “Phasing” orbit...12.1 by 190.1 n.m (22.4 by 352 km\*)



\*See Mission Report Table 6-IV

<https://history.nasa.gov/afi/ap10fi/pics/phasing-insertion.jpg>

# Phasing Orbit State

The Apollo 10 Mission Report list three states representing the phasing orbit

- Cutoff of the Phasing maneuver
- Staging
- Ignition of the Ascent Orbit Insertion maneuver

These are all essentially part of the same arc, with small perturbations during staging

TABLE 6-II.- TRAJECTORY PARAMETERS

| Event                  | Ref. body | Time, hr:min:sec | Latitude, deg | Longitude, deg | Altitude, miles | Space-fixed velocity, ft/sec | Space-fixed flight-path angle, deg | Space-fixed heading angle, deg E of N |
|------------------------|-----------|------------------|---------------|----------------|-----------------|------------------------------|------------------------------------|---------------------------------------|
| Phasing maneuver       |           |                  |               |                |                 |                              |                                    |                                       |
| Ignition               | Moon      | 100:58:25.9      | 0.22S         | 11.19W         | 17.7            | 5 512.4                      | 1.19                               | -91.09                                |
| Cutoff                 | Moon      | 100:59:05.9      | 0.34S         | 13.67W         | 19.0            | 5 672.9                      | 1.88                               | -91.05                                |
| Staging                | Moon      | 102:45:16.9      | 0.82N         | 51.23E         | 31.4            | 5 605.6                      | -3.06                              | -90.75                                |
| Ascent orbit insertion |           |                  |               |                |                 |                              |                                    |                                       |
| Ignition               | Moon      | 102:55:02.1      | 0.30N         | 19.58E         | 11.6            | 5 705.2                      | -0.78                              | -91.06                                |
| Cutoff                 | Moon      | 102:55:17.6      | 0.29N         | 18.72E         | 11.7            | 5 520.6                      | 0.49                               | -91.06                                |

[https://www.hq.nasa.gov/alsj/a410/A10\\_MissionReport.pdf](https://www.hq.nasa.gov/alsj/a410/A10_MissionReport.pdf)

# Time Conversions

- Using a spreadsheet one can convert Mission Elapsed Times to UTC

|                  | Mission Elapsed<br>Time | UTC                   |
|------------------|-------------------------|-----------------------|
| Launch           | 0:00:00.00              | 5/18/1969 16:49:00.00 |
|                  |                         |                       |
| Phasing Burn end | 100:59:05.90            | 5/22/1969 21:48:05.90 |
| Staging          | 102:45:16.90            | 5/22/1969 23:34:16.90 |
| AOI Burn start   | 102:55:02.10            | 5/22/1969 23:44:02.10 |

# Simulation Environment

- Using GMAT R2018a
- GRAIL gravity model:
  - jggrx\_0420a\_sha.tab
- Some customization of output and other paths may be required for your setup



[https://pds-geosciences.wustl.edu/grail/grail-l-lgrs-5-rdr-v1/grail\\_1001/shadr/jggrx\\_0420a\\_sha.tab](https://pds-geosciences.wustl.edu/grail/grail-l-lgrs-5-rdr-v1/grail_1001/shadr/jggrx_0420a_sha.tab)

# Entering Mission Report Values into GMAT

- Using LunaFixed Coordinates, one can plug in values from Mission Report table 6-II directly into the Planetodetic Spacecraft State

TABLE 6-II.- TRAJECTORY PARAMETERS

| Event                  | Ref. body | Time, hr:min:sec | Latitude, deg | Longitude, deg | Altitude, miles | Space-fixed velocity, ft/sec | Space-fixed flight-path angle, deg | Space-fixed heading angle, deg E of N |
|------------------------|-----------|------------------|---------------|----------------|-----------------|------------------------------|------------------------------------|---------------------------------------|
| Cutoff                 | Moon      | 100:59:05.9      | 0.34S         | 13.67W         | 19.0            | 5 672.9                      | 1.58                               | -91.05                                |
| Staging                | Moon      | 102:45:16.9      | 0.82N         | 51.23E         | 31.4            | 5 605.6                      | -3.06                              | -90.75                                |
| Ascent orbit insertion |           |                  |               |                |                 |                              |                                    |                                       |

The screenshot shows the GMAT interface for a spacecraft named 'A10LEM'. The 'Orbit' tab is selected, and the 'Coordinate System' is set to 'LunaFixed'. The 'State Type' is 'Planetodetic'. The 'Elements' section displays the following values:

|                  |                   |        |
|------------------|-------------------|--------|
| PlanetodeticRMAG | 1796.239999999973 | km     |
| PlanetodeticLON  | 51.229999999998   | deg    |
| PlanetodeticLAT  | 0.82000000001757  | deg    |
| PlanetodeticVMAG | 1.7086            | km/sec |
| PlanetodeticAZI  | -90.7499999999997 | deg    |
| PlanetodeticHFP  | -3.05999999999803 | deg    |

Blue arrows indicate the mapping of values from the 'Staging' row of the table above to the input fields in the GMAT interface:

- Time (102:45:16.9) maps to Epoch (22 May 1969 23:34:16.900)
- Latitude (0.82N) maps to PlanetodeticLAT (0.82000000001757)
- Longitude (51.23E) maps to PlanetodeticLON (51.229999999998)
- Altitude (31.4 miles) maps to PlanetodeticRMAG (1796.239999999973 km)
- Space-fixed velocity (5 605.6 ft/sec) maps to PlanetodeticVMAG (1.7086 km/sec)
- Space-fixed heading angle (-90.75 deg) maps to PlanetodeticAZI (-90.7499999999997 deg)
- Space-fixed flight-path angle (-3.06 deg) maps to PlanetodeticHFP (-3.05999999999803 deg)

See next page for notes and caveats!!

# Converting Table 6-II values to GMAT

RMAG: Apollo-era lunar radius was 1738.09 km

- Convert nautical mile altitude to km, and add to 1738.09
- 31.4 n.m. becomes 1796.24 km

Planetodetic VMAG is not the same as Inertial VMAG

- Table 6-II velocity (ft/sec) does not directly translate to LunaFixed coordinates
- In the GUI change to SphericalAZFPA coordinates, then change to MoonInertial coordinate frame, and enter VMAG...1.7086 km/sec
- Change back to MoonInertial/Planetodetic, and GMAT converts VMAG to the value for that frame...1.7133 km/sec\*

HFPA and AZI also differ slightly between fixed and inertial coordinates

- Very small difference at low inclination...I am ignoring it

\* There are better ways to do this in a script, but this works to get you started



# Perturbations during Staging

- Famously, there were unplanned attitude changes during the staging maneuver.
- The plan was to accelerate 2 ft/sec, jettison the stage, then slow down 2 ft/sec, pushing the stage forward and higher. (The retrograde AOI burn was performed 10 minutes later.)
- Telemetry indicates that the stage was actually pushed ~vertically, but the exact direction is not known.
- A change of 2 ft/sec vertically out of 5600 ft/sec represents a change in the Flight Path Angle of  $\sim 0.02$  degrees. I am ignoring it.

See Robin Wheeler's excellent Staging Video and graphic:

<https://history.nasa.gov/afj/ap10fj/video/staging-with-audio.mp4>

<https://history.nasa.gov/afj/ap10fj/pics/staging-cartoon-2.png>

# Automatic GMAT Scripting

- Daniel Estevez has posted python code demonstrating how to run GMAT automatically with sequences of parameters
- I have modified the code for my runs
- For the Monte Carlo run, I generated a large table of orbit state parameters with broad variation...enough to cover any uncertainty in the values in Table 6-II
  - For each parameter set, I ran a one-orbit simulation to check the apolune and perilune\*
  - I eliminated any set that resulted in apo/peri values that differed from table 6-IV by more than  $\pm 20\%$
  - Only  $\sim 30\%$  of the initial parameter sets passed this apo/peri screen

<https://destevez.net/2019/08/trying-to-find-the-dslwp-b-crash-site/>

\*Dumb way to do it, I know, but when you have a hammer, every problem looks like a nail

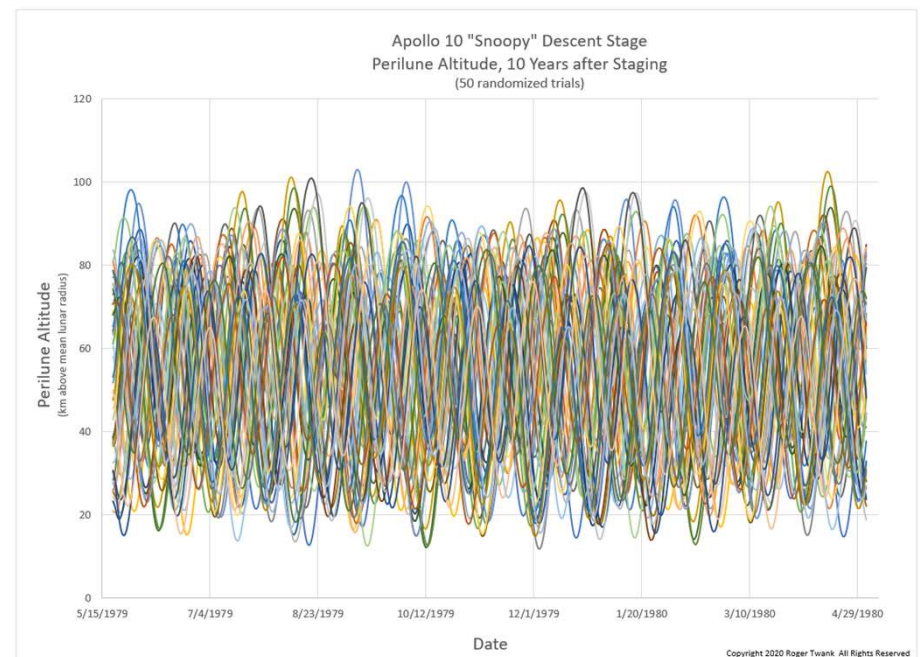
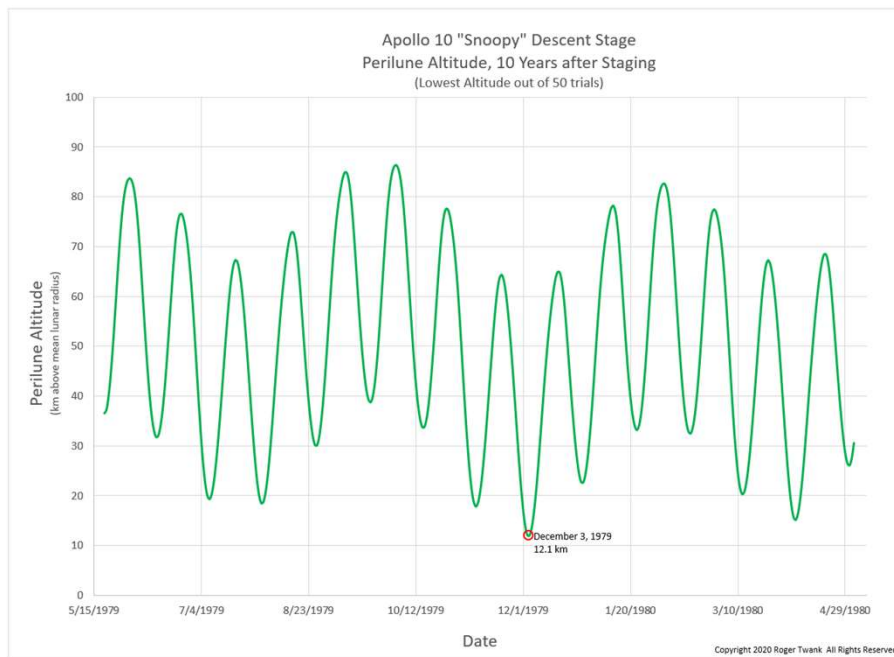
# Generating A Monte Carlo Parameter Set

| Parameter | Trial | RMAG     | Longitude | Latitude | VMAG     | AZI       | HFGA      |         |          |         |         |
|-----------|-------|----------|-----------|----------|----------|-----------|-----------|---------|----------|---------|---------|
| Tweaked   |       | 57.68    | 52.01     | 0.82     | 1.7106   | -90.73    | -3.00     |         |          |         |         |
| MAX       |       | 65.00    | 54        | 0.95     | 1.7300   | -90       | -2.50     |         |          |         |         |
| Min       |       | 50       | 50        | 0.69     | 1.6900   | -91.5     | -3.50     |         |          | Nominal | Nominal |
| Delta     | ▼     | 15.00▼   | 4.00▼     | 0.26▼    | 0.04▼    | 1.50▼     | 1.00▼     | Apolun▼ | Perilun▼ | 21▼     | 35▼     |
|           | 2     | 1790.212 | 52.01993  | 0.856048 | 1.707498 | -91.46026 | -2.781384 | 307.86  | 18.77    | 0.838   | 0.874   |
|           | 4     | 1799.463 | 51.42704  | 0.880245 | 1.697021 | -90.3695  | -2.981621 | 295.72  | 19.79    | 0.884   | 0.840   |
|           | 5     | 1797.177 | 50.35281  | 0.920862 | 1.710414 | -90.31501 | -2.887504 | 346.61  | 26.35    | 1.176   | 0.984   |
|           | 6     | 1788.971 | 50.85838  | 0.813243 | 1.710353 | -91.12977 | -2.703757 | 315.10  | 20.24    | 0.903   | 0.895   |
|           | 7     | 1797.242 | 51.86682  | 0.698828 | 1.710523 | -91.21338 | -3.026656 | 350.24  | 23.62    | 1.054   | 0.995   |
|           | 8     | 1792.543 | 53.56113  | 0.935391 | 1.717845 | -91.06805 | -2.962264 | 367.76  | 22.57    | 1.008   | 1.044   |
|           | 9     | 1791.279 | 50.43389  | 0.804623 | 1.726977 | -91.21315 | -3.06018  | 410.01  | 22.69    | 1.013   | 1.164   |
|           | 10    | 1802.77  | 52.53268  | 0.890792 | 1.699737 | -91.40102 | -3.074774 | 320.37  | 23.55    | 1.051   | 0.910   |
|           | 13    | 1801.024 | 52.51728  | 0.703791 | 1.704662 | -91.1279  | -3.160155 | 338.73  | 22.31    | 0.996   | 0.962   |
|           | 19    | 1790.123 | 50.73203  | 0.772892 | 1.713109 | -90.85354 | -2.511693 | 328.13  | 26.46    | 1.181   | 0.932   |

This shows the first few sets that passed the apo/peri screen

# Other Python Code

- There is a script to consolidate all the result csv files and capture one perilune point per day\*
- It allows me to consolidate everything into a spreadsheet so I can play with the resulting data and plot it



\*It crops the minimum values a bit, I know

# Conclusion

- Have fun!
- Let me know if you find major errors!!!!
- If your results agree with mine, please help me to convince NASA that Snoopy may still be out there, and it's worth 8 hours of radar time at Goldstone to try to find this artifact!
- There is more info on my blog: <https://snoopy.rogertwank.net/>

-@RogerTwank

**102:45:58** Armstrong (onboard): Engine arm is off. Houston, Tranquility Base here. The Eagle has landed.

**102:46:06** Duke: Roger, Twank...Tranquility. We copy you on the ground. You got a bunch of guys about to turn blue. We're breathing again. Right now. Lot

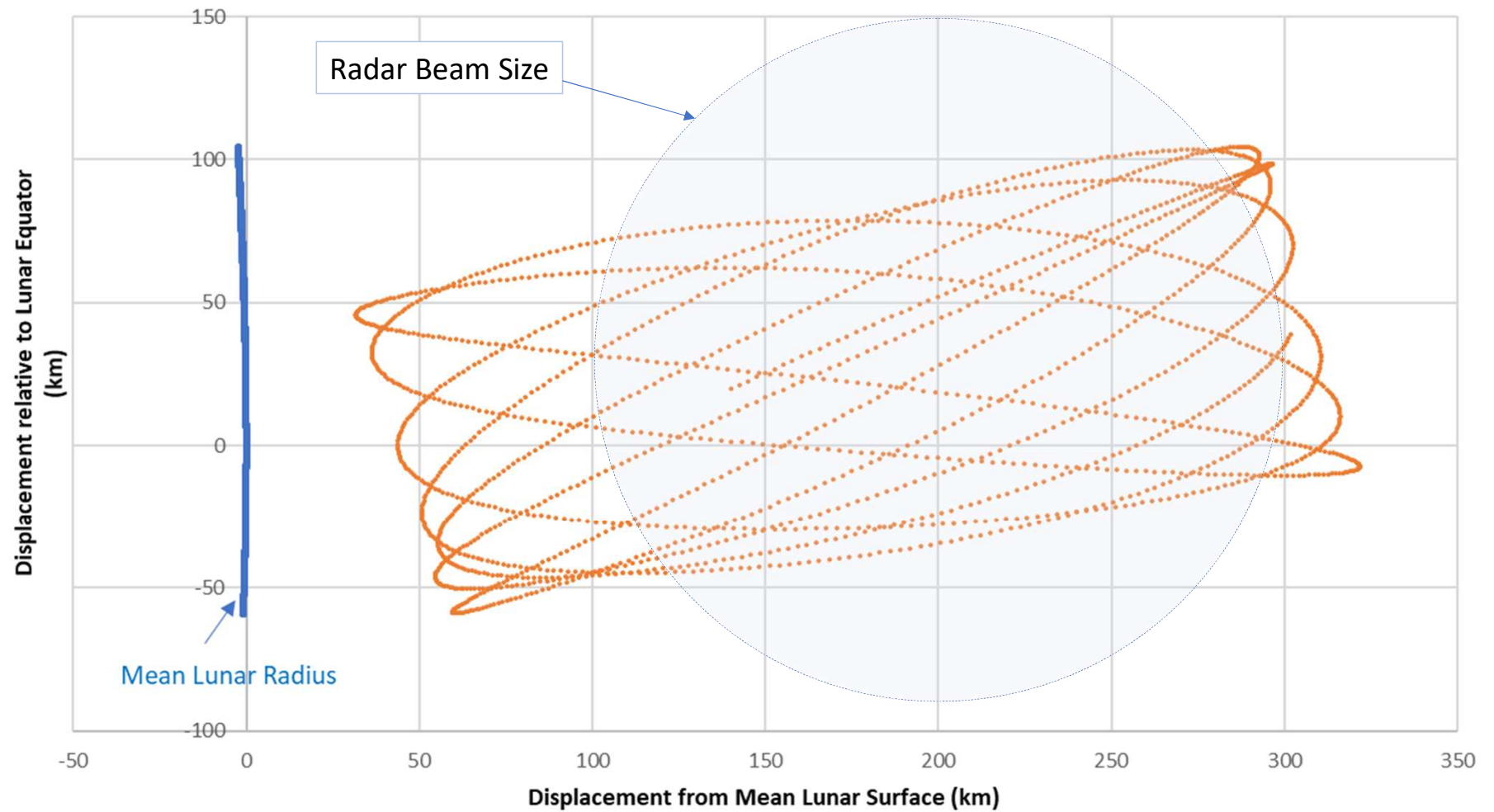
Backup

# Radar Tracking

- NASA has successfully located “lost” lunar satellites using Radar
- Following two slides match up the orbit against the radar beam width at lunar distance
- More about it in this blog post:  
<https://snoopy.robertwank.net/2020/01/how-could-snoopy-be-found.html>

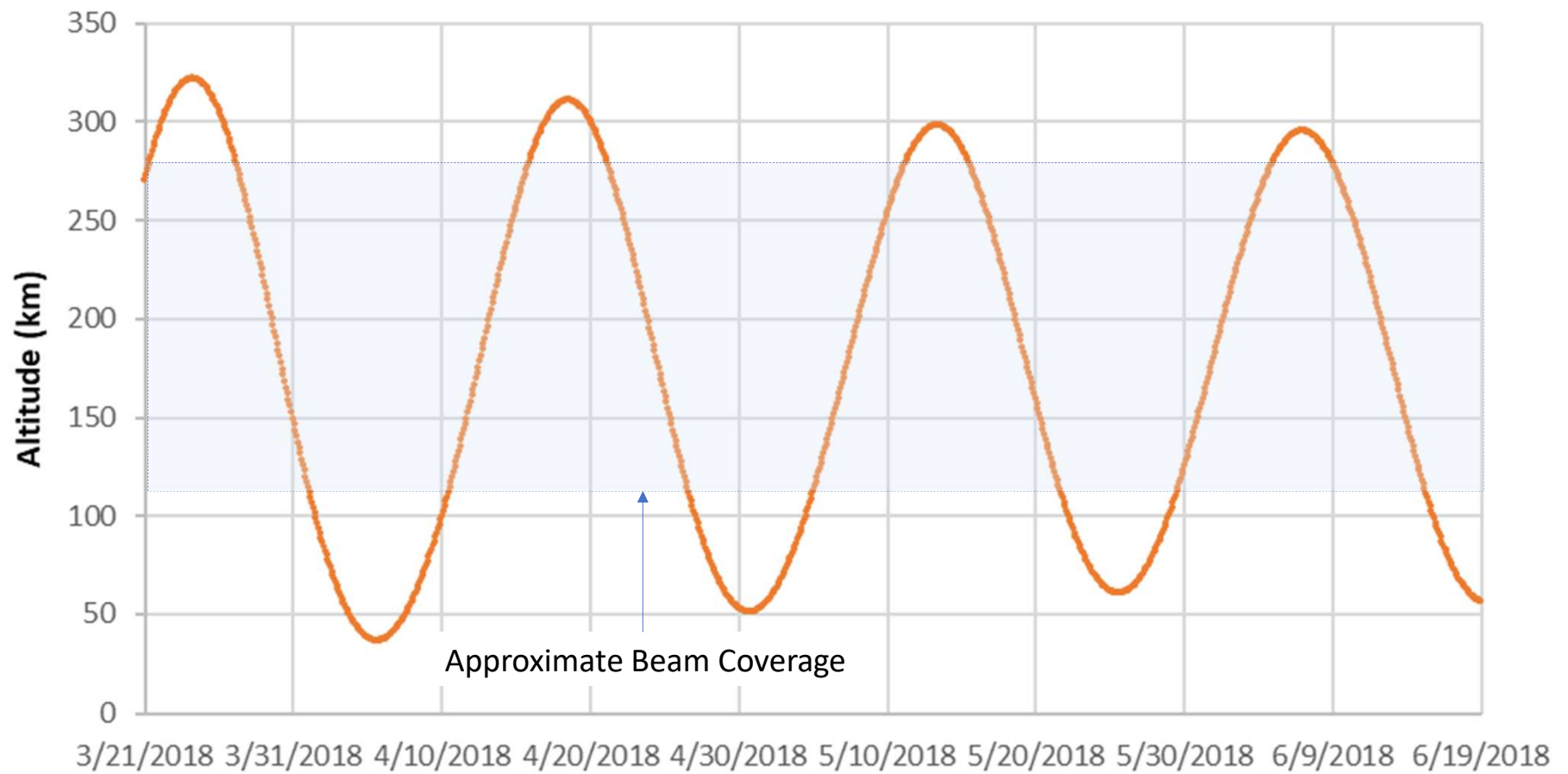
# Altitude vs Latitude at 90 East

(Simulation: January through June, 2018)

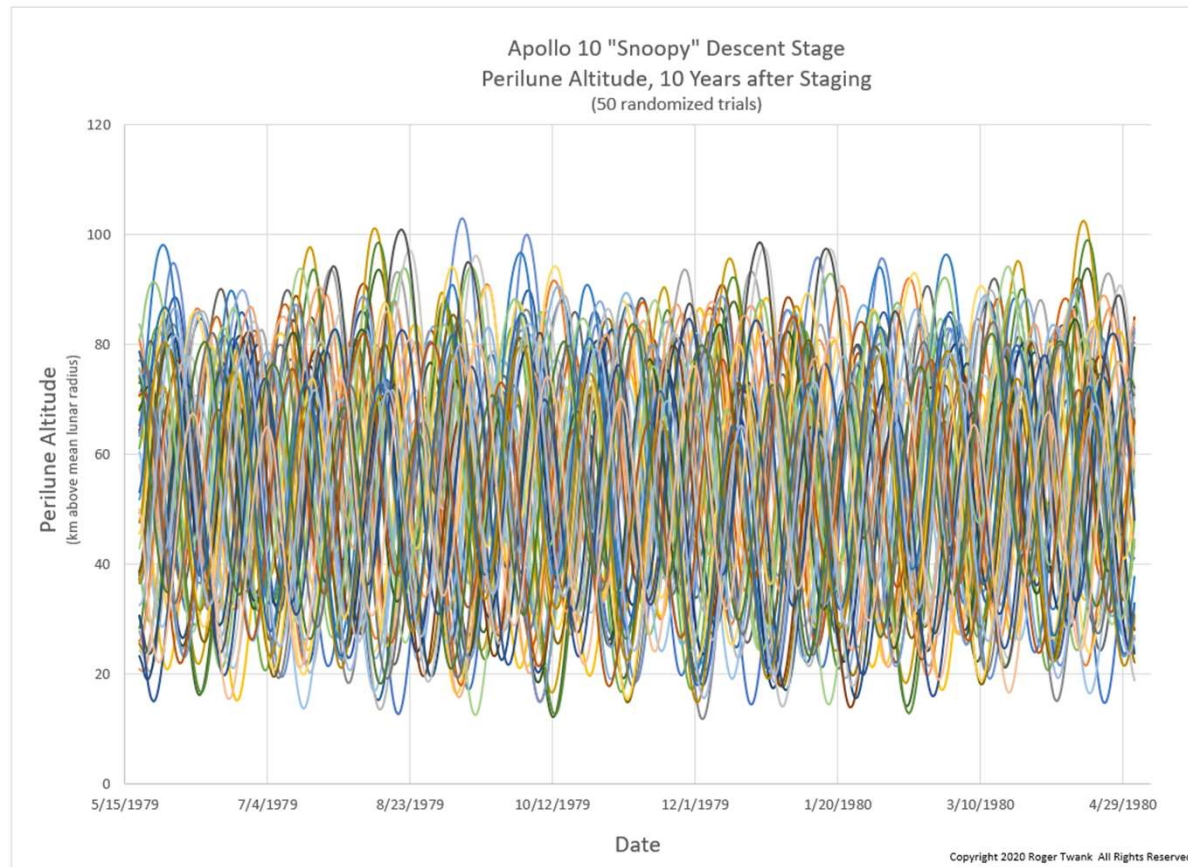




## Simulated Altitude above 90° East Longitude



# Monte Carlo Simulation of Orbit Variations



More about this in my blog...

<https://snoopy.robertwank.net/2020/02/simulating-uncertainty.html>

# Lunar Exosphere Effects

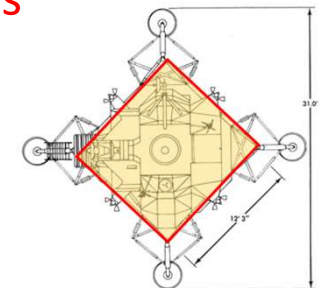
- Estimate density of Lunar Exosphere:  $4\text{e-}18 \text{ grams/cm}^3$
- Estimate (worst case) LM cross section:  $1.4\text{e}5 \text{ cm}^2$
- Estimate Volume swept out by stage during 50 years  $3.5\text{e}19 \text{ cm}^3$ 
  - Total mass of exosphere that has collided with the stage... **145 grams**
  - **Negligible compared to 2138 kg (dry) weight of stage**

<https://nssdc.gsfc.nasa.gov/planetary/factsheet/moonfact.html>

|           |        | #/cubic cm | Atomic weight | Total atomic weight                |
|-----------|--------|------------|---------------|------------------------------------|
| Helium4   | (4He)  | 40000      | 4             | 160000                             |
| Neon 20   | (20Ne) | 40000      | 20            | 800000                             |
| Hydrogen  | (H2)   | 35000      | 2             | 70000                              |
| Argon40   | (40Ar) | 30000      | 40            | 1200000                            |
| Neon22    | (22Ne) | 5000       | 22            | 110000                             |
| Argon36   | (36Ar) | 2000       | 36            | 72000                              |
| Methane   |        | 1000       | 16            | 16000                              |
| Ammonia   |        | 1000       | 17            | 17000                              |
| Carbon Di | (CO2)  | 1000       | 44            | 44000                              |
|           |        |            |               | <b>2489000</b> Atomic Units per cc |
|           |        |            |               | 4.13E-18 grams/cc                  |

<https://snoopy.roberttwank.net/2020/02/atmospheric-drag.html>

| Cross Section |             |
|---------------|-------------|
| 373           | cm per side |
| 1.39E+05      | cm squared  |



|          |                                |          |
|----------|--------------------------------|----------|
| 160000   | cm/sec                         | Velocity |
| 1.58E+09 | Seconds in orbit               |          |
| 2.53E+14 | Total cm travelled in 50 years |          |
| 3.52E+19 | Total volume (cc) swept out    |          |
| 4.13E-18 | grams/cc                       |          |
| 145.53   | grams impacted in 50 years     |          |
| 2.14E+06 | dry weight of stage (grams)    |          |
| 0.0068%  | mass ratio exosphere/stage     |          |

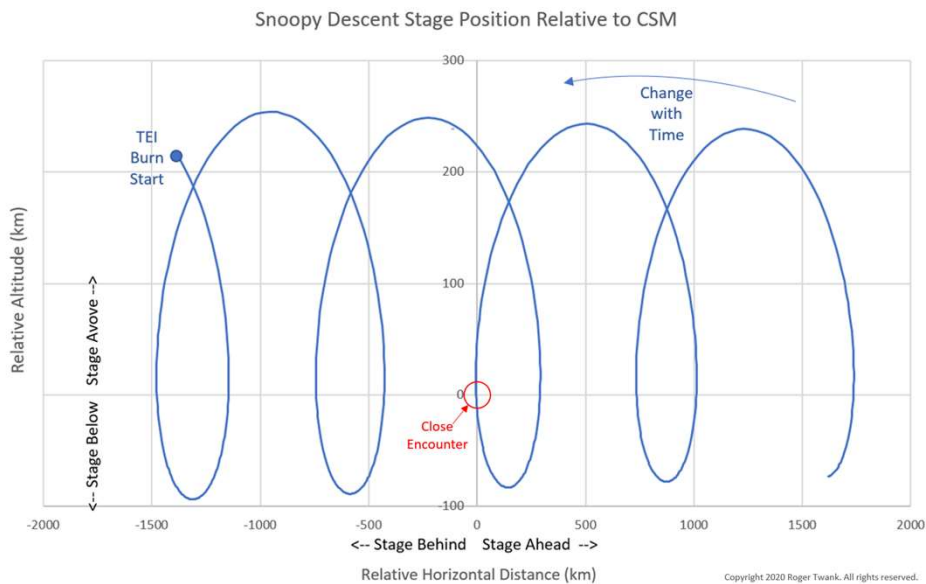
# Sighting Snoopy on May 24th

At 132:15:55 CDR Stafford reported seeing the stage:

- “There he is right down below us; he's cutting across the Taruntius twins. Yes, between Taruntius P and K. And that rascal is right in-plane with us.”

This narrows down the stage orbital period considerably

# Stage Sighting on May 24th



<https://snoopy.robertwank.net/2020/04/the-stage-returns.html>

